

Evaluation of a Coupled Wave-Ice Model in the Western Arctic

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Abstract

The retreat of Arctic sea ice is enabling increased ocean surface wave activity at the sea ice edge, yet the physical processes governing interactions between waves and sea ice are not fully understood. Here, we use a collection of in situ observations of waves in ice to evaluate a recent global climate model experiment that includes coupled interactions between ocean waves and the sea ice floe size distribution. Observations come from subsurface moorings and free-drifting buoys spanning 2012-2019 in the Beaufort Sea, and we group the data based on distance inside the ice edge for comparison with model results. Locally generated wind waves are relatively prevalent in observations beyond 100 km inside the ice but are absent in the model. Low-frequency swell, however, is present in the model, while subsurface moorings located more than 100 km inside the ice do not report any swell with significant wave height exceeding the instruments' detection limits. These results motivate further model development and future observing campaigns, suggesting that local wave generation inside the ice edge may play a significant role for floe fracture while demonstrating a need for more robust constraints on wave attenuation by sea ice.

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2 **Western Arctic**

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8 **Key Points:**

- 9 • We compare in situ observations of ocean surface waves in the Beaufort Sea with
10 a coupled wave-ice model
- 11 • Locally generated wind waves are observed more than 100 km within pack ice, but
12 the model lacks the resolution to generate waves in leads
- 13 • Swell is not observed more than 100 km within pack ice, but the model predicts
14 that swell can persist at least this far in the Beaufort Sea

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Abstract

The retreat of Arctic sea ice is enabling increased ocean surface wave activity at the sea ice edge, yet the physical processes governing interactions between waves and sea ice are not fully understood. Here, we use a collection of in situ observations of waves in ice to evaluate a recent global climate model experiment that includes coupled interactions between ocean waves and the sea ice floe size distribution. Observations come from subsurface moorings and free-drifting buoys spanning 2012-2019 in the Beaufort Sea, and we group the data based on distance inside the ice edge for comparison with model results. Locally generated wind waves are relatively prevalent in observations beyond 100 km inside the ice but are absent in the model. Low-frequency swell, however, is present in the model, while subsurface moorings located more than 100 km inside the ice do not report any swell with significant wave height exceeding the instruments' detection limits. These results motivate further model development and future observing campaigns, suggesting that local wave generation inside the ice edge may play a significant role for floe fracture while demonstrating a need for more robust constraints on wave attenuation by sea ice.

Plain Language Summary

Sea ice, the frozen surface water of polar oceans, is retreating toward the pole in the Arctic Ocean. The increase in open-ocean area around remaining sea ice enables bigger ocean waves, which can travel into sea ice and break ice into smaller pieces. Currently, climate models do not include ocean waves and their impacts on sea ice. In this study, we compare field observations with a model that simulates interactions between waves and sea ice. The observations, spanning 2012-2019 in Arctic waters north of Alaska, come from underwater instruments and floating buoys where the ocean surface is partially ice-covered. We check for differences in wave height, how wave energy is distributed between short and long wavelengths, and whether waves are generated by local winds. We find that local wind waves generated in partial sea ice cover appear in observations but not in the model. Separately, waves generated outside of sea ice that later traveled into ice cover are present in the model but not in observations beyond 100 km inside the ice. Local wave generation in sea ice may be important for changes in ice cover, and these results motivate model development and future observations.

1 Introduction

As the retreat of Arctic sea ice promotes increased ocean surface wave activity (Thomson & Rogers, 2014), interactions between waves and sea ice could play an elevated role in the Arctic climate system. Increasing wave heights have already been observed in the Beaufort Sea where fetch, the open water distance available for wave development, has expanded due to seasonal sea ice loss (X. L. Wang et al., 2015; Liu et al., 2016; Thomson et al., 2016; Smith & Thomson, 2016). Summer sea ice is also becoming less compact near the newly exposed, rougher seas that surround the remnant of sea ice left in the central Arctic (Martin et al., 2014; Thomson, Ackley, et al., 2018; Squire, 2020).

When waves encounter sea ice floes, distinct masses of ice ranging in size from meters to hundreds of kilometers, the ice scatters and dissipates wave energy (Wadhams et al., 1988; Squire et al., 1995; Squire, 2007; Kohout et al., 2014; Meylan et al., 2014; Montiel et al., 2016; Squire, 2020). In turn, ocean surface waves break large ice floes into smaller floes (Mellor et al., 1986; Meylan & Squire, 1994; Langhorne et al., 1998; Marko, 2003; Toyota et al., 2006; Collins et al., 2015), and during freezing conditions, waves can inhibit the formation of an extensive ice sheet by forcing frazil ice crystals to weld into small floes (Shen et al., 2001, 2004; Roach, Smith, & Dean, 2018). The interaction between waves and sea ice could cause a positive feedback: wave-induced ice fracture in-

64 creases the lateral melt potential of floes by exposing more perimeter (Steele, 1992), melt-
65 ing the sea ice cover and facilitating further wave propagation (Kohout et al., 2011; As-
66 plin et al., 2012, 2014; Horvat et al., 2016; Smith et al., 2021).

67 Interactions between waves and sea ice occur in the marginal ice zone (MIZ), the
68 partially ice-covered region that separates interior pack ice from open ocean. We do not
69 have direct estimates of the MIZ’s location and extent because measuring waves in ice
70 at basin scale is an ongoing challenge. While the physical significance of the dynamic
71 MIZ stems from wave presence near the ice edge, a practicable proxy based on interme-
72 diate ice concentrations is often used to represent the MIZ. This proxy is the region with
73 sea ice concentration (SIC) between 15% and 80% and is readily available from passive
74 microwave satellite estimates (Comiso et al., 1997; Strong & Rigor, 2013; Strong et al.,
75 2017). The Arctic MIZ extent, when defined as the area with 15-80% SIC, may be ex-
76 panding relative to the retreating pack ice (Aksenov et al., 2017; Rolph et al., 2020), and
77 wave-ice interactions are emerging as a leading control on seasonal sea ice and the fu-
78 ture state of the MIZ (Thomson, Ackley, et al., 2018).

79 We can obtain a basic understanding of wave statistics through bulk wave char-
80 acteristics, e.g., significant wave height, but full wave spectra contain additional infor-
81 mation that becomes critical for frequency-dependent wave-ice interactions. When con-
82 sidering wave spectra in ice, we expect to see a narrowing of the spectral bandwidth as
83 energy is concentrated at the low frequencies indicative of swell (Thomson et al., 2019).
84 This narrowing occurs as waves enter the ice due to dependence of the wave-attenuation
85 rate on frequency, where low-frequency energy is better able to survive compared to high-
86 frequency energy (Wadhams et al., 1988; Meylan et al., 2014; Rogers et al., 2016). We
87 do not have a comprehensive explanation for the physical processes responsible for the
88 dissipation of wave energy in the MIZ (Meylan et al., 2018).

89 Swell, the low-frequency waves that have traveled outside of their original wind-
90 generation area, can penetrate hundreds of kilometers inside the sea ice edge when the
91 wave heights are large, according to observations from the Antarctic (Kohout et al., 2014;
92 Li et al., 2015) where wave periods can become longer than in the Arctic Ocean. In con-
93 trast, high-frequency waves generated by local winds tend to dissipate during their first
94 10-20 km of travel into the sea ice field, according to Squire and Moore (1980). However,
95 Masson and Leblond (1989) developed a model explaining how local wind waves can be
96 generated in areas of low ice concentration and sparse ice floes. In surface buoy measure-
97 ments, Smith and Thomson (2016) found support for the open water distance between
98 floes as a control parameter for wave energy. Intense winds acting directly on sea ice,
99 rather than on open water, can drive local wave generation even in Arctic pack ice (Johnson
100 et al., 2021). While these studies have provided a constructive framework for studying
101 ice-affected wind waves, we currently have a limited understanding of the impact and
102 prevalence of locally generated, high-frequency wind waves in sea ice.

103 The absence thus far of wave-ice interactions in coupled climate models may ex-
104 plain some of the differences in Arctic sea ice between models and observations reported
105 by several studies (e.g., Shu et al., 2020; Notz & Community, 2020). Tietsche et al. (2014)
106 found that model errors in sea ice concentration are most severe in the MIZ, and Blanchard-
107 Wrigglesworth et al. (2021) hypothesize that ocean waves may be responsible for the greater
108 high-frequency variability in sea ice extent found in observations compared to CMIP mod-
109 els, which do not simulate wave-ice interactions.

110 Despite persistent uncertainty in wave-ice modeling (Meylan & Squire, 1994; Squire,
111 2007; R. Wang & Shen, 2010; Collins & Rogers, 2017; Squire, 2018; Shen, 2019; Voer-
112 mans et al., 2019), recent years have seen major advances in the development of fully
113 coupled wave-ice models (Williams et al., 2013; Horvat & Tziperman, 2015; Roach, Hor-
114 vat, et al., 2018; Roach et al., 2019; Boutin et al., 2018, 2020; Aksenov et al., 2020). Roach,
115 Horvat, et al. (2018) and Roach et al. (2019) incorporated a prognostic sea ice floe size

116 distribution (FSD) in a global sea ice model coupled with an ocean surface wave model,
 117 representing wave-ice interactions in both the Arctic and Antarctic for the first time. This
 118 model includes a physical relationship between floe fracture, lateral melt potential, and
 119 ice-albedo feedback. In contrast to other approaches, the model also includes dependence
 120 of wave attenuation on floe size (Meylan & Squire, 1994; Montiel et al., 2016; Meylan
 121 et al., 2021). The Roach et al. (2019) model is a focus of this paper and is described fur-
 122 ther in section 2.1.

