Topographic roughness on forested hillslopes: a theoretical approach for quantifying hillslope sediment flux from tree throw

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Abstract

Tree uprooting is an observable and consequential process that suddenly moves soil downslope, inverts the soil column, and roughens the surface with pit-mound topography. Quantifying fluxes due to tree throw is complicated by its stochastic nature and estimation requires averaging over a large area or long time. Here, we develop theory that leads to a dimensionless metric directly measurable from high resolution topographic data. The theory explains the flux and topographic roughness as a function of tree throw production and decay rate by creep-like processes. We then form a dimensionless variable that is the ratio of fluxes due to three throw versus creep-like processes. Applying the theory to hillslopes in Southern Indiana, we find that tree throw accounts for 10 to $20\$ % of the hillslope sediment flux. The theoretical and observational findings provide a framework and important constraints on quantifying Critical Zone function from topographic parameters such as roughness.

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Key Points:

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8	• The expected topographic variance is a function of the ratio of tree throw rates
9	to creep-like diffusivity.
10	- Tree throw accounts for 10-20% of the hills lope sediment flux in southern Indi-
11	ana.
12	• Tree throw occurs more frequently on steep, east facing hillslopes which is con-

¹³ sistent with the dominant wind directions.

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14 Abstract

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27 Plain Language Summary

When trees fall on hillslopes, they often uproot a volume of soil that is attached 28 to the roots. Because trees usually fall downslope, this uprooted soil also moves down 29 the hillslope, contributes to erosion, and leaves characteristic pit and mound shapes on 30 the surface. Despite the topographic signature of the process, quantifying how much dirt 31 trees move downslope is complicated by the randomness that drives the process. We de-32 velop theory that explains the roughness of hillslope topography and how it relates to 33 sediment transport rates driven by tree throw. We then map topographic roughness over 34 a county in southern Indiana and demonstrate that tree throw accounts for 10 to 20%35 of the sediment motions on hillslopes. Further, we demonstrate that east facing hillslopes 36 tend to have more tree throw events which coincides with the dominant wind directions 37 and illustrates that extreme wind events drive most tree throw events in southern In-38 diana. 39

40 **1 Introduction**

The rate and style of sediment transport processes on hillslopes are central to understanding landscape evolution (Roering et al., 2001, 2007), geochemical cycling (Maher,
2010; Yoo et al., 2007; Lebedeva & Brantley, 2013), soil production (Heimsath et al., 2001;
Mudd & Furbish, 2004; Gabet & Mudd, 2010; Riebe et al., 2003; Ferrier & Kirchner, 2008),

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sediment supply to watersheds (Syvitski, 2003), and the dynamics of the Critical Zone 45 (Brantley, McDowell, et al., 2017; Brantley, Eissenstat, et al., 2017). On hillslopes, a suite 46 of processes that include freeze-thaw (Anderson, 2002), wetting-drying (Struck et al., 2018), 47 and bioturbation (Gabet et al., 2003) disturb unconsolidated soil and sediment which 48 leads to bulk downslope creep-like motion (Culling, 1963; Furbish et al., 2009). Obser-49 vation and quantification of these creep-like processes is often obfuscated by the small 50 scale over which they operate and the slow bulk transport rates that they produce. Tree 51 throw, however, is a sediment transport process that occurs when trees topple and up-52 root a mass of soil – leaving a clear pit-mound couplet as a topographic signature. In 53 contrast to the suite of creep-like processes, tree throw suddenly moves and mixes soil, 54 which inverts any soil-depth varying chemical or physical properties. Tree throw there-55 fore is a uniquely consequential and measurable process on hillslopes, yet the relative mag-56 nitudes of sediment fluxes due to tree throw and creep-like processes remain unknown. 57

Tree throw has been the subject of many field and numerical studies that quan-58 tify the sediment flux, (Gabet et al., 2003; Martin et al., 2013; Phillips et al., 2017; Han-59 cock & Lowry, 2021; Samonil et al., 2020) or demonstrate the consequences for weath-60 ering and soil production (Gallaway et al., 2009; Gabet & Mudd, 2010; Šamonil et al., 61 2013). Quantifying the sediment flux due to tree throw typically involves measuring the 62 volumes of sediment attached to uprooted trees and constraining event frequency by ei-63 ther dating material deposited beneath mounds (Schaetzl & Follmer, 1990; Samonil et 64 al., 2013) or by tree census (Gallaway et al., 2009; Martin et al., 2013; Šamonil et al., 65 2020). However, tree throw is often caused by rare extreme wind events that impart a 66 drag force on the canopy which exceed a resisting force of the soil. Such events occur with 67 a large range of magnitudes and the recurrence intervals for large events can be on the 68 order of decades (Gallaway et al., 2009; Hancock & Lowry, 2021). Therefore, quantifi-69 cation of tree throw by direct human observation is beyond our capabilities and requires 70 that we average over the full range of the process. This requires either a very long record 71 through time or very large domain that samples a great number of tree throw events. 72 The land surface is a faithful record of past tree throw events as it accumulates pit-mound 73 couplets through time and the topographic roughness of a surface reflects a long record 74 75 of tree throw events.

