Implications of Multiple Corona Bursts in Lightning Processes for Radio Frequency Interferometer Observations

Ningyu Liu¹, Olaf Scholten², Joseph R Dwyer³, Brian Hare², Chris Francis Sterpka³, Julia Tilles⁴, and Frank D Lind⁵

¹The University of New Hampshire ²University of Groningen ³University of New Hampshire ⁴Sandia National Laboratories ⁵MIT

November 24, 2022

Abstract

Recent observations from LOFAR indicate that multiple, spatially distributed corona bursts can occur in lightning processes on the order of 10 microseconds. The close proximity of the corona bursts in space and time poses a great observation challenge for dedicated lightning radio interferometers, typically with < 100 m baselines. This paper reports simulations to show the interferometry results that would be obtained with a typical lightning interferometer for such a lightning process. In particular, spatially-separated corona bursts at fixed locations may be seen as a fast ($>10^7$ m/s) propagating source for an instrument with resolution greater than the spatial separation of the bursts. The implications and suggestions for lightning interferometry studies are discussed in the paper.









Implications of Multiple Corona Bursts in Lightning Processes for Radio Frequency Interferometer Observations

Ningyu Liu¹, Olaf Scholten², Joseph R. Dwyer¹, Brian M. Hare², Christopher F. Sterpka¹, Julia N. Tilles ³, and Frank D. Lind⁴

¹Department of Physics and Astronomy & Space Science Center (EOS), University of New Hampshire, Durham, New Hampshire, USA ²University Groningen, Kapteyn Astronomical Institute, Landleven 12, 9747 AD Groningen, The Netherlands ³Sandia National Laboratories, Albuquerque, NM, USA ⁴MIT Haystack Observatory, Westford, Massachusetts, USA

Key Points:

1

2

3

4

5

6

8

9

10 11

12

16

13	•	Complications of lightning radio interferometer data interpretation due to random
14		nature of the emission sources are investigated
15	•	Multiple corona bursts observed by LOFAR in lightning may be seen as a fast (>

- 10^7 m/s) moving source by typical lightning interferometers
- The resolution of typical lightning interferometers needs to be improved to resolve the structure in lightning processes

 $Corresponding \ author: \ Ningyu \ Liu, \ \texttt{Ningyu}. \texttt{Liu} \texttt{Qunh.edu}$

19 Abstract

Recent observations from LOFAR indicate that multiple, spatially distributed corona 20 bursts can occur in lightning processes on the order of 10 microseconds. The close prox-21 imity of the corona bursts in space and time poses a great observation challenge for ded-22 icated lightning radio interferometers, typically with <100 m baselines. This paper re-23 ports simulations to show the interferometry results that would be obtained with a typ-24 ical lightning interferometer for such a lightning process. In particular, spatially-separated 25 corona bursts at fixed locations may be seen as a fast $(> 10^7 \text{ m/s})$ propagating source 26 for an instrument with resolution greater than the spatial separation of the bursts. The 27 implications and suggestions for lightning interferometry studies are discussed in the pa-28 per. 29

³⁰ Plain Language Summary

Lightning evolution contains brief processes that are critical to its channel forma-31 tion, but their physical mechanisms are poorly understood at present. Those processes 32 emit very high frequency radio emissions, and radio sensor arrays have been used to de-33 tect those emissions to investigate their source processes. The latest observations from 34 the large radio telescope LOFAR show that multiple, intense bursts of radio emission at 35 discrete locations occur in those processes. Here we report simulations to show that such 36 bursts are seen as a fast propagating wave for a typical lightning radio sensor array. Our 37 study suggests that caution is required when interpreting the observations made with 38 such a radio sensor array. 39

40 **1** Introduction

Lightning is a complex and multiscale electrical phenomenon that generates a broad 41 spectrum of electromagnetic radiation. Fast electrical discharge processes occur during 42 lightning development and they generate high frequency (HF, 0.3-3 MHz) and very high 43 frequency (VHF, 30-300 MHz) electromagnetic emissions. These radio frequency (RF) 44 emissions have been utilized to map and/or image lightning via some form of interfer-45 ometry analysis. Important advances have recently been made based on broadband HF/VHF 46 interferometer observations. These include identification of fast breakdown processes ca-47 pable of initiating lightning (Rison et al., 2016; Stock et al., 2017; Tilles et al., 2019; Huang 48 et al., 2021), measurement of perpendicular-to-channel polarization of the radiation of 49 dart leaders (Shao et al., 2018), discovery of needle-like structures on positive leaders (Hare 50 et al., 2019; Pu & Cummer, 2019), and observation of corona bursts of negative leaders 51 at high altitudes (Scholten et al., 2021a). Because the lightning VHF sources can have 52 complex temporal, spatial, and spectral properties, the radiation amplitude has a very 53 large dynamic range, and they occur in a generally noisy environment, lightning inter-54 ferometer observation and interpretation is definitely not a trivial task. 55

