# Probing the southern African lithosphere with magnetotellurics, Part I, model construction

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#### Abstract

The Southern African Magnetotelluric Experiment (SAMTEX) involved the collection of data at over 700 sites in Archean to Proterozoic southern Africa, spanning features including the Kalahari Craton, Bushveld Complex and voluminous kimberlites. Here, we present the first 3D inversions of the full SAMTEX dataset. In this paper, we focus on assessing the robustness of the 3D models by comparing two different inversion codes, jif3D and ModEM, and two different subsets of the data, one containing all acceptable data and the other containing a smaller selection of undistorted, high-quality data. Results show that the main conductive and resistive features are imaged by all inversions, including deep resistive features in the central Kaapvaal Craton and southern Congo Craton and a lithospheric-scale conductor beneath the Bushveld Complex. Despite this, differences exist between the jif3D and ModEM inverse models that derive mainly from the differences in regularization between the models, with jif3D producing models that are very smooth laterally and with depth, while ModEM produces models with more discrete conductive and resistive features. Analysis of the differences between these two inversions can provide a good indication of the model resolution. More minor differences are apparent between models run with different subsets of data, with the models containing all acceptable data featuring higher wavelength conductivity variations than those run with fewer stations but also demonstrating poorer data fit.

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# Key Points: We create the first large-scale conductivity models of southern Africa. We compare different strategies to construct continental scale models and investigate the impact on the results. The main inversion features are common to all models, with most differences being due to regularization.

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#### 18 Abstract

The Southern African Magnetotelluric Experiment (SAMTEX) involved the collection 19 of data at over 700 sites in Archean to Proterozoic southern Africa, spanning features 20 including the Kalahari Craton, Bushveld Complex and voluminous kimberlites. Here, 21 we present the first 3D inversions of the full SAMTEX dataset. In this paper, we focus 22 on assessing the robustness of the 3D models by comparing two different inversion codes, 23 *jif3D* and *ModEM*, and two different subsets of the data, one containing all acceptable 24 data and the other containing a smaller selection of undistorted, high-quality data. Re-25 sults show that the main conductive and resistive features are imaged by all inversions, 26 including deep resistive features in the central Kaapvaal Craton and southern Congo Cra-27 ton and a lithospheric-scale conductor beneath the Bushveld Complex. Despite this, dif-28 ferences exist between the jif3D and ModEM inverse models that derive mainly from the 29 differences in regularization between the models, with *jif3D* producing models that are 30 very smooth laterally and with depth, while *ModEM* produces models with more dis-31 crete conductive and resistive features. Analysis of the differences between these two in-32 versions can provide a good indication of the model resolution. More minor differences 33 are apparent between models run with different subsets of data, with the models con-34 taining all acceptable data featuring higher wavelength conductivity variations than those 35 run with fewer stations but also demonstrating poorer data fit. 36

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#### Plain Language Summary

We investigate the structure of the upper 200 km of the Earth beneath southern 38 Africa. To achieve this, we utilize an electromagnetic geophysical technique called mag-39 netotellurics which is sensitive to variations in electrical resistivity within the Earth. To 40 reconstruct electrical resistivity from magnetotelluric measurements, we use so-called in-41 version algorithms. However, the results are non-unique and a variety of different pa-42 rameters have to be chosen by the user during the inversion process. In order to better 43 understand the possible variability in our Earth models, we use different inversion al-44 gorithms and compare different strategies. This allows us to assess the reliability of our 45 results. Based on our models and their comparison, we infer that the lithosphere, the 46 solid outer shell of the Earth, varies in thickness below our study area and is thickest 47 below central South Africa. In addition, we can detect remnants of past continental col-48

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<sup>49</sup> lisions that have been preserved for hundreds of millions of years since this part of the

<sup>50</sup> world was assembled from the collision of various micro-continents.

#### 51 **1** Introduction

The lithosphere of southern Africa is among the most important in the world for 52 understanding continental evolution (e.g., Lee et al., 2011). It contains extensive, Archean 53 to Paleoproterozoic cratons, including the Kaapvaal, Zimbabwe and Congo cratons, which 54 are also sampled by voluminous kimberlite magmatism (e.g., De Wit et al., 1992; Begg 55 et al., 2009). Investigations of the geological, geochemical and geophysical nature of these 56 cratons help us understand the formation and amalgamation of the Archean continen-57 tal lithosphere and the survival of that lithosphere to the present. The southern African 58 lithosphere also hosts many of the world's largest mineral deposits (Clifford, 1966), in-59 cluding the world's largest platinum group element deposits in the Bushveld Complex 60 (itself the world's largest layered mafic intrusion (e.g., VanTongeren, 2018)), extensive 61 kimberlite-hosted diamond deposits including the Kimberley, Venetia and Jwaneng de-62 posits (e.g., Field et al., 2008), and giant orogenic and placer gold deposits such as those 63 in the Barberton Goldfields and Witwatersrand Basin (e.g., de Ronde & de Wit, 1994). 64 Since the formation of many of these deposits involved lithospheric-scale processes, defin-65 ing the lithospheric architecture and composition of southern Africa not only helps our 66 understanding of continental evolution but also aids mineral exploration. 67

Analysis of the vast mantle xenolith and xenocryst databases has shown spatially 68 and temporally complex patterns of depletion and metasomatism of the southern African 69 mantle (e.g., Griffin et al., 2003; Kobussen et al., 2009; Grégoire et al., 2003). In some 70 cratonic regions, inferences from xenoliths and seismic data can seem contradictory. Many 71 xenoliths have metasomatised and geochemically fertile compositions, while seismic to-72 mography models tend to show fast wave speeds extending to depths >200 km and have 73 been interpreted to represent deep, geochemically depleted lithospheric keels (e.g., Fouch 74 et al., 2004; White-Gaynor et al., 2020). This apparent contradiction has led to the sug-75 gestion that cratonic mantle xenoliths and xenocrysts from southern Africa may be un-76 representative of the cratonic mantle more generally (Griffin et al., 2009). In contrast, 77 seismic receiver function data image several low-velocity anomalies within those south-78 ern African lithospheric keels, which indicate that broad metasomatism may be more widespread 79 than suggested by the tomographic models (Sodoudi et al., 2013; Selway et al., 2015). 80

