# Sensitivity of a Coarse-Resolution Global Ocean Model to Spatially Variable Neutral Diffusion

Ryan M Holmes<sup>1</sup>, Sjoerd Groeskamp<sup>2</sup>, Kial Douglas Stewart<sup>3</sup>, and Trevor John McDougall<sup>4</sup>

<sup>1</sup>University of Sydney <sup>2</sup>Royal Netherlands Institute for Sea Research <sup>3</sup>Australian National University <sup>4</sup>The School of Mathematics and Statistics, University of New South Wales

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#### Abstract

Motivated by recent advances in mapping mesoscale eddy tracer mixing in the ocean we evaluate the sensitivity of a coarseresolution global ocean model to a spatially variable neutral diffusion coefficient  $\lambda = 1$ , we gradually introduce physically-motivated models for the horizontal (mixing length theory) and vertical (surface mode theory) structure of  $\lambda = 1$ n along with suppression of mixing by mean flows. Each structural feature influences the ocean's hydrography and circulation to varying extents, with the suppression of mixing by mean flows being the most important factor and the vertical structure being relatively unimportant. When utilizing the full theory (experiment "FULL') the interhemispheric overturning cell is strengthened by \$2\$ Sv at \$26^\circ\$N (a  $\lambda = 0$ , sim20\% increase), bringing it into better agreement with observations. Zonal mean tracer biases are also reduced in FULL. Neutral diffusion impacts circulation through surface temperature-induced changes in surface buoyancy fluxes and non-linear equation of state effects. Surface buoyancy forcing anomalies are largest in the Southern Ocean where decreased neutral diffusion in FULL leads to surface cooling and enhanced dense-to-light surface watermass transformation, reinforced by reductions in cabbeling and thermobaricity. The increased watermass transformation leads to enhanced mid-latitude stratification and interhemispheric overturning. The spatial structure for  $\lambda = 0$  in FULL is important as it enhances the interhemispheric cell without degrading the Antarctic bottom water cell, unlike a spatially-uniform reduction in  $\lambda = 0$ . These results highlight the sensitivity of modeled circulation to  $\lambda = 0$  and motivate the use of physics-based models for its structure.

# Sensitivity of a Coarse-Resolution Global Ocean Model to Spatially Variable Neutral Diffusion

R. M. Holmes<sup>1,2,3,4</sup>, S. Groeskamp<sup>5</sup>, K.D. Stewart<sup>3,6</sup> and T.J. McDougall<sup>4</sup>

<sup>1</sup>School of Geosciences, University of Sydney, Sydney, Australia
 <sup>2</sup>Climate Change Research Centre, University of New South Wales, Sydney, Australia
 <sup>3</sup>Australian Research Council Centre of Excellence for Climate Extremes, Australia
 <sup>4</sup>School of Mathematics and Statistics, University of New South Wales, Sydney, Australia
 <sup>5</sup>NIOZ Royal Netherlands Institute for Sea Research, Texel, The Netherlands
 <sup>6</sup>Research School of Earth Sciences, Australian National University, Canberra, Australia

# Key Points:

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11	•	A new spatially-variable parameterization for mesoscale neutral diffusion is tested
12		in a 1-degree ocean model
13	•	Both hydrography and circulation are sensitive to the magnitude and spatial struc-
14		ture of neutral diffusion
15	•	A 2Sv enhancement in interhemispheric overturning stems from suppression of neu-
16		tral diffusion by mean flows

Corresponding author: Ryan Holmes, r.holmes@sydney.edu.au

## 17 Abstract

Motivated by recent advances in mapping mesoscale eddy tracer mixing in the ocean we 18 evaluate the sensitivity of a coarse-resolution global ocean model to a spatially variable 19 neutral diffusion coefficient  $\kappa_n(x, y, z)$ . We gradually introduce physically-motivated mod-20 els for the horizontal (mixing length theory) and vertical (surface mode theory) struc-21 ture of  $\kappa_n$  along with suppression of mixing by mean flows. Each structural feature in-22 fluences the ocean's hydrography and circulation to varying extents, with the suppres-23 sion of mixing by mean flows being the most important factor and the vertical structure 24 being relatively unimportant. When utilizing the full theory (experiment "FULL") the 25 interhemispheric overturning cell is strengthened by 2 Sv at 26°N (a  $\sim 20\%$  increase), 26 bringing it into better agreement with observations. Zonal mean tracer biases are also 27 reduced in FULL. Neutral diffusion impacts circulation through surface temperature-28 induced changes in surface buoyancy fluxes and non-linear equation of state effects. Sur-29 face buoyancy forcing anomalies are largest in the Southern Ocean where decreased neu-30 tral diffusion in FULL leads to surface cooling and enhanced dense-to-light surface wa-31 termass transformation, reinforced by reductions in cabbeling and thermobaricity. The 32 increased watermass transformation leads to enhanced mid-latitude stratification and 33 interhemispheric overturning. The spatial structure for  $\kappa_n$  in FULL is important as it 34 enhances the interhemispheric cell without degrading the Antarctic bottom water cell, 35 unlike a spatially-uniform reduction in  $\kappa_n$ . These results highlight the sensitivity of mod-36 eled circulation to  $\kappa_n$  and motivate the use of physics-based models for its structure. 37

## Plain Language Summary:

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The diffusion of tracers such as temperature and salinity along surfaces of constant 39 40 density by the action of mesoscale eddy stirring, known as neutral diffusion, is an important transport process in the ocean which impacts heat, carbon and nutrient bud-41 gets as well as climate variability. However, most global ocean circulation models used 42 for climate studies have a horizontal grid resolution that is too coarse to resolve mesoscale 43 eddies. Thus, the effects of eddy-driven neutral diffusion must be parameterized through 44 the inclusion of a neutral diffusivity parameter  $\kappa_n$ . While the strength of neutral diffu-45 sion is known to vary spatially within the ocean, most models still make simple choices 46 for  $\kappa_n$ ; a constant, or scaled according to the grid resolution. In this study, we exam-47 ine the sensitivity of a coarse-resolution global ocean model to the spatial structure of 48  $\kappa_n$  using a recently developed and physically-motivated three-dimensional mapping of 49 mesoscale mixing. Our results show that the modeled meridional overturning circula-50 tion and tracer structure are sensitive to both the magnitude and the spatial structure 51 of  $\kappa_n$ , suggesting that more attention should be paid to this parameter in future model 52 development. 53

## 54 1 Introduction

The diffusion of tracers along neutral density surfaces through the action of mesoscale 55 eddy stirring, or "neutral diffusion", is an important transport process in the ocean that 56 influences the heat, salt, carbon and nutrient budgets, ocean ventilation, deep and bot-57 tom water formation and climate variability (e.g. Busecke & Abernathey, 2019; England 58 & Rahmstorf, 1999; Gnanadesikan et al., 2015; Griffies et al., 2015; Jones & Abernathey, 59 2019, 2021; Morrison et al., 2013; Sijp et al., 2006; Sijp & England, 2009; Williams et 60 al., 2007; Wolfe et al., 2008). Mesoscale eddies are poorly represented in the global coarse-61 resolution models used for many climate studies and thus the associated neutral diffu-62 sion must be parameterized through the inclusion of an explicit neutral diffusivity,  $\kappa_n$ . 63 Despite significant advances in theory, the spatial and temporal structure of  $\kappa_n$  is poorly 64 understood and many models still make simple choices for  $\kappa_n$  based on ad-hoc, rather 65 than physical, reasoning (e.g. see Table 1 of Meijers (2014) for a summary of neutral physics 66 choices in CMIP5 models). The choice of  $\kappa_n$  has implications for the model represen-67

tation of a large range of processes of climatic relevance (e.g. Ferreira et al., 2005; Gnanadesikan et al., 2017; Pradal & Gnanadesikan, 2014) and is likely to remain a first-order issue for some time given that higher resolution, eddy-resolving coupled models are still
impractical for many applications. In this study, we take advantage of recent advancements in the mapping of mesoscale mixing in the ocean based on theory and observations (Groeskamp et al., 2020) to revisit this issue using a coarse-resolution global ocean
model.