123 The scarcity of observations of waves in ice continues to be an obstacle for both
 124 model evaluation and theoretical understanding. Obtaining valid measurements of wave
 125 spectra is a challenge when sea ice obscures the ocean surface. The variety of ice con-
 126 ditions, ranging from sparse pancake floes to extensive sheets of ice, complicates inter-
 127 pretation, and existing datasets sample a limited range of ocean and sea ice conditions
 128 (Collins et al., 2015). Furthermore, for any fixed location, there is a short window of time
 129 during the ice melt and growth seasons when waves in ice can be observed. Remote sens-
 130 ing is a promising path for extending spatial coverage and obtaining more robust wave-
 131 ice statistics, and recent efforts have produced estimates of wave heights in the presence
 132 of ice using satellite measurements (Ardhuin et al., 2017, 2019; Stopa et al., 2018; Hor-
 133 vat et al., 2020). Nevertheless, basin-scale, long-term observations from remote sensing
 134 are not yet available. Multi-year in situ observations, however, are available from three
 135 recent field campaigns in the Western Arctic: the Arctic Sea State (Thomson, Ackley,
 136 et al., 2018), the Beaufort Gyre Observing System (BGOS), and the Stratified Ocean
 137 Dynamics in the Arctic (SODA) programs. These three sets of measurements are a fo-
 138 cus of this study and are described further in section 2.2.

139 Here, we interpret this collection of in situ observations spanning 2012-2019 in the
 140 Beaufort Sea from subsurface moorings, supplemented by deployments of freely drift-
 141 ing surface buoys during wave events, measuring ocean surface waves in partial ice cover.
 142 We compare the in situ observations with results from the Roach et al. (2019) coupled
 143 sea ice-surface wave model forced with atmospheric reanalysis by evaluating wave heights,
 144 wave spectra, and the nondimensional scaling relations that can distinguish local wind-
 145 generated waves from swell. Global climate models, including the model considered in
 146 this study, have errors in ice-edge position that preclude point-by-point comparison with
 147 individual observations, so here we aggregate multiple datasets into a relatively large sam-
 148 ple to support statistically motivated model evaluation of waves in ice in the Beaufort
 149 Sea.

150 In section 2, we describe the Roach et al. (2019) model and the in situ observations.
 151 We relate the methods of model-observation comparison in section 3 and present results
 152 of the comparisons in section 4. We discuss the results in section 5 and conclude in sec-
 153 tion 6.

154 **2 Model and Observations**

155 **2.1 Coupled Wave-Ice Model**

156 We analyze results from an experiment using the Los Alamos sea ice model, CICE5
 157 (Hunke et al., 2015) coupled to the ocean surface wave model, Wavewatch III v5.16 (The
 158 WAVEWATCH III (R) Development Group (WW3DG), 2016). To simulate wave-ice in-
 159 teractions, the model includes a prognostic FSD developed by Roach, Horvat, et al. (2018)
 160 and Roach et al. (2019). Floe sizes are determined by lateral growth and melt, welding
 161 of floes in freezing conditions, and the ocean surface wave spectrum through floe frac-
 162 ture and wave-dependent new ice formation. Attenuation of wave spectral energy in ice
 163 depends on mean floe size, ice concentration, and ice thickness based on an empirical fit
 164 to floe-scattering theory, including a supplemental attenuation term for long wavelengths
 165 (Meylan et al., 2021). Figure S1 includes illustrative values of wave attenuation coeffi-

Table 1. Summary of In Situ Observations

Dataset	Instrument	Period	(Lat., Lon.)	0-100 km ¹	100+ km ¹
BGOS-A	AWAC	2012-2018	(75 N, 150 W)	27	68
BGOS-D	AWAC	2013-2018	(74 N, 140 W)	84	4
SODA-A	Signature500	2018-2019	(73 N, 148 W)	39	10
SODA-B	Signature500	2018-2019	(75 N, 146 W)	97	3
SODA-C	Signature500	2018-2019	(78 N, 139 W)	0	19
SWIFTs ²	Buoy	Oct-Nov 2015	various	838	22
BGOS-SODA Total (excludes SWIFTs)				247	104

¹Number of valid wave measurements in sample with significant wave height exceeding the 0.3 m detection limit of the BGOS-SODA moorings; data is grouped by distance inside the ice edge (Δ^{dist} ; see section 3.1)

²Represents 27 buoy deployments

166 cients for various floe sizes, ice thickness values, and wave periods. Thicker ice tends to
 167 cause stronger attenuation, whereas the effect of floe size depends on the period consid-
 168 ered. Shorter periods always experience stronger attenuation.

169 Both the sea ice model and ocean surface wave model evolve freely while forced with
 170 JRA-55 atmospheric reanalysis (Kobayashi et al., 2015; Japan Meteorological Agency,
 171 Japan, 2013) and coupled to a slab ocean model (SOM) (Bitz et al., 2012). The SOM
 172 is a single-layer model, diagnosed from the monthly climatology of a control run of the
 173 Community Climate System Model Version 4 (CCSM4), that specifies mixed-layer depths
 174 constant in time, annually periodic ocean surface currents, and an annually periodic ocean
 175 heat transport convergence, the Q_{flux} ; all three SOM input parameters vary in space.
 176 The sea ice and wave models are on a displaced-pole nominal 1° grid (gx1v6), and the
 177 size of model grid cells near observations in the Beaufort Sea is approximately 50 by 50
 178 km. The simulation spans 1979-2019, and we analyze hourly model output over 2012-
 179 2019 in line with the period of observations. The experiment is identical to FSD-WAVEv2
 180 in Roach et al. (2019), except we use a higher coupling frequency between the wave and
 181 sea ice components. Here, the wave and sea ice components exchange the ocean surface
 182 wave spectrum and sea ice concentration, thickness, and mean floe size every hour to bet-
 183 ter resolve short-timescale wave-ice interactions.

184 2.2 In Situ Observations

185 By aggregating sources of observations that span multiple years with generally con-
 186 tinuous sampling, we compile a relatively large dataset to support statistical model eval-
 187 uation. This dataset, denoted henceforth as BGOS-SODA, consists of two groups of sub-
 188 surface moorings, spanning 2012-2019 and five locations in the central Beaufort Sea (Ta-
 189 ble 1; Figure 1). In this section, we briefly review each source of observations.

190 The first group included in the BGOS-SODA aggregate dataset comes from the Beau-
 191 fort Gyre Observing System (Krishfield et al., 2014). BGOS includes two subsurface moor-
 192 ings, BGOS-A and BGOS-D, with upward-looking Nortek Acoustic Wave and Current
 193 (AWAC) instruments for surface tracking. BGOS-A and BGOS-D sample every hour and
 194 began collecting measurements in 2012 and 2013, respectively. Raw data are processed
 195 following Herbers et al. (2012), Kuik et al. (1988), and Thomson, Girton, et al. (2018)
 196 and converted to wave energy spectra. Data from 2012 is reported in Thomson and Rogers
 197 (2014), and a reanalysis of the same data is found in Smith and Thomson (2016). Here,
 198 we employ an extended dataset that is mostly continuous from 2012-2018 (Thomson, 2020).

199 The second group comes from the Stratified Ocean Dynamics in the Arctic project.
 200 Three subsurface moorings, denoted SODA-A, SODA-B, and SODA-C, use the upward-
 201 looking Nortek Signature Doppler profiler for acoustic surface tracking. Raw data from
 202 SODA are quality-controlled using methods comparable to the BGOS methods, produc-
 203 ing measurements of surface wave spectra sampled every two hours. Data from the SODA
 204 moorings first appear in Brenner et al. (2021), but the wave spectra have not been pre-
 205 viously reported. The SODA dataset spans 2018-2019.

206 Both sets of subsurface moorings detect surface gravity waves via altimeter mea-
 207 surements of surface displacement. An important nuance of the moorings is that the sur-
 208 face tracking simultaneously measures surface gravity waves and sea ice draft. However,
 209 the signal from surface waves can be distinguished from that of ice based on spectral char-
 210 acteristics. This separation is part of the quality-control process. Deformed sea ice pro-
 211 duces a “red” spectrum with under-ice topography exhibiting peak spectral variance pri-
 212 marily at low frequencies (Rothrock & Thorndike, 1980), whereas the surface gravity waves
 213 tend to have peak energy in the frequency range of 0.5 to 0.05 Hz, causing sea surface
 214 displacements with distinct spectra in that range. Calm waters and smooth ice both pro-
 215 duce flat (“white”) spectra. If both ice and waves are present, moorings measure a su-
 216 perposition of both signals.

217 The processing strategies for the mooring datasets make use of these different spec-
 218 tral shapes to identify and separate wave signals from sea ice. The postprocessed wave
 219 datasets from BGOS and SODA exclusively contain observations where the surface grav-
 220 ity wave signal is sufficiently strong to be considered a wave, determined by the spec-
 221 tral shape and the total energy in the frequency range of ocean surface waves. If the ice-
 222 draft signal is strong while the surface wave signal is weak, the instrument may be un-
 223 able to produce a valid wave measurement. These instances where only ice draft is de-
 224 tected are excluded from the wave datasets considered here. The resulting wave dataset
 225 almost exclusively contains observations with minimal ice draft detected; when the moor-
 226 ing is in partial ice cover, valid wave measurements appear to come from the water be-
 227 tween ice floes.

228 Separately, we include data from free-drifting surface buoys as a supplemental line
 229 of comparison. These measurements come from Surface Wave Instrument Floats with
 230 Tracking (SWIFTs) (Thomson, 2012) that were deployed for short periods of time dur-
 231 ing large wave events in the Oct-Nov 2015 Arctic Sea State campaign. The SWIFTs mea-
 232 sure ocean surface velocities and infer wave energy spectra every hour using GPS track-
 233 ing (Herbers et al., 2012). Because the SWIFTs do not sample data continuously over
 234 extended periods of time, we cannot use their results for statistical model evaluation. The
 235 surface buoy data from the SWIFTs nonetheless inform interpretation of both the model
 236 results and the BGOS-SODA observations.

237 3 Methods

238 A primary goal of this study is to objectively compare the in situ observations (lo-
 239 cated at specific points) and the model results (generalized over a region). We limit the
 240 model-observation comparison to the central Beaufort Sea region surrounding the ob-
 241 servations: latitudes 72°N to 79°N, longitudes 165°W to 130°W (Figure 1). Ideally, we
 242 would focus on model results from the particular grid cells that contain the location of
 243 each observation. However, even small errors in the model ice edge position and ice con-
 244 centration have substantial impacts on where waves occur in the ice, so we cannot ex-
 245 pect the coupled model to precisely replicate the observed waves at a given location. Rather,
 246 we assess whether the general character of waves in the region is accurately represented
 247 in the model.

