Stratospheric adiabatic mixing rates derived from the vertical gradient of age of air

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Abstract

The circulation of the stratosphere transports important trace gases, including ozone, and can be thought of as having a fast horizontal mixing component and a slow meridional overturning component. Measuring the strength of the circulation directly is not possible, and so it must be inferred from tracer measurements. Long-lived trace gases can be related to the idealized tracer age of air, which describes how long an air parcel has been in the stratosphere. In this paper, we derive a quantitative relationship between the vertical gradient of age and the horizontal mixing between the tropics and the extratropics using a "leaky pipe" framework in isentropic coordinates. Mixing rates of air into and out of the tropics are related to the vertical gradient of age in the tropics and in the extratropics, respectively. The derivation is repeated with the hemispheres separated so that the vertical structure of the mixing in the two hemispheres can be compared directly. These theories are applied to output from an idealized model of the stratosphere and from a realistic chemistry-climate model to test our assumptions and calculate the mixing rates in the models. We then perform a quantitative comparison of the mixing rates in the Northern and Southern hemisphere along with an examination of where such a separation is valid. Finally, we perform a very preliminary calculation of mixing efficiency with satellite data to demonstrate the use of the mixing metric to compare mixing models and data.

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¹⁰ Key Points:

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11	•	A new metric for adiabatic mixing in the stratosphere is developed from the age
12		of air tracer
13	•	We examine hemispheric asymmetry and discuss the slow time evolution of the
14		flow

 We calculate this metric to perform a preliminary comparison between models and satellite data

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17 Abstract

The circulation of the stratosphere transports important trace gases, including ozone, 18 and can be thought of as having a fast horizontal mixing component and a slow merid-19 ional overturning component. Measuring the strength of the circulation directly is not 20 possible, and so it must be inferred from tracer measurements. Long-lived trace gases 21 can be related to the idealized tracer age of air, which describes how long an air parcel 22 has been in the stratosphere. In this paper, we derive a quantitative relationship between 23 the vertical gradient of age and the horizontal mixing between the tropics and the ex-24 tratropics using a "leaky pipe" framework in isentropic coordinates. Mixing rates of air 25 into and out of the tropics are related to the vertical gradient of age in the tropics and 26 in the extratropics, respectively. The derivation is repeated with the hemispheres sep-27 arated so that the vertical structure of the mixing in the two hemispheres can be com-28 pared directly. These theories are applied to output from an idealized model of the strato-29 sphere and from a realistic chemistry-climate model to test our assumptions and calcu-30 late the mixing rates in the models. We then perform a quantitative comparison of the 31 mixing rates in the Northern and Southern hemisphere along with an examination of where 32 such a separation is valid. Finally, we perform a very preliminary calculation of mixing 33 efficiency with satellite data to demonstrate the use of the mixing metric to compare mix-34 ing models and data. 35

36 1 Introduction

Understanding the circulation of the stratosphere has developed through observa-37 tions of trace gases, and in particular ozone (Dobson et al., 1929) and water vapor (Brewer, 38 1949). Both Dobson and Brewer surmised that upward motion in the tropics, followed 39 by slow, poleward movement and downwelling in the extratropics would be consistent 40 with the observed trace gas distributions. Neither meridional motion on a rotating sphere 41 nor vertical motion through a stratified fluid is easily achieved, however; meridional mo-42 tion requires a torque and vertical motion requires diabatic heating. Both of these are 43 provided by the deposition of pseudomomentum by the breaking of planetary-scale waves 44 in the stratosphere. These breaking waves also cause a substantial amount of stirring within 45 the isentropic layers; indeed, this is the dominant effect. This behavior provides the most 46 basic picture of stratospheric circulation: Wave breaking drives rapid isentropic motions, 47 and it also causes slow vertical and poleward motion (Plumb, 2002). The mean mass trans-48 port within the stratosphere has come to be known as the Brewer–Dobson Circulation 49 (BDC) (Butchart, 2014). 50

Over 70 years after Brewer's paper, many inferences about the strength and vari-51 ability of the stratospheric circulation are still tracer-based. Although estimates of trends 52 in the BDC have been calculated from satellite temperature observations (Fu et al., 2015), 53 even this calculation relied on ozone and water vapor data. Tracking the vertical prop-54 agation of the seasonal variations in water vapor concentrations is one example of us-55 ing tracer observations to understand the BDC and mixing (e.g., Glanville & Birner 2017). 56 Variations in lower stratospheric water vapor concentrations are also linked to large-scale 57 changes in the circulation on interannual timescales (Randel et al., 2006). Recent work 58 has also suggested using a combination of many trace gases and inverting a large suite 59 of observations to find a best fit solution (von Clarmann & Grabowski, 2016), although 60 this has yet to be effectively applied in practice. 61

Although chemical tracers can be observed directly, a theoretical tracer is also useful for thinking about the stratospheric circulation. The idealized tracer "age of air" is a measure of how long a parcel of air has been in the stratosphere (Hall & Plumb, 1994) and contains the average history of the trajectories of the bits of air that make up the parcel. Age of air has a zero boundary condition at the tropopause and a unit source as long as it is in the stratosphere, or it can be formulated in terms of a tracer that is conserved in the stratosphere and has a source in the troposphere that is linearly increas ing in time (Boering et al., 1996). Although this is just replacing one idealized tracer with
 another, the linearly increasing tracer is far more realistic.

It is necessary to approximate age from observations because no species has a con-71 stant growth rate or is perfectly conserved; sulfur hexafluoride (SF_6) and carbon diox-72 ide (CO_2) are approximately linearly increasing, but SF₆ has a mesospheric sink and CO₂ 73 has a strong seasonal cycle. To convert these real tracers to the idealized age tracer, cer-74 tain assumptions must be made about the overall distribution of ages that are represented 75 76 in the observed sample (Waugh & Hall, 2002). The details of how age of air is calculated from tracers can change whether the in situ measurements from the past 40 years show 77 a trend or not (Fritsch et al., 2020). Some recent work suggests using a suite of tracers 78 to constrain the distribution of ages (Hauck et al., 2019). However, distinct tracers do 79 not necessarily provide distinct degrees of freedom, since long-lived tracers all have com-80 pact relationships with each other (Plumb, 2007). Moreover, real physical links between 81 the circulation and the tracers are somewhat obfuscated by this purely data-driven ap-82 proach. To best understand the stratosphere, the underlying understanding of the char-83 acteristics and physics of the BDC should be included while attempting to quantify the 84 strength of that circulation. 85

The BDC consists of two branches, a deep branch associated with dissipation of 86 planetary scale waves in the middle and upper stratosphere, and a shallow branch as-87 sociated with breaking of synoptic and planetary waves just above the subtropical jet 88 (Plumb, 2002; T. Birner & Bönisch, 2011; McLandress & Shepherd, 2009). The net zonal 89 mean meridional mass transport is frequently expressed in the form of the Transformed 90 Eulerian Mean (TEM) residual circulation (D. G. Andrews & McIntyre, 1976 e.g., Butchart 91 et al., 2006; Garcia & Randel, 2008) or, more rarely, the diabatic circulation (Linz et al., 92 2016). These treatments are mostly equivalent, depending on the choice of calculation 93 method for the TEM residual circulation (Linz et al., 2019). The diabatic circulation has 94 the advantage that it can be directly related to age (Linz et al., 2016), and thus calcu-95 lated from global satellite tracer measurements (Linz et al., 2017). 96

