Short-periodic VLF emissions observed simultaneously by Van Allen Probes and on the ground

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Abstract

We present simultaneous observations of VLF emissions with periodic (2 or 4 s) bursts by Van Allen Probe near geomagnetic equator and Kannuslehto and Lovozero ground-based sites. The repetition period and ground-spacecraft delay are consistent with guided whistler wave propagation between conjugate ionospheres. In contrast to lightning whistlers, the group velocity dispersion is not accumulated from one burst to another, thus implying a nonlinear mechanism of its compensation. Two regimes are observed. In one regime, Poynting flux direction alternates in the magnetosphere, and the burst period is twice lower than on the ground, that corresponds to single wave packet bouncing along the field line. This regime is switched to the other one, with burst period unchanged in the magnetosphere but halved on the ground. In the second regime, no alternating Poynting flux direction is observed. This second regime corresponds to two symmetrically propagating wave packets synchronously meeting at the equator.

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Key Points:

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10	•	Van Allen Probes and ground based sites observed correlated periodic VLF emis-
11		sions with periods of 2 or 4 s consistent with wave packet bouncing
12	•	Poynting flux directions at Van Allen Probes were opposite in neighboring pulses
13		in one regime and parallel in the other regime

• The pulse period onboard the spacecraft was half of that on the ground in the first regime and the periods were equal in the second regime

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16 Abstract

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²⁹ Plain Language Summary

We present the first observations of VLF periodic emissions (PE) in the equato-30 rial region of the magnetosphere obtained by Van Allen Probe A (VAP-A) spacecraft. 31 These emissions were also observed by ground-based stations Kannuslehto and Lovozero. 32 The similarity of individual pulses for the entire event lasting more than an hour distin-33 guishes periodic emissions from multi-hop whistlers. The PE were detected in the fre-34 35 quency range 1.4–1.7 kHz near the upper frequency of hiss. Using correlation analysis and multicomponent data to determine Poynting flux at VAP-A we obtain delays be-36 tween the periodic elements detected on the ground and by the spacecraft. The PE prop-37 erties are consistent with propagation of isolated whistler wave packets between conju-38 gate hemispheres. The emission period observed by the spacecraft was almost constant 39 at ≈ 2 s and corresponded to the whistler one-hop transit time. The periods of VLF 40 emissions on the ground were about 4 s in the beginning and abruptly decreased to 2 s, 41 in the end of event, i.e. from the two-hop to one-hop whistler transit time. This halv-42 ing of the periods can be interpreted by changing of the PE generation regime within 43 the framework of the passive mode locking mechanism in the magnetospheric cyclotron 44 maser. 45

46 **1** Introduction

Very low frequency (VLF) emissions in the magnetosphere are often observed in the form of periodic or quasiperiodic sequence of bursts. Helliwell (1965) termed periodic emissions (PE) the bursts having repetition periods of 3 to 10 s consistent with individual wave packet propagation between conjugate ionospheres. This period can be very stable in time for long time intervals. Quasi-periodic (QP) emissions have longer periods (usually from 20–30 to 300 s), and the inter-element interval can vary smoothly due to several factors (Manninen et al., 2014).

Such events can last tens of minutes and even several hours (Manninen et al., 2014),
 which obviously requires amplification of whistler mode waves in the magnetosphere to
 compensate for the losses due to nonideal ionospheric reflection and refractive spread ing of wave energy.

Periodic emissions are divided into two subtypes which Helliwell (1965) termed dispersive and non-dispersive. The period of dispersive PE has a systematic frequency-time dispersion typical of multi-hop whistler-mode waves. The period of non-dispersive PE does not change with frequency, i.e., the effect of group velocity dispersion is not accumulated from pulse to pulse, and successive wave packets have the same shape on the dynamical spectrogram. Engebretson et al. (2004) demonstrated a transition of echoing whistlers to PE and
 then to QP emissions. Manninen et al. (2014) were able to reliably associate PEs ob served inside QP emissions with the two-hop whistler mode period. Both papers sug gested that PEs were generated in a localized region, in the outer plasmasphere/plasmapause.