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3.1 Distance Inside the Ice Edge

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To generalize the comparison, we group observations and model results based on a calculated distance from the ice edge, denoted as Δ^{dist} . Following convention, the ice edge is defined as the 15% ice concentration contour, roughly separating partial ice cover from open water. Δ^{dist} for a given location inside the ice cover is calculated purely from the ice concentration. The calculation is the Haversine distance to the nearest open water location, i.e., an ocean grid cell with SIC less than 15%. We note that the Δ^{dist} metric does not directly represent the distance along which wave attenuation occurs. The distance into the ice that a wave will travel before full dissipation depends on its direction of propagation, whereas this grouping by Δ^{dist} rather distinguishes locations based on their separation from open ocean. For simplicity, we show three Δ^{dist} groups: open water (SIC < 15%), 0-100 km inside the ice edge (equivalent to approximately two 50x50 km grid cells), and 100+ km inside the ice edge. We choose to group the data based on Δ^{dist} for three reasons:

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1. Waves attenuate exponentially with distance as they enter ice cover (Squire & Moore, 1980; Wadhams et al., 1988; Meylan et al., 2018).
2. Groupings based on Δ^{dist} reduce dependence on replicating the true ice-edge position in the model; this enables comparison between locations that are similar in the model and the in situ observations (based on their relative Δ^{dist}), rather than comparison between only the precise locations of the observations.
3. Specific estimates of ice concentration from passive microwave satellite data are highly uncertain in partial ice cover, but identification of the 15% concentration contour has higher confidence based on good agreement with ice-edge positions determined by aircraft (Cavalieri et al., 1991; Fetterer, 2002; Fetterer et al., 2017).

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We estimate the time-varying Δ^{dist} for each in situ observation using the NOAA/NSIDC Climate Data Record (CDR) of sea ice concentration, a daily satellite product derived from passive microwave observations (Fetterer et al., 2017). We regrid the satellite estimates from the native 25-km resolution to the model's nominal 1° resolution grid before computing Δ^{dist} , ensuring consistency between the model and observations. This produces a Δ^{dist} for each in situ observation and each model grid cell in the Beaufort Sea at all points in time.

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3.2 Nondimensional Scaling for Wind-Generated Ocean Waves

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To support interpretation of wave statistics, we employ nondimensional scaling relations for wind-generated waves following Young (1999). These relations enable separation of wind waves from swell and provide an estimate of the implied fetch for observed wind waves in partial ice cover. We calculate the following nondimensional variables for wave energy E , frequency F , and fetch distance X :

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$$E = \left(\frac{gH_s}{4U_{10}^2} \right)^2, \quad F = \frac{f_p U_{10}}{g}, \quad X = \frac{gx}{U_{10}^2}, \quad (1)$$

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where g is the gravitational acceleration; U_{10} is the 10-meter wind speed at the location of each in situ observation and model grid cell from JRA-55 reanalysis; H_s is the significant wave height, defined as 4σ where σ^2 is the variance of the sea-surface height; f_p is the peak frequency; and x is the fetch, i.e., the distance over which waves are generated by local winds. H_s and f_p are measured in situ and provided in model output. The fetch x is not measured but rather inferred for specific wind waves as described below; we refer to this variable as the implied fetch.

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In the marginal sea region of the observations considered, wave generation is generally limited by fetch rather than wind duration (Hasselmann et al., 1973; Thomson & Rogers, 2014). Several studies have developed empirical estimates of power laws for E

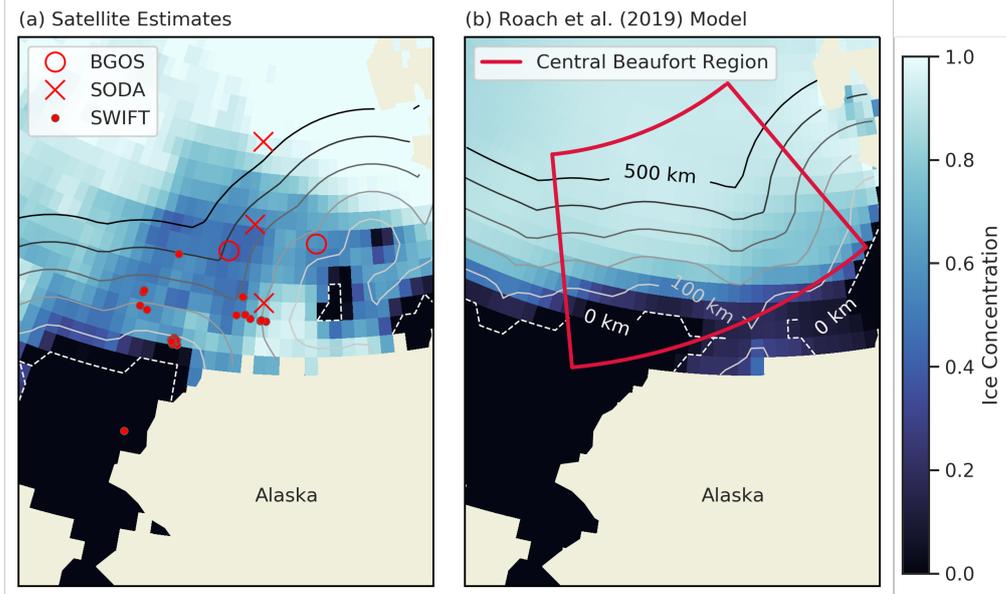


Figure 1. Sea ice concentration (color shading) and corresponding Δ^{dist} (contour lines every 100 km from 0-500 km) at a sample, illustrative date (23 July 2018). (a) Satellite estimates of concentration with locations of in situ observations (red symbols). (b) Results from Roach et al. (2019) model with region used for comparison with observations (red box). Note that the 0-km-distance contour simultaneously denotes 15% ice concentration.

296 vs. X and F vs. X that describe wind-generated waves in a fetch-limited regime. Young
 297 (1999) combined these estimates into the relations

$$298 \quad E = (7.5 \pm 2.0) \times 10^{-7} X^{0.8} \quad (2)$$

$$299 \quad F = (2.0 \pm 0.3) X^{-0.25}, \quad (3)$$

301 which apply at least until reaching a fully developed limit for pure wind seas at $E_{max} =$
 302 $(3.6 \pm 0.9) \times 10^{-3}$ and $F_{min} = 0.13 \pm 0.02$. Using equation (1), we reformulate these
 303 power laws in terms of the variables available from measurements and modeling, E and
 304 F :

$$305 \quad E = (6.9 \pm 3.8) \times 10^{-6} F^{-3.2}. \quad (4)$$

306 We identify waves that are accurately described by fetch-limited local wind gen-
 307 eration, i.e., wind waves, as those that fall within the uncertainty bounds of the line de-
 308 fined by the power law in equation (4). If a spectrum has less energy E than predicted
 309 by the wind-wave power law for a given frequency F , and it has a wave age greater than
 310 1, we determine that the spectrum represents swell, i.e., long-period waves produced by
 311 nonlocal winds.

312 Wave age $\frac{c}{U}$ is a nondimensional parameter defined by the ratio of the dominant
 313 phase speed c_p to the wind speed U_{10} , where we treat $c_p = \frac{g}{2\pi f_p}$ following the deep-water
 314 limit for surface gravity waves. When the wave age exceeds 1, waves travel faster than
 315 the winds. We note that wave age can be expressed in terms of F using equation (1) such
 316 that $\frac{c}{U} = (2\pi F)^{-1}$, and wave age is greater than 1 when F is less than $\frac{1}{2\pi}$.

317 Taking only the spectra that appear to be fetch-limited local wind waves, based
 318 on equation (4) and wave age as described above, we can calculate an implied fetch x

319 corresponding to each wind-wave spectrum. This dimensional variable x is recovered by
 320 solving for the nondimensional X in equation (2) based on the known energy E , then
 321 using equation (1) to restore the dimension. The implied fetch is an estimate of the open
 322 water distance that would be required for local winds to generate a given wind-wave spec-
 323 trum.

324 4 Results

325 4.1 Significant Wave Height

326 We compare the significant wave height H_s statistics by aggregating observations
 327 from the five BGOS and SODA moorings into a single dataset. Figure 2 shows the com-
 328 bined BGOS-SODA wave height distributions in open water ($\text{SIC} < 15\%$), 0-100 km Δ^{dist} ,
 329 and $\Delta^{\text{dist}} > 100$ km. The lower bound for H_s is set at 0.3 m for the aggregate dataset
 330 to account for detection limits that vary across instruments. Model results are similarly
 331 represented as a histogram by aggregating the 2012-2019 statistics from each grid cell
 332 in the Beaufort Sea region surrounding the observations.

333 The H_s distributions have similar shapes in open water (Figure 2a), but the model
 334 has more frequent large waves, with 18% of H_s greater than 2.0 m compared to 9% in
 335 observations. The observations show slightly greater probability for smaller waves be-
 336 tween 0.5 and 1.0 m. We note that sampling bias likely influences the open water com-
 337 parison given that we do not control for distance outside the ice edge, i.e., all open wa-
 338 ter results are in a single group. A detailed analysis of open water results, however, is
 339 outside the scope of this study.

340 We find more notable differences between the distributions in partial ice. The 0-
 341 100 km group (Figure 2b) displays a strong contrast, where the model's distribution is
 342 dominated by the smallest waves near the lower-limit of the domain, while observations
 343 show a higher prevalence of large waves. The model has only 13% of H_s greater than 1.0
 344 m, whereas 35% of observations exceed 1.0 m.

345 The 100+ km Δ^{dist} distributions differ most strongly in terms of kurtosis (Figure
 346 2c). The model has a prominent peak at the smallest end of wave heights, paired with
 347 a thicker tail of large waves. 9% of the model's H_s exceed 1.0 m, whereas the 104 ob-
 348 servations at 100+ km do not report any H_s beyond that magnitude. Only 5% of ob-
 349 served H_s exceed 0.75 m, and the distribution is relatively uniform between 0.30 and 0.75
 350 m. We discuss how sampling biases could affect this model-observation comparison in
 351 discussion section 5.2 below, but we emphasize here that the absence of H_s beyond 1.0
 352 m in BGOS-SODA observations cannot be attributed to instrument errors. Such large
 353 wave heights exceed minimum wave height detection limits by significant margins and
 354 are reported in open water and at 0-100 km Δ^{dist} . The absence of H_s greater than 1.0
 355 m in the BGOS-SODA observations of Figure 2c is a robust result within the limit of
 356 our sample size. To provide some insight on differences in the distributions, we turn to
 357 the spectra.