Since the step-change improvement in non eddy-resolving ocean models associated 75 with the work of Gent and McWilliams (1990) (hereafter GM) and the movement away 76 from simple horizontal diffusive closures (due to the detrimental "Veronis effect", Gough 77 & Lin, 1995; McDougall & Church, 1986; Veronis, 1975) toward rotated along-isopycnal 78 or neutral diffusion (Griffies et al., 1998; McDougall et al., 2014; Redi, 1982; Solomon, 79 1971), how to choose the GM coefficient,  $\kappa_{GM}$ , and the neutral tracer diffusivity,  $\kappa_n$ , has 80 become an important topic of research. A range of theories have been developed, most 81 of which focus primarily on the adiabatic eddy-driven circulation represented by  $\kappa_{GM}$ 82 (e.g. Cessi, 2008; Eden & Greatbatch, 2008; Eden et al., 2009; Jansen et al., 2019, 2015; 83 Jansen & Held, 2014; Marshall & Adcroft, 2010; Pearson et al., 2017; Smith & Vallis, 84 2002; Treguier et al., 1997; Visbeck et al., 1997). Some of these schemes are based on 85 energy conservation and consider the effects of mesoscale eddies in the momentum bud-86 get (e.g. Eden & Greatbatch, 2008; Jansen et al., 2019; Jansen & Held, 2014; Juricke et 87 al., 2020). However, the independent choice of the neutral diffusivity  $\kappa_n$  has received less 88 attention. While some models make the choice  $\kappa_n = \kappa_{GM}$ , theory and diagnostics from 89 high-resolution models and field experiments suggests that the two may be quite differ-90 ent (e.g. Abernathey et al., 2013, 2010; Smith & Marshall, 2009; Vollmer & Eden, 2013). 91 Experience with model tuning suggests that the choice  $\kappa_n = \kappa_{GM}$  can be problematic 92 and thus many models that use sophisticated flow-dependent schemes for  $\kappa_{GM}$  retain 93 simple ad-hoc choices (often constant, or scaled according to the grid spacing) for  $\kappa_n$  not 94 necessarily based on physical reasoning (e.g. Gnanadesikan et al., 2006; Griffies et al., 95 2004; Johns et al., 2006; Jungclaus et al., 2010; Voldoire et al., 2013). 96

Documentation of the independent sensitivity of coarse-resolution climate simu-97 lations to  $\kappa_n$  remains limited, despite the model tuning performed behind the scenes at 98 modeling centers. While  $\kappa_{GM}$  is known to have strong impacts on the ocean's overturn-99 ing circulation and the Antarctic Circumpolar Current (ACC) strength,  $\kappa_n$  may be just 100 as important as  $\kappa_{GM}$  for determining thermocline stratification and abyssal tracer dis-101 tributions (e.g. Danabasoglu & McWilliams, 1995). Danabasoglu and Marshall (2007) 102 showed improvements in upper-ocean temperature biases and heat transport in their coarse-103 resolution simulations when the vertical structure of  $\kappa_{GM}$  was surface-intensified. Intro-104 ducing a similar vertical structure in  $\kappa_n$  showed small additional improvements. Cou-105 pled model studies show that large (~ 600%) changes in a spatially-uniform  $\kappa_n$  can have 106 significant impacts on high-latitude processes, where along-isopycnal temperature and 107 salinity gradients are typically largest, including sea-ice formation, surface fluxes, strat-108 ification and deep convection (Pradal & Gnanadesikan, 2014; Sijp et al., 2006; Sijp & 109 England, 2009).  $\kappa_n$  is also thought to influence tropical climate variability (Gnanade-110 sikan et al., 2017). We also note recent studies recommending that anisotropic effects, 111 that are not addressed here, should be taken into account (Bachman et al., 2020; Stan-112 ley et al., 2020). 113

In this article we isolate the sensitivity of a coarse-resolution ocean model to  $\kappa_n$ , independently of  $\kappa_{GM}$ , using the theory- and observation-based three-dimensional maps of  $\kappa_n$  recently constructed by Groeskamp et al. (2020). As a sensitivity test, we consider only static maps of  $\kappa_n$ , leaving the development of a dynamic parameterization better suited to production use for future studies. We separate the impacts of the various structural ingredients included in Groeskamp et al. (2020)'s  $\kappa_n$ ; the mixing length theory that governs the horizontal structure, the surface mode theory that governs the vertical struc-



Figure 1. (a) The structure of  $\kappa_n$  in the ACCESS-OM2 control simulation (CTRL) indicating the impact of the grid-scaling factor [Eq. (4)]. (b) The two-dimensional time-averaged spatial structure of  $\kappa_{GM}$  from CTRL determined according to the "baroclinic zone" dynamical setting of Griffies (2012); Griffies et al. (2005) and a maximum (minimum) of 600 m<sup>2</sup> s<sup>-1</sup> (50 m<sup>2</sup> s<sup>-1</sup>) used for all experiments.

ture (LaCasce, 2017) and the suppression of mixing by mean flows (Ferrari & Nikurashin, 121 2010). The use of an ocean-only model, rather than a coupled climate model, allows a 122 clean attribution of cause and effect, avoiding runaway air-sea feedbacks. In such a sys-123 tem where the wind-forcing is fixed, the impact of variations in  $\kappa_n$  on the interior buoy-124 ancy structure and thus circulation should only arise through changes in surface heat 125 and buoyancy fluxes (e.g. Guilyardi et al., 2001; Hieronymus & Nycander, 2013) or non-126 linear equation of state effects such as cabbeling and thermobaricity (Klocker & McDougall, 127 2010; McDougall, 1987). Our model and experimental design, along with a brief sum-128 mary of the  $\kappa_n$  theory of Groeskamp et al. (2020), is presented in Section 2.1. Section 129 3 presents an analysis of the sensitivity of the meridional overturning circulation (MOC) 130 and tracer distributions to  $\kappa_n$ , along with a discussion of the associated mechanisms. Sec-131 tion 4 summarizes our results and discusses drawbacks and next steps. 132

## 133 2 Methods

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## 2.1 The global ocean sea-ice model

We use the coarse 1° horizontal resolution configuration of the global ocean sea-135 ice model ACCESS-OM2 (Kiss et al., 2020), which couples together the Modular Ocean 136 Model version 5.1 (MOM5, Griffies, 2012) and the Los Alamos Sea Ice Model version 5.1.2 137 (CICE, Hunke et al., 2015). Forcing is taken from the JRA55-do reanalysis (Tsujino et 138 al., 2018) and consists of a repeating cycle of the period May 1990 to April 1991 (Stew-139 art et al., 2019). Simulations are compared after 1000 years of spin-up from World Ocean 140 Atlas 2013 (WOA13, Locarnini et al., 2013; Zweng et al., 2013) initial conditions. More 141 information on ACCESS-OM2 including details on numerical algorithms, parameteri-142 zations and parameter choices is contained elsewhere (e.g. Holmes et al., 2021; Kiss et 143 al., 2020; Stewart et al., 2017). 144

In ACCESS-OM2 the GM eddy transport parameterization is implemented via skewdiffusion (Griffies, 1998). The  $\kappa_{GM}$  structure, not altered in this study, is uniform in the vertical and dynamically dependent on the horizontal buoyancy gradient averaged over the top 2000 m according to the "baroclinic zone" setting (see Griffies, 2012; Griffies et al., 2005, Fig. 1b) with a maximum (minimum) of 600 m<sup>2</sup> s<sup>-1</sup> (50 m<sup>2</sup> s<sup>-1</sup>).

