Bayesian framework for inversion of second-order stress glut moments: application to the 2020 Mw 7.7 Caribbean Earthquake

James Atterholt¹ and Zachary E. Ross¹

¹California Institute of Technology

November 22, 2022

Abstract

We present a fully Bayesian inverse scheme to determine second moments of the stress glut using teleseismic earthquake seismograms. The second moments form a low-dimensional, physically-motivated representation of the rupture process that captures its spatial extent, source duration, and directivity effects. We determine an ensemble of second moment solutions by employing Hamiltonian Monte Carlo and automatic differentiation to efficiently approximate the posterior. Our method explicitly constrains the parameter space to be symmetric positive definite, ensuring the derived source properties have physically meaningful values. The framework accounts for the autocorrelation structure of the errors and incorporates hyperpriors on the uncertainty. We validate the methodology using a synthetic test and subsequently apply it to the 2020 Mw 7.7 Caribbean earthquake. The second moments determined for this event indicate the rupture was nearly unilateral and relatively compact along-strike. The solutions from this inverse framework can resolve ambiguities between slip distributions with minimal a priori assumptions on the rupture process.

Supplementary Figures

1



Figure S1. Kernel density estimate plots for multiple chains describing the distributions of independent components of the second moments of the stress glut for the 2020 Caribbean earthquake. Different colors (blue, red, and green) represent different chains of the inversion.



Figure S2. Distribution of hyperparameter σ determined in the inversion using real data and included in the inversion using synthetic data.

-1-

Bayesian framework for inversion of second-order stress glut moments: application to the 2020 M_w7.7 Caribbean Earthquake

James Atterholt¹ and Zachary E. $Ross^1$

¹Seismological Laboratory, California Institute of Technology, Pasadena, California, USA 91125

6 Key Points:

4

7	•	We develop a Bayesian inverse scheme to solve for stress glut second moments of
8		earthquakes using teleseismic data.
9	•	We sample the positive-definite constrained posterior distribution using Hamiltonian
10		Monte Carlo sampling and automatic differentiation.
11	•	Using the 2020 $M_w 7.7$ Caribbean Earthquake as an example, we demonstrate the
12		efficacy and utility of this inverse framework.

 $Corresponding \ author: \ James \ Atterholt, \verb+atterholt@caltech.edu$

13 Abstract

We present a fully Bayesian inverse scheme to determine second moments of the stress 14 glut using teleseismic earthquake seismograms. The second moments form a low-dimensional. 15 physically-motivated representation of the rupture process that captures its spatial extent, 16 source duration, and directivity effects. We determine an ensemble of second moment so-17 lutions by employing Hamiltonian Monte Carlo and automatic differentiation to efficiently 18 approximate the posterior. Our method explicitly constrains the parameter space to be 19 symmetric positive definite, ensuring the derived source properties have physically mean-20 21 ingful values. The framework accounts for the autocorrelation structure of the errors and incorporates hyperpriors on the uncertainty. We validate the methodology using a synthetic 22 test and subsequently apply it to the 2020 $M_w 7.7$ Caribbean earthquake. The second mo-23 ments determined for this event indicate the rupture was nearly unilateral and relatively 24 compact along-strike. The solutions from this inverse framework can resolve ambiguities 25 between slip distributions with minimal a priori assumptions on the rupture process. 26

27 Plain Language Summary

Earthquake science is presented with the challenging problem of determining properties 28 of earthquake sources that occur deep within the Earth using observations made at the sur-29 face of the Earth. Typically, the process for determining these important quantities involves 30 finding solutions to complicated optimization problems that, given the necessarily poor data 31 coverage, are poorly constrained. With this challenge in mind, we present a framework to 32 solve for some fundamental properties of earthquake sources like spatial extent, rupture 33 propagation direction, and duration. This approach requires few assumptions about the 34 geometry of the fault that ruptured and the dynamics of the rupture process, in contrast to 35 more traditional methods. This procedure also provides a probabilistic description of these 36 earthquake source properties, which is essential, because the uncertainty inherent to this 37 problem dictates that we cannot confidently choose any one particular solution. We demon-38 strate this method's utility by applying it to the 2020 Magnitude 7.7 Caribbean Earthquake. 39 Through this application, we show that this framework can both determine properties of 40 earthquake sources that have historically been difficult to constrain and successfully resolve 41 ambiguities between solutions of more traditional techniques. 42

43 Introduction

Earthquakes are complicated physical processes that dynamically vary in space and 44 time. Better understanding the factors that control earthquake behavior consequently re-45 quires constraining the finite source properties of earthquakes. In pursuit of this under-46 standing, high dimensional estimates of finite source properties are routinely computed for 47 significant earthquakes (e.g. Wald & Heaton, 1992; Ammon, 2005; M. Moreno et al., 2010; 48 Ide et al., 2011; Ross et al., 2019). These estimates usually involve the inversion for slip 49 on a predefined fault plane using some combination of seismic, geodetic, and tsunami data 50 51 with kinematic constraints placed on the rupture propagation (Hartzell & Heaton, 1983; Du et al., 1992; Saito et al., 2011). These solutions, termed fault slip distributions, are valuable 52 in that they provide a detailed image of time-dependent slip behavior. But, the necessary 53 user-defined parameterization, general lack of sensitivity to rupture velocity, and necessary 54 regularization makes these estimates of finite source properties strongly nonunique (e.g. 55 Lay, 2018). This nonuniqueness presents challenges to objectively comparing finite source 56 properties between events, and thus limits our ability to discern patterns in earthquake 57 behavior that could inform a deeper understanding of earthquake phenomenology. 58

The limitations of routinely computed estimates of finite source properties motivates 59 the development of alternative estimates that overcome these limitations. One potential al-60 ternative is the second moment formulation (G. Backus & Mulcahy, 1976a, 1976b), in which 61 higher-order mathematical moments of the stress glut, a source representational quantity, 62 are used to describe basic properties of the rupture process in space and time. Higher-order 63 stress glut moments have been successfully computed in the past (Bukchin, 1995; McGuire et 64 al., 2000, 2001, 2002; McGuire, 2004; Chen, 2005; Meng et al., 2020), but this methodology 65 has received little attention compared to slip inversions. The second-moment formulation 66 yields low-dimensional, physically-motivated estimates of the spatial extent, directivity, and 67 duration of earthquake ruptures. It requires no prior knowledge of the rupture velocity, 68 and makes only mild assumptions about the source geometry. Being free of gridding and 69 associated discretization issues that complicate slip inversions, the second moment formu-70 lation can more objectively facilitate comparisons between events, helping to find common 71 patterns. Illuminating these patterns may help address outstanding questions in earthquake 72 science relating to how fault zones may facilitate or impede earthquake ruptures. 73