Modeling and theoretical work has shown that filamentary streamer discharges can 56 radiate strongly in the HF and VHF bands (Shi et al., 2016, 2019), and they are believed 57 to be the main source of the HF and VHF radiation from lightning (Liu et al., 2019, 2020; 58 Liu & Dwyer, 2020). For many lightning processes, such as a leader step or lightning ini-59 tiating fast breakdown, a large number $(10^5 - 10^8)$ of streamers are believed to be involved 60 (Liu et al., 2019, 2020; Liu & Dwyer, 2020). Those processes have a typical timescale 61 of at least one microsecond and a spatial scale of at least a few meters, in contrast to 62 the nanosecond timescale and centimeter spatial scale of a streamer. The large differ-63 ence in those scales implies that there is inherent random nature in both spatial and tem-64 poral distributions of streamer occurrences in a lightning process. 65

In this study, we attempt to demonstrate how the random nature of streamer oc-66 currences in a lightning process can complicate the analysis of lightning interferometer 67 observations. Our study focuses on the initiation stage of lightning, which typically con-68 tains only few channel branches, making the analysis of the interferometer observation 69 easier. One common feature in the RF observation of lightning initiation is that a train 70 of strong bipolar pulses occurs in the first few milliseconds (e.g., Nag et al., 2009; Mar-71 shall et al., 2014; Belz et al., 2020; Tilles, 2020). They are called initial breakdown pulses 72 (IBPs), which are best observed by a RF sensor sensitive to lower RF frequency bands 73 (e.g., 1 kHz-1 MHz). The duration of an IBP varies from 20 to 100 μ s, with a mean of 74 $\sim 60 \ \mu s$. There are usually narrow subpulses superimposed on the initial half cycle of the 75 waveform (e.g., Nag et al., 2009; Belz et al., 2020; Tilles, 2020). 76

A typical broadband VHF interferometer for lightning observation consists of three 77 radio sensors with a baseline shorter than 100 m (Sun et al., 2013; Stock et al., 2014; Ri-78 son et al., 2016; Stock et al., 2017; Shao et al., 2018; Lyu et al., 2019; Tilles et al., 2019, 79 2020; Belz et al., 2020). The passband of the sensor spans from the upper HF band to 80 the lower VHF band, e.g., 10-90 MHz for the interferometer developed by the New Mex-81 ico Tech (Stock et al., 2014; Rison et al., 2016). The resulting angular resolution limit 82 for non super-resolution analysis is $\lambda/b = 0.06$ radians, where λ is the wavelength and 83 b is the baseline length, corresponding to 600 m at a distance of 10 km. The observa-84 tions obtained with such an interferometer indicate that IBPs are coincident with strong 85 VHF bursts and the VHF source activity shows greatly accelerated vertical motion over 86 a distance of 100 m or so, typically during the initial half cycle of the IBP. The speed 87 of the accelerated vertical motion exceeds 10^7 m/s (Belz et al., 2020; Tilles, 2020). It has 88 been proposed that IBPs are generated by fast breakdown, the same as narrow bipolar events (NBEs) (Belz et al., 2020). Belz et al. (2020) also found that gamma-ray produc-90 tion by lightning is directly connected to strong IBPs. 91

Better resolution can be achieved with a large radio telescope like LOFAR (Hare 92 et al., 2019, 2020; Scholten et al., 2021a, 2021b). A recently-developed interferometry 93 imaging code called interferometric 3-Dimensional (TRI-D) imager allows for meter scale 94 accuracy in the LOFAR emission sources at a temporal resolution of 100 ns, which is able 95 to show the structures within a lightning leader step (Scholten et al., 2021b) (see (Hare 96 et al., 2020) as well for the leader step structure). The results reported by Scholten et 97 al. (2021) indicate that during an IBP multiple corona bursts occur at discrete locations 98 within a volume of approximately $100 \times 100 \times 100$ m³ and there is no indication of a 99 continuously propagating wave of intense electrical breakdown. 100

In this paper, we present simulations to show the results a typical lightning interferometer with a small number of elements would obtain for IBPs consisting of multiple corona bursts and to give some ideas on the requirements for an interferometer to resolve those corona bursts.

