The physics behind the hypothesis of alternation

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Abstract

The hypothesis of alternation leads to the idea of immunity after local disaster which, notwithstanding it sounds reasonable, it has been frequently rejected by objective testing. More generally the estimate of the occurrence probability of the next big shock on the basis of the time delay from the last earthquake still represents a big challenge. The problem is that this issue cannot be addressed only on the basis of historical catalogs which contain to few well documented big shocks and decades of future observations appear necessary. On the other hand, recent results have shown that important insights can be obtained from the spatial organization of aftershocks and its relationship to the mainshock slip profile.

Here we address this issue by monitoring the stress evolution together with the occurrence of big shocks and their aftershocks in a physical model where the seismic fault is described as an elastic layer embedded in a ductile medium. The model reproduces all relevant statistical features of earthquake occurrence and allows us to perform accurate testing of the hypothesis of alternation and its consequences, particularly on the side of aftershock spatial patterns. We demonstrate that the hypothesis of characteristic earthquakes is not valid but that is possible to achieve insights on the time until the next big shock on the basis of the percentage of aftershocks occurring inside the high slip contour of the mainshock.

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6	Key Points:
7	• We investigate the hypothesis of alternation in a physical model of a seismic fault
8	presenting realistic features of aftershock occurrence
9	• We find that aftershocks do not occur in large-slip areas which become relocked
10	and the next mainshock occurs in different fault regions
11	• We find that the time until the next big shock is inversely proportional to the per-
12	centage of aftershocks inside the mainshock slip contour

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13 Abstract

The hypothesis of alternation leads to the idea of immunity after local disaster which, 14 notwithstanding it sounds reasonable, it has been frequently rejected by objective test-15 ing. More generally the estimate of the occurrence probability of the next big shock on 16 the basis of the time delay from the last earthquake still represents a big challenge. The 17 problem is that this issue cannot be addressed only on the basis of historical catalogs 18 which contain to few well documented big shocks and decades of future observations ap-19 pear necessary. On the other hand, recent results have shown that important insights 20 can be obtained from the spatial organization of aftershocks and its relationship to the 21 mainshock slip profile. Here we address this issue by monitoring the stress evolution to-22 gether with the occurrence of big shocks and their aftershocks in a physical model where 23 the seismic fault is described as an elastic layer embedded in a ductile medium. The model 24 reproduces all relevant statistical features of earthquake occurrence and allows us to per-25 form accurate testing of the hypothesis of alternation and its consequences, particularly 26 on the side of aftershock spatial patterns. We demonstrate that the hypothesis of char-27 acteristic earthquakes is not valid but that is possible to achieve insights on the time un-28 til the next big shock on the basis of the percentage of aftershocks occurring inside the 29 high slip contour of the mainshock. 30

31 **1** Introduction

The hypothesis of alternation dates back to Gilbert (1909) and states that "When a large amount of stored energy has been discharged in the production of a great earthquake and its after-shocks, it would seem theoretically that the next great seismic event in the same seismic district was more likely to occur at some other place, and that successive great events would be distributed with a sort of alternation through the districts..." In the same manuscript, however, Gilbert concluded "..its corollary of local immunity after local disaster is more alluring than safe".

After 115 years from the fundamental warning raised by Gilbert, the range of va-39 lidity of his hypothesis of "alternation" is not yet fixed. In particular, after the devel-40 opment of the elastic rebound theory, the hypothesis of alternation has been gradually 41 replaced by a stronger hypothesis which is usually termed seismic gap or seismic cycle 42 model. This model assumes that consecutive earthquakes substantially re-rupture the 43 same fault segment, nucleating characteristic earthquakes which are roughly equal in size 44 and roughly periodic in time. As a consequence the terms gap model and characteris-45 tic earthquake model are often used as synonyms and several predictions have been ac-46 cordingly formulated for different geographic regions, as for instance in (McCann et al., 47 1979) and (Nishenko, 1991). This model is still often adopted in earthquake prediction 48 even if many studies (Kagan & Jackson, 1991; Rong et al., 2003) have shown that the 49 gap hypothesis can be rejected with a high confidence level and, as stated by Mulargia 50 et al. (2017), "no recent work makes a strong data-based case in support of these pre-51 dictions". In particular, the spatio-temporal organization of events considered by Rong 52 et al. (2003) appears more consistent with the scenario where large earthquakes follow 53 a Poisson process in time where large earthquake occurrence is fully unpredictable. Nev-54 ertheless, the failure of the gap model, intended as characteristic model, does not imply 55 the failure of the alternation hypothesis as originally formulated by Gilbert. Indeed, the 56 situation becomes more intriguing if one relaxes the assumption of a characteristic size 57 and location of subsequent earthquakes and takes into account the possibility that sub-58 sequent ruptures are allowed to have only partial overlaps. This has recently done in a 59 study (Roth et al., 2017) conducted along the South American subduction zone for the 60 last 500 years, which shows that recurrence times of magnitude $m \ge 7$ earthquakes present 61 some tendencies towards short-time clustering. This result, which is apparently in op-62 position to the hypothesis of alternation, can be still consistent with it if one takes into 63 account that in the data analysis of Roth et al. (2017) only the overlap between epicen-64