Our contributions in this paper are as follows. We develop a Bayesian inverse scheme for 74 second moments using teleseismic data. We employ Hamiltonian Monte Carlo sampling and 75 automatic differentiation to efficiently sample from the posterior distribution. In doing so, we 76 apply a set of transformations that ensure positive definiteness of the second moments. We 77 demonstrate the efficacy of our methodology by applying the inversion scheme to the 2020 78 M_w 7.7 Caribbean Earthquake. We show that our methodology is useful for both inferring 79 source parameters that are poorly constrained by other source estimation procedures and 80 resolving ambiguities between finite slip distributions. 81

$_{82}$ Case study: the 2020 M_w7.7 Caribbean earthquake

Event background and tectonic summary

On January 28, 2020, a large earthquake occurred in the Caribbean Sea near the Cay-84 man Islands. The global Centroid Moment Tensor (gCMT) (Dziewonski et al., 1981; Ek-85 ström et al., 2012) solution of this earthquake suggests that the event was a largely double-86 couple, nearly vertically dipping, strike-slip earthquake with a moment magnitude of $M_w 7.7$ 87 (GCMT, 2020). The geographic setting of this event is shown in Figure 1. This event took 88 place near the northern margin of the Gonâve Microplate, an elongated plate that charac-89 terizes a portion of the boundary between the North American and Caribbean plates. The 90 dominant local structural feature in this region is the Mid-Cayman Rise, which produces 91 seafloor spreading that is partially accommodated by the transform faults that bound the 92 Gonâve Microplate (Mann et al., 1995; DeMets & Wiggins-Grandison, 2007). The centroid 93 location and focal mechanism of the Caribbean Earthquake suggest that this event likely ruptured the Oriente Fault, a left-lateral transform fault that constitutes the boundary be-95 tween the North American Plate and the Gonâve Microplate. Though the spreading rate 96 of the Mid-Cayman Rise is slow (DeMets & Wiggins-Grandison, 2007), the segments of 97 the Oriente Fault neighboring the Caribbean Earthquake have produced numerous M6+ 98 earthquakes in recent history (Van Dusen & Doser, 2000; B. Moreno et al., 2002). 99

Despite its large magnitude, there are few finite rupture solutions for the Caribbean 100 Earthquake to date (USGS, 2020; Tadapansawut et al., 2021). Though these solutions agree 101 that the Caribbean earthquake likely ruptured unilaterally to the SW along the Oriente 102 Fault, there is no consensus on some fundamental source parameters, such as the rupture's 103 lateral extent. In particular, the USGS solution for this event suggests that most of the 104 slip was confined within an 80 km length along the fault, while the Tadapansawut et al. 105 solution suggests a much larger slip region that extends well over 300 km. Thus, in addition 106 to producing statistically robust estimates of rupture characteristics, this second moment 107 formulation may prove useful in resolving first-order differences between slip distributions. 108

109 Data

83

In this study we use vertical component seismic data from 52 Global Seismographic 110 Network (GSN) stations (Figure 1). We selected these stations by evaluating how well the 111 waveforms were approximated by point source synthetics computed using the gCMT so-112 lution. The seismograms used in the inversion are 700 second windows about the surface 113 wave packet that we manually selected from 7200 second windows that start at the gCMT 114 centroid time for the Caribbean Earthquake. We down-sample the waveform data to 0.1 Hz115 sampling rate to somewhat reduce the correlation between samples, while keeping computa-116 tional demands minimal. As part of the construction of the forward propagation matrix, we 117 computed the Green's tensor using the gCMT moment tensor and centroid location, which 118 we perturbed to compute the requisite spatial derivatives numerically. 119

120 Methodology

121 Stress Glut Moments

Because an earthquake is constituted by a localized zone of inelastic deformation, we 122 can represent the source region as a localized departure from elasticity. These departures 123 can be quantified using the so-called stress glut, Γ , the tensor field computed by applying 124 an idealized Hooke's law to the inelastic component of strain in a system (G. Backus & 125 Mulcahy, 1976a, 1976b). The stress glut is nonzero only within the source region. The 126 stress glut is a complete representation of a seismic source in space and time that can be 127 used to reproduce displacements everywhere on Earth for an arbitrary source (Dahlen & 128 Tromp, 1998). Given the typically sparse distribution of seismic observations, solving for 129 the full stress glut is an ill-posed problem. We can simplify the stress glut by assuming the 130 source geometry is constant in space and time: 131

$$\Gamma_{ij}(\xi,\tau) = \hat{\mathbf{M}}_{ij}f(\xi,\tau) \tag{1}$$

Where is $\mathbf{\hat{M}}$ is the normalized mean seismic moment tensor and f is the scalar function. This approximation reduces the solution from a tensor field to a scalar field and is most valid for seismic sources with stable source mechanisms.

We can further reduce the dimensionality of the stress glut by first recognizing that 135 any scalar function in a bounded interval may be uniquely determined by its collection of 136 polynomial moments. Because f captures a static displacement, f is nonzero for infinite 137 time and thus occupies an unbounded interval, but f vanishes to zero at the cessation of 138 rupture and is thus captured within a bounded interval. Hence, considering that the stress 139 glut prescribes displacements due to an arbitrary seismic source, we can represent seismic 140 displacements as the superposition of the spatio-temporal moments of the rate function f. 141 At low frequencies, we can truncate this infinite series such that we only include terms with 142 moments of order $m + n \leq 2$. We can then explicitly define the measured displacements for 143 a station i at low frequencies as: 144

$$u_{i}(\mathbf{r},t) = \dot{f}^{(0,0)}(\xi_{c},\tau_{c})\mathbf{M}_{jl}\frac{d}{d\xi_{l}}\int_{-\infty}^{+\infty}\mathbf{G}_{ij}(\xi_{c},\tau_{c},\mathbf{r},t)dt$$

$$-\dot{f}_{m}^{(1,1)}(\xi_{c},\tau_{c})\mathbf{M}_{jl}\frac{d}{d\xi_{m}}\frac{d}{d\xi_{l}}\mathbf{G}_{ij}(\xi_{c},\tau_{c},\mathbf{r},t)$$

$$+\frac{1}{2}\dot{f}_{mn}^{(2,0)}(\xi_{c},\tau_{c})\mathbf{M}_{jl}\frac{d}{d\xi_{m}}\frac{d}{d\xi_{l}}\frac{d}{d\xi_{l}}\int_{-\infty}^{+\infty}\mathbf{G}_{ij}(\xi_{c},\tau_{c},\mathbf{r},t)dt$$

$$+\frac{1}{2}\dot{f}^{(0,2)}(\xi_{c},\tau_{c})\mathbf{M}_{jl}\frac{d}{d\xi_{l}}\frac{d}{dt}\mathbf{G}_{ij}(\xi_{c},\tau_{c},\mathbf{r},t)$$
(2)

Where **G** is a Green's tensor prescribing the path effects from a source with the centroid location ξ_c and centroid time τ_c to an arbitrary station with the location **r** at time *t*, and $\dot{f}^{(m,n)}(\xi_c, \tau_c)$ is the moment of the scalar rate function $\dot{f}(\xi, \tau)$ of spatial order *m* and temporal order *n* taken about the source centroid in space and time (Bukchin, 1995).