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Here and in the accompanying manuscript, we add new magnetotelluric (MT) con-81 straints to understanding the architecture, composition and evolution of the southern 82 African lithosphere. MT data are sensitive to mantle metasomatism, both through the 83 hydration of nominally anhydrous mantle minerals and through the precipitation of meta-84 somatic minerals (e.g., Selway, 2014), and MT interpretations are generally consistent 85 with mantle xenolith and xenocryst compositions (Özaydın et al., 2021). Therefore, MT 86 models of southern Africa can provide new insights into the composition and metaso-87 matism of the lithosphere. To do this, we have analysed and inverted the Southern African 88 Magnetotelluric Experiment (SAMTEX) database (Jones et al., 2009). These data were 89 collected between 2003–2008 and comprise more than 700 MT stations including broad-90 band MT (BBMT) and long-period MT (LMT) measurements along more than 15,000 91 line km crossing South Africa, Botswana and Namibia. 92

In this paper, we describe the first 3D MT models of the entire SAMTEX dataset. 93 In contrast to when SAMTEX was collected, 3D MT inversions are now routine. How-94 ever, different inversion codes use different regularizations, model discretizations and for-95 ward modelling approaches, and the impact of these differences is not well understood. 96 Therefore, we have inverted the dataset with two different algorithms jif3D (Moorkamp 97 et al., 2011) and *ModEM* (Kelbert et al., 2014)) to compare results and ensure only the 98 most robust features are interpreted. In the accompanying paper, we interpret the mod-99 els in terms of the composition and evolution of the southern African lithospheric man-100 tle. 101

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## 2 The SAMTEX magnetotelluric dataset

Magnetotellurics (MT) is a passive electromagnetic technique to infer the resistiv-103 ity of the subsurface from measurements at the surface (Chave & Jones, 2012). Together 104 with seismic tomography and potential field methods (e.g., gravity, magnetics), MT is 105 one of the foremost geophysical techniques to image the structure of the lithosphere-asthenosphere 106 system. It has been used to investigate continental lithospheric structures in many re-107 gions around the world (e.g., Jones, 1999; Gatzemeier & Moorkamp, 2005; Rao et al., 108 2014; Wannamaker et al., 2017; Selway, 2018) and has been a component of large national 109 programs in the United States (Kelbert, 2019), Australia (Kirkby et al., 2020) and China 110 (S.-W. Dong et al., 2013). Based on simultaneous measurements of naturally occurring 111

variations of the electric field  $\mathbf{E}$  and the magnetic field  $\mathbf{B}$  we can estimate the frequency-

dependent, complex-valued magnetotelluric impedance Z, viz.

$$\mathbf{E} = \mathbf{Z}\mathbf{B}.\tag{1}$$

This estimation process is based on robust statistical methods and thus gives formal estimates of data uncertainties (e.g., Chave & Thomson, 2003) although these are typically increased before use in an inversion algorithm (e.g., Miensopust, 2017, and discussion below).

The MT response estimates used for our inversions were acquired during the South-118 ern African Magnetotelluric Experiment (SAMTEX) between 2003–2008 (Jones et al., 119 2009). They comprise more than 700 broadband MT (BBMT) and long-period MT (LMT) 120 measurements across South Africa, Botswana and Namibia. The primary goal of SAM-121 TEX was to image the lithospheric architecture of the cratons and mobile belts in the 122 region, and thus measurements were taken at intervals of roughly 20 km and at periods 123 0.01 - 10,000 s for the BBMT sites, and 60 km at 10 s - 10,000 s for the LMT sites. Due 124 to long recording times and favourable noise conditions in many parts of the study area, 125 the data quality at many sites is excellent throughout the period range. To date there 126 have been a number of publications performing modelling and inversions for different sub-127 regions and profiles (Hamilton et al., 2006; Muller et al., 2009; Miensopust et al., 2011; 128 Evans et al., 2011; Khoza et al., 2013; Finn et al., 2015; Moorkamp et al., 2019). In ad-129 dition, maps of resistivity directly derived from the data at selected periods have been 130 used to investigate the structure and composition of the lithosphere-asthenosphere sys-131 tem (Jones et al., 2012, 2013) and multi-observable petrological-geophysical models have 132 been created based on subsets of the data (Fullea et al., 2011). Still, to date, no three-133 dimensional resistivity models of the lithosphere based on all the available data have been 134 published. 135

We show representative data from six stations across the array in Figure 2. Their locations are shown as yellow stars in Figure 1. We concentrate on the period range of 1-10,000 s as lithospheric-scale structures are the focus of our modelling efforts. The sites show good data quality throughout the plotted period range, although at the longest periods (> 1,000 s), the scatter and error estimates increase at some of the sites (e.g., KAP45). The off-diagonal apparent resistivity sounding curves highlight a moderately conductive

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shallow subsurface ( $\approx 10 \ \Omega m$  at short periods) at the northern sites RAK011A and ZIM117.

<sup>143</sup> Further south, at sites KIM428 and KAL014, the short period apparent resistivities are

generally comparable but slightly higher, while the southernmost sites, KAP045 and KAP019,

show significantly higher short period apparent resistivities of  $\geq 500 \ \Omega m$ . Beneath this

<sup>146</sup> surface layer, the sounding curves of the four northern sites suggest that resistivity in-

147 creases with depth to a maximum of  $\approx 500 \ \Omega$ m at  $\approx 500 \ s$ , before either remaining con-

stant or decreasing slightly at longer periods. In contrast, at the two southern sites (KAP45

and KAP19), most of the apparent resistivity curves have higher initial values and de-

<sup>150</sup> crease with period.