Typical metrics for the BDC either are explicitly global or are for the tropics only, 97 precluding separation of the two hemispheres. The two hemispheres should not be ex-98 pected to be symmetric, however. The climatological wave driving in the Northern and qq Southern hemispheres differ (e.g. Labitzke et al. 1980, Rosenlof 1996). Furthermore, long-100 term variability in the two hemispheres also differs; with the development of the ozone 101 hole in the Southern Hemisphere until year 2000 and then the subsequent, erratic, and 102 ongoing recovery (Solomon et al., 2016), asymmetric long-term variability seems rather 103 likely (Polvani et al., 2019). Moreover, observations of the time evolution of certain trace 104 gases suggest such asymmetric changes in the circulation (Mahieu et al., 2014). These 105 factors all indicate a need for tracer-based, quantitative metrics for the circulation that 106 can separate the variability in the two hemispheres. 107

The wave breaking that drives the meridional flow also causes turbulent, irreversible 108 mixing (McIntyre & Palmer, 1984), sometimes referred to as "two-way mixing" because 109 of the two-way mass exchange between the tropics and the midlatitudes (Garny et al., 110 2014). Stratospheric mixing is quite uncertain, with state-of-the-art models disagreeing 111 by at least a factor of two by one metric (Dietmüller et al., 2018). Previous studies of 112 mixing have used two main approaches: 1) treating mixing as a diffusivity (Newman et 113 al., 1986; Haynes & Shuckburgh, 2000; Allen & Nakamura, 2001; Leibensperger & Plumb, 114 2014) and 2) using age of air to infer some metric of mixing (Garny et al., 2014; Ploeger, 115 116 Abalos, et al., 2015; Ploeger, Riese, et al., 2015; Ray et al., 2010, 2014, 2016; Moore et al., 2014). The present work will also use age, and so a brief summary of the latter is 117 in order. 118

In the calculation of "Aging by Mixing" (Garny et al., 2014; Ploeger, Abalos, et 119 al., 2015; Ploeger, Riese, et al., 2015), the age of air calculated from an ideal age tracer 120 in a model is compared to the age that air would be if it were to simply age at a con-121 stant rate following the TEM residual circulation streamfunction, and the difference is 122 surmised to be due to mixing. This creates a two dimensional zonal mean structure of 123 "Aging by Mixing", which clearly demonstrates that age reflects both the residual cir-124 culation and mixing. Beyond qualitative comparisons, however, this two-dimensional field 125 is difficult to interpret, and this method is useful for models only. Another age-based tech-126 nique used to examine mixing adapts the Tropical Leaky Pipe (TLP) of Neu & Plumb 127 (1999) to look at mixing efficiency and to understand the impact of mixing on age (Ray 128 et al., 2010, 2014, 2016; Moore et al., 2014). The TLP model envisions a well-mixed "trop-129 ical pipe" that is relatively isolated from the well-mixed extratropics with a constant ver-130 tical velocity in the tropics and a constant mixing efficiency between the two regions. Its 131 vertical coordinate is height, which has the advantage of being physically intuitive. The 132 adaptations of the model have relaxed some of the assumptions, allowing for vertical vari-133 ations in the vertical velocity, and have incorporated multiple trace gases. The studies 134 by Ray et al. (2014) and Ray et al. (2016) include running the TLP with Lagrangian for-135 ward particle trajectories to be able to examine the full age spectra and mixing. These 136 various approaches to mixing yield quantitatively different results, as they are quanti-137 fying different (though related) things. 138

More recently, the isentropic age-budget theory proposed in Linz et al. (2016) and 139 in this paper has been applied to quantify and compare differences in stratospheric trans-140 port among state-of-the-art primitive equation solvers (a.k.a. dynamical cores). An in-141 termodel stratospheric transport benchmark test (proposed in Gupta et al., 2020) revealed 142 a strong impact of numerics on transport. Modern cores with different numerics were 143 identically forced at varying resolutions, but were found to converge towards different 144 stratospheric circulation and strikingly different stratospheric age. A following study (Gupta 145 et al., submitted) aimed at understanding this spread in age, used the theory along with 146 a numerically integrated TLP with vertically varying parameters estimated from mod-147 els to isolate the contribution of each process (diabatic circulation, isentropic mixing and 148 numerical diffusion) towards the spread. The study found a strong tropical control on 149 stratospheric tracer transport and concluded that persisting differences in model repre-150 sentation of both diabatic circulation and mixing, even at high resolution, can lead to 151 a significant intermodel spread in stratospheric trace gas transport. 152

In this paper, we seek to provide a comprehensive description of the stratospheric circulation in terms of age. We derive a new relationship between age of air and the circulation analytically based on the TLP framework in isentropic coordinates. The use of isentropic coordinates allows for a straightforward separation of the diabatic circulation from the adiabatic mixing. This is an extension of the theory developed for the diabatic circulation in Linz et al. (2016), and this theory also requires neither model runs nor Lagrangian trajectory calculations for calculating metrics of stratospheric transport.

We derive a theory to calculate the mean adiabatic mixing at every level using the 160 vertical gradient of age (Section 2) in separate hemispheres, thus improving upon the 161 TLP model by considering vertical variations in mixing and in vertical velocity. In Sec-162 tion 4, we apply the theory to output from an idealized and a comprehensive model (de-163 scribed in Section 3), and we show the circumstances under which the hemispheres can 164 be treated separately. Critically, the mixing metric can be calculated from observations, 165 and with numerous caveats about the limitations of both the theory and especially the 166 data, we do so using satellite data in Section 5. Implications and limitations of this study 167 are discussed in Section 6. 168

¹⁶⁹ 2 Theory

Linz et al. (2016) related the age of air on an isentropic surface to the mass flux through that surface. Starting from the ideal age equation, assuming steady state and neglecting diabatic diffusion, they showed that the difference in the the mass-flux-weighted age of downwelling and upwelling air on an isentropic surface is equal to the ratio of total mass above that surface to the total diabatic overturning flux through that surface:

$$\Delta \Gamma = M/\mathcal{M}.\tag{1}$$

 $\Delta \Gamma = \Gamma_d - \Gamma_u \text{ is the difference in mass-flux-weighted age averaged over the downwelling$ and upwelling regions, <math>M is the total mass above the isentrope and \mathcal{M} is the overturning mass flux through the isentrope. This is related to the TLP of Neu & Plumb (1999), who divided the stratosphere into "tropics" and "extratropics" based on the edge of the surf zone rather than the zero in upwelling. The key to establishing a parallel relationship to the TLP is to define the ages with a mass-flux weighting. The mass-flux-weighted downwelling and upwelling ages, Γ_d and Γ_u respectively, are defined:

$$\Gamma_u(\theta) = \left[\int_{up} \sigma \dot{\theta} dA\right]^{-1} \int_{up} \sigma \dot{\theta} \Gamma dA, \qquad (2)$$

182 and

$$\Gamma_d(\theta) = \left[\int_{down} \sigma \dot{\theta} dA \right]^{-1} \int_{down} \sigma \dot{\theta} \Gamma dA.$$
(3)

where Γ is the age, $\dot{\theta}$ is the diabatic vertical velocity, $\sigma = -g^{-1}\partial p/\partial \theta$ is the isentropic 183 density, and the upwelling and downwelling regions are defined as where $\theta > 0$ and where 184 $\dot{\theta} < 0$, respectively. Integration over each region is designated by the integration lim-185 its up and down. These regions can vary in the vertical. Like Neu & Plumb (1999), we 186 make the simplifying assumption that the air coming into the tropics has the average 187 age of the extratropical region (Γ_d), and likewise the air leaving the tropics has the av-188 erage age of the tropical region (Γ_{μ}) , although the definitions here are mass-flux-weighted. 189 This assumption is one of the primary sources of error in this method. Hemispheric sym-190 metry is implied (because both tropical boundaries are treated together). 191