Several of the moments are of routine use in seismology, while the rest are worked with 149 sparingly. The moment of order m+n=0 is the scalar moment of the source. The moments 150 of order m + n = 1 correspond to the spatial (m = 1) and temporal (n = 1) centroids of the 151 source. Perhaps unfamiliar are the moments of order m + n = 2; these moments describe 152 low-dimensional finite properties of earthquake sources. In particular, $\dot{f}^{(2,0)}(\xi_{\mathbf{c}},\tau_c)$ is the 153 spatial covariance of the stress glut, $\dot{f}^{(1,1)}(\xi_{\mathbf{c}},\tau_c)$ is the spatio-temporal covariance of the 154 stress glut, and $\dot{f}^{(0,2)}(\xi_{\mathbf{c}},\tau_c)$ is the temporal variance of the stress glut. These so-called 155 second moments yield low-dimensional, physically-motivated approximations of the source 156 volume, source directivity, and source duration respectively (G. E. Backus, 1977). 157



Figure 1. Left: Geographic setting of the 2020 Caribbean earthquake. Focal mechanism is the gCMT solution for the 2020 Caribbean earthquake. Gray dots indicate the locations of USGS cataloged aftershocks for the event. Red line indicates the boundary between the North American and Caribbean plates (Bird, 2003). Map coloring is reflective of seafloor depth. Right: Global distribution of stations from which waveforms were used in this study.

158 Waveform preprocessing

To compute the Green's tensor, we use the Preliminary Reference Earth Model (PREM) 159 (Dziewonski & Anderson, 1981) and the normal mode summation package Mineos (Masters 160 et al., 2011). To improve stability when approximating integrals and derivatives, we compute 161 this Green's tensor at a high sampling rate (20 Hz). We take the necessary temporal and 162 spatial derivatives and integrals of this Green's tensor numerically using a centered finite 163 difference approximation. For the spatial derivatives, the finite difference offsets from the 164 spatial centroid are 250 m. The construction of the forward propagation matrix described 165 in this study require both the gCMT moment tensor and the Green's tensor derivatives and 166 integrals. 167

We bandpass the observed waveforms and green tensor between 100 and 200 seconds 168 and perform a visual quality control by comparing the displacements of the synthetic point 169 source representation of our source with the observed waveforms. Because the contribution 170 of moments of order $m + n \ge 2$ should be small, the synthetic waveforms produced using a 171 point source approximation should be similar to the observed waveforms. We thus remove 172 stations that did not show a good match between the synthetic point source displacements 173 and the observed waveforms. We then align the Green's tensor and observed displacements 174 of the remaining stations via cross correlation, and we manually pick the arrivals of and 175 determine the window lengths for the surface wave packets at each station. These windows 176 constitute the time-segments of the Green's tensor and observed waveforms included in the 177 forward propagation matrix and data vector used in this study respectively. 178

179 The Inverse Problem

Though equation 2 appears unruly, many of the terms that constitute it are easily accessible. For a given source, we can observe $u_i(\mathbf{r}, t)$ using seismic instrumentation; we can solve for **G**, **M**, and (ξ_c, τ_c) using routine techniques; and we can compute the necessary derivatives and integrals using numerical methods. Thus, in equation 2, only the moments of the scalar function \dot{f} are unknown. We can then pose equation 2 as a linear inverse problem:

$$\mathbf{d} = \mathbf{F}\mathbf{p} \tag{3}$$

where **d** is a vector of measured displacements, **F** is a forward propagation matrix of spatial and temporal integrals and derivatives of **G**, the columns of which are weighted by the components of **M**, and **p** is a vector of parameters which constitute the lower-order moments of the stress glut.

Numerous Bayesian methods for source parameter inversion have been proposed for 190 problems such as focal mechanism estimation (Wéber, 2006; Walsh et al., 2009; Lee et al., 191 2011; Duputel et al., 2014) and slip distribution estimation (Monelli et al., 2009; Minson et 192 al., 2013). Bayesian approaches for source estimation are growing in popularity because the 193 probabilistic nature of these inversions is such that they do not require the user to choose a 194 single solution for problems that, due to uncertainty, have many potential solutions. Instead, 195 Bayesian approaches provide ensembles of solutions that are informed by prior distributions 196 determined by physical constraints or ground truth. The Bayesian formulation described 197 here allows for the computation of an ensemble of solutions for second moments that rep-198 resent distributions of potential low-dimensional finite source properties for an earthquake 199 source. 200

The posterior distribution for this problem can be written as follows (e.g. Tarantola, 2005),

$$p(\mathbf{p}, \sigma | \mathbf{d}) \propto p(\mathbf{d} | \sigma, \mathbf{p}) \ p(\sigma) \ p(\mathbf{p}),$$
 (4)

where σ is a hyperparameter. For the likelihood term, $p(\mathbf{d}|\sigma, \mathbf{p})$, we use a multivariate normal distribution,

$$p(\mathbf{d}|\sigma, \mathbf{p}) \propto \frac{1}{\sqrt{|\Sigma|}} \exp(-\frac{1}{2} (\mathbf{d} - \mathbf{F}\mathbf{p})^T \boldsymbol{\Sigma}^{-1} (\mathbf{d} - \mathbf{F}\mathbf{p}))$$
(5)

Since the observations are time-series data, errors in the forward model will result in temporal autocorrelation. We can account for this correlation structure through the data covariance matrix, Σ , as outlined in (Duputel et al., 2014). If both points d_i and d_j are recorded by the same station:

$$\Sigma_{ij} = \sigma \cdot \exp(-|i - j|\delta t / \Delta t) \tag{6}$$

Where δt is the sampling rate, and Δt is the shortest period information included in the time-series. This correlation structure accounts for temporal correlation in the errors, but not any spatial correlation. In this paper we assume that the observations are spatially distributed sparsely enough that spatially-correlated errors are negligible.

We use uninformed priors in this case study. But, this framework is flexible such that informed priors can easily be incorporated (Gelman et al., 2010). That is, with the physical interpretation of the second moment properties that we will describe shortly, priors on the spatial extent, directivity, and duration may be imposed given observational ground truth. For example, if the true nodal plane of an earthquake is known, Gaussian priors may be placed on the spatial second moment parameters to restrict the principal eigenvector of the spatial covariance matrix to abut the true nodal plane.

