

Joint Dependence of Longwave Feedback on Surface Temperature and Relative Humidity

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Abstract

Understanding how the outgoing long-wave radiation (OLR) depends on surface temperature is a climate problem of long standing. Various studies have suggested that clear-sky OLR varies linearly with surface temperature, with a longwave clear-sky feedback that is independent of surface temperature and relative humidity. However, this uniformity lies in tension with the notion that humidity controls tropical stability (e.g. the “furnace” and “radiator fins” of Pierrehumbert, 1995). Here we explore the state-dependence of longwave clear-sky feedback as a function of both surface temperature and column relative humidity. We find that a strong relative humidity-dependence in the feedback emerges above 275 K, stemming from the closing of the H₂O window. We construct a simple model for estimating the all-sky feedback and find that although clouds lower the zonal-mean longwave feedback, the dependence on humidity remains significant.

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Key Points:

- The longwave clear-sky feedback exhibits a significant RH-dependence at high temperatures.
- Tropical variations in longwave clear-sky feedback (e.g. “radiator fins”) are a consequence of this RH-dependence.
- Cloud radiative effects estimated from a simple model do not qualitatively change this picture.

Abstract

Understanding how the outgoing long-wave radiation (OLR) depends on surface temperature is a climate problem of long standing. Various studies have suggested that clear-sky OLR varies linearly with surface temperature, with a longwave clear-sky feedback that is independent of surface temperature and relative humidity. However, this uniformity lies in tension with the notion that humidity controls tropical stability (e.g. the “furnace” and “radiator fins” of Pierrehumbert (1995)). Here we explore the state-dependence of longwave clear-sky feedback as a function of both surface temperature and column relative humidity. We find that a strong relative humidity-dependence in the feedback emerges above 275 K, stemming from the closing of the H₂O window. We construct a simple model for estimating the all-sky feedback and find that although clouds lower the zonal-mean longwave feedback, the dependence on humidity remains significant.

Plain Language Summary

The dependence of outgoing longwave radiation radiation (OLR) on surface temperature (i.e. the feedback) is a major determinant of the climate’s stability. Various investigators have suggested that the feedback is largely independent of both surface temperature and relative humidity, which implies that the climate stability is also independent of surface temperature and relative humidity. However, this uniformity seems to contradict other work which shows that the subtropics are relatively stable and the deep tropics are relatively unstable, implying the feedback must vary between the two regions. We resolve this apparent contradiction by systematically computing the feedback as a function of both surface temperature and relative humidity. Above 275 K, the feedback depends significantly on relative humidity. We then show the feedback does indeed vary in the tropics and that this difference arises from regional differences in relative humidity. Finally, we estimate the effects of clouds on the feedback with a simple model and find that although clouds have a destabilizing influence, the significant dependence on relative humidity is retained. Our work gives a renewed appreciation for how the feedback can vary significantly with both surface temperature and relative humidity.

1 Introduction

The longwave clear-sky feedback parameter λ_{cs} relates a change in clear-sky outgoing longwave radiation OLR_{cs} to a change in surface temperature T_s ,

$$\lambda_{cs} \equiv \frac{dOLR_{cs}}{dT_s} \quad (\text{Wm}^{-2}\text{K}^{-1}). \quad (1)$$

It is a measure of the stability of the the climate and thus is a well studied quantity, with a canonical value for its global mean of about $2.2 \pm 10\%$ $\text{Wm}^{-2}\text{K}^{-1}$ (Budyko, 1969; R. D. Cess et al., 1989, 1990; Raval et al., 1994; Bony et al., 1995; Allan et al., 1999; Dessler et al., 2008; Chung et al., 2010; Jeevanjee, 2018; Koll & Cronin, 2018; Zhang et al., 2020).

The convergence of the global mean value of λ_{cs} across both observations and the model hierarchy suggests robust physics that is insensitive to the idiosyncrasies of the individual studies. Recently, Koll and Cronin (2018) gave an explanation of this physics as a balance between increasing surface Planck feedback and decreasing surface transmissivity. They verified that $\lambda_{cs} \approx 2.2 \text{ Wm}^{-1}\text{K}^{-1}$ for a wide of T_s in a column model. Zhang et al. (2020) then extended this analysis to GCMs and similarly found λ_{cs} to be independent of both T_s and free-tropospheric relative humidity (RH).

This work on the uniformity of feedback lies in tension with the notion that meridional variations in clear-sky relative humidity are important in controlling tropical stability. In particular, Pierrehumbert (1995) argued that the warm and moist deep tropics, with active deep convection (furnace) are close to a local runaway greenhouse, but

are radiatively stabilized by the warm, yet dryer, and more quiescent subtropics (radiator fins). However, Pierrehumbert (1995) was equivocal on whether the furnace and radiator fins manifest as tropical variations in OLR_{cs} , or rather in λ_{cs} , which is the more relevant parameter for stability. Indeed, as we shall show later, the latitudinal variations in OLR_{cs} in the tropics are quite muted compared to OLR_{cs} variations over the globe. Here, then, we will pursue the idea that radiator fins manifest instead as tropical variations in λ_{cs} .

Clouds are another process that may play a role in controlling the structure of zonal-mean feedback. Pierrehumbert (1995) argued for the presence of tropical furnaces and radiator fins using only clear-sky physics. However, humid regions and cloudy regions often go hand-in-hand, and high clouds are known to have a robust influence on the longwave feedback (Zelinka & Hartmann, 2010), so we might expect the longwave all-sky feedback parameter λ_{as} to look different from λ_{cs} in the zonal mean.

We lack clarity on whether the phenomenology of the furnace and radiator fins are better described by OLR_{cs} or by λ_{cs} . Relatedly there is a tension between the constancy of λ_{cs} observed across studies and the notion that humidity variations control tropical stability, and it is unclear how clouds might modulate this relationship. This state of affairs motivates us to ask the following questions:

1. Do furnaces and radiator fins indeed manifest as a contrast in the zonal-mean λ_{cs} ?
2. How do we reconcile variations in λ_{cs} implied by furnaces and radiator fins when other studies suggest λ_{cs} is approximately constant?
3. How do clouds modify the meridional structure of longwave feedback?

To this end we first construct a “phase space”, in which λ_{cs} is computed as a joint function of T_s and column RH. Below 275 K, we find that λ_{cs} stays within 10% of $2.2 \text{ Wm}^{-2}\text{K}^{-1}$, even as RH varies. Above 275 K, however, a significant RH-dependence emerges, leading to much greater variations in λ_{cs} . We show that this RH-dependence stems from the closing of the H_2O window. The tropical contrast in zonal-mean λ_{cs} is, then, a consequence of this RH-dependence at high temperatures. Finally, we construct a simple model for evaluating the all-sky feedback and find that although clouds decrease the zonal-mean feedback, the RH-dependence remains significant.