tral coordinates is taken into account and that most of the $m \gtrsim 7$ earthquakes rupture 65 only a part of the seismogenic width. Consistently with the hypothesis of alternation, 66 indeed, the partial rupture can cause the stress increase along the unbroken part of the 67 fault width which, in turn, can raise the probability of subsequent earthquakes with sim-68 ilar epicentral coordinates in the near future. This scenario is avoided if one restricts the 69 study to magnitude $m \geq 8$ earthquakes, which are sufficiently large to rupture the full 70 seismogenic zone. Interestingly, in this case Roth et al. (2017) find a weak quasi-periodic 71 temporal organization of events, consistent with the hypothesis of alternation. The prob-72 lem in this case is that the statistical sample is so small, only 20 recurrences, that a def-73 inite conclusion cannot be drawn. To this extent one should need data with a much more 74 accurate hypocentral localization or a much larger statistical sample, not available from 75 historical seismicity. In particular, because of the long time interval between big shocks, 76 many decades of observations would be necessary to have an appropriate sample to sta-77 tistically address this issue. 78

Here we try to give an immediate answer to the fundamental question about the 79 validity of the hypothesis of alternation by recasting to the information provided by re-80 alistic physical models for seismic faults. In particular we present results for a physical 81 model which is able to capture the complex magnitude-spatio-temporal pattern of seis-82 micity, including the occurrence of aftershocks. This last feature can provide very use-83 ful insights on the hypothesis of alternation as recently shown by Wetzler et al. (2018). 84 Indeed, the stress loading mechanism behind the hypothesis of alternation predicts that 85 aftershocks must be located outside the region involved during the mainshock slip or, 86 at most, in regions with low levels of the mainshock slip. This peculiar aftershock pat-87 tern has been recently enlightened in real data by Wetzler et al. (2018) after considering 101 large subduction zone plate boundary mainshocks with well determined coseis-89 mic slip distributions. This accurate study has revealed a deficit of aftershocks inside the 90 mainshock slip area consistently with the hypothesis of large slip areas re-locking. The 91 observation that larger aftershocks typically occur farther away than smaller ones (van der 92 Elst & Shaw, 2015) represents another feature of aftershock occurrence supporting the 93 hypothesis of alternation. More generally, framing the organization of aftershocks in space, 94 time and magnitude within the hypothesis of alternation could lead to very useful pre-95 dictions for the occurrence of the next large earthquake. A striking example is represented by the very interesting prediction, proposed by Wetzler et al. (2018), that the tempo-97 ral distance to the subsequent larger earthquake is smaller the larger is the number of 98 aftershocks inside the high slip contour of the mainshock. Indeed, according to the hyqq pothesis of alternation, an intense aftershock activity inside the mainshock high-slip zone 100 could suggest that the mainshock has released only a small portion of the accumulated 101 shear stress and therefore one could expect a shortest waiting time up to the next main-102 shock. This prediction can be easily put in a testable form but, taking still into account 103 that the occurrence of large earthquakes with overlapping slip regions is a rare event, 104 its experimental validation will need decades of observations. 105

Results of Wetzler et al. (2018) therefore reveals the importance of physical mod-106 els with realistic spatio-temporal patterns of aftershocks in order to test ideas and at the 107 same time to improve existing predictions. Here we demonstrate that it is possible to 108 recover all the main predictions of the hypothesis of alternation within a physical model 109 which quantitatively reproduces the relevant scaling laws of aftershock occurrence. The 110 model, indeed, also reproduces the GR law which is a well established empirical law in-111 dicating that earthquake magnitudes follow an exponential distribution covering a broad 112 magnitude range, in opposition to the seismic cycle model which predicts that only a char-113 acteristic value of the magnitude should be observed. The model we consider is a gen-114 eralization of the Burridge-Knopoff (BK) (Burrige & Knopoff, 1967) model where the 115 seismic fault is described as an elastic interface composed of springs and blocks subject 116 to a velocity-weakening friction law. The original BK model, however, does not produce 117 a "genuine" aftershock activity which is instead observed if the BK interface is embed-118

ded in a more ductile region (Petrillo et al., 2020). This is modeled as a second extended
interface subject to velocity-strengthening rheology and, because of the coupling between
the two interfaces, the stress drop of large earthquakes induces an afterslip dynamics (Perfettini
& Avouac, 2004, 2007) in the velocity strengthening layer. This in turn triggers the occurrence of aftershocks in the velocity weakening layer and this mechanism leads to an
aftershock number which decays in time as a power law, as predicted by the Omori law
(Omori, 1894).

A complete description of the physical model is given in (Petrillo et al., 2020) where also the main results about the spatio-temporal organization of simulated earthquakes can be found. In the following section we describe the main features of the model with results presented in the subsequent section. The last section is devoted to discussions and conclusions.

¹³¹ 2 The model

We consider a rectangular fault, of size $L_x = 15000a$ and $L_y = 200a$, modeled 132 as an elastic layer composed of springs and blocks, where a is the rest length of the springs. 133 The local stress on each block is the sum of two contributions $f_i + q_i$. The stress f_i orig-134 inates from the elastic interaction with the other blocks of the fault layer whereas q_i is 135 the stress induced by the interaction with the ductile region. The model exhibits three 136 distinct phases: the slip phase corresponds to earthquake nucleation and slip propaga-137 tion, the afterslip phase when aftershocks occur and the interseismic phase when the fault 138 is locked. An earthquake is defined as a series of slips occurring during the slip phase 139 and starting from the initial instability of the *i*-th block, whose position defines the epi-140 central coordinates of the earthquake. More precisely, the slip phase is entered as soon 141 as the local stress $f_i + g_i$ overcomes a local random frictional stress threshold τ_i^{th} . The 142 block i is unstable and performs a slip with a stress drop Δf which leads to the follow-143 ing stress redistribution 144