The total number of parameters in this inverse problem is 11, and we approximate $p(\mathbf{p}, \sigma | \mathbf{d})$ using Markov Chain Monte Carlo (MCMC) sampling to obtain an ensemble of solutions. We do not solve for the zeroth or first order moments, and instead use the gCMT solution as our moment tensor and centroid location. Because the parameter space is quite large, we sample the posterior distribution using Hamiltonian Monte Carlo (HMC) sampling (Neal, 2010), which is an instance of the Metropolis-Hastings algorithm that can efficiently sample large parameter spaces using principles from Hamiltonian dynamics. This is accomplished in part by incorporating gradient information into the sampling process; however, it requires a means to also compute gradients efficiently. Here, we accomplish this through the use of reverse-mode automatic differentiation (Innes, 2019).

For each chain in this inversion, we draw 5000 samples from the posterior distributions 230 after drawing 5000 burn-in samples. In this inversion, the momentum distribution has a 231 diagonal mass matrix and the samples are updated using an ordinary leapfrog integrator 232 (Neal, 2010). The only hyperparameter in this inversion is σ , which we use to construct 233 the covariance matrix according to equation 6. To evaluate convergence, we run at least 234 235 3 chains of the inversion and compute the Gelman-Rubin diagnostic using the computed set of chains (Gelman & Rubin, 1992). That is, we compare the variability within chains 236 to the variability between chains to determine if the chains all converge to the same target 237 distributions. 238

Additionally, because the second moments of the stress glut are covariances, only a subset of the parameter space produces valid solutions. Specifically, the second moments are symmetric positive definite,

$$\mathbf{X} = \begin{bmatrix} \dot{f}^{(2,0)}(\xi_{\mathbf{c}},\tau_c) & \dot{f}^{(1,1)}(\xi_{\mathbf{c}},\tau_c) \\ \dot{f}^{(1,1)}(\xi_{\mathbf{c}},\tau_c)^T & \dot{f}^{(0,2)}(\xi_{\mathbf{c}},\tau_c) \end{bmatrix} \succeq 0.$$
(7)

242 Physically, this is equivalent to saying that the spatial extent and duration of the source are both non-negative. Typically, when performing a constrained Bayesian inversion, the easiest 243 course of action is to sample under an unconstrained parameter space and subsequently 244 transform those parameters into the necessarily constrained parameter space (Gelman et al., 245 2010). To this end, we note that, by the Cholesky Factorization Theorem, every symmetric 246 positive-definite matrix can be decomposed into the product of some lower triangular matrix 247 with a positive diagonal and the transpose of that same lower triangular matrix. This means 248 that given \mathbf{X} , there exists a lower triangular matrix \mathbf{L} with positive diagonal components 249 such that: 250

$$\mathbf{X} = \mathbf{L}\mathbf{L}^T \tag{8}$$

Thus, we can sample freely from the unconstrained off-diagonal components of \mathbf{L} and from 251 the natural logarithm of the diagonal components of **L**. Then, to evaluate our sample 252 against our data, we can simply build \mathbf{L} using our sample components and then construct 253 **X** using equation 5. From **X** we can extract a valid \mathbf{p} with which we evaluate the likelihood 254 of our sample. A keen observer may notice that while \mathbf{X} need only be symmetric posi-255 tive semi-definite, the Cholesky factorization forces \mathbf{X} to be positive definite. In practice, 256 this distinction is inconsequential, as a positive semi-definite X suggests that at least one 257 dimension of the source is identically zero, which will never be true in reality. 258

259 **Results**

Before showing the application of this methodology to real data, we will show a test 260 of the outlined inversion procedure using a synthetic source. We can also use this test 261 to determine the resolvability of the parameters of the Caribbean earthquake. To these 262 ends, we prescribe a 60x20 km rectangular fault with a strike and dip corresponding to the 263 nodal plane of the gCMT solution that is aligned with the Oriente Fault. We then define 264 a grid of point sources, each with the gCMT source mechanism and equal fraction of the 265 gCMT moment, along this prescribed fault such that the spatial release of moment can 266 be approximated as uniform distributions of moment release along the strike and dip of 267 the fault. We delay the activation of these point sources according to a prescribed rupture 268 velocity of 1.2 km/s along strike, resulting in an event duration of 50 s, such that the moment 269 release with time can also be approximated as a uniform distribution. Using the fact that 270 the width of a uniform distribution is equal to $2\sqrt{3}\sigma$, where σ is the standard deviation of 271 the Gaussian approximation of that uniform distribution, we can determine the true second 272 moment solution for this synthetic source. In the interest of evaluating the resolvability of 273 parameters for the Caribbean earthquake, we invert for these second moments using the 274 same distribution of stations and the same windowing procedure that we use for the real 275 event. For this test, we also use the mean σ from the inversion of real data so we could 276 assess how visible known features are in the presence of realistic error. The joint probability 277 distributions for each pair of inverted parameters are shown in Figure 7. These plots show 278 that most of the parameters are either uncorrelated or weakly correlated with each other, 279 with the exception of some of the spatio-temporal terms with their spatial counterparts and 280 some closely related spatial terms. 281

We can further test the fidelity of our inversion results by computing synthetic waveforms using equation 2 and evaluating the fit to the observed waveforms generated for this synthetic example. The waveforms for an ensemble of second moment solutions from a single chain for the synthetic test are shown for a subset of stations with a large diversity of azimuths and distances in Figure 3. The waveform fits match the synthetic observations very well, particularly when the full ensemble of solutions is considered.

In order to represent the second moment solutions for the synthetic test in a more 288 physically interpretable way, we convert the second moments into measures of volume, di-289 rectivity, and duration. To estimate the volume of moment release from this source, we 290 define an ellipsoid using the eigenvalues and eigenvectors of the spatial second moment of 291 the event, $\dot{f}^{(2,0)}(\xi_{\mathbf{c}},\tau_c)$. Assuming the spatial moment distribution follows a 3-dimensional 292 Gaussian function, this ellipsoid represents the volume encompassing 95% of the moment 293 released during the earthquake. The projections of the ellipsoids for the ensemble of solu-294 tions from a single chain from the synthetic test are shown in Figure 4. We can also infer 295 the instantaneous velocity of the moment centroid, an estimate of directivity, by dividing 296 the spatiotemporal second moment of the source, $\dot{f}^{(1,1)}(\xi_c, \tau_c)$, by the temporal second mo-297 ment of the source, $\dot{f}^{(0,2)}(\xi_c, \tau_c)$. The map-view projections and Z-components of these 298 velocity vectors for the synthetic test are given in Figure 4. Finally, we can estimate the 299 source duration if we assume the moment rate function of the earthquake is a Gaussian 300 distribution about the temporal centroid. Then, the second temporal moment of the source, 301 $\dot{f}^{(0,2)}(\xi_{\mathbf{c}},\tau_c)$, defines the variance of that moment-rate function. These Gaussian approxi-302 mations to the moment-rate function for the synthetic test are plotted in Figure 4. Figure 303 4 also allows us to evaluate how well the ensemble of solutions captures the true solution 304 for this test. Indeed, the true along-strike length, vertical extent, directivity, and duration 305 all fall within the ensemble of solutions which suggests these are well constrained features 306 in this inversion. 307

