

The spacecraft wake as a tool to detect cold ions: Turning a problem into a feature

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Abstract

Wakes behind spacecraft caused by supersonic drifting positive ions are common in plasmas and disturb in situ measurements. We concentrate on observations of the electric field with double-probe instruments. When the equivalent spacecraft charging is small compared to the ion drift energy the wake effects are caused by the spacecraft body and can be compensated for. We discuss examples from the Cluster spacecraft in the solar wind, including statistics of the direction, width and electrostatic potential of wakes, and compare with an analytical model. When the equivalent positive spacecraft charging is large compared to the ion drift energy, an enhanced wake forms. In this case observations of the geophysical electric field with the double-probe technique becomes extremely challenging. Rather, the wake can be used to estimate the flux of cold (eV) positive ions. We discuss such examples from the Cluster spacecraft in the low-density magnetospheric lobes. For an intermediate range of parameters, when the equivalent charging of the spacecraft is similar to the drift energy of the ions, also the charged wire booms of a double-probe instrument must be taken into account. We discuss an example of these effects from the MMS spacecraft near the magnetopause. We find that the observed wake characteristics provide information which can be used for scientific studies. An important example is the enhanced wakes used to estimate the outflow of ionospheric origin in the magnetospheric lobes to about 10^{26} cold (eV) ions/s, constituting a large fraction of the mass outflow from planet Earth.

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6 **Key Points:**

- 7 • Plasma wakes are common behind scientific spacecraft
8 • Wakes in the solar wind can be compensated for in data analysis
9 • Enhanced wakes in the polar lobes can be used to detect cold outflowing ions

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Abstract

Wakes behind spacecraft caused by supersonic drifting positive ions are common in collisionless plasmas and disturb in situ measurements. We concentrate on observations of the electric field with double-probe instruments. When the equivalent spacecraft charging is small compared to the ion drift energy the wake effects are caused by the spacecraft body and can be compensated for in a reasonable way. We discuss examples from the Cluster spacecraft in the solar wind, including statistics of the direction, width and electrostatic potential of wakes, and compare with an analytical model. When the equivalent positive spacecraft charging is large compared to the ion drift energy, an enhanced wake forms. In this case observations of the geophysical electric field with the double-probe technique becomes extremely challenging. Rather, the wake can be used to estimate the flux of cold (eV) positive ions. We discuss such examples from the Cluster spacecraft in the low-density magnetospheric lobes. For an intermediate range of parameters, when the equivalent charging of the spacecraft is similar to the drift energy of the ions, also the charged wire booms of a double-probe instrument must be taken into account. We discuss an example of these effects from the MMS spacecraft near the magnetopause. Overall we find that the observed wake characteristics provide information which can be used for scientific studies. An important example is the enhanced wakes used to estimate the outflow of ionospheric origin in the magnetospheric lobes to about 10^{26} cold (eV) ions/s, constituting a large fraction of the mass outflow from planet Earth.

Plain Language Summary

Wakes caused by spacecraft motion or drifting plasma are common behind spacecraft with scientific instruments and disturb in situ observations of space plasmas. In the solar wind, the wake behind a Cluster spacecraft is caused by the spacecraft body, is narrow, and can partly be compensated for when analysing data. In the regions above the Earth's polar regions, the wake behind a Cluster spacecraft is caused by an electrostatic structure around the positively charged spacecraft, causing an enhanced wake. The charging stops positive ions from reaching the spacecraft. Rather, this wake can be used to estimate the flux of cold (eV) positive ions escaping from the ionosphere. Above the poles the flux is about 10^{26} ions/s, constituting a large fraction of the mass outflow from planet Earth. For an intermediate range of parameters, when the drift energy of the ions is comparable to the equivalent charge of the spacecraft, also the charged wire booms of a double-probe instrument must be taken into account to extract useful information from the observations. We discuss such examples from the MMS spacecraft near the magnetopause.

1 Introduction

Wakes behind obstacles in supersonic flows are common in nature. Here we discuss wakes in collisionless plasmas, in particular behind spacecraft. In situ observations are a powerful tool to observe space plasmas, but includes the problem of the spacecraft disturbing the plasma of interest. We concentrate on observations of electric fields, and in particular on the local electric field around the spacecraft induced by wake formation. In many situations spacecraft wakes are caused by flows which are supersonic with respect to the ion thermal speed, but subsonic with respect to the electron thermal speed. The result is that the wake charges negatively until the potential is sufficiently negative to prohibit further accumulation of electrons, hence causing an enhancement of the local electric field.

We discuss electric field observations obtained with long wire booms in the spin plane of the Cluster and MMS spacecraft. In some cases the wake is due to the spacecraft body itself and the transverse extent is limited. Here effects on electric field observations can routinely be removed and observations of the geophysical electric field are mainly unaffected (Khotyaintsev et al., 2014). We show examples of Cluster observations

in the solar wind (Eriksson et al., 2006, 2007). The direction of the wake gives the direction of solar wind. We show that statistics of the width and electrostatic potential of solar wind wakes are in reasonable agreement with a simple analytical model. In other cases the wake is not due to the spacecraft body but to an extended electrostatic structure around a positively charged spacecraft scattering positive ions. Here the wake is extended and observations of the local electric field are complicated to use for investigations of the geophysical E-field. Rather, the detection of this extended wake can be used to gain information on the cold ions causing the wake. We show examples of Cluster observations in the polar lobes and discuss how this extended wake can be used for statistical studies of the outflow of cold ionospheric ions (Engwall, Eriksson, Cully, André, Torbert, & Vaith, 2009; Engwall, Eriksson, Cully, André, Puhl-Quinn, et al., 2009; André et al., 2015). In some cases of intermediate parameters, with a positively charged spacecraft but ions that can still reach the satellite, the electrostatic structure around a spacecraft can not be approximated by a sphere but the charged long wire booms of an E-field instrument must be considered. We show an example observed close to the magnetopause by MMS (Toledo-Redondo et al., 2019). For comparison, we briefly discuss wakes in the ionosphere where effects of a negatively charged spacecraft and smaller Debye lengths and gyro radii are important. Overall we find that understanding the physics behind the spacecraft wakes, the local effects on electric field observations can sometimes be removed and most of the observations can be used as originally intended. When this is not possible, sometimes entirely new geophysical parameters such as ion flux can be estimated.

2 Wakes in different situations

An object moving in a neutral gas dominated by collisions is either sub- or supersonic. We consider collisionless plasmas. The drift velocity of such a plasma is often larger than the thermal speed of the ions but smaller than the thermal speed of the electrons. Since the drift is supersonic with respect to the ions but subsonic with respect to the electrons, it can be called mesosonic. (We here use the term "supersonic" when comparing ion drift and thermal speeds, since for equal ion and electron temperatures the ion acoustic speed is similar to the ion thermal speed.) A mesosonic drift will cause a negatively charged wake. Hence the presence of a spacecraft in a drifting plasma can cause a local electric field in the vicinity of the spacecraft.

2.1 Charged spacecraft

Spacecraft are usually charged, which affects observations of the local plasma. In Low Earth Orbit in the high density ionosphere, spacecraft are often negatively charged due to the large flux of ionospheric electrons. At higher altitudes in a low density plasma, the photoelectrons emitted by a spacecraft in sunlight can dominate the charging process, causing positive charging. Any deviation from charge neutrality will significantly affect charged particles with an energy similar to the equivalent spacecraft charging. This can in turn influence wake formation and the corresponding local electric field. Spacecraft charging is well known in near-Earth plasmas as discussed below, and also for interplanetary spacecraft such as Rosetta investigating comet 67P (Johansson et al., 2020; Bergman et al., 2020).

2.2 Spacecraft and instruments

The wakes we consider in detail are related to the ESA Cluster (Escoubet et al., 2001) and NASA MMS (Burch et al., 2016) spacecraft, launched 2000 and 2015, respectively. Both are four-spacecraft missions for detailed investigations of space plasma physics. All satellites have long wire booms in the spin plane, used for observations of the electric field (Pedersen et al., 1998; Maynard, 1998). The Cluster Electric Field and Wave (EFW) instrument includes two pairs of probes on wire booms on each satellite. Each

109 pair has a probe-to-probe separation of 88 m, and the electric field is obtained from the
 110 potential difference between the probes (Gustafsson et al., 1997, 2001). The satellites
 111 have a diameter and height of 2.9 and 1.3 m, respectively. The spherical probes have a
 112 diameter of 8 cm and the cylindrical pre-amplifiers located 1.5 m closer to the satellite
 113 have the same diameter. To avoid shadow on the probes from the pre-amplifiers, the short
 114 stiff booms carrying magnetometers, and from the spacecraft body, the spin plane was
 115 initially inclined a few degrees with respect to the ecliptic plane. Figures 1a,b show one
 116 Cluster satellite in different phases of the ~ 4 -second spin. The MMS spacecraft have a
 117 similar diameter, a spin period of ~ 20 s, and the Spin-plane Double Probe instrument
 118 (SDP) has a probe-to-probe separation of 120 m (Lindqvist et al., 2016). The MMS satel-
 119 lites also have an Axial Double Probe instrument with cylindrical sensors separated by
 120 32 m along the spin axis (Ergun et al., 2016).

121 Both the Cluster and the MMS spacecraft have additional instruments for obser-
 122 vations of quasi-static electric fields, based on a completely different technique. The Elec-
 123 tron Drift Instruments (EDI) on Cluster (Paschmann et al., 1997, 2001) and MMS (Torbert
 124 et al., 2016) measure the drift of artificially emitted high-energy (0.25–1 keV) electrons
 125 as they gyrate back to the spacecraft under the influence of the geophysical magnetic
 126 field (Paschmann et al., 1998). These electrons can have gyro radii of several kilometers
 127 and are not significantly affected by the local wake. The EDI instruments are therefore
 128 not sensitive to spacecraft-plasma interactions but are limited to reasonably steady and
 129 strong magnetic fields ($\gtrsim 30$ nT) and quasi-static electric field ($\lesssim 10$ Hz), while double-
 130 probe instruments can be used up to MHz frequencies and have additional data prod-
 131 ucts such as spacecraft potential, which can be used for density estimates (Eriksson et
 132 al., 2006; Pedersen et al., 2008). In addition, both Cluster and MMS have instruments
 133 for Active Spacecraft Potential Control (ASPOC), reducing positive potential by emit-
 134 ting positive ions (Torkar et al., 2001, 2016).

135 **2.3 Narrow and enhanced wakes**

136 Cases of practical importance include spacecraft in the solar wind when the nar-
 137 row wake is caused by the spacecraft body, and spacecraft in the polar lobes when the
 138 wake is caused by an electrostatic structure around a positively charged spacecraft scat-
 139 tering positive ions. These two examples are illustrated in Fig. 1c, d. For simplicity, in
 140 this figure we consider the plasma flow to be in the spin plane of the spacecraft. The nar-
 141 row wake in Fig. 1c will not affect the electric field observations in the spin phase illus-
 142 trated in Fig. 1a when both probe pairs are at a large angle to the flow, but will severely
 143 affect observations in the phase shown in Fig. 1b when one of the probe pairs (3-4) is
 144 aligned with the flow. The enhanced wake (Fig. 1d) will affect the observations for most
 145 directions of the wire booms.

146 **2.4 Wakes in low Earth orbit**

147 The basic theory of spacecraft wakes was understood early in the space age (Alpert
 148 et al., 1965; Gurevich et al., 1969) and during the first decades a substantial amount of
 149 observations in LEO accumulated (Hastings, 1995). Many early wake studies concentrated
 150 on these low altitudes since several satellites, including most manned spacecraft, oper-
 151 ate in the ionosphere. At low altitudes in the high density ionosphere a spacecraft typ-
 152 ically has negative charge due to the high electron flux, causing the ions to fill the wake
 153 more effectively (Fig. 1e). An orbiting satellite is moving at 7-8 km/s in a rather dense
 154 plasma and strong magnetic field, the Debye length and electron gyro radius are typ-
 155 ically smaller than the satellite dimensions, while the ion gyro radius can be compar-
 156 able to the spacecraft dimensions (see Table 1 for examples of parameters). This is in con-
 157 trast to the regions at higher altitudes we consider below where Debye lengths and gyro
 158 radii are larger than the spacecraft dimensions. The small Debye length in LEO gives
 159 large wake potentials, which further concentrated early studies to low altitudes. Recent

160 simulations of wakes and related effects include the geomagnetic field for orbiting space-
 161 craft in LEO such as Freja (Miyake et al., 2020), and also for slower sounding rockets
 162 (Darian et al., 2017), and their booms of a few meters (Paulsson et al., 2018; Paulsson
 163 et al., 2019). Wakes in LEO can also be of practical interest for close-proximity forma-
 164 tion flying (Maxwell et al., 2021).

165 2.5 Wakes behind natural objects

166 We concentrate on wakes behind artificial conducting spacecraft and understand-
 167 ing of their effects. This understanding is valuable for interpretation of in situ observa-
 168 tions. Overall understanding of wakes is also important for investigations of natural ob-
 169 jects not further discussed here. This includes small objects such as charged dust (Miloch
 170 et al., 2017; Darian et al., 2019). This also includes large objects such as the Moon, see
 171 Rasca et al. (2021) and references therein. As another example, investigations of solar
 172 wind interactions, including wake formation, with a metal-rich asteroid such as 16 Psy-
 173 che can be used to understand the present electromagnetic environment and compare
 174 scenarios for formation and solidification (Fatemi & Poppe, 2018).

175 3 Spacecraft wakes in different space plasma

176 Polar orbiting spacecraft, such as Cluster, can investigate both the solar wind and
 177 the polar lobes. In both cases the density is much lower than in the ionosphere. It was
 178 early realized that a spacecraft in a low density plasma generally will be positively charged
 179 since satellite photo-emission dominates the influx of electrons from the surrounding plasma
 180 (Whipple, 1965). However, there are only a few early investigations relevant for wakes
 181 behind positive spacecraft potentials, as summarized by Engwall, Eriksson, and Forest
 182 (2006) and Eriksson et al. (2007). Observations of wakes behind positively charged space-
 183 craft are discussed below. Some relevant simulations of spacecraft wakes and the effects
 184 on double probe observations are given by Engwall, Eriksson, and Forest (2006), Miyake
 185 et al. (2013) and Miyake and Usui (2016).