$$\begin{aligned}
f_i(t) &\to f_i(t) - 4\Delta f \\
f_j(t) &\to f_j(t) + \Delta f \\
g_i(t) &\to g_i(t) - 4\Theta\Delta f \\
g_j(t) &\to g_j(t) + (\Theta - \epsilon)\Delta f
\end{aligned}$$
(1)

where i corresponds to the index of each of the four blocks on the fault which are near-145 est neighbor of the *i*-th block, whereas Θ and ϵ are two model parameters. In particu-146 lar, $\Theta \in [0,1]$ quantifies the elastic interaction between the two layers and if $\Theta = 0$ 147 the fault does not interact with the ductile layer whereas the maximum interaction is 148 obtained when $\Theta = 1$. At the same time ϵ controls the amount of stress dissipated and 149 when $\epsilon = 0$ all the stress drop of the *i*-th block is transferred to nearest neighbor block. 150 Nevertheless, since blocks on the fault border have a number of nearest neighbor blocks 151 smaller than four, a further dissipation mechanism is present also when $\epsilon = 0$. 152

After the slip of the block *i* the friction threshold is updated and a new value τ_i^{th} is extracted from a Gaussian distribution with mean $\overline{\tau}$ and standard deviation σ . The stress redistribution can cause the instability of one or more blocks *j*, leading to the propagation of the stress in further blocks via a cascading process. The slip phase, i.e. the earthquake, ends when $f_i + g_i < \tau_i^{th}$ in all sites.

¹⁵⁸ We introduce the quantity $n_k(i)$ for the number of slips performed by the *i*-th block ¹⁵⁹ during the *k*-th earthquake and, since to each slip corresponds a stress drop Δf , the fi-¹⁶⁰ nal local stress drop in the site *i* after the *k*-th earthquake is $\delta f_k(i) = n_k(i)\Delta f$. There-¹⁶¹ fore, the seismic moment M_k released during the *k*-th earthquake can be defined as $M_k \propto$ ¹⁶² $\sum_i \delta f_k(i)$, where the sum extends over all blocks. We finally define the moment mag-¹⁶³ nitude $m_k = (2/3) \log_{10} M_k$, where we have set to zero the arbitrary additive constant.

Furthermore, for each earthquake k, we measure the maximum slip n_k^{\max} as the max-164 imum value of $n_k(i)$ over all blocks. We then define the χ -contour as the continuous line 165 separating the region with $n_k(i) > \chi n_k^{\max}$ from the one with $n_k(i) < \chi n_k^{\max}$, where 166 $\chi \in [0,1]$. For $\chi = 0$ the χ -contour corresponds to the border of the slipped area. We 167 also define the slipped area $A_k(\chi)$ as the total number of sites internal to the χ -contour, 168 i.e. the total number of sites with $n_k(i) > \chi n_k^{max}$. Another measured quantity is the overlap $Q_{k,j}(\chi)$ between the earthquakes k and j, defined as the intersection between 169 170 the slipped areas of the two earthquakes $A_k(\chi) \cap A_j(\chi)$. More precisely $Q_{k,j}(\chi)$ is de-171 fined as the sum over all blocks i such that $n_k(i) > \chi n_k^{max}$ and also $n_i(i) > \chi n_i^{max}$. 172

At the end of the slip phase, because of Eq.s (1), sites which have performed at least one slip during the earthquake present a negative value $g_i(t_0) < 0$. Nevertheless, because of the afterslip dynamics of the ductile layer the afterslip phase starts and $g_i(t)$ continues to evolve in time

$$g_i(t) = g_i(t_0)\Phi(t - t_0).$$
 (2)

Here $\Phi(t)$ is a logarithmic decreasing function of time obtained from the stationary so-173 lution of the rate-and-state friction law ((Dieterich, 1972; Ruina, 1983; Chris, 1998; Lip-174 piello, Petrillo, Landes, & Rosso, 2021)). The afterslip process Eq.(2) leads to a loga-175 rithmic increase of the local stress and eventually to the occurrence of an instability at 176 time t_1 in the site j, such that $f_j + g_j(t_0)\Phi(t_1 - t_0) = \tau_j^{th}$. A new earthquake, i.e. an 177 aftershock, then nucleates from the epicenter j and the slip phase is entered again. The 178 process is iterated such as many aftershocks can be triggered and the afterslip phase ends 179 when $g_i(t_{end}) = 0$ in all sites. At this point the inter-seismic phase starts with the stress 180 $g_i(t)$ growing linearly in time $g_i(t) = (t - t_{end})\dot{g}$, where \dot{g} is a very slow tectonic rate 181 \dot{g} . The linear growth of $g_i(t)$ will lead to a new instability in a given site j where $f_j(t_{end})$ + 182 $(t-t_{end})\dot{g} = \tau_i^{th}$ and, therefore, a new earthquake is triggered. The event triggered at 183 the end of the inter-seismic phase is considered the first event of a new seismic sequence. 184 The end of the seismic sequence corresponds to the end of the afterslip phase t_{end} and 185 we define the mainshock as the largest earthquake in the sequence and its aftershocks 186 or foreshocks are all subsequent or previous earthquakes, respectively, belonging to the 187 same sequence. 188