The observations of periodic emissions at conjugate stations (Lokken et al., 1961) showed that the emissions appeared alternately at the two stations with a time delay about one-hop whistler transit time. Helliwell (1963); Helliwell and Brice (1964) demonstrated the examples in which the periods of dispersive and nondispersive PEs and the whistlermode two-hop group delay were the same. This led to a suggestion that the subsequent periodic elements (bursts) may be triggered by the previous ones (Helliwell, 1963, 1965).

Another mechanism of PE generation proposed by Dowden (1962) is related to the
 period of charged particle bouncing between conjugate hemispheres.

An advanced theoretical model of non-dispersive PE was developed by Bespalov (1984). The model is based on a passive mode locking regime in the cyclotron instability in which the group velocity dispersion is compensated by quasi-linear modification of the energetic electron distribution function. However, this model assumes that electron bounce periods are much shorter that the whistler hop scales. Overall, the PE phenomenon remains poorly studied.

Periodic emissions were reported mainly from ground-based observations. Two examples of PE observations by a low-orbiting DEMETER spacecraft have been reported by Bespalov et al. (2010).

In this paper we present the first report of conjugate detection of PE on the ground and onboard magnetospheric spacecraft.

⁸⁷ 2 Instruments and data

Van Allen Probes (earlier Radiation Belt Storm Probes, RBSP) are two identical spacecraft that had low-inclination (10°) orbits with 600 km perigee and 30000 km apogee (Mauk et al., 2012). Wave measurements were made by the Electric and Magnetic Field Instrument Suite and Integrated Science (EMFISIS) (Kletzing et al., 2013).

In this paper we use data of waveform (WFR) and high-frequency (HFR) receivers. The WFR comprises a six-channel waveform receiver, simultaneously samples all three electric and all three magnetic components of waves in the frequency range of ~ 10 Hz to 12 kHz with a 35 kHz sampling rate and 16 bits of digitization. The waveforms are recorded during 6-s intervals.

Plasma density was obtained from HFR spectra by using the upper hybrid resonance (UHR) line (Kurth et al., 2015).

Ground-based observations of VLF signals were carried out in Northern Finland 99 at Kannuslehto (KAN, 67.74° N, 26.27° E; L = 5.51) and Lovozero (LOZ, 67.98° N, 35.08° E; 100 L = 5.54). The distance between KAN and LOZ is 400 km. The measurements are per-101 formed by two orthogonal vertical magnetic loop antennas oriented in the north-south 102 and east–west directions and by a vertical electric field sensor installed at LOZ. Elec-103 tric field measurements allow us to resolve the 180° ambiguity in the Poynting flux di-104 rection. More detailed descriptions of the hardware are given in (Manninen, 2005; Fe-105 dorenko et al., 2014). 106



Figure 1. Spectrograms of PE for two 15-s intervals at KAN ((a) and (e), magnetic PSD) and VAP-A: (b) and (f) magnetic PSD, (c) and (g) Poynting flux polar angle θ_S , (d) and (h) wave normal angle θ_k . (i) Magnetic PSD at KAN for a 2-min interval.

¹⁰⁷ 3 Observations

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3.1 Overview of the event

We consider the event of 03 March 2019. Periodic emissions were observed from 15:35 to 17:05 UT at KAN and LOZ and from 15:51 to 17:07 UT at VAP-A. During this event, VAP-A was near the equator (MLAT varied from 0.5° to -0.5°). The waveforms were recorded by EMFISIS for two adjacent 6-s intervals every 4 minutes. The geomagnetic activity during the PE observations was low: $K_{\rm p} = 1-$, $D_{\rm st} = -11$ nT.