Now, we invert for the second moments of the 2020 Caribbean event using the real data. The distributions of the 10 independent parameters of the second moments for a single chain of the inversion using the real data are shown in Figure 5. We run the inversion for a set of chains, shown in Figure S1, and compute the Gelman-Rubin diagnostic (Gelman & Rubin,



Figure 2. Marginal and joint probability density plots for the 10 independent parameters inverted for the synthetic test in this study. Off-diagonal plots are 2-dimensional histogram plots representing the joint probability distribution for each pair of independent parameters. On-diagonal plots are kernel density estimate plots for the marginal distributions of the adjacent joint probability distributions.



Figure 3. Waveform fits for a subset of the windowed waveforms for the synthetic test conducted in this study. Waveforms are labeled according to the GSN station at which they were generated. Black waveforms are synthetic observations. Gray waveforms are generated using a single solution from the ensemble of solutions from our inversion. Waveforms from each solution in the ensemble are plotted. Red waveforms are generated using the mean solution of the ensemble of solutions from our inversion.



Figure 4. Physically motivated representation of the ensemble of second moment solutions for the synthetic test. Top row: Projections of the spatial ellipsoid generated using the eigenvalues and eigenvectors of the spatial covariance matrix of the stress glut distribution. This ellipsoid is projected into map-view (left), into the NZ-plane (middle), and into the EZ-plane (right). Bottom row: Instances of the directivity vector representing the instantaneous velocity of the centroid of the source and instances of the Gaussian approximation of the source-time function of the source. Directivity vectors are projected into map-view (left) and the distribution of Z-components of the directivity vectors is plotted as a histogram (middle). Gaussian approximations of the sourcetime function are plotted relative to the centroid time (right). Gray-scale represents the ensemble of solutions for which, with the exception of the histogram of directivity vector Z-components, darkness represents the density of the plotted solutions. Red represents the mean solution. Blue represents the true solution.



Figure 5. Marginal and joint probability density plots for the 10 independent parameters inverted for in this study. Off-diagonal plots are 2-dimensional histogram plots representing the joint probability distribution for each pair of independent parameters. On-diagonal plots are kernel density estimate plots for the marginal distributions of the adjacent joint probability distributions.

1992) using these chains. The Gelman-Rubin values are far less than 1.1, suggesting that 312 the chains have converged to the target posterior distributions for the second moments. 313 The joint probability distributions for each pair of parameters are shown in Figure 5. The 314 distribution for the hyperparameter σ is shown in Figure S2. As with the synthetic test, 315 these joint distributions show that the inverted parameters are mostly uncorrelated with 316 each other. We can also evaluate the waveform fits for the inversion using real data. These 317 waveform fits are shown in Figure 6. The computed waveforms for the ensemble of solutions 318 inverted for under this framework fit the observed waveforms reasonably well. 319

Given that some of the features are well resolved, under the assumtion that the stress glut rate is distributed as a 4-dimensional Gaussian function, we can use these ensembles of second moments to constrain features of the fault rupture. In particular, the map-view projection of the volume ellipsoid shown in Figure 7 closely follows the strike of the Oriente Fault, and suggests that 95% of the moment of this event was released in an along-strike length of approximately 90.31 ± 4.59 km. Additionally, the vertical extent of the volume



Figure 6. Waveform fits for a subset of the windowed waveforms used in this study. Waveforms are labeled according to the GSN station at which they were recorded. Black waveforms are observations. Gray waveforms are generated using a single solution from the ensemble of solutions from our inversion. Waveforms from each solution in the ensemble are plotted. Red waveforms are generated using the mean solution of the ensemble of solutions from our inversion.



Figure 7. Physically motivated representation of the ensemble of second moment solutions for the 2020 Caribbean event. Top row: Projections of the spatial ellipsoid generated using the eigenvalues and eigenvectors of the spatial covariance matrix of the stress glut distribution. This ellipsoid is projected into map-view (left), into the NZ-plane (middle), and into the EZ-plane (right). Bottom row: Instances of the vector representing the instantaneous velocity of the centroid of the source and instances of the Gaussian approximation of the source-time function of the source. The directivity vectors are projected into map-view (left) and the distribution of Z-components of the directivity vector is plotted as a histogram (middle). Gaussian approximations of the source-time function are plotted relative to the centroid time (right). Gray-scale represents the ensemble of solutions for which, with the exception of the histogram of directivity vector Z-components, darkness represents the density of the plotted solutions. Red represents the mean solution.

ellipsoid suggests that 95% of the moment of this event was released in a depth range of 326 approximately 30.01 ± 3.96 km. The directivity vectors inform both the preferred direction 327 of rupture and the magnitude of the directivity. As illustrated by Figure 7, this event 328 is unilateral to the SW and aligned with the Oriente Fault. Also, there is a smaller Z-329 directional component in all of the directivity vectors in our ensemble. The magnitude 330 of the directivity measured in this study is approximately 2.128 ± 0.148 km/s to the SW. 331 Finally, under the assumption that the moment of this event was released as a Gaussian 332 distribution in time, the moment-rate functions derived from the temporal second moments 333 from this solution suggest that 95% of the moment for our earthquake was released in a 334 span of 41.92 ± 1.28 seconds. 335



Figure 8. Summary figure of the spatial and directivity features of the 2020 Caribbean Earthquake as derived from the second moment inversion. Left: Map view projection of the second moment ellipsoid and the second moment directivity vector. Gray-scale lines represent the ensemble of solutions and their density. Red line represents the mean solution. Blue vector represents the directivity vector according to the same values shown on the axes but in units of km/s and exaggerated by a factor of 10. Green line represents the true nodal plane from the gCMT solution for the event, which is approximately aligned with the strike of the Oriente Fault. Yellow star represents the centroid position. Right: On-fault projection of the second moment ellipsoid and second moment directivity vector. Line colors match the line colors of the plot to the left. Purple line represents the elevation of the seafloor at the centroid position.