358 4.2 Wave Spectra

359 Even if the bulk wave parameter H_s appears accurately represented, the model can
 360 have significant biases in how wave energy is distributed between low and high frequen-
 361 cies. Inspecting the full wave spectra reveals that similar H_s may have dramatically dif-
 362 ferent signatures in frequency space, and these model-observations differences can high-
 363 light disagreement in wave attenuation and generation processes. Additionally, we in-
 364 troduce spectra from the SWIFT surface buoys as a supplemental line of comparison,
 365 recalling that SWIFTs preferentially sample significant wave events as part of experi-
 366 ment design.

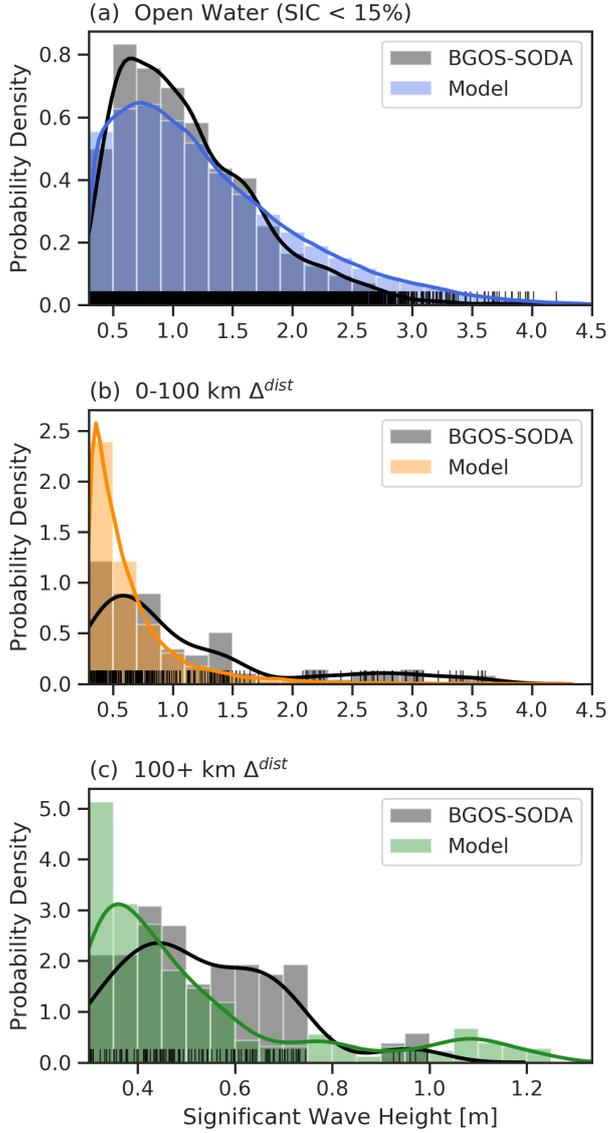


Figure 2. Histograms and density curves for significant wave height H_s distributions in (a) open water (sea ice concentration $< 15\%$), (b) 0-100 km Δ^{dist} , and (c) 100+ km Δ^{dist} , spanning 2012-2019 in the Beaufort Sea. In situ observations (black) are aggregated from two BGOS and three SODA moorings, and rug plots of vertical black lines along the x-axes denote exact values of individual observations. Model results (colors) are from the Roach et al. (2019) model, restricted to the Beaufort region surrounding observations. The lower bound on the domain for H_s is set at 0.3 m, limiting the results to those exceeding the detection limit for all moorings considered. Note the different x-axis scale in panel (c).

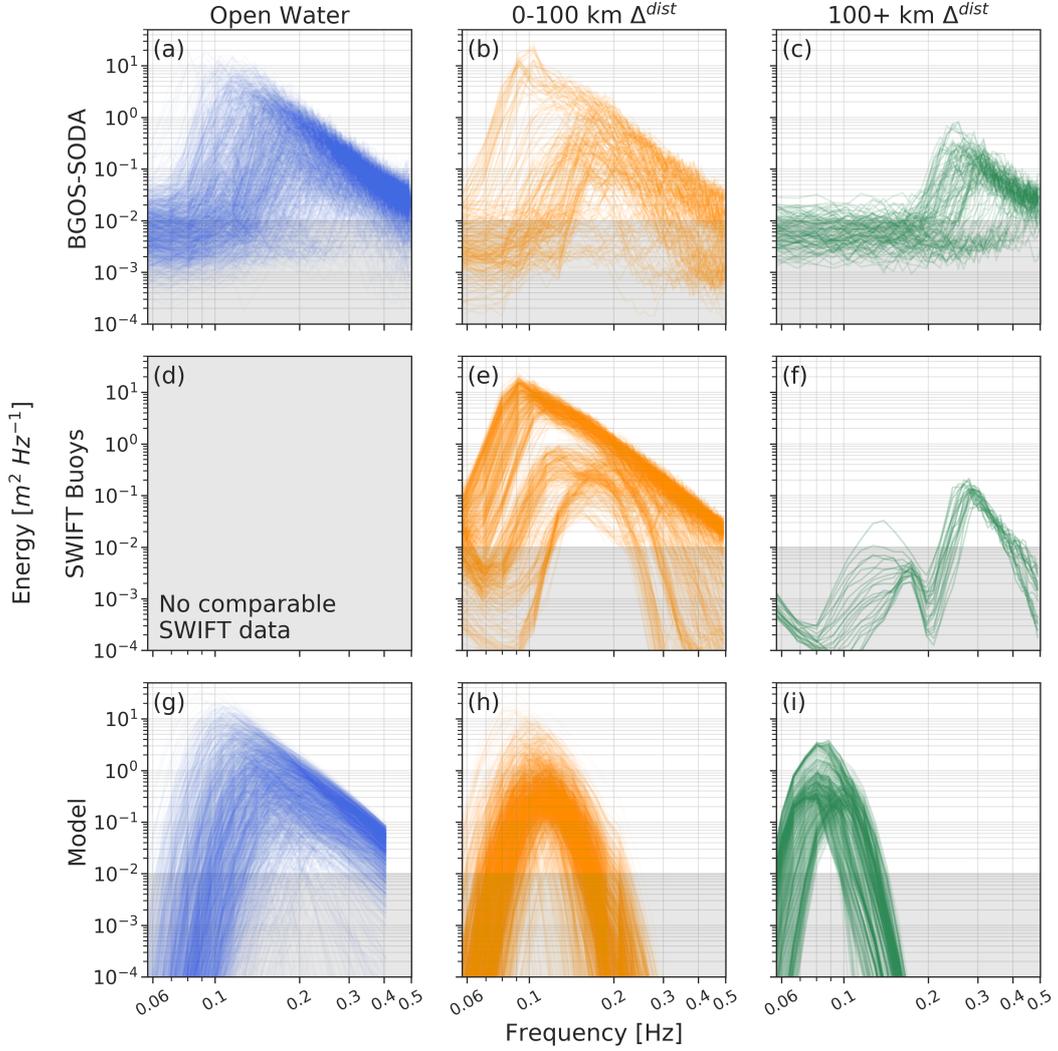


Figure 3. Ocean surface wave spectra grouped by distance inside the ice edge (Δ^{dist}). Top row (a)-(c): BGOS-SODA mooring observations. Middle row (d)-(f): SWIFT surface buoys. Bottom row (g)-(i): Roach et al. (2019) model results from grid cells in central Beaufort region surrounding observations. Open water (SIC < 15%) in left column, 0-100 km Δ^{dist} in center column, and 100+ km Δ^{dist} in right column. Only spectra with H_s greater than 0.3 m are shown. Gray shading represents the approximate BGOS-SODA detection limit and is included on all panels for ease of comparison.

367 The open water (SIC < 15%) spectra are generally in agreement between the moor-
 368 ings and the model (Figure 3a,g). We can identify the prominent spectral shape of lo-
 369 cally developed wind waves in open water in both panels. These spectra exemplify a char-
 370 acteristic power-law relationship between energy and frequency (different from the nondimensional-
 371 scaling power law described in section 3.2) in the high-frequency spectral tail, i.e., the
 372 portion of the spectrum where frequency f is higher than the peak frequency f_p . In open
 373 water, the spectral tail follows a consistent f^{-4} slope down from f_p (Phillips, 1985; Thom-
 374 son et al., 2013; Lenain & Melville, 2017).

375 In sea ice, the spectral tail is typically steeper than f^{-4} in observations and model
 376 results. This steeper tail has been reported in observations before (Rogers et al., 2016;
 377 Thomson et al., 2021) and is consistent with the notion that sea ice dissipates high-frequency
 378 energy most effectively. Data from the 0-100 km transition into ice, illustrated most clearly
 379 by the fan of spectral tails in the SWIFT spectra (Figure 3e) but also visible in the moor-
 380 ings (Figure 3b), demonstrates that waves undergo a frequency-dependent attenuation
 381 while traveling through partial ice and preferentially lose energy at the highest frequen-
 382 cies. The model does not show the same spread of spectral-tail slopes seen in observa-
 383 tions, even in the first 0-100 km of partial ice (Figure 3h); all energy at high frequen-
 384 cies has been eliminated. A spectral shape similar to the model results, however, can be
 385 seen in some observed spectra at 0-100 km (Figure 3b,e), albeit shifted so that f_p tends
 386 to be at slightly higher frequencies in observations.

387 Moving to 100+ km Δ^{dist} , we see a structural difference between the spectra in the
 388 model and those in the observations. In Figure 3i, the model shows waves retaining sig-
 389 nificant low-frequency energy far into the ice, and all of these model spectra are devoid
 390 of any high-frequency energy. On the other hand, the BGOS-SODA observations (Fig-
 391 ure 3c) have a spectral signature that is, perhaps surprisingly, reminiscent of a short-wave
 392 subset of the open water spectra. These spectral tails follow the f^{-4} slope, and all en-
 393 ergy is at relatively high frequencies. The contrast between the model's low-frequency
 394 energy and the BGOS-SODA high-frequency waves suggests that there are two separate
 395 modes displayed in the spectra at 100+ km Δ^{dist} . The SWIFTs in Figure 3f show bi-
 396 modal spectra that appear to have a swell wave group at lower frequencies concurrent
 397 with a local-wind-wave group at higher frequencies. Notably, the swell group in these
 398 bimodal spectra has higher f_p and less energy compared to the model results in Figure
 399 3i, and energy is mostly below the BGOS-SODA detection limit.