The event comprised two time intervals with different characteristics. Figures 1a– h show the spectrograms for two intervals near the beginning and the end of the event. A longer (2-minute) interval for KAN is shown in Figure 1i. Using singular value decomposition (SVD) technique (Santolík et al., 2003) we found that the waves at VAP-A were right-hand circularly polarized (not shown) and had fairly low wave normal angles to the geomagnetic field (Figures 1d and 1h), i.e., were electromagnetic whistler mode waves.

The magnetic planarity (not shown) exceeded 0.5 most of the time, so the wave propagation analysis can be considered reliable.

At 15:55 UT PE are seen in the frequency range 1.2–1.7 kHz, on top of a hiss band. The power modulation period is $T \approx 4$ s at KAN and $T \approx 2$ s at VAP-A (Figures 1a and 1b).

The spectra at KAN and VAP-A remained the same till 16:53 UT when a change occurred. The spectra after the change are shown in Figures 1e–1f. The PE frequency and intensity became slightly higher, and the period was $T \approx 2$ s both at KAN and VAP-A.

The period change occurred sharply, as is seen in Figure 1i. The first additional peak with 2-s interval appeared between the peaks at 16:53:21 and 16:53:25.



Figure 2. Correlation coefficient between the magnetic PSD VAP-A and KAN for the time intervals shown in Figures 1a–1d (a) and Figures 1e–1h (b). The PSD at VAP-A was multiplied by ± 1 for Poynting flux directed from/to KAN.

3.2 Wave propagation directions onboard VAP-A

Figures 1c and 1g show the Poynting flux polar angles θ_S for VAP-A observations. The neighboring pulses at VAP-A have clearly opposite propagation directions at 15:55 UT (Figure 1c). The same is true for the entire time interval till 16:53 UT. For the pulses propagating in one direction, the period at VAP-A coincides with that at KAN.

At 16:59 UT (Figure 1f), when the PE power modulation periods at VAP-A and KAN are the same, the Poynting flux at VAP-A has one dominant direction corresponding to southward propagation in all pulses. This direction is away from the geomagnetic equator, since VAP-A was at MLAT = -0.46° at that time.

The hiss at frequencies below PE does not show a dominant propagation direction during both intervals.

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3.3 Time delay between PE observed on the ground and RBSP-A

Figure 2 shows the correlation coefficient R between the pulses observed at VAP-A and KAN taking into account the propagation direction of waves at VAP-A. It was calculated after multiplying the magnetic field PSD by $-\text{sgn}(\cos \theta_S)$. Therefore, positive/negative correlation is expected for wave packets propagating away from/to KAN $(\theta_S = 180^{\circ}/0^{\circ})$.

In Figure 2a, the interval between positive maxima of R is ~ 4 s, corresponding to the pulse repetition period at KAN. The maximum at $\tau \simeq 1$ s corresponds to the pulses detected first at KAN and then propagating to VAP-A. The negative minimum at $\tau \simeq -1$ s corresponds to the pulses detected first at VAP-A and propagating towards KAN. The absolute delay values for these maximum and minimum are the same (1 s), that is consistent with the same propagation path.

In Figure 2b, the interval between positive maxima of R is about ~ 2 s, and also equal to the repetition period at KAN that halved by that time. The first maximum with positive delay τ remains at 1 s, that implies the same propagation path from KAN to VAP-A as earlier. Recall that the propagation direction at VAP-A is not alternating in this case (Figure 1g). Therefore, wave packets (i.e., the power maxima) always correspond to positive R. The negative R minima are reached when a maximum amplitude at VAP-A corresponds a minimum at KAN.