¹⁰⁵ 2 Simulation Model

The main goal of simulation is to reproduce the interferometer images of synthetic VHF sources with specified spatial and temporal properties to understand the interferometer observations. The simulation consists of two main stages. The first stage simulates the VHF radiation from sources and the signals recorded by the sensors. At the second stage, the signals are processed and then used to obtain the image of the source with interferometry analysis.

Figure 1a shows a plan view of the observation geometry considered in our simulation. For simplicity, we consider an interferometer of three elements only. The sensors form an equilateral triangle as shown by the three closely-packed triangles in the figure, with one of the baselines parallel to the x axis. The VHF emission sources are at x =



Figure 1. (a) Observation geometry in the simulation. (b) Histogram of the streamer onset.

y = 0, and the plan distance from the center of the sensor triangle to the source is 8 km, i.e., the center of the sensor triangle is at (8 km, -135°) in polar coordinates. The sources are at approximately 6 km altitude, and the distance from a sensor to the source is then about 10 km. This geometry closely represents the IBPs in cloud-to-ground lightning analyzed in (Tilles, 2020).

In the simulation, the right most sensor is set as the reference sensor or viewing point, for which the interferometric images are constructed. Its location varies as the baseline changes, because the location of the sensor triangle center is fixed. The images are made for a small area of 1.6° azimuth and 2° elevation centered around the centroid of the sources. In this setting, the location of the center of the image relative to the reference antenna varies when the baseline length changes, and its azimuth is about 45°, but not exactly.

128

2.1 Simple Model for VHF Radiating Corona Bursts in IBPs

The VHF radiation source model used in our study is formulated based on LOFAR 129 observations. As mentioned in Introduction, the LOFAR data indicate that an IBP con-130 tains multiple corona bursts at different locations. In our simulation, we simply assume 131 there are two corona bursts at two different altitudes: 6.1 km and 6.0 km, i.e., a 100 m 132 height difference. We further assume that each burst contains 10^4 streamers, with the 133 burst at the higher altitude occurring a few microseconds earlier. The onset times of the 134 streamers within a burst are randomly drawn from an asymmetric Laplace distribution, 135 with a 0.4 μ s rise time and 1 μ s fall time. Figure 1b shows the histogram of the streamer 136 onset for a simulation case reported below, where the peaks of the two bursts are sep-137 arated by 10 μ s in time. 138

The streamers are assumed to be identical, and each generates a brief current pulse, which is assumed to be a double exponential function with a rise time of 1 ns and a fall time of 250 ns (Liu et al., 2019; Liu & Dwyer, 2020). The streamer current pulse and spectrum of the radiated field are shown by Figure S1 in Supplementary information.

143

2.2 Cross-correlation Based Imaging Technique

To construct the image using the recorded signals, we adopt the same cross-correlation based imaging technique as Stock (2014) and Tilles et al. (2019). Cross-correlations between signals from pairs of sensors are calculated and used to assign intensities to image pixels. In addition, a beamforming technique is implemented in our simulation in
order to improve the temporal resolution and accuracy. If we know where the source region is, we can use the center of the source region to estimate the respective time delays
from the source to the sensors and then use the estimated delays to preliminarily align
the signals. In this way, a smaller time window can be used to calculate the cross-correlation,
which improves the temporal resolution.

The above description can be represented mathematically as follows. Suppose the time series recorded by each sensor is denoted by $E_i(t)$ and the time-shifted signal by $E_i^{o}(t)$, we have

$$E_i^{\mathbf{o}}(t) = E_i(t + \tau_i),\tag{1}$$

where τ_i is the light travel time from the center of the source region to the *i*th sensor. The center of the source region is also set as the center (denoted by point *o*) of the image in the simulation. Let d_i^{o} represent the distance between point *o* and the *i*th sensor, then $\tau_i = d_i^{o}/c$.

To obtain the beamformed image frame corresponding to a time interval $[t_n, t_n + T]$, where T is the time integration window size or exposure time of the image, the cross correlation between every pair of antennas i and j, R_{ij}^{o} , is calculated:

$$R_{ij}^{o}(t_n, \tau_{ij}) = \int_{t_n}^{t_n+T} E_j^{o}(t+\tau_{ij}) E_i^{o}(t) dt, \qquad (2)$$

where τ_{ij} is the time delay between the time-shifted series. Substituting equation (1) into (2) and changing the integration variable to $(t + \tau_i)$,

167
$$R_{ij}^{o}(t_n, \tau_{ij}) = \int_{t_n + \tau_i}^{t_n + \tau_i + T} E_j(t + \tau_{ij} + \tau_j - \tau_i) E_i(t) dt = R_{ij}(t_n + \tau_i, \tau_{ij} + \tau_j - \tau_i).$$
(3)

Note $R_{ij}(t_n + \tau_i, \tau_{ij} + \tau_j - \tau_i)$ is the cross correlation between the non-shifted time series. From the observation geometry, we have $(d_{ij} \cos \alpha_{ij})/c = \tau_{ij} + \tau_j - \tau_i$, where d_{ij} is the baseline and α_{ij} is the directional angle. So

$$\tau_{ij} = \frac{d_{ij} \cos \alpha_{ij}}{c} - \tau_j + \tau_i.$$
(4)

Equation (4) relates the directional angle to the delay between the shifted time series of the two sensors.