2 Results

2.1 Exploring the state dependence of λ_{cs}

We first address Question 2, by exploring the state dependence of λ_{cs} as a function of both T_s and RH. We use RH as a state variable because RH-based feedbacks have certain advantages over specific humidity (q_v) based feedbacks both from a thermodynamic point of view (Held & Shell, 2012) and from a radiative point of view (Jeevanjee et al., 2021), as specific humidity already has a de facto strong temperature dependence through the Clausius-Clapeyron relation. To compute radiative transfer we use PyRADS, a validated line-by-line column model (Koll & Cronin, 2019). We used the model in 1-D radiative-convective equilibrium, following (Koll & Cronin, 2018), in which a moist adiabat profile is assumed. We set the CO_2 concentration to 340 ppmv, the number of pressure levels to 30, and consider a spectral range between 0.1 and 3500 cm^{-1} at 0.01 cm^{-1} resolution. We only then need to specify the surface temperature and a vertically-uniform relative humidity to compute OLR_{cs} for the column. For more details of atmospheric structure and spectral databases, see “Materials and Methods” in Koll and Cronin (2018).

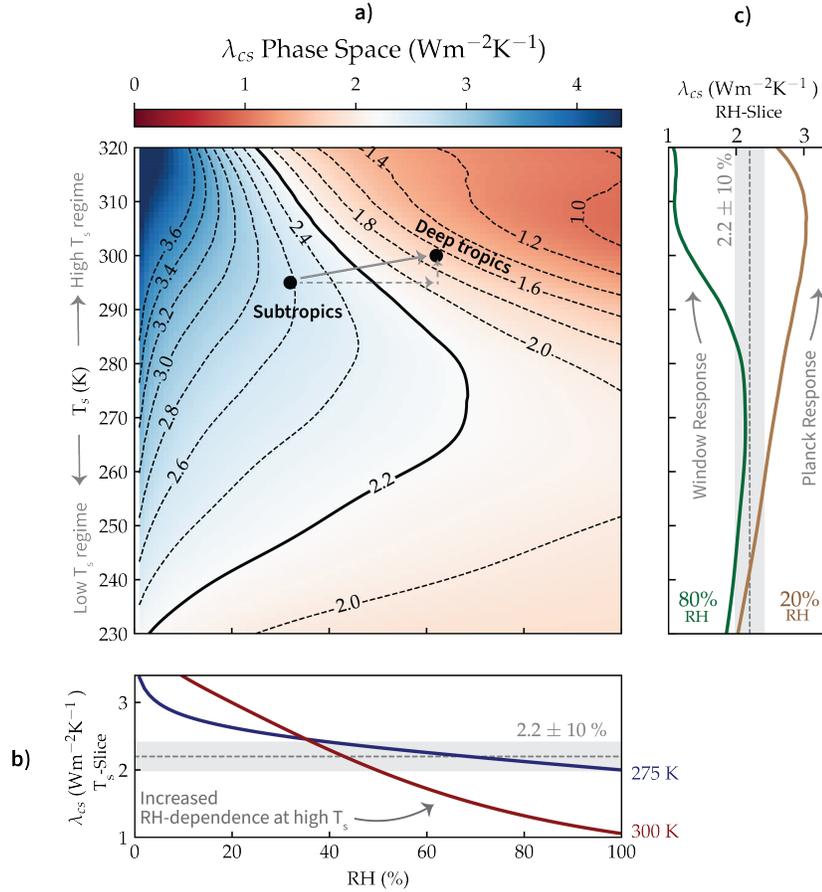


Figure 1. Exploration of state dependence of longwave clear-sky feedback λ_{cs} in a column model. (a) λ_{cs} phase space as a function of surface temperature T_s and column relative humidity RH, with contours indicating values of λ_{cs} . See Equation (2) for details of the calculation. Typical temperatures and humidity of the subtropics and deep tropics are noted as ~ 295 K/ 30% , and ~ 300 K/ 60% , respectively. The gray arrows indicate different pathways to move from the subtropics to the deep tropics. (b) Cross section of λ_{cs} phase space at 275 K and 300 K. (c) Cross section of λ_{cs} phase space at 20% and 80% relative humidity.

We calculate λ_{cs} in the following way. We first compute OLR_{cs} for some T_s and RH; we then perturb the surface temperature by an amount ΔT , and allow the moist-adiabatic atmosphere to respond while holding RH fixed; finally we calculate the perturbed outgoing longwave radiation and take the finite difference between the two states. In summary:

$$\lambda_{cs} \approx \frac{OLR_{cs}(T_s + \Delta T, RH) - OLR_{cs}(T_s, RH)}{\Delta T}, \quad (2)$$

104 where $\Delta T = 1$ K in our calculations. Note that the Planck feedback and the lapse-rate
 105 feedback are included in λ_{cs} . The moist adiabat is not satisfied in the mid-latitudes, but
 106 we note that the lapse-rate feedback is small when RH is fixed (R. Cess, 1975; Held &
 107 Shell, 2012; Zelinka et al., 2020; Jeevanjee et al., 2021). We exclude the RH-feedback for
 108 simplicity and because its value in the global mean is $< 0.1 \text{ Wm}^{-2}\text{K}^{-1}$ (Held & Shell,
 109 2012; Zelinka et al., 2020).

110 Our results are summarized in Figure 1a) for surface temperatures between 230 K
 111 and 320 K and relative humidities between 0% and 100%. We identify 275 K as the de
 112 facto boundary between a low temperature regime and a high temperature regime be-
 113 cause each region exhibits distinct behaviors for λ_{cs} . Below 275 K, there is a very small
 114 RH-dependence — for values of RH between 20% and 80%, λ_{cs} remains within 10% of
 115 $2.2 \text{ Wm}^{-2}\text{K}^{-1}$. Above 275 K, however, a significant RH-dependence emerges: the value
 116 of λ_{cs} differs from $2.2 \text{ Wm}^{-2}\text{K}^{-1} \pm$ by much more than 10% over the same range of hu-
 117 midity. We explicitly plot the RH-dependence of λ_{cs} at 275K and 300K (Figure 1b) to
 118 highlight this difference in behaviour. Thus, in response to Question 2, a λ_{cs} value of 2.2
 119 $\text{Wm}^{-2}\text{K}^{-1}$ will occur over much of the globe, and in particular will manifest as the slope
 120 of an OLR_{cs} vs T_s regression, as in Figure 1 of Koll and Cronin (2018). Nonetheless, Fig-
 121 ure 1 shows that λ_{cs} can still vary considerably at the higher temperatures of Earth’s
 122 tropics.

123 2.2 Importance of the H₂O window

124 This section provides additional context about λ_{cs} by focusing on the underlying
 125 radiation physics that controls the climate response.