3.4 Wave propagation directions on the ground

The geomagnetic projection of VAP-A orbit to the Northern ionosphere is shown 162 in Figure 3a. We used two-component measurements at KAN to calculate the angle α 163 of the polarization ellipse minor axis (Figure 3b). Three-component measurements at 164 LOZ allow us to obtain the directions of VLF wave Poynting flux on the ground. More 165 precisely, we calculate the azimuthal angle α_S of the direction opposite to the Poynting 166 flux (backazimuth) counted from north. These angles are shown in Figure 3c. No clear 167 preference of a single propagation direction is obvious from Figures 3b and 3c, so we con-168 structed distributions of the Poynting flux backazimuth in the frequency range of 1400 169 to 1700 Hz where the PE were observed. We filtered out the odd power-line harmonics 170 in the frequency ranges $f = 50 * (2n-1) \pm 2$ Hz having a great power level. The data 171 in a moving time window (0.5 s) were binned according to the propagation angle, and 172 the total Poynting flux corresponding to every bin was calculated. These results are shown 173 in Figures 3d and 3e. A preferential south-west direction ($\alpha_S \approx 135^\circ$) can be seen dur-174 ing the entire event. However, one also easily identifies another direction ($\alpha_S \approx 315^\circ$), 175 corresponding to the waves propagating from north-east. This second direction becomes 176 more prominent since 16:40 UT, and the corresponding maximum is shifted to $\alpha_S \approx 270^\circ$. 177 However, the period change at 16:53:20 UT is not associated with a sharp redistribution 178 over the propagation directions. 179

Note that the scales in Figures 3d and 3e are absolute, i.e., one can see the wave
 intensity variations. In particular, the intensity decreased from 16:13 to 16:20 UT, and
 additional increase is seen after 16:40 UT.

183 4 Discussion

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4.1 Space-time structure of the VLF waves in PEs

Figure 4 shows periods of PE at KAN and VAP-A plotted by using the intervals of simultaneously available data. The period of $T \approx 4$ s was constant at KAN since the start of PE observations, i.e., for almost 1.5 h. During that time, the Poynting flux direction at VAP-A was alternating from pulse to pulse. At 16:53 UT, the period at KAN sharply decreased twofold. This period of 2 s was observed for 12 min, to 17:05 UT, i.e., till the end of this event. The power modulation period at VAP-A was about 2 s during the entire observation interval.

We calculated the one-hop times assuming field-aligned propagation of whistlermode waves and using plasma density and magnetic field measured by VAP-A. A gyrotropic $(N_e \propto |\vec{B}|)$ distribution of electron density N_e along the geomagnetic field \vec{B} was assumed, and a dipole \vec{B} model was used. These results for f = 1500 Hz are also shown in Figure 4. The calculated group propagation time is in good agreement with the power repetition period at VAP-A and exceeds twice the measured time delay of 1 s between KAN and VAP-A.

Taking into account that VAP-A was very close to the equator, the delays of 1 s between VAP-A and KAN measured during the first part of the event, imply the onehop time of $\simeq 2$ s, i.e., close to the calculated value. The two-hop time is $\simeq 4$ s, i.e., equal to the repetition period at KAN. Therefore, both the dynamic spectra of VLF waves at KAN and VAP-A (Figures 1a to 1c) and the structure of ground-spacecraft correlation coefficient *R* (Figure 2a) correspond to a single wave packet oscillating back and forth along a magnetic flux tube.

After the change at 16:53 UT, the period is equal to $T_{\rm g}$ both at KAN and VAP-A. This can naturally be explained by the existence of two whistler-mode wave packets propagating almost symmetrically between the hemispheres. These wave packets meet at the equator, and the period there remains equal to $T_{\rm g}$. If the powers of these wave



Figure 3. (a) Geomagnetic projection of the VAP-A orbit on the map. The trajectory part where PEs were observed is marked by a thick segment. (b) Angle of the polarization ellipse minor axis at KAN. (c) Poynting flux backazimuth at LOZ. (d) and (e) Poynting flux distributions over the propagation angles at LOZ.