186 3.1 Wake in the solar wind (narrow wake)

187 As the solar wind ion flow is supersonic, a wake will form behind a spacecraft in
 188 this medium. Because of photoelectron emission, the spacecraft is typically charged to
 189 a few volts positive. The ion flow energy $mv_i^2/2$ is usually much larger than the spacecraft-
 190 to-plasma potential eV_{SC} (spacecraft charging) and is also larger than the ion thermal
 191 energy KT_i (and the often similar electron thermal energy KT_e), see Table 1 for exam-
 192 ples of parameters:

$$193 \quad mv_i^2/2 \gg eV_{SC}, \quad mv_i^2/2 > KT_i \sim KT_e. \quad (1)$$

194 This supersonic ion drift gives a narrow transverse width of the wake, whose cross-
 195 section immediately behind the spacecraft has the size and shape of the spacecraft body,
 196 see Fig. 1c. For typical solar wind speeds and electron temperatures the solar wind is
 197 subsonic with respect to the electrons, which therefore can enter the wake. The wake be-
 comes negatively charged.

198 The effect on a double probe electric field observation is clear, repetitive at the rate
 199 related to the satellite spin period, and easy to identify. Figure 2 shows an example of
 200 wake effects on electric field observations by the Cluster1 EFW probe pair 1-2 in the so-
 201 lar wind. The spikes in the observed electric field (blue) are seen every 2 seconds, or twice
 202 per spin period (4 s). This corresponds to each of the probes 1 and 2 encountering the
 203 the wake once per spin.

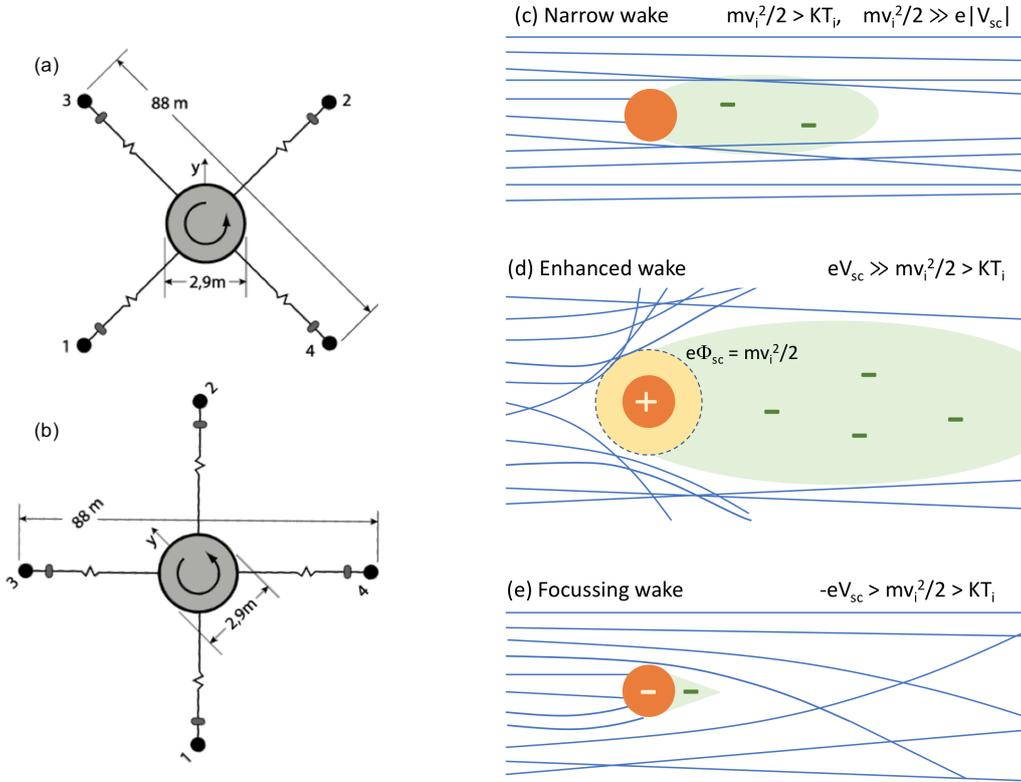


Figure 1. Left panel, (a) and (b): Sketch of the Electric Field and Wave instrument on Cluster, using probes on long wire booms, in two different phases of the 4 second satellite spin. Right panel: Some wake cases. Positive ion trajectories are shown in blue, motion is from left to right. The spacecraft is indicated in orange, the green shaded regions indicate negative space charge. (c) When the ion energies are large compared to the equivalent charge of the spacecraft and in the wake, the wake transverse size close to the spacecraft is set by the spacecraft dimensions and the length depends on the ratio of ion flow to thermal speed (e.g. Cluster in the solar wind) (d) For a very positive spacecraft, the ions undergo Rutherford scattering on the potential Φ_{sc} from the spacecraft, creating an enhanced wake. The dashed circle indicates the equipotential of the spacecraft electrostatic field where $e\Phi_{sc} = mv_i^2/2$ around which ions will scatter (e.g. Cluster in the polar lobes). (e) For the commonly studied ionospheric case, the focussing effect of a negative spacecraft fills in the wake more effectively than in case (c). For all examples the particles are assumed to be unmagnetized which is often a good approximation for wake studies in the solar wind and polar lobes, but not always in the ionosphere. For some parameters also the charging of long wire booms are important for the ion trajectories, see Fig. 7

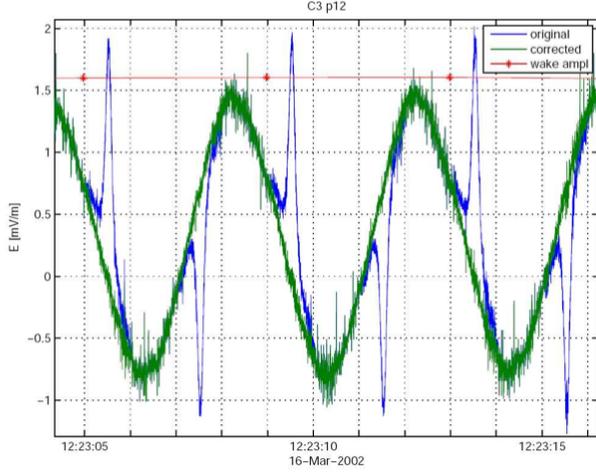


Figure 2. Solar wind wake signature observed by one probe pair (1-2) of the EFW instrument on one Cluster spacecraft (C3). The blue curve is the original raw data sampled at 450 Hz, while the green curve shows the data after wake removal (see text). The red stars, bounded together with by the red line, shows the wake amplitude determined in the removal process, once for each 4 s spacecraft spin. In the case of a narrow wake, the wake signatures can be compensated for. From Eriksson et al. (2007).

204 We have developed an algorithm for the EFW instrument to detect and remove the
 205 local wake electric field from the data (Eriksson et al., 2006; Khotyaintsev et al., 2014).
 206 The process involves taking a weighted average of a few 4-second satellite spins which
 207 will not affect the very repetitive artificial wake signatures much, while natural wave ac-
 208 tivity will mainly be removed. Using these averaged data, the artificial signature is iden-
 209 tified and then subtracted from the original observation using an algorithm in several
 210 steps (Eriksson et al., 2007). The algorithm used to remove the wake from electric field
 211 data to be archived collects three primary characteristics of the wake: direction in the
 212 satellite spin plane (wake spin angle), amplitude and width (quantified as the full width
 213 at half maximum value, FWHM).

214 The main features of the observed wake can be compared to a simple theoretical
 215 model. The ions have a large gyroradius (Table 1) and as further discussed below the
 216 ion trajectories can be well approximated by straight lines on the length-scale of the wire
 217 booms. In this model a solar wind ion distribution with drift energy $mv_i/2$ and thermal
 218 energy KT_i is stopped by the spacecraft body but no other effect of the spacecraft is in-
 219 cluded. Describing the ions by a drifting Maxwellian, the ion density in the wake formed
 220 behind the spacecraft can then be calculated by integrating the distribution function over
 221 all ion energies and all directions of motion except those blocked by the spacecraft.
 222 Writing the ion density in the wake as $n_i = n_0 - \delta n$ and setting the solar wind to flow
 223 in the $+z$ direction, we then have (Alpert et al., 1965)

$$\begin{aligned} \delta n(x, y, z) &= \frac{n_0}{\pi z^2} M^2 \exp\left(-M^2 \frac{x^2 + z^2}{z^2}\right) \\ &\cdot \int_S \exp\left(-M^2 \frac{x_0^2 + z_0^2 - 2xx_0 - 2zz_0}{z^2}\right) dx_0 dy_0 \end{aligned} \quad (2)$$

224 where M is the ion flow Mach number,

$$M = \sqrt{\frac{m_i v_i^2}{2KT_i}}, \quad (3)$$

and S is the spacecraft cross section in the xy plane. Numerical evaluation of this integral can be used to find the density in the wake at the position of the EFW probes. The ions gradually fill the wake due to their random thermal motion. At the same time the wake widens as ions outside the low density region move into the wake. In this model, the ion charge is not important for the ion motion. In the solar wind this is a good approximation. When reaching potentials $\sim -KT_e/e$ (where e is the elementary charge) the density of electrons filling the wake reaches an equilibrium. As $KT_e \sim 10$ eV in the solar wind, this negative potential has quite small impact on the motion of the ions with $mv_i^2/2 \sim 1$ keV.

The quantity measured by EFW is the wake potential Φ_w . The electrons are essentially unmagnetized at the scales of interest (Table 1) and an electron gas in thermal equilibrium is well described by the Boltzmann relation

$$\Phi_w = \frac{KT_e}{e} \ln \frac{n_e}{n_0} \quad (4)$$

By assuming quasi-neutrality, $n_e \approx n_i$ we can find the wake potential by combining equations (2) and (4). This approximation assumes a short the Debye length, and we return below to how well this last assumption can be expected to hold.

Predicted EFW observations of wake width (FWHM) and amplitude (peak magnitude of the observed potential) as the probes cross the wake, as function of the solar wind ion flow Mach number, are given in Fig. 3. For the numerical integration of equation 2, the spacecraft cross section has been described as a rectangle 1x3 m in size and the probe moves across the wake 44 meters away from the centre of the spacecraft. Three different angles of the solar wind flow direction to the satellite spin plane (wake elevation angle) have been considered in Fig. 3. Until May 2014 the Cluster satellite spin axes were actively kept at a tilt with respect to the direction to the Sun (the Solar Aspect Angle, SAA) of typically $95^\circ \pm 1^\circ$. For a solar wind flowing in the ecliptic plane, this would correspond to a wake elevation angle of 5° in Fig. 3. This angle of course varies due to variations of the solar wind direction. Deviations in the solar wind direction from the average are often within 2-3°, e.g. Tsyganenko and Fairfield (2004), so in Fig. 3 wake elevation angles of 3-7° should be most relevant.

We note that after May 2014, the SAA remains closer to 90° since the tilt angle is not actively controlled. This lowers spacecraft fuel consumption but interferes with high resolution EFW observations due to shadow on each probe during a short period each spin. For quasi-static (spin resolution) electric field data this can be compensated for in a similar way as for a narrow wake. To keep the wake analysis as simple as possible, this latter time period is not considered here.

The wake width (FWHM) in Figure 3a is given in degrees, where 360° defines a full spacecraft spin. The curves for the three wake elevation angles fall on top of each other, to the accuracy of the numerical evaluation. The reason for this is the essentially Gaussian shape of the wake ensured by equation (2) at distances far behind (as compared to spacecraft dimensions) a spacecraft of any shape. The shape of a Gaussian is independent of the amplitude, which means that the observed shape of the wake will not depend on how far away from the centre of the wake a probe crosses. Thus, we expect the measured FWHM value to be a very robust determination.

On the other hand, the highest (absolute) value of the observed wake potential, here referred to as the wake amplitude, is a less stable measure. The wake amplitude does depend on how far away from the wake centre the probe passes during the spin, and thus on the wake elevation angle. This amplitude also depends on the electron temperature T_e and the Debye length. Figure 3b shows characteristic values of the wake amplitude, relevant for $KT_e = 10$ eV and short Debye lengths, so that Eqn. 4 can be used to calculate the potential. The exact numerical value can therefore not easily be compared to any single observation, but the scaling with flow angle is adequately described. For high

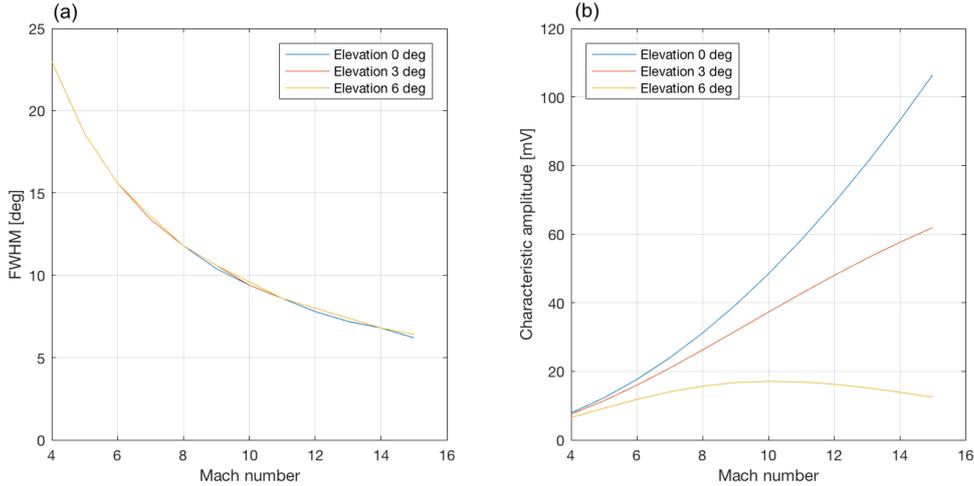


Figure 3. Theoretical wake potential properties at the EFW probes, calculated by numerical integration of Equation (2), as function of solar wind ion flow Mach number for three different wake elevation angles of the solar wind direction with respect to the spacecraft spin plane (containing the EFW wire booms). (a) The width (FWHM) of the wake is a robust estimate and lines for all angles are the same within the accuracy of the numerical calculation. (b) The estimated amplitude is a characteristic value relevant for typical solar wind parameters, including $KT_e \approx 10$ eV, not the exact peak potential in the wake.