336 Discussion

In general, the ensemble of solutions for the Caribbean earthquake is well constrained 337 and largely agrees with what is already known about the event. As is shown in Figure 338 8, the largest principal axis of the ellipsoid representation is well-aligned with the Oriente 339 Fault. Also shown in Figure 8, the directivity vector aligns with the Oriente Fault and 340 suggests a rupture that propagates from the NE to the SW. This unilateral behavior is 341 well-constrained in other estimates of directivity for this source. Additionally, the Gaussian 342 source-time functions for this event suggest that the bulk of the moment release occurs 343 within a span of 40 seconds, and nearly all of the moment release occurs within 80 seconds. 344 This source duration agrees reasonably well with other duration estimates for this source 345 (USGS, 2020; Tadapansawut et al., 2021). 346

The joint probability distributions shown in Figure 5 suggest that most of the indepen-347 dent parameters of the second moments of the stress glut are uncorrelated. While there are 348 exceptions, this suggests that the lengths of the principal axes of the ellipsoid describing the 349 source volume vary independently. Likewise, changing the magnitude of the directivity along 350 one axis does not necessitate a change of the magnitude of the directivity along another axis. 351 Interestingly, the source duration, determined by the second temporal moment, is uncorre-352 lated with the spatial second moments of the stress glut. This suggests that changing the 353 volume of the source does not imply a change in duration. This non-correlation implies that 354 a change in volume may be correlated with changes in rupture propagation speed and/or 355 directivity. This relationship is partially evidenced by the high correlation between some of 356 the spatial moments with some of the spatiotemporal moments. 357

The low dimensional second moment estimate of the 2020 Caribbean Earthquake illustrates the unique potential of this methodology for producing probabilistic estimates of finite source properties with few a priori assumptions on the fault geometry and rupture dynamics. The only requirement is a centroid moment tensor solution, which fits nicely into this framework, as the zeroth and first moments represent the scalar moment and centroid position of the earthquake respectively. In fact, the centroid moment tensor solution may be

solved concurrently with the second moment solution, but this introduces nonlinearity and 364 significant additional computational/numerical complexity. The only constraint required 365 in the inversion is that the source be non-negative in extent, which does not exclude any 366 possible source scenarios. However, it is indeed easy to impose additional constraints on the second moments through the use of informed priors on the inversion parameters. Such in-368 formed priors should be imposed with the understanding that the second moments describe 369 a covariance matrix of a 4-dimensional Gaussian function. That is, informed priors are not 370 necessarily being placed on the possible source dimensions, but instead are being placed on 371 the possible Gaussian approximations of the source dimensions. 372

Indeed, the physical representations of these second moment solutions, such as the rep-373 resentation of the Caribbean Earthquake shown in Figure 7, should be interpreted with the 374 understanding that these solutions are probabilistic estimates of Gaussian approximations 375 of the source characteristics. For example, if a spatial extent ellipsoid solution has a vertical 376 extent that exceeds the surface of the Earth, this solution is not necessarily unphysical, but 377 instead may suggest a rupture distribution with a moment release that is biased towards 378 shallower depths. In fact, Gaussian functions only vanish at infinity. The ellipsoid represen-379 tation extends out to 2σ of the spatial distribution of the stress glut, but the choice of the 380 factor of 2 is to some extent arbitrary. Indeed, for any solution for any earthquake source, 381 there exists an n such that $n\sigma$ exceeds the surface of the Earth with nonzero probability. 382 The spatial and temporal components of the second moment solution should be interpreted 383 from this perspective. 384

With an understanding of the character of these solutions, we can draw probabilistically motivated conclusions regarding characteristics of the Caribbean Earthquake from these solutions. For example, there are large discrepancies in the along-strike spatial extent of this rupture between fault slip distribution studies. The estimate for the extent of the along-strike rupture most agrees with the USGS finite slip distribution results. That is, we estimate that most of the moment of the earthquake was released within an along-strike distance of approximately 90.31 ± 4.59 km.

One remarkable insight into this earthquake comes from the estimate of the vertical 392 spatial extent of the second moment solution. The solution suggests that the moment release 393 of this earthquake was distributed over a large depth range that spanned approximately 394 30.01 ± 3.96 km. The GCMT solution for this earthquake places the centroid depth at 23.9 395 km, which is fairly deep for an oceanic strike-slip earthquake. The large vertical extent estimate suggests that this earthquake ruptured perhaps much deeper than the centroid 397 depth, and thus implies that, as illustrated in Figure 8, the seismogenic zone is thick in this 398 location. This observation may signify that the section of oceanic lithosphere that ruptured 399 is cold (Abercrombie & Ekström, 2001) and may yield insights into the vertical structure 400 and heat flow of ocean-continent transform margins. 401

Additionally, the directivity metric, the instantaneous velocity of the centroid of the 402 source, is quite large at 2.128 ± 0.148 km/s. The instantaneous velocity of the centroid is 403 identically zero for purely bilateral ruptures and equal to the rupture speed for unilateral 404 ruptures. We can estimate the maximum rupture speed for this event by dividing the square 405 root of the largest eigenvalue of the stress glut spatial covariance with the square root of the 406 stress glut temporal covariance, which yields an average maximum rupture speed of 2.155 407 km/s. The agreement between the instantaneous velocity of the centroid of this source and 408 the average maximum rupture speed suggests a near purely unilateral rupture for this event. 409

410 Conclusions

In this study, we develop a Bayesian framework for computing second moments of the 411 stress glut of earthquakes using teleseismic data. This framework incorporates a positive-412 definite constraint under Cholesky decomposition and employs Hamiltonian Monte Carlo 413 sampling to efficiently probe the parameter space. This methodology provides robust esti-414 mates of uncertainty by sampling the posterior distribution of solutions with dynamic error 415 computation and accounting for the temporal correlation structure in the waveform data. 416 These second moments of the stress glut provide a low-dimensional, physically-motivated 417 418 representation of source volume, directivity, and duration that requires no a priori assumptions and is repeatable and comparable between events. We verify this methodology using 419 a synthetic test and apply this framework to the 2020 $M_w 7.7$ Caribbean earthquake. We 420 show that our solutions for this event provide event parameters that largely agree with the 421 available ground truth. We also show that our solutions can be used to resolve ambiguities 422 between higher-order finite source solutions. Finally, we show that our solution may be used 423 to infer source parameters that have historically been difficult to constrain, such as vertical 424 rupture extent. 425