The main assumptions of the model are that the slip and the subsequent stress re-189 distribution Eq.s (1) occurs so fast that $\Phi(t)$ is constant during the whole slip phase. At 190 the same time we assume that the stress rate \dot{g} is such small that the effect of tectonic 191 drive is negligible during the afterslip phase. Accordingly, we measure times in units of 192 $t_d = \Delta f/\dot{g}$, which is the typical waiting time between two subsequent seismic sequences 193 whereas the typical duration of an aftershock sequence is much smaller than t_d . We re-194 mark that our model, together with Θ and ϵ , presents only one extra parameter which 195 is the standard deviation σ , which quantifies the level of friction heterogeneity. In the 196 case $\Theta = 0$ and $\sigma = 0$ the model coincides with the Olami, Feder, Christensen (OFC) 197 model (Olami et al., 1992) whereas for $\Theta = 0$ and $\sigma > 0$ the model corresponds to 198 the elastic interface depinning model, sometimes defined OFC^{*} model (de Arcangelis et 199 al., 2016). Similar behaviors of the model with $\Theta > 0$ and $\sigma > 0$ are found in other 200 models (Jagla, 2010; Jagla & Kolton, 2010; Jagla, 2011, 2013, 2014; F. m. c. P. Landes 201 et al., 2015; Lippiello et al., 2015; F. P. Landes, 2016; F. P. Landes & Lippiello, 2016; 202 Zhang & Shcherbakov, 2016) which generalize the OFC model by adding a relaxation 203 mechanism responsible for aftershocks and implement heterogeneities in the friction thresh-204 olds τ_i^{th} . 205

We present results for a numerical catalog containing 10000 sequences, setting $\Theta = 0.5$ and $\sigma = 5$. We have verified that similar results are obtained for $\Theta \in [0.2, 0.7]$ and $\sigma > 2$. Furthermore we mostly focus only on mainshocks with $A_k(\chi = 0) > A^{th} = L_y^2$, i.e. earthquakes sufficiently large to expand over the whole seismogenic thickness L_y . Results do not depend on the specific value of A^{th} for sufficiently large A^{th} .

211 3 Results

In Fig.1a we present the temporal evolution of a numerical catalog by plotting the 212 magnitude as function of the time. The figure clearly enlightens the presence of tempo-213 ral clustering with aftershocks mostly concentrated soon after the occurrence of the largest 214 earthquake of each sequence. Fig.1 also shows the efficiency of the model in reproduc-215 ing the GR law. Indeed, we show that the magnitude distribution clearly follows an ex-216 ponential law $P(m) \sim 10^{-bm}$ with $b \simeq 1$ up to values $m \lesssim 4$ (Fig.1b). The distribu-217 tion becomes flatter at larger magnitudes, indicating that the number of $m \gtrsim 4$ earth-218 quakes is larger than the one expected by extrapolating the small m behavior. As shown 219 in (Petrillo et al., 2020) these deviations are caused by events with $A_k(\chi = 0) \gtrsim A^{th} =$ 220 L_y^2 which span over the whole vertical direction, whereas for $L_y \gg 1$ the GR law ex-221 tends over a larger magnitude range. The behavior of Fig.1b therefore suggests the co-222 existence of the GR law with the occurrence of characteristic earthquakes which are suf-223 ficiently large to rupture the whole seismogenic depth. At the same time Fig.1c shows 224 that the number of aftershocks exhibits an hyperbolic decay as function of the time since 225 the mainshock, consistent with the instrumental Omori law. 226

In Fig.1d we plot the stress drop configuration after a typical large mainshock zoom-244 ing in a region surrounding its epicenter. We observe that the stress drop is highly het-245 erogeneous with the high-slip region mostly located around the epicenter whereas the 246 stress drop slightly decreases approaching zero outside the ($\chi = 0$)-contour. In Fig.1d 247 we also plot the epicentral positions of aftershocks showing that the majority of after-248 shocks are located close to the ($\chi = 0$)-contour. In particular the slipped area of the 249 largest aftershocks mostly extend within regions where $n_k(i)/n_k^{\max} \lesssim 0.2$. In order to 250 verify that the pattern observed in Fig.1d is a stable feature of all aftershock sequences, 251 for each mainshock k, we sort its aftershocks in temporal order and indicate with j(k) =252 $1, ..., n_k^{aft}$, the index associated to each after shock. We have verified (Petrillo et al., 2020) that the total number of after shocks n_k^{aft} exponentially depends on the magnitude of the 253 254 mainshock, consistently with the productivity law (de Arcangelis et al., 2016). For each 255 aftershock we measure the quantity $\Delta r_{i(k),k}(\chi)$ defined as the distance of the epicenter 256 of the j(k)-th aftershock from the χ -contour of the k-th mainshock. We adopt the con-257 vention used in (Wetzler et al., 2018) to associate negative (positive) values to $\Delta r_{i(k),k}(\chi)$ 258 if the aftershock epicenter is internal (external) to the χ contour. As clearly evident from 259 Fig.1d the shape of the ($\chi = 0$)-contour is quite irregular, nevertheless we can define 260 a typical size of the slipped area of the k-th mainshock, $R_k = \sqrt{A_k(\chi = 0)/\pi}$, which 261 corresponds to assume a circular shape of the $(\chi = 0)$ -contour. This allows us to ob-262 tain the spatial distribution of aftershocks averaging over mainshocks of different sizes 263 by introducing the re-scaled variable $\Delta r_{j(k),k}(\chi)/R_k$. In the hypothesis of aftershocks 264 homogeneously distributed within the slipped area, and under the assumption of a cir-265 cular contour, the distribution of $\Delta r_{i(k),k}(\chi)/R_k$ is expected to linearly increase up to 266 $\Delta r_{j(k),k}(\chi) = 0$. Results plotted in Fig.2a show instead a deficit of aftershocks with re-267 spect to the uniform distribution at small values of $\Delta r_{j(k),k}(\chi)/R_k < -0.5$ and con-268 versely an excess when $\Delta r_{j(k),k}(\chi) \simeq 0$. This clearly indicates that the majority of af-269 tershocks are spatially located close to the border of the slipped area whereas only few 270 aftershocks occur well inside the slip contour. This feature becomes more evident the 271 larger is the value of χ , indicating that the deficit of interior aftershocks becomes more 272 pronounced when we consider high slip regions. This clearly supports the idea that high 273 slip regions are more stable, in good agreement with the same analysis performed by (Wetzler 274 et al., 2018) on real world mainshocks. We also observe that the deficit of interior after-275 shocks becomes more pronounced if one restricts the previous analysis to aftershocks with 276 magnitude larger than a given magnitude threshold m_{th} . By increasing m_{th} , indeed, the 277 number of interiors aftershock decreases (Fig.2b) whereas the peak close to $\Delta r_{i(k),k}(\chi) \simeq$ 278 0 becomes more pronounced. This feature further supports the hypothesis of alterna-279 tion indicating that the largest aftershocks preferentially occur in regions of low main-280 shock slip. 281