<sup>151</sup> **3 Inversions** 

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# 3.1 Inversion Algorithms

We invert the observed MT impedances with two different inversion algorithms (Moorkamp 153 et al., 2011; Kelbert et al., 2014) and two different strategies for each code. This helps 154 us to address model uncertainties related to algorithm-specific choices, such as regular-155 ization, error floor, model discretization, and precision of the forward modelling engine. 156 As a result of these choices, each code will fit different aspects of the data, including those 157 affected by noise, to different degrees. As both algorithms used here are well established, 158 we only give a brief summary of each algorithm and focus on comparing the differences 159 and the potential impact on the results. 160

For two inversions, we use the MT inversion module of the joint inversion frame-161 work jif3D (Moorkamp et al., 2011). The numerical basis of the forward modelling en-162 gine and the gradient calculation are presented in Avdeev & Avdeeva (2009) and Avdeeva 163 et al. (2015). It utilizes an integral-equation based forward engine x3d (Avdeev et al., 164 1997) and includes a correction for galvanic distortion at each site (Avdeeva et al., 2015; 165 Moorkamp et al., 2020). Galvanic distortion of magnetotelluric impedances is typically 166 caused by charge accumulation at small structures (compared to the induction length 167 scale), and it can mathematically be described as a site-specific, frequency-independent 168 multiplication of the impedances with a real-valued matrix  $\mathbf{C}$  (Chave & Jones, 2012). 169 In *jif3D* distortion correction is achieved by estimating the elements of  $\mathbf{C}$  as part of the 170 inversion and multiplying the synthetic impedance  $\mathbf{Z}_{synth}$  at each site with the corre-171

sponding distortion matrix when calculating the data misfit. Details on this methodology can be found in Avdeeva et al. (2015).

The inversion algorithm has been used on a range of MT datasets, both commer-174 cial and academic, including imaging the fault structure for an intra-plate event in Botswana 175 (Moorkamp et al., 2019) and hydrothermal fluids in the central Andes (Pearce et al., 2020). 176 Due to the integral equation based forward modelling algorithm, the horizontal cell sizes 177 need to be constant in both orthogonal horizontal directions. In the vertical direction, 178 cell sizes can vary and are typically fine near the surface, increasing by a constant fac-179 tor with depth to match the decreasing resolution of MT data. The discretized region 180 is embedded in a layered half-space that is kept constant throughout the inversion. Some 181 care must be taken to avoid the strong influence of this background conductivity struc-182 ture on the inversion results. In order to enforce positive conductivity values during op-183 timization and restrict model conductivities to realistic values, conductivities in each model 184 cell are transformed using the generalized model parameter scheme described in Moorkamp 185 et al. (2011). This allows us to use an unconstrained optimization algorithm based on 186 a limited-memory quasi-Newton method (L-BFGS, Avdeeva & Avdeev, 2006) to min-187 imize the objective function. Within jif3D we regularize the inversion through a first-188 order approximation of the spatial gradient of the generalized model parameters. This 189 approach has the advantage of equalizing the vast range of Earth conductivities ( $\approx 10^{-1}$ 190 to  $10^6 \ \Omega m$ ) to a range between approximately -2 and 2, and ensuring that the regular-191 ization operates similarly in all parts of the model. As the regularization is purely smooth-192 ness based, it has the potential disadvantage that structures may horizontally or verti-193 cally smear into regions of low resolution, such as those with poor site coverage in the 194 heterogeneous SAMTEX array. However, this could be considered a form of natural in-195 terpolation. 196

The other two inversions were performed using *ModEM*, a well-established and freely 197 available 3D MT inversion code (Egbert & Kelbert, 2012; Kelbert et al., 2014). It is widely 198 used in the academic community and has seen applications on datasets around the world 199 (e.g., Kelbert & Egbert, 2012; Meqbel et al., 2014; H. Dong et al., 2020; Robertson et 200 al., 2020). Its forward engine is based on a finite-difference formulation (e.g., Mackie et 201 al., 1994; Egbert & Kelbert, 2012) and its modular structure allows for inversion of dif-202 ferent combinations of electromagnetic data (e.g., Campanya et al., 2016). Compared 203 to *jif3D* the gridding requirements are less strict with variable-sized rectilinear cells in 204

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all three coordinate directions. Furthermore, no background layered half-space is pre-205 scribed; instead, the grid must be extensive enough that secondary electromagnetic fields 206 are insignificant at the model boundaries. Thus, a typical strategy for designing inver-207 sion grids in *ModEM* is to use an inner core with constant horizontal cell size and padding 208 cells of increasing size around it. In *ModEM* the natural logarithm of conductivity is used 209 as a model parameter which enforces positivity of conductivity and has an equalizing ef-210 fect similar to the generalized model parameters in jif3D. ModEM does not allow the 211 range of permitted conductivities to be directly limited, but the regularization limits the 212 difference from a prior model, often the starting model, and lateral variations of conduc-213 tivity simultaneously (Egbert & Kelbert, 2012). Compared to a pure smoothing-based 214 regularization, this combined approach should reduce smearing but can result in arti-215 ficial changes in conductivity if the prior model is not representative of the average con-216 ductivity in the region. In this case, poorly-resolved regions of the model will be kept 217 at prior conductivity values, whereas well-resolved regions will exhibit a different con-218 ductivity. 219

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#### 3.2 Data selection

Within each inversion algorithm, we ran an "all data" inversion of the entire SAM-TEX dataset (with only clearly erroneous stations removed) and another "selected" inversion of a subset of the data. This approach was designed to test the impacts of heterogeneous station coverage and of noisy and distorted data on the results of each inversion algorithm.

SAMTEX station coverage is highly heterogeneous compared to other large-scale 226 initiatives such as USArray (Kelbert, 2019) or AusLAMP (e.g., Robertson et al., 2016; 227 Kirkby et al., 2020; Thiel et al., 2020). Due to logistical constraints and the still preva-228 lent two-dimensional inversion approaches at the time of planning the measurements, data 229 were collected in relatively dense transects separated by significant gaps. In a 3D regional 230 model, the crustal structure will therefore be strongly represented in the data near those 231 profiles and completely absent in regions without coverage. In contrast, deeper features 232 (50-200 km) will at least be partially sensed by the data even in regions without direct 233 station coverage. For this reason, the focus of our inversions will largely be on the re-234 gional imaging of the mantle lithosphere-asthenosphere system. To image the mantle, 235 dense sampling along the profiles could be either beneficial or detrimental. On the one 236

hand, dense coverage should result in redundant information and thus reduce the influence of noise for deep imaging, but on the other hand, dense measurements can be highly
affected by local structures that cannot be represented well in the regional model. This
issue might be further exacerbated by the need to choose a global regularization parameter for the model, as localized structures in densely covered areas might require a small
regularization parameter. However, small regularization parameters might be inappropriate for regions without dense coverage.

