# Evidence on a Class of Azimuthally Propagating Dipolarization Structures in the Earth's Magnetosphere from 4 to 30 Re

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#### Abstract

We report observational evidence for a class of coherent magnetic dipolarization structures that are long lived and radially extensive. The reported dipolarization structures, a subset of general dipolarizations, typically remain coherent over 20-30 min in real time, 3-6 hours in MLT, and 10-20 Re in radial distance. Arrays of more than three spacecraft in non-collinear geometry are used to determine the propagation vector, including both the normal speed and direction, of such dipolarizations in the equatorial plane. The determined azimuthal propagation is ~3 deg/min, which corresponds to ~50 km/s at 6.6 Re. This speed is consistent with those obtained from two azimuthally separated spacecraft in previous works. Further analysis suggests that these azimuthally propagating dipolarizations (APDs) are often finger-like in shape, ranging from 5 to 20 Re in length and several Re in width. The reported APD may accompany the earthward flow channel and dipolarizing flux bundle (DFB).

# Evidence on a Class of Azimuthally Propagating Dipolarization Structures in the Earth's Magnetosphere from 4 to 30 Re

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# Key Points:

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10	•	A class of dipolarizations propagate azimuthally at 3 deg/min, or 50 km/s at
11		6.6 Re
12	•	The azimuthally propagating dipolarizations (APDs) are finger-like: $\sim 2$ Re wide
13		and up to 20 Re long
14	•	APDs often propagate away from midnight, sweep over 3-6 hours in local time
15		in 20-30 min

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#### 16 Abstract

We report observational evidence for a class of coherent magnetic dipolarization struc-17 tures that are long lived and radially extensive. The reported dipolarization structures, 18 a subset of general dipolarizations, typically remain coherent over 20-30 min in real 19 time, 3-6 hours in MLT, and 10-20 Re in radial distance. Arrays of more than three 20 spacecraft in non-collinear geometry are used to determine the propagation vector, 21 including both the normal speed and direction, of such dipolarizations in the equato-22 rial plane. The determined azimuthal propagation is  $\sim 3 \text{ deg/min}$ , which corresponds 23 to  $\sim 50$  km/s at 6.6 Re. This speed is consistent with those obtained from two az-24 imuthally separated spacecraft in previous works. Further analysis suggests that these 25 azimuthally propagating dipolarizations (APDs) are often finger-like in shape, ranging 26 from 5 to 20 Re in length and several Re in width. The reported APD may accompany 27 the earthward flow channel and dipolarizing flux bundle (DFB). 28

#### <sup>29</sup> 1 Introduction

Dipolarization describes the sudden change of the Earth's magnetic field from a 30 stretched to dipole configuration. Consequently, the accepted observational signature 31 of a dipolarization is the sudden increase of the poloidal tilt angle of the magnetic 32 field (Nagai, 1982; Ohtani et al., 2018). Since early observations (Cummings et al., 33 1968), dipolarization has been a focus of attention because it plays a central role in 34 the energy release in the Earth's magnetotail (Lui, 1996; Angelopoulos et al., 2008). 35 It has been extensively studied from the MHD (magnetohydrodynamic) scale down to 36 kinetic scales (Fu et al., 2020, and references therein). In this paper, we focus on the 37 spatial evolution of dipolarizations and determine the propagation speed and direction 38 and related MHD scale properties. Such information is crucial in understanding how 39 dipolarization couples the Earth's magnetosphere and ionosphere. 40

Ohtani et al. (2018) studied the azimuthal evolution of dipolarizations within 41 and around 6.6 Re using the technique of 2-spacecraft timing on the tilt angle data. 42 The authors found that, statistically, the azimuthal phase speed of the propagation is 43 30-50 km/s and divergent around midnight. The phase speed and divergent pattern 44 are consistent with an earlier study at 6.6 Re (Nagai, 1982). However, due to the lim-45 itations of 2-spacecraft timing, the full propagation vector has not yet been examined. 46 For example, in Figure 1, the phase speed along the line connecting spacecraft 1 and 47 2 is 48

$$|\vec{v}_{1,2}| = |\vec{v}_n|/(\hat{v}_n \cdot \hat{s}_{1,2}),\tag{1}$$

which is often larger than the normal speed  $|\vec{v}_n|$ . This argument also applies for any number of co-linear spacecraft. In this paper, we extend the earlier studies by adopting the technique of 3-spacecraft timing to explicitly determine the full propagation vector and by studying a broader region from 4 to 30 Re.

Two dipolarization related structures have been proposed and extensively studied 53 beyond 6.6 Re. A dipolarizing flux bundle (DFB) or dipolarization front is a 3D flux 54 tube (Liu et al., 2013, 2014), which has an equatorial cross section of about 2 Re wide 55 and long (c.f. Figure 10). In addition, both smaller (0.3 Re, (Nakamura et al., 2002)) 56 and larger (3-4 Re, (Huang et al., 2015)) azimuthal widths have been reported in 57 case studies. A DFB probably propagates earthward because timing around midnight 58 shows that its earthward phase speed is about 300-500 km/s (Runov et al., 2009, 2011) 59 and because DFBs are typically accompanied by earthward bursty bulk flows (BBFs) 60 (Baumjohann et al., 1990; Angelopoulos et al., 1992) at a similar speed. However, a 61 Cluster study shows that earthward BBFs may also be observed with an azimuthally 62 propagating dipolarization front (Nakamura et al., 2002). The second type is related 63

to the azimuthal and tailward expansion of the dipolarized region (Baumjohann et al.,
1999; Nakamura et al., 2011). The proposed explanation is the pileup of magnetic
flux due to the earthward BBFs and DFBs. This explanation is supported by tail
observations and MHD simulations (Sigsbee et al., 2005; Birn et al., 2019; Merkin et al.,
2019). In Section 5, we will discuss the relation between the azimuthally propagating
dipolarizations reported herein to these two types of dipolarizations structures.