275 Mach numbers and large wake elevation angles, the observed amplitude may be less than
 276 20% of the actual maximum voltage on the wake axis (blue curve). For small angles, the
 277 maximum amplitude increases with the Mach number, due to the decreasing ability of
 278 ions to enter the wake and fill out the density. For higher wake elevation angles the op-
 279 posite effect can be seen at sufficiently fast flow ($M > 10$), as the wake gets more and
 280 more narrow and in the end will only marginally reach the probe.

281 To compare with observations, statistics from solar wind wake data from one probe
 282 pair (1-2) on Cluster spacecraft C4 are shown in Figure 4. This figure includes 22.9×10^6
 283 identified wake signatures, each corresponding to one 4-second spacecraft spin. Obser-
 284 vations are from 2006-2014, January 15 to April 15 each year, corresponding to the times
 285 when the orbit perigee is on the dayside and the spacecraft spend significant time in the
 286 solar wind. Data are sampled at 25 samples/s (normal mode) and sometimes 450 sam-
 287 ples/s (burst mode), corresponding to a spin angular resolution of 3.6° and 0.2° , respec-
 288 tively. Panel (a) shows the wake spin angle, with zero defined as radially away from the
 289 Sun. If the solar wind flow was always radial in an inertial frame, the tangent of this an-
 290 gle would be the ratio of the spacecraft tangential velocity with respect to the Sun (in-
 291 cluding the orbital speed of the Earth, which dominates over the spacecraft speed around
 292 Earth) and the solar wind flow speed. The histogram could then be re-scaled to provide
 293 solar wind flow speed statistics. However, as the solar wind tangential speed is rarely zero
 294 even in a sun-fixed inertial frame, additional information on this speed must be provided
 295 to find the solar wind radial speed at any given moment. Nevertheless, by assuming that
 296 the tangential solar wind velocity (in a solar inertial frame) has a symmetrical distribu-
 297 tion with average value of zero, we may still use Figure 4a to find the mean solar wind
 298 speed for this data set. The median value of 5.0° (with a range of 4.0 to 6.0 for the in-
 299 dividual years) combined with the Earth's average orbital speed of 30 km/s then yields
 300 a typical solar wind radial speed of ~ 340 km/s. In this case, this is only an order of mag-
 301 nitude estimate showing that the method is reasonable. The estimate of the solar wind

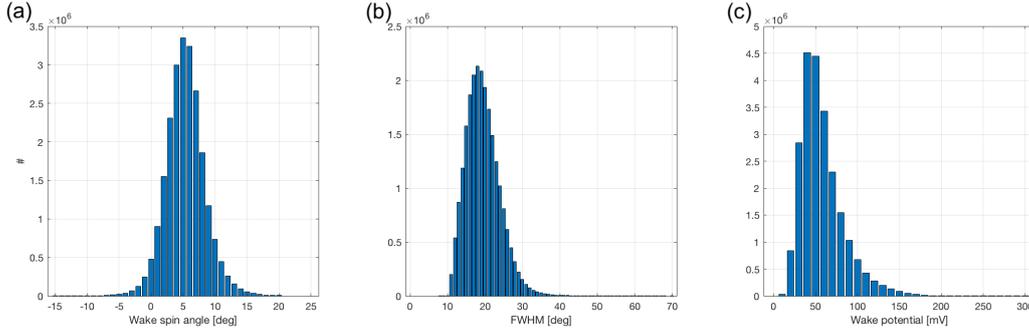


Figure 4. Solar wind wake characteristics observed by one probe pair (1-2) of the EFW instrument on Cluster 4 during three months (Jan 15 to Apr 15) of each of the years 2006-2014, in total about 22.9×10^6 data points. (a) Spin phase of the wake centre (wake spin angle), with zero corresponding to the antisunward direction. (b) Full width (in degrees) at half minimum of the wave voltage signal. (c) Wake amplitude, i.e. the maximum of the observed probe potential (as compared to the value outside the wake).

302 direction deviation is reliable, but in the normal telemetry mode the typical deviation
 303 is only slightly larger than the angular resolution. We note that we have not used any
 304 selection criteria other than data quality, e.g., concerning fast and slow solar wind. In
 305 section 3.2 we use a similar technique to determine the drift velocity of ions in the pol-
 306 ar lobes, but based on individual spacecraft spins with a well determined wake direc-
 307 tion and using another technique to determine the perpendicular velocity.

308 Panel (b) in Figure 4 shows the distribution of wake widths, defined by the observed
 309 FWHM, which as discussed above is expected to be a very robust observable. The me-
 310 dian of 19° (15° to 20°) can be compared to the theoretical prediction in Figure 3a, where
 311 it can be seen to correspond to a Mach number of about 5. For the solar wind speed of
 312 340 km/s corresponding to the peak in solar wind direction discussed above, this yields
 313 an ion temperature of about 20 eV, again a reasonable order of magnitude estimate for
 314 the solar wind. With the observed wake width, we can return to the quasi-neutrality as-
 315 sumption we introduced when using equation (4) to estimate a theoretical value of the
 316 wake potential. For the 44 m-long wire booms of EFW, a FWHM value of 19° corresponds
 317 to transverse width of about 15 m across the wake. At the spacecraft location, the width
 318 of the wake is set by the spacecraft body. At 44 m from the spacecraft, the ion random
 319 thermal motion has moved ions from outside the low density region into a wider but less
 320 depleted wake.

321 A wake width of 15 m is similar to the Debye length in a typical solar wind plasma
 322 with density 5 cm^{-3} and electron temperature 10 eV (Table 1). For typical parameters,
 323 the Debye length is short enough for the quasi-neutrality assumption to be reasonable,
 324 and Figure 3b will give an order of magnitude estimate of the wake amplitude.

325 Figure 4c displays the maximum potential found by the probes when crossing the
 326 wake. The observations have a median of 52 mV (42 - 69 mV), with respect to the am-
 327 bient surrounding plasma. To compare with Figure 3b we consider $M=5$ - 10 , (consistent
 328 with typical ion temperatures and solar wind velocities), for the assumed typical elec-
 329 tron temperature of 10 eV, and wake elevation angles of 3 - 7° . This gives amplitudes of
 330 10 - 30 mV, and reasonable agreement between our simple model and observations.

331 Our analytical model as well as particle-in-cell simulations (Miyake & Usui, 2016),
 332 indicate that the narrow solar wind wake extends well beyond the 44 meter EFW wire

333 booms. Using this simple model, many properties of solar wind wakes can be estimated.
 334 This can be used as a tool, both to investigate the solar wind and to understand the ef-
 335 fects on in situ observation. As solar wind parameters usually can be obtained by ion
 336 spectrometers, there has been little reason to develop the wake model described above
 337 to provide e.g. solar wind direction and ion temperature estimates. However, as we will
 338 see in next Section, there are other situations when the wake signature may give the only
 339 practical means to observe an otherwise hidden ion population.

340 3.2 Wake in the polar lobes (enhanced wake)

341 At high altitudes in the polar lobes the density is even lower than in the solar wind
 342 (Haaland et al., 2017). In this low density plasma, spacecraft charging is often high (tens
 343 of volts) since photoelectrons emitted from the satellite dominate its current balance (Pedersen,
 344 1995). The drift energy of ions originating in the ionosphere (a few eV) is often lower
 345 than the equivalent spacecraft charging, and the drift of the cold ions is often supersonic
 346 (Table 1), hence

$$KT_i < mv_i^2/2 < eV_{SC}. \quad (5)$$

347 Thus, the ions are not deflected by the physical spacecraft structure but rather by
 348 a much larger electrostatic structure. This will cause an enhanced wake, Fig. 1d. Also,
 349 ions will not reach the spacecraft and can not be directly detected. Some first studies
 350 of an enhanced wake behind a positively charged spacecraft are presented by Pedersen
 351 et al. (1984) and Bauer et al. (1983).

352 With supersonic positive ions but subsonic electrons the wake will be negatively
 353 charged. This is similar to the solar wind, but this is an enhanced wake with much larger
 354 transverse dimensions. The local wake electric field will dominate observations by a wire
 355 boom instrument, and the geophysical field can not routinely be recovered. The wake
 356 electric field can be obvious over large regions in the polar lobes. Figure 5 shows data
 357 from the EFW double-probe instrument (red line) and the EDI electron drift instrument
 358 (blue line) on two Cluster spacecraft (C1 and C3) (Eriksson et al., 2006). During the first
 359 part of this 1.5 hour interval the two instruments agree reasonably well most of the time.
 360 The EFW probe-to-plasma potential V_{ps} shown for both spacecraft is essentially the neg-
 361 ative of the spacecraft potential V_{SC} and hence indicates density variations. For conver-
 362 sion of V_{ps} to density, see Lybekk et al. (2012). After 04:20 UT, V_{ps} and hence the den-
 363 sity decreases, and the spacecraft potential increases on C1. At the same time, the EFW
 364 and EDI electric fields start to clearly deviate on C1.

365 The large positive potential V_{SC} can cause an enhanced wake when outflowing cold
 366 ions are present, relation (5). The data in Fig. 5 are consistent with a local (order 100
 367 m) wake electric field observed by EFW, while the EDI observations are only marginally
 368 affected. Note that both instruments are making good observations, but one is of a lo-
 369 cal electric field dominated by an artificial field caused by the presence of a charged space-
 370 craft, while the other is an observation over a larger region of a mainly undisturbed geo-
 371 physical electric field. On C2 the ASPOC instrument is turned on at about 04:20 UT.
 372 The spacecraft potential is immediately reduced, as intended. The EFW and EDI ob-
 373 servations become similar, further confirming the scenario of an enhanced wake which
 374 is much reduced when the spacecraft charging is reduced. A spacecraft potential of about
 375 +7 V remains, possibly causing some of the remaining difference between the EFW and
 376 EDI observations.

377 Figure 6 shows 30 minutes of data from C3. When ASPOC is on, the difference be-
 378 tween EFW and EDI is much reduced. In addition, four 4-second spacecraft spins are
 379 shown from one probe-pair, when ASPOC is off. With an amplitude of a few mV/m the
 380 signal is often non-sinusoidal, as in the top panel of Figure 6. For higher positive space-

381 craft potential (tens of volts) the signal can be sinusoidal and hard to distinguish from
 382 a geophysical quasi-static electric field.

383 In cases of a strongly charged spacecraft (in practise, very low density) the charged
 384 booms will give a significant contribution to the size of the extended wake. The electro-
 385 static structure scattering cold ion can in many cases not be approximated by a sphere
 386 centered at the spacecraft and the sketch in Fig. 1d is then oversimplified. However, since
 387 the ions do not reach the spacecraft the details of the scattering potential is often not
 388 of any practical importance. For the case of intermediate spacecraft charging, when the
 389 ions can just marginally not reach the spacecraft (the spacecraft body has the main in-
 390 fluence) or can indeed marginally reach the spacecraft (but effects of the charged booms
 391 must be taken into account) see section 3.3 below.

392 It is sometimes difficult to discern between local electric fields due to enhanced wakes
 393 and geophysical electric fields, and interpretation of data from double-probe instruments
 394 should be performed with caution, in particular in regions with possible cold ion drifts.
 395 For routine archiving purposes of Cluster EFW data, an algorithm is using a combina-
 396 tion of parameters including spacecraft potential, magnetic field direction and different
 397 electric field components. When the magnetic field is close to the Cluster spin plane, the
 398 algorithm searches for indications of a large local parallel electric field. (A large geophys-
 399 ical electric field parallel to the magnetic field would give high-energy particles, which
 400 are not observed.) For other magnetic field directions, different perpendicular compo-
 401 nents of the electric field are compared (assuming zero parallel electric field, since ob-
 402 servations are obtained only in the spin plane.) Higher ratios indicate a higher proba-
 403 bility of an enhanced wake. For more focused investigations, when EDI data are avail-
 404 able, significant differences between EFW and EDI observations can be used as an in-
 405 dication of a wake. Sometimes a combination of wake and geophysical electric fields, ob-
 406 served by EFW and EDI, can be used for scientific investigations, see section 4 on iono-
 407 spheric outflow below.

408 For a narrow solar wind wake (section (3.1)), the wake electric field is observed by
 409 EFW during a small part of the spacecraft spin. Here the wake signature can removed,
 410 and the geophysical electric field can be obtained in many directions (Fig. 2). For an en-
 411 hanced wake in the lobes, the electric field observed by EFW is again a sum of a wake
 412 field and a geophysical field. But here the wake field is observed during the whole space-
 413 craft spin (Fig. 6). Engwall and Eriksson (2006) showed examples indicating that it is
 414 in principle possible to obtain the geophysical electric field from the EFW instrument
 415 also for an enhanced wake, by considering the Fourier spectrum of the observed signal.
 416 This requires that the spin-period signal from one probe-pair is not a sinusoidal (some
 417 signal from the geophysical field can be detected). The spin tone harmonics in this spec-
 418 trum are due only to the wake, whose direction thereby can be determined and the wake
 419 removed. This method is complicated to use, partly due to the the so-called sunward off-
 420 set (Cully et al., 2003; Khotyaintsev et al., 2014) but can in principle be attempted on
 421 an event basis. Our observations, and also simulations (Engwall, Eriksson, & Forest, 2006;
 422 Eriksson et al., 2010; Miyake & Usui, 2016), indicate that the enhanced polar lobe wake
 423 extends well beyond the 44 meter EFW wire booms. There is no attempt to routinely
 424 obtain the geophysical electric field but this situation is used for statistical investigations
 425 of the flux of cold ions, see section 4.