In the default version of ACCESS-OM2 the neutral diffusivity  $\kappa_n$  is constant at 600 m<sup>2</sup> s<sup>-1</sup>. 150 This is altered for our experiments (see Section 2.3). To avoid unphysically large tracer 151 fluxes the diffusive flux tapering method of Danabasoglu and McWilliams (1995) is used 152 such that the fluxes are tapered where the neutral slope is large. This method avoids the 153 potential for large spurious diapycnal fluxes that comes with alternative slope clipping 154 methods. In ACCESS-OM2 the neutral diffusion operator is reduced to horizontal dif-155 fusion in the top surface layer (of thickness  $\sim 2m$ ) and bottom topography grid cells (Fer-156 rari et al., 2008), meaning that the neutral diffusion parameterization can directly drive 157 some diapycnal flux there, along with interactions with surface boundary layer turbu-158 lence and surface fluxes (de Lavergne, Groeskamp, Zika, & Johnson, 2022). We also note 159 that model implementations of rotated neutral diffusion are affected by various numer-160 ical discretization errors that can create spurious diapycnal fluxes that are non-trivial 161 to quantify and are treated elsewhere (e.g. Beckers et al., 1998, 2000; Griffies et al., 1998; 162 Groeskamp et al., 2019; Lemarié et al., 2012; Shao et al., 2020; Urakawa et al., 2020). 163

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# 2.2 A physics-based theory for the spatial structure of the neutral diffusivity

We follow Groeskamp et al. (2020) by building up physically-motivated three-dimensional maps of  $\kappa_n$  based on the following elements.

## <sup>168</sup> Two-dimensional mixing length theory (MLT)

Mixing-length theory (Prandtl, 1925) provides a two-dimensional structure for surface eddy-driven horizontal diffusion,

$$\kappa_{MLT}(x,y) = \Gamma u_{rms} L_{mix}, \tag{1}$$

where  $\Gamma$  is a mixing efficiency (here taken as 0.35, Klocker & Abernathey, 2013),  $u_{rms}$ is an RMS geostrophic velocity taken from altimetry observations and  $L_{mix}$  is a mixing length taken here as the deformation radius,  $L_d$ , associated with the first "surface mode" (LaCasce, 2017; LaCasce & Groeskamp, 2020), including an equatorial adjustment following Hallberg (2013).

## 177 Surface mode theory

A three-dimensional map can be obtained by assuming that  $u_{rms}$  follows the vertical structure of the first surface mode (LaCasce, 2017),

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$$u_{rms}(x, y, z) = \phi(x, y, z) \sqrt{2EKE_0(x, y)}, \qquad (2)$$

(3)

where  $\phi(x, y, z)$  is obtained by solving the Sturm-Liouville problem dependent on the stratification profile at each horizontal location assuming that the horizontal velocity is zero at the bottom.

## 184 Mixing suppression by mean flows

We also include a factor that accounts for the suppression of neutral diffusion by mean flows following the theory of Ferrari and Nikurashin (2010). This factor has the form,

 $S(x, y, z) = \frac{1}{1 + k^2 \gamma^{-2} (c_w - U)^2},$ 

where  $\gamma$  is an eddy time-scale (here a tunable parameter set to  $\gamma^{-1} = 1.68$  days following Groeskamp et al. (2020)'s fit to NATRE and DIMES data), k is the zonal eddy wavenumber,  $c_w$  is an eddy drift speed and U is the mean velocity. k and  $c_w$  are determined according to surface mode theory, while U here comes from the thermal wind relation applied to climatological ocean observations (note that a reference level velocity is not needed, Groeskamp et al., 2020).

Experiment	Description	Volume-mean $\kappa_n \ (m^2 \ s^{-1})$	Surface-mean $\kappa_n \ (m^2 \ s^{-1})$
CTRL	$600 \text{ m}^2 \text{ s}^{-1} \text{ maximum}$	373	385
HIGH	$1200 \text{ m}^2 \text{ s}^{-1} \text{ maximum}$	747	770
LOW	$100 \text{ m}^2 \text{ s}^{-1} \text{ maximum}$	64	62
MLT2D	Mixing-length theory	1808	1693
MLT3D	MLT2D + vertical modes	473	1693
FULL	MLT3D + suppression	222	503

 Table 1.
 List of ACCESS-OM2 experiments

#### <sup>195</sup> Grid-scaling factor

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As even coarse-resolution models can resolve some eddy activity in the tropics where the associated length scales are larger, we also include a grid-scaling factor, not considered by Groeskamp et al. (2020), that reduces  $\kappa_n$  where eddy-mixing may be resolved following Hallberg (2013),

$$g(x,y) = \frac{\Delta^2}{\Delta^2 + L_d^2},\tag{4}$$

where  $\Delta$  is a measure of the grid spacing, taken as the harmonic mean of the zonal and meridional grid spacings,

$$\Delta = \frac{2\Delta x \Delta y}{\Delta x + \Delta y},\tag{5}$$

and we take the surface mode deformation radius (LaCasce, 2017) rather than the standard first-baroclinic deformation radius for  $L_d$  in Eq. (4). We also set a minimum on  $\kappa_n$ of 20 m<sup>2</sup> s<sup>-1</sup> (following Adcroft et al., 2019).

#### 207 2.3 Experiments

The experiments considered in this study are listed in Table 1. Our control experiment (CTRL) is identical to the ACCESS-OM2 default configuration except that it includes the grid-scaling factor [Eq. (4)] which reduces  $\kappa_n$  near the Equator (Fig. 1a). This grid-scaling reduction near the equator has negligible impact on the simulations relative to the differences between the other experiments described below.

CTRL will be compared to five other experiments. All experiments include the grid-213 scaling factor [Eq. (4)]. HIGH and LOW are scaled versions of CTRL with a maximum 214 coefficient of 1200  $m^2 s^{-1}$  (HIGH) or 100  $m^2 s^{-1}$  (LOW). Experiment MLT2D introduces 215 horizontal variations in  $\kappa_n$  through mixing length theory [Eq. (1)]. MLT2D has a sig-216 nificantly larger  $\kappa_n$  throughout the tropics and mid-latitudes compared to CTRL with 217 decreases only in the very high-latitudes (Fig. 2a). Experiment MLT3D then adds the 218 vertical modal structure [Eq. (2)] which results in a decay of  $\kappa_n$  with depth (Fig. 2b). 219 Finally FULL adds the effects of mixing suppression by mean flows [Eq. (3)]. This fac-220 tor significantly reduces  $\kappa_n$  throughout the domain (compare Figs. 2a,b with 2c,d, the 221 surface mean  $\kappa_n$  is reduced by more than a factor of 3, Table 1). Compared to CTRL, 222 FULL is characterized by higher values in the shallow mid-latitudes and lower values in 223 the high-latitudes and at depth (Fig. 2d). The mean flow suppression factor can also re-224 sult in subsurface maximum's in  $\kappa_n$ , notably in the ACC region (Fig. 2d) where subsur-225 face critical layers form as the mean flow speed decays in the vertical, consistent with 226 theory and diagnostics from high-resolution idealized models (e.g. Abernathey et al., 2013, 227 2010; Ferrari & Nikurashin, 2010; Smith & Marshall, 2009). 228



Figure 2. (a,c) Surface  $\kappa_n$  and (b,d) zonal mean  $\kappa_n$  for experiments (a,b) MLT3D (c,d) FULL. The thick (thin) blue contours indicate the 600 m<sup>2</sup> s<sup>-1</sup> (1200 m<sup>2</sup> s<sup>-1</sup>) isosurfaces.

# 229 3 Results

We begin by describing the temporal behavior of the solutions over the 1000 year spin-up period (Section 3.1) and the observed changes in the ocean's zonal-mean overturning circulation (Section 3.2), meridional heat transport (3.3) and tracer fields (Section 3.4). The mechanisms linking the neutral diffusivity to changes in the interhemispheric overturning cell are then explored in Sections 3.5-3.8. Section 3.9 discusses the Antarctic bottom water cell.

