# Plasma Parameters from Quasi-Thermal Noise Observed by Parker Solar Probe: A New Model for the Antenna Response

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November 21, 2022

# Abstract

Quasi-Thermal Noise (QTN) spectroscopy is a reliable diagnostic routinely used for measuring electron density and temperature in space plasmas. The observed spectrum depends on both antenna geometry and plasma kinetic properties. Parker Solar Probe (PSP), launched in 2018, is equipped with an antenna system consisting of two linear dipoles with a significant gap between the antenna arms. Such a configuration, not utilized on previous missions, cannot be completely described by current models of the antenna response function. In this work, we calculate the current distribution and the corresponding response function for the PSP antenna geometry, and use these results to generate synthetic QTN spectra. Applying this model to the Encounter 7 observations from PSP provides accurate estimations of electron density and temperature, which are in very good agreement with particle analyzer measurements.









# Plasma Parameters from Quasi-Thermal Noise Observed by Parker Solar Probe: A New Model for the Antenna Response

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18	•	We model the antenna response for the unique geometry of linear dipole antenna
19		containing a gap between arms
20	•	This antenna response is used to improve plasma parameters determination from
21		the observed quasi-thermal noise spectrum
22	•	The proposed model yields derived electron parameters consistent with those from
23		the SWEAP/SPAN instrument suite onboard Parker Solar Probe

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#### 24 Abstract

Quasi-Thermal Noise (QTN) spectroscopy is a reliable diagnostic routinely used for mea-25 suring electron density and temperature in space plasmas. The observed spectrum de-26 pends on both antenna geometry and plasma kinetic properties. Parker Solar Probe (PSP), 27 launched in 2018, is equipped with an antenna system consisting of two linear dipoles 28 with a significant gap between the antenna arms. Such a configuration, not utilized on 29 previous missions, cannot be completely described by current models of the antenna re-30 sponse function. In this work, we calculate the current distribution and the correspond-31 ing response function for the PSP antenna geometry, and use these results to generate 32 synthetic QTN spectra. Applying this model to the Encounter 7 observations from PSP 33 provides accurate estimations of electron density and temperature, which are in very good 34 agreement with particle analyzer measurements. 35

# <sup>36</sup> Plain Language Summary

Parker Solar Probe (PSP) is a NASA mission that is travelling much closer to the 37 Sun than any previous spacecraft. A primary consequence of this specific trajectory are 38 multiple adaptations in the design of instruments (radio instruments, magnetometers, 39 particle detectors etc.) and their complex accommodations on the spacecraft. This ar-40 ticle investigates effects of the specific PSP radio antenna geometry to high-frequency 41 electric field observations. We apply Quasi-Thermal Noise Spectroscopy, a well estab-42 lished method for determining plasma density and temperature, to PSP instruments, and 43 validate the results by comparing the parameter values from radio observations to the 44 ones obtained by particle analyzers onboard PSP. 45

#### 46 1 Introduction

QTN spectroscopy, theoretically described more than half a century ago (Andronov, 47 1966; Fejer & Kan, 1969), is a powerful tool to diagnose space plasmas using a passive 48 electric antenna related to a sensitive radio receiver. Since this method was fully expanded 49 to solar wind and pioneered aboard ISEE-3 (Meyer-Vernet, 1979; Hoang et al., 1980), 50 it has been routinely used to infer in-situ electron densities and temperatures on vari-51 ous missions in the solar wind: IMP-6 (Kellogg, 1981), Ulysses (Maksimovic et al., 1995; 52 Issautier et al., 1996, 1999; Le Chat et al., 2011), Wind (Maksimovic et al., 1998; Issautier 53 et al., 2005; Martinović et al., 2020), STEREO (Zouganelis et al., 2010; Martinović et 54 al., 2016), and planetary missions such as *Cassini* (Moncuquet et al., 1997, 2005). 55