In this paper, we describe a statistical study of the propagation direction and 70 speed of dipolarizations in the equatorial plane from 4 to 30 Re. We search for events 71 when >3 spacecraft observe similar dipolarization signatures, so that the propaga-72 tion vector can be robustly determined using multiple combinations of 3 non-collinear 73 spacecraft. Using this propagation velocity, other important properties can be de-74 termined, including the azimuthal width, radial extent, life-time, and propagation 75 extent. We report evidence for a class of dipolarizations which propagate azimuthally 76 and extend well beyond geosynchronous orbit, reaching to 30 Re in some events. The 77 observed properties suggest a new scenario for how dipolarizations propagate in the 78 magnetotail. A discussion on the limitations of our dataset is also included. 79

#### 80 2 Instrumentation

The primary data set to analyze dipolarizations is the DC magnetic field. There 81 are 11 spacecraft available in the region of interest with a DC magnetometer, including 82 the 2 Van Allen Probes (RBA/B) launched in 2012 (Kletzing et al., 2013), the 5 83 THEMIS spacecraft (THA/B/C/D/E) launched in 2007 (Auster et al., 2008), the 3 84 GOES spacecraft (G13/14/15) launched in 2006-2010 (Singer et al., 1996), and the 4 85 MMS spacecraft launched in 2015 (Torbert et al., 2016). Only MMS1 is used since 86 the MMS separations are too small for definitive timing. All magnetic field data are 87 down-sampled to a common cadence of 10 sec, to facilitate a uniform treatment in 88 later calculations. 89

The apogees of the spacecraft we use are at 5.8 Re, 6.6 Re (circular orbit), and 90 beyond 10 Re for the RBSP, GOES, and THEMIS/MMS missions, respectively. As 91 a result of the apogee separation, the spacecraft utilized for each event cover a large 92 area of the equatorial plane, typically on the order of 3-6 hr in MLT  $\times$  5-20 Re in 93  $R_{xy}$ . These spacecraft can be off the magnetic equator by ~20 deg due to the wobble 94 of the earth's dipole axis. We will show that this z-separation from the magnetic 95 equator introduces a significant error in timing along the radial direction but not 96 in the azimuthal direction. We define the error  $\delta MLT$  and  $\delta R_{xy}$  as the difference 97 between the in-situ position of a spacecraft and its equatorial footpoint in MLT and 98  $R_{xy}$  respectively. For all the dipolarizations studied in this paper,  $\delta R_{xy}$  is 1.5 Re on 99 average. Its standard deviation is 2.5 Re and its maximum absolute value is 16 Re. 100 These results show that the error in  $R_{xy}$  due to the z-separation is comparable to the 101 typical range in radial distance (5-20 Re) and thus the error is significant. These results 102 are based on the mapping with the T89 model but other models provide essentially 103 the same results. Similarly,  $\delta MLT$  is 0.02 hr on average. Its standard deviation is 0.08 104 hr and its maximum absolute value is 0.4 hr. These results are much smaller than the 105 range in MLT (3-6 hr) and thus the error due to the z-separation in azimuthal timing is 106 negligible. Therefore, we primarily study the azimuthal propagation of dipolarizations 107 with this dataset. Throughout our paper, we use the in-situ positions to perform 108 timing because they do not include the possible errors associated with the equatorial 109 footpoints. The reported dipolarization structures would be more radially extensive if 110 the equatorial footpoints were used (Apatenkov et al., 2007). 111

#### **3 Example Events**

Figure 2 shows a dipolarization event on August 28, 2014 when an individual 113 dipolarization was observed by 6 spacecraft. The left hand panels show the detrended 114 tilt angle  $\theta$  of the measured magnetic field at each satellite. The dipolarization, seen as 115 the ramp of increasing  $\theta$ , lasted for 5-10 min at each satellite while remaining coherent 116 for over  $\sim 30$  min. The spacecraft were distributed in the post-midnight sector over 6 117 hours in MLT and from 5 to 12 Re (Figure 3f). As discussed in Appendix A, for each 118 dipolarization, we determine its major properties including the duration  $\Delta T$ , the net 119 tilt angle change  $\Delta \theta$ , and the "ramp time" (the center time of the ramp). Appendix 120 A also presents the method used to remove background magnetic field changes and 121 identify dipolarizations. The right hand panels in Figure 2 show the  $\theta$  data are aligned 122 based on the ramp time. The time lag of the ramp times is consistent with results 123 from cross-correlation, as presented in Appendix B and Figure 13. Several interesting 124 features can be seen in Figure 2. The dipolarization remained coherent for  $\sim 30$  min. 125 The change of tilt angle was about 40-50 deg near local midnight (panel a-1 and a-2), 126 about 30 deg around 2 MLT (panel a-4), and below 10 deg around dawn (panel a-5 127 and a-6), suggesting an azimuthal decay of  $\Delta \theta$  in MLT. Similar characteristics are seen 128 in the other events in this section and the larger data set described in Section 4. 129

Figure 3 displays how we determine the dipolarization propagation and the rele-130 vant properties. To relate the time and location of the dipolarization observations, the 131 detrended tilt angle  $\theta$  in Figure 2 are re-plotted in Figure 3c and 3d, color-coded along 132 the spacecraft tracks in MLT and  $x_{SM}$  respectively. Panel 3b uses the same color-133 coding to show the data for 16 hours around the event in panel 3c and 3d. The longer 134 period was during the recovery phase of a geomagnetic storm and contained two large 135 substorms when AE exceeded 1000 nT (Figure 3a). In Figure 3b, several examples are 136 marked when dipolarizations were seen to "drift" in MLT away from midnight. Such 137 drifts in MLT were very common during this and other storms/substorms. 138

Figure 3f shows the propagation velocity  $\vec{v}_n$  determined from 3-spacecraft timing. In the equatorial plane (Figure 1), we have

$$\begin{aligned} (\vec{r}_1 - \vec{r}_2) \cdot \hat{v}_n &= |\vec{v}_n| (t_1 - t_2) \\ (\vec{r}_1 - \vec{r}_3) \cdot \hat{v}_n &= |\vec{v}_n| (t_1 - t_3), \end{aligned}$$

$$(2)$$

where  $t_{1,2,3}$  is the ramp time of the dipolarization at spacecraft 1, 2, and 3 and  $\vec{r}_{1,2,3}$ 141 is the corresponding location. This is a linear equation in  $\hat{v}_n/|\vec{v}_n|$ , which is solvable 142 when 1, 2, and 3 are non-collinear and when the time lags are well determined.  $\vec{v}_n$  is 143 then obtained from  $\hat{v}_n/|\vec{v}_n|$ . Non-collinearity requires that a triangle formed by the 3 144 spacecraft cannot be too acute or obtuse. We require that triangles to have all angles 145 within 15 and 165 deg. Figure 3f shows an example of a triangle of good geometry 146 in the August 28, 2014 event, and Figure 4e shows all triangle combinations of both 147 good and bad geometries for a different event. In addition, we use the ramp times to 148 calculate the time lag between any two spacecraft. For the purpose of error control, 149 time lags are independently determined from cross-correlation. The  $\vec{v}_n$  vectors of a 150 certain triangle calculated from the two methods are required to be consistent: the 151 difference in magnitudes <20% and in directions <30 deg. In this study, we define a 152 "triad" as a triangle when both the geometry and timing criteria are satisfied. 153

In the August 28, 2014 event, there are  $20 (C_6^3)$  possible triangles. Applying the above criteria results in 13 triads where reliable timing can be obtained, corresponding to the 13 vectors in Figure 3f. The ramp times of the dipolarization at the 6 spacecraft are marked by the boxes in Figure 3 panels c and d and listed in Figure 2. Note that although we place no restriction on the size of a triad, the typical separation among spacecraft in a triad is larger than 1 Re. Our dataset is dominated by triangles with large spacecraft separations. This is when the ramp times are well separated and thus clearly resolved. For this reason, although TH-A/D/E routinely form local triangles, these triangles do not contribute much to the dataset because they often do not pass the timing criteria.