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## 3.1 Scalar variables and model spin-up

In order to allow for the slow adjustment of the deep ocean all experiments have 237 been spun-up for 1000 years (Fig. 3). The choice of  $\kappa_n$  has a strong impact on the drift 238 in global ocean heat content (compare solid lines in Fig. 3a). The evolution of global ocean 239 heat content is determined by the net air-sea heat flux, which depends through the bulk 240 formula on the sea surface temperature (SST). Indeed, those experiments with gener-241 ally smaller values of  $\kappa_n$  have cooler global-mean SST in the first few 100 years that drives 242 a positive drift in ocean heat content (e.g. experiment LOW, green lines in Fig. 3a,b). 243 In contrast, larger values of  $\kappa_n$  correspond to warmer transient SSTs and net ocean heat 244 loss (e.g. experiment HIGH, orange lines in Fig. 3a,b). However, the structure in  $\kappa_n$  also 245 impacts the SST and ocean heat content trends; SST is warmest in experiments MLT2D 246 and MLT3D which may be because of the strong neutral diffusion in the Western Bound-247 ary Current regions (e.g. Fig. 2a). 248

The choice of  $\kappa_n$  also has an impact on both the interhemispheric (alternatively "deep", "upper", or North Atlantic Deep Water, NADW) and Antarctic bottom water



Figure 3. Time series of (a) global average Conservative Temperature (°C), (b) global average SST (°C), (c) the maximum of the global MOC in potential density (referenced to 2000 dbar,  $\sigma_2$ ) at 26°N (Sv), a proxy for the strength of the interhemispheric overturning cell and (d) the minimum of the global  $\sigma_2$  MOC at 40°S (Sv), a proxy for the strength of the bottom water cell from all experiments. The dashed black line in panel c indicates the observational value of 17.2 Sv from the RAPID array in the Atlantic (McCarthy et al., 2015). A 10-year running mean smoothing has been applied to panels b-d. The blue bar in panel c indicates the averaging period used for most comparative diagnostics in later figures.

cells of the zonally-integrated MOC in potential density coordinates (Fig. 3c,d). The deep cell achieves equilibrium after  $\sim 600$  years, while the bottom water cell is still trending after 1000 years. In the remainder of the article we focus on differences in the circulation and tracer structure averaged over the last 100 years (blue bar in Fig. 3c).

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## 3.2 The meridional overturning circulation

Stronger (weaker) neutral diffusion drives a broad weakening (strengthening) of the 256 interhemispheric overturning cell (blue in HIGH, Fig. 4c and red in LOW, Fig. 4e). These 257 changes in the deep cell are dominated by the Atlantic basin (not shown) as part of the 258 Atlantic MOC (AMOC). Accompanying these changes in the magnitude of the overturn-259 ing are shifts in the density of the NADW outflow, which becomes denser when  $\kappa_n$  is in-260 creased in HIGH (red patch below  $\sigma_2 = 1036.5 \text{ kg m}^{-3}$  in the Northern Hemisphere 261 in Fig. 4c) and less dense in LOW (Fig. 4e). These changes in NADW density may be 262 a consistent response to the change in the strength of the AMOC, in these quasi-equilibrated 263 simulations where the interior density field has had sufficient time to adjust. A weaker 264 AMOC reduces the input of warm surface water into the North Atlantic (see Section 3.3), 265 leading to SST cooling, reduced surface heat loss, and reduced NADW formation while 266 the NADW that is formed is denser. Likewise, with increased input of warm surface wa-267 ter into the North Atlantic under an enhanced AMOC, there is more surface heat loss 268 leading to more NADW formation but at lighter density classes. The shift in NADW out-269

flow density are also consistent with the entire ocean being denser (lighter) and less (more) stratified in HIGH (LOW), as will be discussed in more detail in Section 3.4.

Change in the bottom water cell mirror those in the interhemispheric cell. The bottom water cell is stronger in HIGH and weaker in LOW (Fig. 4c,e below  $\sigma_2 = 1036.9$ , also see Fig. 3d). However, these changes are less linear than for the interhemispheric cell; with a strong shut down in LOW compared to a weak strengthening in HIGH. This asymmetry may be partially explained by the overlap in density between the denser NADW outflow in HIGH and the bottom-cell.

Adding spatial structure to  $\kappa_n$  in the MLT2D, MLT3D and FULL experiments has 278 additional impacts. Experiments MLT2D and MLT3D, both corresponding to an increase 279 in the global average  $\kappa_n$  compared to CTRL (see Table 1), show a similar pattern of anoma-280 lous overturning to HIGH, albeit with weaker anomalies (compare Figs. 4g,i with Fig. 281 4c). The weaker MOC anomalies in MLT2D compared to HIGH, despite MLT2D hav-282 ing a larger surface- and volume-mean  $\kappa_n$  (see Table 1), highlights the importance of the 283 horizontal structure of  $\kappa_n$ . In particular, it suggests that the smaller or similar  $\kappa_n$  at high-284 latitudes in MLT2D (compared to CTRL or HIGH) are more important than the much 285 larger values at mid-latitudes (Fig. 2a). MLT2D and MLT3D are similar, suggesting that 286 the vertical structure of  $\kappa_n$  has only a minor impact on the MOC. Compared to CTRL, 287 MLT2D and MLT3D are characterized more by a shift in the peak density of the inter-288 hemispheric cell rather than a change in strength (compare red and purple with blue lines 289 in Figs. 5a,b). 290

The weakening of  $\kappa_n$  through mean-flow suppression introduced in FULL has a sig-291 nificant impact on the MOC, with a similar pattern of MOC anomalies to LOW (Fig. 292 4k). The interhemispheric cell responses in FULL and LOW are both around 2 Sv (a 10-293 20% change from CTRL), although in FULL there is a smaller shift in the density of the 294 maximum overturning (compare green and brown with blue lines in Fig. 5a,b). While 295 the purpose of this study is not to better tune the model, it should be noted that ACCESS-296 OM2 has a weak interhemispheric cell compared to observations (compare solid lines to 297 dashed RAPID estimate in Fig. 3a), a comparison that is improved in FULL and LOW 298 (note that the cell is better represented in the  $1/4^{\circ}$  and  $1/10^{\circ}$  configurations of ACCESS-299 OM2, Kiss et al., 2020). While this suggests that  $\kappa_n$  may be too large in ACCESS-OM2, 300 the structure in  $\kappa_n$  is also clearly important. While LOW results in a strong, consistent 301 weakening of the likely already too weak bottom water cell (Kiss et al., 2020), FULL has 302 a negligible impact on the bottom water cell (Figs. 4e,k, 3d). Changes in the bottom wa-303 ter cell are discussed further in Section 3.9. 304

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## 3.3 Meridional heat transport

The ocean's meridional heat transport (MHT) is influenced by  $\kappa_n$  both directly, 306 from changes in the diffusive component of MHT, and indirectly due to circulation (e.g. 307 MOC) changes. The diffusive component of MHT (dashed lines in Fig. 6) is only sig-308 nificant in CTRL in the Southern Ocean south of ~ 40°S, where its sensitivity to  $\kappa_n$ 309 dominates the changes in total MHT (compare solid and dashed lines in Fig. 6b). The 310 weak change in the advective/circulation component of MHT in the Southern Ocean con-311 312 trasts with results from coupled models where wind changes are permitted and compensation between diffusive and advective heat transport can occur (e.g. Pradal & Gnanade-313 sikan, 2014). North of  $\sim 40^{\circ}$ S changes in total MHT are largely driven by the changes 314 in the AMOC discussed above (Fig. 6d). In FULL, the change in the MHT in the At-315 lantic is about 0.05PW, corresponding to 8-17% of the CTRL MHT in the Atlantic. 316 In the HIGH and LOW experiments there are also some small changes in the South Pa-317 cific and Indian Oceans, which are largely absent in FULL (Fig. 6c). This is linked to 318 the lack of change in the bottom water cell in FULL. The bottom water cell anomalies 319