QTN spectrum depends on two sets of inputs: 1) kinetic plasma properties, reflected 56 through the electron VDF shape, and described by characteristic plasma functions that 57 depend on the VDF, and 2) antenna shape and configuration, described by the antenna 58 response function (ARF). For a comprehensive review of the QTN spectroscopy theory 59 see e.g. Meyer-Vernet and Perche (1989); Meyer-Vernet et al. (2017). All the aforemen-60 tioned missions have significantly different characteristic spectra due to different antenna 61 configurations. These differences can be summed up in two broad categories: 1) the vis-62 ibility of the plasma peak just above the electron plasma frequency  $f_p = \omega_p/2\pi = (2\pi)^{-1}\sqrt{n_e e^2/\epsilon_0 m_e}$ , 63 depending on the ratio between the antenna length  $L_{ant}$  and Debye length  $L_D$ , where 64  $L_D = \sqrt{\epsilon_0 k_b T_e / n_e e^2}$  and 2) the effects of the impact noise, determined by the ratio of 65 the antenna length to its radius  $L_{ant}/a_{ant}$ . Here,  $\epsilon_0$  is the dielectric permittivity of vac-66 uum,  $k_b$  is the Boltzmann constant, and  $n_e$ , e and  $m_e$  are electron density, charge and 67 mass, respectively. A common feature of spacecraft launched before PSP was a dipole 68 antenna configuration with a negligibly small gap between the antenna arms, and the 69 spacecraft body effects being also considered as negligible. The *PSP* FIELDS suite (Bale 70 71 et al., 2016) is equipped with a set of two wire dipoles, with each arm  $L_{ant} = 2m \log 2$ The spacecraft (SC) body separates the antenna ports, creating a gap between the arms 72 of each dipole of 2d = 2.98m, a length comparable to  $L_{ant}$ . Configurations that fea-73

ture the gap operate only on PSP FIELDS (Bale et al., 2016) and Solar Orbiter Radio 74 and Plasma Waves (RPW) (Maksimović, Bale, Chust, et al., 2020) instruments, and ini-75 tial observations showed that the total electron density could be inferred by locating the 76 peak of the signal at  $f_p \sim \sqrt{n_e}$  (Bale et al., 2019). However, the shape of the observed 77 QTN spectra cannot be modelled by the ARFs derived for the case of dipoles without 78 a gap (Kuehl, 1966, 1967). As the discrepancies due to this gap primarily appear in the 79 vicinity of the plasma peak, preliminary studies were able to estimate electron core tem-80 perature  $T_c$  (Moncuquet et al., 2020) and total temperature  $T_e$  (Maksimović, Bale, Berčič, 81 et al., 2020; Liu et al., 2021) by separately analyzing power levels below and above  $f_p$ , 82 respectively. 83

The primary task of this paper is to characterize the FIELDS QTN spectrum shape 84 given the unique instrument configuration by providing a single model valid both below 85 and above  $f_p$ . To accomplish this, in Section 2 we derive the ARF using the antenna and 86 (SC) current distribution calculated using the AWAS software (Dorđević et al., 2002). 87 Then, in Section 3 we calculate the theoretical model of the QTN spectrum and fit it 88 to observations from PSP Encounter 7 (E7) for periods where the antenna was unbiased. 89 The results show very good agreement with observations obtained by the SWEAP SPAN 90 instrument suite (Kasper et al., 2016; Whittlesey et al., 2020) and previous preliminary 91 QTN spectrum processing (Moncuquet et al., 2020). Finally, we discuss the future use 92 of this model, as well as potential shortcomings in Section 4. 93

### 94 2 Methods

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## 2.1 FIELDS instrument observations