The noise levels of SAMTEX data are also heterogeneous (Figure 3). Some sites 244 show significant noise across the whole period range, with either highly scattered or phys-245 ically unrealistic data (e.g., ELG010A). These sites were excluded from all inversions. 246 Of the remaining sites, some (e.g., BOT405) display smooth sounding curves with phases 247 in quadrant but also demonstrate large offsets between the apparent resistivity curves, 248 indicating local static distortion. Others (e.g., KAP047 and WIN011) show similar signs 249 of static distortion and additionally display rapidly varying phases that extend out of 250 the quadrant, which could indicate local noise or strong resistivity contrasts in the shal-251 low subsurface. Even though jif3D can correct for distortion and strategies have been 252 devised for *ModEM* to mimic the effects of distortion (Meqbel et al., 2014), it is unclear 253 to what degree the information from these sites is useful to constrain deep structures and 254 whether fitting distorted sites prevents fitting other data. To investigate the impact of 255 such sites, they were therefore retained in the "all data" inversion but excluded from the 256 "selected" inversion. To further reduce station density and to assess the impact of het-257 erogeneous station coverage, additional stations with low-quality long-period data (> 500-258 10000 s) were also removed. After the selection procedure, the resulting "selected" dataset 259 has a station spacing along the station transects of  $\sim 30-80$  km in most regions, com-260 pared to  $\sim 20$  km for the "all data" dataset (compare blue and red dots in Figure 1). 261

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# 3.3 Inversion Setup

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To be able to accommodate the entire region in a single model with acceptable computational run times, the horizontal discretization for the core region was chosen to be 15 km in the northing and easting directions for all inversions. Including the padding cells for the runs with *ModEM*, the inversion domain comprises  $132 \times 133 \times 53$  cells with a vertical discretization of 50 m for the topmost cells increasing up 141 km at the bottom of the domain. Information on ocean bathymetry was introduced from the ETOPO1

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global topographic dataset, and seawater was assigned a resistivity of 0.3  $\Omega m$ . On land, no topography was considered, and a starting resistivity of 100  $\Omega m$  was assigned to all cells.

Inversions for *ModEM* were run with error floors of 5% of  $\sqrt{Z_{xy}Z_{yx}}$  on all tensor elements. The starting  $\lambda$  was set to 10 and decreased by a factor of 5 when the inversion when RMS misfit difference is less than 0.002. An isotropic smoothing operator was constructed with the covariance matrix set to 0.4 in all directions. For the inversions with *jif3D*, we used the same error floor as for the inversions with *ModEM*. We removed the outer padding cells from the grid used for modelling in *ModEM* resulting in a mesh with 119 × 120 × 48 cells and chose a fixed background resistivity of 100  $\Omega m$ .

The inversions for *jif3D* were run with a similar approach to regularization as the inversions with ModEM. However we used different values for the regularization parameter, staring with  $\lambda = 1,000$  and reducing it to  $\lambda = 1$  in the final iterations, since the influence of the regularization on the inversion is different between the two algorithms. The initial iterations did not include any distortion correction, but this was enabled after the first regularization change as this has been shown to yield stable results (Moorkamp et al., 2020).

#### 286 4 Data fit

For the selected datasets the inversion algorithms reach a final RMS of 1.7 (jif3D)287 and 2.3 (ModEM) after 200 and 146 inversion iterations, respectively. For the inversion 288 of the full datasets, the corresponding RMS values are 2.7 and 5.0, respectively. We show 289 the final root-mean-square (RMS) misfit at each site for all frequencies in Figure 5. When 290 we only invert the selected data (bottom row) using both jif3D and ModEM we achieve 291 a relatively homogeneous RMS between 1.5 and 2.5 at the majority of sites, and only 292 a few sites exceed RMS values of 4.5. While there are some differences in how well sites 293 are fit, the overall pattern is comparable and some sites are fit better in one inversion 294 or the other. In contrast, when inverting the maximum amount of data, the distribution 295 of RMS becomes much more heterogeneous. Many sites are still in the 1.5 to 2.5 range, 296 but some sites exceed RMS values of 10. This effect appears to be more pronounced for 297 ModEM than *jif3D* and some sites that were fit well in the "selected" inversion are now 298 fitted significantly worse. These observations confirm that some data that were excluded 299

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are, in fact, problematic for the inversion. At least for some of these sites, the distortion correction used by jif3D helps to achieve a better fit. The question remains, though, to which degree this impacts the final models.

Figure 4 shows the estimated values of the distortion matrix  $\mathbf{C}$  for the two *jif3D* 303 inversions at the central area of the array around the sites BOT405 and KAP047 (Fig-304 ure 3) that were previously identified as distorted (a version with all stations can be found 305 in the supplementary material). For the selected data inversion,  $\mathbf{C}$  is close to the iden-306 tity matrix at virtually all sites indicating little to no galvanic distortion. This demon-307 strates that the data selection process successfully removed stations with significant dis-308 tortion and that the inversion algorithm does not introduce artificial distortion, for ex-309 ample, to achieve a low data misfit with a smooth model. When inverting the complete 310 data set, some but not all of the additional sites show significant distortion and sites BOT405 311 and KAP047 are among the most distorted (Figure 4). 312

In theory, if galvanic distortion is caused by structures that are small compared to 313 the typical induction scale length at short periods (Chave & Jones, 2012) and the dis-314 tortion correction only represents this structure-related distortion, the estimates of C 315 at neighbouring sites should show little correlation. Although this is the case in some 316 regions, we also see clusters of sites with very similar distortion estimates, e.g., south of 317 site BOT405. Here the estimate of  $C_{xx}$  is consistently larger than unity and  $C_{yy}$  smaller 318 than unity at most sites. There are two possible explanations for this phenomenon: a) 319 It is possible that these sites were all installed in similar geological conditions, for ex-320 ample, when looking for softer ground in an environment dominated by outcropping bedrock. 321 b) More likely, the distortion estimates capture variability in structures that can, in prin-322 ciple, be resolved by MT measurements but cannot be represented by the chosen hor-323 izontal discretization of 15 km, i.e. they account for the so-called model discrepancy (Kennedy 324 & O'Hagan, 2001). These stations are located at the northern end of the Kaapvaal Cra-325 ton crossing into the Magondi Mobile Belt, and thus it is likely that significant defor-326 mation is recorded in the crust. 327