Figure 1. (a). A typical part interval of the numerical catalog containing 11 sequences. We 227 plot the magnitude of each event m versus its occurrence time (in t_d units). Different arrows 228 identify the temporal position of the mainshock in each sequence. According to our choice of 229 model parameters, the duration of after shock sequences is much smaller than t_d and after shock 230 occurrence appears roughly simultaneous to the mainshock occurrence. (b) The magnitude 231 distribution P(m). The orange dashed line is the GR law with b = 1.0. (c) The number of af-232 tershocks as function of time since the mainshock. The magenta dashed line is the hyperbolic 233 Omori decay 1/t. (d) The stress drop configuration after a mainshock with epicentral coordinates 234 (4421a, 149a). Different colors correspond to different level of the stress drop χ as indicated in 235 the color code. Pink circle dots represent the $\chi = 0$ -contour of aftershocks with m > 1.8 whose 236 epicenters are identified by black stars with red contour. Smaller black stars represent the epicen-237 ters of all m > 1 aftershocks. The big six-pointed star is the mainshock epicenter. 238



Figure 2. (a) The distribution of $\Delta r_{j(k),k}(\chi)/R_k$ for m > 0 aftershocks. Different colors correspond to different χ values. (b) The same as panel (a) keeping $\chi = 0$ fixed and considering aftershocks with magnitude larger than m_{th} and different m_{th} values. The dashed magenta line is the expected distribution in the case of aftershocks uniformly distributed in space within the slip area.

3.1 Correlation between pre-stress level and mainshock occurrence

We next define the pre-stress level, at the time $t = t_k$ immediately before the occurrence of the k-th mainshock, as

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$$F_k^{\text{pre}}(t) = \sum_{i \in C(R_k, x(k))} (f_i(t) + g_i(t))$$
(3)

where $C(R_k, x(k))$ is a circle of radius $R_k = \sqrt{A_k(\chi = 0)}/\pi$ centered in x(k), which is the centroid of the ($\chi = 0$)-contour. The above definition allows us to compare the actual pre-stress level on the slipped patch of the fault with the stress level $F_{k'}^{\rm pre}$ in other regions of the same fault and of the same size R_k . The quantity $F_{k'}^{\text{pre}}$ is indeed defined as in Eq.(3) but replacing $C(R_k, x(k))$ with $C(R_k, x_{ran})$, i.e. a circle of the same radius R_k but with center in a random position x_{ran} . We apply periodic boundary conditions for the evaluation of $F_{k'}^{\text{pre}}$. By exploring 1000 random positions x_{ran} , for each mainshock k, we evaluate the difference $\Delta F = F_k^{\text{pre}}(t_k) - F_{k'}^{\text{pre}}(t_k)$ and, considering all mainshocks, we construct its distribution (Fig.3a). Interestingly we find that the support of the distribution of ΔF substantially presents only positive values, indicating that for all main-shocks we almost never find a region with $F_{k'}^{\text{pre}}(t_k) > F_k^{\text{pre}}(t_k)$. We can therefore conclude that, in the large majority of cases, the slipped area is the region with the highest pre-stress level on the fault, supporting the idea that the largest hazard must be associated to the most stressed region. However the actual level of the stress on a fault is practically inaccessible in real world experiments. At the same time, assuming a roughly constant tectonic loading, the stress level is expected to be roughly proportional to the time distance since the last earthquake, an information which is much more easy to achieve experimentally. Accordingly, we also introduce the quantity

$$T_k^{\text{pre}}(t) = \sum_{i \in C(R, x(k))} \left(t - t_k^{last}(i) \right) \tag{4}$$

where $t_k^{last}(i)$ is the last time, before t_k , that the site *i* has been involved in a slipping process. We adopt the same definition of C(R, x(k)) as above and therefore T_k^{pre} is a measure of the average temporal distance from the last slip of the region internal to the circle C(R, x(k)). As in the analysis of Fig.3a we also compute the quantity $T_{k'}^{\text{pre}}$ centering the circle in a random position x_{ran} and we plot the distribution of $T_k^{\text{pre}} - T_{k'}^{\text{pre}}$ in Fig.3b. We recover a pattern very similar to Fig.3a, with the support of the distribution