426 Acknowledgments

This work was partially funded by the National Science Foundation's (NSF) Graduate Re-427 search Fellowships Program (GRFP) under grant number DGE-1745301. The teleseismic 428 waveforms used in this study are from the Global Seismographic Network (GSN) oper-429 ated by Scripps Institution of Oceanography (II: IRIS/IDA; https://doi.org/10.7914/SN/II) 430 (Scripps Institution Of Oceanography, 1986) and the Albuquerque Seismological Laboratory 431 (IU: IRIS/USGS; https://doi.org/10.7914/SN/IU) (Albuquerque Seismological Laboratory 432 (ASL)/USGS, 1988). These waveforms and associated metadata used in this study were ac-433 cessed through the IRIS Data Management Center (DMC). The centroid and moment tensor 434 solution used in this study were obtained from Global Centroid Moment Tensor (gCMT) 435 catalog (Dziewonski et al., 1981; Ekström et al., 2012) at https://www.globalcmt.org/. 436 The synthetic waveforms used in this study were generated using the software Mineos, ver-437 sion 1.0.2 (Masters et al., 2011), available at https://geodynamics.org/cig/software/mineos/ 438 through the Computational Infrastructure for Geodynamics (CIG). Figure 1 was generated 439 using The Generic Mapping Tools (GMT), version 6 (Wessel et al., 2019), available at 440 https://www.generic-mapping-tools.org/. 441

442 References

446

447

448

- Abercrombie, R. E., & Ekström, G. (2001). Earthquake slip on oceanic transform faults.
 Nature, 410(6824), 74–77. doi: 10.1038/35065064
 Albuquerque Seismological Laboratory (ASL)/USGS. (1988). Global Seismograph Network
 - (GSN IRIS/USGS). International Federation of Digital Seismograph Networks. Retrieved from http://www.fdsn.org/doi/10.7914/SN/IU doi: 10.7914/SN/IU
 - Ammon, C. J. (2005). Rupture process of the 2004 Sumatra-Andaman Earthquake. *Science*, 308 (5725), 1133–1139. doi: 10.1126/science.1112260
- Backus, G., & Mulcahy, M. (1976a). Moment tensors and other phenomenological descriptions of seismic sources–I. Continuous displacements. *Geophysical Journal International*, 46(2), 341–361. doi: 10.1111/j.1365-246X.1976.tb04162.x
- Backus, G., & Mulcahy, M. (1976b). Moment tensors and other phenomenological de scriptions of seismic sources-II. Discontinuous displacements. *Geophysical Journal International*, 47(2), 301–329. doi: 10.1111/j.1365-246X.1976.tb01275.x
- Backus, G. E. (1977). Interpreting the seismic glut moments of total degree two or less. *Geophysical Journal International*, 51(1), 1–25. doi: 10.1111/j.1365-246X.1977.tb04187
 .x
- Bird, P. (2003). An updated digital model of plate boundaries. *Geochemistry, Geophysics, Geosystems*, 4(3), 297–356. doi: 10.1029/2001GC000252
- Bukchin, B. (1995). Determination of stress glut moments of total degree 2 from teleseismic
 surface wave amplitude spectra. *Tectonophysics*, 248 (3-4), 185–191. doi: 10.1016/
 0040-1951 (94)00271-A
- Chen, P. (2005). Finite-moment tensor of the 3 September 2002 Yorba Linda Earthquake.
 Bulletin of the Seismological Society of America, 95(3), 1170–1180. doi: 10.1785/ 0120040094
- Dahlen, F., & Tromp, J. (1998). Theoretical global seismology. Princeton, N.J.: Princeton
 University Press.
- ⁴⁶⁹ DeMets, C., & Wiggins-Grandison, M. (2007). Deformation of Jamaica and motion of the
 ⁴⁷⁰ Gonâve microplate from GPS and seismic data. *Geophysical Journal International*,
 ⁴⁷¹ 168(1), 362–378. doi: 10.1111/j.1365-246X.2006.03236.x
- ⁴⁷² Du, Y., Aydin, A., & Segall, P. (1992). Comparison of various inversion techniques as
 ⁴⁷³ applied to the determination of a geophysical deformation model for the 1983 Borah
 ⁴⁷⁴ Peak Earthquake. Bulletin of the Seismological Society of America, 82(4), 1840–1866.
- ⁴⁷⁵ Duputel, Z., Agram, P. S., Simons, M., Minson, S. E., & Beck, J. L. (2014). Accounting
 ⁴⁷⁶ for prediction uncertainty when inferring subsurface fault slip. *Geophysical Journal* ⁴⁷⁷ *International*, 197(1), 464–482. doi: 10.1093/gji/ggt517

- Dziewonski, A. M., & Anderson, D. L. (1981). Preliminary reference earth model. *Geophys- ical Journal International*, 25, 297–356.
- Dziewonski, A. M., Chou, T. A., & Woodhouse, J. H. (1981). Determination of earthquake
 source parameters from waveform data for studies of global and regional seismicity.
 Journal of Geophysical Research: Solid Earth, 86(B4), 2825–2852. doi: 10.1029/
 JB086iB04p02825
- Ekström, G., Nettles, M., & Dziewoński, A. (2012). The global CMT project 2004–2010:
 Centroid-moment tensors for 13,017 earthquakes. *Physics of the Earth and Planetary Interiors*, 200-201, 1–9. doi: 10.1016/j.pepi.2012.04.002
- 487
 GCMT. (2020). Mw 7.7 cuba region. Retrieved from https://www.globalcmt.org/

 488
 cgi-bin/globalcmt-cgi-bin/CMT5/form?itype=ymd&yr=2020&mo=1&day=

 489
 1&otype=ymd&oyr=2020&omo=2&oday=1&jyr=1976&jday=1&ojyr=1976&ojday=

 490
 1&nday=1&lmw=7.5&umw=10&lms=0&ums=10&lmb=0&umb=10&llat=-90&ulat=

 491
 90&llon=-180&ulon=180&lhd=0&uhd=1000<s=-9999&uts=9999&lpe1=0&upe1=

 492
 90&lpe2=0&upe2=90&list=0
- Gelman, A., Carlin, J., Stern, H., Dunson, D., Vehtari, A., & Rubin, D. (2010). Bayesian
 data analysis. Boca Raton, F.L.: Chapman and Hall-CRC Press.
 - Gelman, A., & Rubin, D. (1992). Inference from iterative simulation using multiple sequences. Statistical Science, 7(4), 457–511.