For each pixel, its directional angle with respect to a baseline is calculated first and 174 the corresponding delay τ_{ij} between the two shifted time series is found by using equa-175 tion (4). The intensity of the pixel is then given by $R_{ij}^{o}(t_n, \tau_{ij})$. For the last step, inter-176 polation is necessary as $R_{ij}^{o}(t_n, \tau_{ij})$ is found at discrete times or only the cross correla-177 tions at discrete angels α_{ij} are known. Test runs indicate a higher order interpolation 178 scheme is necessary to obtain accurate results, and cubic spline interpolation with the 179 not-a-knot end condition is used in our study. Furthermore, the same interpolation scheme 180 is also used to preliminarily align the signals at the beamforming step. 181

Intensities from all baselines are then added together to obtain the total intensity of that pixel. Denote the intensity of the *n*th frame from a baseline as $I_{ij}(n, \alpha_{ij}) = R_{ij}^{o}(t_n, \tau_{ij})$, we have

$$I(n, \vec{r}) = \sum_{i}^{M} \sum_{j=i+1}^{M} I_{ij}(n, \alpha_{ij}),$$
(5)

185

156

164

171

where M is the total number of sensors.

If the *i*th antenna is the reference antenna, the time of the *n*th image frame is set to $(t_n + T/2 + \tau_i)$.

Case	Burst Time Separation (μs)	Passband (MHz)	Baseline (m)	Integration Time Window (μs)	Frame Time Shift (μs)
А	10	10-90	100	1.4	0.35
В	10	30-80	100	0.1	0.1
\mathbf{C}	5	30-80	800	0.1	0.1
D	10	100-200	200	0.02	0.02

Table 1. Parameters of the Four Simulation Cases

189 **3 Results**

Results from four simulation cases are presented below, and Table 1 gives the pa-190 rameters of each simulation case. We consider two values for the time separation between 191 the two bursts: 5 and 10 μ s. Given the duration of IBPs, 10 μ s represents a moderate 192 value of the time separation between the bursts, and 5 μ s for relatively narrow IBP pulses. 193 In calculating the radiated electric field, a time step of 1 nanosecond (i.e., 1 GHz sam-194 pling frequency) is used. For each case, a bandpass filter is applied to the recored sig-195 nals to obtain the specified bandwidth. Frame time shift is the time between two con-196 secutive images, and there is no sample overlap between the images except for Case A, 197 where the time shift is one quarter of the time integration window. Case A represents 198 the typical configuration that was used in (Tilles et al., 2019, 2020; Tilles, 2020). As a 199 large time integration window is used for this case, it is unnecessary to apply the beam-200 forming technique. Except the baseline and the number of antennas, Cases B and C rep-201 resent the configuration of the latest LOFAR studies (Scholten et al., 2021b, 2021). The 202 last case is a system that represents a moderate increase in both the passband frequency 203 and baseline of a typical radio interferometer dedicated to lightning research. 204

Figure 2 presents the simulation results from Case A. The three images correspond 205 to three different time intervals, with their respective center times given in the figure. 206 The bandwidth limited signal in Figure 2b shows although the two bursts are nominally 207 separated by 10 μ s, streamer activity is nearly continuous between them. The circles in 208 Figure 2c give the heights (relative to 6 km) of the maximum intensity pixel of the im-209 ages, while Figure 2d shows the temporal variation of the intensity of the same pixel. Each 210 image in Figure 2a corresponds to either a peak or trough in Figure 2d. The large size 211 of the main lobe in each image even under a narrow display intensity range is consistent 212 with the nominal angular resolution of this case: $\lambda/b \simeq 0.06$ radians or 3.4 degrees. Be-213 fore 44 μ s or slightly after 46 μ s, the maximum intensity pixel overlaps with the loca-214 tion of the active streamer burst. The smooth transition in height from approximately 215 80 m to 20 m, starting slightly after 44 μ s and ending slightly after 46 μ s, makes it ap-216 pear that the source moves with a speed of $\simeq 3 \times 10^7$ m/s. The image at 45.753 μ s shows 217 that the maximum intensity pixel of that image is approximately at the mid point be-218 tween the two bursts. Figure 2d shows that the intensity reaches the maximal value at 219 the peaks of the bursts and is relatively small between the two bursts. The difference 220 between the maximal and minimal values is, however, less than three orders of magni-221 tude (note that the maximal intensity shown in the image at 45.753 μ s is less than three 222 orders of magnitude than the other two images), which is well within the dynamic range 223 of a RF sensor of at least 12 bits. The image is made for a constant radial distance from 224 the reference center, equal to the distance from the reference sensor to the center of the 225 image at the mid point between the two bursts, i.e., (0 m, 0 m, 6050 m). This causes the 226 heights of the two bursts are not exactly at 0 and 100 m (i.e., 6 and 6.1 km relative to 227 ground), respectively. 228