400 4.3 Fetch Scaling

401 We find that the distinction between swell and wind waves generally can be reduced
 402 to the nondimensional scaling of two bulk wave parameters, H_s and f_p , rather than re-
 403 quiring inspection of the full spectra. Whereas the H_s distributions in Figure 2 compare
 404 amounts of wave energy, the distributions in Figure 4 compare how the swell and wind-
 405 wave modes are represented. Figure 4 applies the nondimensional scaling relations be-
 406 tween energy and peak frequency to observations and the model, and it also includes the
 407 power law for local wind-wave generation (see section 3.2). The points that follow the
 408 power law are identified as locally generated wind waves, while points located below the
 409 line, i.e., those with less energy than predicted by the power law for a given peak fre-
 410 quency, and with wave age greater than 1 are identified as swell. These modes are not
 411 always well-separated because nonlocal swell and local wave generation can co-occur.

412 The power law captures most of the open water (Figure 4a) observations and model
 413 output, but a nonlocal component can be identified in both the model and observations
 414 that pulls some of the points below the power-law line and towards low F such that the
 415 wave age is greater than 1. This consistency between the model and observations sug-
 416 gests that there is not a significant bias in the prevailing wave modes in open water.

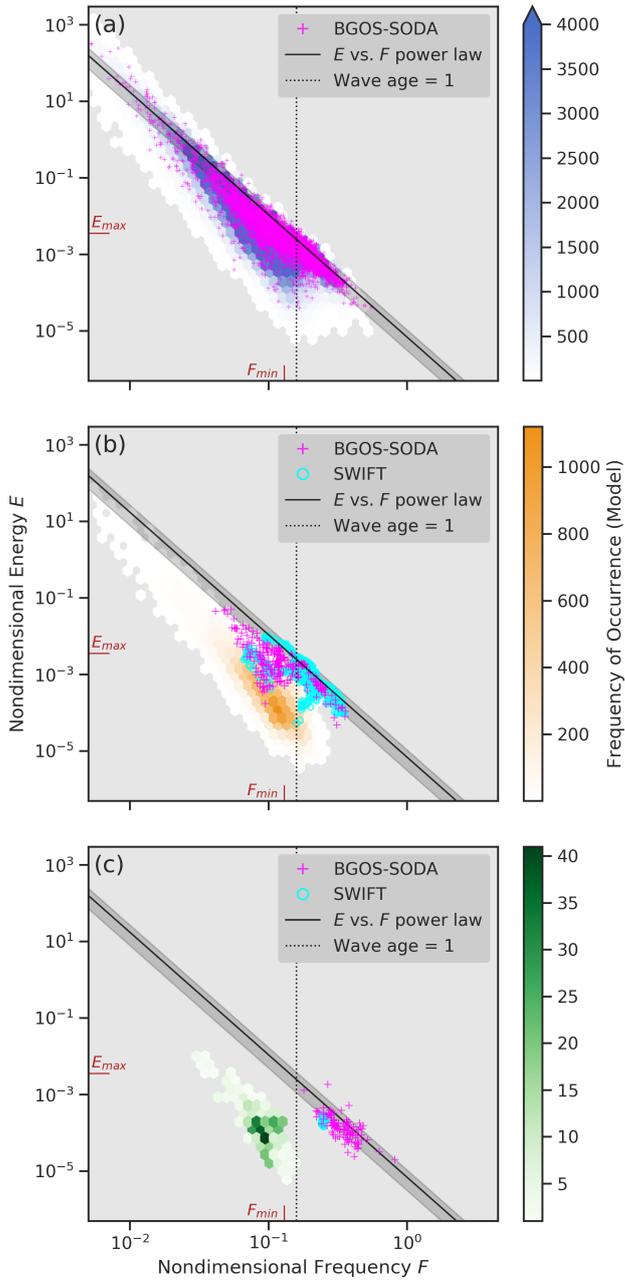


Figure 4. Nondimensional scaling of wave energy vs. peak frequency grouped by distance inside the ice edge (Δ^{dist}). Observations shown as scatter plots (BGOS and SODA moorings as + symbols; SWIFT surface buoys as O symbols). Roach et al. (2019) model results from central Beaufort region surrounding observations shown as 2-d histograms (color shading), where the hourly mean at each model grid cell is a separate data point. (a) Open water (SIC < 15%), (b) 0-100 km Δ^{dist} , and (c) 100+ km Δ^{dist} . Only results with $H_s > 0.3$ m are shown. Power law (black line) with confidence intervals (shading) of E vs. F for wind-generated, fetch-limited waves, with the fully developed limit (E_{max} and F_{min}) for pure wind seas denoted in red (Young, 1999). Dashed line at $F = (2\pi)^{-1}$ indicates wave age = 1; where $F < (2\pi)^{-1}$, wave age > 1.

417 In partial ice, the results for the model become distinct from the observations. At
 418 0-100 km Δ^{dist} (Figure 4b), the model immediately clusters at lower energies away from
 419 the power law, i.e., the swell mode dominates. In observations at 0-100 km, we see a spread
 420 both on and off the power-law relation. Recall that this spread, due to the combined pres-
 421 ence of swell, local wind waves, and attenuation by the ice cover, can be seen in the moor-
 422 ing and SWIFT spectra (Figures 3b,e).

423 At 100+ km Δ^{dist} , separation between the model and the observations is most def-
 424 inite (Figure 4c). The model displays only the swell mode of lower energies with wave
 425 age greater than 1 and is removed from the wind-wave power law even more strongly than
 426 in the 0-100 km zone. The observations behave differently; they do not continue spread-
 427 ing away from the power law toward lower energies as seen in their 0-100 km subset. In-
 428 stead, they return to clustering along the power law, indicating local wind-wave gener-
 429 ation at 100+ km Δ^{dist} . The observations thus suggest that local wave generation is a
 430 significant source of wave activity far within the marginal ice zone, and this source is not
 431 captured in the model.

432 5 Discussion

433 While the coupled wave-ice model of Roach et al. (2019) broadly captures the range
 434 of significant wave heights in BGOS-SODA observations, comparing the shapes of the
 435 H_s distributions suggests there may be substantial differences which are not apparent
 436 when considering the bulk parameter for wave energy alone. The spectral details are im-
 437 portant given the frequency dependence of wave attenuation and floe fracture. Two key
 438 questions emerge from the spectra and nondimensional scaling at 100+ km Δ^{dist} : why
 439 do BGOS-SODA observations show wind waves but no swell, and why does the model
 440 show swell but no wind waves?

441 5.1 Wind Waves

442 Sea ice is known to filter out high-frequency wave energy, but BGOS-SODA ob-
 443 servations nevertheless reveal a prevalence of high-frequency wind waves at 100+ km Δ^{dist}
 444 (Figure 4c). A possible explanation is that local generation of wind waves, perhaps in
 445 leads or the open water areas between sparse ice floes, occurs at significant distances in-
 446 side the MIZ. In Figure 5, we calculate the implied fetch for each wind-wave spectrum
 447 in BGOS-SODA observations according to the scaling relations (as described in section
 448 3.2). All observed wind waves at 100+ km Δ^{dist} could be generated by winds blowing
 449 over open water distances estimated to be less than 50 km.

450 Wind waves in ice are absent in model results for the central Beaufort due to mul-
 451 tiple potential factors. First, the short implied fetch of the observed wind waves reveals
 452 that they are a sub-grid-scale process. The distance across the model grid cells, which
 453 are approximately 50 by 50 km in this region, is longer than the implied fetch for all ob-
 454 served wind waves at 100+ km Δ^{dist} (Figure 5). These short waves are sensitive to model
 455 parameters that control sub-grid-scale wave generation in partial ice.

456 Additionally, the model is biased high for intermediate ice concentrations (Figure
 457 6), i.e., the 15-80% concentration range, at 100+ km Δ^{dist} during the summer melt sea-
 458 son when wind waves in ice occur in observations (Figure S2). We focus on bias in the
 459 15-80% intermediate concentration range conventionally considered part of the MIZ. We
 460 exclude compact pack ice (SIC > 80%) because the large number of compact pack ice
 461 grid cells dominates the distribution. For the intermediate-concentration subset of grid
 462 cells, satellite estimates indicate a greater proportion of low ice concentrations compared
 463 to the model (also see Figure 1 for an illustrative example). Because wind-wave gener-
 464 ation in Wavewatch III is scaled by a coefficient equal to the local open water fraction,
 465 the bias toward high ice concentrations excessively inhibits local wave generation at 100+

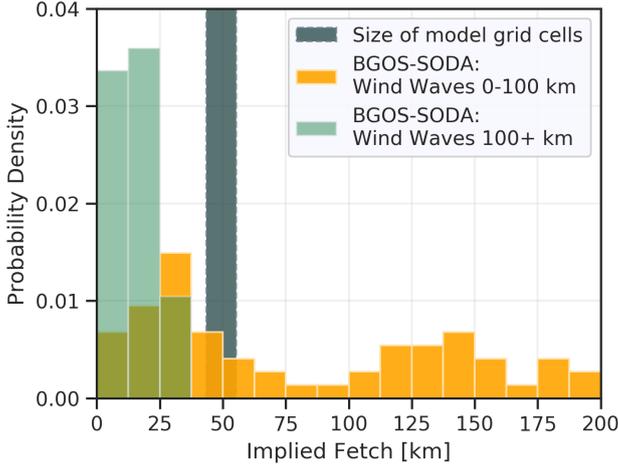


Figure 5. Histograms of implied fetch for locally generated wind waves from BGOS and SODA mooring observations. Observations located 0-100 km Δ^{dist} (orange) and 100+ km Δ^{dist} (green). Size range of Roach et al. (2019) model grid cells (approximately 50x50 km) in the vicinity of observations shown as dark shading with dashed border.