The overturning mass flux, the diabatic circulation, is equal in the upwelling and downwelling regions in steady state and is given by

$$\int_{up} \sigma \dot{\theta} dA = -\int_{down} \sigma \dot{\theta} dA = \mathcal{M}(\theta). \tag{4}$$

These equations and definitions, repeated from Linz et al. (2016), demonstrate that the horizontal difference of age is set exclusively by the diabatic circulation. In Figure 1a, an idealized diabatic circulation streamfunction is shown in isentropic coordinates with one level that is wholly within the stratosphere highlighted. The upwelling and downwelling regions are in green and purple respectively. Mixing has no role in setting the difference in age along the isentropic surface, but mixing will be critical in determining the vertical gradient.

In what follows, we show that that the vertical (cross-isentropic) gradient of age is related to the adiabatic mixing, with the assumption of steady state and neglecting diabatic diffusion.

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2.1 Vertical tropical age gradient

Consider the schematic in Figure 1b. A second isentropic surface is now highlighted. (Both θ_1 and θ_2 are wholly within the stratosphere.) The regions where the vertical velocity, $\dot{\theta}$, is upwards are again shown in purple and the regions where it is downwards are shown in green. For the sake of this current qualitative argument, let the hemispheres



Figure 1. Schematics of the stratospheric circulation: a) global circulation in dotted and thin solid lines through one isentrope, with upwelling region shown in purple and downwelling regions shown in green. Upwelling and downwelling mass fluxes are shown in purple and green arrows, respectively, and have a mass-flux-weighted mean age of Γ_u and Γ_d . b) as before, but with an additional isentropic layer shown. The dash-dot lines represent the edges of the tropical pipe, or the turnaround latitudes. This is where the diabatic vertical velocity, $\dot{\theta}$, is zero and they can have a varying latitude with height. c) same as b), but with mixing into and out of the tropics shown in orange arrows. d) Same as in c) but now with separate hemispheres that are divided by a dynamical equator (light gray solid line) corresponding to the zero streamline in the time mean of the circulation. Here the Northern Hemisphere is shown as having a greater meridional extent, consistent with reanalyses. Although this diagram shows the dynamical equator as vertical, it can also vary with height.

to be symmetric and consider that both the average age and the upwelling mass flux are 209 known at the first level. Then, in the absence of mixing, the upwelling age on θ_2 is the 210 sum of the age at θ_1 and the time it takes for air to traverse the distance from $\theta_2 - \theta_1$. 211 If the air at θ_2 is any older, this additional age is due to mixing between the upwelling 212 and the downwelling regions. Because the upwelling mass flux can be determined by the 213 difference between the upwelling and downwelling age, according to (1), the mixing can 214 thus be determined by knowledge of the vertical age gradient and the horizontal age dif-215 ference. Figure 1c is identical to 1b with the addition of orange arrows that represent 216 the total mass flux into and out of the tropics due to this horizontal transport. 217

We develop the above qualitative arguments into a quantitative theory by considering the integration of the ideal age equation above an isentope in the tropical region to gain insight into the mixing between the tropics and extratropics. Here, "tropics" will
be used to refer to the region where air is upwelling through an isentrope, and the "extratropics" where air is downwelling. Age is considered to be well-mixed within tropics
and within the extratropics. As before, this is a steady-state derivation where the diabatic diffusion is negligible.

The ideal age equation (Waugh & Hall, 2002) states that the total derivative of age is equal to a source of 1 (year/year):

$$\frac{\partial \Gamma}{\partial t} + \mathcal{L}(\Gamma) = 1, \tag{5}$$

where \mathcal{L} is the advection-diffusion operator, with a boundary condition of zero age at the tropopause.

Because we are considering the statistically steady state, we neglect the time derivative. Integrating this equation over the total mass above the upwelling region of an isentrope (using the divergence theorem to address the bottom and extratropical boundaries) yields:

$$\int_{up} \mathbf{n} \cdot \mathbf{F}^{\Gamma} dA - \int \oint \sigma V_{in} \Gamma dl d\theta + \int \oint \sigma V_{out} \Gamma dl d\theta = \int_{\mathcal{V}_{up}} \sigma dA d\theta.$$
(6)

 V_{in} and V_{out} are the integrated meridional velocity across the boundary between the upwelling and downwelling regions, **n** is the vertical unit normal vector in isentropic coordinates, and \mathbf{F}^{Γ} is the mass-weighted age flux. Because diabatic diffusion is assumed to be negligible, the vertical transport is purely advective, and taking the vertical derivative in entropy results in

$$\frac{\partial}{\partial \theta} \int_{up} \sigma \dot{\theta} \Gamma dA - \oint \sigma V_{in} \Gamma dl + \oint \sigma V_{out} \Gamma dl = \int_{up} \sigma dA.$$
⁽⁷⁾

It is useful to define the entrainment and detrainment mass fluxes μ_{in} and μ_{out} (units of mass per unit theta per unit time) as follows:

$$\mu_{in} = \oint \sigma V_{in} dl, \tag{8}$$

240 and

$$\mu_{out} = \oint \sigma V_{out} dl. \tag{9}$$

The integral of the density will be indicated by $\Sigma_u = \int_{up} \sigma dA$. With these notation changes and simplifications, we can rewrite (7) as:

$$\frac{\partial}{\partial \theta} \int_{up} \sigma \dot{\theta} \Gamma dA + \mu_{out} \Gamma_u - \mu_{in} \Gamma_d = \Sigma_u.$$
(10)

Then, the change in the diabatic circulation with entropy is due to the difference between the entrainment and detrainment mass fluxes:

$$\frac{\partial \mathcal{M}}{\partial \theta} = \mu_{in} - \mu_{out} = \frac{\partial}{\partial \theta} \int_{up} \sigma \dot{\theta} dA.$$
(11)

We rewrite (10) in terms of \mathcal{M} and Γ_u :

$$\frac{\partial}{\partial \theta} \mathcal{M} \Gamma_u + \mu_{out} \Gamma_u - \mu_{in} \Gamma_d = \Sigma_u, \tag{12}$$

and with (11), this becomes

$$\mathcal{M}\frac{\partial\Gamma_u}{\partial\theta} = \Sigma_u + \mu_{in}\Delta\Gamma.$$
(13)

The right hand side of this equation includes the two processes that determine the increase of age: Σ_u , which is the mass-weighted rate at which the air ages along the diabatic circulation, and $\mu_{in}\Delta\Gamma$, which is the rate at which adiabatic mixing between the tropics and extratropics increases the age of air. The mixing rate can be defined as μ_{in}/Σ_u . Apart from μ_{in} , all of the terms in (13) can be easily diagnosed.

The equivalent extratropical expression is

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$$-\mathcal{M}\frac{\partial\Gamma_d}{\partial\theta} = \Sigma_d - \mu_{out}\Delta\Gamma,\tag{14}$$

which can be derived in essentially the same way, and the derivation for the Southern Hemisphere extratropics is included as an Appendix.