On PSP, the RFS component of the FIELDS suite collects the electric field fluc-96 tuations up to 19.2 MHz (Pulupa et al., 2017). Within RFS, LFR and HFR cover fre-97 quency ranges of 10 kHz - 1.7 MHz and 1.3 - 19.2 MHz, respectively, both with 64 log-98 arithmically spaced frequencies, providing  $\sim 4.5\%$  resolution. The measurements of in-99 terest for this work are collected in dipole mode, where the difference of voltages at the 100 antenna terminals is processed using a Polyphase Filter Bank and Fast Fourier Trans-101 form algorithm. The spectra downloaded to ground at standard  $\sim 3.5s$  cadence are av-102 erages of several tens of sampled spectra, where the statistical uncertainty of the power 103 in each averaged spectrum is held below 0.3 dB (Pulupa et al., 2017). During specified 104 parts of each encounter, bias current is applied to the antennas in order to keep the an-105 tenna potential close to the potential of the undisturbed plasma. Applying the bias cur-106 rent maximizes the response of the low frequency voltage measurement to the electric 107 field signals of interest, while minimizing the response to plasma density fluctuations. 108 Unfortunately, the biased current produces an increased impact noise signal just below 109 the plasma frequency. As compensating for this bias-induced signal is beyond the intended 110 scope of this work, we will only focus on time periods where the FIELDS antennas were 111 not biased. This approach was enabled during PSP E7, as unbiased intervals appear daily 112 (Jan 15-22, 2021), lasting 2 times 4 minutes for each dipole. In this work, we focus on 113 V1-V2 dipole, that operated with no bias during 05:48 - 05:52 and 17:48 - 17:52 each day. 114 In lieu of applying an algorithm that filters out low-frequency non-QTN signal compo-115 nents, such as wave activity and instrument gain effects, from the spectrum (Martinović 116 et al., 2020), we use only the signal above 100 kHz, corresponding to approximately  $0.25 f_p$ , 117 avoiding the resistively coupled antenna regime (Bonnell et al., 2019). We derive the plasma 118 parameters from both the full resolution observations, and one minute median values, 119 with medians having a purpose of removing any short term signal pollution. Electron 120 VDF moments—core and halo density and temperature, are found via standard Levenberg-121 Marquardt least square fit of merged LFR/HFR data and theoretical spectra explained 122 below. Proton parameters are used as errorless initial input, and are provided by fitting 123 the SPAN-i measured proton VDFs (see, e.g. Verniero et al. (2020)). 124

### 2.2 Quasi-Thermal Noise Spectroscopy

The QTN is modelled for a proton-electron plasma, with the electron VDF consisting of two isotropic Maxwellians—a thermal core and suprathermal halo, and the proton VDF being a charge-neutralizing background isotropic Maxwellian. The synthetic QTN spectrum  $V^2(f)$  is calculated using contributions from electrons  $V_{\rm qtn}^2$ , protons  $V_{\rm pn}^2$ , impact (shot) noise  $V_{\rm sn}^2$  and galaxy radiation  $V_{\rm gal}^2$  as

$$V^{2} = \Gamma^{2} \left( V_{\rm qtn}^{2} + V_{\rm pn}^{2} + V_{\rm sn}^{2} + V_{\rm gal}^{2} \right) + V_{\rm lfr}^{2}.$$
 (1)

Here,  $\Gamma$  is the antenna gain and the instrument noise is estimated to be  $V_{lfr}^2 \approx 2.3 \cdot 10^{-17} V^2/Hz$  (Bale et al., 2016; Maksimović, Bale, Berčič, et al., 2020). Proton noise  $V_{pn}^2$ , important 132 133 below  $f_p$ , is estimated assuming the solar wind velocity  $\mathbf{v}_{sw}$  is perpendicular to the FIELDS 134 135 antenna, using the functional form given by Equation 22 from Issautier et al. (1999). We find proton contribution to be small compared to the impact noise at low frequencies close 136 to perihelion, in agreement with theoretical predictions (Meyer-Vernet et al., 2017), but 137 it still must be included for analysis close to  $f_p$ . Impact noise  $V_{sn}^2$  is calculated using Equa-138 tion 15 from Martinović et al. (2016), and is very small compared to  $V_{\rm qtn}^2$  near the peak. 139 The level of the galaxy radiation power  $V_{\rm gal}^2$  is calculated using the model given by Novaco 140 and Brown (1978), with same parameters used in the Encounter 1 (E1) study by Maksimović, 141 Bale, Berčič, et al. (2020). The galaxy and instrument noise signals are non-negligible 142 only at very high frequency end of the spectrum and are expected to have only a minor 143 contribution to the estimated values of halo temperature. For an isotropic Maxwellian, 144 the electron contribution is (Chateau & Meyer-Vernet, 1989) 145

$$V_{\rm qtn}^2(\omega) = \frac{16m_e\omega_p^2}{\pi\epsilon_0} \int_0^\infty \frac{B(k,\omega)F(k)}{k^2|\epsilon_L(k,\omega)|^2} dk.$$
 (2)