Figure 2. Case A simulation results. (a) Images at three different times. In each image, black '+' represents the center of the image, the two circles give the locations of the two streamer bursts, and the solid circle shows the location of the maximum intensity pixel. (b) The bandwidth limited signal from the reference sensor. (c) The height of the maximum intensity pixel relative to 6 km altitude. (d) The value of the maximum intensity pixel.

Figure 3 shows the simulation results from Case B. As the baseline is the same be-229 tween this case and Case A and the frequency passband is approximately the same, the 230 images of Case B are similar to those shown in Figure 2, which are omitted here. The 231 apparent fast descending motion of the source can also be seen around 44-46 μ s, with 232 a similar change in the height and thus a similar speed. Because the time integration win-233 dow is more than a factor of ten smaller than Case A, the fluctuations in the height and 234 intensity of the maximum intensity pixel are much larger. The smaller time integration 235 window also results in smaller intensity values. 236

Figure 4 presents the results from cases C and D. For Case C, the baseline is in-237 creased to 800 m while the bandwidth is kept the same as Case B, resulting in a much 238 better angular resolution. The main lobe in Figure 4a is much smaller in size, compar-239 ing to those in Figure 2a. Figure 4b shows that the streamer activity continuously oc-240 curs from the beginning of the first burst through the end of the second burst. It is clear, 241 however, from Figure 4c that the sources have discrete locations instead of forming a grad-242 ual descending trajectory. Due to the random nature of the streamer onset in each burst. 243 the locations of the maximum intensity pixel between the two bursts can jump between 244 the two true source locations. Finally, because of the smaller time separation between 245 the bursts, the minimum intensity is less than two orders of magnitude smaller than the 246 maximum intensity, as shown by Figure 4d. Overall, the increased baseline or improved 247 angular resolution allows for resolving the two bursts even with a smaller time separa-248 tion of 5 μ s. 249

For Case D, both the passband frequency and baseline are moderately increased from Case A, so the angular resolution is better than Case A. The size of the main lobe shown in Figure 4e is smaller than that of Case A, but not as small as that of Case C. The time integration window 20 ns of this case is twice the reciprocal of the bandwidth,



Figure 3. Case B simulation results. (a) The bandwidth limited signal from the reference sensor. (b) The height of the maximum intensity pixel relative to 6 km altitude. (c) The value of the maximum intensity pixel.

and beamforming is definitely required in order to use such a small time window. For this configuration, simply tracking the location of the maximum intensity pixel can tell that the radiation is not produced by a single moving source but by sources at discrete locations. Abrupt changes in the source height do occur in the time interval between the two bursts. The source height there is determined by which burst happens to generate stronger radiation in the corresponding 20 ns time window. Consistently, sudden changes occur in the intensity of the image.

$_{261}$ 4 Discussion

The present study demonstrates that careful interpretation of lightning VHF in-262 terferometer observations is required because the emission sources may have complex spa-263 tial and temporal properties while the resolution of a typical lightning interferometer is 264 limited. Even for a simple case of two corona bursts with reasonable separation in space 265 and time considered here, the simulation results show that entirely different views of the 266 spatiotemporal evolution of the source can be obtained with different interferometer spec-267 ifications and imaging parameters. On the positive side, this also means that great op-268 portunities for advancing lightning physics await for lightning interferometry studies with 269 improved resolution. It should be pointed out that in our simulation the bursts are at 270 fixed locations and noise is not included for convenience, which will also make resolv-271 ing the realistic corona bursts more challenging. 272

To resolve the corona bursts that occur in close space and time, the spatial resolution of the instrument is the key. When the main lobe of the instrument is too large, extending over an area larger than the spatial separation between the bursts, the max-