We compare the data fit for the distorted site BOT405 and and the exemplary sites RAK011A, KIM428 and KAP045 for the *ModEM* "all data" inversion (Figure 6) and the *jif3D* "all data" inversion (Figure 7). The difference between observed and predicted data for site BOT405 clearly shows how the distortion correction in *jif3D* helps to achieve

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a better fit to the off-diagonal apparent resistivity curves. Whereas the model response 332 from ModEM converges to a common apparent resistivity value at short periods, jif3D333 reproduces the constant offset between the two curves. Interestingly, although the off-334 diagonal phases are fit differently by both inversions, there is no clearly superior fit by 335 either of the two models. At sites RAK011A and KIM428, both models produce virtu-336 ally identical responses for the off-diagonal apparent resistivities and phases and match 337 the observed data well. At site KIM428, the models reproduce all variations of the curves, 338 while at site RAK011A, the overall shape is reproduced well by the models, but the phase 339 anomaly in the xy-component at periods between 50-100 s is not fully reproduced by ei-340 ther model. At both stations, the diagonal elements are significantly smaller than the 341 off-diagonal elements and are matched better by the jif3D inversion than the ModEM 342 inversion. It is our experience that distortion correction helps to match diagonal elements 343 better even when these are small (Moorkamp et al., 2020). The data at site KAP045 are 344 matched differently by the two inversions, and again the difference is more pronounced 345 in the phase than in apparent resistivity. The response from *ModEM* reproduces the short 346 period phases well but shows small but consistent differences in the overall shape. In com-347 parison, jif3D appears to reproduce aspects of the general shape better but does match 348 the phases exactly in any period range. 349

The observed differences in model fit highlight that different inversion algorithms 350 reproduce different aspects of the observed data that go beyond the changes expected 351 from simply modifying the regularization in a single inversion algorithm. This contrast-352 ing behaviour illustrates the value of inverting data with multiple inversion algorithms. 353 It also shows that distortion correction can help fit certain aspects of the data, as demon-354 strated by the misfit maps, but this does not necessarily imply that all aspects of the 355 data are matched more closely. All in all both inversions with all data match the obser-356 vations at the majority of sites well. We therefore expect both models to provide rea-357 sonable representations of electrical resistivity in the vicinity of the measurements sites. 358

**5 Resistivity models** 

We show horizontal cross-sections through the derived inversion models between 50 and 200 km depth in 50 km intervals (Figures 8 - 11) as well as vertical slices in the east-west direction at latitude 22° south (Figure 12) and along the Kaapvaal (Figure 13) and Kimberley (Figure 14) profiles (see also Figure 1 for location of these profiles). The

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different inversions show very similar large-scale structures, e.g., a generally resistive ( $\geq$ 364 500  $\Omega m$ ) central region below 50 km depth, which is significantly more resistive than the 365 starting model (100  $\Omega m$ ). Embedded in this resistive lithosphere are several large con-366 ductors, typically associated with boundaries of different geological units. Even though 367 the large-scale picture is similar for all models, there are significant differences in the de-368 tailed resistivity structures and values between the inversion results. We will therefore 369 start with a description of the main features based on the "all data" jif3D model and 370 discuss how these are expressed in the other models. In the next section, we use the dif-371 ferences and similarities between the models to appraise the robustness and resolution 372 of inversion results. 373

We observe the maximum resistivity ( $\geq 5,000 \ \Omega m$ ) around the south-eastern part 374 of the array (labelled the Kaapvaal Resistor (KR) on the horizontal slices) and the north-375 western part of the array, north of the Damara Conductive Belt (DCB). In both cases, 376 the maximum resistivity is located at depths between 50–100 km and appears to decrease 377 at 150 km depth and below. These observations are compatible with the thick, dry litho-378 spheric mantle associated with the roots of the Kaapvaal Craton and the Congo Cra-379 ton, respectively (e.g., Evans et al., 2011; Jones et al., 2013; Khoza et al., 2013). In the 380 central part of the array, around latitude 24° south, is a roughly east-west striking band 381 of reduced resistivity (~100  $\Omega m$ ) in the deeper slices (150 km and below) which becomes 382 more resistive in the shallower parts of the model. We term the central structure in this 383 band at approximately 24° east the Molopo Farms Conductor (MFC). It can be iden-384 tified as a zone of decreased resistivity (< 20  $\Omega m$ ) on the 150 km and 200 km depth slices 385 from the two ModEM inversions. The *jif3D* based inversions only show a weak signa-386 ture at 150 km but show a structure with similarly low resistivity displaced slightly to 387 the north-west at 200 km depth. The conductor associated with Bushveld Complex (Bushveld 388 Conductor, BC) appears on all different modelling schemes north of the Kaapvaal Re-389 sistor (KR, Figure 13). Even though its conductivity differs from model to model, less 390 than 10  $\Omega m$  in the inversions with *ModEM* and 30–50  $\Omega m$  in the inversions with *jif3D* 391 , its spatial extent is consistent between models and it is consistently positioned beneath 392 the surface expression of the Bushveld intrusive complex, suggesting that it is a robustly 393 modelled feature. 394

Further south, the *ModEM* inversions indicate a low resistivity zone  $(20 \ \Omega m)$  at a depth of 50 km near the south-western terminus of the Kaapvaal Craton, which we term

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the Southern Kaapvaal Conductor (SKC). The "selected data" *ModEM* inversion shows this low resistivity extending to depths  $\geq 150$  km, but this is less clearly visible in the inversion with all data. Both *jif3D* inversions show decreased resistivities of 100  $\Omega$  m compared to the surrounding 1,000  $\Omega m$ , but no structures with the low resistivity indicated by *ModEM*.

In the north-western part of the array, the signature of the Damara Conductive Belt 402 (DCB), previously identified by Khoza et al. (2013), is apparent at a depth of 50 km in 403 all inversions. It is an east-west striking band of decreased resistivity (~10  $\Omega m$ ), inter-404 preted to be associated with the collision between the Congo Craton and the adjacent 405 mobile belts. At depths of more than 100 km, the inversions with all data also contain 406 an approximately north-south striking, low resistivity feature. The inversions with se-407 lected data also show slightly decreased resistivity in the same region, but it appears that 408 some information on this feature is contained in the sites excluded in the selection pro-409 cess. 410

In addition to these four features discussed above, the model contains a variety of other structures. We do not go into further detail on all these features here but in the second part of this study (Özaydin et al., 2021) we investigate the relationships between the geoelectric lithospheric architecture, composition, tectonic and magmatic history of the southern Africa in detail.