We solve equation 14 for the adiabatic rate of entrainment into the downwelling region:

$$\frac{\mu_{out}}{\Sigma_d} = \frac{\mathcal{M}}{\Sigma_d \Delta \Gamma} \frac{\partial \Gamma_d}{\partial \theta} + \frac{1}{\Delta \Gamma},\tag{15}$$

²⁵⁷ and similarly express the adiabatic rate of entrainment into the upwelling region

$$\frac{\mu_{in}}{\Sigma_u} = \frac{\mathcal{M}}{\Sigma_u \Delta \Gamma} \frac{\partial \Gamma_u}{\partial \theta} - \frac{1}{\Delta \Gamma}.$$
(16)

The mixing rate derived in this way is closely related to previous work, such as that 258 by Garny et al. (2014) or Neu and Plumb (1999). With the formulation of this theory 259 in isentropic coordinates, the mean entrainment mass flux, μ_{in} , is necessarily the adi-260 abatic contribution, and our treatment has avoided the assumptions of constant mixing 261 efficiency and vertical velocity with height. Mixing efficiency, ϵ , was defined as the ra-262 tio of the entrainment mass flux into the tropics to the net detrainment mass flux into 263 the extratropics by Neu & Plumb (1999) and has been used frequently since (e.g. Ray 264 et al., 2016, Dietmüller et al., 2018). In our framework, ϵ is height dependent, and is given 265 by the expression 266

$$\epsilon = \frac{\mu_{in}}{\mu_{out} - \mu_{in}} = \frac{\mu_{in}}{\partial \mathcal{M} / \partial \theta}.$$
(17)

Subject to caveats about mass-flux-weighting as opposed to area-weighting and the assumptions of hemispheric symmetry and a well-mixed extratropics, this enables a direct estimation of the adiabatic mixing from age of air data. The steady-state assumption is necessary for this result to apply, however, and so long data records are required to perform this calculation.

2.2 Circulation in each hemisphere

Figure 1d shows schematically the separation of the two hemispheres with the adi-273 abatic mixing in orange and the diabatic circulation shown in the purple and green ar-274 rows. The hemispheres are separated by a dynamical equator, which is the zero stream-275 line of the steady state flow and need not be constant in the vertical. Using this zero stream-276 line as the separation will ensure that there is no net mass flux from one hemisphere to 277 the other, helping to make the hemispheres more like closed systems. The dash-dot lines 278 show the separation between the upwelling and downwelling regions, corresponding to 279 the zero of the diabatic velocity. These also can vary in the vertical. There is still an as-280 sumption related to hemispheric symmetry that is necessary, namely that the mass-flux-281 weighted age of upwelling air in the two different hemispheres is equal $(\Gamma_{u_S} = \Gamma_{u_N})$, 282 or close enough so that mixing across the zero streamline is negligible for the total age 283 budget. This assumption is naturally met by the prior assumption of well-mixed trop-284 ics and is therefore not a more stringent requirement than in the global mean case. If 285 that assumption is valid, any adiabatic mixing within the tropics will have no impact 286 on the treatment of two separate hemispheres as closed systems. If the assumption is not 287



Figure 2. Zonal mean, time mean age of air shown in colors versus latitude and potential temperature for a) the idealized model, b) the WACCM model and c) the GOZCARDS N₂O-age product (Linz, 2017). Contours are spaced every 0.5 years. Also shown in a) and b) are the streamlines calculated based on the total diabatic circulation in kg m⁻¹ s⁻¹ with contours spaced logarithmically. White areas in c) are places where sometimes the N₂O measurement is out of the range of the relationship between N₂O and age of air.

valid, we could nevertheless make progress by considering the net age flux between the
 two hemispheres as a separate term in the age budget, and we are examining this in on going work.

If the hemispheres are closed systems, the theory described in Linz et al. (2016) and briefly revisited above can be applied separately to each hemisphere. We state some consequences of this application. The total diabatic mass flux through an isentropic surface is now separated into Northern hemisphere mass flux, $\mathcal{M}_{\mathcal{N}}$, and Southern hemisphere mass flux, $\mathcal{M}_{\mathcal{S}}$:

$$\mathcal{M} = \mathcal{M}_{\mathcal{N}} + \mathcal{M}_{\mathcal{S}}.\tag{18}$$

Similarly, the total mass above the isentropic surface in each hemisphere $(M_N \text{ and } M_S)$ will be the total mass above the surface within the hemisphere, such that

$$M = M_{\mathcal{N}} + M_{\mathcal{S}}.\tag{19}$$

The age difference in each hemisphere is the difference between the mass-flux-weighted age of air downwelling through the isentrope in that hemisphere and the mass-flux-weighted age of upwelling air averaged between the $\dot{\theta} = 0$ line and the dynamic equator. Assuming no exchange between the two hemispheres or that the air exchanged in the tropics is of the same age, we have

$$\Delta\Gamma_{\mathcal{S}}\mathcal{M}_{\mathcal{S}} = M_{\mathcal{S}} \tag{20}$$

303 and

$$\Delta\Gamma_{\mathcal{N}}\mathcal{M}_{\mathcal{N}} = M_{\mathcal{N}}.$$
(21)

The derivation for the relationship between the mixing and the vertical gradient of age is nearly identical to the global tropical case considered above. In the Appendix, we have perfomed this derivation for the Southern hemisphere extratropics, and we state the results for the Southern hemisphere tropics and extratropics here:

$$\mathcal{M}_{\mathcal{S}}\frac{\partial\Gamma_{u_{\mathcal{S}}}}{\partial\theta} = \Sigma_{u_{\mathcal{S}}} + \mu_{in_{\mathcal{S}}}\Delta\Gamma_{\mathcal{S}},\tag{22}$$

308 and

$$-\mathcal{M}_{\mathcal{S}}\frac{\partial\Gamma_{d_{\mathcal{S}}}}{\partial\theta} = \Sigma_{d_{\mathcal{S}}} - \mu_{out_{\mathcal{S}}}\Delta\Gamma_{\mathcal{S}}.$$
(23)

These hold for the Northern hemisphere as well. Thus, using the age distribution, the temperature, and the pressure, the mean entrainment and detrainment mass fluxes can be determined for both hemispheres. For this to be valid, the mixing of age across the dynamical equator should be negligible for the age budget. The dynamical equator can move with time, but integrating over long enough periods for the steady state assumption to be valid should cause the effect of this movement on the age transport to be small.