Figure 4. Results from simulation cases C and D. (a, e) The image with the highest intensity during the entire simulation. In the image, black '+' represents the center of the image, the two circles give the locations of the two streamer bursts, and '*' shows the location of the maximum intensity pixel. (b, f) The bandwidth limited signal from the reference sensor. (c, g) The height of the maximum intensity pixel relative to 6 km altitude. (d, h) The value of the maximum intensity pixel.

imal intensity can appear at a location between them at the moment when the two bursts 276 have comparable intensities. To improve the angular resolution λ/b , either the baseline, 277 frequency, or both can be increased, as demonstrated by the simulation cases C and D. 278 One factor that should also be taken into account is the source spectrum. The HF and 279 VHF frequency spectrum of a corona burst is determined by the spectrum of individ-280 ual streamers (Liu et al., 2019, 2020; Liu & Dwver, 2020). Although the streamer spec-281 trum considered here quickly rolls off above a few tens of MHz (see Figure S1), the re-282 cent study by Pu et al. (2021) indicates the streamer spectrum in lightning processes can 283 extend to higher frequency range. Therefore, increasing the frequency of the sensor should 284 be effective in improving the resolution for at least some lightning processes. 285

It is also worth implementing algorithms or methods that can improve the tem-286 poral resolution of the imaging, such as the beamforming technique. Increasing the tem-287 poral resolution helps through reducing the chance of streamers from any two bursts to 288 occur within the time window of an image. Its effectiveness depends on the number of 289 streamers in a corona burst and separation between the bursts. In addition, future stud-290 ies should explore imaging techniques beyond time difference of arrival based approaches. 291 Imaging algorithms utilizing larger numbers of baselines in Fourier based approaches com-292 bined with deconvolution such as CLEAN (Clark, 1980) are one direction similar to as-293 tronomical imaging. Multiple source direction of arrival algorithms based on covariance 294 estimations such as MUSIC (Schmidt, 1986) are another direction. These algorithms have significant advantages for resolving ambiguities, using array degrees of freedom to en-296 able estimation of multiple sources, and ultimately helping to resolve corona bursts. Ad-297 ditionally, these approaches are more suitable for the formal incorporation of array cal-298 ibration to remove the effects of the interferometer element and array responses. 299

Finally, simulation can provide a good understanding of the dependence of the ob-300 tained source dynamics on the burst parameters to aid the analysis of the interferom-301 eter data. For instance, the apparent fast downward motion in Case A is inferred dur-302 ing the fall of the first burst and the rise of the second. The apparent speed then con-303 tains information about those times. In the case when radio sensors may be saturated 304 during the corona bursts, and the interferometer does not have the resolution to resolve 305 individual bursts, the apparent speed can still be determined (interferometry is gener-306 ally robust in the case of signal saturation) and can still give information about the spa-307 tiotemporal evolution of the individual corona bursts. Another example is to understand 308 and constrain the bidirectional development of fast breakdown reported by Huang et al. 309 (2021). The bidirectional fast breakdown likely contains separate VHF sources that prop-310 agate either upward or downward. Simulations can provide the constraints on the source 311 parameters in order for the sources to be resolved by a particular instrument. In fact, 312 work is currently underway to simulate LOFAR observations to investigate accuracy and 313 imaging artifacts of the LOFAR interferometry analysis (Scholten et al., 2021). 314

315 Open Research

The MATLAB scripts and functions used to obtain the results reported in the paper are available here: https://doi.org/10.5281/zenodo.5761824.

318 Acknowledgments

³¹⁹ This research was supported in part by AFOSR Awards FA9550-18-1-0358 and FA9550-

- 21-1-0366 to the University of New Hampshire and a subaward of DARPA HR00112120003
- Grant to Embry-Riddle Aeronautical University.

322 References

Belz, J. W., Krehbiel, P. R., Remington, J., Stanley, M. A., Abbasi, R. U., LeVon,