126 Since λ_{cs} is dominated by surface emission through the H₂O window (Koll & Cronin,
 127 2018), the wavenumbers at which H₂O absorption is negligible for surface emission, we
 128 expect the window to play an important role in the RH-dependence of λ_{cs} at high tem-
 129 peratures. To display the H₂O window, we plot the surface-to-space transmission \mathcal{T}_ν , which
 130 measures the portion of surface emission at wavenumber ν that escapes to space. At a
 131 surface temperature of 275 K (Figure 2a), the H₂O window remains open as the rela-
 132 tive humidity is increased from 12.5% to 100%. At a surface temperature of 300 K (Fig-
 133 ure 2b), however, the H₂O window closes rapidly as the relative humidity is increased
 134 from 12.5% to 100%. This is due to activation of H₂O continuum absorption (Koll & Cronin,
 135 2018). Thus relative humidity variations are sufficient to close the H₂O window, but only
 136 at high temperatures.

137 Koll and Cronin (2018) emphasized the robustness of $\lambda_{cs} \approx 2.2 \text{ Wm}^{-2}\text{K}^{-1}$ as aris-
 138 ing from a balance between the closing of the H₂O window and the nonlinear $4\sigma T_s^3$ sur-
 139 face Planck feedback. However, at high temperatures this balance is not guaranteed and
 140 depends on RH. The H₂O window closes much faster with temperature at 80% RH than
 141 at 20% RH (Figure 2), leading to a “Planck-dominated” response at low RH, and a “window-
 142 dominated” response at high RH (Figure 1c).

143 2.3 Tropical variations in λ_{cs}

144 In Question 1 we asked whether the furnaces and radiator fins described in Pierrehumbert
 145 (1995) manifest as a contrast in the zonal-mean λ_{cs} . To answer this question we will com-
 146 pute time- and zonal-mean T_s and RH from ERA5 reanalysis (Hersbach et al., 2020) and

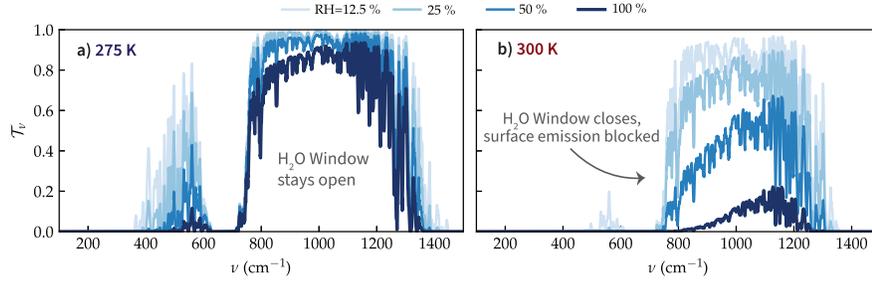


Figure 2. The closing of the H_2O window is sensitive to relative humidity at high surface temperatures. The surface-to-space transmission \mathcal{T}_ν is plotted as a function of wavenumber ν for a surface temperature of 275 K (a) and 300 K (b), and a relative humidity of 12.5%, 25%, 50%, and 100%. The H_2O window is where $\mathcal{T}_\nu \approx 1$ and surface emission escapes directly to space. We use a SavitzkyGolay filter with a 5 cm^{-1} width to smooth these plots.

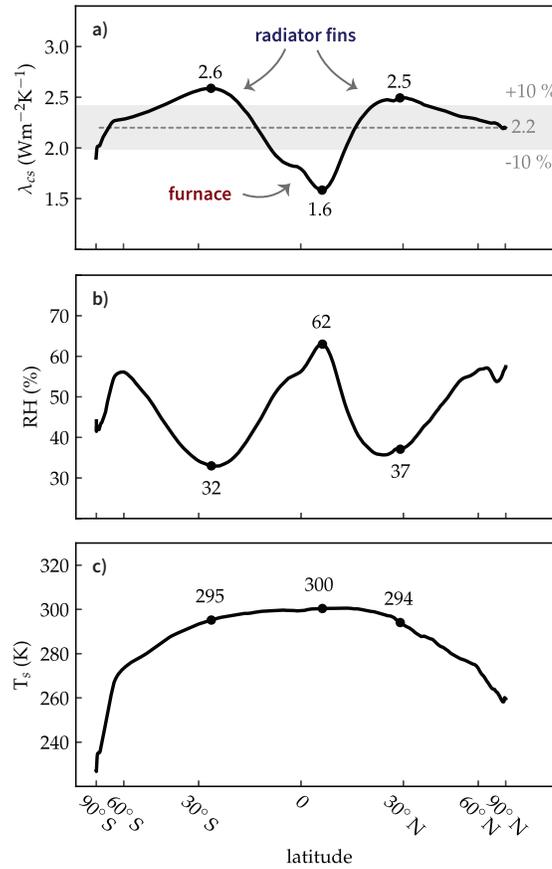


Figure 3. Furnaces and radiator fins manifest as meridional variations in longwave clear-sky feedback λ_{cs} . (a) Zonal-mean λ_{cs} is diagnosed from Figure 1, using the reanalysis zonal-mean RH (b) and the reanalysis zonal-mean T_s (c) as inputs. The shaded region in (a) represents the global mean value of $2.2 \pm 10\% \text{ Wm}^{-2}\text{K}^{-1}$ reported in other studies. We posit that the local maxima and minimum of λ_{cs} that lie outside this range should be considered the “radiator fins” and “furnace”, respectively, of the the tropics. Note the equal-area scaling of the x-axis.

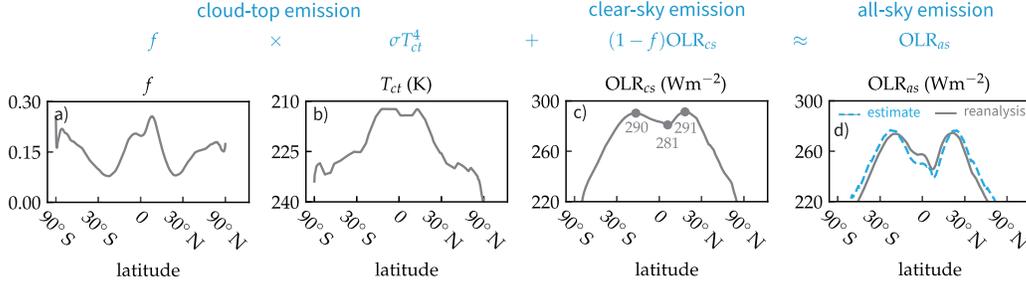


Figure 4. A simple model for zonal-mean all-sky emission. (a) cloud-top fraction f , (b) cloud-top temperature T_{ct} , (c) clear-sky emission OLR_{cs} , and (d) all-sky emission OLR_{as} . The gray curves are from ERA5 reanalysis. The dashed-blue curve in (d) is our simple estimate produced by the equation above the panels (see Equation 3). Note the equal-area scaling of the x-axis.

147 use these values to read off zonal-mean λ_{cs} from the phase space of Figure 1. We take
 148 hourly data sub-sampled every 6 hours from January 1 - December 31, 1981 and compute
 149 annual averages. Following Zhang et al. (2020), we calculate a free-tropospheric col-
 150 umn RH as the water vapor mass between 850 hPa and the 300 hPa divided by the satu-
 151 rated water vapor mass within the column. Finally, we exclude the boundary layer RH
 152 and stratospheric water vapor because of their limited impact on the OLR (Zhang et al.,
 153 2020).