Plasma VDF functions  $B(k, \omega)$  and  $\epsilon_L(k, \omega)$  describe total amount of energy of the plasma and its response to fluctuations, respectively. These two functions are determined by plasma properties only, are not affected by the instrumentation and are explained in detail elsewhere (Meyer-Vernet & Perche, 1989; Martinović, 2016). The ARF  $F(\mathbf{k})$  is given as a Fourier transform of the antenna current  $\mathbf{j}_{\mathbf{a}}(\mathbf{k})$  along the dipole, normalized to a value at the antenna terminals  $I_a$ , and integrated over the entire solid angle  $\Omega$  for a given value of wavevector  $\mathbf{k}$ 

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$$F(k) = \frac{1}{32\pi} \int \frac{|\mathbf{k} \cdot \mathbf{j}_{\mathbf{a}}(\mathbf{k})|^2}{I_a^2} d\Omega$$
(3)

From Equation 3 it is clear that the structure of the antenna current distribution  $\mathbf{j}_{\mathbf{a}}(\mathbf{r})$ significantly impacts the determination of the ARF.

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# 2.3 Determination of current distribution via AWAS software

In order to characterize the antenna current distribution, we use the AWAS software package (Đorđević et al., 2002). AWAS is a versatile program for analyzing wire antennas and scatterers assembled from arbitrarily located and interconnected straightline segments. Wire antennas can be modeled in free space, as done below, or located above a perfectly conducting plane, and can be analyzed in transmitting or receiving modes to calculate port matrix parameters, current distribution, near fields, and far fields.

The top panel of Figure 1 shows the 2D AWAS model of *PSP*. The SC body (shaded 164 in grey) is approximated by a simple set of four orthogonal conductive wires, marked as 165 segments 1-4 (blue numbers), extending between the node (reference point in the coor-166 dinate system marked by a red number) 1 and 2-5, respectively. The two dipoles are mod-167 eled as pairs of segments (5,7) and (6,8). Ports (antenna terminals) are marked by green 168 dots and modelled as ideal current generators. Dimensions of segments reflect the FIELDS 169 configuration, with wire segments 1-4 that replace the SC body being 1.49 m long, and 170 antenna segments 5-8 2 m long (Bale et al., 2016). We assign the x axis to a line of a 171



Figure 1. Top: PSP model in AWAS, with nodes (red), ports (green), and segments (blue) indicated (with labels for segment 1 and port 1 overlapped on each other). The SC body, which the model replaces with wires, is shaded in grey. Middle: AWAS solution for the current distribution between nodes 6 and 8 from the top panel (black), compared to models with the current flowing through the SC body having maximum (pink) (Meyer-Vernet & Perche, 1989) or zero value (grey). The current drops by a factor of  $\zeta \approx 1/3$  compared to the values at antenna terminals. Bottom: Antenna response function calculated for various antenna configurations described in the text. The color coding for the unlabeled lines is the same as on the middle panel.

linear dipole extending between nodes 6 (x = 3.49 m) and 8 (x = -3.49 m), where the 172 point of origin is at the center of the SC 2D quadratic geometry. 173

Once the antenna geometry is set, AWAS calculates currents and fields in and around 174 antennas by solving a two-potential equation (see, e.g. (Dorđević et al., 1979; Popović 175 et al., 1982)). This equation is numerically solved using the method of moments (Harrington, 176 1993) with the current distribution approximated by a polynomial (Dorđević et al., 1991). 177 This way, we provide values of the antenna current at any point within segments 1-8. 178 Details of the procedure are given in Chapter 6 of (Đorđević et al., 2002). 179