Figure 4. Global MOC in potential density (referenced to 2000 dbar)  $\sigma_2$ -latitude coordinates for the (a) CTRL, (b) HIGH, (d), LOW, (f) MLT2D, (h) MLT3D and (j) FULL experiments. The  $\sigma_2$  density bin sizes are 0.125kgm<sup>-3</sup>. Red (green) colors indicate clockwise (anti-clockwise) circulation. The panels on the right show the difference between each run and the CTRL experiment, with red (blue) colors indicating anomalous clockwise (anti-clockwise) circulation. Thus red (blue) colors indicate a strengthening of the interhemispheric (bottom water) cells, labeled in panel a, and vice versa. The red solid line in each panel marks  $\sigma_2 = 1036.3125$ , the density of the maximum overturning streamfunction in the Southern Ocean in CTRL (panel a). The dashed red lines in panels b,d,f,h and j indicate the equivalent maximum overturning density in each



Figure 5. (a) Anomaly in the maximum transport of the interhemispheric cell, defined as the maximum value of the  $\sigma_2$  overturning streamfunction at densities denser than 1035.6 kg m<sup>-3</sup>, and (b) the corresponding density as a function of latitude. All curves have been smoothed using a 15-point moving average filter in latitude.

dominate the Indo-Pacific density-space overturning differences between LOW and FULL (compare Fig. 4e,k).

#### 322 3.4 Zonal mean tracer fields

The changes in  $\kappa_n$  have an impact on zonal mean temperature and salinity biases 323 (Fig. 7). CTRL has a warm and salty bias reaching 1.5°C and 0.3 psu in the upper 1000 m 324 north of  $60^{\circ}$ S and a cold/fresh bias south of  $60^{\circ}$ S and below 2500 m depth when com-325 pared to observations (Figs. 7e,f). Compared to CTRL, HIGH shows large-scale cool-326 ing of the ocean below the top 500m, a saltier upper ocean and reduced ideal age through-327 out most of the interior (indicating increased ventilation, Fig. 7h-j, England & Rahm-328 storf, 1999; Jones & Abernathey, 2019). The bulk cooling with increased  $\kappa_n$  is consis-329 tent with Danabasoglu and McWilliams (1995) who found similar results when varying 330  $\kappa_n$  and  $\kappa_{GM}$  in tandem. Changes in LOW are largely opposite to HIGH and are con-331 sistent with an increase in the interhemispheric cell, although the anomalies are some-332 what stronger in LOW than HIGH with warming in the Southern Ocean reaching 1.5°C 333 (Fig. 7l-n). 334

Adding spatial structure to  $\kappa_n$  further alters the hydrography. The surface-intensified 335 increase in  $\kappa_n$  in MLT3D drives cooling and increased ventilation (with some surface-336 intensified salinification) that is focused in the upper ocean compared to HIGH (com-337 pare Figs. 7h,p,i,q,j,k). FULL shows anomalies that are similar to LOW as  $\kappa_n$  is reduced 338 in most locations (Fig. 7s). However, FULL is cooler than LOW (and CTRL) in the up-339 per 1000 m in the mid-latitudes and tropics (Fig. 7t). Encouragingly, the warming/salinification 340 in the deep ocean and high latitudes, and the cooling/freshening above 1000 m, in FULL 341 largely opposes the CTRL WOA13 biases (compare Figs. 7t,k to Figs. 7e,f), meaning 342 that these biases are reduced in FULL. 343



**Figure 6.** Meridional heat transport (MHT, PW) in (a) CTRL and MHT anomalies for the (b) global ocean, the (c) Indo-Pacific and the (d) Atlantic basins in HIGH, LOW and FULL. The solid lines show the total MHT and the dashed lines show the component due to neutral diffusion.

## 344

#### 3.5 Where do changes in neutral mixing have an impact?

We now turn to the mechanisms that link the circulation and tracer anomalies dis-345 cussed above to the structure of  $\kappa_n$ . While  $\kappa_{GM}$  directly affects the residual overturn-346 ing circulation and isopycnal slopes, particularly in the Southern Ocean and in deep-water 347 formation regions (e.g. Döös & Webb, 1994; England & Rahmstorf, 1999; Gent, 2011), 348 the impact of  $\kappa_n$  on circulation is less obvious as neutral diffusion does not have a di-349 rect impact on the ocean's density field. Instead,  $\kappa_n$  impacts the circulation indirectly 350 by altering the surface buoyancy forcing and through non-linear equation of state effects 351 such as cabbeling (Klocker & McDougall, 2010) as will be discussed in Sections 3.6 and 352 3.7 respectively. These impacts are strongest where along-isopycnal temperature and salin-353 ity gradients strongest; in the Southern Ocean between  $40^{\circ}$ S and  $60^{\circ}$ S and in the North 354 Atlantic (Fig. 8a,b, also see Fig. 6a). In both these regions there is a distinct pattern 355 of cold and fresh surface waters and warm and salty interior waters following isopycnals 356 (Fig. 8a, Fig. 7b,c), due to net precipitation and sea ice melt at high-latitudes. Thus, 357 increases in  $\kappa_n$  (e.g. in HIGH) have their largest impacts here, where surface-intensified 358 salinification and depth-intensified cooling (compared to CTRL) reflect a reduction in 359 the along-isopycnal temperature and salinity gradients (Fig. 7h,i). In contrast, decreas-360 ing  $\kappa_n$  in LOW leads to weak surface cooling, strong surface freshening and salinifica-361 tion/warming at depth (Fig. 7,l,m). SST changes are weaker than temperature changes 362 at depth because they are damped by surface flux responses. 363



Figure 7. Zonal-mean (a,g,k,o,s)  $\kappa_n$  and (h,l,p,t) temperature, (i,m,q,u) salinity and (j,n,f,v) ideal age anomalies compared to the CTRL experiment (b,c,d) for experiments (g-j) HIGH, (k-n) LOW, (o-r) MLT3D and (s-v) FULL. MLT2D (not shown) has similar temperature and salinity anomalies to MLT3D. (e) Temperature and (f) salinity biases of CTRL relative to WOA13. The black contours represent  $\sigma_2$  potential density contours at 0.1 kg m<sup>-3</sup> spacing. The thin blue contours in panels g-v indicate the 600 m<sup>2</sup> s<sup>-1</sup>  $\kappa_n$  isosurface.



Figure 8. (a) Salinity on the  $\sigma_2 = 1036.3125 \text{ kg m}^{-3}$  isopycnal and (b) the magnitude of the vertically-integrated lateral heat flux due to neutral diffusion in CTRL. Along-isopycnal salinity gradients are strongest at high-latitudes. As  $\kappa_n$  is constant outside the equatorial region in CTRL, the heat flux in panel b indicates the presence of strong instantaneous along-isopycnal temperature and salinity gradients throughout the water-column, where changes in  $\kappa_n$  would be expected to have their largest impact.