154 We might expect a significant drop in λ_{cs} from the subtropics to the deep tropics
 155 by looking at representative values of T_s and RH in the λ_{cs} -phase space (Figure 1). In-
 156 deed, the meridional structure of zonal-mean λ_{cs} calculated as described above, shows
 157 λ_{cs} varying from 2.6 to 1.6 $Wm^{-2}K^{-1}$ in the tropics, a 38% drop (Figure 3a). Both
 158 the subtropical maxima and deep tropical minimum lie outside the $2.2 \pm 10\%$ $Wm^{-2}K^{-1}$
 159 range. We posit that these extrema of λ_{cs} should be considered the true “radiator fins”
 160 and “furnace”, respectively, of the the tropics.

161 We can test whether the significant drop in λ_{cs} between the radiator fins and the
 162 furnace is due to the difference in humidity, as emphasized by Pierrehumbert (1995), or
 163 if the drop is due to the difference in temperature. If we look again at the phase space
 164 in Figure 1, we can take a path that goes from the subtropics to the deep tropics in two
 165 parts: a first part with constant surface temperature, and a second part with constant
 166 relative humidity (see the dashed gray arrows). In this region of phase space, the dou-
 167 bling of relative humidity from 30% to 60% causes a much larger change in λ_{cs} than the
 168 increase in surface temperature from 295 K to 300 K does.

169 Our answer to Question 2 is then: zonal-mean λ_{cs} exhibits local extrema, which
 170 may be usefully viewed as the furnace and radiator fins of the tropics. Furthermore, these
 171 extrema are indeed due to RH variations, consistent with Pierrehumbert (1995). λ_{cs} ex-
 172 hibits a local maxima in the subtropics because they are hot and dry enough for the feed-
 173 back to exhibit a Planck-dominated response, and λ_{cs} exhibits a local minimum in the
 174 deep tropics because it is hot and moist enough for the feedback to exhibit a window-
 175 dominated response (Figure 1c).

176 2.4 Incorporating the effects of cloudiness

177 In Question 3, we asked whether clouds affect the meridional structure in zonal-
 178 mean longwave feedback in the tropics. Rather than explicitly compute cloud feedbacks,

179 which is beyond the scope of this paper, we try to estimate them by constructing a simple
 180 model for how clouds modify longwave emission. To validate the approach, we first
 181 estimate the all-sky OLR, OLR_{as} , from a few inputs: OLR_{cs} , the cloud-top fraction f ,
 182 and the cloud-top temperature, T_{ct} . OLR_{cs} is taken directly from ERA5 reanalysis. f
 183 is diagnosed from ERA5 reanalysis as the local max of the zonal-mean cloud fraction profile
 184 above a 550 hPa threshold, which is used to avoid misidentifying cloud tops with bound-
 185 ary layer cloudiness. T_{ct} is the atmospheric temperature at which cloud fraction profile
 186 peaks. We smooth the T_{ct} with a Savitzky-Golay filter with a 10° latitude width to ac-
 187 count for sharp jumps in T_{ct} arising from the limited vertical resolution. This method
 188 of identifying cloud tops is similar to Thompson et al. (2017). We show our methodol-
 189 ogy in the SI.

190 To estimate OLR_{as} , we first consider the effect of high clouds, which block long-
 191 wave emission from lower levels and replace it with their own longwave emission from
 192 cloud tops. We assume high cloud emission acts like a black body and occurs high enough
 193 in the atmosphere that emission travels directly to space (Siebesma et al., 2020). As for
 194 low clouds, we grossly assume the low clouds emit at a temperature close enough to T_s
 195 that they only negligibly alter the outgoing radiation (D. Hartmann, 2015). Given these
 196 assumptions, we can now write down a simple expression for OLR_{as} :

$$OLR_{as} \approx \sigma T_{ct}^4 f + OLR_{cs}(1 - f). \quad (3)$$

197 This model is similar in some ways to the conceptual model created in (Soden et al., 2008)
 198 to examine cross-field correlations between clear-sky and cloud feedbacks.

199 To get a sense of what the inputs to equation 3 look like, we plot annual- and zonal-
 200 mean f , T_{ct} , OLR_{cs} , and OLR_{as} from ERA5 reanalysis in gray in Figure 4. Note the muted
 201 latitudinal dependence of OLR_{cs} compared to variations in OLR_{cs} throughout the rest
 202 of the globe. This is inconsistent with the notion of radiator fins as significant subtrop-
 203 ical maxima in OLR_{cs} , which is why focus on λ_{cs} instead. OLR_{as} does have more sig-
 204 nificant tropical extrema, but these should not be interpreted as a furnace and radiator
 205 fins because the longwave warming effect of deep tropical clouds is balanced by their short-
 206 wave cooling effect (Pierrehumbert, 1995; D. L. Hartmann & Berry, 2017).

207 We test the approximate all-sky radiation from Equation 3 against OLR_{as} directly
 208 output from ERA5 analysis, which includes cloud opacities and comprehensive radiative
 209 transfer in its calculation. We find that our model does an acceptable job in replicat-
 210 ing the reanalysis (Figure 4), which gives us enough confidence in this model to proceed.

211 We now use Equation 3 to compute the longwave all-sky feedback, λ_{as} . We first
 212 assume high cloud temperatures do not change appreciably with warming, consistent with
 213 a fixed anvil temperature (FAT) hypothesis (D. Hartmann & Larson, 2002; Zelinka &
 214 Hartmann, 2010). Although f can change with warming (Bony et al., 2016; Saint-Lu et
 215 al., 2020), the high cloud area feedback is quite uncertain (Wing et al., 2020; Sherwood
 216 et al., 2020), so for simplicity we assume f is constant with warming. Differentiating Equa-
 217 tion 3 with respect to T_s yields:

$$\lambda_{as} = \lambda_{cs}(1 - f). \quad (4)$$

218 This equation makes it conceptually clear how clouds modify λ_{cs} : the longwave feedback
 219 over clouds is 0. Since f is positive definite (Figure 4), $\lambda_{as} \leq \lambda_{cs}$ always. This is well
 220 demonstrated in the meridional structure of λ_{as} in Figure 5a. The all-sky feedback looks
 221 like a simple translation downward of the clear-sky feedback, and there is still a signif-
 222 icant ($\sim 50\%$) variation in λ_{as} from the subtropics to the deep tropics. Our answer to
 223 Question 3 is then: Clouds have a destabilizing influence on the longwave feedback. How-
 224 ever, the structure of all-sky feedback looks similar to clear-sky feedback, implying that
 225 the RH-dependence from clear-sky effects still dominate the meridional structure.