In this paper, we develop theory for the expected topographic roughness (quanti fied by the topographic variance) of a hillslope for a given frequency of tree throw events

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Figure 1. (A) Image of a tree throw root ball and (B) the subsequent transition to a characteristic pit-mound couplet. On many hillslopes in southern Indiana pit-mound couplets are the primary roughness features which creates the pocked texture. This texture is visible from (C) 0.25 m and (D) 0.76 m resolution digital elevation models. Hatch marks on the images are equal intervals of meters.

and magnitude of topographic smoothing from creep-like processes. We then leverage 78 the theory to form a dimensionless variable that is composed entirely of measurable to-79 pographic variables and is the ratio of the hillslope sediment flux due to tree throw ver-80 sus all creep-like processes. Topographic roughness created by tree throw is observable 81 in high resolution topographic data and the theory may be applied across large areas. 82 We apply the theory to 1,910 hillslopes selected from over 800 km^2 in southern Indiana 83 (Brown County) to obtain estimates of the percentage of the flux due to tree throw. We 84 demonstrate that tree throw accounts for approximately 10-20% of the hillslope sediment 85 flux and highlight an aspect-dependency that is consistent with dominant wind direc-86 tions in southern Indiana. 87

⁸⁸ 2 Theory

Here we construct the ratio of sediment flux due to tree throw versus creep-like processes. We develop analytical expressions for the flux due to tree throw and the expected topographic variance that reflects the balance between roughness production by tree throw and roughness erasure by creep-like processes. These two components are then combined to form the desired ratio of volumetric fluxes.

94 2.1 Flux due to tree throw

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Previous work quantifies the flux due to tree throw as the product of the frequency of the process and the volume that it mobilizes, which can be measured from the volumes of either pits or uprooted sediment attached to roots (Gabet et al., 2003; Gallaway et al., 2009; Hellmer et al., 2015; Phillips et al., 2017). We present a similar formulation, but cast it in probabilistic terms for particle travel distances. The mean flux for any process is (Furbish & Haff, 2010; Doane et al., 2018)

$$\bar{q}(x,y) = E(x,y)\mu_r(x,y) \tag{1}$$

where $E [L^3 L^{-2}T^{-1}]$ is a volumetric entrainment rate and μ_r is the mean travel distance. E involves the frequency of tree throw events per unit area and the volume of root balls, which is a stochastic and noise-driven component that is not directly measurable over short timescales or small spatial scales. In contrast, particle travel distances relate directly to the geometry of pit-mound couplets (Figure 2).

We define an initial couplet geometry that is an approximation to those observed in nature (Figure 2),

 $\zeta'(x,y) = \frac{2Ax}{l^2} e^{-\left(\frac{x^2}{l^2} + \frac{y^2}{w^2}\right)},$ (2)

where ζ' [L] is the land-surface elevation, x and y [L] are horizontal positions, A [L²] is 109 a squared amplitude, and l and w are characteristic length scales. Note that (2) is a Gaus-110 sian in the y-direction and a derivative of a Gaussian in the x-direction. Previous work 111 has suggested alternative forms (two anti-symmetric semi-spheres) for the initial con-112 dition of pit-mound couplets (Gabet et al., 2003; Gabet & Mudd, 2010; Martin et al., 113 2013; Samonil et al., 2020); however, we prefer this formulation as it approximates nat-114 ural couplet geometries and is mathematically simple to work with. The form of (2) rep-115 resents the initial condition of pit-mound couplets once the tree roots have rotted away 116 (5-10 years after the tree topples in temperate environments (Schaetzl & Follmer, 1990)) 117 so that the couplet may evolve by creep-like processes. With this definition of the ini-118 tial condition, the 'throw' component involves the tree toppling and the decay of roots 119 which drops particles and constructs smooth pit-mound couplets. Based on (1), (2), and 120 using the idealized geometry of couplets and allowing for A and l to be random variables, 121 we find that the average flux due to tree throw on a hillslope is (Appendix A), 122

$$q_{TT}(x,y) = p(x,y)\frac{\sqrt{2}\pi\mu_A \left(\mu_l^2 + \sigma_l^2\right)}{\phi}, \qquad (3)$$