## 3.6 The surface flux response to $\kappa_n$

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Changes in SST induced by changes in  $\kappa_n$  impact the surface heat and freshwa-365 ter fluxes through the bulk formula (Large & Yeager, 2004, additional feedbacks would 366 play a role in a coupled model). In the zonal mean, changes in SST are strongest in the 367 Southern Ocean around and just north of  $60^{\circ}$ S and in the North Atlantic north of  $40^{\circ}$ N 368 (Fig. 9a). SST changes in the tropics and mid-latitudes are minimal. The surface cool-369 ing in the Southern Ocean when  $\kappa_n$  is reduced (LOW, orange lines in Fig. 9) induces 370 an anomalous heat flux into the ocean at these latitudes through the bulk formula  $(Q_H,$ 371 Fig. 9c). North of  $\sim 64^{\circ}$ S the cooling also reduces evaporation, resulting in an increase 372 in the net surface volume flux into the ocean (P-E+R+I, Fig. 9d). Thus, changes in both 373 surface heat and volume fluxes in response to the (initially compensated) SST anoma-374 lies lead to an anomalous buoyancy flux into the ocean when SST is cooled (LOW and 375 FULL, orange and green lines in Fig. 9e) and an anomalous buoyancy flux out of the ocean 376 when SST is warmed (HIGH, blue line in Fig. 9e). 377

The above physical interpretation for the changes in buoyancy flux holds outside 378 of the region of permanent influence of sea ice (north of  $\sim 65^{\circ}$ S in the Southern Hemi-379 sphere, Fig. 9g). South of  $65^{\circ}$ S in HIGH there is instead an increase in the surface vol-380 ume flux into the ocean associated with enhanced sea-ice melt driven by the increased 381 upward neutral-diffusive heat flux (blue line in Fig. 9d). However, in these experiments the changes in sea-ice cover are relatively minor (Fig. 9g, being restricted to movements 383 of the seasonal maximum sea-ice edge of a maximum of a few degrees latitude, not shown) 384 and buoyancy flux anomalies in the sea-ice affected region are weaker than further north-385 ward (Fig. 9e). Note that the relatively minor role of sea-ice changes here contrasts with 386 studies performed in coupled models where atmosphere-ocean-sea ice feedbacks can am-387 plify the response to changes in neutral diffusion (e.g. Pradal & Gnanadesikan, 2014). 388

Surface property and flux anomalies are large and variable in the North Atlantic, reflecting the strong direct impact of AMOC changes. Surface heat and buoyancy flux anomalies north of 45°N are as large as the weak CTRL heat and buoyancy fluxes in these regions (not shown). Below we will argue that AMOC changes (and their subsequent impacts on surface flux anomalies in the North Atlantic) are driven by the changes in the Southern Ocean.



Figure 9. Anomalies compared to CTRL in zonal-mean (a) SST, (b) SSS and zonal total (c) surface heat  $(Q_H)$ , (d) surface volume (including precipitation, evaporation, river runoff and ice-ocean volume exchanges, P-E+R+I), (e) surface buoyancy  $(Q_B)$  and (f) vertically-integrated cabbeling and thermobaricity buoyancy flux convergence anomalies in the HIGH (blue), LOW (orange) and FULL (green dashed) experiments. The fluxes in panels c-f are positive when into the ocean (i.e. a positive  $Q_b$  indicates a lightening of surface waters). Each curve has been smoothed using a 5-point latitude smoother for display purposes. (g) The seasonal maximum of the zonal mean sea ice-area fraction.

<sup>395</sup> Changes in  $\kappa_n$  also impact the zonal mean sea surface salinity (SSS) which fresh-<sup>396</sup> ens (becomes saltier) when  $\kappa_n$  is decreased (increased, Fig. 9b). These SSS anomalies <sup>397</sup> are relatively uniform across the whole globe and reflect the increased export of fresh-<sup>398</sup> water northward out of the Southern Ocean when the interhemispheric overturning cell <sup>399</sup> is enhanced.

The buoyancy flux anomalies between  $\sim 65^{\circ}$ S and  $55^{\circ}$ S (Fig. 9e) that result from 400 the SST anomalies, drive a modification in surface flux-driven watermass transforma-401 tion. When  $\kappa_n$  is reduced the resulting positive anomalous buoyancy flux into the ocean 402 (LOW and FULL in Fig. 9e) drives an anomalous cold-to-warm or dense-to-light wa-403 termass transformation. This response, which is at equilibrium, suggests that more up-404 welled water is being converted to lighter waters and moving northward as part of the 405 interhemispheric overturning cell, rather than being converted to denser waters and par-406 ticipating in the bottom water cell. The changes in buoyancy fluxes are therefore con-407 sistent with an enhanced interhemispheric overturning cell. In contrast, when  $\kappa_n$  is in-408 creased the anomalous buoyancy flux is out of the ocean (HIGH in Fig. 9e) and thus surface-409 driven "diapycnal upwelling" is reduced at these latitudes, consistent with a reduced in-410 terhemispheric overturning cell. It is important to note that these are quasi-equilibrium 411 anomalies. The SST anomalies induced by the changes in  $\kappa_n$  are initially compensated. 412 The surface buoyancy flux response to these initial anomalies first acts to change the sur-413 face and interior buoyancy field (as described in Section 3.8) before settling into this new 414 equilibrium. However, these surface buoyancy flux driven watermass transformation changes 415 are also reinforced by changes in watermass transformation associated with cabbeling 416 and thermobaricity. 417

418

## 3.7 Cabbeling and thermobaricity

<sup>419</sup> Changes in  $\kappa_n$  can also lead directly to changes in the interior buoyancy structure <sup>420</sup> (and thus circulation), though non-linear equation of state effects. Straightforward ma-<sup>421</sup> nipulation of the neutral diffusion source term on the RHS of the material time deriva-<sup>422</sup> tive for locally referenced potential density  $D\rho/Dt$  (e.g. see Section 36 of Griffies, 2012) <sup>423</sup> yields,

423

433

$$-\rho_0 \alpha \nabla \cdot \mathbf{J}^\Theta + \rho_0 \beta \nabla \cdot \mathbf{J}^S = \kappa_n \rho_0 \left( C |\nabla_n \Theta|^2 + T \nabla_n P \cdot \nabla_n \Theta \right), \tag{6}$$

where  $\rho$  is locally referenced potential density,  $\Theta$  is Conservative Temperature (McDougall, 2003; McDougall & Barker, 2011), S is salinity (ACCESS-OM2 ostensibly uses practical salinity as its prognostic salt variable and the Jackett et al., 2006, pre-TEOS10 equation of state),  $\alpha$  and  $\beta$  are the thermal expansion and haline contraction coefficients,  $\mathbf{J}^{\Theta}$ and  $\mathbf{J}^{S}$  are the neutral diffusive fluxes of  $\Theta$  and S,  $\nabla_{n}$  represents the two-dimensional horizontal gradient operator along neutral directions, P is pressure and,

$$C = \frac{\partial \alpha}{\partial \Theta} + 2\frac{\alpha}{\beta}\frac{\partial \alpha}{\partial S} - \left(\frac{\alpha}{\beta}\right)^2 \frac{\partial \beta}{\partial S},\tag{7}$$

$$T = \frac{\hat{o}}{\hat{o}}$$

$$T = \frac{\partial \alpha}{\partial P} - \frac{\alpha}{\beta} \frac{\partial \beta}{\partial P}.$$
(8)

While the neutral diffusive fluxes  $\mathbf{J}^{\Theta}$  and  $\mathbf{J}^{S}$  are directed along neutral tangent planes 434 by construction, the dependence of  $\alpha$  and  $\beta$  on temperature and salinity [*cabbeling*, Eq 435 (7)] and pressure [themobaricity, Eq. (8)] can result in a material source of density and 436 thus a diapycnal volume flux (Groeskamp et al., 2016; Klocker & McDougall, 2010; Mc-437 Dougall, 1987; Nycander et al., 2015). Here we quantify cabbeling and thermobaricity 438 as buoyancy flux convergences using Eq. (6), consistent with the numerical discretiza-439 tion of the neutral fluxes themselves as described in more detail in Chapter 36 of Griffies 440 (2012).441

In CTRL, cabbeling acts as a sink of zonally-integrated buoyancy in the high-latitude regions where along-isopycnal temperature gradients are largest (Fig. 10a). Cabbeling



Figure 10. Zonal sum of the buoyancy flux convergence due to (a,c,e,g) cabbeling and (b,d,f,h) thermobaricity quantified using Eq. (6) (converted to buoyancy by multiplying by  $-g/\rho_0$ ) in the CTRL, HIGH, LOW and FULL experiments. Note that the thermobaricity color scale is one half that of the cabbeling scale.