426 3.3 Intermediate parameters

427 In an intermediate parameter range, supersonic cold ions can marginally reach the
 428 charged spacecraft but are significantly affected by both the charged spacecraft and the
 429 charged wire booms of an electric field instrument. In this case

$$mv_i^2/2 \gtrsim eV_{SC}, \quad mv_i^2/2 > KT_i. \quad (6)$$

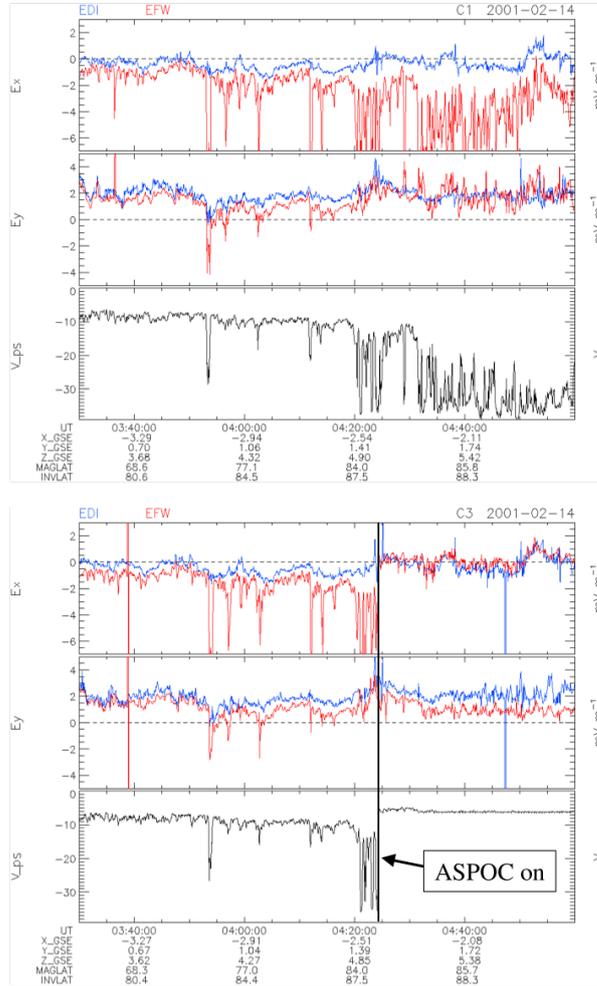


Figure 5. Effects of enhanced wakes in the polar lobes. Cluster EFW (double-probe, red line) and EDI (electron drift, blue line) instrument electric field observations in the satellite spin plane, E_x and E_y (close to GSE x- and y-components) on spacecraft C1 and C3. The probe-to-spacecraft potential V_{ps} is used to indicate the density (low V_{ps} corresponds to low density and high positive spacecraft potential). During the second part of the time interval high spacecraft charging together with supersonic cold ions cause a significant local wake electric field observed by EFW. When ASPOC is turned on onboard C3 spacecraft charging and the wake are reduced, and the local wake electric field is much reduced. From Eriksson et al. (2006)

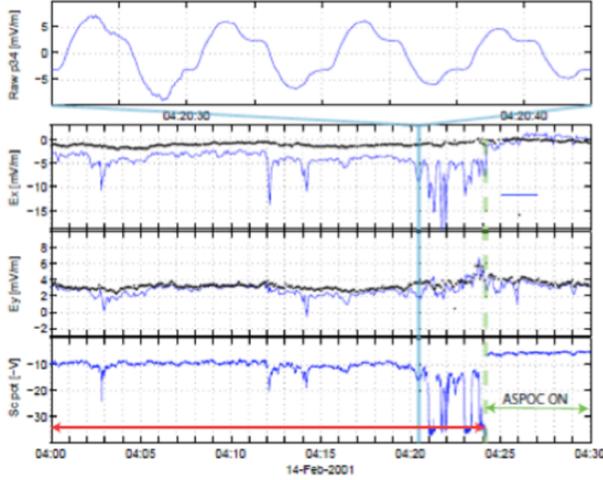


Figure 6. Effects of enhanced wakes in the polar lobes, detailed view of part of the event in Fig. 5 for Cluster spacecraft C3. The upper panel shows four 4-second spins of one EFW probe-pair. The non-sinusoidal signal indicates an intermediate size of the enhanced wake, a large wake would essentially enclose also the booms and the signal would be a sine-wave. An enhanced wake gives a large local electric field which can be used to investigate supersonic cold ions. Reducing spacecraft charging and hence the wakes makes it possible to observe the geophysical electric field with a double-probe instrument.

430 Figure 7 illustrates how the electric field instrument wire booms on MMS are important for the ions trajectories, in this case just inside the magnetopause (Toledo-Redondo
 431 et al., 2019). The upper part of the figure shows sketches of a changing situation as the spacecraft spins: Ions are deflected by the electric field of charged booms and can not
 432 reach particle detectors on the spacecraft, or the ions are focused into on-board detectors, see also the simulations by Miyake et al. (2013). The wake behind the spacecraft
 433 changes as a function of the spin phase, and the electrostatic potential structure cannot be approximated as spherical. The three lower panels show MMS observations of this
 434 effect. Fig. 7c shows the electric field in the spin plane. Every ~ 5 s, i.e., a quarter of the MMS spin period, the double probes measure a non-geophysical wake electric field (marked
 435 with vertical black lines), while the electric field measured between the electric field spikes is a geophysical field which is supported by a good agreement between the measured \mathbf{E}
 436 and $-\mathbf{v} \times \mathbf{B}$ (not shown). Fig. 7d shows the ion density, measured using an ion detector (black), and inferred from the plasma frequency (blue). An artificial dropout in plasma
 437 density is measured by the ion detector when the wire booms are aligned to the cold ion flow which is then deflected, as illustrated in Fig. 7a. Density enhancements are also observed
 438 by the detector between the vertical black lines, which are consistent with Fig. 7b, although no independent validation of the calibration of the low-energy channels of the
 439 ion instrument has been performed for this time period. Fig. 7e shows the omnidirectional spectrogram recorded by the ion instrument and the spacecraft potential (black
 440 line). The cold proton beam has drift energies of about 2 times the equivalent spacecraft potential, and the repetitive detection gaps every quarter of spin can be clearly observed.
 441 The light blue signature at ~ 100 eV corresponds to cold He^+ , and detection gaps near the vertical black lines can also be observed, despite their drift energy is about 8 times
 442 larger than the spacecraft potential. This can be attributed to deflection of the ions by the electric fields pointing outward from the charged wire booms. See also Barrie et al.
 443 (2019) for an additional discussion on particle orbits near the charged MMS satellites.
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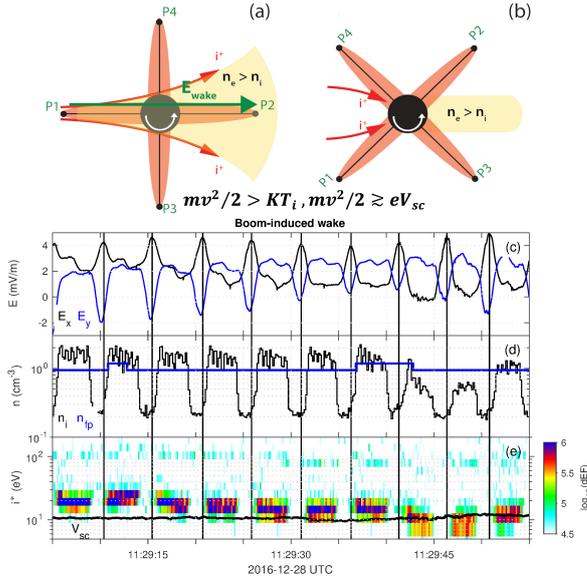


Figure 7. Sketch of one MMS spacecraft with wire booms in a flow of ions (see also Fig. 1). Panels (a) and (b): Sketch of two phases of the 20 s spacecraft spin. Positive potential around the wire booms is indicated in orange, negative space charge in the wake is indicated in yellow, positive ion orbits are shown in red. (c) Two components of the electric field, (d) density obtained from ion (n_i) data and from the plasma frequency (n_{lp}) (e) ion flux and the spacecraft potential, see Toledo-Redondo et al. (2019). For a supersonic ion flow with drift velocity similar to the equivalent spacecraft charging, the charged wire booms have large influence on the ion orbits and cause a periodic behaviour of observed particles and electric fields.

457 Care must be taken not to confuse periodic behaviour of electric field and parti-
 458 cle data (Fig. 7) with natural wave phenomena. A clear warning sign is a steady peri-
 459 odicity at a multiple of the satellite spin frequency. Also, when the spacecraft charging
 460 is similar to the equivalent ion drift energy (at the magnetopause, often $\mathbf{E} \times \mathbf{B}$ drift) a
 461 spherically symmetric potential structure around the spacecraft body can not be used
 462 to correct particle observations (Toledo-Redondo et al., 2019). The example in Fig. 7 is
 463 unusually clear but particle moments may be affected by asymmetric charging also when
 464 periodic effects are not so obvious.

465 4 The enhanced wake as a tool to detect cold ions

466 It has been suggested for decades that cold ions from the high-latitude ionosphere
 467 can dominate the density and outflow in the high-altitude magnetospheric tail lobes (Chappell
 468 et al., 1980; Moore, 1984; Olsen et al., 1985; Chappell, 2015). These positive ions often
 469 have a drift energy of one or a few eV, and even lower thermal energy, and hence can
 470 not reach a spacecraft charged positively to tens of volts. Such a supersonic outflowing
 471 "polar wind" was predicted by Axford (1968) and Banks and Holzer (1968). There are
 472 several studies of outflowing ions in the polar regions at altitudes up to a few Earth radii
 473 (Cully et al., 2003; Abe et al., 2004; Huddleston et al., 2005; Peterson et al., 2006, 2008;
 474 Nilsson et al., 2013), see reviews by Yau and André (1997), Yau et al. (2007), Moore and
 475 Horwitz (2007), André and Cully (2012), Yamauchi (2019), Yau et al. (2021) and André
 476 et al. (2021). However, at higher altitudes many ions can not reach a positively charged
 477 spacecraft. On the Polar spacecraft the charging could during some periods be artificially
 478 reduced down to a few volts positive by emitting a plasma cloud but still a significant

479 fraction of the cold outflowing ions could be missed (Moore et al., 1997; Su et al., 1998;
 480 Engwall, Eriksson, Cully, André, Puhl-Quinn, et al., 2009). An alternative method based
 481 on Cluster observations does not depend on the ions reaching the spacecraft, but is rather
 482 using the enhanced wake induced by the drifting cold ions to estimate the flux of these
 483 ions (Engwall, Eriksson, Cully, André, Puhl-Quinn, et al., 2009). While the enhanced
 484 wakes make observations of the geophysical electric field with a double-probe instrument
 485 complicated and often impossible, these wakes make it possible to detect a previously
 486 hidden cold ion population.

487 The wake-method to estimate the cold ion drift velocity is based on the local elec-
 488 tric field (observed by the EFW double-probe instrument) combined with the large-scale
 489 geophysical electric field (observed by the EDI instrument). The wake electric field is ob-
 490 tained as the difference between the local and the geophysical electric fields. In the lobes
 491 the ions can be treated as unmagnetized on the wake length scale (Table 1) and the di-
 492 rection of the wake electric field gives the ion drift direction. The ion drift perpendic-
 493 ular to the ambient magnetic field is given by the geophysical electric field (EDI) and
 494 magnetic field observations from the Fluxgate Magnetometer (FGM) (Balogh et al., 2001).
 495 Since the perpendicular velocity component and the direction of the flow are known, the
 496 parallel component can be inferred. This technique has been verified in the magnetotail
 497 (Engwall, Eriksson, André, et al., 2006), studied with simulations (Engwall, Eriksson,
 498 & Forest, 2006) and is further discussed by (Engwall, Eriksson, Cully, André, Torbert,
 499 & Vaith, 2009).

500 The density can be estimated by calibrating observations of the spacecraft poten-
 501 tial obtained by the Cluster EFW instrument (Pedersen et al., 2008; Svenes et al., 2008;
 502 Lybekk et al., 2012; Haaland et al., 2012). The potential induced by the wake is small,
 503 tens of millivolts (Fig. 4), compared to the spacecraft potential of tens of volts (Fig. 5),
 504 and has negligible effect on this estimate. The density and the outflow velocity gives the
 505 ion flux.

506 In summary, the presence of a supersonic flow of low-energy ions can be inferred
 507 by detecting a wake electric field, obtained as large enough difference between the quasi-
 508 static electric fields observed by the EFW (total electric field) and EDI (geophysical elec-
 509 tric field) instruments. To estimate the parallel drift velocity, observations of the per-
 510 pendicular $\mathbf{E} \times \mathbf{B}$ drift velocity from the geophysical quasi-static electric field (EDI) and
 511 the geophysical magnetic field (FGM) are needed, together with the direction of the wake
 512 electric field. The ion flux can then be estimated from the drift velocity and the density.
 513 Details concerning the data analysis and error estimates are given by Engwall, Eriksson,
 514 Cully, André, Puhl-Quinn, et al. (2009) and in Appendix A of André et al. (2015).

515 One ion flux estimate can be obtained for each 4-second Cluster spacecraft spin (Engwall,
 516 Eriksson, Cully, André, Torbert, & Vaith, 2009; Engwall, Eriksson, Cully, André, Puhl-
 517 Quinn, et al., 2009). Even when applying rather strict limits to minimize errors, 320,000
 518 data points (satellite spins) can be used from early 2001 to 2010 (from the peak of so-
 519 lar cycle 23 to beyond the minimum of solar cycle 24) (André et al., 2015). The low-energy
 520 ions usually dominate the density and the outward flux in the geomagnetic tail lobes dur-
 521 ing all parts of the solar cycle. The wake method does not determine the mass of the out-
 522 flowing ions, but most are believed to be low-mass H^+ . Heavier ions such as O^+ would
 523 have higher energy than lighter ions for a given drift velocity. These ions would be eas-
 524 ier to detect onboard a charged spacecraft and would then not contribute to an enhanced
 525 wake. Also, observations at lower altitudes with less spacecraft charging, and also ob-
 526 servations using artificial reduction of the spacecraft charging, indicates that most ions
 527 are H^+ (Su et al., 1998). The global outflow is of the order of 10^{26} ions/s and often dom-
 528 inates over the outflow at higher energies (Engwall, Eriksson, Cully, André, Torbert, &
 529 Vaith, 2009; André & Cully, 2012; André et al., 2015). Depending on overall geophys-
 530 ical conditions the ions may not immediately leave the magnetosphere (Haaland et al.,
 531 2012) but are likely to eventually be lost to the solar wind (André et al., 2015, 2021).