Figure 2. (a) Two dimensional view of an idealized pit-mound couplet. (b) Comparison of idealized and natural pit-mound couplet illustrating good agreement. (c) Conceptual diagram illustrating how we calculate the probability function of travel distances, r. l and w are characterisic length scales of pit-mound couplets and μ_r is the mean particle travel distance.

where μ_X and σ_X^2 refer to the mean and variance of variable X, and we have introduced $\phi = l/w$ because we expect l and w to co-vary on a given slope. The production rate, p [L⁻² T⁻¹], is the only variable that is not directly measurable from topography.

The idealized pit-mound geometry should vary with slope. When trees fall on pro-127 gressively steeper slopes, more of the uprooted sediment moves further downslope, which 128 increases l and ϕ (Gabet et al., 2003). To account for this we numerically simulate a one-129 dimensional model of pit-mound formation on different slopes which suggests $l \approx 1 + 1$ 130 S where S is land-surface slope (S4). We note that equation (3) assumes that all trees 131 fall directly downslope but, in nature, trees can fall in all directions. However, observa-132 tions of tree throw resulting from ice storms demonstrates that trees typically fall downs-133 lope (Hellmer et al., 2015), which indicates that they tend to have weaker resiting forces 134 in the downslope direction. Most pit-mound couplets are oriented along hillslope con-135 tours in southern Indiana, suggesting that downslope transport is the dominant mode 136 of tree throw in this setting. 137

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2.2 Topographic Roughness

Tree throw is the only geomorphic process we know of that adds topographic roughness to soil mantled and forested hillslopes at the scale of meters. Topographic roughness can be quantified with the average concavity (Booth et al., 2017; LaHusen et al., 2016), fitted polynomial functions (Milodowski et al., 2015), and the standard deviation or variance of detrended topography (Roth et al., 2020). We use the topographic vari-

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ance to quantify roughness because we can derive an analytical solution for the expected
variance that reflects the balance between tree throw frequency and the pace of couplet
degradation by creep-like processes.

¹⁴⁷ Couplets degrade by the action of all creep-like processes which drive the creation ¹⁴⁸ and collapse of porosity. When the land-surface is inclined, this leads to downslope sed-¹⁴⁹ iment motion at a rate that scales with slope (Furbish et al., 2009). A linear model for ¹⁵⁰ creep-like processes has a long legacy in geomorphology (Culling, 1963),

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$$q_c = -D\nabla\zeta, \qquad (4)$$

where $q_c [L^2 T^{-1}]$ is the volumetric flux, $D [L^2 T^{-1}]$ is a topographic diffusivity, and ζ is the land-surface elevation. Placing (4) into the Exner equation leads to the linear diffusion equation for the evolution of topography (Fernandes & Dietrich, 1997; Furbish & Fagherazzi, 2001; Richardson et al., 2019),

$$\frac{\partial \zeta}{\partial t} = D\nabla^2 \zeta \,. \tag{5}$$

We note that nonlinear slope- (Roering et al., 2001) and soil thickness-dependent (Furbish et al., 2009; Mudd & Furbish, 2004; Johnstone & Hilley, 2015) formulations are alternative flux models. However, neither of these models leads to a significant difference in the evolution of topographic variance for pit-mound couplets (S2) so we only consider linear diffusion here.

We solve the diffusion equation for topography with an initial condition represented 162 by (2) to understand the temporal evolution of the topographic variance of a single pit-163 mound couplet. To do so, we transform the problem into the wavenumber domain via 164 the Fourier Transform and apply Parseval's Theorem, which states that the integral of 165 the square of Fourier Transform amplitudes is equal to the integral of the square of the 166 signal in the arithmetic domain (Appendix B). The sum of squares equals the sample 167 variance when one divides by the size of the domain so these two steps lead to an an-168 alytical solution for the time evolution of topographic variance of a pit-mound couplet. 169 The topographic variance of an entire hillslope is the integral of all couplets of all ages, 170 which amounts to a convolution of tree throw production and decay rates, 171

$$\sigma_{\zeta}^{2}(t) = \frac{A^{2}w^{2}l^{2}\pi}{32} \int_{-\infty}^{t} p(t') \left[\frac{l^{2}}{4} + D[t-t']\right]^{-3/2} \left[\frac{w^{2}}{4} + D[t-t']\right]^{-1/2} dt', \qquad (6)$$

where t' is an earlier time and t-t' is a couplet age. Given a time-series of tree throw production rates, (6) describes the topographic variance at any moment. The produc-