Figure 3. The distribution of $F_k^{\text{pre}} - F_{k'}^{\text{pre}}$ (panel (a)) and the distribution of $T_k^{\text{pre}} - T_{k'}^{\text{pre}}$ 299 (panel (b)). Both distributions are obtained considering 1000 mainshocks and 1000 different ran-300 dom positions x_{ran} for each mainshock. 301

presenting only positive values. Unexpectedly, the distribution of $T_k^{\text{pre}}(t_k) - T_{k'}^{\text{pre}}(t_k)$ is even more shifted towards the right than the distribution of $F_k^{\text{pre}}(t_k) - F_{k'}^{\text{pre}}(t_k)$. Re-289 290 sults of Fig.3 clearly show that the region hosting the future mainshock is with a very 291 high probability a gap region, i.e. the region with the largest value of T_k^{pre} . We remark 292 that in our model the shear stress rate is homogeneous in space and constant in time and 293 that, for a more appropriate definition of the average temporal distance since the last 294 slip, $T_k^{\rm pre}(t_k)$ must be multiplied by the average value of the shear stress rate, where av-295 eraging must be performed both in space, over the circle C(R, x(k)), and in time. Ac-296 cordingly, in real word seismicity, the comparison between different patches of the same 297 fault and/or of different faults is much more complicated than in our model. 298

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3.2 Time evolution to the next instability

Fig.3 shows that at the time of instability, the region which hosts the impending 303 earthquake is very frequently a gap region. However it also shows the existence of re-gions with similar stress conditions $(F_{k'}^{\text{pre}} \simeq F_{k}^{\text{pre}})$ or similar time delay since the last shock $(T_{k'}^{\text{pre}} \simeq T_{k}^{\text{pre}})$ that will experience a mainshock only at much later times. This 304 305 306 implies that the hypothesis of alternation only holds probabilistically. This feature is clearly 307 enlightened by the temporal evolution of the stress as the mainshock is approaching. At 308 variance with the previous section when the time was fixed at the onset of the next main-309 shock change in space, now we consider a fixed space region, i.e. the circle C(R, x(k)), 310 and study the evolution of F_k^{pre} and F_k^{pre} at different times. In particular, we consider 311 the quantity $F_k^{\text{pre}}(t)$, defined in Eq.3, at different time distances $t = t_k - \delta t$ from the 312 k-th mainshock. It represents the stress level in the region that will host the subsequent 313

mainshock, evaluate a time δt before the mainshock occurrence. We have then evaluated 314 $F_{k}^{\text{pre}}(t_{k}-\delta t)$ for all the 1000 mainshocks and obtained its probability density, defined 315 as the number of mainshocks with $F_k^{\text{pre}}(t_k - \delta t)$ in a given interval $[F, F + \delta F)$ divided 316 by 1000 and by δF . We plot results in Fig.4a for δt values ranging from $\delta t = 15$, cor-317 responding to the typical waiting time between two mainshocks, to $\delta t = 0$, i.e. at the 318 onset of the mainshock occurrence. We observe that the distribution presents a Gaus-319 sian shape which is substantially independent of δt with a roughly constant standard de-320 viation and a mean value which monotonically increases as δt approaches zero. In par-321 ticular we find that values of $F_k^{\text{pre}}(t) \gtrsim 4.4$ are observed only when $\delta t = 0$, signalling 322 the imminence of a mainshock in that area. Nevertheless, several mainshocks are also 323 observed to occur when $F_k^{\text{pre}}(t) \leq 4.2$, when in the majority of cases the mainshock is observed at a much later times. This clearly shows that the hypothesis of alternation holds 324 325 on average since there is a non-null probability to observe a mainshock in a region with 326 a relatively small stress level. This feature becomes even more pronounced when we con-327 sider the evolution of the distribution of $T_k^{\text{pre}}(t_k - \delta t)$ at different δt . In this case, in-328 deed, the distribution is broad at all times δt and in particular we find a clear intersec-329 tion between the distributions evaluated at $\delta t = 15$ and the one at $\delta t = 0$. This im-330 plies that it is probable to have a mainshocks such as its hosting region already presents 331 at a time $\delta t = 15$, i.e. much before the occurrence of the mainshock, a gap value $T_{\mu}^{\rm pre}(t)$ 332 which is larger than the one observed, for other mainshocks, immediately before their 333 occurrence ($\delta t = 0$). We therefore find that the time distance to the next failure, i.e. 334 δt , of a given region C(R, x(k)), is only weakly correlated to the time distance from the 335 previous failure, i.e. $T_k^{\text{pre}}(t)$. This result does not contradict the one of Fig.3: at a given 336 time a mainshock has an higher probability to occur in a gap region but the temporal 337 organization of mainshocks is not trivial and the value $T_k^{\text{pre}}(t)$ does not univocally de-338 termine how close the region is to failure. Indeed Fig.4b shows that the probability that, 339 conditioned to the local value of $T_{mes} = T_k^{\text{pre}}$ measured at a given time t, the next big 340 mainshock will occur in that region at the subsequent time $t+\delta t$, is very low. This prob-341 ability can be however obtained from the intersection point of the vertical line passing 342 for $T_{mes} = T_k^{\text{pre}}$ with the curves at different δt in Fig.4b. 343