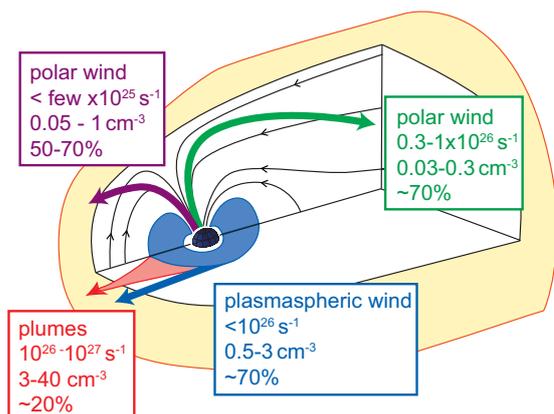


Figure 8. Overview of cold (eV) ion outflow. Typical outflow rates and densities are given together with the approximate fraction of time cold ions dominate the number density. For high latitudes, this fraction is estimated from observations of enhanced spacecraft wakes indicating cold ions with supersonic drift. For the magnetopause, a combination of methods is used. Cold ions often dominate the density of the magnetosphere. The drift paths are not obtained from local observations and are discussed in several studies, see text for references. (Figure from André and Cully (2012)).

532 This outflow is a significant part of the total mass outflow from Earth (André, 2015).
 533 Figure 8 shows an overview of low-energy ion outflow. The Cluster wake-method to de-
 534 tect cold ions has been a major method to obtain this overall picture.

535 5 Summary

536 Wakes in collisionless plasmas are common, both behind spacecraft and other ob-
 537 stacles. Behind spacecraft, wakes caused by positive supersonic ions are a well known
 538 problem affecting in situ observations, including electric field observations. Sometimes
 539 the effects of the wake are minor, easy to detect, and can be compensated for in a rea-
 540 sonable way (e.g., the solar wind). Sometimes the effects of the wake are major, due to
 541 an enhanced wake caused by a very positively charged spacecraft, and makes observa-
 542 tions of the geophysical electric field complicated or impossible, at least close to the satel-
 543 lite (e.g., the low-density polar lobes). In this situation detection of the wake can be used
 544 to detect the drifting cold ions, using electric field double-probe instruments. Together
 545 with other instruments also the cold ion flux can be estimated. The charging of the long
 546 wire booms of a double-probe instrument contributes to the electrostatic structure scat-
 547 tering drifting cold ions. For a very charged spacecraft, typical for the polar lobes, the
 548 details of this electrostatic structure can often be ignored when interpreting observations.
 549 For an intermediate range of parameters, when the drift energy of the cold ions is simi-
 550 lar to the equivalent spacecraft charging, also the charging of the wire booms must be
 551 considered in detail when interpreting data.

552 Some common phenomena related to the Cluster EFW double-probe instrument
 553 are not discussed in detail here. One example is the spurious electric fields in the plas-
 554 masphere. Fields that are not geophysical of the order 1-2 mV/m, mainly in the sun-
 555 ward direction, are detected by an empirical algorithm, (Puhl-Quinn et al., 2008; Khotyaint-
 556 sev et al., 2014). This spurious field seems partly related to a subsonic ion flow and the
 557 long wire booms (Miyake et al., 2015).

558 Plasma wakes behind spacecraft with instruments for in situ plasma observations
 559 are common. These wakes change the local plasma environment, as compared to the geo-
 560 physical conditions without the spacecraft. The wakes can make some observations of
 561 geophysical parameters complicated, and sometimes impossible. With understanding of
 562 the physics causing the wakes, the local effects can in many situations be compensated
 563 for. In some situations otherwise inaccessible geophysical parameters can be estimated,
 564 using the wake caused by the presence of the spacecraft. An important example is the
 565 flux of cold positive ions in the polar lobes. This flux of the order of 10^{26} ions/s consti-
 566 tutes a significant part of the mass outflow from planet Earth. Often these positive ions
 567 can not reach a positively charged spacecraft. Rather, the ion flux can be obtained from
 568 the properties of the enhanced wake.

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 573 are available from <https://lasp.colorado.edu/mms/sdc/public/>. We acknowledge support
 574 from the ISSI international team Cold plasma of ionospheric origin at the Earth's mag-
 575 netosphere.

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Examples of parameters: Low Earth Orbit, upper ionosphere

n (cm ⁻³)	KT_e (eV)	KT_i (eV)	B (nT)	ions	v_i (km/s)	V_{SC}
1000	1	1	40000	H ⁺ or O ⁺	8	-1

λ_D (m)	ρ_e (m)	ρ_i (m)	v_{th} (km/s)	$mv_i^2/2$ (eV)
0.22	0.055	2.3	13	0.3

Useful relations

$$\lambda_D < L_{SC} \quad \rho_e < L_{SC} \quad \rho_i \approx L_{SC}$$

Examples of parameters: Solar wind (narrow wake)

n (cm ⁻³)	KT_e (eV)	KT_i (eV)	B (nT)	ions	v_i (km/s)	V_{SC}
5	10	10	5	H ⁺	400	+5

λ_D (m)	ρ_e (m)	ρ_i (m)	v_{th} (km/s)	$mv_i^2/2$ (eV)
10	1400	60000	41	830

Useful relations

$$KT_i < mv_i^2/2 \quad mv_i^2/2 \gg eV_{SC} \quad \lambda_D > L_{SC} \quad \rho_e \gg L_{SC} \quad \rho_e \gg L_{boom} \quad \rho_i \gg L_{boom}$$

Examples of parameters: Polar lobes (enhanced wake)

n (cm ⁻³)	KT_e (eV)	KT_i (eV)	B (nT)	ions	v_i (km/s)	V_{SC}
0.1	2	1	20	H ⁺	30	+40

λ_D (m)	ρ_e (m)	ρ_i (m)	v_{th} (km/s)	$mv_i^2/2$ (eV)
30	160	4800	13	5

Useful relations

$$KT_i < mv_i^2/2 \ll eV_{SC} \quad \lambda_D \gg L_{SC} \quad \rho_e \gg L_{SC} \quad \rho_e > L_{boom} \quad \rho_i \gg L_{boom}$$

Examples of parameters: Spacecraft dimensions

Spacecraft body	Wire booms
$L_{SC} \approx 2$ m	$L_{boom} \approx 100$ m

Table 1. Examples of parameters for LEO in the upper ionosphere, solar wind and polar lobes. Here n , KT_e , KT_i , B , v_i and V_{SC} are the density, electron and ion thermal energies, geomagnetic field, ion drift velocity and spacecraft potential. From this we derive λ_D , ρ_e , ρ_i , v_{th} $mv_i^2/2$, the Debye length, electron and ion gyroradii, thermal ion velocity and ion drift energy. Typical length scales of a spacecraft main body and wire booms are also given, L_{SC} and L_{boom} . In LEO, the drift velocity is taken to be the velocity of an orbiting spacecraft, while a sounding rocket moves much slower, and derived parameters are given for H⁺. In the solar wind, the drift velocity is an example of a solar wind velocity, and in the polar lobes a typical outflow velocity of ionospheric ions is given. For an overview of near-Earth plasma parameters see textbooks, e. g. Kivelson and Russell (1995). Relevant parameters from the upper ionosphere are given by Miyake et al. (2020), from the solar wind by Eriksson et al. (2006, 2007), and from the polar lobes by Engwall, Eriksson, Cully, André, Puhl-Quinn, et al. (2009), André et al. (2015) and Haaland et al. (2017). Sketches of corresponding wakes are given in Figure 1.

Figure 1 (left).png. efwx2.png

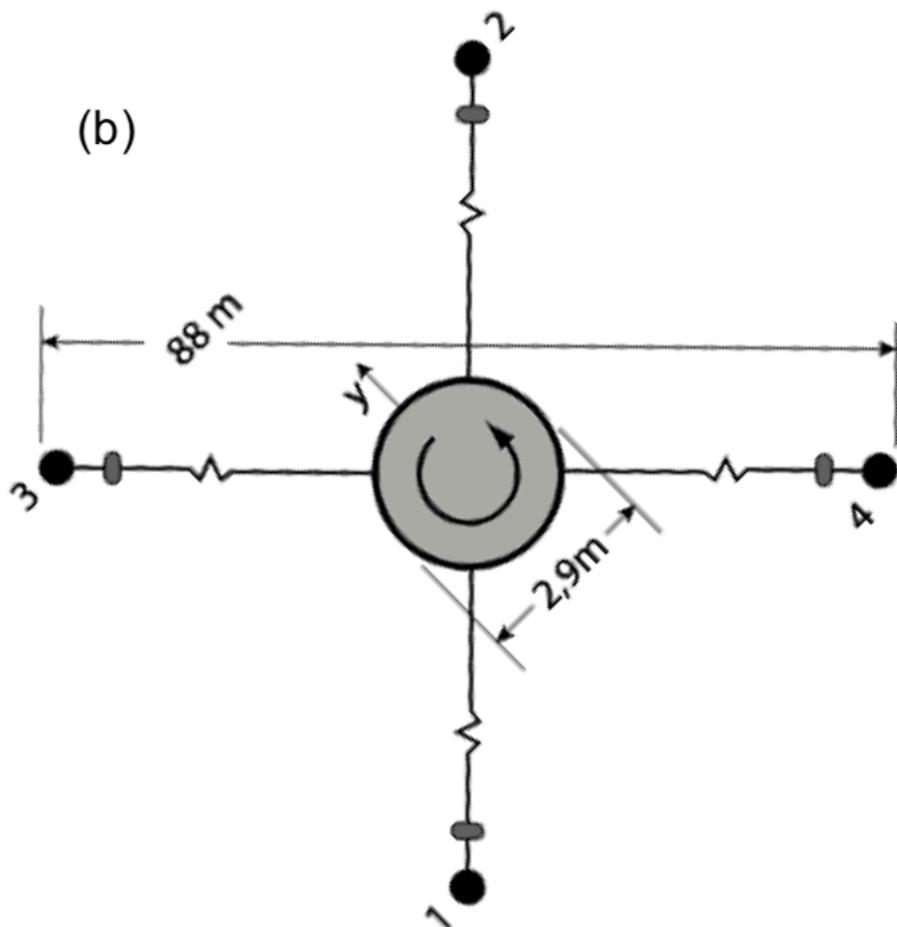
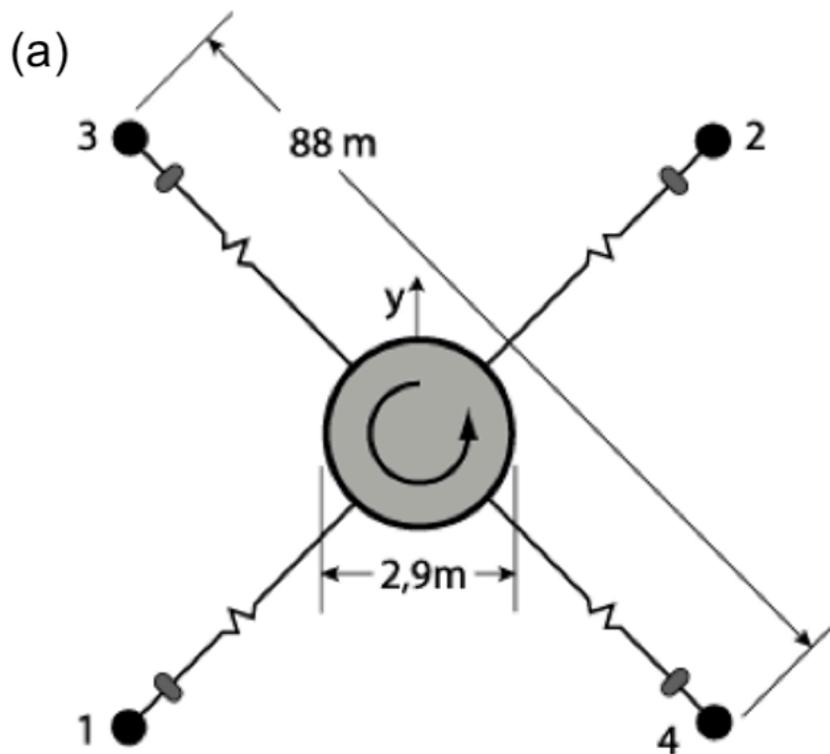


Figure 1 (right).png.