Figure 3. a) A rough surface that is the result of a numerical simulation with D = 0.005 and a mean production rate of one tree per year per 10,000 m². b) The time series of one hundred numerical simulations with the same parameters (gray) and the expected variance (red).

tion rate of tree throw will be some noisy signal through time and so too is the time series of topographic variance. For the purpose of this paper, we consider the expected topographic variance, which only involves the mean production rate, μ_p . Performing the integration in (6) (over all couplets of all ages) yields the expected topographic variance

$$E(\sigma_{\zeta}^{2}) = \frac{\mu_{p} A^{2} l^{2} \pi}{4D(\phi^{2} + \phi)}.$$
(7)

If we allow for A and l to be random variables with finite covariance, then the expected topographic variance is

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$$E(\sigma_{\zeta}^{2}) = \frac{\mu_{p}\left(\left(\mu_{A}^{2} + \sigma_{A}^{2}\right)\left(\mu_{l}^{2} + \sigma_{l}^{2}\right) + cov(A^{2}, L^{2})\right)\pi}{4D\left(\phi^{2} + \phi\right)}.$$
(8)

We numerically test this result by simulating random production and diffusion (equa-183 tion 5) of pit-mound couplets on a flat surface. For each one year time step, a number 184 of new pit-mound couplets is selected from an exponential distribution of production rates. 185 The exponential distribution reflects our intuition that at a single hillslope and in most 186 years, zero to few tree throw events will occur and there will be rare years with many 187 tree throw events. The model then populates a two-dimensional domain with new pit-188 mound couplets with parameters that are chosen from distributions that have a small 189 but finite amount of covariance. Roughness on the numerical surface initially increases 190 until it reaches a steady state value which it oscillates around and coincides with (8) (Fig-191 ure 3). 192

Although (8) accurately predicts the expected topographic variance of the numerical model, it contains two unknown rate constants, μ_p and D. Previous efforts attempt to understand values of D from a statistical mechanics (Furbish et al., 2009) or empir-

- ical perspective (Richardson et al., 2019). However, identifying the value of D for a par-
- ¹⁹⁷ticular landscape remains a challenge and is a source of uncertainty. There are also es-
- timates of tree throw production rates (Schaetzl et al., 1990; Phillips et al., 2017; Šamonil
- et al., 2020), but the stochasticity of tree throw over timescales of decades to centuries
- limits the constraints of μ_p .
- Equation 8 demonstrates that rougher hillslopes reflect a relatively high tree throw production rate and low diffusivity. Although we cannot know μ_p and D apriori, we can learn about the relative magnitude of the sediment fluxes due to tree throw and creeplike processes. First, we rewrite the expression for q_{TT} by rearranging (8) to solve for μ_p . This places σ_{ζ}^2 and D in the numerator of (3). Forming the ratio then leads to,
 - $R = \frac{q_{TT}}{q_c} = 4\sqrt{2} \frac{\mu_A (\phi + 1)}{(\mu_A^2 + \sigma_A^2)} \frac{\sigma_\zeta^2}{|S|},$ (9)
- where we have assumed that $cov(A^2, L^2)$ is negligible (S3). Note that all parts of (9) are measurable from high resolution topographic data. We now turn to calculations of R by measuring σ_{ζ}^2 , |S|, and parameterization of A and ϕ in a forested landscape.

3 Measuring topographic variance and R with high-resolution topography raphy

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3.1 Constraining pit-mound geometry

We parameterize A, l, and ϕ by fitting the idealized couplet geometry to pit-mound 213 couplets that are clearly visible in high resolution topography. We fit 101 pit-mound cou-214 plets from 0.25 m resolution, drone-collected lidar (S1). Couplets that we identify from 215 lidar are likely to vary in age and therefore may have partially diffused. The shape A/(wl)216 of each pit-mound couplet is a proxy for age, and the youngest will have the largest value 217 of this ratio (i.e. tall and narrow). We select the 50 freshest/youngest based on this met-218 ric and extract values for μ_A = 0.68, σ_A^2 = 0.05, ϕ = 0.83, and Cov (A^2, L^2) = 0.005 219 (S3). The covariance and variance terms are negligible relative to the average values and 220 so they may be dropped from (8)221

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3.2 Measuring Topographic Variance