- R., ... Zundel, Z. (2020, December). Observations of the Origin of Downward 324 Terrestrial Gamma-Ray Flashes. J. Geophys. Res. Atmos., 125(23), e31940. 325 doi: 10.1029/2019JD031940 326 Clark, B. G. (1980, September).An efficient implementation of the algorithm 327 'CLEAN'. Astron. Astrophys., 89(3), 377. 328 Hare, B. M., Scholten, O., Dwyer, J., Ebert, U., Nijdam, S., Bonardi, A., ... 329 Winchen, T. (2020, March). Radio emission reveals inner meter-scale structure 330 of negative lightning leader steps. Phys. Rev. Lett., 124 (10), 105101. doi: 331 10.1103/PhysRevLett.124.105101 332 Hare, B. M., Scholten, O., Dwyer, J., Trinh, T. N. G., Buitink, S., ter Veen, S., ... 333 others (2019, Apr). Needle-like structures discovered on positively charged 334 lightning branches. Nature, 568, 360-363. doi: 10.1038/s41586-019-1086-6 335 Huang, A., Cummer, S. A., & Pu, Y. (2021, April). Lightning initiation from fast 336 negative breakdown is led by positive polarity dominated streamers. Geophys. 337 Res. Lett., 48(8), e91553. doi: 10.1029/2020GL091553 338 Liu, N. Y., & Dwyer, J. R. (2020, December). Thunderstorm high frequency radio 339 bursts with weak low frequency radiation. Geophys. Res. Lett., 47(23), e90325. 340 doi: 10.1029/2020GL090325 341 Liu, N. Y., Dwyer, J. R., & Tilles, J. N. (2020, July). Electromagnetic radiation 342 spectrum of a composite system. Phys. Rev. Lett., 125(2), 025101. doi: 10343 .1103/PhysRevLett.125.025101 344 Liu, N. Y., Dwyer, J. R., Tilles, J. N., Stanley, M. A., Krehbiel, P. R., Rison, 345 W., ... Wilson, J. G. (2019).Understanding the radio spectrum of nar-346 row bipolar events. J. Geophys. Res. Atmos., 124, 10134-10153. doi: 347 10.1029/2019JD030439 348 Lyu, F., Cummer, S. A., Qin, Z., & Chen, M. (2019, Mar). Lightning initiation pro-349 cesses imaged with very high frequency broadband interferometry. J. Geophys. 350 Res. Atmos., 124, 2994-3004. doi: 10.1029/2018JD029817 351 Marshall, T. C., Schulz, W., Karunarathna, N., Karunarathne, S., Stolzenburg, M., 352 Vergeiner, C., & Warner, T. (2014, January). On the percentage of lightning 353 flashes that begin with initial breakdown pulses. J. Geophys. Res. Atmos., 354 119, 445-460. doi: 10.1002/2013JD020854 355 Nag, A., DeCarlo, B. A., & Rakov, V. A. (2009, Feb). Analysis of microsecond-356 and submicrosecond-scale electric field pulses produced by cloud and 357 ground lightning discharges. Atmos. Res., 91(2), 316-325. doi: 10.1016/ 358 j.atmosres.2008.01.014 359 Pu, Y., & Cummer, S. A. (2019, November). Needles and lightning leader dynam-360 ics imaged with 100-200 MHz broadband VHF interferometry. Geophys. Res. 361 Lett., 46(22), 13,556-13,563. doi: 10.1029/2019GL085635 362 Pu, Y., Cummer, S. A., & Liu, N. (2021). VHF radio spectrum of a positive leader 363 and implications for electric fields. Geophysical Research Letters, 48(11), 364 e2021GL093145. 365 Rison, W., Krehbiel, P. R., Stock, M. G., Edens, H. E., Shao, X.-M., Thomas, 366 R. J., ... Zhang, Y. (2016).Observations of narrow bipolar events re-367 veal how lightning is initiated in thunderstorms. Nat. Commun., 7. doi: 368 10.1038/ncomms10721 Schmidt, R. (1986).Multiple emitter location and signal parameter estimation. 370 34(3), 276-280.371 Scholten, O., Hare, B. M., Dwyer, J., Liu, N., Sterpka, C., Buitink, S., ... Winchen, 372 Т. (2021a). Distinguishing features of high altitude negative leaders as ob-373 served with LOFAR. Atmos. Res., 260, 105688. Retrieved from https:// 374 www.sciencedirect.com/science/article/pii/S0169809521002404 doi: 375 https://doi.org/10.1016/j.atmosres.2021.105688 376 Scholten, O., Hare, B. M., Dwyer, J., Liu, N., Sterpka, C., Buitink, S., ... ter Veen, 377
- 378 S. (2021b, September). Time resolved 3D interferometric imaging of a sec-