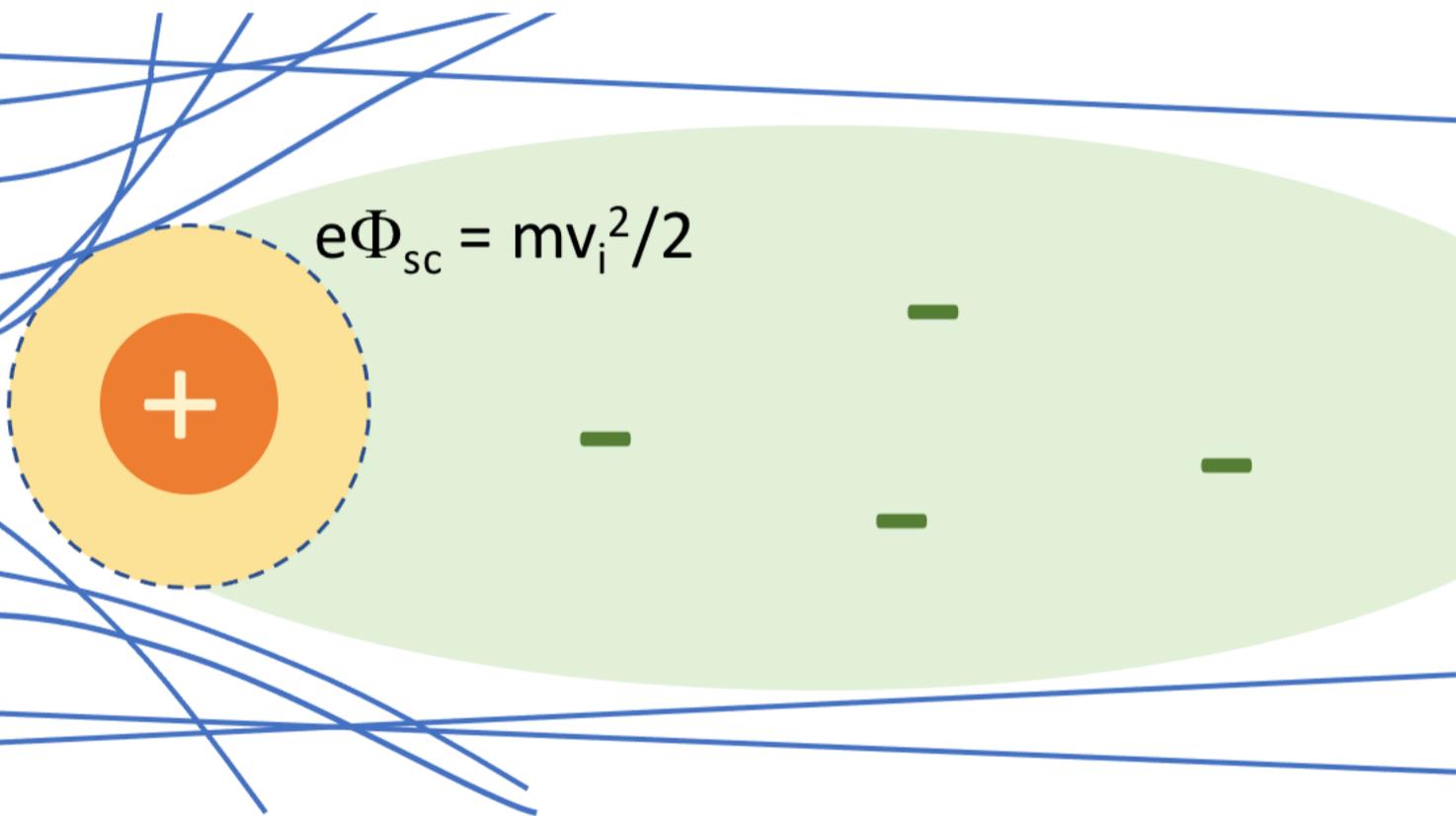
(c) Narrow wake

$$mv_i^2/2 > KT_i, \quad mv_i^2/2 \gg e|V_{sc}|$$



(d) Enhanced wake

$$eV_{sc} \gg mv_i^2/2 > KT_i$$



(e) Focussing wake

$$-eV_{sc} > mv_i^2/2 > KT_i$$

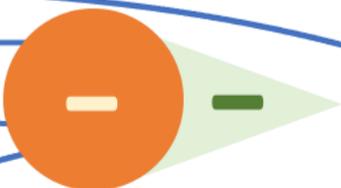


Figure 2.png.

C3 p12

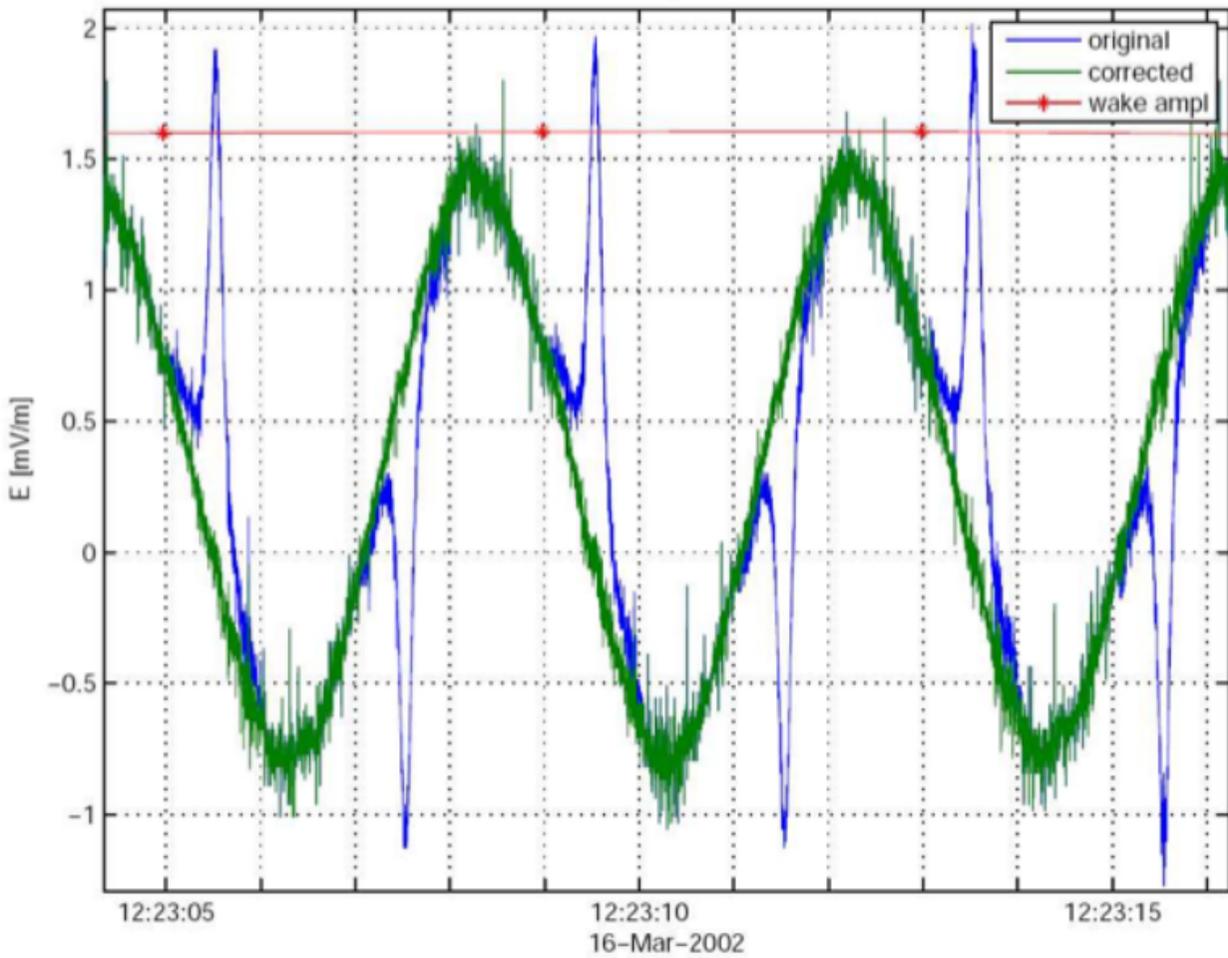


Figure 3.png.

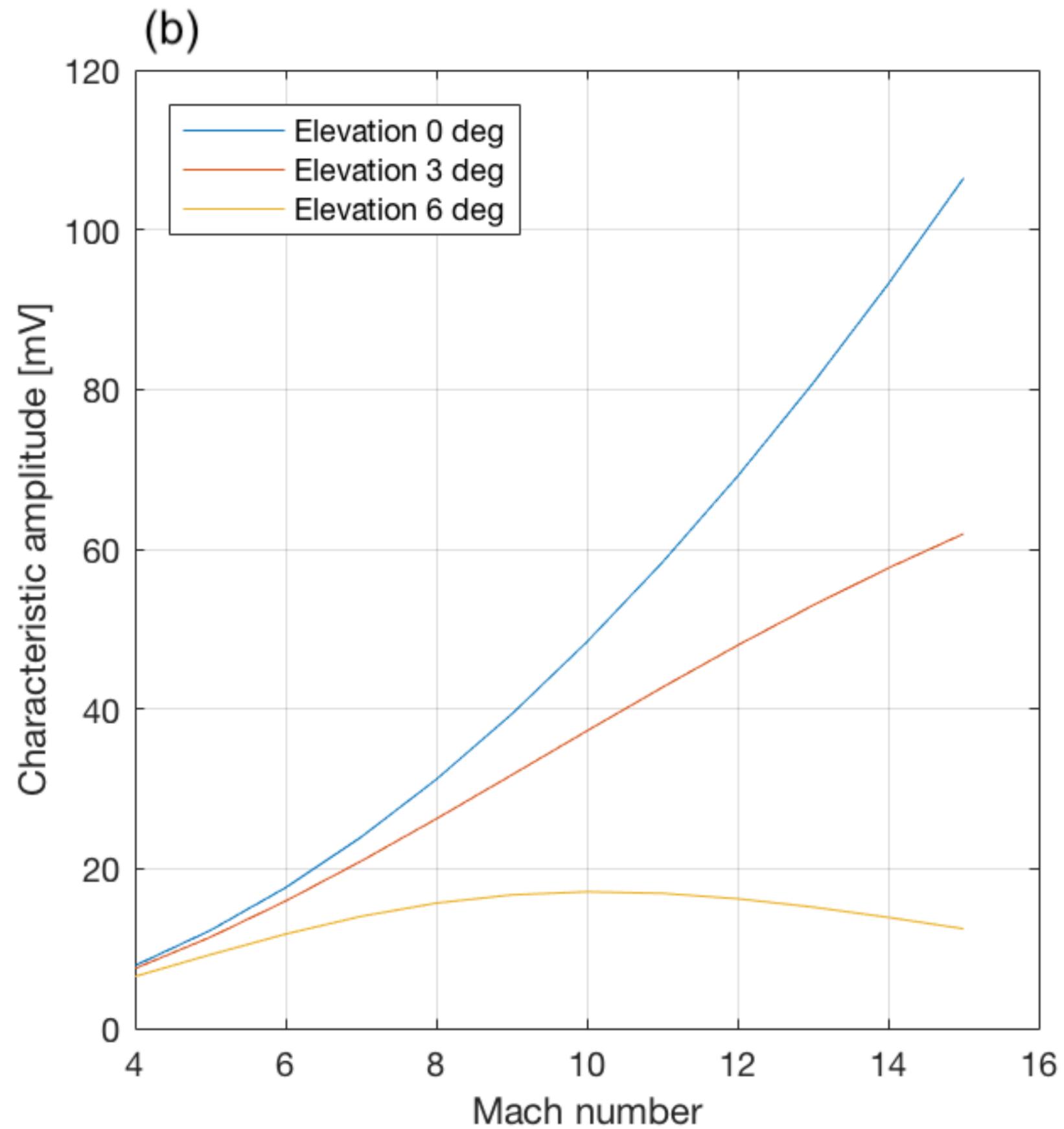
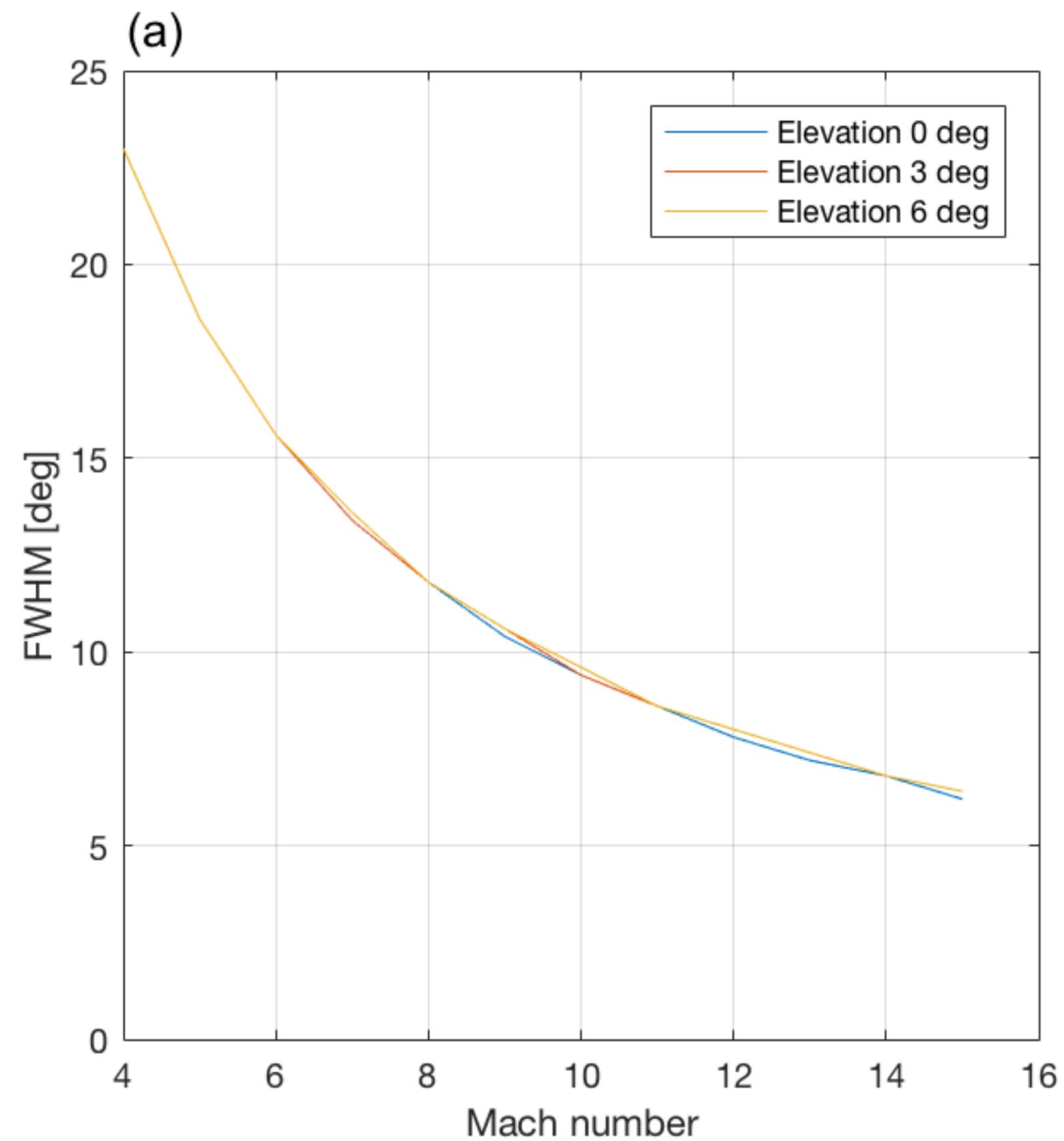


Figure 4.png.