The velocity vectors show that the dipolarization propagation is everywhere az-164 imuthal for this event. Because the propagation was azimuthal, we can quantify the 165 azimuthal speed by fitting the ramp times and the corresponding MLTs to calculate the 166 angular speed. Figure 3c shows that the angular speed is -2.1 deg/min, where negative 167 value means eastward. We note that each velocity vector in Figure 3f is calculated 168 from the corresponding triad (e.g. the triad of G15/THD/THE). The magnitude of a 169 velocity vector is thus significantly averaged over the triad. For this reason, the az-170 imuthal motion is more accurately determined by the linear fit. In Figure 3c, a linear 171 fit is performed for the observed times of the dipolarization at each spacecraft and 172 the corresponding MLTs. The  $r^2$  of the linear fit is 1, suggesting that the azimuthal 173 propagation was close to a pure rotation. The angular speed scales to  $\sim 25$  km/s at 6.6 174 Re, which is comparable to the typical azimuthal phase speed of 30-50 km/s measured 175 from 2-spacecraft timing (Nagai, 1982; Ohtani et al., 2018). 176

To estimate the azimuthal width of the dipolarization, which refers to the region 177 of increasing tilt angle, we define the angular width  $W = |\omega_{2D}| \min(\Delta T_i)$ , where 178  $\Delta T_i$  is the duration of the individual dipolarization at the satellites. In this event, 179 W = 10 deg, which converts to an azimuthal width  $W' = W \cdot 10$  Re  $\sim 1.8$  Re at the 180 distance of 10 Re. W' is comparable to the typical value of 2 Re in previous studies 181 (Liu et al., 2013; Huang et al., 2015). In addition, the spatial distribution of the 182 spacecraft provides the lower limit of the radial and local time extent. Given that the 183 propagation is determined as azimuthal, the local time extent (6 hr) is the minimum 184 extent of the propagation whereas the radial extent (7 Re) is the minimum length of 185 the structure. Based on these observations, the observed dipolarization was a finger-186 shaped structure, about 1.8 Re wide and at least 7 Re long (light blue region in Figure 187 3f), which propagated azimuthally from the local midnight to at least dawn (the blue 188 arrow in Figure 3f). Figure 3d shows that misleading results can be obtained when 189 only radial cuts of the data are examined. In this case, one would conclude that the 190 dipolarization was first observed around 7 Re and propagated inward and outward. 191 However, examination in both the azimuthal and radial directions shows that this is 192 not the case for the August 28, 2014 event. 193

Figure 4 shows a similar event on January 09, 2008 in the post-midnight sector 194 during a minor substorm at 11:40 UT (panel a). The propagation vectors can be 195 determined at 3 triads (panel d) and again show an azimuthal propagation. A linear fit 196 shows that the azimuthal propagation is close to a pure rotation (high  $r^2 = 0.92$ ), with 197 an angular speed of -1.6 deg/min (from linear fit, panel b). This value is consistent 198 with  $\omega_{2D} = -1.9 \pm 0.1$  deg/min, which is averaged from the velocity vectors. The 199 angular width of the dipolarization was W = 10 deg, which scales to W' = 1.8 Re at 200 10 Re. The dipolarization was seen over 10 Re (10-20 Re, panel d), 2 hours in MLT 201 (panel b), and 15 minutes in real time. Due to limitations related to available satellites 202 and their orbits, a given event covers either a large radial distance but limited local 203 time or a limited radial distance but large local time. The January 09, 2008 event is 204 205 an example of the former whereas the August 28, 2014 event is the latter.

Two additional events in the pre-midnight sector are shown in Figure 5 and 206 6. Both events were associated with substorms of AE > 500 nT. In the March 28, 207 2017 event (Figure 5), an individual dipolarization was seen by 5 spacecraft during 208 15 minutes in real time. It propagated westward at an angular speed of 4.4 deg/min 209 (linear fit, Figure 5b). The angular width was 8 deg, which scales to W' = 1.4 Re 210 at 10 Re. The propagation was seen at least over 6 Re (6 to 12 Re) and 5 hours 211 in MLT (-2 to -7 MLT, Figure 5b). In the February 29, 2008 event (Figure 6), an 212 individual dipolarization was seen to propagate westward at 9.1 deg/min (linear fit, 213

Figure 6b). The propagation was at least over 10 Re (7 to 17 Re) and 4 hours in MLT (0 to -4 MLT). The angular width of this dipolarization (47 deg) is much larger than the previous dipolarizations. The statistical survey discussed in Section 4 shows that the angular width is typically 10 deg but can be much larger as in the February 29, 2008 event.

In the examples in Figures 3 to 6, the dipolarizations propagated azimuthally 219 away from midnight, consistent with previous studies within geosynchronous orbit 220 (Nagai, 1982; Ohtani et al., 2018). However, there are "unusual" dipolarizations that 221 propagate azimuthally toward midnight most often in the pre-midnight sector. Figure 222 7 shows such an example on March 20, 2008. In this event, the angular speed was 223 -3.5 deg/min (linear fit, Figure 7b). The angular width was 8 deg. The propagation 224 was seen at least over 20 Re (8 to 28 Re) and 4 hours in MLT (-4 to 0 MLT). The 225 reason for the "unusual" dipolarizations is unknown. A possible interpretation is that 226 the center of the diverging propagation pattern sometimes shifts away from midnight. 227 For example, the dipolarization shown in Figure 7 was first seen around -3 MLT. 228 This is a possible location of substorm onset, which is likely to be the center of the 229 divergence. Another possibility is that the unusual dipolarizations arise from some 230 dayside processes (e.g., shock impact, dayside reconnection). For example, in Figure 231 15d, some eastward propagating dipolarizations are seen around -6 MLT, which is more 232 likely to be related to dayside processes than substorm onset. 233

#### <sup>234</sup> 4 Statistical Properties

We initially identified 61 coherent dipolarization events, as described in Appendix 235 C. Of those, 40 were azimuthally propagating, 66% eastward and 34% westward. The 236 other 21 were radially propagating. As shown in Figure 15d, the eastward events 237 (blue) are more often in the pre-midnight sector whereas the westward events (green) 238 are mostly in the post-midnight sector. The distribution of the azimuthal events 239 shows a diverging pattern where the separator is around [-3,0] MLT. Interestingly, this 240 coincides with the typical MLT of auroral substorm onset (e.g. Liou et al., 2002). 241 As discussed in Appendix C.5, there were also 21 events that propagated radially. 242 Due to potential errors in determining the radial velocity (Section 2), we focus on the 243 azimuthal events. 244