We used a 2017 lidar survey of Indiana collected via the USGS 3D elevation program, that produced digital elevation models (DEMs) at 0.76 m resolution to measure

topographic variance. We emphasize that 0.76 m resolution DEMs are capable of cap-225 turing the majority of topographic variance from tree throw (S1). We focus our study 226 on Brown County, which is a rural county in south-central Indiana with moderate re-227 lief (200 meters) and locally steep slopes (up to ≈ 1). The Borden Group, a Missippian 228 siltstone interbedded with limestone, underlies the entire county (Thompson & Sowder, 229 2005). Brown County is south of the southern terminus of the last glacial extent and the 230 topography lacks glacial roughness features like hummocky topography or glacial errat-231 ics so that hillslope roughness is reliably created by tree throw. 232

We manually define 1,910 forested hillslopes in Brown County that are minimally 233 dissected by first-order gullies. We first run a high-pass filter over 1.5x1.5 km sections 234 of the land surface with a Gaussian filter with a length scale of 3.8 meters (5 pixels) to 235 filter out hillslope- and valley-scale topography. The high pass filter highlights a num-236 ber of roughness features including pit-mound couplets, channel banks, geologic contacts, 237 and infrastructure. We manually exclude hillslopes with these other roughness features. 238 For each area of interest, we calculate the topographic roughness as the variance of the 239 high pass filter output. 240

241 4 Results

Measurements of topographic variance for 1910 hillslopes from Brown county (Fig-242 ure 4a) span over an order of magnitude from 0.001 up to 0.03. There is a modest pos-243 itive relationship between topographic variance and slope (Figure 4b). However, the spread 244 of measured variance values also increases with slope. Topographic variance also depends 245 on slope aspect (Figure 4c) with northeast facing slopes having the largest measured val-246 ues and west-facing slopes having the lowest. We observe the same trend in the distri-247 bution of average slopes of the hillslopes that we selected with east-facing slopes gen-248 erally being steeper than west facing slopes (Figure 4d). The reason for the slope-magnitude 249 sampling discrepancy between east and west slopes is that there is an aspect-dependent 250 drainage density in which first order channels and gullies tend to dissect steep west fac-251 ing slopes more frequently than steep east facing slopes. This limits our ability to sam-252 ple steep west facing slopes as channelization processes overprint the hillslopes. 253

Sediment flux due to tree throw increases by roughly 50% on east facing slopes (Figure 4f). The average values of R (calculated by weighting hillslopes by area) vary from

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0.12 to 0.22 on west- and east-facing slopes respectively (Figure 4e), accounting for $q_{TT}/(q_c + q_{TT}) = 11\%$ and 18% of the hillslope sediment flux on those slopes. Several thousand eddy covariance measurements of wind velocity from a nearby AmeriFlux tower demonstrate that wind blows most frequently to the northeast and least frequently to the west (Novick & Phillips, 2020) suggesting that the larger R and variance on east-facing hillslopes is caused by wind-blown tree throw as opposed to trees aging or snow loading.

The spread in R values (Figure 4e) should not be interpreted as a range of tree throw frequency because it reflects the stochastic nature of tree throw. Only the average value of R is meaningful. By sampling 1910 hillslopes across Brown County, we attempt to exchange space for time so that for each primary direction, we have sampled values that approach the full range of natural topographic roughness and the average sample roughness is approximately equal to the expected roughness for a given population of hillslopes (e.g. east vs west).



Figure 4. a) Hillshade of Brown County, IN with points of selected hillslopes colored by the measured topographic variance. b) Topographic variance as a function of slope. Cumulative probability plots of measured topographic variance (c) and slope (d) colored by aspect. e) Rose diagram of violin plots for R illustrating a modest aspect dependency. f) Rose diagram of wind speeds (colors) and relative frequencies (gray).

²⁶⁹ 5 Discussion and Conclusions

We have developed theory that explains the topographic roughness of forested hill-270 slopes and a tool that maps the relative contributions to the volumetric sediment flux 271 from tree throw and creep-like processes. The topographic variance of a hillslope at any 272 moment is a convolution of a noisy signal through time that depends on the stochastic 273 occurrence of tree throw events and their decay due to creep-like processes. This leads 274 to a noisy signal of topographic roughness that oscillates around an expected value. In 275 general, greater average frequency of tree throw occurrences per area per time and lower 276 values for diffusivity lead to rougher hillslopes (e.g. the p/D term in Equation 8). This 277 is the first theory to address topographic roughness due to tree throw of forest floors and 278 is key for developing methods for quantifying tree throw. 279