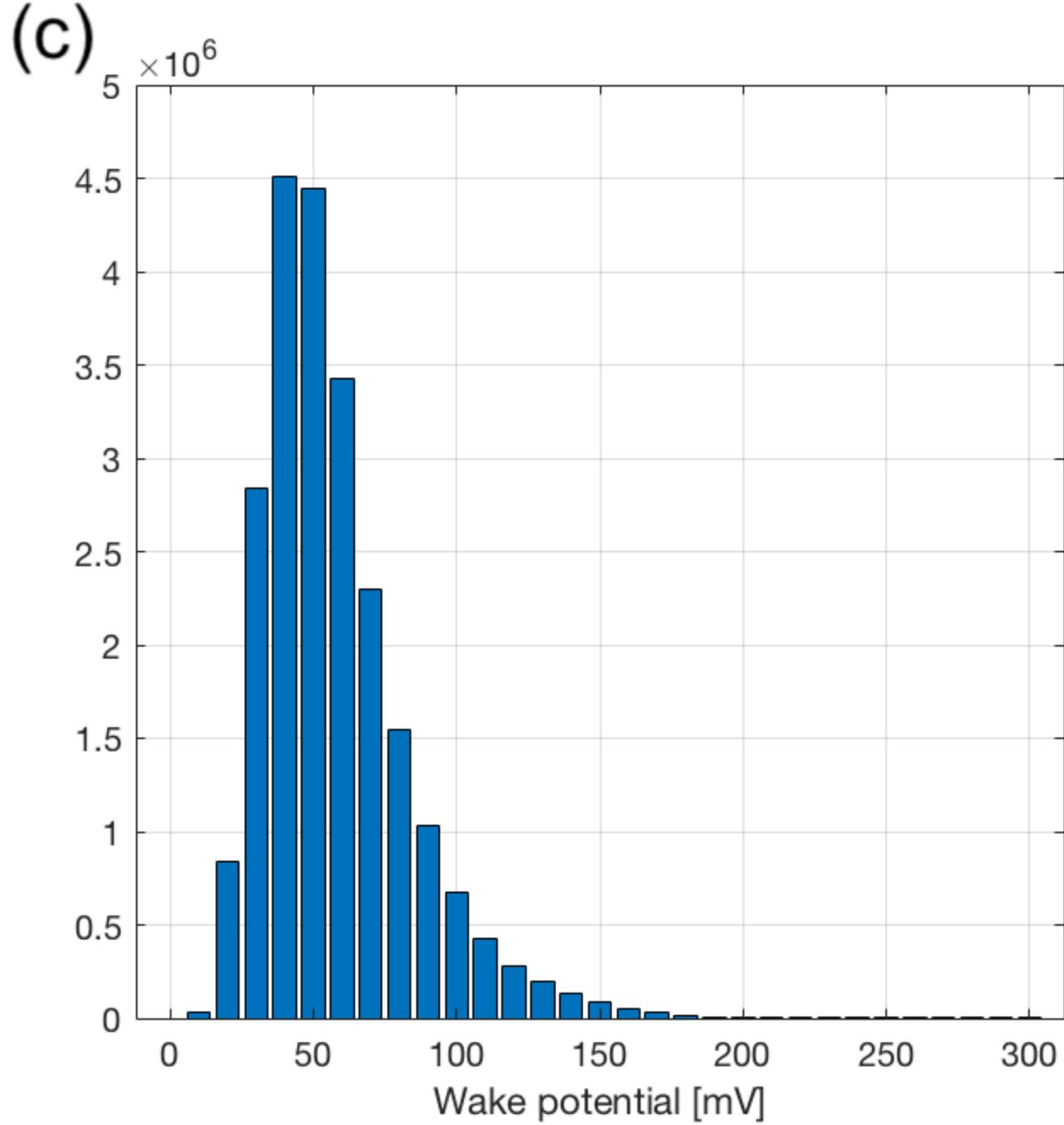
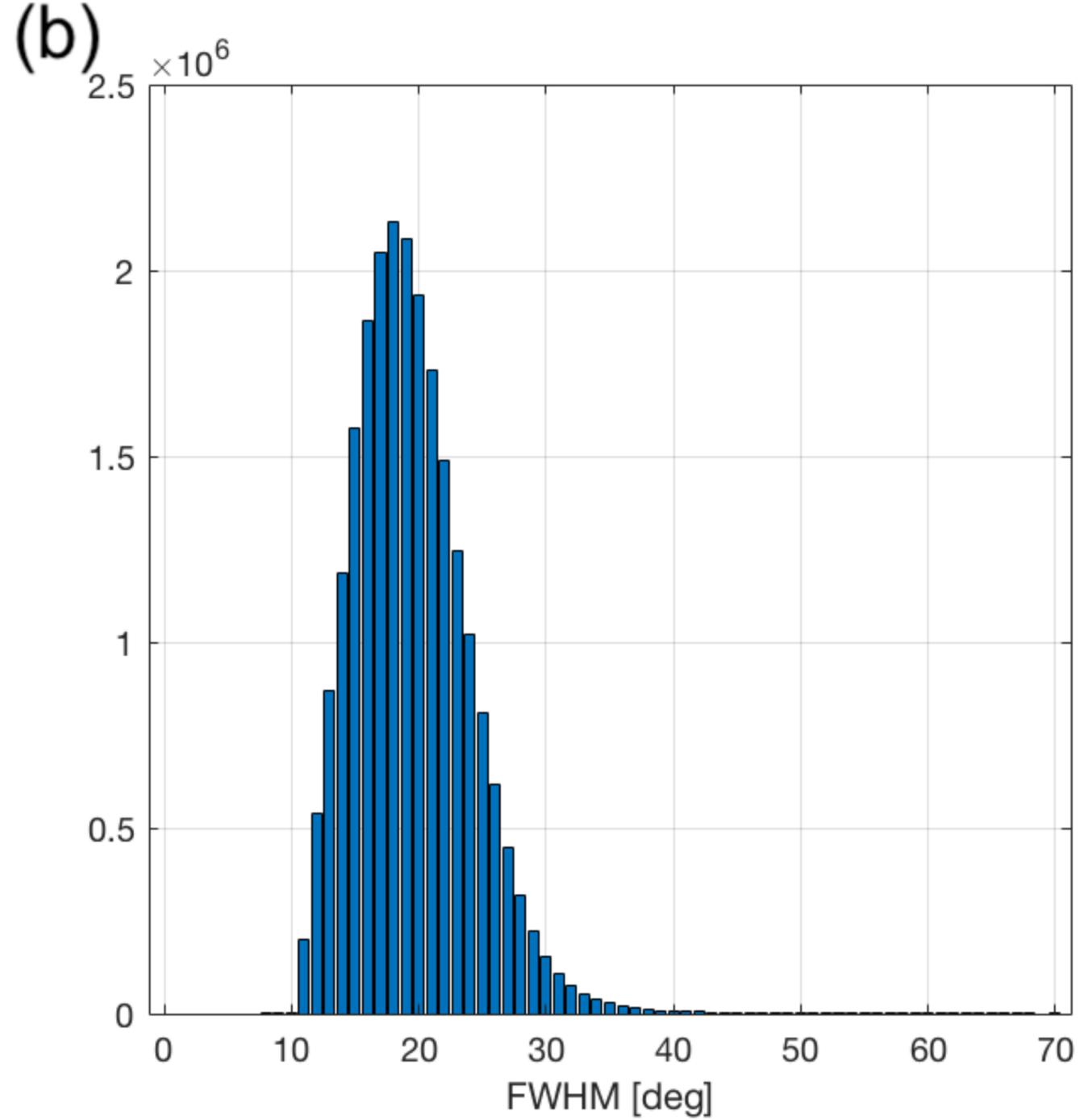
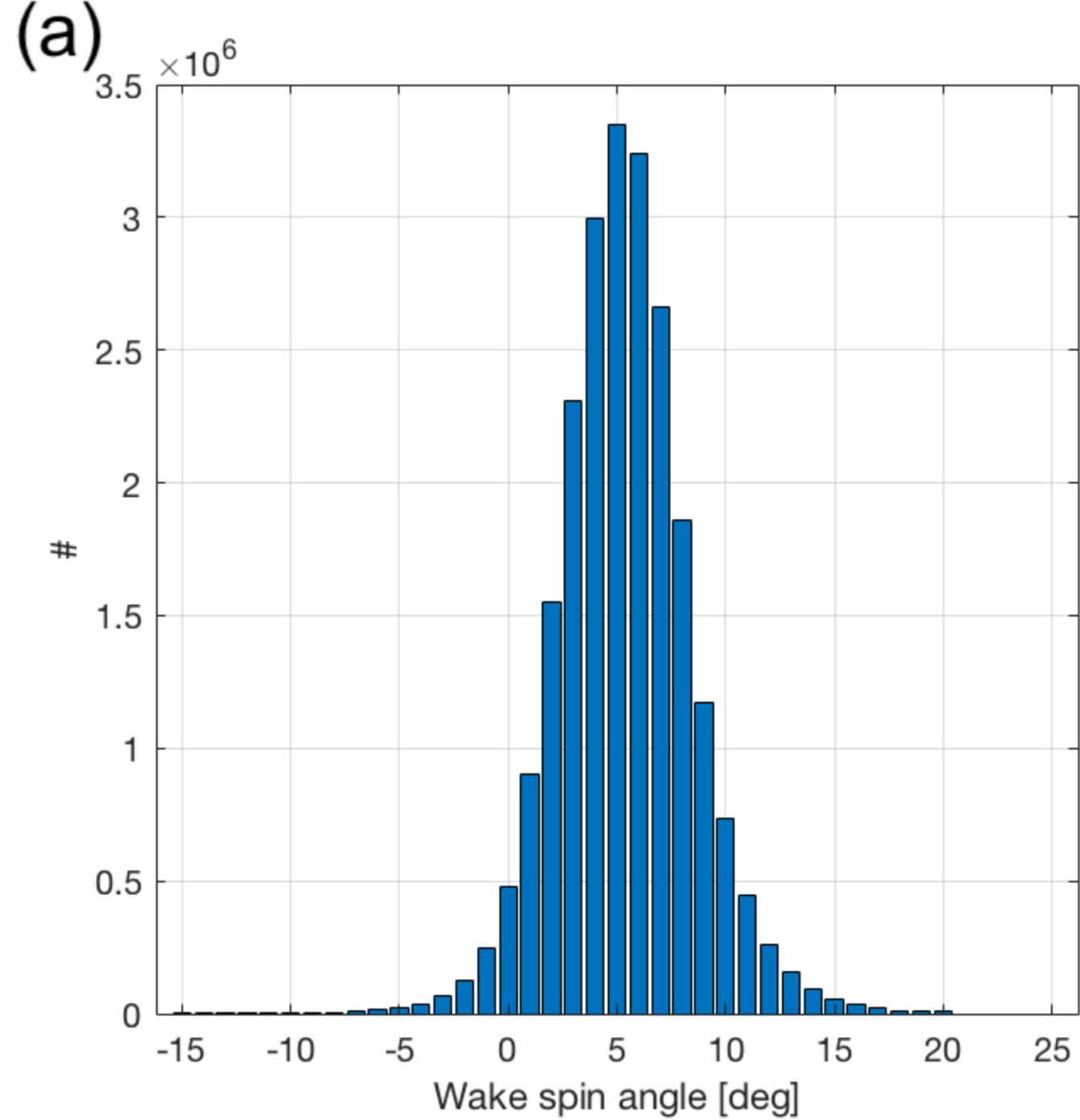


Figure 5.png.

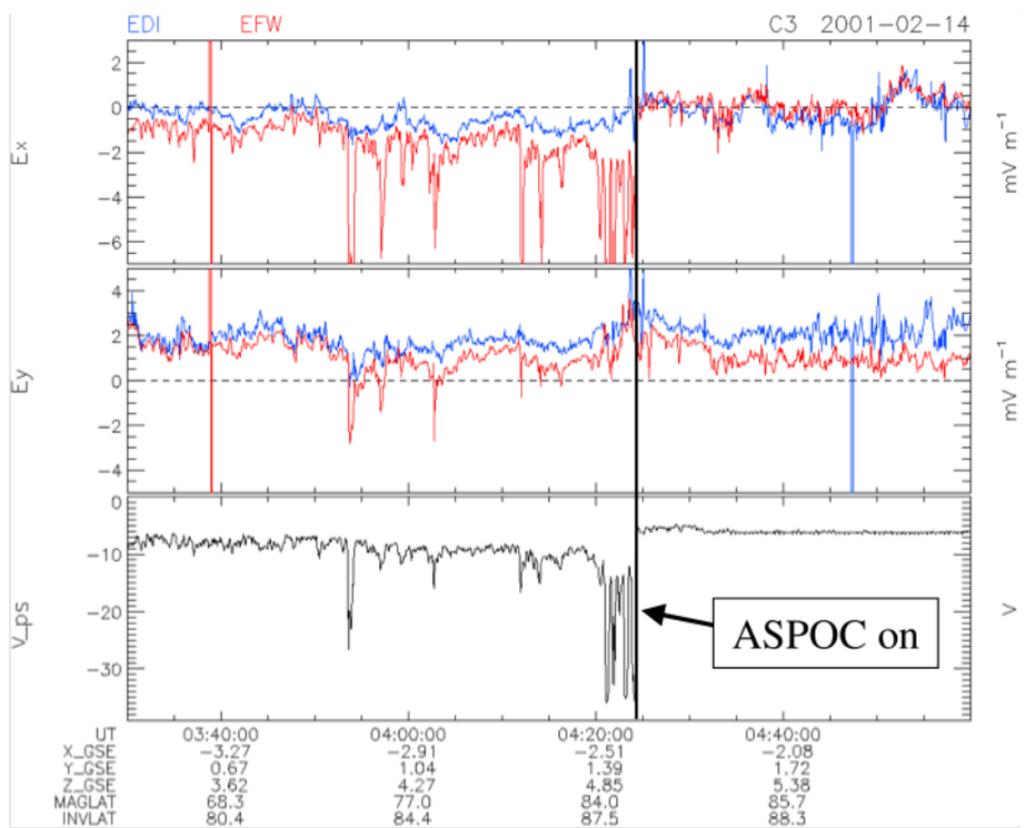
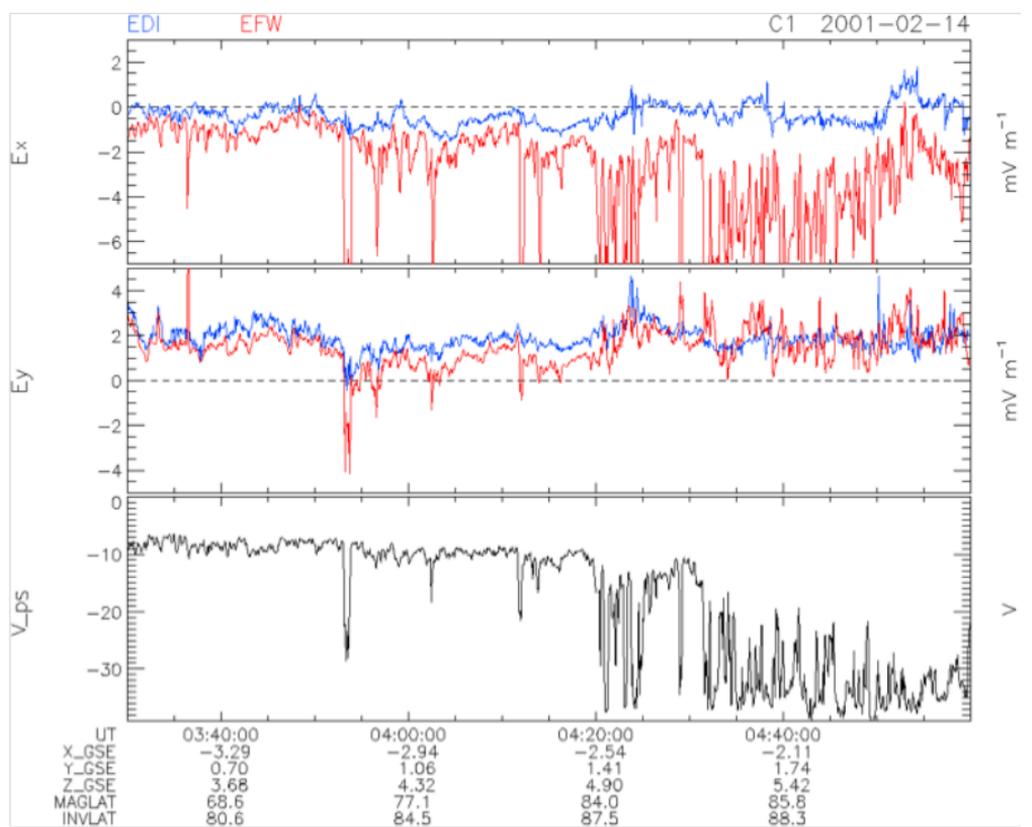