Using the same methods as in Section 3, we focus on the properties of the APDs 245 including the propagation velocity  $v_{2D}$ , the angular speed  $\omega$ , and the azimuthal width 246 W'. These quantities can be directly determined from the 3-spacecraft timing mea-247 surements. In addition, quantities including the life time  $\tau$ , which corresponds to when 248 the dipolarization is first and last seen by the involved spacecraft, and the propaga-249 tion extent in MLT and radial extent are also examined. Limited by the spacecraft 250 distribution, these quantities only provide the lower limit of the real temporal or spa-251 tial extent. Figure 8 shows the histograms of the properties for the 40 ADPs. The 252 azimuthal speed  $|v_{2D}|$  (panel d) is ~50 km/s and the angular speed  $|\omega|$  (panel e) is ~3 253 deg/min. These values are consistent with previous studies within and around geosyn-254 chronous orbit (Nagai, 1982; Ohtani et al., 2018). The azimuthal width W' (panel f) 255 is on the order of 3-4 Re, but can be >10 Re in cases like the February 29, 2008 event 256 (Figure 6). Panel a shows that the mean life time is at least 17 minutes. Panels b and 257 c show that the average radial extent is 7.6 Re and the average propagation extent 258 is 3.3 hr in MLT. In panel c, there are two peaks: one peak is around 5 Re, which 259 corresponds to the dataset covering 4-12 Re, and a second smaller peak around 20 Re, 260 which corresponds to the smaller THEMIS dataset covering 10-30 Re. The fact that 261 the peaks are around the radial extent of both data sets suggests that the radial extent 262 is likely to be much larger than the average value of 7.6 Re. In addition, as mentioned 263 in Section 2, the radial extend would be larger due to the z-separation around the 264 equatorial plane (Apatenkov et al., 2007). 265

Figure 9 shows the shape of all azimuthal dipolarizations in the equatorial plane. 266 The region refers to the ramps of increasing tilt angle. The azimuthal width in Figure 267 8f and the radial extent in Figure 8b are used. To draw the boxes, we use the angular 268 width determined through 3-spacecraft timing and assume it is the same over the full 269 radial extent. Figure 9 shows that the azimuthal dipolarizations are typically finger-270 like, but can be wide sometimes (e.g., the February 29, 2008 event, Figure 6). The 271 histogram insert shows the ratio of length over width. The average ratio is 2.8 and the 272 ratio is greater than 1 for most events. 273

#### <sup>274</sup> 5 Discussion and Conclusion

The propagation of dipolarizations in the magnetotail has been previously sta-275 tistically studied inside geosynchronous orbit (6.6 Re) and studies found slow ( $\sim 50$ 276 km/s) azimuthal phase speeds (Nagai, 1982; Ohtani et al., 2018). In addition, other 277 dipolarization related structures are known to propagate. Dipolarizing flux bundles 278 (DFBs) have a fast (500 km/s) earthward phase velocity (Runov et al., 2009, 2011; 279 Liu et al., 2013, 2014). Magnetic field pileups have a slow tailward and azimuthal 280 expansion (Baumjohann et al., 1999; Nakamura et al., 2011). The APDs in our study 281 have a typical angular speed of 3 deg/min, which scales to 30-50 km/s at 6.6 Re. This 282 value is consistent with the dipolarizations studied by Nagai (1982) and Ohtani et al. 283 (2018). Other similarities include the duration of the ramp of increasing tilt angle 284 (5-10 min) and the divergent pattern around midnight. Therefore, we argue that the dipolarizations previously observed around geosynchronous orbit are the earthward 286 portion of the APDs in our study. However, as we showed in Figure 9, the APDs can 287 extend well beyond geosynchronous orbit, often penetrating into the mid-tail (20-30 288 Re). 289

We propose a possible picture for dipolarization propagation in the magnetotail, 290 connecting the APDs reported herein to previously studied dipolarization structures 291 (c.f. Figure 10). DFBs have life times on the order of several minutes, which is the time 202 for earthward propagation at 500 km/s from 20 to 5 Re. After the first several minutes, 293 all the trailing magnetic flux tubes form a slice of dipolarized region around a certain 294 local time, corresponding to a finger-like cross-section in the equatorial plane. Two 295 APDs expand both eastward and westward, in the next 20-30 min. This is the time 296 for them to propagate from around midnight to local dawn and dusk at 3 deg/min. 297 Both DFB and APD contribute to the tailward and azimuthal transport of magnetic 298 flux, i.e., the expansion of the pileup region (Angelopoulos et al., 1996). 299

We note that the event criteria do not allow us to perform a robust study of 300 how dipolarization structures propagate around midnight. This is due to two reasons. 301 First, the 3-spacecraft timing technique requires a non-collinear geometry to robustly 302 determine the propagation velocity. However, since the THEMIS spacecraft are de-303 signed to line up around midnight, we have a low count of possible events around midnight. This can be seen in Figure 16 and is explained in Appendix C. Second, 305 timing along the earth-sun line shows that dipolarization structures around midnight 306 propagate primarily radially: DFBs earthward and pileups tailward. As mentioned in 307 Section 2, the z-separation of the spacecraft around the equator introduces significant 308 error in determining the radial propagation velocities. Therefore, we cannot directly 309 verify the tailward or earthward propagation for dipolarization structures around mid-310 night. However, a possible synthesis picture is described above and in Figure 10. 311

Despite these limitations, our analysis approach is well suited to study azimuthally propagating dipolarizations. Based on the determined propagation velocity, we determined the azimuthal width to be 2.3 Re on average and ranges typically from 0.5 to 5 Re (Figure 8f). The value and range are consistent with previous studies of direct (Liu et al., 2013; Huang et al., 2015; Nakamura et al., 2002) or indirect (Ohtani et

al., 2018) measurements. In addition, we show that the APDs are radially extensive 317 (7.8 Re on average, Figure 8c). This raises questions about how the magnetotail cou-318 ples to the auroral ionosphere. Dipolarizations around geosynchronous orbit are often 319 discussed in the context of current systems related to substorms (McPherron et al., 320 1973; Kepko et al., 2015, and references therein). It is thought that the region II 321 current couples the night auroral ionosphere to the near-earth tail. However, if 322 these dipolarizations are the earthward portion of ADPs, then they extend well into 323 the mid-tail, how such radially extensive dipolarizations are coupled to the ionosphere 324 needs further investigations. 325