495

496

500

501

502

503

504

505

506

507

508

509

510

515

516

517

518

- Hartzell, S. H., & Heaton, T. H. (1983). Inversion of strong ground motion and teleseismic
 waveform data for the fault rupture history of the 1979 Imperial Valley, California
 Earthquake. Bulletin of the Seismological Society of America, 73(6), 1553–1583.
 - Ide, S., Baltay, A., & Beroza, G. C. (2011). Shallow Dynamic Overshoot and Energetic Deep Rupture in the 2011 Mw 9.0 Tohoku-Oki Earthquake. *Science*, 332(6036), 1426–1429. doi: 10.1126/science.1207020
 - Innes, M. (2019). Don't Unroll Adjoint: Differentiating SSA-Form Programs. arXiv:1810.07951 [cs].
 - Lay, T. (2018). A review of the rupture characteristics of the 2011 Tohoku-oki Mw 9.1 earthquake. *Tectonophysics*, 733, 4–36. doi: 10.1016/j.tecto.2017.09.022
 - Lee, E., Chen, P., Jordan, T. H., & Wang, L. (2011). Rapid full-wave centroid moment tensor (CMT) inversion in a three-dimensional earth structure model for earthquakes in Southern California: Rapid full-wave CMT inversion. *Geophysical Journal International*, 186(1), 311–330. doi: 10.1111/j.1365-246X.2011.05031.x
- Mann, P., Taylor, F., Edwards, R., & Ku, T.-L. (1995). Actively evolving microplate formation by oblique collision and sideways motion along strike-slip faults: An example from the northeastern Caribbean plate margin. *Tectonophysics*, 246(1-3), 1–69. doi: 10.1016/0040-1951(94)00268-E
 - Masters, G., Woodhouse, J., & Freeman, G. (2011). *Mineos.* Retrieved from https://geodynamics.org/cig/software/mineos/
 - McGuire, J. J. (2004). Estimating Finite Source Properties of Small Earthquake Ruptures. Bulletin of the Seismological Society of America, 94(2), 377–393. doi: 10.1785/0120030091
- McGuire, J. J., Zhao, L., & Jordan, T. H. (2000). Rupture dimensions of the 1998 Antarctic
 Earthquake from low-frequency waves. *Geophysical Research Letters*, 27(15), 2305–2308. doi: 10.1029/1999GL011186
- McGuire, J. J., Zhao, L., & Jordan, T. H. (2001). Teleseismic inversion for the second-degree moments of earthquake space-time distributions. *Geophysical Journal International*, 145(3), 661–678. doi: 10.1046/j.1365-246x.2001.01414.x
- McGuire, J. J., Zhao, L., & Jordan, T. H. (2002). Predominance of Unilateral Rupture for a Global Catalog of Large Earthquakes. *Bulletin of the Seismological Society of America*, 92(8), 3309–3317. doi: 10.1785/0120010293
- Meng, H., McGuire, J. J., & Ben-Zion, Y. (2020). Semiautomated estimates of directivity
 and related source properties of small to moderate Southern California earthquakes
 using second seismic moments. Journal of Geophysical Research: Solid Earth, 125(4),
 e2019JB018566. doi: 10.1029/2019JB018566

- Minson, S. E., Simons, M., & Beck, J. L. (2013). Bayesian inversion for finite fault earth quake source models I—theory and algorithm. *Geophysical Journal International*,
 194(3), 1701–1726. doi: 10.1093/gji/ggt180
- Monelli, D., Mai, P. M., Jónsson, S., & Giardini, D. (2009). Bayesian imaging of the 2000
 Western Tottori (Japan) earthquake through fitting of strong motion and GPS data.
 Geophysical Journal International, 176(1), 135–150. doi: 10.1111/j.1365-246X.2008
 .03943.x
- Moreno, B., Grandison, M., & Atakan, K. (2002). Crustal velocity model along the south ern Cuban margin: implications for the tectonic regime at an active plate boundary.
 Geophysical Journal International, 151(2), 632–645. doi: 10.1046/j.1365-246X.2002
 .01810.x
- Moreno, M., Rosenau, M., & Oncken, O. (2010). 2010 Maule earthquake slip correlates
 with pre-seismic locking of Andean subduction zone. Nature, 467(7312), 198–202.
 doi: 10.1038/nature09349
 - Neal, R. (2010). *MCMC using Hamiltonian dynamics*. Boca Raton, F.L.: Chapman and Hall-CRC Press.

547

548

549

550

551

555

556

557

564

- Ross, Z. E., Idini, B., Jia, Z., Stephenson, O. L., Zhong, M., Wang, X., ... Jung, J. (2019). Hierarchical interlocked orthogonal faulting in the 2019 Ridgecrest earthquake sequence. *Science*, 366(6463), 346–351. doi: 10.1126/science.aaz0109
- Saito, T., Ito, Y., Inazu, D., & Hino, R. (2011). Tsunami source of the 2011 Tohoku Oki earthquake, Japan: Inversion analysis based on dispersive tsunami simulations.
 Geophysical Research Letters, 38(7), L00G19. doi: 10.1029/2011GL049089
 - Scripps Institution Of Oceanography. (1986). IRIS/IDA Seismic Network. International Federation of Digital Seismograph Networks. Retrieved from http://www.fdsn.org/ doi/10.7914/SN/II doi: 10.7914/SN/II
- Tadapansawut, T., Okuwaki, R., Yagi, Y., & Yamashita, S. (2021). Rupture Process of the
 2020 Caribbean Earthquake Along the Oriente Transform Fault, Involving Supershear
 Rupture and Geometric Complexity of Fault. *Geophysical Research Letters*, 48(1),
 e2020GL090899. doi: 10.1029/2020GL090899
- Tarantola, A. (2005). Inverse Problem Theory and Methods for Model Parameter Estima tion. Philidelphia, P.A.: Society for Industrial and Applied Mathematics.
 - USGS. (2020). *M 7.7-123km nnw of lucea, jamaica*. Retrieved from https://earthquake .usgs.gov/earthquakes/eventpage/us60007idc/executive
- Van Dusen, S. R., & Doser, D. I. (2000). Faulting processes of historic (1917–1962) M 6.0
 earthquakes along the North-central Caribbean margin. *Pure and Applied Geophysics*, 157(5), 719–736. doi: 10.1007/PL00001115
- Wald, D. J., & Heaton, T. H. (1992). Spatial and temporal distribution of slip for the 1992
 Landers, California, Earthquake. Bulletin of the Seismological Society of America, 84(3), 668–691.
- Walsh, D., Arnold, R., & Townend, J. (2009). A Bayesian approach to determining and parametrizing earthquake focal mechanisms. *Geophysical Journal International*, 176(1), 235–255. doi: 10.1111/j.1365-246X.2008.03979.x
- Wessel, P., Luis, J. F., Uieda, L., Scharroo, R., Wobbe, F., Smith, W. H. F., & Tian, D.
 (2019). The generic mapping tools. Retrieved from https://www.generic-mapping
 -tools.org/
- Wéber, Z. (2006). Probabilistic local waveform inversion for moment tensor and hypocentral
 location. *Geophysical Journal International*, 165(2), 607–621. doi: 10.1111/j.1365
 -246X.2006.02934.x