316 3 Model and Data Descriptions

Linz et al. (2016) tested the relationship between the diabatic circulation and the 317 difference in upwelling and downwelling age of air on an isentrope using an idealized model 318 with and without a seasonal cycle. We utilize a closely related idealized model setup here. 319 The use of idealized models enables focus on the key resolved dynamical processes by 320 not introducing any uncertainties on global circulation and transport related to phys-321 ical parameterizations. Moreover, the use of idealized models alongside comprehensive 322 ones provides a testbed to evaluate the theory in Section 2 in the absence of any explicit 323 trends in circulation which might be present in a freely evolving comprehensive model. 324

The study employs the FV3 finite volume dry dynamical core developed at the Geo-325 physical Fluid Dynamics Laboratory (Putman & Lin, 2007). The core uses a cubed-sphere 326 discretization in the horizontal and uses Lagrangian coordinates in the vertical. The model 327 is integrated using a C48 cubed sphere horizontal grid which corresponds to an effective 328 horizontal resolution of 2°. In the vertical, 40 $\sigma-p$ hybrid levels are employed, of which 329 24 pure-pressure levels are located between the model top and 100hPa. A similar setup, 330 but devoid of a seasonal cycle, has also been previous employed by (Gupta et al., 2020) 331 to study the impact of numerics and resolution on the climatological age of air profile 332 in the stratosphere. 333

We work with dry dynamics and do not include moisture or oceans. Diabatic heat-334 ing in the troposphere and stratosphere, in the idealized model, is represented by New-335 tonian relaxation towards a slightly modified version of the analytical equilibrium tem-336 perature profiles proposed in Held & Suarez (1994) and Polvani & Kushner (2002) re-337 spectively. The modification implements a seasonally varying temperature profile in both 338 the troposphere and stratosphere and is identical to the one proposed in Kushner & Polvani 339 (2006). The vertical lapse rate parameter γ in the forcing, which determines the strato-340 spheric polar vortex strength, is set to $\gamma = -6$ K/km and the maximum hemispheric asym-341 metry parameter ϵ is set to $\epsilon = 10$ K. Seasonality in the tropospheric forcing is imple-342 mented by allowing the ϵ parameter to oscillate between -10 K and 10 K annually. Sim-343 ilarly, in the stratosphere the equilibrium temperature at the poles annually oscillates 344 between the vertically increasing US Standard Temperature (1976) profile and the uni-345 form lapse rate (γ) radiative cooling profile. The equilibrium temperature is further mod-346 ified to raise the climatological tropopause in the model closer to the observed tropopause. 347 (Details of the modification are provided in Appendix B.) 348

The southern hemisphere has no topography. To represent stronger planetary wave forcing in the Northern Hemisphere, a sinusoidal wave-2 topography as in Gerber & Polvani (2009)) with a height amplitude of 4 km centered at 45° N was imposed. The contrast in boundary wave forcing presents an extreme test for the hemispheric separation theory.

The age is computed by introducing a clock tracer near the surface (Hall & Plumb, 1994). In the source region, defined as $p \ge 700$ hPa to be consistent with the height of surface friction layer in Held & Suarez (1994), the clock tracer concentration χ is specified to be $\chi(\lambda, \phi, p, t) = t$ for $p \geq 700$ hPa, where t is the model integration time, λ is the longitude and ϕ is the latitude. The model is run for 50 years, and the last 25 years are used for this analysis in order to ensure the upper level age distribution has reached steady state.

Given the absence of so many physical processes in the idealized model; to better 361 understand the application of both the age difference theory and the vertical age gra-362 dient theory developed above, we use a comprehensive global model. The model is the 363 Community Earth System Model 1 Whole Atmosphere Community Climate Model (WACCM), 364 an interactive chemistry-climate model (Marsh et al., 2013; Garcia et al., 2017). This 365 model has the physical parameterizations and finite-volume dynamical core (Lin, 2004) 366 from the Community Atmosphere Model, version 4 (Neale et al., 2013), and its domain 367 extends from the surface to 140 km, with 31 pressure levels from 193-0.3 hPa. The hor-368 izontal resolution is 2.5° longitude by 1.875° latitude. The WACCM simulations are based 369 on the Chemistry Climate Model Initiative REF-C1 scenario (Morgenstern et al., 2017). 370 An ideal age tracer is included and is specified as in Garcia et al. (2011), with a uniform 371 mixing ratio at the lower boundary that is linearly increasing in time. The model is forced 372 with observed sea surface temperatures. The Quasi-Biennial Oscillation is nudged to ob-373 served winds, but otherwise the model evolves freely. The model run begins in 1979 and 374 ends in 2014. Because this model run is clearly not in steady state, with at minimum 375 a trend and substantial interannual variability in the sea surface temperatures, we use 376 this to test the steady-state assumption and to calculate the diagnostics described above. 377

The age data used in this paper (Linz, 2017) are a product created from the N_2O 378 observations from the merged satellite data product Global OZone Chemistry And Re-379 lated trace gas Data records for the Stratosphere (GOZCARDS) (Froidevaux et al., 2015). 380 This is a combination of observations from the Microwave Limb Sounder (MLS) (Livesey 381 et al., 2011), the Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) 382 (Fischer et al., 2008), and the Atmospheric Chemistry Experiment Fourier Transform 383 Spectrometer (ACE-FTS, Bernath et al., 2005). MIPAS observations ceased in 2012. Long-384 lived tracers in the stratosphere have compact relationships (Plumb, 2002), and the par-385 ticular relationship between N_2O and age of air was calculated from in situ data from 386 campaigns in the 1990s (A. E. Andrews et al., 2001). This empirical relationship was ap-387 plied to calculate age of air from the GOZCARDS N_2O for Linz et al. (2017), account-388 ing for the trend in tropospheric N_2O (US Environmental Protection Agency, 2016). There 389 are numerous uncertainties associated with this conversion, including but not limited to 390 the potential non-stationarity of the relationship between N_2O and age of air and the 391 expected meridional variation of the relationship (Plumb & Ko, 1992) that was neglected 392 by A. E. Andrews et al. (2001). Evidence for both of these being non-negligible was found 393 recently when B. Birner et al. (2020) updated the relationship between N₂O and age of 394 air with in situ observations of stratospheric air measured by the tropospheric aircraft 395 campaigns of the 2010s (B. Birner et al., 2020). This calculation showed distinct rela-396 tionships in the Northern and Southern Hemisphere and possibly also disagreement with 397 the A. E. Andrews et al. (2001) relationship for older ages in the Northern Hemisphere. 398 The data used by B. Birner et al. (2020) was taken somewhat incidentally during flights 399 that were designed for primarily tropospheric characterization, and so they are limited 400 in sampling locations and times when significant stratospheric intrusions were detected 401 in the troposphere based on low water vapor and high ozone concentrations. These tended 402 to be quite high latitude, making the Northern Hemisphere comparison with A. E. An-403 drews et al. (2001) somewhat inappropriate. We proceed with the GOZCARDS N₂O-404 age calculated with the relationship from A. E. Andrews et al. (2001), but we empha-405 size that the results from this calculation are not going to have a clearly defined error 406 estimate. 407

To compare the mean state of these three products, consider Figure 2. This shows 408 the zonal mean, time-mean age distribution for the N_2O -age and both models, and the 409 streamfunctions for the models as well. Age is lowest in the tropics, where air is upwelling, 410 and it is oldest at the poles, especially in the Southern Hemisphere. This hemispheric 411 asymmetry at the poles is more pronounced in the realistic model than in the idealized 412 model. The idealized model has significantly older ages and a weaker streamfunction than 413 the comprehensive model. Note that for the idealized model, the air at 400 K is already 414 0.5 years old because of the weak tropospheric circulation and the reference of age to the 415 700 hPa level. The comprehensive model is also younger than the N_2O -age by about a 416 vear. The shape of the isopleths beneath 550 K is quite similar, and above that level, 417 the N_2O -age has shallower slopes from the tropics to the midlatitudes. This will be dis-418 cussed again in Section 5. 419