Figure 4. Characteristic time scales related to the PE event: repetition periods of PE at KAN (T_{KAN}) and VAP-A (T_{VAP}), one-hop whistler-mode time time $T_{g\,1500\,\text{Hz}}$, delay τ of the signal at VAP-A with respect to KAN at 1435 Hz and 1572 Hz, and one half of bounce periods of electrons with parallel energies corresponding to the cyclotron resonance at 1400 Hz and 1800 Hz.

packets were equal, then the Poynting flux would not have had a predominant direction.
In the opposite case, the direction of the wave packet with higher amplitude prevails.

The latter variant is realized in our case, since the Poynting flux is directed south-212 ward in all pulses at VAP-A (Figure 1g). This scheme explains the positive maximum 213 of R at the negative delay $\tau \approx -1$ s in Figure 2b. This delay, equal to the half-hop time, 214 corresponds to the northward propagating pulses reaching KAN, but these pulses are not 215 seen at VAP-A since they are hidden behind the southward propagating pulses having 216 higher amplitudes. The positive sign of R agrees well with the prevalence of southward 217 propagating pulses (recall that the power was multiplied by $-\cos(\theta_S)$ when calculating 218 R). 219

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4.2 Possible location of PE emission source

Periodic emissions reported above had similar spectra on the ground and onboard VAP-A, and there was a stable time delay during the entire interval of conjugate observations. The period halving at KAN coincided with the change in Poynting flux variation at VAP-A from alternating to one-directional. These facts suggest a common source of the signals observed at KAN and VAP-A.

The preferential south-west direction ($\alpha \approx 135^{\circ}$) direction that is seen on the angular distribution maps in Figures 3c to 3d is close to the magnetic projection of the VAP-A trajectory to the ground, which allows us to assume that VAP-A could have passed the source region at the time of event. This assumption seems to agree with long-term PE detection onboard VAP-A and with the fact that the observed time delays between the waves at VAP-A and KAN were consistent with the field-aligned propagation of whistler mode waves. PE started somewhat later at VAP-A (15:51 UT) than at KAN and LOZ (15:35 UT), and during that time VAP-A moved along the same L = 5.9. We can speculate that VAP-A reached a source flux tube at 15:55. Later on VAP-A observed the PE till 17:07 UT when it was at L = 5.6, and the event stopped simultaneously both at KAN and VAP-A.

The presence of the other preferred azimuth of wave propagation at LOZ that is obvious in Figure 3d is difficult to explain in any other way than by assuming that the ducted waves occupying the source flux tube (passed by or close to VAP-A) could also propagate in some other directions after their reflections from the ionosphere and thus spread across the geomagnetic field. Similar spreading could also occur if some waves leave the ducted regime and are reflected from the lower-hybrid resonance region (Shklyar & Jiříček, 2000).

Overall, the propagation direction on the ground was not very clear (Figures 3b 245 to 3d), which could indicate a fairly close location of the region of wave propagation to 246 the ground to KAN and LOZ. This is consistent with the fact that the polarization at 247 KAN and LOZ (not shown) was right-handed during the event. We do not know the ac-248 tual extent of the source region, so we may speculate that it could be extended in lon-249 gitude and thus occupy the flux tubes closer to KAN and LOZ than those crossed by VAP-250 A. However, an extended source implies rather high synchronization of wave generation 251 over a large area, which may be problematic to explain theoretically. 252

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4.3 Possible generation mechanisms

Taking into account long event duration, it is obvious that the wave packet energy losses at each hop were compensated by the amplification in the equatorial region. A large number of hops implies ducted propagation in the magnetosphere, which is consistent with the observed and calculated ground–spacecraft delays. Ducting seems to require density inhomogeneities that are not detected by VAP-A. However, we may suggest that shallow ducts not detectable by the VAP-A instruments could exist. Possible ducting role of such inhomogeneities was discussed by Hanzelka and Santolík (2019).