466 km Δ^{dist} . We note that the lack of local wave generation could be partially responsible
 467 for the high concentration bias, just as the high concentrations are potentially respon-
 468 sible for suppressing wave generation.

469 Wind bias in the model could also be partially responsible. However, model winds
 470 come from atmospheric reanalysis. We believe error in the reanalysis is not a likely ex-
 471 planation, although we note that reanalysis does not always capture wind events in the
 472 MIZ (e.g., Brenner et al., 2020).

473 Are these high-frequency wind waves important for modeling wave-ice interactions?
 474 In the Roach et al. (2019) model, waves can impact the FSD via floe fracture, described
 475 using the sub-grid-scale parameterization developed by Horvat and Tziperman (2015).
 476 To test the importance of the observed high-frequency wind waves for floe fracture, we
 477 input the median, 75th percentile, and maximum wave spectra, ranked by H_s , from BGOS-
 478 SODA observations at 100+ km Δ^{dist} to the Horvat and Tziperman (2015) parameter-
 479 ization (computed offline). This parameterization generates realizations of the sea sur-
 480 face height using the ocean surface wave spectrum and computes the strain applied to
 481 sea ice floes. A statistical distribution of resulting fractured floe sizes is constructed by
 482 computing the distances where the strain field exceeds a critical value. Figure 7a shows
 483 the resulting floe size distributions that would be formed by the observed wave spectra
 484 in Figure 7c with a representative ice thickness of 0.5 m.

485 These results suggest that the locally generated waves at 100+ km Δ^{dist} tend to
 486 be strong enough to fracture sea ice: the median H_s spectrum reduces 71% of the ice
 487 area to floes with radius less than 15 m. Steele (1992) found that, for floes with radius
 488 less than 15 m, lateral melt plays a critical role in Arctic summer conditions, which is
 489 when these waves appear in observations (Figure S2). Smaller floes make the dominant
 490 contribution to cumulative floe perimeter, so short wind waves in ice appear to enhance
 491 the lateral melt potential of ice floes and should be a priority for future wave-ice model
 492 development.

493 Note that we cannot expect model spectra to be identical to the observed spectra
 494 in partial ice because the model also represents all of the surface area where waves are

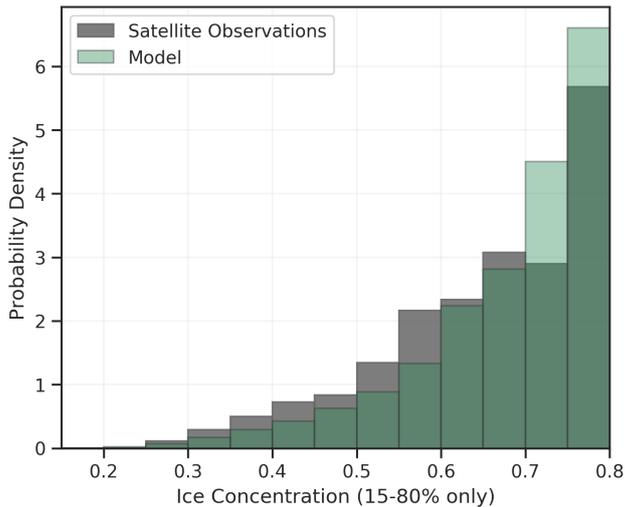


Figure 6. Histograms of intermediate (15-80%) sea ice concentrations during summer melt season (Jun-Jul-Aug) for grid cells located 100+ km Δ^{dist} , spanning 2012-2019 in the central Beaufort region surrounding the in situ observations. Satellite estimates (black) are from the NOAA/NSIDC Climate Data Record, and model results (green) are from the Roach et al. (2019) model.

495 damped by ice floes. A model grid cell aims to capture mean wave statistics over a par-
 496 tial ice region, but the in situ observations shown here appear to capture wave spectra
 497 from open water points between floes (see section 2.2 and the discussion that follows in
 498 section 5.2). We speculate that reconciling the model-observations difference in high-frequency
 499 energy does not require that model spectra become identical to those from the BGOS-
 500 SODA observations at 100+ km Δ^{dist} . However, the complete absence of high-frequency
 501 energy in the model spectra is striking and demands attention.

502 5.2 Swell

503 Now, we will address why BGOS-SODA observations do not show any swell at 100+
 504 km Δ^{dist} while the model does. Generally, the low-frequency energy of swell experiences
 505 less dissipation than high-frequency energy during travel through partial ice cover. We
 506 anticipated that observations far inside the ice edge would preferentially show wave en-
 507 ergy at low frequencies, similar to what we see in the model results. While large swells
 508 are relatively rare, for now, in the central Beaufort even in open water (Thomson & Rogers,
 509 2014), the absence of low-frequency energy in BGOS-SODA observations from 100+ km
 510 Δ^{dist} , given its presence at 0-100 km, is conspicuous. In this section, we first consider
 511 why BGOS-SODA might not show any swell at 100+ km Δ^{dist} .

512 Could the BGOS-SODA data processing exclude swell spectra because those spectra
 513 also have a sea ice signal from under-ice topography? Recall that the subsurface BGOS-
 514 SODA measurements can represent a superposition of both ocean surface waves and sea
 515 ice draft, which each have distinct spectral shapes (see section 2.2). When sea ice is present
 516 above the moorings, the processing of the altimeter-based measurements may fail to re-
 517 cognize waves due to the additional signal from the ice. Therefore, the lack of swell spec-
 518 tra with H_s greater than 0.3 m at 100 km+ Δ^{dist} in the BGOS-SODA observations could
 519 be partly a result of sampling bias if the swell is always coincident with a strong signal
 520 from ice. We first test this possibility by manually inspecting individual spectra in the
 521 original SODA records. We are able to find some measurements that have been excluded

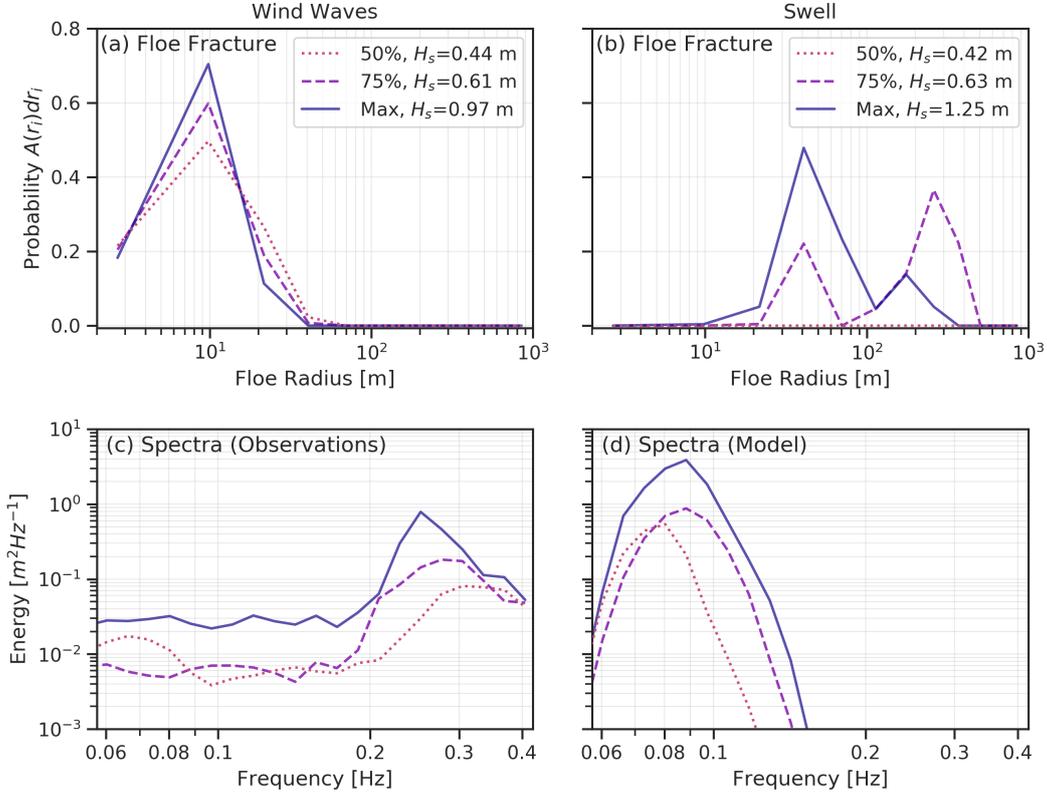


Figure 7. (a)-(b) Histograms of predicted floe-size distributions resulting from corresponding wave spectra in (c)-(d), respectively, present at 100+ km Δ^{dist} , based on the Horvat and Tziperman (2015) parametrization and assuming ice thickness of 0.5 m. Floe sizes in (a)-(b) are binned into probability distributions $A(r)$ where $A(r)dr$ is the fraction of ice area with floe radius between r and $r + dr$. Plots show the probability $A(r_i)dr_i$ at each of the following bin centers i : 3, 10, 22, 41, 70, 114, 176, 260, 370, 506, 668, and 850 m. Wave spectra represent the approximate median (50th percentile), 75th percentile, and maximum based on H_s from (c) wind waves in BGOS-SODA observations and (d) swell in the Roach et al. (2019) model results, excluding spectra with H_s less than 0.3 m. Spectra in (c) have been interpolated to the frequency domain resolved in the Roach et al. (2019) model. Note that the 50th percentile swell spectra in (d) does not cause any floe fracture and appears as a zero line in (b).

522 by data processing from the wave dataset considered in this study and which have spec-
 523 tral shapes suggesting a combination of both sea ice and swell. However, the H_s of the
 524 apparent swell in these spectra are less than 0.3 m, and the waves generally occur out-
 525 side of the 100+ km Δ^{dist} range. While this manual inspection method is not exhaus-
 526 tive, it suggests there are no pervasive issues in the processing causing swell to be omit-
 527 ted from the data.