4 Applying the theory in an idealized and a realistic model

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420

4.1 Time Dependence

The steady-state assumption means that this theory is not applicable to high fre-422 quency variability, and so we investigate the timescale over which averaging must be per-423 formed for the theory to be useful. We test to see how well the steady-state age differ-424 ence theory in equation (1) holds in these two models with different lengths of averag-425 ing. An example of such a comparison is shown in Figure 3, where the ratio of the mass 426 above each isentropic surface to the mass flux through that surface is plotted against the 427 mass-flux-weighted age of air difference between downwelling and upwelling air through 428 each isentropic surface. Averages using one year are shown in the empty circles, and av-429 erages over five years are shown in the stars. Note that the averaging itself is performed 430 after the division. The points are colored according to the isentropic level, with the navy 431 points in the lower stratosphere and yellow points in the upper stratosphere. The one-432 to-one line predicted by (1) is shown in the dashed black line. For the idealized model 433 (left panel), one year averages cluster together relatively closely, but the five year aver-434 ages show a reduced spread. For the comprehensive WACCM model (right panel), the 435 one year averages show dramatically more spread than the variability captured by the 436 idealized model suggesting a more important role for the time-dependent terms, but the 437 variability between five year averages is quite small. Calculations of the magnitude of 438 the time-dependent terms show that with this averaging length, they are negligible (not 439 shown, see Linz et al. 2016 for details of time dependent terms). At the lower levels, the 440 points fall above the one-to-one line predicted by the theory, which is consistent with stronger 441 diabatic diffusion in the lowermost stratosphere (Sparling et al., 1997). In both models, 442 there is a local maximum in the age difference at around 500-550 K, which indicates a 443 relative minimum in the velocities. In the upper levels, the points fall on the line. At the 444 uppermost levels the points fall slightly below the line, which is unexplained (and phys-445 ically inconsistent). This discrepancy can be amplified with a different choice of time-446 averaging (i.e. by averaging in time before performing the division). This small effect 447 could be an indication of imperfections associated with performing the calculations on 448 isentropic levels after interpolation as opposed to performing the calculations on model 449 levels and then interpolating to isentropes. It could also be the result of unrealistic nu-450 merical diffusion (c.f. Gupta et al., 2020). 451

452

4.2 Separating hemispheres

As discussed in the introduction, the circulation in the Southern Hemisphere is expected to evolve in time differently from that in the Northern Hemisphere.

When we separate the two hemispheres according to the theory in Section 2.2, we assume that the exchange of tropical air across the equator associated with the seasonal cycle and other time variation has negligible impact on the total age budget for each hemi-



Figure 3. Scatter plots of the ratio of mass above each isentropic surface to the mass flux through the isentropic surface against the difference in mass-flux-weighted age of downwelling and upwelling air through that surface for a) the idealized model and b) the WACCM model. One year averages are shown in the empty circles and five year averages are shown in the stars. The relationship predicted by the theory of Linz et al. (2016) is shown in the black dashed one-to-one line. Different colors show different isentropic levels in K.

sphere, allowing the hemispheres to be treated as two independent systems. To see whether 458 this assumption is reasonable, we can once more test the validity of (1) and see whether 459 this separation of the two hemispheres has made the agreement with the theory worse. 460 If, for example, the Southern Hemisphere tropical air were younger and mixed substan-461 tially into the Northern Hemisphere, then age difference in the Northern Hemisphere would 462 be larger than predicted by the theory, and points for the Northern Hemisphere would 463 tend to fall below the one-to-one theory line. Figure 4 is the same type of scatter plot 464 as in Figure 3 but now averaged over the entire time period and showing different hemi-465 spheres in the different symbols. In the idealized model (left panel), the Southern Hemi-466 sphere (diamonds) has a substantially reduced age difference than the global mean age 467 difference (stars), but the ratio of the mass to the mass flux does not decrease accord-468 ingly. Meanwhile, the agreement with theory from the Northern Hemisphere (squares) 469 is better than the global agreement. The implication is that in the lower stratosphere, 470 there is some exchange of air that is not of the same age, increasing the Northern Hemi-471 sphere age difference and decreasing the Southern Hemisphere age difference. Above about 472 800 K, the two hemispheres agree as well with the theory as the global average. For the 473 WACCM model (right panel), the Northern and Southern Hemispheres both agree as 474 well with the theory as the global up to about 500 K, at which point the Northern Hemi-475 sphere agreement breaks down. Although both models have problematic regions, we pro-476 ceed to calculate the mixing diagnostics as an example. 477

With the caveat that there are regions where the hemispheric independence breaks down, we can still examine the separation between the hemispheres and the overall mixing rates. The mixing rates into and out of the tropics for the two models and their separate hemispheres are shown in Figure 5. The WACCM model separation is mostly reliable below 500 K, and in this region, we see that mixing into the tropics peaks on a higher isentropic level in the the Southern Hemisphere than in the Northern Hemisphere. The



Figure 4. As in Figure 3, except now averaged over the entire period (as specified in Section 3. Global means are shown in the stars, and the Northern Hemisphere and Southern Hemisphere, separated according to the theory in Section 2.2, are shown in squares and diamonds, respectively. Colors again show the isentropic levels. The one-to-one line of the theory is the dashed line.

mixing out of the tropics in the Northern Hemisphere peaks at the same level as the mixing into the tropics, but this mixing is much stronger than in the Southern Hemisphere.
This asymmetry may be due to the monsoonal circulation (Vogel et al., 2019). In the
idealized model, we expect Northern Hemisphere mixing to be larger than Southern Hemisphere mixing, as there is no zonally asymmetric forcing applied in the Southern Hemisphere. Where the results can be relied on, i.e. above about 700K, this is certainly the
case.

For the global average mixing rates, we see that almost no air is mixed into the trop-491 ics above 600 K in either model. Mixing into the extratropics has a local minimum for 492 both models at 600 K, which is above the local minimum in the relative diabatic veloc-493 ities at 500-550 K (this minimum can be seen as the maximum value of the age differ-494 ence in Figure 3). If wave breaking is driving both the adiabatic mixing at a given level 495 and the diabatic circulation at that level and below, this distribution of mixing is con-496 sistent. For both models, there is some mixing into the extratropics above about 800K, 497 implying an increase in wave breaking there. Note in this plot that the mixing into the 498 tropics for the WACCM model hovers just below zero above 700K and around 380K. This 499 is not an issue with the mechanics of the calculation, but instead implies that the assump-500 tions about the uniformity of the age of air within the upwelling and downwelling regions 501 is (unsurprisingly) flawed. Such weakly negative mixing flux above 600 K were also ob-502 tained by Gupta et al. (submitted) who used the isentropic framework proposed in this 503 study to estimate the mixing flux into the tropics in idealized models, but for a perpet-504 ual winter solstice climatology. Strong horizontal gradients of age in the upwelling and 505 downwelling region in their models led to an overestimation of the mixed age difference 506 $\Delta\Gamma$ resulting in underestimation of mixing fluxes. Additional examination to quantify 507 this bias is warranted in future work. The global results are qualitatively similar to the 508 global results from Ray et al. (2016) for the Canadian Middle Atmosphere Model, although 509



Figure 5. Mixing rate into (μ_{in}, a) and out of (μ_{out}, b) the tropics for the idealized model (green) and the WACCM model (purple) versus potential temperature. Global averages are in the solid lines, while the Northern Hemisphere averages are in the dash-dot lines and the Southern Hemisphere averages are in the dotted lines.

quantitative comparisons are difficult because of the different coordinate system and assumptions in that study.