We model the system as a transmitting antenna in a vacuum, which corresponds 180 to a receiving antenna in a medium via reciprocity theorem (see, e.g. (Schelkunoff & Friis, 181 1952; Balanis, 1997)). The current at ports 1 and 2 is set to an arbitrary value of  $I_a =$ 182 1A, while currents at the opposite sides of the SC body for each dipole—ports 3 and 4, 183 respectively—are set to  $-I_a$ . Middle panel shows one-dimensional cut through the AWAS 184 solution along x axis with normalized values of the current. The normalized current  $j_x/I_a$ 185 is found to be lower in intensity within segments 1 and 3, with a minimum value at 1-186  $\zeta \approx 2/3$  of maximum at ports 1 and 3. Therefore, the resulting profile suggests a lin-187 ear decay inside the SC body, with a minimum being different for a factor  $\zeta$  compared 188 to the one at the terminals. The numerical value  $\zeta \sim 0.33$  is justified a posteriori in 189 application to FIELDS data. This is notably lower than the prediction of maximum cur-190 rent throughout the SC body (Meyer-Vernet & Perche, 1989), given by pink dashed line. 191 This current distribution will be used to calculate the antenna response, and then QTN 192 spectrum. 193

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# **3** Results and Discussion

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#### 3.1 Antenna response function for FIELDS

Assuming a current in the x direction, the Fourier transform of the current distri-196 bution calculated by AWAS is given as 197

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$$j_x(k_x) = \frac{2\left(\zeta(\cos(k_xd) - 1) + k_xd\sin(k_xd)\right)}{k_x^2d} - \frac{2(k_xL_{ant}\sin(k_xd) + \cos(k_x(d + L_{ant})) - \cos(k_xd))}{k_x^2L_{ant}}$$
(4)

This expression can be directly inserted in Equation 3. While analytical integration of 200 this expression is not possible, a numerical solution is given as a black line on the *bot*-201 tom panel of Figure 1. The obtained function has similarities with both linear and spher-202 ical dipole solutions, with the two peaks corresponding to the peaks of these two func-203 tions. Namely, for very large wavelengths (small k) the antenna samples waves that span 204 across the entire SC. In this regime, the response is dominated by the current close to 205 and across the SC body, having the dominant signal for the case of maximum current through the SC body (magenta), while AWAS solution has a lower response due to non-207 zero value of parameter  $\zeta$ . For smaller wavelengths (larger k), the antenna arms increas-208 ingly sample uncorrelated signals. Here, the response of a hypothetical configuration with 209 zero SC current (grey) starts behaving like a dipole of infinitely small spheres at distance  $2L_{ant}$  (orange), while the AWAS solution shows a slight increase in signal due to this ef-211 fect before settling to a linear decrease characteristic for a linear dipole with no gap (blue). 212

We interpret this result as a consequence of the ratio  $L_{ant}/d \sim 1$ . If the antenna 213 arms are long compared to the gap  $(L_{ant}/d \gg 1)$ , then the gap can be neglected, re-214 ducing the problem to the one encountered by multiple previous missions. Another asymp-215 totic behavior is for the case  $L_{ant}/d \ll 1$ , where it reduces to a theoretical double sphere 216 dipole configuration. However, as neither of these approximate results was valid for PSP 217 configuration, numerical evaluation of ARF is necessary. 218

# 3.2 Plasma parameters from QTN spectroscopy

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In this Section, we apply the new antenna response model, detailed in Section 2.3, 220 to QTN spectra from PSP E7 to extract electron VDF parameters. The left panels of 221 Figure 2 show examples of fits to 1-minute median values of RFS data sampled with un-222 biased V1-V2 dipole. Due to the very large number of sampled spectra during each of 223 the 1-minute intervals, every panel shown represents a median of 14-17 downloaded spec-224 tra. Each spectrum downloaded from the spacecraft is an average of 40-80 on-board sam-225 ples. Therefore, an instrument performs a total of 680-1360 observations per minute, and 226 estimated uncertainty of the 1-minute averaged spectrum data points is 0.05-0.08 dB. 227 The fitted part of the spectrum, shown as green dots, is essentially comprised of only QTN, 228 instrument noise and galaxy radiation contributions, which allows for an accurate de-229 termination of electron VDF parameters with very small uncertainties. For each of 64 230 1-minute spectra (sampled for 8 days during 8 minutes per day when no antenna bias-231 ing was applied; see Section 2.1), we use multiple sets of initial guesses for electron pa-232 rameters  $n_e$ ,  $T_c$ ,  $n_h/n_c$  and  $T_h/T_c$  to find absolute  $\chi^2$  minimum, and also visually inspect 233 the fits. Then, the results from these 1-minute fits are used as an initial guess for fitting 234 the spectra in full resolution. 235