Based on the azimuthal width and radial extent, we show that the azimuthally 326 propagating dipolarizations are often finger-like structures (Figure 9). The structure 327 refers to the region of increasing tilt angle, which is usually associated with high 328 magnetic gradients. Such structures provide a possible mechanism for transporting 329 energetic particles through gradient B drift, which is suggested in simulations (e.g. 330 Ukhorskiy et al., 2018; Gabrielse et al., 2017). In the August 28, 2014 event in Figure 331 3, the gradient associated with the dipolarization  $\nabla |B|$  ranges from 50 to 200 nT/Re. 332 This gradient is much larger than the gradient of 1 to 10 nT/Re associated with the 333 background magnetic field. The large gradient, presumably aligns with the 2D shape 334 of the dipolarization, provides an elongated radial channel for keV to MeV particles 335 to transport inward or outward. Furthermore, the APDs are enduring (last several 336 10s minutes) and can propagate well into the dayside. Sergeev et al. (2006) report 337 evidence for a diverging propagation of flapping motions in the magnetotail (10-30 338 Re). Although flapping events are explicitly excluded in our dataset (Section C), the 339 APDs have similar radial extent and propagation pattern as the flapping motion of 340 the plasma sheet. The similarities raise questions on the physical relation between the 341 two phenomena. 342

In summary, the propagation of dipolarizations in the Earth's magnetotail was 343 studied using 3-spacecraft timing. We provide observational evidence for a class of 344 dipolarizations that propagate azimuthally at the angular speed of  $\sim 3 \text{ deg/min}$ , which 345 scales to  $\sim 50$  km/s at 6.6 Re. These structures are often finger-like in shape, several Re 346 wide and 5-20 Re long. The structures sweep across the magnetotail during the course 347 of 20-30 min and often reach out well into the dayside. These observations raise ques-348 tions related to several fundamental processes during geomagnetic storms/substorms, 349 including the possible connection to other dipolarization structures (dipolarizing flux 350 bundle and pileup), the azimuthally propagating flapping motion of the plasma sheet, 351 a possible mechanism for efficient radial transport of keV to MeV particles through 352 gradient B drift, and the coupling to the auroral ionosphere. 353

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Figure 1. Measuring the 2D propagation speed  $\vec{v}_n$  of a dipolarization in the x-y plane using 3 non-collinear spacecraft. Note that the phase velocity  $|\vec{v}_{1,2}|$  measured by a 2-spacecraft timing is in general larger than  $|\vec{v}_n|$ , especially when the spacecraft separation is perpendicular to  $\vec{v}_{1,2}$ .

### Appendix A Method used to detrend tilt angles and identify dipolarizations

By definition, dipolarizations correspond to a sudden increase of the poloidal tilt 366 of the magnetic field. Therefore, dipolarization identification involves the detection 367 of the region over which the tilt angle increases, which we call the "ramp". The 368 change of tilt angle, which is the key information, needs to be extracted from the 369 background magnetic field change, which decreases more than one order magnitude 370 from within 6.6 Re to 10-30 Re. Thus, to enable inter-comparison at all distances, 371 the tilt angle of the measured magnetic field  $B_{x,y,z}$ , defined as  $\alpha_{\text{meas}} = \arcsin(B_z/|B|)$ 372 in the SM coordinate, is detrended as follow. A slowly varying background due to 373 the spacecraft motion within the earth's dipole field is estimated by the T89 model 374 (Tsyganenko, 1989) with default inputs, from which the associated model tilt angle 375  $\alpha_{T89}$  is calculated. The difference,  $\alpha_{meas} - \alpha_{T89}$ , is then detrended through a 60-min 376 boxcar average to remove residue offsets. Figure 11 illustrates the background removal 377 using an example at THD in the August 28, 2014 event. Panel a shows the original 378 tilt angle  $\alpha_{\text{meas}}$  (black) and panel b shows the detrended tilt angle  $\theta$  (black). The 379 background (=  $\theta - \alpha_{\text{meas}}$ ) is shown as the blue curve in panel a. It is clear that the 380 detrended tilt angle  $\theta$  retains the large scale fluctuations in the original tilt angle data. 381

Detection of ramps with the appropriate change in tilt angle is performed by an 382 automated algorithm based on the detrended tilt angle  $\theta$ . Because the detrended tilt 383 angle  $\theta$  fluctuates around 0 due to the boxcar averaging, a ramp is identified as a region 384 of positive slope about 0. As shown in Figure 11c, the start and end times  $(t_S \text{ and } t_E)$ 385 of the ramp are defined as where  $d\theta/dt$  exceeds its local standard deviation by 1 sigma. 386 Consequently, the algorithm further determines (1) the duration  $\Delta T = t_E - t_S$ , (2) the 387 change of tilt angle  $\Delta \theta = \theta(t_E) - \theta(t_S)$ , and (3) the "ramp time" =  $(t_E + t_S)/2$ . To 388 remove small scale fluctuations on top of the main ramp,  $\theta$  is smoothed over a 2-min 389 window (non-smoothed  $\theta$  are used in all other calculations). The smoothed version is 390 shown in Figure 11b (red). 391

A initial survey of the detected ramps showed that a small fraction of them were flapping events, boundary crossings, and ULF waves. These ramps are either quasiperiodic, or contain abrupt (< 1 min) and large (> 80 deg) changes in  $\Delta\theta$ . To exclude



Figure 2. The detrended tilt angle  $\theta$  in real time (left) and after removing the time lags (right), during the August 28, 2014 event. An individual dipolarization was observed at 6 satellites during the course of ~30 min. The duration of the ramp of increasing tilt angle ranged about 5-10 min at the satellites. The vertical dashed line in the left panels indicates the "ramp time" of the dipolarization at each satellite. Data in the right hand panels are aligned according to the ramp time. Details on detecting ramps and dipolarizations and detrending the tilt angle are explained in Appendix A.



Figure 3. The dipolarization signatures during the recovery phase of a storm on August 28 2014. Panel a shows the Dst and AE indices. Panel b shows the detrended tilt angle colorcoded along spacecraft trajectories in the UT-MLT plane.  $\theta$  is scaled by exp  $(-z^2/2)$ , where z = MLT/4, to compensate the decay of  $\theta$  in MLT (c.f. Figure 12). Panel c zooms in to a section of panel b. Panel d shows the same data on the UT-X plane. Panel e shows with time lag removed (same data in Figure 2). The arrows indicate the ramp times in real time and bars on the left shows the y-scale. Panel f shows the velocity vectors of propagation at all triads. A triad is when a triangle is sufficiently non-collinear and 3-spacecraft timing can be robustly done. The foot of each arrow is at the center of the corresponding triad (e.g., the triad among G15/THD/THE). The inferred 2D shape of the dipolarization and its propagation extent are marked by the blue region and the curved arrow. As shown in panel f, the propagation was primarily azimuthal. Given that the propagation is, a linear fit is done for the ramp times and MLTs (panel c, dotted line) to quantify the angular speed. The high  $r^2$  of the linear fit suggests that the propagation is close to a pure rotation. Note that the vectors in panel f are not local velocities but averaged over the corresponding triad. For this reason, their magnitudes are all comparable. In principle, local speed should scale with distance for a pure rotation.