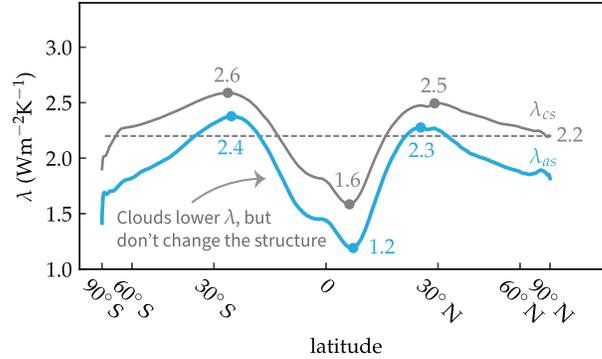


Figure 5. Incorporating clouds into the longwave feedback. Zonal-mean all-sky feedback (λ_{as} , blue) is diagnosed from zonal-mean clear-sky feedback (λ_{cs} , gray) and zonal-mean cloud-top fraction f . See Equation 4 for details. Note the equal-area scaling of the x-axis.

3 Discussion

Our work can be summarized as follows:

1. At high temperatures, variations in RH are sufficient to close the H₂O window, driving deviations in λ_{cs} from the typical value of $2.2 \text{ Wm}^{-2}\text{K}^{-1}$ (Figure 1).
2. Furnaces and radiator fins can be interpreted as tropical extrema in zonal-mean λ_{cs} as a consequence of the RH-dependence (Figure 3).
3. Cloud radiative effects can be estimated with a simple equation to reconstruct the all-sky OLR (Figure 4), which we then use to estimate the all-sky feedback. Clouds lower the feedback relative to clear skies, but the RH-dependence of the feedback is still significant (Figure 5).

3.1 Comparison to other work

We have demonstrated a reason for why a large contrast in λ_{cs} emerges in the tropics. However, Zhang et al. (2020) analyzed GCMs and suggested that the dip in zonal mean λ_{cs} to $1 \text{ Wm}^{-2}\text{K}^{-1}$ in their study results from local column RH increases. Column RH is fixed in our study and yet we still get a significant tropical dip in λ_{cs} to $1.6 \text{ Wm}^{-2}\text{K}^{-1}$. Therefore, this suggests that climatological RH is as important as local RH changes in GCMs in causing tropical deviations from the global mean value of $\lambda_{cs} \approx 2.2 \text{ Wm}^{-2}\text{K}^{-1}$.

Our results for the zonal-mean feedback cannot be directly compared to other studies of zonal mean feedback (e.g. Feldl and Roe (2013a, 2013b); Armour et al. (2013)) for two reasons. The first is that our λ_{cs} is not equal to the sum of the Planck, Lapse-Rate, and q_v feedbacks, because these feedbacks include “cloud climatological effects” (Yoshimori et al., 2020), i.e. these feedbacks are calculated in the presence of clouds from the control simulation. Furthermore, our λ_{as} is also not equal to this sum of conventional feedbacks, because those feedbacks fix the cloud pressure, whereas we fix the cloud temperature. These issues were discussed in detail by Yoshimori et al. (2020), and our λ_{as} should be comparable to their T-FRAT feedback in which the RH and cloud temperatures are fixed. Further work could explicitly explore such comparisons.

Our new understanding of the state dependence of λ_{cs} gives context to previous results. For example, Meraner et al. (2013); Bloch-Johnson et al. (2021) attributed an increase in equilibrium climate sensitivity to the decrease in λ_{cs} with warming. We ex-

257 pect these variations in λ_{cs} to be enhanced in climates hotter than present-day Earth
 258 and conversely to be suppressed in climates cooler than present-day Earth. Our partic-
 259 ular calculation of the λ_{cs} phase space assumed that the CO₂ concentration is fixed at
 260 340 ppmv, which neglects the increasingly important role of CO₂ in stabilizing the cli-
 261 mate at high CO₂ concentrations (Seeley & Jeevanjee, 2020). However, the strength in
 262 our approach of studying the joint dependence of λ_{cs} on T_s and RH is its generality, for
 263 our approach can not only be applied to our present-day climate, but to past climates
 264 like the Eocene, Pliocene, and Last Glacial Maximum, and to future climates predicted
 265 from different RCP scenarios.

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267 ERA5 data is available from <https://doi.org/10.24381/cds.bd0915c6>. Data from
 268 the PyRADS calculations are available from [https://www.dropbox.com/sh/vam6f6t7vvyj74x/
 269 AAAZtYqz-SbaIvvjrzt81_Wra?dl=0](https://www.dropbox.com/sh/vam6f6t7vvyj74x/AAAZtYqz-SbaIvvjrzt81_Wra?dl=0) and will be available in a Zenodo repository upon
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Figure 1.