On right panels, we compare the best fit QTN model that uses the current distri-236 bution calculated in Section 2.3 with previously applied models. As already noted above, 237 neglecting the gap between the antenna arms (blue) does not reproduce the measured 238 spectrum neither close to  $f_p$  nor at high frequencies. Two asymptotic SC body current 239 models also do not produce accurate representations of the observed spectrum—if max-240 imum uniform current is assumed (magenta), the signal is notably overestimated in the 241 vicinity of  $f_p$ , while setting the SC current to zero in the gap region both underestimates 242 the signal around the resonance and shows a 'sphere dipole-like' behavior at high fre-243 quencies, where fluctuations of larger wavelength dominantly contribute to the spectrum 244 (Meyer-Vernet, 1979). The different shape of the illustrated curves compared to the ob-245 served spectra makes any fitting procedure unfeasible, and we were not able to obtain 246 satisfying overall agreement with observations, or sensible values of VDF moments with 247 any of the previously applied current distribution models. Variation of the parameter 248  $\zeta$  by more than  $\sim 2-3\%$  also disables the model from meaningfully converging to the 249 data, regardless of the plasma parameters used. 250

Figure 3 illustrates median values of fitted  $n_e$  and  $T_c$  for sets of four 1-minute un-251 biased intervals, plotted as black dots. We find agreement within 20% between total elec-252 tron density and proton density provided by SPAN-I fits. We do not compare our results 253 with electron density provided by SPAN-E, as it is already calibrated to  $f_p$  values ob-254 tained from the QTN plasma peak. This discrepancy is not surprising as, even though 255  $n_e$  is related to plasma peak frequency and is therefore the most reliable parameter in 256 the QTN analysis, SPAN-I has a large fraction of the proton VDF moving in and out 257 of the instrument field of view due to both instrument orientation with respect to the 258 sunward direction (see Kasper et al. (2016); Woodham et al. (2021) for details of SPAN-259 I setup) and plasma flow following magnetic field reversals or 'switchbacks', which oc-260 cur at timescales from seconds to tens of minutes (see e.g. Dudok de Wit et al. (2020); 261 Martinović et al. (2021)). The brown line shows the values of the  $n_e$  obtained using the 262 263 method introduced in Moncuquet et al. (2020) (further on referred to as M20). The M20 method relies on combination of plasma peak tracing based on the steepest slope in the 264 QTN signal (Moncuquet et al., 2005; Kasaba et al., 2020) and fitting limited parts of the 265 spectrum below  $f_p$  using the antenna response function given at Meyer-Vernet and Perche 266 (1989) (violet lines at *middle* and *bottom* panels of Figure 1). Density values between 267 the two data sets obtained from QTN observations are similar to the level of M20  $n_e$  un-268 certainties (orange error bars), that are of the order of  $\sim 9\%$  due to the instrument res-269 olution. A small systematic discrepancy is notable, probably due to dependency of the 270 plasma peak location in the frequency space from  $L_{ant}/L_D$  ratio; see Figure 2 in (Meyer-271



Figure 2. Three examples of the QTN spectrum fit. Left: Example of the QTN model fits to 1-minute median values of LFR V1-V2 dipole data with obtained electron parameter values and uncertainties, with  $L_{ant}/L_D \approx [1.25, 1.37, 1.38]$  from top to bottom, respectively. Right: Comparison of the QTN model assuming current distribution calculated via AWAS (same parameters as on the left panels) with other theoretical models illustrated in Figure 1, using the same color coding. Note that the double sphere dipole spectrum is an order of magnitude above the data level and is not shown.