379	tion of a negative leader with LOFAR. Phys. Rev. D, $104(6)$, 063022. doi:
380	10.1103/PhysRevD.104.063022
381	Scholten, O., Hare, B. M., Dwyer, J., Liu, N., Sterpka, C., Kolmasov, I., ter
382	veen, S. (2021, October). Interferometric imaging of intensely radiating
383	negative leaders. arAiv e-prints, arAiv:2110.02547.
384	Shao, AM., no, C., Callfey, M., Granalli, F., naylies, D., Dowers, G., Ras-
385	(DIMAR) observations of lightning discharges. Deveoling new physics insights
386	(DIMAR) observations of lightning discharges. Revealing new physics insights into breakdown processes L Geophice Res. Atmag. 192(18) 10.326 10.340
387	Betrieved from https://agupubs.onlinelibrary.uiley.com/doi/abs/
388	10 1029/2018 ID029096 d_{0i} : 10 1020/2018 ID020006
389	Shi F Liu N V Dwyer I B k Ibaddadene K (2019) VHF and UHF elec-
201	tromagnetic radiation produced by streamers in lightning Geonbus Res Lett
302	46 443-451 doi: 10.1029/2018GL080309
393	Shi, F., Liu, N. Y., & Rassoul, H. K. (2016). Properties of relatively long streamers
394	initiated from an isolated hydrometeor. J. Geophys. Res. Atmos., 121, 7284–
395	7295. doi: 10.1002/2015JD024580
396	Stock, M. (2014). Broadband interferometry of lightning (Doctoral dissertation,
397	New Mexico Institute of Mining and Technology). Retrieved from https://
398	www.proquest.com/dissertations-theses/broadband-interferometry
399	-lightning/docview/1660201463/se-2
400	Stock, M. G., Akita, M., Krehbiel, P. R., Rison, W., Edens, H. E., Kawasaki, Z., &
401	Stanley, M. A. (2014). Continuous broadband digital interferometry of light-
402	ning using a generalized cross-correlation algorithm. J. Geophys. Res. Atmos.,
403	119, 3134-3165. Retrieved from http://dx.doi.org/10.1002/2013JD020217
404	doi: 10.1002/2013JD020217
405	Stock, M. G., Krehbiel, P. R., Lapierre, J., Wu, T., Stanley, M. A., & Edens, H. E.
406	(2017). Fast positive breakdown in lightning. J. Geophys. Res. Atmos., 122,
407	8135-8152. Retrieved from https://agupubs.onlinelibrary.wiley.com/
408	doi/abs/10.1002/2016JD025909 doi: 10.1002/2016JD025909
409	Sun, Z., Qie, X., Liu, M., Cao, D., & Wang, D. (2013, July). Lightning VHF
410	radiation location system based on short-baseline TDOA technique —
411	Validation in rocket-triggered lightning. Atmos. Res., 129, 58-66. doi:
412	10.1016 J.atmosres. 2012.11.010
413	Tilles, J. N. (2020). Broadband radio mapping and imaging of lightning processes
414	(Doctoral dissertation, University of New Hampshire, Durnam, NH). Retrieved
415	Tilles IN Knehbiel D. D. Stenley M. A. Dison W. Lin N. V. Lun E.
416	Wilson I (2020 October) Padic interference of spectrations of an energetia
417	in aloud pulse reveal large currents generated by relativistic discharges
418	G_{eonbus} Res A_{tmos} 195(20) a 22602 doi: 10.1020/2020 ID022602
419	Tilles I N Liu N V Stanley M A Krebbiel P R Rison W Stock M C
420	Wilson I G (2019) Fast negative breakdown in thunderstorms Nat
421	C_{ommun} 10 doi: 10.1038/s41467-019-09621-z
422	Continuant, 10. 401. 10.1000/ STITOL 013-03021-2

Supporting Information for "Implications of Multiple Corona Bursts in Lightning Processes for Radio Frequency Interferometer Observations"

Ningyu Liu¹, Olaf Scholten², Joseph R. Dwyer¹, Brian M. Hare²,

Christopher F. Sterpka¹, Julia N. Tilles³, and Frank D. Lind⁴

¹Department of Physics and Astronomy & Space Science Center (EOS), University of New Hampshire, Durham, New Hampshire,

USA

²University Groningen, Kapteyn Astronomical Institute, Landleven 12, 9747 AD Groningen, The Netherlands

 $^3 \mathrm{Sandia}$ National Laboratories, Albuquerque, NM, USA

 $^4\mathrm{MIT}$ Haystack Observatory, Westford, Massachusetts, USA

Contents of this file

1. Figures S1

December 6, 2021, 10:36am



Figure S1. (a) The current moment pulse of a streamer. (b) The time derivative of the streamer current moment. (c) The frequency spectrum of the streamer current moment time derivative. The streamer current moment pulse is a double exponential function with a rise time of 1 ns, a fall time of 250 ns, and a peak of $\simeq 1$ A-m. As the radiated field is proportional to the dM/dt, each streamer produces a narrow field pulse of $\simeq 4$ ns followed by a weak and relatively long tail. The frequency spectrum of dM/dt shows the radiation is peaked in the HF and VHF bands.