**Figure 4.** The dipolarization signatures and timing results for the January 09, 2008 event. Panel a-d are in the same format as panel a, c, e, f in Figure 3. Panel e-1 to e-4 show all 4 triangle combinations out of the 4 available spacecraft. 3-spacecraft timing is performed in the 3 triads of good geometry. This example shows another dipolarization in the post-midnight sector, which extended from 10 to 20 Re.



Figure 5. The dipolarization signatures and timing results for the March 28, 2017 event. Panels are in the same format in Figure 4. This examples shows a dipolarization in the pre-midnight sector.



Figure 6. The dipolarization signatures and timing results for the February 29, 2008 event. Panels are in the same format in Figure 4. This example shows a dipolarization which was very wide in azimuth.



Figure 7. The dipolarization signatures and timing results for the March 20, 2008 event. Panels are in the same format in Figure 4. This example shows a dipolarization propagated azimuthally toward the midnight.



**Figure 8.** Properties of the azimuthal dipolarizations. In each panel, the histogram shows the distribution of the property and the mean value is marked by the vertical line.



Figure 9. The 2D shape of all azimuthal dipolarization events. The events are differentiated by color, to help resolve overlapping shapes. For each event, the 2D shape is determined by the radial extent of the involved spacecraft and the angular width W. The center of the 2D shape is at the center of the MLT of the propagation extent. The figure and the histogram show that the structures are often finger-like and radially extensive. Note that the darker events often range from 5-12 Re, which is probably limited by spacecraft distribution.



**Figure 10.** A model to illustrate the azimuthal expansion of the dipolarization structures reported in this study. The azimuthal expansion is likely to be closely related to dipolarizing flux bundles, which have been extensively studied.

them, we select ramps that are isolated and with a clear step-up increase of tilt angle. 395 The criteria are: (1) the duration of the ramp  $\Delta T > 1$  min; (2) the change of tilt 396 angle  $\Delta \theta < 80$  deg; (3) the next ramp detected by the same spacecraft is after > 10 397 min; and (4) the tilt angle  $\theta$  remains positive > 8 min in total or >4 min continuously 398 in the same 10 min. In addition, to focus on the largest events, we select the ramps 399 with  $\Delta \theta \cdot e^{(MLT/4)^2/2} > 8$  deg. The scaling factor arises to compensate the decaying 400 trend of  $\Delta \theta$  in MLT. In Figure 12,  $\Delta \theta$  of 40,000 randomly selected ramps (before the 401 above criteria are applied) are binned every 2 hours in MLT. Percentile contours at 402 10%, 50%, and 90% levels of the sorted data over the bins show a decay in MLT. The 403 contours are empirically modeled by  $e^{-z^2/2}$ , resulting in a decay rate of  $z \sim MLT/4$ . Based on the percentiles, the criteria  $\Delta \theta \cdot e^{(MLT/4)^2/2} > 8$  deg selects the top 25% 404 405 ramps. In summary, ramps pass all above criteria are isolated dipolarizations with 406 significant jump in tilt angle and remain dipole-like after the jump. 407

#### <sup>408</sup> Appendix B Cross-correlation analysis on dipolarizations

Cross-correlation analysis is used to determine the coherency of dipolarizations 409 seen on 2 satellites and to limit the errors in the 3-spacecraft timing. The identifica-410 tion algorithm described in Appendix A not only identifies a dipolarization but also 411 determines its duration  $\Delta T$ , which is the width of the ramp of increasing tilt angle, 412 and its ramp time, which is the center time of the ramp. The window size for the cross-413 correlation is chosen to be 5 times the smallest of the  $\Delta T$  of the 2 dipolarizations. The 414 cross-correlation is calculated over this window size centered around the ramp time 415 for each satellite. Figure 13 shows the cross-correlation results for the dipolarizations 416 in the August 28, 2014 event. To follow the temporal evolution, the 6 dipolarizations 417 are sorted by their ramp times, forming 5 pairs for cross-correlation. In panels on 418 the right, the error associated with the cross-correlation is calculated according to 419 Equation (1.7) in Paschmann and W. Daly (2008)420



Figure 11. An example showing the algorithm to detect a ramp of increasing tilt angle and determine its properties. Panel a shows the tilt angle  $\alpha$  calculated from the measured magnetic field in solar magnetic (SM) coordinates. The T89 model of the earth's magnetic field is subtracted and the result is detrended using a boxcar average over 60 min. Panel b shows the detrended tilt angle  $\theta$ . A dipolarization corresponds to a positive slope centered around 0. To focus on the main ramp associated with a dipolarization, the tilt angle is smoothed over 2 min to remove small scale fluctuations. Panel c shows the derivative of the smoothed  $\theta$  (black) and its local standard deviation over 2 min (green). The start and end times ( $t_S$  and  $t_E$ ) of the ramp are identified as where  $d\theta/dt$  exceeds the local standard deviation by one sigma. Consequently, we define the duration  $\Delta T = t_E - t_S$ , the change of tilt angle  $\Delta \theta = \theta(t_E) - \theta(t_S)$ , and the "ramp time" =  $(t_E + t_S)/2$  for the ramp. In Appendix A, we further identify isolated ramps which correspond to dipolarizations, as quasi-periodical ramps correspond to flapping event, boundary crossings, and ULF waves.