Figure 3. Overview of 1-minute median RFS observations fit, comparing proton (SPAN-I, blue) and electron densities from QTN spectroscopy using M20 algorithm (brown) and our model (black) on top panel; and electron core temperatures from SPAN-e (green) with both QTN data sets on bottom panel. Parameter uncertainties for black dots are of the order of the symbol size. The values of  $T_c$  from SPAN-E and our method do not differ for more than 10% for higher, and no more than 25% for lower temperatures. The missing interval in the afternoon of January 18 had a clearly resolved plasma peak, but also a significantly increased non-QTN signal below  $f_p$ , and confident estimation of  $T_c$  was not possible.

Vernet & Perche, 1989) for more details. These small corrections will be discussed in length
in the future when a more robust data sets become available from both later Encounters and biased intervals.

Values of  $T_c$  are in overall agreement with SPAN-E results, with discrepancies within 275 10% closer to the PSP E7 closest approach, increasing to  $\sim 25\%$  outbound. The differ-276 ence between the two sets of results is reasonably small and we consider that its vari-277 ation may be due to the change in contribution of the electron noise to the overall QTN 278 spectrum. First, as electron temperature increases, the error in  $V_{pn}^2$  estimate due to the 279 antenna orientation (Issautier et al., 1999) becomes less significant. Second, the impor-280 tance of the impact noise decreases below  $f_p$  as  $T_c$  increases and the  $L_{ant}/L_D$  ratio in-281 crease. The increase in discrepancy matches with the decrease of  $L_{ant}/L_D$  from ~ 1.4– 282 1.5 to  $\sim 1$  during the last three days of the observed interval. Also, precision of the SPAN-283 E parameters is increased with the VDF moments due to increased signal-to-noise ra-284 tio. Our results show a very good agreement in terms of general trend with  $T_c$  values pro-285 vided by M20, and fall within the range of large variations. As already noted for den-286 sity, a thorough discussion on the differences between the different techniques will re-287 quire future analysis of unbiased intervals and is not within the scope of this paper. 288

Figure 4 shows the fitted values obtained from full resolution measurements, which 289 do not notably deviate from initial 1-minute fits. Standard deviations are less than 3%290 for  $n_e$  (approximately half of the instrument resolution) and less than 15% for  $T_c$ . These 291 results demonstrate the potential for the usage of full resolution *PSP* QTN measurements 292 to accurately extract electron VDF parameters in the near-Sun environment, as well as 293 for advanced data products, such as level of the density fluctuations at sub-ion scales. 294 For unbiased intervals, M20 values of  $T_c$  are not provided, while values of  $n_e$  are not shown 295 due to very large uncertainties, which make direct comparison inconvenient. 296

#### <sup>297</sup> 4 Conclusions

QTN spectroscopy is a powerful in situ tool to accurately yield electron plasma pa-298 rameters from levels of electric field fluctuations measured by an antenna in a plasma. 299 The unique configuration of the PSP/FIELDS antennas caused previously applied an-300 tenna response models to either under- or overestimate the theoretical predictions around 301 electron plasma frequency, and therefore made fitting of the full frequency range of QTN 302 spectra unfeasible. In this article, we propose a new model of for the antenna response that using a SC current distribution calculated via simplified *PSP* geometry scheme in 304 AWAS software. Fitting of the generic QTN model to observations provides accurate val-305 ues of electron VDF parameters, with very low uncertainties and small spreads over minutes-306 long time intervals. 307

Here, we must note that a more realistic description of the suprathermal electron VDF as measured by PSP would include a significant strahl population, (Halekas et al., 2020). A detailed description of how strahl electrons affect QTN spectra is an open question and is a matter of future research. Therefore, even though our examples are in agreement with recently measured strahl temperatures being ~ 100 eV (Berčič et al., 2020), initial scarce calculations show that the peak width, and therefore  $n_h$ , might be primarily affected by the strahl, and the results for suprathermal parameters from this model should be handled with care.