Our theory assumes that at the scale of meters, pit-mound couplets are the primary 280 roughness feature on hillslopes. Temperate, moderate relief, forested hillslopes lack other 281 sources of roughness such as gopher mounds (Jyotsna & Haff, 1997), sediment mounds 282 that form under shrubs (Worman & Furbish, 2019) (semi-arid), landslides (LaHusen et 283 al., 2016; Booth et al., 2017) and their scarps (steeplands), and solifluction lobes (Glade 284 et al., 2021) (periglacial). Fossorial mammals either produce topographic roughness that 285 are too small (e.g. mole hills) or far too rare (e.g. bear burrows) to explain the observed 286 meter scale roughness in these landscapes. Lithologic contacts in such landscapes are lo-287 calized and affect few hillslopes. Creep-like processes unconditionally smooth topogra-288 phy (Furbish & Fagherazzi, 2001) so in forested settings we are confident that the to-289 pographic roughness in this setting is primarily driven by the production and decay of 290 tree throw couplets. 291

We have developed a topographic variable, R, to describe the relative fluxes due 292 to roughening processes (i.e. tree throw) and smoothing processes (e.g. creep). R is di-293 rectly measurable from topography and allows for widespread quantification of a pro-294 cess that is driven by stochastic events that occur with frequencies that frustrate direct 295 human observation. The roughness of the land-surface is a record of all past events over 296 timescales of decades to centuries which is required for measuring the contribution to 297 the flux for tree throw. In southern Indiana, R indicates that tree throw accounts for 298 roughly 11% to 18% of volumetric sediment flux. 299

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Despite the clearly rough hillslopes of southern Indiana, 11 to 18% represents a some-300 what modest contribution to the total hillslope sediment flux. However, we suggest that 301 tree throw is unlikely to contribute a majority of the volumetric sediment flux for sev-302 eral reasons. First, because soil is an unconsolidated medium, creep will always occur 303 (Ferdowsi et al., 2018; Deshpande et al., 2021) and tree throw can never account for all 304 of the volumetric flux. Second, although rough hillslopes are common in southern In-305 diana and are clearly observable, there are many more smooth and moderately rough hill-306 slopes (Figure 4b,c,e) that dominate the landscape. Third, tree throw is limited by pop-307 ulation dynamics (Gallaway et al., 2009; Gabet & Mudd, 2010) which sets the spacing 308 of trees, recruitment of new saplings, and growth rates. All of these may amount to an 309 upper limit of R being around what we have measured in southern Indiana. However, 310 further measurement of R in other settings are required to more definitively quantify the 311 limits of tree throw. 312

Despite the relatively small contributions to the volumetric flux, tree throw is a unique 313 hillslope transport process that may have an outsized role in influencing Critical Zone 314 processes. Tree throw episodically and suddenly creates topographic roughness, inverts 315 the soil column, and has the potential to expose fresh bedrock. Each of these has po-316 tential implications to affect hydrologic pathways (Phillips et al., 2017)), soil develop-317 ment (Samonil et al., 2020), chemical weathering, and soil production rates (Gabet & 318 Mudd, 2010). We anticipate that R will be a valuable tool that is readily available for 319 quantifying the magnitude and frequency of tree throw and its impact on the Critical 320 Zone. 321

Appendix A Mean Travel Distance

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We calculate the mean travel distance by assuming that a particle may be entrained/deposited from any location within the pit/mound. The pit and mound individually have a morphology that resembles a Rayleigh distribution,

$$f_z(z) = \frac{2z}{\omega^2} e^{-\frac{z^2}{\omega^2}} \tag{A1}$$

where z is the random variable and ω is a parameter. The mean of a Rayleigh distribution is

$$\mu_r = \frac{\sqrt{\pi}}{2}l. \tag{A2}$$

The total travel distance is the difference between the mean deposition location and mean entrainment location,

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$$\mu_r(r) = \sqrt{\pi}l \,. \tag{A3}$$

The volumetric entrainment rate, is the volume of the pit multiplied by a production rate, $p [L^{-2}],$

$$E(x,y) = p(x,y)\sqrt{\pi}l \int_{-\infty}^{\infty} \int_{-\infty}^{0} -\frac{2Ax}{l^2} e^{\left(-\frac{x^2}{l^2}\frac{y^2}{w^2}\right)} \mathrm{d}x\mathrm{d}y = p(x,y)\sqrt{2\pi}Awl.$$
(A4)

Equations (A3) and (A4) combine to form (3).