Figure 12. Change of tilt angle  $\Delta\theta$  versus MLT for 40,000 randomly selected ramps identified in the region of interest. The  $\Delta\theta$  data are binned every 2 hours in MLT and sorted within each bin. Percentile contours at 10%, 50%, and 90% levels of the sorted data over the bins are plotted and empirically fitted by  $e^{-z^2/2}$ , resulting in a decay rate of  $z \sim MLT/4$ . To select the top 25% ramps, we use the criteria  $\Delta\theta \cdot e^{(MLT/4)^2/2} > 8$  deg.

$$(\mathrm{err})^2 = \frac{1}{M-1} \frac{1-cc}{cc} \frac{2\left\langle \delta\theta^2 \right\rangle}{\left\langle (d\theta/dt)^2 \right\rangle}$$

where M is the number of data points, cc is the maximum cross correlation,  $\langle \delta \theta^2 \rangle$ 421 is the average square of the deviation of from its mean value, and  $\langle (d\theta/dt)^2 \rangle$  is the 422 average slope square of  $\theta$ . Because the calculated uncertainty is typically much smaller 423 than the data rate (10 sec), it is not used in the error analysis. Instead, we require 424 that the timing results based on the two methods, cross correlation and ramp time 425 difference, must agree. For each triad, we require that the two methods to provide 426 consistent velocity vectors: (1) the magnitude difference is <20%; and (2) the angle 427 difference is < 30 deg. Because the criteria ensure that timing results are essentially 428 the same from the two methods, for simplicity, we use the timing results based on the 429 ramp times in the figures throughout this paper. 430

# A31 Appendix C Event Selection for Azimuthally Propagating Dipolar-A32 izations

The examples of dipolarization structures shown in Section 3 motivated a procedure to search for similar events. To robustly determine the propagation, the velocity vector is required to be consistently determined by at least two triads, involving a minimum of 4 spacecraft per event. The event selection procedure is summarized in Table 1, Figure 16, and described below.

#### 438 C.1 Step 1: Identify dipolarizations in ROI

For each satellite, we search for dipolarizations with a steady (> 1 min) and welldefined step-up ramp of the tilt angle (see Appendix A for further details). To exclude



Figure 13. Cross-correlation between spacecraft pairs in the August 28, 2014 event. In each row, the left panel plots the data within the window of cross-correlation after the proper time lag removed in black (red) for the first (second) satellite. The window size is 5 times the smallest of the  $\Delta T$  of the two dipolarizations. The right panel plots the cross-correlation as a function of time lag. The center of the x-axis is the difference between the ramp times of the two dipolarizations. The time lag corresponding to the maximum cross-correlation is marked by the vertical dashed line. The deviation from the center is the difference of time lags from the two methods: ramp time difference and cross correlation. The uncertainty of cross-correlation itself, calculated based on Equation (1.7) in Paschmann and W. Daly (2008), is listed in the right panels but not used for error analysis because it is much smaller than the data rate of 10 sec of the tilt angle  $\theta$ .

ID	# of DP	Rate	Description
1	$19,\!584$	N/A	All isolated DPs identified per involved spacecraft (SC).
2	1,909	10%	A subset of all, when an individual DP is seen by $>3$ SC,
			but also contains stochastic DPs which are transient or local.
3	737	38%	Coherent DP candidates, when an individual DP is seen by $>3$ SC and the propagation vectors are robustly
			determined. Stochastic DPs are removed through co-
			herency analysis.
4	274	37%	Coherent DP events, when the propagation is along a certain direction.

**Table 1.** Event selection procedure for dipolarizations (DPs). The "rate" refers to the ratio of the number of dipolarization in the previous over the current step.

ULF waves, flapping events, and boundary crossings, which include quasi-periodic 441 increases in the tilt angle, isolated dipolarizations are selected, where the satellite 442 sees no other dipolarization in 10 min. The search is within a "region of interest" 443 (ROI, c.f., Figure 16) between 4 and 30 Re radial distance and within  $\pm 9$  MLT of 444 midnight. In addition, the ROI was bounded using the Shu model of the magnetopause 445 (Shue et al., 1998) with a high dynamic pressure (10 nPa) as the input, to exclude 446 magnetopause crossings which may resemble dipolarizations. Two searches within 447 the ROI are performed. The first was between 4 and 12 Re over 5 years (Oct 2012) 448 to 2017) using RBSP-A/B, TH-A/D/E, GOES-13/14/15, and MMS-1. The second 449 search extended from 12 to 30 Re, using 2.5 years of data from TH-A/B/C/D/E. In 450 all, 19,584 dipolarizations on a single spacecraft level were identified (Figure 16a). As 451 expected, most dipolarizations are identified around the apogee of the spacecraft, for 452 example, around 10 Re for TH-A/D/E and around 20 Re for TH-C. Figure 14 shows 453 all dipolarizations identified during 4 hours around the August 28, 2014 event. The 454 figure also shows that although the identified dipolarizations are isolated, i.e., a given 455 spacecraft sees only 1 dipolarization in the 10-minute window, each dipolarization 456 as seen by different spacecraft could be either closely spaced in ramp time or very 457 separated in ramp time. 458

459

#### C.2 Step 2: Apply a mathematical filter to scale down the search

Figure 14 shows the construction of a spacecraft sequence, which is used to se-460 lect the dipolarizations which could provide robust 3-spacecraft timing (about 10%) 461 of all identified dipolarization). Dipolarizations are weaved together and sorted on 462 the basis of the ramp time, resulting in a spacecraft sequence that includes a set of 463 dipolarizations sorted on the basis of consistent spatial location and ramp time. The 464 spacecraft sequence is critical for selecting events because it carries information on how 465 the temporal evolution of a dipolarization can be observed by randomly distributed spacecraft. For example, a dipolarization which propagates in a certain direction can 467 be systematically seen by many spacecraft en route. Such a situation corresponds to 468 a section in the spacecraft sequence without a given spacecraft appearing more than 469 once in the sequence (i.e., seeing what must be two different dipolarizations), for ex-470 ample, the section of the first 6 spacecraft (THD-THE-G15-THA-RBB-G13) in Figure 471 14. In this study, we select the sections to contain >3 different spacecraft so that the 472 propagation direction and speed can be determined at at least two locations. The sec-473 tion (THD-THE-THA) at the end of the time interval is rejected because the section 474 contains only 3 spacecraft. The figure also shows another type of dipolarization, which 475 is stochastic in the sense that the dipolarization is local in space or time. For example, 476

the dipolarization around 12:30 UT is only seen by THA. The selected sections may 477 contain such stochastic dipolarizations. We eliminate sections that contain stochas-478 tic dipolarizations through coherency analysis as explained in Section C.3. Here we 479 emphasize that the spacecraft sequence is random, meaning not space/time ordered 480 in a consistent propagation sense. Because the spacecraft have very different orbits, 481 there is not always a consistent spacing in radial distance and local time. THA, THD 482 and THE are always consistently spaced in MLT for this interval, while the geosyn-483 chronous spacecraft may see a given event at any MLT. Based on the randomness, 484 the chance of finding a section with m different spacecraft when n spacecraft is avail-485 able in a random sequence is  $P_n^m/n^m$  (P for permutation). The theoretical selection 486 rate is  $c(n) = \sum_{m=4}^{n} P_n^m / n^m$ . In typical cases, the number of available spacecraft is 487 n = 4,5,6, thus c(4) = 9%, c(5) = 23%, c(6) = 33%. Figure 16b shows that the 488 actual selection rate is larger as more spacecraft are available closer to earth. The 489 actual selection rate tends to be smaller than the theoretical value because n could 490 be smaller than 4. In Figure 16b, the selection rates are 0 in the green bins because 491 the original counts are low (Figure 16a) and thus the expectation is  $\sim 0$ . In all, 606 492 sections containing 1,909 dipolarizations are selected, which corresponds to an average 493 selection rate of 10% (19,584 total). 494