has been shown to be important for the formation of Antarctic Intermediate Water (e.g. 444 Nycander et al., 2015). Thermobaricity has a smaller impact as a sink of buoyancy through-445 out the Southern Ocean interior as well as a source in isolated regions near the surface 446 (Fig. 10b, note the color-scale difference between Figs. 10a,b). When  $\kappa_n$  is increased (de-447 creased) in HIGH (LOW/FULL), cabbeling and thermobaricity are increased (decreased) 448 with little change in pattern. Thus, in the LOW and FULL experiments, we expect a 449 decrease in the magnitude of light-to-dense watermass transformation, or an anomalous 450 dense-to-light transformation, due to non-linear equation of state effects in these regions. 451

Vertically integrating the anomalous cabbeling and thermobaricity flux convergences 452 allows the associated transformation to be compared quantitatively to the surface-driven 453 transformation anomalies in a bulk sense (compare Figs. 9e,f). Between 65°S and 50°S 454 where the surface buoyancy flux anomalies are largest, the reduction in cabbeling and 455 thermobaricity in LOW and FULL corresponds to an effective positive buoyancy flux 456 anomaly of 30-50% the size of the surface buoyancy flux anomalies. Furthermore, there 457 is also a significant reduction in cabbeling and thermobaricity in LOW and FULL further 458 north, up to  $40^{\circ}$ S. In contrast, changes in cabbeling and thermobaricity in the North At-459 lantic are much smaller than the changes in the surface buoyancy flux. The impact of 460 these changes on the density field is examined next. 461

#### 462

## 3.8 Impacts on interior density and circulation

The additional buoyancy fluxed into the ocean through the surface when  $\kappa_n$  is reduced in LOW is carried northwards in the downwelling arm of the Southern Ocean overturning circulation. Combined with reduced cabbeling and thermobaricity (e.g. Fig. 10e near 40°S), this leads to a broad lightening of the "bowl" of waters in the upper ~ 1000m in the tropics and mid-latitudes (Fig. 11f), a signal in density that is more coherent than in temperature or salinity (compare Figs. 11e,f). This bowl is approximately bound below by the  $\sigma_2$  isopycnal corresponding to the maximum in the Southern Ocean overturn-



Figure 11. Zonal mean (a,d,g,j)  $\kappa_n$ , (b,c,h,k) temperature anomalies and (c,f,i,l)  $\sigma_2$  potential density anomalies in (a,b,c) HIGH, (d,e,f) LOW, (g,h,i) MLT3D and (j,k,l) FULL in the Southern Hemisphere. The black contours show  $\sigma_2$  at 0.1 kg m<sup>-3</sup> intervals. The solid (dashed) red lines indicate the CTRL (HIGH/LOW/MLT3D/FULL) 1036.3125 kg m<sup>-3</sup>  $\sigma_2$  isopycnal, which corresponds to the maximum in the CTRL overturning streamfunction. The dotted red lines indicate the maximum overturning isopycnal in the perturbation experiments (see Fig. 5).

ing streamfunction (red lines in Fig. 11, as quantified from Fig. 5), which outcrops near 470 the latitude of maximum wind stress separating Ekman-driven upwelling to the south 471 from downwelling to the north (Stewart & Hogg, 2019; Stewart et al., 2021). In CTRL 472 the maximum overturning is found on the  $\sigma_2 = 1036.3125$  kg m<sup>-3</sup> isopycnal (red solid 473 lines in all panels of Fig. 11), which shifts either northward (in HIGH and MLT3D, dashed 474 red lines in Figs. 11a,g) or southward (in LOW and FULL, Figs. 11d,j), consistent with 475 the changes in transformation. As the surface winds are fixed in these experiments<sup>1</sup> this 476 results in a shift in the projection of the wind stress onto the outcropping density field 477 (Fig. 12). For example, in LOW the density marking both the zero wind stress curl (com-478 pare green and blue lines in Fig. 12) and the maximum in the Southern Ocean overturn-479 ing streamfunction (compare dashed and dotted lines in Figs. 11d,e,f, or Figs. 4a,d) be-480 comes lighter. 481

<sup>482</sup> The coherent upper ocean density changes (Fig. 11c,f,i,l) illustrate that experiments <sup>483</sup> with reduced  $\kappa_n$  have a stronger upper ocean stratification and vice versa. Stronger up-<sup>484</sup> per ocean stratification leads to an enhanced interhemispheric cell overturning through <sup>485</sup> thermal wind balance (e.g. Wolfe & Cessi, 2010) and is consistent with the requirement <sup>486</sup> that more overturning balances increased surface flux-driven, and decreased cabbeling

 $<sup>^1</sup>$  note that the impact of changes in surface currents (through relative wind) and SST on the wind stress are less than 1%.



Figure 12. Wind stress curl binned into  $\sigma_2$  coordinates using the annual mean surface  $\sigma_2$  and wind stress fields. The isopycnal corresponding to the zero in the wind stress curl shifts toward lighter (denser) densities in the experiments where  $\kappa_n$  is decreased (increased). Note that the isopycnals associated with the zero wind-stress curl and those identified as marking the maximum in the Southern Ocean overturning streamfunction do not correspond exactly due to modification by surface flux- and mixing-driven watermass transformation.

and thermobaricity-driven, dense-to-light watermass transformation. This mechanism
is illustrated in Fig. 13 and summarized in the caption.

The mechanism illustrated in Fig. 13 suggests that changes in the North Atlantic 489 are slave to what happens in the Southern Ocean. Our results appear to be inconsistent 490 with the alternative hypothesis that changes in  $\kappa_n$  in the North Atlantic are the main 491 driver. An increase in  $\kappa_n$  in the North Atlantic would, like in the Southern Ocean, be 492 expected to lead to an initially compensated warming and salinification at the surface. 493 In addition to providing more salty water to the surface, a warmer surface leads to en-494 hanced heat loss and evaporation and enhanced light-to-dense water mass transforma-495 tion at the surface in the North Atlantic. Thus, one would expect an intensification of 496 NADW formation and the interhemispheric overturning cell under an increase in  $\kappa_n$ . This 497 is opposite to the changes we see in the HIGH experiment. However, we note that NADW 498 formation in low-resolution ocean models may be sensitive to other parameters, such as 499 the surface salinity restoring rate ( $\sim 40 \text{m}/365$  days in ACCESS-OM2, on the lower end 500 of many of the models participating in the Ocean Model Intercomparison Program, OMIP-501 2, Tsujino et al. (2020)). The contribution of Northern Hemisphere versus Southern Hemi-502 sphere processes to the control of the interhemispheric overturning cell is still under de-503 bate (e.g. Bishop et al., 2016; Delworth & Zeng, 2008; Hogg et al., 2017; Jochum & Eden, 504 2015). The drivers likely depend on the response time-scale (here we examine quasi-equilibrium 505 simulations). 506

507

## 3.9 The Antarctic bottom water cell

The anomalies in overturning in HIGH and LOW emphasize that changes in the interhemispheric cell are often accompanied by changes in the bottom water cell of the opposite sign. This may arise from a competition between conversion of water upwelled in the Southern Ocean; when more water is converted into lighter mode and interme-



Figure 13. A schematic illustrating how changes in  $\kappa_n$  influence the strength of the interhemispheric overturning cell through a zonal average across the Southern Ocean. In CTRL (top) the maximum overturning occurs along the isopycnal (green line) whose outcrop separates the Ekman suction to the south from Ekman pumping to the north (large gray arrows). Across this isopycnal there is dense-to-light watermass transformation (thick orange arrow) driven by the surface buoyancy flux into the ocean (curly orange arrows). Along this isopycnal, surface waters are cold/fresh (blue region) while deeper waters are warm/salty (red region), with the strength of this gradient influenced by neutral diffusion (green curly arrow). Cabbeling and thermobaricity (cyan lines) drive some light-to-dense transformation along these gradients. The interhemispheric and bottom water overturning cells are illustrated in magenta.