The vertical slices through the model shown in Figures 12 - 14 confirm the infer-416 ences made by comparing the horizontal slices, showing similar low and high resistivity 417 features. However, the exact locations, shapes and resistivity values vary between the 418 different inversions. In all cases, the "all data" inversions show stronger resistivity con-419 trasts and more localized features than the "selected data" inversions for the same in-420 version algorithm, particularly in the upper 50 km. Below this depth, the differences be-421 tween using all data and selected data are less pronounced, but persist. For example, the 422 ModEM "all data" slice along the KAP line (Figure 13) shows a low resistivity zone at 423 a depth of 200 km towards the northern (right) end of the profile. This feature is not 424 clear in the "selected data" inversion, which shows resistivity values comparable with 425 the starting model, possibly suggesting that there is little resolution in this region. Com-426 paring the results from the two different inversion algorithms, *ModEM* appears to favour 427

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 $_{428}$  more concentrated features at depth while in *jif3D* the features are generally more dis-

<sup>429</sup> tributed with less sharp edges.

#### 430 6 Model appraisal

To provide a quantitative view on the differences between the models, we plot model 431 difference matrices at a depth of 50 km in Figure 15 and 150 km in Figure 16. In both 432 cases, we show a horizontal slice through each model at the respective depth on the di-433 agonal. Plots above the diagonal show the difference in logarithmic resistivity for the dif-434 ferent model combinations, while plots below the diagonal show the corresponding re-435 sistivity difference histograms. The model histograms show significant differences in re-436 sistivity between all model combinations of up to 2 orders of magnitude (2 in logarith-437 mic units), even though for the vast majority of model cells, the difference is less than 438  $\pm 1$  order of magnitude. The histograms appear to be slightly wider at 50 km depth than 439 at 150 km depth. Most histograms are centered around a difference of zero, suggesting 440 that there is no significant overall bias in the resistivities retrieved in each inversion, ex-441 cept the histogram for the two inversions with selected data, which is centered around 442  $\approx 0.2$ , indicating that the model produced by *jif3D* is consistently more resistive. 443

The histograms clearly illustrate that the largest resistivity differences are produced by using different algorithms to invert the same dataset, while smaller differences are produced by inverting different subsets of data with the same inversion algorithm. At both depths and for both inversion algorithms, the histograms comparing the "selected" and "all data" inversions show highly symmetric shapes and a concentrated peak at zero, while the other histograms are generally broader and exhibit more structure.

The spatial difference plots in Figures 15 and 16 add more detail to the global re-450 sistivity differences displayed in the histograms. Spatial comparisons between the jif3D451 and *ModEM* models using both "selected data" and "all data" datasets at both depths 452 consistently show that the iif3D models have higher average resistivities over much of 453 the model space than the *ModEM* models, except for in the south-western part of the 454 array where jif3D produces a consistently less resistive model. The south-western region 455 is the part of the model most poorly constrained by station coverage. These differences 456 sum to a resistivity difference histogram that centers on zero. In all difference plots, we 457 also see a correlation between locations of large scale tectonic boundaries and changes 458

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in sign of the resistivity difference, particularly along the northern margin of the NamaquaNatal Belt and the margins of the Damara and Ghanzi-Chobe belts. While the details
vary, this phenomenon is observed in all combinations of models to varying degrees. This
indicates that the differences in the models are not merely due to fitting aspects of the
data differently or the influence of noisy measurements, but each inversion images the
Earth in a different way.

Comparisons between the two "selected data" inversions and the two "all data" in-465 versions demonstrate that data selection has a significant impact on model differences. 466 The spatial difference plots for the jif3D and ModEM "selected data" inversions reveal 467 broad zones of consistent resistivity differences, while those for the two "all data" inver-468 sions show much more inhomogeneous, spatially varying resistivity differences. This re-469 sults from the stronger influence of regularization in the "selected data" inversions, lead-470 ing to overall smoother models. When adding data, the wavelength of the patterns de-471 creases, and we see more fine-scaled differences, together with relatively sharp changes 472 between positive and negative differences. Some of the largest differences are located in 473 regions without site coverage, e.g., southeast of the KAP line or in the gaps between mea-474 surement lines in the northern part of the array. 475

The most likely candidate for causing many of these differences is the different reg-476 ularization schemes. This factor is most clearly seen in the comparison between mod-477 els produced with the "selected" dataset as the influence of regularization is strongest 478 there. Where the Earth is more resistive than the starting model in both inversions, jif3D479 consistently estimates higher resistivities than ModEM. Conversely, where the inversions 480 indicate lower resistivities than the starting model, jif3D underestimates resistivity com-481 pared to *ModEM* on the larger scale. Both observations can be explained by the fact that 482 *ModEM* minimizes the difference to the reference model and smoothness simultaneously, 483 while jif3D only aims at recovering a smooth model. This behaviour can explain the ob-484 served correlation between major tectonic boundaries and changes in sign of the resis-485 tivity difference. A resistive geological region is likely to be modelled with a higher re-486 sistivity in *jif3D* than *ModEM*, and an adjacent conductive geological region is likely to 487 be modelled with a lower resistivity in jif3D than ModEM. The model difference plot there-488 fore highlights the boundary between these two regions. 489

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Without additional information, we cannot say which of the inversions is more rep-490 resentative of the true resistivity within the Earth. However, we tried to reduce the ef-491 fect of regularization in *ModEM* by running an additional inversion with a starting and 492 reference model based on laterally smoothed apparent resistivities. To construct this model, 493 for each measurement site we construct a circle with a 4-degree radius centred on the 494 site and take the median apparent resistivity value of all sites within the circle at peri-495 ods longer than 100 s. The resulting resistivity value is assigned to all cells below this 106 site. We then perform a linear interpolation of logarithmic resistivity between these val-497 ues to determine the resistivity in each model cell. The resulting model (Figure 17) shows 498 laterally varying resistivities between 50 and 1,000  $\Omega m$  and regions of high resistivity that 499 correlate with the most resistive regions identified in the previous inversions. 500