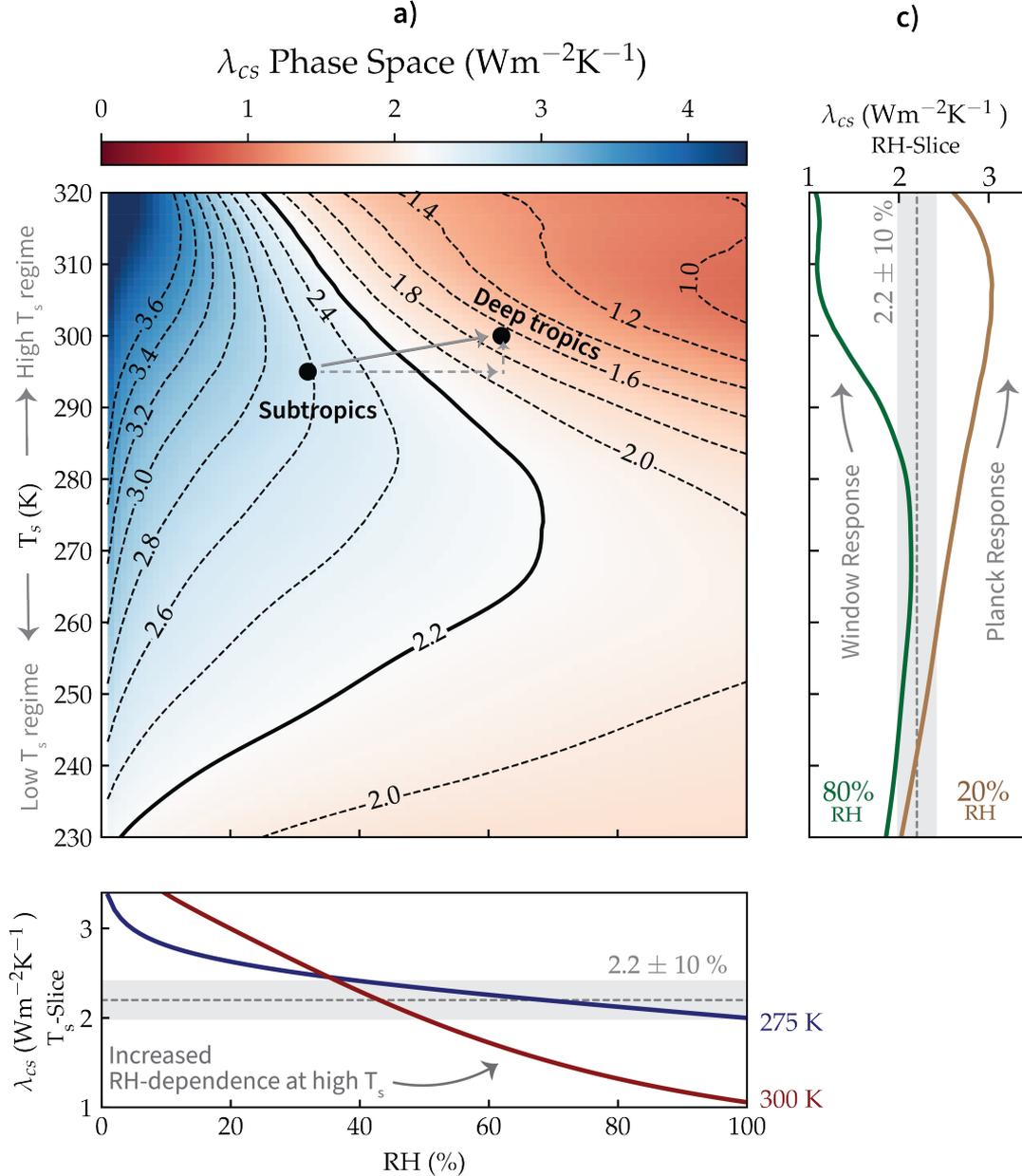


Figure 2.

— RH=12.5 % — 25 % — 50 % — 100 %

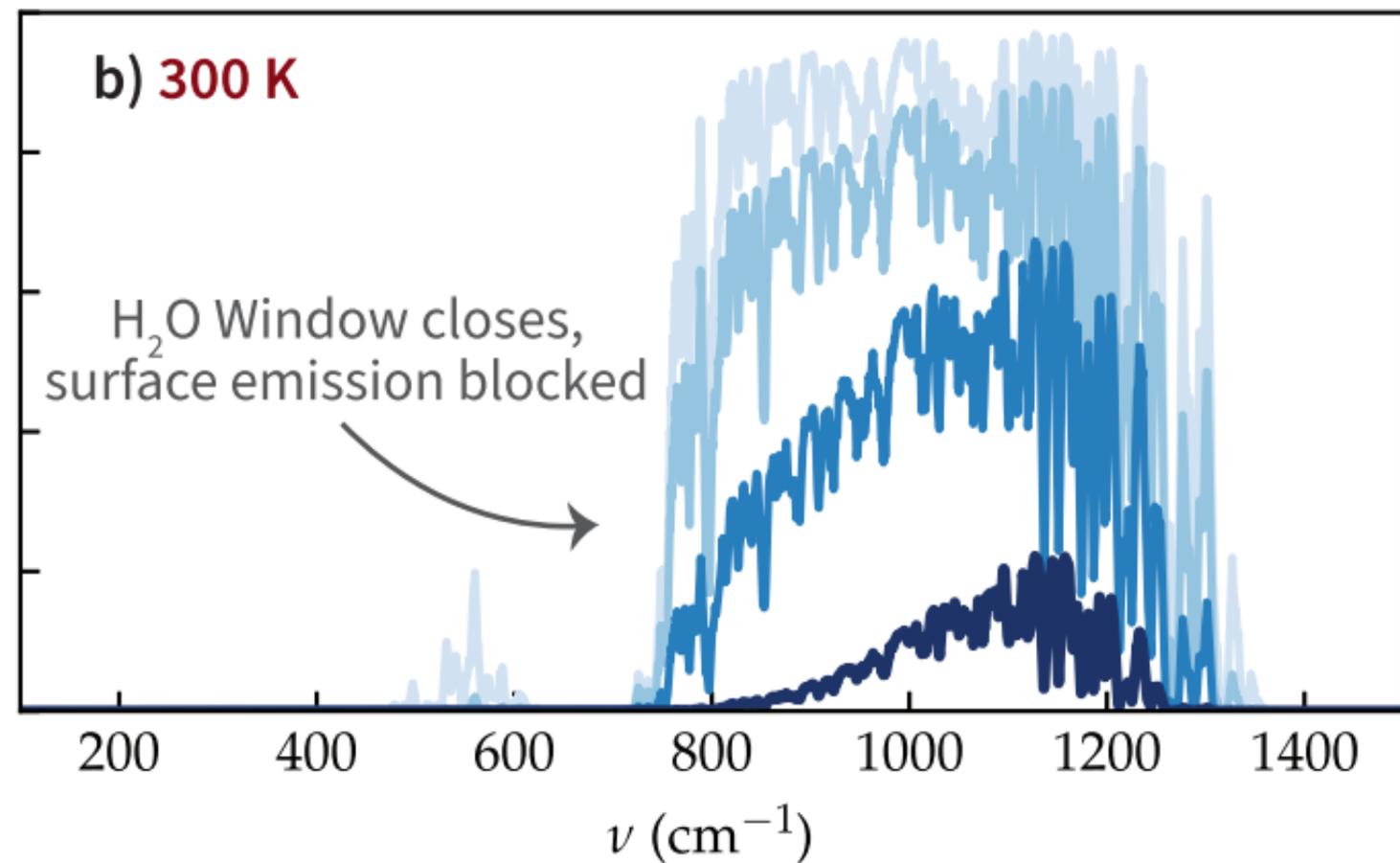
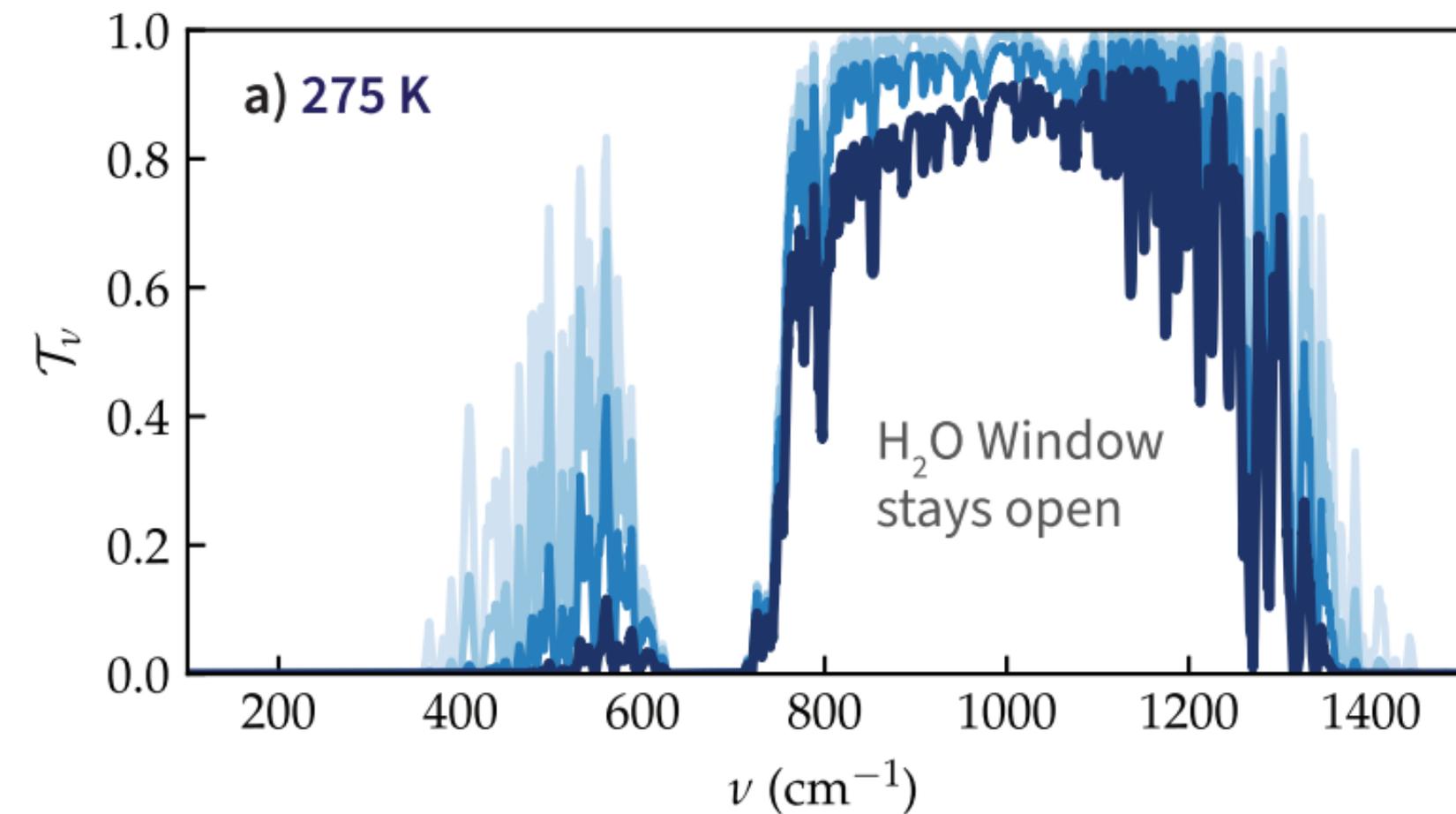