528 Could some swell be entirely hidden by the sea ice signal? If this were the case, the
 529 swell signal would be so much weaker relative to the ice signal that it would not emerge
 530 from underneath the ice’s red spectrum, i.e., the swell would have no detectable spec-
 531 tral signature. Reprocessing of all individual spectra (including when no waves are ap-
 532 parent) allows us to set an upper bound on the H_s of swell that may be hidden from ob-
 533 servation based on the spectrum that is measured, which also includes the ice signal. The
 534 upper bound is determined by integrating the spectra over a frequency band associated
 535 with swell; the true H_s of any hidden swell in this band must be much less than the ap-
 536 parent H_s , i.e., the upper bound, due to how the swell spectral shape compares to a mea-
 537 sured red spectrum. If we choose a narrow swell band of 0.08-0.125 Hz based on the peak
 538 frequencies of swell in the model results, we find that 6% of the 10,283 SODA measure-
 539 ments that appear to be ice spectra exceed an H_s upper bound of 0.3 m, correspond-
 540 ing to the minimum H_s used throughout the analysis. It is possible that some nontriv-
 541 ial swell could exist hidden in these ice spectra, but we do not find any further evidence
 542 of swell with H_s greater than 0.3 m in this band.

543 We also note that the absence of swell at 100+ km Δ^{dist} is supported by spectra
 544 constructed from the moorings’ pressure data (not shown). These represent independent
 545 estimates of wave signals using a separate instrument on the moorings. The pressure spec-
 546 tra from under ice also do not report H_s greater than the 0.3 m cutoff. A noteworthy
 547 supporting example comes from the 11 Oct 2015 event analyzed in Thomson et al. (2019)
 548 (see their Figure 2), which shows a swell spectrum from BGOS-A pressure data while
 549 the mooring was under ice near a major storm. In that case, the BGOS-A H_s is less than
 550 0.1 m.

551 We conclude that the 100+ km Δ^{dist} BGOS-SODA observations do not display any
 552 swell spectra because any swell that reached the moorings must have been too small to
 553 emerge with a sufficient signal. Perhaps the swell that evaded detection by the moor-
 554 ings resembles the swell (lower frequency) wave group in the bimodal SWIFT spectra
 555 (Figure 3f), which has energy mostly below the moorings’ detection limits. Based on the
 556 recent wave climate near these moorings, large swells penetrating beyond 100 km Δ^{dist}
 557 in the Beaufort Sea are rare enough that they do not appear in this aggregate dataset.

558 The model output at 100+ km Δ^{dist} (Figures 2c, 3i, 4c) includes a number of waves
 559 exceeding the BGOS-SODA detection limit of 0.3 m H_s , with maximum H_s in the model
 560 reaching 1.25 m. Given that we do not see any evidence in BGOS-SODA of swells that
 561 approach the size of those in the model, this appears to suggest that the model overes-
 562 timates the persistence of swell in ice, at least in the Beaufort Sea. The model’s excess
 563 swell could be attributable to an open water bias that lingers as swell enters the ice, rather
 564 than the wave attenuation rate. If incident waves have energy at too-low frequencies in
 565 open water, the swell could survive at greater distances inside the MIZ. Comparison of
 566 the open water peak-frequency distributions, limited to the ice-growth season when swell
 567 is most often present in the model at 100+ km Δ^{dist} (Figure S3a), does not indicate any
 568 clear model bias toward low peak frequencies. However, there is an apparent bias of larger
 569 H_s that could sustain the swell if that bias were present in the subset of waves that prop-
 570 agate into the MIZ. These explanations for the model swell are speculative, and more
 571 data is needed to support further investigation.

572 Finally, we consider whether the excess swell has a significant impact on floe size.
 573 Unlike the high-frequency wind waves, which efficiently reduce floes to small sizes, the

574 low-frequency swell has a less drastic effect. We repeat the floe-fracture test from the
 575 wind-wave discussion in section 5.1, now for swell from the model spectra at 100+ km
 576 Δ^{dist} using the Horvat and Tziperman (2015) parameterization (Figure 7b). This pa-
 577 rameterization suggests that even the biased-high swell in the model fractures floes pre-
 578 dominantly into large radius categories, with less than 1% of the ice area reduced to floe
 579 radius less than 15 m even for the maximum H_s . In the case of the median H_s , the swell
 580 does not cause any floe fracture. Moreover, the swell tends to occur in months of freez-
 581 ing conditions while new ice is forming and the ice edge is moving southward rather than
 582 melting and retreating (Figure S2). Overestimation of swell in the model is still a con-
 583 cern, but it appears less consequential for floe fracture and ice melt compared to the wind
 584 waves.

585 6 Conclusions

586 We investigate differences between the Roach et al. (2019) coupled wave-ice model
 587 and an aggregated dataset of recent in situ observations of waves in pack ice from the
 588 central Beaufort Sea. We group the data and model output by distance inside the ice
 589 edge, denoted Δ^{dist} , to enable a statistical comparison. The distributions of significant
 590 wave height are similar in open water but have more notable differences in sea ice. The
 591 model tends to have smaller H_s than observations in the first 0-100 km of pack ice and
 592 greater kurtosis compared to observations beyond 100 km Δ^{dist} .

593 The wave spectra and nondimensional scaling of energy and frequency illuminate
 594 different prevailing modes of waves at 100+ km Δ^{dist} between the model and observa-
 595 tions. We find that observations show significant generation of local wind waves during
 596 the ice-melt season at 100+ km Δ^{dist} . The model lacks the resolution to generate the
 597 high-frequency wind waves that might arise if leads or open water areas between sparse
 598 ice floes were resolved explicitly rather than parameterized based on the sea ice concen-
 599 tration within a grid cell, which is the scheme currently implemented in Wavewatch III.
 600 These wind waves appear to cause substantial floe fracture and enhance lateral melt po-
 601 tential. Therefore, resolving or improving the parameterization of local wind-wave gen-
 602 eration in the MIZ should be considered a priority in future model development.

603 On the other hand, the swell mode appears only in the model at 100+ km Δ^{dist} ,
 604 not in the BGOS-SODA observations. Low-frequency energy appears to be overstated
 605 in the model at 100+ km Δ^{dist} . This swell in the model appears predominantly during
 606 the ice-growth season and has a relatively minor impact on floe fracture and melt po-
 607 tential compared to the wind waves.

608 The comparisons with observations in this study reveal important areas of devel-
 609 opment for modeling interactions between waves and sea ice. Combining multiple wave
 610 datasets to form a relatively large sample is an effective approach for model evaluation
 611 and could be replicated in other regions. However, we need more robust observations of
 612 wave spectra in sea ice across seasons at basin scale. These observations would enable
 613 stronger constraints on the physics of wave attenuation and generation in the MIZ which
 614 are critical to model development and theoretical understanding.

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 619 Ocean Sciences, and the BGOS datasets used in this study are available at digital.lib.washington.edu/researchworks/
 620 SWIFT buoy data were collected and made available by the Arctic Sea State program
 621 and can be found at www.apl.uw.edu/swift. SODA data is available at digital.lib.washington.edu/researchworks/
 622 NOAA/NSIDC Climate Data Record estimates of sea ice concentration from passive mi-

623 crowdave satellite observations are available at nsidc.org/data/G02202. Model output used
 624 in this study is publicly available via Zenodo at <https://doi.org/10.5281/zenodo.5545098>.
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Supporting Information for “Evaluation of a Coupled Wave-Ice Model in the Western Arctic”

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Contents of this file

1. Figures S1 to S3

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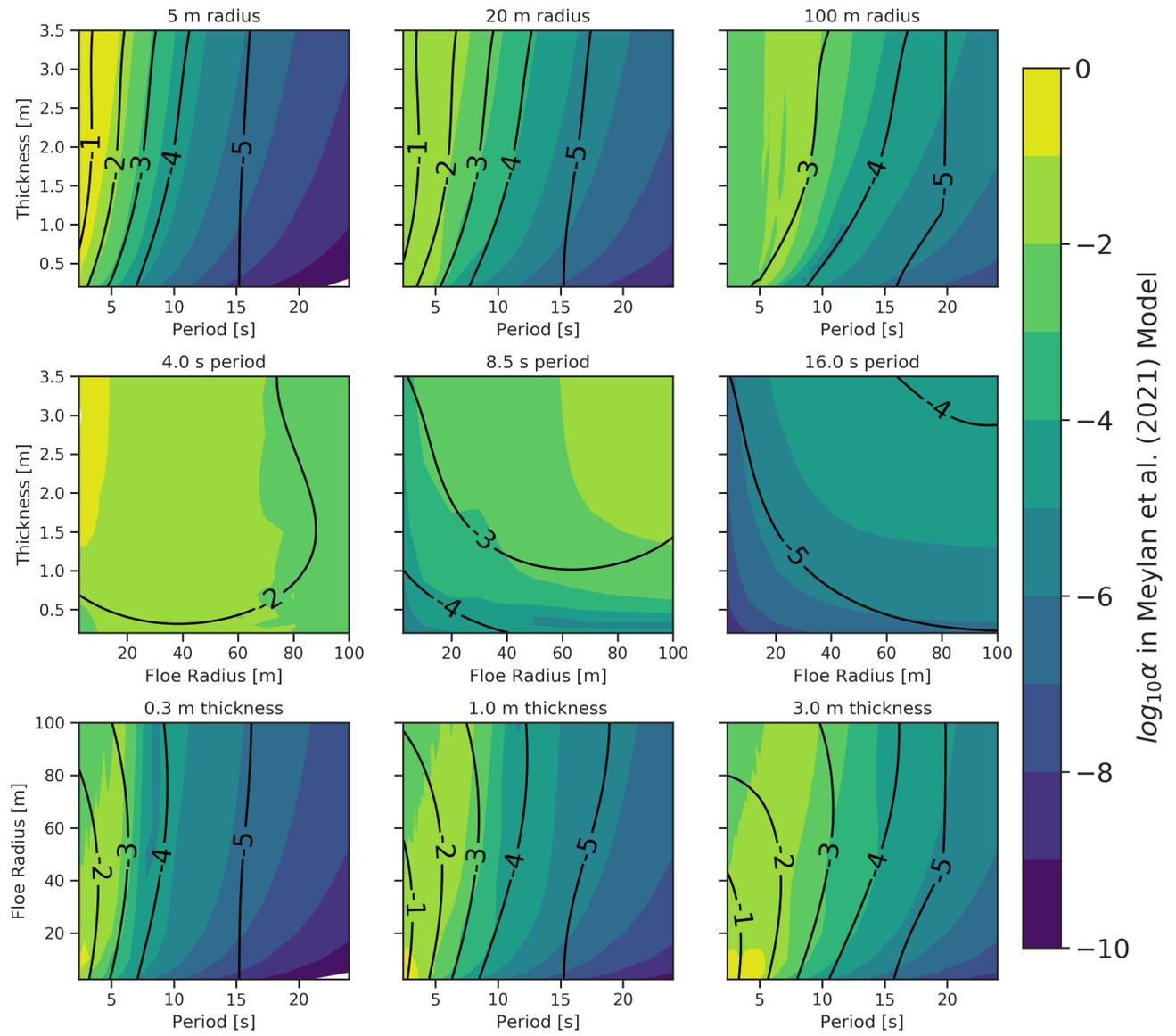


Figure S1. See caption on following page.