The resulting median inversion model (Figures 18 and 19) fits the selected data to 501 an RMS comparable with the inversion run from a homogeneous half-space. Compared 502 to the homogeneous inversion run, the average resistivities at 50 km depth (Figure 18) 503 and 150 km depth (Figure 19) are higher, particularly in regions that are not directly 504 covered by sites. Conductive anomalies show a very similar pattern to the previous in-505 versions, although the shape and location differ slightly in some cases, including some 506 of the individual conductors that form the Damara Conductive Belt at 50 km depth (com-507 pare Figure 8 and Figure 18) or the Southern Kaapvaal Conductor at 150 km depth. These 508 changes are not significant enough to imply a different geological interpretation of these 509 structures. 510

The spatial difference plot and difference histogram comparing the median inver-511 sion and the inversion of the same data with jif3D reveals some interesting changes com-512 pared to the inversion with a homogeneous starting model. Visually, the spatial differ-513 ence plot for the median model contains a lot less long-wavelength structure and is dom-514 inated by more small scale differences. This contrast is particularly visible at 50 km depth 515 where jif3D previously produced consistently higher resistivities in the central model re-516 gion. However, the spatial difference plot for the median model displays a much more 517 variable pattern where the sign of the conductivity difference changes within smaller dis-518 tances. At 150 km depth, the effect is less pronounced yet still observable. 519

The difference histogram comparing the median inversion and the jif3D inversion at 50 km depth has a maximum very close to zero, while the histogram comparing the

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homogeneous inversion and jif3D is offset to slightly positive values with a maximum 522 at  $\approx 0.2$ . While still not fully symmetric, the maximum and minimum (most negative) 523 differences now show a similar magnitude. At 150 km depth, the impact of the starting 524 model on the histogram is even more pronounced and the median model histogram is 525 more significantly offset to negative values associated with the higher average resistiv-526 ity of the median model. While the average resistivities inverted from the homogeneous 527 ModEM are downward biased compared to jif3D, the median model ModEM resistiv-528 ities are upward biased. 529

#### 530

# 7 Discussion and Conclusions

The main goal of this paper is to present a new 3D conductivity model for southern Africa and use the different inversion methodologies to understand uncertainties in the results better. An additional result is that the detailed comparisons of the models also reveal some technical aspects of inversions and regularization that are of interest to both algorithm developers and practitioners and thus warrant some discussion before describing some of the geological interpretations implied by these models.

It is our impression that most of the differences between the results from the two 537 inversion algorithms stem from the different regularization philosophies. The purely smooth-538 ness based approach followed by jif3D spreads out structures to their maximum possi-539 ble extent, most clearly visible in Figure 13. Selecting such a smoothing operator has 540 the disadvantage that conductive anomalies can be smeared out, and their boundaries 541 can be challenging to identify. In contrast, the mixed regularization approach pursued 542 by ModEM typically produces more localized structures. On the flip side, the regular-543 ization toward a reference model appears to bias the large scale resistivity toward this 544 model, particularly in regions of low sensitivity. This observation is mirrored by the sys-545 tematic study of Robertson et al. (2020). Taken together, we conclude that for large ar-546 rays with heterogeneous coverage such as this, jif3D produces models with more repre-547 sentative large-scale resistivity values, while *ModEM* produces more focused and local-548 ized anomalies. To some degree, a more representative large-scale resistivity can be ob-549 tained with ModEM with a median-based starting model, as shown by the comparison 550 at 50 km depth. Still, the shift in bias at 150 km shows that possibly a more detailed 551 starting model with varying resistivity with depth is necessary to obtain good average 552 resistivities over large areas. Alternatively, one could design a regularization scheme where 553

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the balance between smoothness and damping toward a reference model can be finely adjusted. While it seems that such an approach could combine the advantages of both regularization approaches, it is questionable how an optimal balance could be objectively found and how practical such a scheme would be for routine application.

The effect of inverting for only selected, high-quality data or the maximum amount 558 of data is similar regardless of the inversion algorithm. In both cases, the inclusion of 559 more data increases the misfit of the final models as potentially problematic sites are in-560 troduced. To some degree, this effect is reduced by the distortion correction employed 561 in jif3D which can deal with problems associated with galvanic distortion and achieve 562 a better fit at many sites. At the same time, the models with more data exhibit stronger 563 resistivity contrasts and additional structures, e.g., the north-south striking conductor 564 in the north-western part of the study area that extends from the Congo Craton into the 565 Damara Belt. Given the similarity of these features for both inversion algorithms and 566 the acceptable misfit for the inversion with jif3D, we conclude that these are not arte-567 facts caused by noisy data, but that these features are due to information about the re-568 sistivity of the Earth contained in the measurements included in the "all data" models. 569 Still, the inversions with selected data contain the same general features as the inver-570 sions with all data. Based on the similarity with other models and the data fit, our two 571 preferred models are the ones produced by jif3D with all data and the ModEM inver-572 sion with a median starting/reference model and selected data. 573

The most prominent features of our two preferred models are: (1) A resistive core 574 of the Kaapvaal Craton as indicated by the Kaapvaal Resistor. This region of high re-575 sistivity  $(> 1,000\Omega m)$  extends to depths of 150 km (ModEM) to 200 km (jif3D) and 576 indicates a dry lithospheric mantle in line with previous 2D interpretations (Evans et al., 577 2011) and experimental electrical conductivity of common mantle minerals (e.g., Karato 578 & Wang, 2012; Ozaydın & Selway, 2020). (2) Other high resistivity regions at depths of 579 100 km and greater include the Congo Craton in the north-west (Kamanjab Inlier) and 580 northern Botswana in the north-eastern part of the array suggesting the presence of litho-581 sphere with a broadly similar composition in these regions. (3) These resistors are in-582 tersected by several deep-seated conductors that are present to varying extents in all in-583 version models. These include the Molopo Farms conductor, the Bushveld conductor and 584 the north-south striking feature below the Congo Craton and Damara Belt. In the lat-585 ter case, a possible interpretation is a shallower lithosphere-asthenosphere boundary com-586

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pared to the thick cratonic roots of the Kaapvaal and Congo Cratons (Celli et al., 2020).
In contrast, the Molopo Farms Conductor and the Bushveld Conductor are likely expressions of emplacement of metasomatic material during episodes of magmatism (Beukes et al., 2019).