Figure 3.

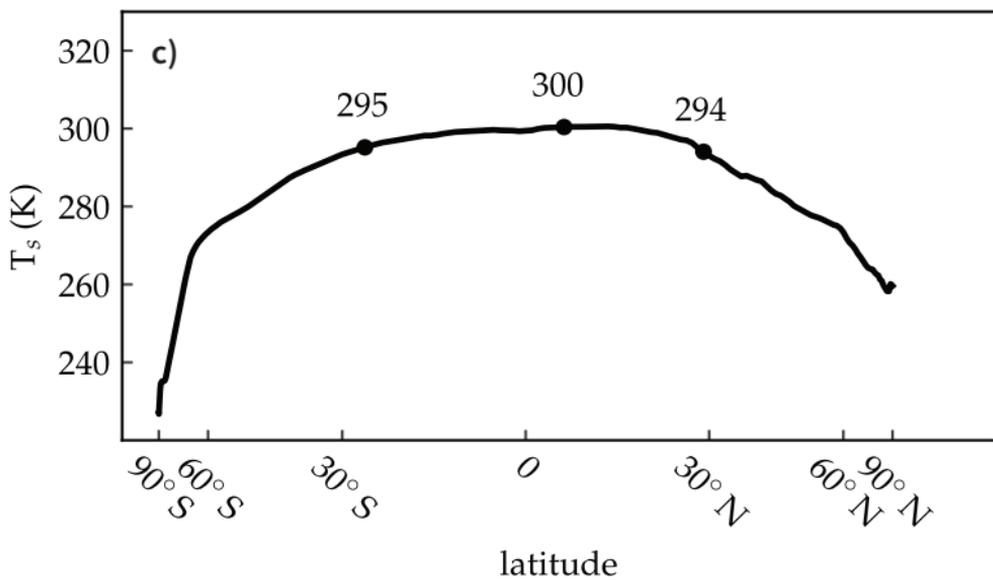
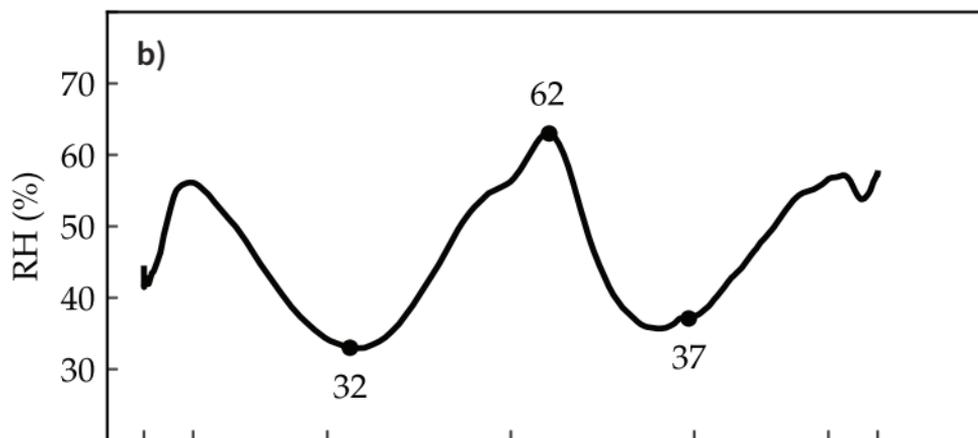
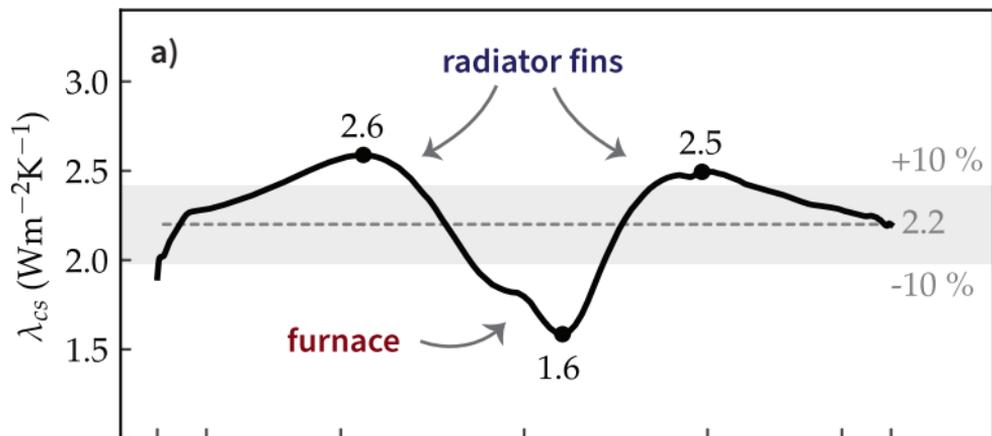