337 Appendix B Topographic Variance

The Fourier transform of (1) is

$$\hat{\zeta}(k_x, k_y) = -4iAwlk_x \pi e^{-\frac{k_x^2 l^2}{4} - \frac{k_y^2 w^2}{4}}, \qquad (B1)$$

where k_x and k_y is the wavenumber $[L^{-1}]$ (radians per unit length) in the x and y directions. The analytical solution for the diffusion of a couplet through time in wavenumber domain (B1) is

$$\hat{\zeta}(k_x, k_y, t) = -4iAwlk_x\pi e^{-k_x^2 \left(Dt + \frac{t^2}{4}\right) - k_y^2 \left(Dt + \frac{w^2}{4}\right)}$$
(B2)

where t [T] is age of the couplet. Parseval's Theorem states that the integral of the squared amplitudes of a Fourier transform equals the sum of squares of the original signal. Roughness has a mean of zero, so in this case Parseval's Theorem is directly related to topographic variance and we obtain a time-evolution of topographic variance of a single pitmound couplet. This step yields,

$$\sigma_{\zeta}^{2}(t) = \frac{1}{4\pi^{2}H} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |\hat{\zeta}(k_{x}, k_{y}, t)|^{2} \mathrm{d}k_{x} \mathrm{d}k_{y} = \frac{A^{2}w^{2}l^{2}\pi}{32H} \left(\frac{l^{2}}{4} + Dt\right)^{-3/2} \left(\frac{w^{2}}{4} + Dt\right)^{-1/2},$$
(B3)

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where
$$H$$
 [L²] is the area of the domain. The topographic variance of an entire hillslope
is the integral over all couplets of all ages which is presented in (6). Note that the pro-
duction rate, p has units (L⁻² T⁻¹) so that H is now included in p .

353 Acknowledgments

³⁵⁴ Data and Python scripts used to generate data are available at https://github.com/tdoane/Topographic-

Variance/ and will be available in a maintained in the IUScholarWorks repository upon

- ³⁵⁶ publication (https://openscholarship.indiana.edu/data-deposit). This project was sup ³⁵⁷ ported by the Environmental Resilience Institute, funded by Indiana Universitys Pre-
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Supporting Information for Topographic roughness on forested hillslopes: a theoretical approach for quantifying hillslope sediment flux from tree throw

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Introduction Here we provide supplemental information that supports the results presented in the main text. We address several items. First, we consider the role that DEM resolution plays. We compare measurements of topographic variance of the same hillslope from two different data sources and demonstrate that, so long as a DEM has a resolution less than a meter that it captures the majority of topographic variance. Second, we demonstrate that different flux models do not result in a meaningful difference in the

evolution of topographic variance of a single pit-mound couplet. Therefore, the results do not strongly depend on the choice of flux model. Third, we explain how we parameterized natural pit-mound couplets using high resolution topographic data. Fourth, we consider how initial pit-mound couplet geometry will vary on increasingly sloped terrain. On steeper slopes, more sediment is 'thrown' downslope and l increases. We present results from a simple numerical exercise which demonstrates that l increases linearly with land-surface slope. Last, we present a table of measured R values for 8 directions and the number of measurements in each direction.

1. Resolution We note that the measured topographic variance may differ between the 0.76 m and 0.25m resolution datasets. We anticipate that the finer resolution is closer to the actual resolution, however, we also anticipate that the difference between them is relatively small and does not alter the quantification of tree throw. To demonstrate this, measurements of topographic variance of a single hillslope on private property in Washington County demonstrates similar estimates of the topographic variance whether it is calculated using 0.25 m or 0.76 m-resolution topographic data. On a single hillslope, the measured topographic variance on 0.76 m and 0.25 m resolution topographic data are 0.012 and 0.014 m². We are confident that the 0.76 m resolution data is capable of capturing a clear majority of the topographic variance at the meter scale. Lidar data for the high resolution DEM from Washington County was collected by a drone in December 2018. Data collection and processing are outlined in (Lewis et al., 2020).