A more detailed interpretation of the resistivity structures recovered by these inversions requires careful consideration of the geological history of the region and the relationships between resistivity, composition and temperature. These considerations are beyond the scope of this study and are presented in a companion paper (Özaydin et al., 2021).

We have constructed a set of 3D models for southern Africa based on two subsets 596 of the SAMTEX magnetotelluric dataset and utilizing two independent inversion algo-597 rithms. Despite some differences in the shape of structures and the recovered resistiv-598 ities, the models show strong similarities. Previous efforts using these data either used 599 the whole dataset but did not perform inversions or were concentrated on regional sub-600 sets of the data. Thus the models presented here are the first large-scale resistivity mod-601 els of the region and can serve as a resource for further investigations and integration 602 with other observations such as gravity and seismology. 603

#### 604 Acronyms

- 605 **BBMT** Broad-Band Magnetotelluric
- 606 **BC** Bushveld Conductor
- 607 **DCB** Damara Conductive Belt
- 608 **MT** Magnetotelluric
- 609 **KR** Kaapvaal Resistor
- 610 LMT Long-period Magnetotelluric
- 611 MFC Molopo Farms Conductor
- 612 SAMTEX South African Magnetotelluric Experiment
- 613 SKC Southern Kaapvaal Conductor



Figure 1. Map of the study area. We show the SAMTEX magnetotelluric measurement sites considered in the full data inversions as blue dots and the sites considered in the inversions with selected data as red dots. Yellow stars indicate exemplary stations for different regions shown in Figure 2 and red stars poor quality data excluded from some of the inversions and shown in Figure 3. The red, green and yellow lines mark the locations of vertical model profiles along the Kimberley, Kaapvaal and 22 degree south lines, respectively. Black lines mark the boundaries of tectonic provinces based on McCourt et al. (2013).



**Figure 2.** Six exemplary sites representing different regions within the inversion domain. For each site we plot apparent resistivity and phase of the four impedance elements. Off-diagonal (xy and yx) apparent resistivities are plotted with a consistent y-axis to highlight differences in average resistivity between different regions, while apparent resistivity for the diagonal components is plotted with a different scale for each site for better readability.



Figure 3. Examples of data excluded from the inversions with selected data. Site ELG10A shows overall problematic data and has been excluded from all inversions while the other sites show potentially problematic features as discussed in the text but have been retained for the inversions with maximum data.



Figure 4. Map of misfit for the four inversion runs. We show the error normalized RMS across all frequencies at each site.



**Figure 5.** Map of distortion estimates for the inversions with *jif3D* in the central region of the array. We show the estimates for the inversion with all data as circles and for the selected data inversion as squares. These have been displaced north from the original locations for better visibility. Colors mark the deviation of the distortion matrix elements from the identity matrix. We highlight sites BOT405 and KAP047 shown in Figure 3 with black stars.



#### Data fit ModEM

Figure 6. Comparison between observed data (symbols) and predicted data (lines) for the inversion run with *ModEM* and all data for four selected sites marked in Figure 1.



# Data fit jif3D

**Figure 7.** Comparison between observed data (symbols) and predicted data (lines) for the inversion run with *jif3D* and all data for four selected sites marked in Figure 1.



#### MT models at 50 km depth

**Figure 8.** Horizontal slices through the inversion models at a depth of 50 km. We mark several notable structures: Bushveldt Conductor (BC), Damara Conductive Belt (DCB), Kaapvaal Resistor (KR), Molopo Farms Conductor (MFC), Southern Kaapvaal Conductor (SKC).



## MT models at 100 km depth

Figure 9. Horizontal slices through the inversion models at a depth of 100 km. For an explanation of abbreviations see Figure 8.



#### MT models at 150 km depth

Figure 10. Horizontal slices through the inversion models at a depth of 150 km. For an explanation of abbreviations see Figure 8.



## MT models at 200 km depth

Figure 11. Horizontal slices through the inversion models at a depth of 200 km. For an explanation of abbreviations see Figure 8.



# EW Slices at 22 degree South

Figure 12. East-west slice through the four inversion models at 22 degree southern latitude (yellow line in Figure 1).



Figure 13. Vertical model slices through the four inversion models along the KAP line (green line in Figure 1). From top to bottom the inversion runs are: *jif3D* with selected data, *ModEM* with selected data, *jif3D* with all data, *ModEM* with all data.



Figure 14. Vertical model slices through the four inversion models along the Kimberley line (red line in Figure 1). From top to bottom the inversion runs are: *jif3D* with selected data, *ModEM* with selected data, *jif3D* with all data, *ModEM* with all data.

#### Model difference at 50 km depth



Figure 15. Difference matrix for the four inversion runs at a depth of 50 km. We plot the resistivity slice for each model on the diagonal. Plots above the diagonal show the difference in logarithmic resistivity between pairs of models as labelled above each column, Plots below the diagonal show the corresponding histogram.

#### Model difference at 150 km depth



Figure 16. Difference matrix for the four inversion runs at a depth of 150 km. We plot the resistivity slice for each model on the diagonal. Plots above the diagonal show the difference in logarithmic resistivity between pairs of models as labelled above each column, Plots below the diagonal show the corresponding histogram.



Figure 17. Starting model derived from median apparent resistivity for the inversion with ModEM. Note the reduced range of resistivities in the color bar compared to the other model plots.

# Model difference at 50 km depth



Figure 18. Difference matrix for the ModEM inversion runs with a homogeneous starting model and a median apparent resistivity starting model at a depth of 50 km.

# Model difference at 150 km depth



Figure 19. Difference matrix for the ModEM inversion runs with a homogeneous starting model and a median apparent resistivity starting model at a depth of 150 km.

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- IRIS SPUD repository at https://doi.org/10.17611/DP/EMTF/SAMTEX. Download in-
- structions for the ModEM inversion software can be found at https://sites.google
- .com/site/modularem/download. jif3D is available via subversion at https://svn.code
- .sf.net/p/jif3d/jif3dsvn/trunk/jif3D. Figure 1 was prepared using GMT 6.1 (Wes-
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