When  $\kappa_n$  is reduced (as in LOW or FULL, bottom) along-isopycnal temperature-salinity contrasts are increased leading to cooling/freshening at the surface and warming/salinification at depth. The surface buoyancy flux into the ocean increases in response to surface cooling, leading to increased dense-to-light watermass transformation (orange arrow). The lighter surface waters are carried into the interior along the downwelling arm of the interhemispheric overturning cell, which combined with reduced cabbeling/thermobaricity leads to a lightening of the upper ocean in the mid-latitudes (illustrated by a southward shift of isopycnals illustrated with green lines). This lightening of the upper mid-latitude oceans results in an increased mid-latitude stratification that strengthens the interhemispheric overturning cell through thermal wind balance (e.g. Wolfe & Cessi, 2010, thick magenta line in bottom panel).

diate waters as part of the interhemispheric cell less is converted into denser waters and 512 enters the bottom water cell, and vice versa. Indeed, when  $\kappa_n$  is increased (HIGH), the 513 surface density is increased around the entire Southern Ocean, resulting in larger areas 514 of deeper mixed-layers and indicating enhanced bottom water formation (Fig. 14b). In 515 LOW the response is largely opposite of that in HIGH (Fig. 14c). However, in FULL 516 the surface density anomalies, while having a similar pattern to those in LOW, are sig-517 nificantly reduced in amplitude (Fig. 14d). Similarly, the shoaling of deep mixed layers 518 is much reduced in FULL. This is linked to the stronger neutral diffusion in FULL com-519 pared to LOW across much of the interior Southern Ocean (compare Figs. 14e,f) which 520 supplies heat to the surface. As a consequence, the FULL experiment largely maintains 521 its formation of Antarctic bottom water in contrast to LOW (e.g. compare Figs. 4e and 522 4k). 523

# 524 4 Summary and Discussion

In this study, we have examined the impact of varying physics-based choices for the spatial structure of the neutral diffusivity  $\kappa_n$  arising from unresolved mesoscale eddy stirring, based on the theory and observational study of Groeskamp et al. (2020), on a coarse-resolution global ocean sea-ice model (ACCESS-OM2). We show that ACCESS-OM2's overturning circulation and tracer structure are sensitive to both the magnitude and the spatial structure of  $\kappa_n$ . Results can be summarized as follows:

- 1. In general, stronger (weaker) neutral diffusion leads to a weakening (strengthen-531 ing) in the interhemispheric overturning cell through changes in SST and surface 532 heat, freshwater and buoyancy flux-driven watermass transformation, along with 533 changes in cabbeling and thermobaricity, in the Southern Ocean (as summarized 534 in the schematic in Fig. 13). Changes of  $\pm 2Sv$  (or up to 20%) were found in the 535 interhemispheric cell across our suite of experiments (Figs. 3c, 4). As the surface 536 winds are fixed in these experiments, these changes highlight not only the impor-537 tance of neutral diffusion, but also of buoyancy forcing for the modeled overturn-538 ing circulation. 539
- 2. Our results suggest that the vertical structure based on surface-mode theory (La-540 Casce, 2017) in  $\kappa_n$  has only a modest impact on circulation and tracer fields (com-541 pare MLT2D and MLT3D in Figs. 4,7). In general,  $\kappa_n$  variations at high-latitudes 542 had stronger impacts than at low-latitudes. Most importantly, the effects of mix-543 ing suppression by mean-flows (Ferrari & Nikurashin, 2010) were first-order. Mean-544 flow suppression reduced  $\kappa_n$  throughout much of the ocean (particularly near the 545 surface, compare Figs. 2b,d) and strongly impacted the circulation and tracer struc-546 ture (compared to simulations utilizing mixing length theory only). 547
- 3. The spatial structure for  $\kappa_n$  based on the "best guess" configuration from Groeskamp 548 et al. (2020) in experiment FULL showed the best overall match to observations 549 taking into account the magnitudes of the 1) interhemispheric cell, 2) bottom wa-550 ter cell and 3) zonal mean tracer biases. In particular, the FULL experiment achieved 551 a stronger interhemispheric cell without reducing the bottom water cell, unlike in 552 the spatially-uniform reduction experiment LOW. The use of the FULL spatial 553 structure for  $\kappa_n$  leads to better agreement between the coarse-resolution ACCESS-554 OM2 overturning circulation and meridional heat transport with the high-resolution 555 ACCESS-OM2-025 and ACCESS-OM2-01 configurations (Kiss et al., 2020), where 556 the spatial structure of mesoscale eddy-driven stirring is better resolved. 557

<sup>558</sup> While drawing strong conclusions from a single-model study must be treated with <sup>559</sup> caution given the potential for error compensation, the sensitivity of circulation and hy-<sup>560</sup> drography to  $\kappa_n$  motivates further investigation of the use of the Groeskamp et al. (2020) <sup>561</sup> scheme as a parameterization. However, before use for production purposes further work <sup>562</sup> is needed. For example, the model stratification and flow fields should be used for the



Figure 14. Annual-mean surface density ( $\sigma_0$ , kg m<sup>-3</sup>) plots south of 40°S for (a) CTRL and anomalies from CTRL for the (b) HIGH, (c) LOW and (d) FULL experiments. The annualmean mixed layer depth is contoured at 500 m intervals in black. The red contours indicates the monthly-maximum 50% sea-ice extent (CTRL with dashed contours, HIGH, LOW and FULL with solid contours). Surface values of the neutral diffusivity in (e) LOW and (f) FULL.

calculation of modes, the deformation radius and the mean-flow suppression factor. The
theory could also be combined with a 2D dynamical model for the EKE field (e.g. Adcroft et al., 2019; Jansen et al., 2015). We also note that while the use of an ocean-only
model here helped with the attribution of cause and effect, a similar study performed
in a coupled atmosphere-ocean model is needed to evaluate the impact of additional wind,
buoyancy and sea-ice feedbacks (e.g. Pradal & Gnanadesikan, 2014) that may complicate the response.

We have focused on the neutral diffusivity  $\kappa_n$  in this article and have not discussed 570 similar changes in  $\kappa_{GM}$ . Preliminary experiments indicate that, while spatially-uniform 571 changes in  $\kappa_{GM}$  equivalent to HIGH and LOW have a larger impact on circulation than 572  $\kappa_n$ , more subtle changes in its structure (e.g. equivalent to FULL vs. CTRL with  $\kappa_{GM} =$ 573  $\kappa_n$ ) induce circulation and zonal mean tracer anomalies no larger than those associated 574 with  $\kappa_n$  only. While further work is required, and more sophisticated theories for  $\kappa_{GM}$ 575 and the inclusion of eddy effects on momentum and energy already exist, these results 576 suggest that  $\kappa_n$  deserves more attention in coarse-resolution model sensitivity studies. 577

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Figure 1.

CTRL surface  $\kappa_n$ 



Figure 2.



Figure 3.



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Figure 4.



Figure 5.



Figure 6.





Figure 7.





Latitude (°N)

Figure 8.

![](_page_45_Figure_0.jpeg)

Figure 9.

![](_page_47_Figure_0.jpeg)

Latitude (°N)

Figure 10.

![](_page_49_Figure_0.jpeg)

![](_page_49_Figure_1.jpeg)

Figure 11.

![](_page_51_Figure_0.jpeg)

![](_page_51_Figure_3.jpeg)

Figure 12.

![](_page_53_Figure_0.jpeg)

Figure 13.

![](_page_55_Figure_0.jpeg)

Figure 14.

![](_page_57_Picture_0.jpeg)

![](_page_57_Figure_1.jpeg)

![](_page_57_Figure_2.jpeg)

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![](_page_57_Figure_3.jpeg)

(d) FULL

![](_page_57_Figure_5.jpeg)

![](_page_57_Picture_6.jpeg)

![](_page_57_Figure_7.jpeg)

![](_page_57_Picture_8.jpeg)