#### 495

#### C.3 Step 3: Select coherent dipolarization candidates

Within each selected section, stochastic dipolarizations are eliminated by requir-496 ing that (1) dipolarization pairs adjacent in ramp time are within 30 min; (2) the 497 average time separation of all pairs < 8 min; and (3) the average cross-correlation of 498 all pairs >0.5. The first two criteria ensures that a propagating dipolarization is sam-499 pled consistently and continuously in time, whereas the third criterion ensures the 500 coherency. Note that although each dipolarization is isolated in the sense that no 501 other dipolarization is seen by the same spacecraft within 10 min, two dipolarizations 502 adjacent in ramp time and from different spacecraft can be close in time. Next, Equa-503 tion (2) is solved based on both the time difference of the ramp times and on the 504 time lags of maximum cross-correlation. As described in Section B, for each triad, 505 the two methods must agree to within 20% for the velocity magnitude and within 30 506 deg for direction. For simplicity, we use the velocity vectors based on the ramp time 507 difference in the paper. Using this approach, we identified 164 sections containing 737 508 dipolarizations on a single spacecraft level, which we call the "coherent dipolarization" 509 candidates. These are events when similar dipolarization signatures are seen at >3510 spacecraft and the propagation vectors can be robustly determined in >2 triads. The 511 selection rate is 38%, (737 selected from 1,909 dipolarizations, Figure 16c), providing 512 a crude estimation on the occurrence rate of what we defined to be a coherent dipolar-513 ization among general dipolarizations: for a certain isolated dipolarization observed by 514 a satellite, there is a high chance (38%) that the dipolarization propagates coherently 515 in space. 516

517

#### C.4 Step 4: Select coherent dipolarization events

Each of the 164 candidates contains at least two robustly determined propagation 518 519 vectors. 61 of them, which we call the coherent dipolarization events, show propagation in a consistent direction, i.e., the scatter of the vectors is small. Specifically, the 520 standard deviation of the direction is <20 deg and the standard deviation of the 521 magnitudes is <30% of the mean. The other candidates, however, contain inconsistent 522 velocity vectors, which could due to several reasons. For example, the propagation 523 vectors are diverging if the region enclosed by the spacecraft is where an individual 524 dipolarization develops. The propagation vectors could be inconsistent in direction for 525 a dipolarization with a corrugated phase front. In the rest of the paper, we will focus on 526 the 61 coherent dipolarization events, because they present the simple situation when 527

an individual dipolarization propagates along a certain direction within the region enclosed by the involved spacecraft.

530

# C.5 Azimuthally propagating dipolarizations

We have identified 61 coherent dipolarization events as described in the previous 531 sections. Of those, 66% (40 events) propagated primarily azimuthally (41% eastward 532 and 25% westward), while the rest 34% (21 events) propagated radially (21\% inward 533 and 13% outward). Figure 15 shows the distribution of the events in MLT. In the 534 figure, the azimuthal events are marked as the blue and green points and the radial 535 events are marked by purple and red points. The distribution of the points follows the 536 picture of cylindrical coordinate (radial-azimuthal, panels a and b), not the Cartesian 537 coordinate (x-y, panel c). 538

We note that although the propagation velocities in the 61 coherent dipolar-539 ization events are robustly determined, the robustness, referring to the 3-spacecraft 540 timing technique, can be affected by the z-separation around the magnetic equator. As 541 mentioned in Section 2, the z-separation primarily affects the radial but not azimuthal 542 propagation velocities. The z-separation may cause uncertainty in determining the 543 radial distance of the spacecraft in the magnetic equator. The uncertainty introduces 544 potential error in the radial speed, however, radial events are still radial because the 545 radial separation of the spacecraft is typically larger than the uncertainty, i.e., the 546 propagation direction is unlikely to be affected. Therefore it is interesting that the 547 number of radial events is roughly 1/2 of the azimuthal events. This is consistent with 548 the picture shown in Figure 15, where one radially propagating dipolarization is accompanied by two azimuthally propagating dipolarizations in eastward and westward. 550 In addition, a significant number of these radial events are propagating tailward. The 551 potential abundance of tailward propagating dipolarization has not been documented 552 before. The tailward propagation may be related to physical processes like the pile-up 553 of magnetic fluxes (Baumjohann et al., 1999) or near-earth reconnection (Angelopoulos 554 et al., 2020). 555



Figure 14. The location in MLT and UT of each dipolarization (red box) identified during this 4 hour interval around the August 28, 2014 event. The plot is in the same format as Figure 3b. For each spacecraft track, the corresponding spacecraft is explicitly marked, to illustrate how a spacecraft sequence is constructed from the dipolarizations identified on each spacecraft. The spacecraft sequence, obtained by sorting the dipolarizations using the ramp time for each spacecraft, is used to select the dipolarizations which could provide robust 3-spacecraft timing (Section C.2).



Figure 15. Direction of the velocity vectors  $\vec{v}_{2D}$  as a function of MLT for the coherent dipolarization events. Schematics of dipolarization propagate (a) azimuthally, (b) radially, and (c) sunward. They can be distinguished in (d) MLT vs  $\phi$ , where  $\phi$  is the angle between SM x-axis and  $\vec{v}_{2D}$ . In panel d, the four orthogonal directions in the polar coordinate are checked, including eastward (blue), westward (green), radially inward (red), and outward (purple). Each cross corresponds to a  $\vec{v}_{2D}$  vector. The vectors in one event are connected by gray lines. The majority of events are azimuthal (eastward/westward more often in post-/pre-midnight). The distribution of the radial events may not be statistically significant because the counts are low.



**Figure 16.** The distribution of dipolarizations and selection rate of each step in the event selection procedure as described in Section C. Panel a shows the distribution of all identified dipolarizations in the equatorial plane in step 1. The boundary of the region of interest (ROI) is marked by the black curves. Panel b shows the selection rate from step 1 to 2. The select rate of the green bins is 0. Similarly, panel c and d shows the selection rate from step 2 to 3 and from step 3 to 4, respectively. In panel d, the gap of dipolarization appears around midnight may suggest the propagation direction is more complicated around midnight (c.f. Section 5 for a more detailed discussion).

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Figure 1.



Figure 2.



Figure 3.



Figure 4.



Figure 5.



Figure 6.



Figure 7.



Figure 8.



Figure 9.



Figure 10.



Figure 11.



Figure 12.



∆θ (deg)

Figure 13.



Figure 14.



Figure 15.



Figure 16.