The results shown here are intended to enable future studies, primarily by expanding this model to account for biased antenna signals, providing a full survey of VDF moments throughout multiple *PSP* encounters. In the theoretical realm, the primary remaining open question is the effect of the strahl population, which is expected to be largely increased as we approach the Sun (Maksimović, Zouganelis, et al., 2005; Štverak et al., 2009; Berčič et al., 2020), on the QTN spectrum. The effects of strahl are expected to



Figure 4. Comparison of SPAN parameters (same spatial and color scheme as on Figure 3) for three example intervals from E7 not represented on Figure 2. The full resolution fits are shown with error bars. The spread of  $T_c$  values obtained by QTN spectroscopy is lower than 20% for all 1-minute intervals.

be important around  $f_p$ . As mentioned above, visibility of the plasma peak, and there-

fore the strahl signal, depends on the  $L_{ant}/L_D$  ratio, which is steadily increasing as we

approach the Sun (Maksimović, Issautier, et al., 2005) and has surpassed unity during

the closest approach of PSP in E7. As future encounters in 2023 and 2024 are expected

to make *PSP* the first non-spinning SC with  $L_{ant}/L_D \gg 1$ , there is a potential for plasma

resonance peak to be sufficiently well resolved for small differences between halo and strahl

signals to be tested by observations.

## 329 Acronyms

- **PSP** Parker Solar Probe
- 331 **QTN** Quasi-Thermal Noise
- <sup>332</sup> **VDF** Velocity Distribution Function
- 333 STEREO Solar TErrestial REsearch Observatory
- AWAS Analysis of Wire Antennas and Scatterers
- 335 **SWEAP** Solar Wind Electrons, Protons & Alphas
- 336 **SPAN-I(E)** Solar Probe ANalyzer for Ions (Electrons)
- <sup>337</sup> **RFS** Radio Frequency Spectrometer
- <sup>338</sup> **LFR** Low Frequency Receiver
- 339 **HFR** High Frequency Receiver
- 340 **SPDF** Space Physics Data Facility

## 341 Acknowledgments

We thank Michel Moncuquet for enlightening discussions on the LFR data processing. 342 Parker Solar Probe was designed, built, and is now operated by the Johns Hopkins Ap-343 plied Physics Laboratory as part of NASA's Living with a Star (LWS) program (con-344 tract NNN06AA01C). Support from the LWS management and technical team has played 345 a critical role in the success of the Parker Solar Probe mission. The authors acknowl-346 edge CNES (Centre National d Etudes Spatiales), CNRS (Centre National de la Recherche 347 Scientifique), the Observatoire de PARIS, NASA and the FIELDS/RFS team for their support to the PSP/SQTN data production, and the CDPP (Centre de Donnees de la 349 Physique des Plasmas) for their archiving and provision. The FIELDS experiment was 350 developed and is operated under NASA contract NNN06AA01C. The SWEAP Inves-351 tigation and this publication are supported by the PSP mission under NASA contract 352 NNN06AA01C. M. M. Martinović and K. G. Klein were financially supported by NASA 353 grant 80NSSC19K0521. PSP FIELDS LFR/HFR data is available at http://sprg.ssl 354 .berkeley.edu/data/psp/data/sci/fields/12/rfs\_lfr/ and http://sprg.ssl.berkeley 355 .edu/data/psp/data/sci/fields/12/rfs\_hfr/. PSP SWEAP SPAN-I/SPAN-E data 356 can be found at http://sweap.cfa.harvard.edu/pub/data/sci/sweap/spi/L3/ and 357 http://sweap.cfa.harvard.edu/pub/data/sci/sweap/spe/L3/. The M20 data set 358 is accessible at French national data centre for natural plasmas of the solar system http:// 359 www.cdpp.eu/ under Missions@Archive / PARKER SOLAR PROBE MISSION / PARKER 360 SOLAR PROBE FIELDS Experiment / PARKER SOLAR PROBE FIELDS - Simplified Quasi-Thermal 361

<sup>362</sup> Noise (SQTN) Spectroscopy.

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Figure 1.







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Figure 2\_1.



Figure 2\_2.



Figure 2\_3.



Figure 3.



Figure 4.