The dispersion related difference in $T_{\rm g}$ between the lower and upper PE frequencies (1400 and 1700 Hz) reaches 0.1 s (not shown). Therefore, the persistent dynamic spectrum of subsequent pulses requires a nonlinear factor that compensates for the group velocity dispersion. This stable shape distinguishes the PE from multi-hop whistlers for which the dispersion effect is accumulated from pulse to pulse.

A model based on quasi-linear modification of the energetic-electron distribution 266 function by the generated waves was proposed by Bespalov (1984). This model in general complies with a hypothesis suggested by Helliwell (1963, 1965), that each previous 268 element excites the next one. However, a self-consistent nature of this process is stressed 269 in the model. The generation of pulses with repeating dynamic spectrum is similar to 270 passive mode locking in masers and lasers, that is a specific form of mode competition. 271 In this case, each pulse modifies the distribution function in such a way that only those 272 portions of the reflected pulse that match the primary pulse are amplified on the next 273 hop, while the dispersed portions are damped. 274

According to this model, the pulse repetition period on the ground can be $2T_g/n$, where *n* is integer. The longest period corresponds to a single pulse bouncing back and forth between the conjugate ionospheres. This case corresponds to the beginning of our event.

A sharp halving of the repetition period on the ground can be related to a change in the generation regime in the magnetospheric cyclotron maser. This change could be caused by a variation in either energetic particle population in the generation region or the VLF wave reflection in one or both hemispheres. We did not notice any strong changes in the energetic particle population detected by VAP-A. Therefore, if the spacecraft crossed the source region during PE observations, the change in the generation regime was probably related to the ionospheric reflection change. Indeed, the local time of the event approximately corresponded to the solar terminator passing.

Another factor that could be related to the generation regime change is an increase in the wave power that is evident from ground-based observations (Figure 3d). We cannot say whether this increase is caused by magnetospheric conditions or ionospheric reflection but, in its turn, it can incluence the ionospheric reflection via precipitating electron flux (Villalon et al., 1989).

A good agreement between the calculated one-hop whistler time and the pulse pe-292 riod, as well as the sharp halving of the repetition period speak in favor of the passive 293 mode locking regime. On the other hand, quantitative development of this model was done by using bounce-averaged equation for the energetic electron distribution function. 295 Calculated bounce times for the low pitch-angle resonant electrons shown in Figure 4 296 are close to the wave hop times. Therefore, the model of Bespalov (1984); Bespalov et 297 al. (2010) requires an improvement taking into account bounce resonance effects, in or-298 der to be quantitatively applicable for the reported event. Recall that the idea to relate 299 PE period with the electron bounce period was suggested by Dowden (1962). 300

301 5 Conclusions

In summary, we have observed periodic VLF emissions at VAP-A and ground-based 302 stations KAN and LOZ. To our knowledge, this is the first report on conjugate obser-303 vation of periodic emissions in the near-equatorial magnetosphere and on the ground, 304 although this emission type is well known since 1960s from ground-based observations. 305 The similarity of dynamic spectra of individual pulses for the entire event lasting more 306 than an hour distinguishes periodic emissions from multi-hop whistlers. The repetition 307 period on the ground was 4 s in the first part of the event, and it halved sharply for the 308 second part, while the power repetition period onboard VAP-A was 2 s during the en-300 tire event. These periods and delays between the wave pulses detected on the ground 310 and by VAP-A are consistent with field-aligned propagation of whistler mode waves. Halv-311 ing of the repetition period corresponded to a change from the regime with a single wave 312 packet bouncing back and forth along the field line to the other regime, with two wave 313 packets propagating symmetrically in time that synchronously meet at the equator. The 314 Poynting flux direction remained the same in the second regime, which implies that one 315 of the two wave packets had slightly higher amplitude. Both observed regimes are con-316 sistent with a model of passive mode locking in the magnetosphere whistler-mode cy-317 clotron maser, and a sharp transition from one regime to the other could occur to the 318 change in the ionospheric reflection of VLF waves related to the terminator crossing. 319

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