Summarizing, we find that even if in our model tectonic loading is constant, the 344 occurrence of mainshocks is not periodic in time but is broad distributed. This feature 345 can be also enlightened by considering the distribution of recurrence times between over-346 lapping mainshocks. More precisely we define that two $m > m_{th}$ mainshocks j and k 347 overlap if the distance between their epicenters is smaller than the maximum between 348 R_i and R_k . In other words, one epicenter must be located within the slipping area of 349 the other mainshock. We then define $\Delta t_{j,k}$ as the temporal distance between a main-350 shock k and its subsequent overlapping mainshock j. The probability density function 351 of $\Delta t_{j,k}$ is plotted in Fig.5 as function of the normalized recurrence time, obtained by 352 dividing $\Delta t_{j,k}$ by its average value $\langle \Delta t_{j,k} \rangle$. If we set $m_{th} = 3.5$, which is sufficiently large to have $A_k(\chi = 0) > A^{th} = L_y^2$, we find (Fig.5a) that the probability density distri-353 354 bution presents a peak around $\Delta t_{j,k} \simeq \langle \Delta t_{j,k} \rangle$, indicating a quasi-periodic behavior. 355 The probability density distribution is however broad presenting, with non-vanishing fre-356 quency, recurrence times as smaller as $0.1\langle \Delta t_{i,k}\rangle$ and also as large as $3\langle \Delta t_{i,k}\rangle$. Interest-357 ingly the behavior of the probability density distribution of the numerical catalog ap-358 pears in qualitative agreement with the one obtained by (Roth et al., 2017) from the his-359 torical record of m > 8 earthquakes along the South American subduction zone. A more 360 quantitative comparison between the numerical and the historical distribution is mean-361 ingless since, as anticipated in the introduction, the historical distribution is obtained 362 with only 20 recurrence times. At the same time, by considering a smaller $m_{th} = 3$ we 363 find (Fig.5b) the presence of a peak at $\Delta t_{j,k} \simeq 0$ indicating short-time clustering rem-364 iniscent of the one obtained from historical data of (Roth et al., 2017) when all m > 7365 earthquakes are included in the analysis. In our data set the peak at short time is caused 366 by m > 3 aftershocks which occur close in space to the mainshock, causing their spa-367 tial overlap with it, and also close in time, leading to $\Delta t_{i,k} \simeq 0$. 368



Figure 4. (a) The probability density of the stress level $F_k^{\text{pre}}(t_k - \delta t)$ inside a region of size R_k centered in the mainshock epicenter evaluated at a time distance δt before the mainshock occurrence. (b) The probability density of the average time delay $T_k^{\text{pre}}(t_k - \delta t)$ inside a region of size R_k centered in the mainshock epicenter evaluated at a time distance δt before the mainshock occurrence. Different curves correspond to different δt values (see the legend).



Figure 5. The probability density of recurrence times between successive overlapping earth-374 quakes is plotted as function of recurrence times divided by their average. Black circles are used 375 for data from the numerical catalog considering earthquakes with magnitude $m \geq 3.5$ which are 376 sufficiently large to break all the seismogenic depth $(A_k(\chi = 0) \gtrsim L_y^2)$ in panel (a) and consid-377 ering all $m \geq 3$ earthquakes in panel (b). Filled green diamonds represent the same quantity 378 extrapolated from Fig.4 of (Roth et al., 2017) obtained from historical data of the South Ameri-379 can subduction zone considering $m \ge 8$ earthquakes in panel (a) and $m \ge 7$ earthquakes in panel 380 (b). 381



Figure 6. The parametric plot of Δt_k versus $\rho_k^{int}(\chi)$. Different colors correspond to different values of χ . Colored continuous lines represents the best linear fit $\Delta t_k = T_M - 120\rho_k^{int}(\chi)$, for each data set with $T_M = 101, 79, 65, 47$ for $\chi = 0, 0.15, 0.3, 0.5$, respectively.

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3.3 The temporal distance until the next mainshock

We next explore the conjecture (Wetzler et al., 2018) that an excess of interior af-383 tershocks could indicate a smaller stress drop of the mainshock and therefore a shorter 384 time for the reactivation of the fault patch. For this kind of analysis we first evaluate 385 the percentage of interior aftershocks of the k-th mainshock, $\rho_k^{int}(\chi)$, defined as the ra-386 tio between aftershocks with $\Delta r_{j(k),k}(\chi) < 0$ and the total aftershock number n_k^{aft} . We 387 then assume that a subsequent mainshock j slips over the region involved by the slip pro-388 cess of a previous mainshock k, if $Q_{k,j}(\chi = 0) > 0.5A_j(\chi = 0)$. This criterion corre-389 sponds to the condition that two mainshocks are overlapping if there exists an overlap 390 larger than the 50% between their slipping regions. We next indicate with $\Delta t_k = t_i -$ 391 t_k the waiting time between two subsequent overlapping mainshocks and in Fig.6 we present 392 the parametric plot of Δt_k versus $\rho_k^{int}(\chi)$, for all overlapping mainshocks in the numer-393 ical catalog. Results clearly enlighten the correlation between Δt_k and $\rho_k^{int}(\chi)$ support-394 ing the prediction that a larger percentage of interior earthquakes (larger $\rho_k^{int}(\chi)$) indi-395 cates a smaller waiting time Δt_k to the next repeated mainshock. This result holds for 396 all considered values of χ and for instance, for $\chi = 0.5$, we find that the waiting time 397 to the next mainshock is of order of $100t_d$ when the percentage of interior aftershocks 398 are larger than the 40% and becomes about 400 times larger $(4E5t_d)$ when this percent-399 age is smaller than the 10%. Even if data are scattered, a linear fit $\Delta t_k = T_M - \phi_M \rho_k^{int}(\chi)$ 400 appears consistent with data, with $\phi_M \simeq 120$ independent of χ and $T_M \in [47, 101]$ 401 according to the χ value. This information can be very useful to improve mainshock fore-402 casting. 403