Figure S1. Illustrative frequency-dependent wave attenuation coefficients based on varying floe size, ice thickness, and wave period applied in the Roach et al. (2019) model (black contours). Computing S_{ice} , the source term for wave-ice interactions, involves multiplying the wave spectral energy by a wave attenuation coefficient α , which represents the exponential rate of attenuation over distance travelled in ice (see Meylan et al. (2021) for full discussion). When α is relatively large, the ice causes strong attenuation. Contour labels and color contours indicate $\log_{10}\alpha$; the zero contour represents maximum attenuation while negative values represent weaker attenuation. Top row shows attenuation coefficients for fixed floe sizes, middle row for fixed wave periods, and bottom row for fixed ice thickness values. Scattering model from Meylan et al. (2021) shown as color-shading contours. Attenuation rates from the Roach et al. (2019) model are shown as black contour lines with labels. In Roach et al. (2019), a cubic polynomial fit to the Meylan et al. (2021) scattering model is used to approximate the scattering component of wave attenuation. Total attenuation in the Roach et al. (2019) model comes not only from the fit to the scattering model but also from an additional contribution for relatively long periods based on measurements reported in Meylan et al. (2014). This additional contribution based on the wave period T is $\alpha = c_1 T^{-2} + c_2 T^{-4}$, where $c_1 = 2.12 \times 10^{-3} \text{ s}^2\text{m}^{-1}$ and $c_2 = 4.59 \times 10^{-2} \text{ s}^4\text{m}^{-1}$. In Roach et al. (2019), for periods less than 5 s, α is purely based on the fit to the scattering model. For periods between 5 and 20 s, α is the sum of the fit to the scattering model and the additional contribution from the period T . Beyond 20 s, α is entirely determined by the T terms.

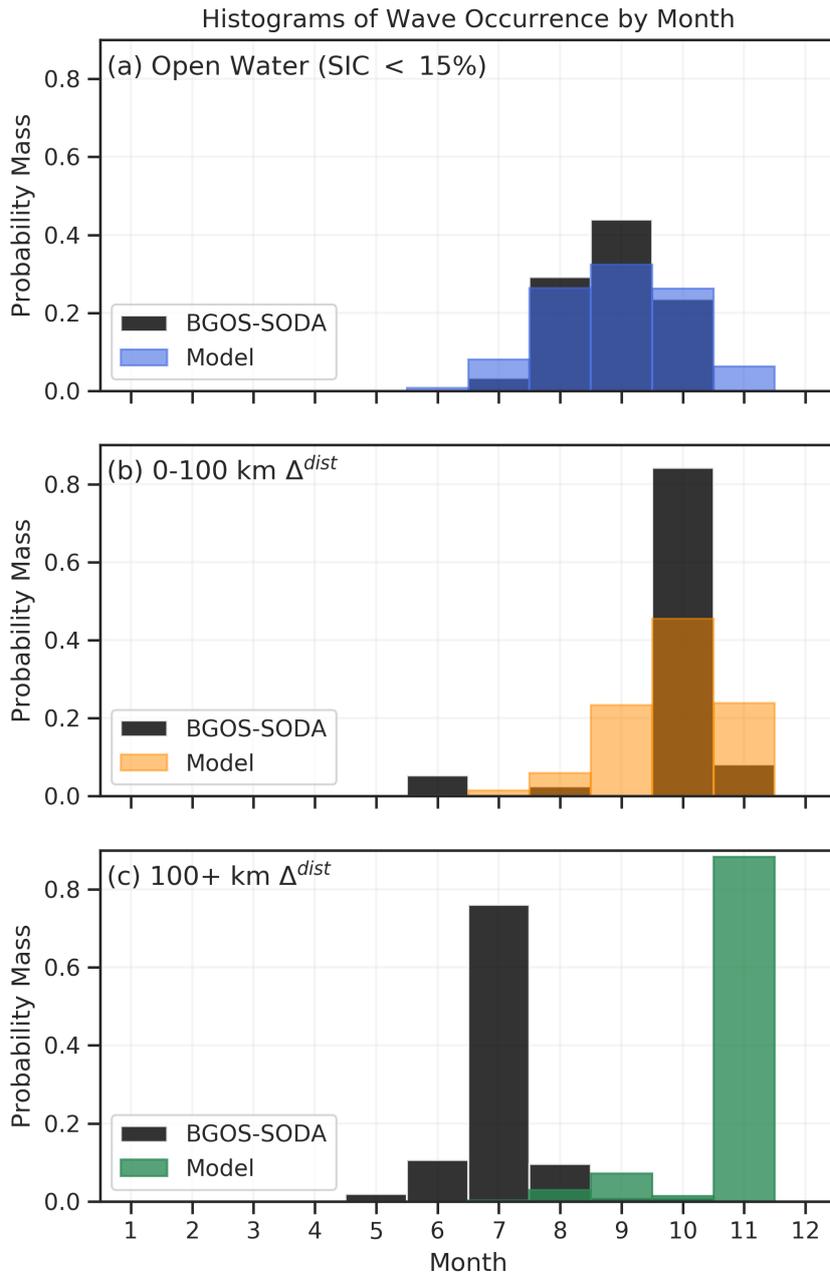


Figure S2. Histogram of wave occurrence by month for significant wave height > 0.3 m, spanning 2012-2019 and grouped by Δ^{dist} . Observations (black) represent combined BGOS and SODA datasets. Model (colors) represents results from Roach et al. (2019), aggregating grid cells in the central Beaufort region surrounding observations.

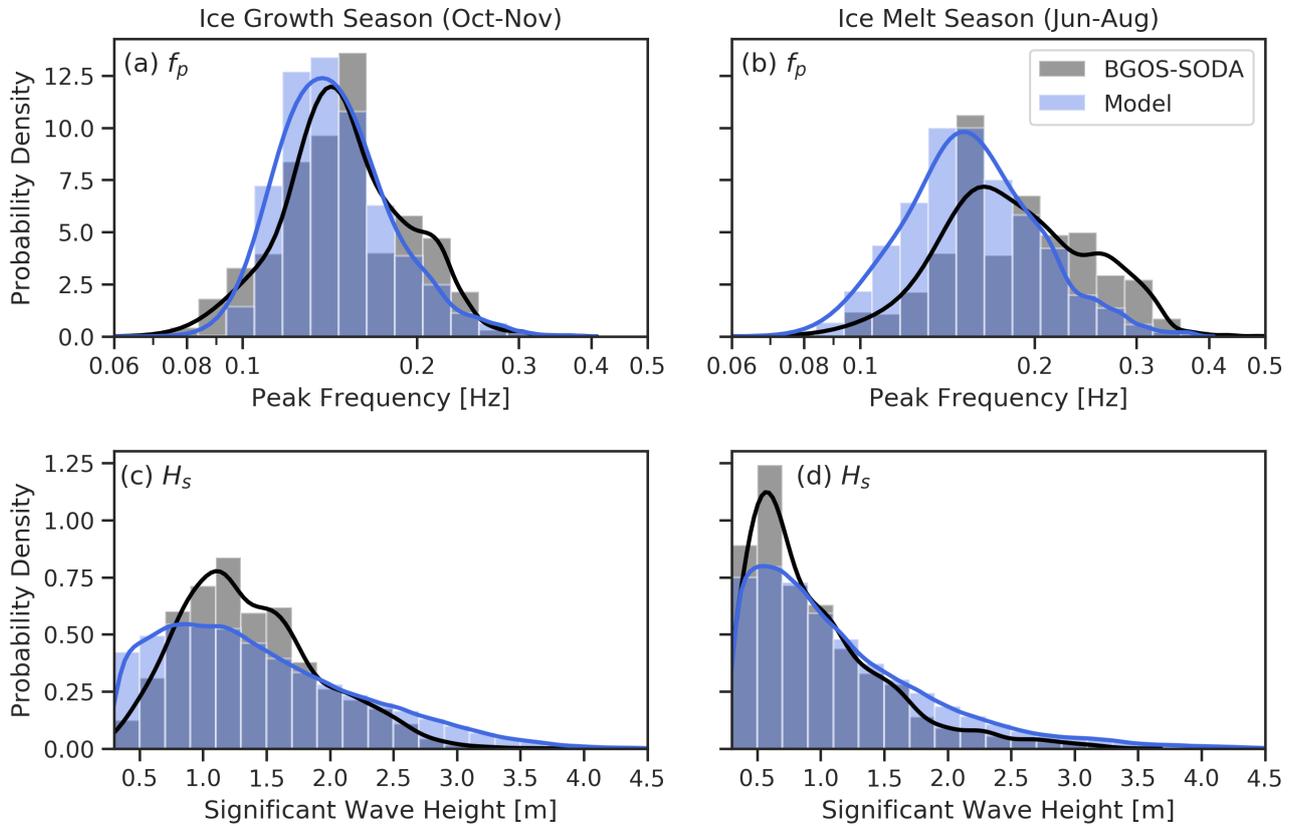


Figure S3. Histogram of (top row) peak frequency and (bottom row) significant wave height for spectra with $H_s > 0.3$ m in open water (SIC < 15%), spanning 2012-2019, during the months of (left column) October and November when new ice is forming and (right column) June through August when the sea ice edge is retreating. Observations (black) represent combined BGOS-SODA dataset. Model (blue) represents results from Roach et al. (2019), aggregating grid cells in the Beaufort region surrounding observations. Note that swell occurs in the model during the ice growth season, panels (a,c).