Figure 4.

cloud-top emission

 f \times σT_{ct}^4 $+$

clear-sky emission

 $(1 - f) \text{OLR}_{cs}$ \approx

all-sky emission

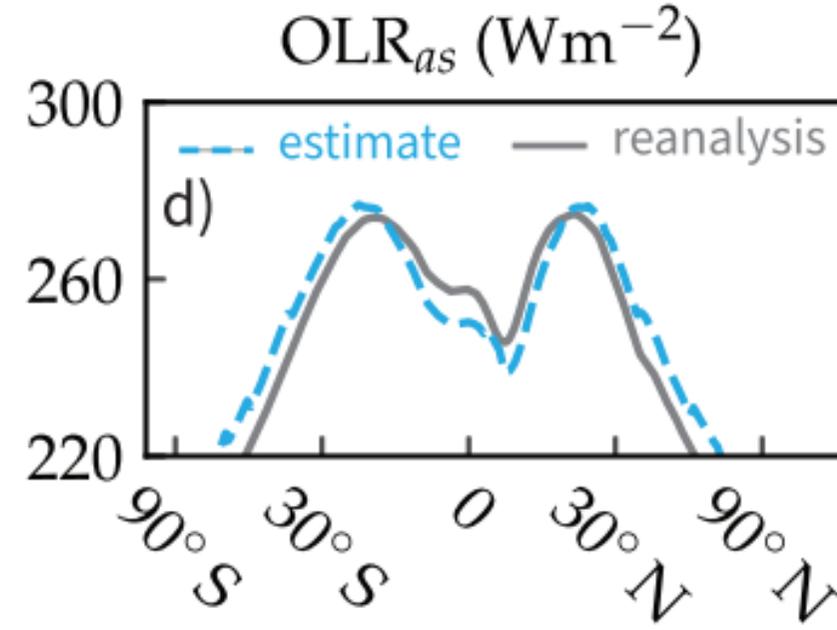
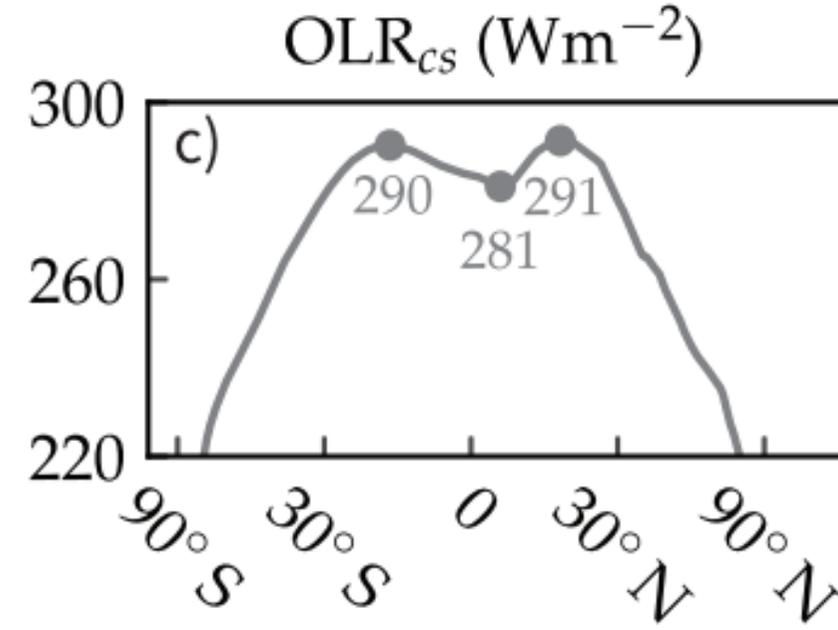
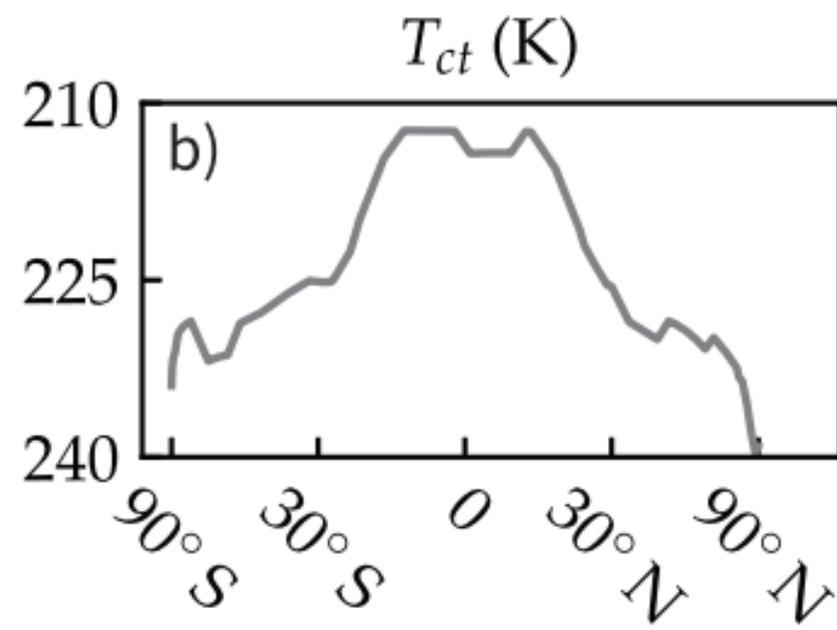
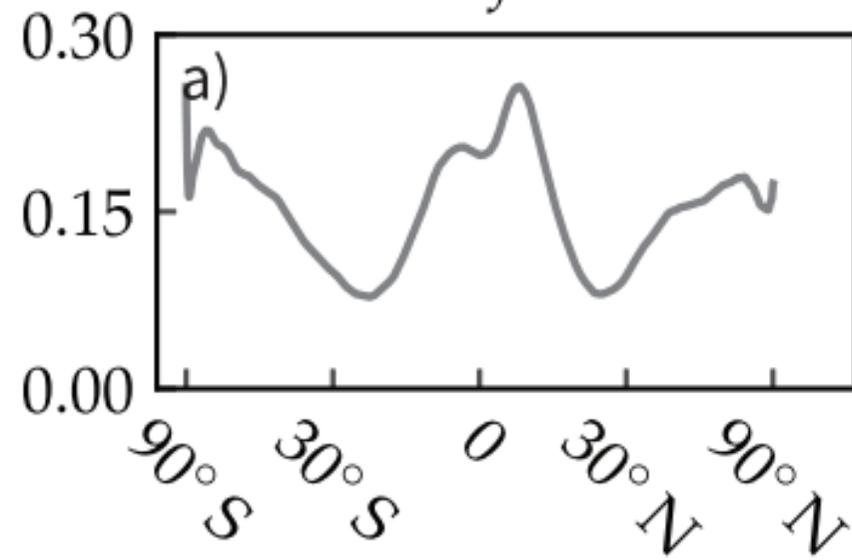
 OLR_{as} 

Figure 5.