$_{512}$ 5 Comparison with N₂O-age

One of the most potentially powerful applications of this theory is the ability to 513 use observations to compare more directly to models—to compare like-to-like with sim-514 ple, global metrics. Although there are numerous caveats about the current observational 515 global age of air products that are available and about the age of air from N_2O in par-516 ticular, we nevertheless think it is a valuable demonstration to apply the theory to a satel-517 lite record. We are demonstrating the method, but we will not calculate the error bars, 518 as we currently cannot determine what should even be included in such a calculation. 519 An incomplete list includes: the bias introduced by using area-weighting instead of mass 520 flux weighting, uncertainty due to reanalysis choice for calculating pressure levels and 521 pressure-to-isentrope conversion, uncertainty in the calculation of the CO_2 lag time, un-522 certainty in the relationship between N₂O and CO₂ lag time (in particular, the use of 523 a relationship from data that is over a decade older than the satellite record's beginning 524 date), the use of a relationship that has been defined primarily by Northern Hemisphere 525 midlatitude in situ data to characterize global age of air (A. E. Andrews et al., 2001) (even 526 though the tropical and extratropical relationships should differ, e.g. Plumb 2007), un-527 certainty in vertical gradients introduced by satellite weighting functions, and uncertainty 528 due to the non-uniformity of age within the tropics and within the extratropics. As such, 529 these calculations should be taken as only a first guess. 530

Because of the limited extent of the relationship between N_2O and CO_2 lag time, the vertical extent of age coverage is much greater in the tropics than in the extratropics (see Figure 2). We therefore calculate the vertical age gradient in the tropics, and this is a more reliable metric than the other global metrics. It is not, however, a complete characterization of the mixing (c.f. Eq. 13), since the total overturning strength and horizontal age gradients are also important. In Figure 6 we find remarkable agree-



Figure 6. The vertical gradient of the mean upwelling age of air (mass flux weighted for models, area-weighted for N_2O -age) for the ideal model (green), WACCM model (purple), and for the N_2O -age (black). The only levels for which the data record is complete are shown in the thick black line, while the dash-dot black line shows the mean vertical age gradient while ignoring the data gaps. There are far fewer gaps in the tropics than in the extratropics, so this is more reliable than the age difference shown later.

ment in the vertical age difference in the tropics between WACCM and the N_2O -age where 537 the full data exists, and the idealized model also agrees reasonably well between 480 and 538 500 K. Higher up, the vertical age gradient is larger in the idealized model than in the 539 WACCM model. All three profiles show a peak in the lower stratosphere (lower in the 540 idealized model than in WACCM and the N_2O -age) associated with a peak in the mix-541 ing into the tropics at that level. Agreement in the vertical gradient of age in the trop-542 ics only implies agreement in mixing if there is also agreement in the overturning, but 543 the quantitative similarity between the vertical age gradient in the tropics between WACCM 544 model and the N_2O -age is remarkable. 545

Finally, we look at the two primary summary statistics: the overturning circula-546 tion strength and the mixing efficiency, ϵ . These require the full global data coverage, 547 and so we calculate these wherever we have any data, even if the temporal coverage is 548 incomplete. The levels where we have global observational age data for the entire length 549 of the record are shown in the thick, solid black lines in Figure 7. The comparison of the 550 total overturning, based on the horizontal age gradient, is shown in Figure 7a, and the 551 idealized model is shown to have significantly weaker circulation. The WACCM model 552 agrees fairly closely with the N_2O -age calculation. The mixing efficiency is shown in Fig-553 ure 7b, and here too there is agreement between the WACCM model and the N_2O -age 554 calculation, where full satellite data exists. Higher up, the mixing efficiency implied by 555 the N_2O is much greater than that in both of the models, but we caution that the ex-556 tratropical data is very limited there. The idealized model has a lower mixing efficiency, 557 consistent with what we saw previously in Figure 4. This global model-to-model com-558 parison is also a particularly useful application of this theory, as these are well defined 559 metrics describing the global stratospheric circulation. 560



Figure 7. Summary statistics for both models and for the N2O-age product. Mixing rate into and out of the tropics for the two hemispheres and the global average for WACCM.

⁵⁶¹ 6 Discussion and Conclusions

We have derived a method to calculate a diagnostic for the mixing rate between 562 the tropics and extratropics from the spatial gradients of age of air, in steady state and 563 assuming diabatic diffusion is small. By formulating the theory based on the TLP frame-564 work of Neu & Plumb (1999) on isentropic levels, we allow for both the diabatic veloc-565 ities and the mixing efficiency to vary in the vertical. The vertical gradient of age in the 566 extratropics informs the mean detrainment rate out of the tropics, and the vertical gra-567 dient of age of air in the tropics informs the mean entrainment rate into the tropics. Tak-568 ing advantage of the theory of Linz et al. (2016), we can use the quasi-horizontal differ-569 ence of downwelling and upwelling age of air to calculate the diabatic circulation strength. 570 With observations of age, temperature and pressure, we can calculate both a tropical en-571 trainment and detrainment mass flux. Stratospheric age of air alone is sufficient to quan-572 titatively determine the circulation as defined by these global or hemispheric averages 573 in steady-state. We note that unlike the theory of Linz et al. (2016), the mixing met-574 ric is a diagnostic tool that reflects the assumptions we have made about the system (for 575 example, that the average age that mixes from the extratropics into the tropics is the 576 mass-flux-weighted mean age of downwelling air). However, these assumptions are nec-577 essary to develop the theory to relate age of air observations to the adiabatic mixing, and 578 we believe this will prove to be useful to compare model runs with an age tracer to strato-579 spheric age observations. 580

This method is limited because of the steady-state assumption. Linz et al. (2016) 581 showed that in an idealized model, annual averages were generally sufficient for the steady-582 state assumption to hold for the relationship between the diabatic circulation strength 583 and the age difference between downwelling and upwelling air. Linz et al. (2017) used 584 five year averages of two data products to calculate the mean circulation strength, and 585 implicitly demonstrate that these five-year averages are good enough using a realistic model. 586 Here, we more systematically examine that treatment and find that a five-year average 587 is indeed sufficient. Because mixing timescales tend to be shorter than the diabatic cir-588 culation timescales, it seems likely that the minimum period of averaging for the steady-589 state assumption to apply would be limited by the diabatic component. However, this 590

is not straightforward to test—a comparison to the more traditional effective diffusivity analysis in a realistic model would be a first step. The steady-state assumption also
necessarily makes this theory inappropriate for examining short term changes to the circulation. Instead, it is more appropriate for characterizing and comparing model mean
adiabatic mixing to the mean adiabatic mixing of the true atmosphere and the decadal
variations in these.