Figure 6.png.

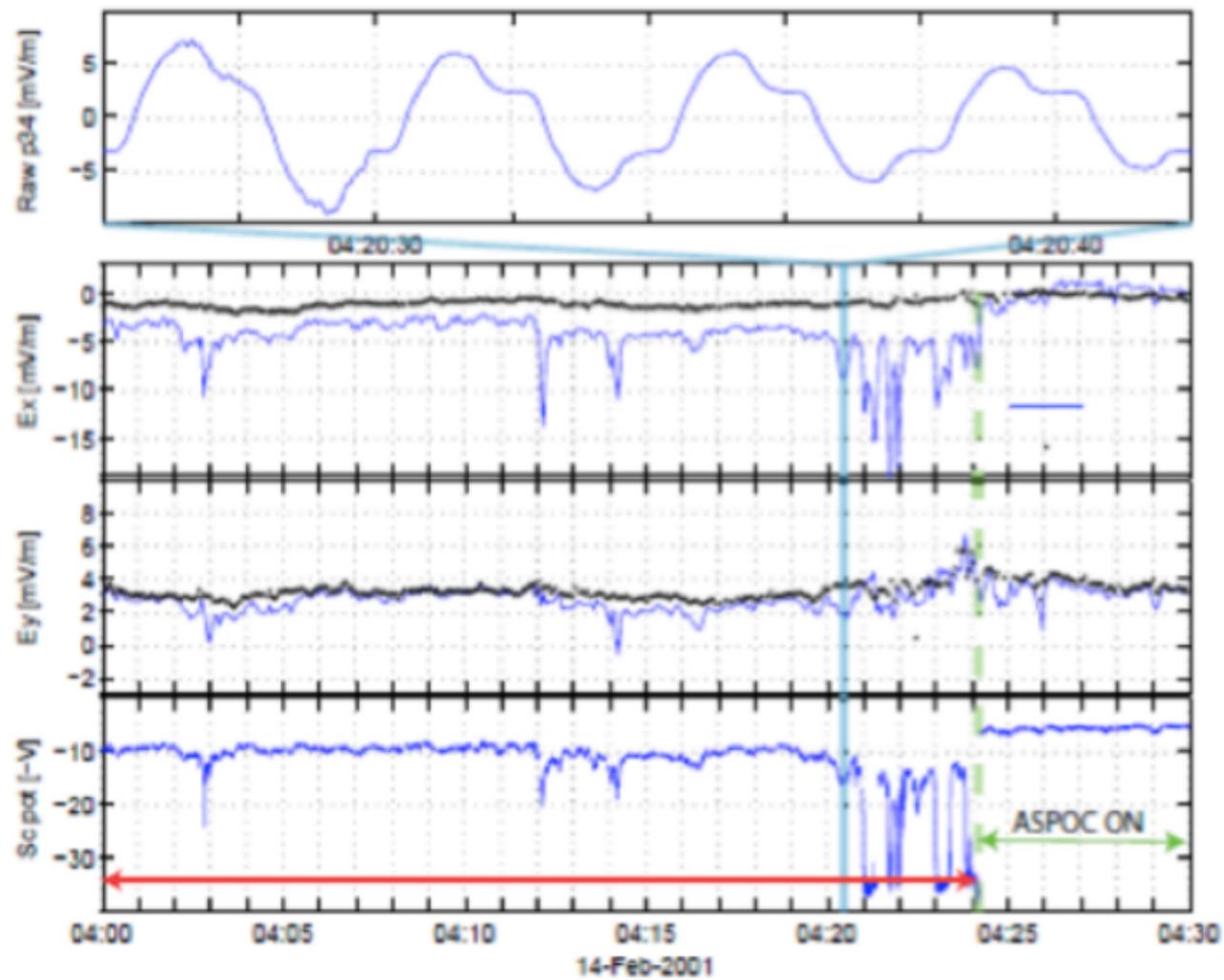


Figure 7.eps.

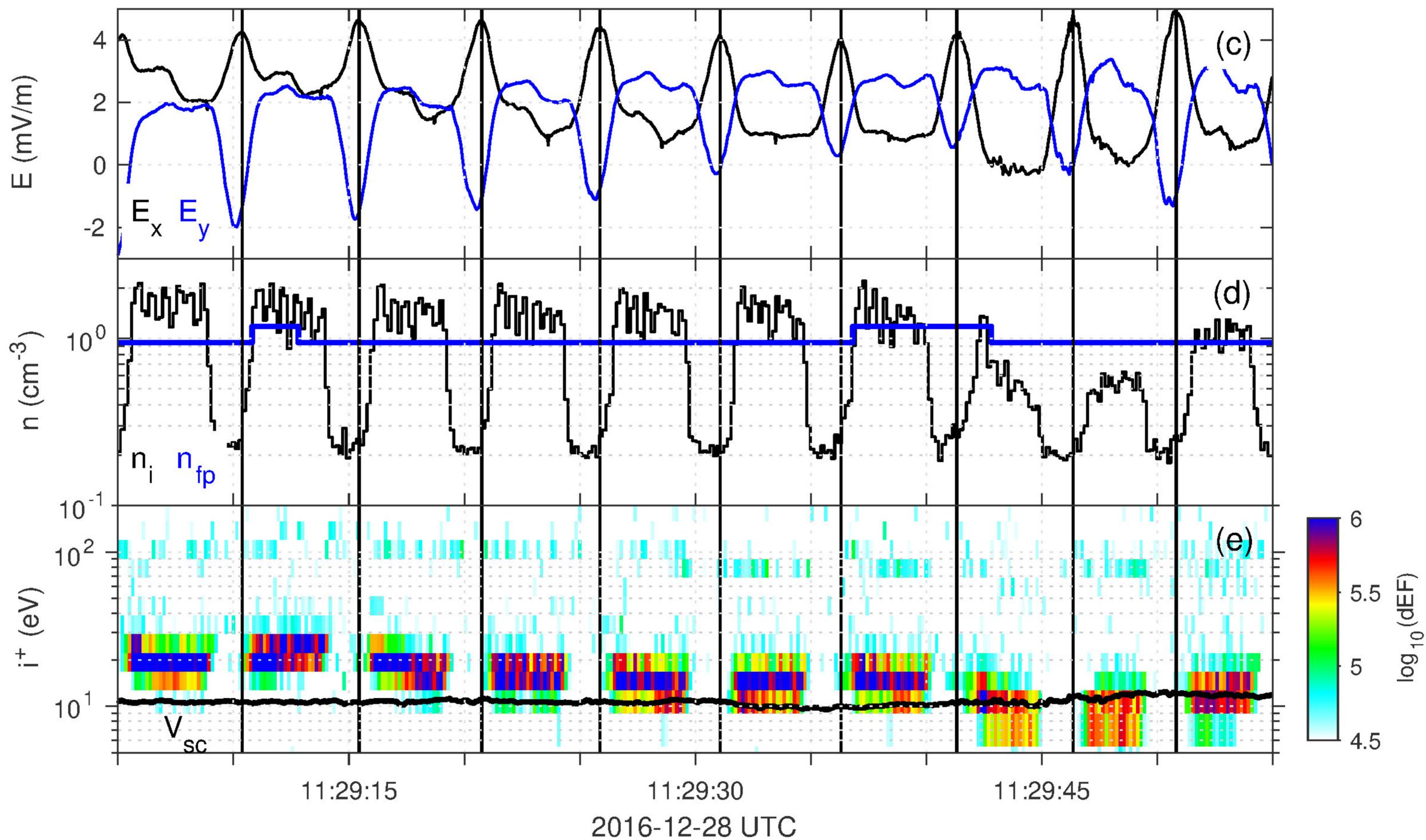
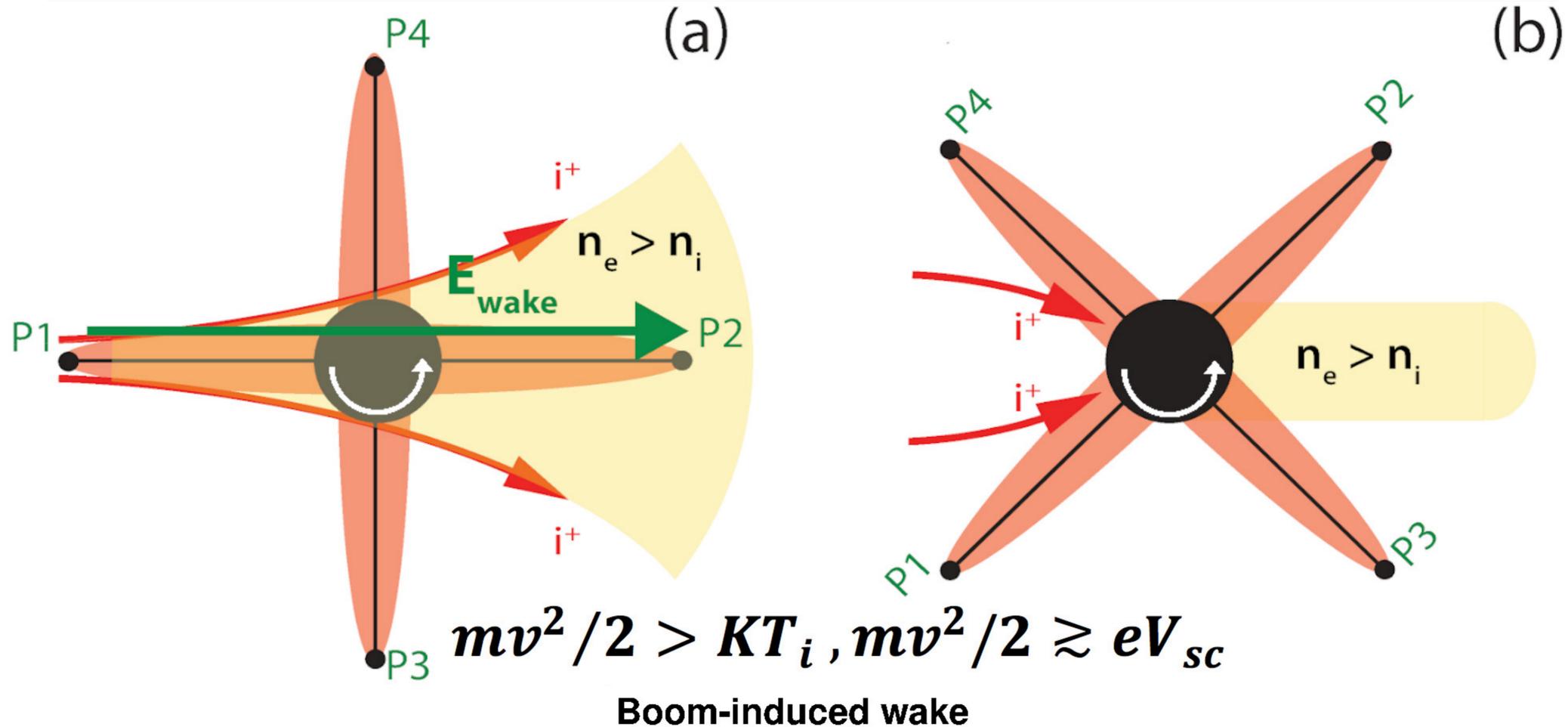


Figure 8.eps.

polar wind
 $< \text{few } \times 10^{25} \text{ s}^{-1}$
 $0.05 - 1 \text{ cm}^{-3}$
50-70%

polar wind
 $0.3 - 1 \times 10^{26} \text{ s}^{-1}$
 $0.03 - 0.3 \text{ cm}^{-3}$
~70%

plumes
 $10^{26} - 10^{27} \text{ s}^{-1}$
 $3 - 40 \text{ cm}^{-3}$
~20%

plasmaspheric wind
 $< 10^{26} \text{ s}^{-1}$
 $0.5 - 3 \text{ cm}^{-3}$
~70%