407 4 Discussion and Conclusions

Large earthquakes are rare events and this prevents the development of efficient 408 forecasting models based only on the statistical information provided by the few histor-409 ical large earthquakes. Therefore, the only possibility to make a skilful forecasting, with-410 out waiting to collect data for decades or even centuries, is to recast to physical mod-411 els. The identification of the correct model is therefore a fundamental step preliminary 412 to the formulation of a good forecasting hypothesis. In particular, the gap model orig-413 inates from the description of the fault as a single block driven at a constant rate un-414 415 der a constant Coulomb friction. Within this description, indeed, the block will perform slips of equal size at regular time intervals. The model however neglects several key fea-416 tures of earthquake triggering such as time-dependent stress transfer mechanisms, which 417 are responsible for aftershock occurrence, as well as heterogeneity in friction level and 418 in the stress drop, etc... Roth et al. has already shown that the description of the fault 419 as a single block under a rate-and-state friction law, after implementing an heterogeneous 420 instead of constant stress drop, leads to a temporal organization of large events in much 421 better agreement with experimental recurrence times. In their study, however, the length 422 of the slipping patch is not controlled by the pre-existing stress condition but it is im-423 posed by hand to be consistent with the GR law. The GR law, conversely, spontaneously 424 originates within the BK description of the fault where many blocks are assumed to be 425 elastically connected within each other (de Arcangelis et al., 2016). Starting from this 426 description and taking into account friction heterogeneity together with the coupling with 427 a more ductile layer where afterslip occurs, here we present a a model that also repro-428 duces realistic feature of aftershock occurrence in space, time and magnitude. The model 429 appears the appropriate numerical laboratory where forecasting hypotheses can be tested 430 and validated. In this study, in particular, we have tested the hypothesis of alternation 431 formulated by Gilbert (1909) more than 120 years ago and stating that "the next great 432 seismic event in the same seismic district was more likely to occur at some other place". 433 Our model shows that even if we implement a shear stress rate which is uniform in space 434 and constant in time, the *characteristic* scenario where large earthquakes are roughly pe-435 riodic in time must be discarded. Nonetheless, even if the time distance to the next fail-436 ure is weakly correlated to the time distance from the previous earthquake, we find that 437 the next large earthquake has an higher probability to be hosted by a gap region. Fur-438 thermore our study demonstrates the usefulness of aftershocks to have insights on the 439 timing of the next large earthquake, coherently with the direction identified by Wetzler 440 et al. (2018) from real world seismic data. In particular, our results provide further sup-441 port to the scenario presented in Fig.8B of Wetzler et al. (2018) corresponding to a de-442 ficiency of aftershock activity within the core of the coseismic slip area, and a concen-443 tration near the perimeter. As concluding by Wetzler et al. (2018), even if this interpre-444 tation provides the best description of real world seismicity, other scenarios could not 445 be completely excluded because of the uncertainty in slip areas and aftershock locations. 446 In our numerical study these problems are not present and the deficiency of aftershocks 447 is clearly proven. Moreover we also demonstrate the validity of the conjecture proposed 448 by Wetzler et al. (2018) that the temporal distance to the subsequent large earthquake 449 is smaller the larger is the percentage of aftershocks inside the high slip contour of the 450 mainshock. 451

More generally the preented model can be used to validate patterns that, because of instrumental uncertainties, emerge less clearly from real world data. For instance, the model exhibits (Petrillo et al., 2020) a decrease in the b-value of the GR law during premainshock seismicity which has been also proposed as a distinct feature of instrumental foreshocks (Gulia & Wiemer, 2019; Lippiello, Petrillo, & Godano, 2021). A better understanding of these patterns in the physical model can be fundamental to better test this hypothesis in instrumental data.

At the same time the agreement between spatial patterns of numerical and instru-459 mental aftershocks suggests that the mechanism responsible for aftershock triggering is 460 correctly implemented in our model. This represents a further support to the hypoth-461 esis that aftershocks are induced by afterslip (Perfettini & Avouac, 2004, 2007; Lippiello et al., 2019; Petrillo et al., 2020; Lippiello, Petrillo, Landes, & Rosso, 2021). On the other 463 hand, the model we present neglects many features of real fault systems. As an exam-464 ple, it considers an isolated fault ignoring the interaction among different faults which 465 can cause a time advance or delay to the next mainshock and it assumes a constant and 466 homogeneous shear stress rate. This makes the application of our findings to real world 467 seismic occurrence not straightforward. 468

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476 Data availability: The source code of the numerical model is available from the
477 corresponding author. Numerical data that support the findings of this study are avail478 able from the corresponding author upon reasonable request.

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