Many stratospheric processes, such as ozone depletion and recovery, affect the hemi-597 spheres asymmetrically, and so the global-average picture is useful, but incomplete. We 598 derived the relationships for the hemispheres separately; however, to do so, we assumed that the two hemispheres act as independent closed systems, which is not reasonable. 600 This is only true if the air that is exchanged across the equator is of approximately the 601 same age, and so the assumption introduces errors. For quantitative use, the errors in-602 troduced would need further examination, and the exchange could be included in the bud-603 get explicitly in a slightly more complex formulation of the theory. In the WACCM model 604 the assumption of hemispheric independence appears to be reasonable up to about 500 605 K, and there is more mixing in the Northern Hemisphere than the Southern Hemisphere. In the idealized run the assumption holds for the middle to upper stratosphere, and al-607 though mixing is weak, the Northern hemisphere has more mixing than the Southern hemi-608 sphere, consistent with the stronger forcing. These mixing rates were consistent with what 609 could be expected based on the different forcing in the Northern and Southern Hemi-610 spheres, and so we conclude that this approach might be viable, though it would be more 611 useful with an explicit treatment of interhemispheric transport. Globally we find a rel-612 ative minimum in mixing around 600 K and complete isolation of the tropics above this 613 level. 614

This theory holds potential to enable calculations of the mean adiabatic mixing of 615 the real stratosphere from age of air observations. We have performed an example cal-616 culation using N_2O satellite observations combined with in situ observations. We dis-617 cussed many limitations in section 5, but we highlight a few here: the uncertainty in the 618 determination of age from N_2O for numerous reasons, the vertical resolution and sam-619 pling pattern of the satellite, and the effect of area-weighting rather than mass-flux weight-620 ing. Before we have reliable mixing estimates from satellites, these uncertainties and oth-621 ers must be addressed. However, this is a promising first step, and the comprehensive 622 WACCM model agrees remarkably well with the mixing estimates from the N_2O -age in 623 the regions where data coverage is substantial. The quantification of the stratospheric 624 circulation from observations in a way that enables meaningful comparisons with mod-625 els is an important topic of study, and this theory provides a significant step forward to-626 wards that goal. 627

628 Appendix A

For the derivation of the Southern Hemisphere extratropical mixing rate, start again with the ideal age equation (Waugh & Hall, 2002):

$$\frac{\partial \Gamma}{\partial t} + \mathcal{L}(\Gamma) = 1. \tag{1}$$

As before, we assume that diabatic diffusion is negligible and make the assumption of steady-state flow. Then we integrate this equation over the volume above the Southern Hemisphere downwelling region on an isentrope:

$$\int_{\mathcal{S}_{down}} \mathbf{n} \cdot \mathbf{F}^{\Gamma} dA - \int \oint \sigma V_{in} \Gamma dl d\theta + \int \oint \sigma V_{out} \Gamma dl d\theta = \int_{\mathcal{S}_{\mathcal{V}_{down}}} \sigma dA d\theta.$$
(2)

⁶³⁴ dl is now only over the one surface that divides the Southern extratropics from the trop-⁶³⁵ ics, the Southern $\dot{\theta} = 0$ line. Then take the vertical derivative in entropy to obtain

$$\frac{\partial}{\partial \theta} \int_{\mathcal{S}_{down}} \sigma \dot{\theta} \Gamma dA - \oint \sigma V_{in} \Gamma dl + \oint \sigma V_{out} \Gamma dl = \int_{\mathcal{S}_{\mathcal{V}_{down}}} \sigma dA.$$
(3)

c.f. (7). The air coming into the extratropics is assumed to have the mass-flux-weighted average age of the tropical region (Γ_{u_S}), and likewise the air leaving the extratropics has the mass-flux-weighted average age of the Southern extratropical region (Γ_{d_S}). Define the entrainment and detrainment mass fluxes μ_{in_S} and μ_{out_S} :

$$\mu_{ins} = \oint \sigma V_{in} dl, \tag{4}$$

640 and

$$\mu_{out_{\mathcal{S}}} = \oint \sigma V_{out} dl, \tag{5}$$

⁶⁴¹ recalling that the line integral is now only across the Southern Hemisphere surface be-⁶⁴² tween the tropics and extratropics. Then rewrite the integral of the density as $\Sigma_{d_S} = \int_{S_{down}} \sigma dA$. With these notation changes and simplifications, we can rewrite (3) as:

$$\frac{\partial}{\partial \theta} \int_{\mathcal{S}_{up}} \sigma \dot{\theta} \Gamma dA - \mu_{out_{\mathcal{S}}} \Gamma_{u_{\mathcal{S}}} + \mu_{in_{\mathcal{S}}} \Gamma_{d_{\mathcal{S}}} = \Sigma_{d_{\mathcal{S}}}.$$
 (6)

As globally, the change in the Southern Hemisphere diabatic circulation with entropy is due to the difference between the entrainment and detrainment mass fluxes:

$$\frac{\partial \mathcal{M}_{\mathcal{S}}}{\partial \theta} = \mu_{ins} - \mu_{outs} = \frac{\partial}{\partial \theta} \int_{\mathcal{S}_{up}} \sigma \dot{\theta} dA = -\frac{\partial}{\partial \theta} \int_{\mathcal{S}_{down}} \sigma \dot{\theta}.$$
 (7)

⁶⁴⁶ We rewrite (6) in terms of $\mathcal{M}_{\mathcal{S}}$ and $\Gamma_{d_{\mathcal{S}}}$:

$$-\frac{\partial}{\partial\theta}\mathcal{M}_{\mathcal{S}}\Gamma_{d_{\mathcal{S}}} - \mu_{out_{\mathcal{S}}}\Gamma_{u_{\mathcal{S}}} + \mu_{in_{\mathcal{S}}}\Gamma_{d_{\mathcal{S}}} = \Sigma_{d_{\mathcal{S}}},\tag{8}$$

647 Appendix B

⁶⁴⁸ Diabatic heating in the idealized model is provided through Newtonian relaxation ⁶⁴⁹ of the model atmosphere temperature towards an analytical equilibrium temperature pro-⁶⁵⁰ file T_{eq} . The equilibrium temperature profile in the Polvani-Kushner stratosphere is com-⁶⁵¹ puted using the U.S. 1976 Standard Atmosphere profile (from rocketsondes and satel-⁶⁵² lite data). This profile records the vertical variation of atmospheric temperature and pres-⁶⁵³ sure at eight different atmospheric heights between the surface and 71 km. The tropopause ⁶⁵⁴ height in the idealized model is adjusted by modifying T_{eq} in the upper troposphere lower ⁶⁵⁵ stratosphere (UTLS) region by adjusting the U.S. 1976 Standard Atmosphere profile.

The profile is piecewise linear i.e., the temperature is assumed to vary linearly between each of the eight points with a fixed lapse rate in the region. For the first two levels near the surface, the temperature steadily decreases at a lapse rate of -6.5 K/km, decreasing from 288.15 K to 216.65 K between 1000 hPa and 223.36 hPa respectively. In the UTLS, the levels 223.36 hPa and 54 hPa are isothermal with a temperature of 216.65 K. In the middle stratosphere, between 54 hPa and 8.5 hPa, the temperature increases again at a constant rate from 216.65 K to 228.6 K respectively.

The tropopause height in the idealized model employed in the study is raised by lowering the equilibrium temperature in the UTLS from its default value of 216.65 K to a new forcing temperature of 200 K. The static stability (lapse rate) between 1000 hPa and 223.36 hPa and between 223.36 hPa and 54 hPa is kept unchanged at -6.5 K/km and 0 K/km respectively. As a result, the 200 K forcing temperature is associated with ⁶⁶⁸ a pressure height of roughly 150 hPa and, therefore, the isothermal UTLS region is now ⁶⁶⁹ relaxed towards an equilibrium temperature of 200 K instead of 216.5 K. Any forcing ⁶⁷⁰ temperature less than 216.65 K raises the tropopause height; and the forcing temper-⁶⁷¹ ature of 200 K raises the climatological tropical tropopause in the model roughly from ⁶⁷² 200 hPa (~ 12 km) to 140 hPa (~ 14 km).

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- of this article. The authors have consulted with the JGR-Atmospheres editorial staff and
- ⁶⁹⁰ Editor-in-Chief about these circumstances prior to submission.

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