2. Flux Models We have developed and demonstrated a theory for topographic roughness of forest floors that casts the expected topographic roughness in terms of the rate of

tree throw production and the rate of topographic degradation by linear diffusion which is driven by creep-like processes. There are alternatives to linear diffusion to describe topographic evolution, namely nonlinear (Roering et al., 2001, 2007) and soil thickness (Furbish et al., 2009; Mudd & Furbish, 2004) dependent models. The nonlinear model (CITE Roering et al., 1999) is widely used and states that the flux increases nonlinearly with land-surface slope until a critical gradient,

$$q_c = -D_{cn} \frac{\nabla \zeta}{1 - \left(\frac{|\nabla \zeta|}{S_c}\right)^2},\tag{1}$$

where D_n [L² T⁻¹] is a topographic diffusivity and S_c is a critical slope above which the flux is unbound. A soil thickness-dependent model results from variations in particle motions that vary with depth within the soil. In most soils, porosity decreases with depth and leads to an exponential-like porosity profile which results in an exponential particle velocity profile. In general, thicker soils will have a greater particle velocity near the surface and have larger depth-averaged velocities which leads to a soil-thickness dependency which can be approximated by (Furbish et al., 2009),

$$q_c = -D_n h(x) \frac{\partial \zeta}{\partial x} \,, \tag{2}$$

where D_{ch} [L T⁻¹] is another topographic diffusivity for creep-like processes but has different units than D_c and incorporates the depth-dependency of transport. Using either of these two alternatives to describe the flux will change the time evolution of pit-mound couplets. Numerical simulation of pit-mound couplets according to all three models demonstrates that, although they lead to slight differences in topographic evolution, the evolution of topographic variance follow similar paths.

3. Fitting Pit-Mound Couplets

We use high resolution DEMs with 0.25 m resolution to inform our parameters for pitmound couplet geometry. An approximately 1 km² plot of land in south-central Indiana was scanned with a lidar-equipped UAV-drone. This particular site has over 600 mapped pit-mound couplets. We selected over 100 of these and fit the idealized geometry to them using a routine in Python which returned values for A, l, w, the orientation, and a squared difference between the observed and modeled. The average difference between observed and modeled is often less than 0.1 meters (Figure B1). In many cases, the amplitudes and dimensions of the couplets appear to match the natural couplets. However, the mismatch also includes the differences between the rough and potentially sloped ground outside of the couplet which contributes to the mismatch values.

4. Initial Pit-Mound Geometry We expect that the initial pit-mound couplet geometry varies with slope because, on steeper slopes, more sediment is deposited downslope of the pit. This will lengthen the couplet, and *l* should be longer on steeper slopes. We have created a simple one-dimensional model that simulates the initial uprooting and deposition of sediment on hillslopes with different steepness. The model treats a root mass as a one-dimensional rectangle that gets uprooted so that the long axis is perpendicular to the land-surface. This mass of sediment is then virtually dropped to the land-surface which creates an angular profile of a pit-mound couplet, which has unrealistic slopes (Figure S4a). The model numerically diffuses the angular pit-mound couplet until the maximum slope is below a critical slope. In this case, we have set a critical slope of 1. Running this model on couplets formed on different slopes produces pit-mount couplet geometries that vary with land-surface slope (Figure S4b). In particular, there is a nonlinear relation-

ship between the length-scale of couplet geometries and land-surface slope (Figure S4c). We simplify this relationship and assume a linear relationship as most slopes in southern Indiana are below 0.6.

Data Table of measured R values by direction and the number of hillslopes measured.

Aspect	\bar{R}	# hillslopes
North	0.18	292
Northeast	0.22	410
East	0.22	463
Southeast	0.19	189
South	0.19	63
Southwest	0.16	100
West	0.14	163
Northwest	0.17	231

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Figure S1. High pass filter of topography of a hillslope in Washington County, IN from 0.25-m (a) and 0.76-m (b) resolution data. The same pit-mound couplets are clearly visible in both datasets and measured variance values are similar.

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Figure S2. (a) Topographic evolution of a pit-mound couplet according to linear, nonlinear, and soil thickness-dependent transport models. Pit-mound couplets were originally on a background slope of 0.4 and we have used $S_c=1.2$ and $\mu_h=1$ m (b) Time evolution of topographic variance of pit mound couplets according to all three models. The choice of model is apparently relatively unimportant for the time-series of topographic variance of pit-mound couplets.



Figure S3. (a) Parameters extracted from 101 couplets from 0.25 m resolution lidar. Red dots are identified as the freshest as the 50 highest values of A/lw. (b) Four examples of natural couplets (colored surface) and the fit couplet (contours) with average deviation over the domain recorded in the top of the image.



Figure S4. a) One dimensional model of an initial pit-mound couplet where a rectangle is uprooted perpendicular to the slope and all mass is dropped straight down on different slopes. On steeper slopes, more sediment falls downslope of the pit. b) Initial conditions of pit-mound couplets when we diffuse the profiles in (a) until a threshold slope is met which is 1 in this case. c) Length-scale of the idealized pit-mound couplet that best fits the initial conditions in (b).