

# Broadband Infrasond Signal of a Collapsing Glacier

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## Abstract

A major ice collapse (20.000 m<sup>3</sup>) from a hanging glacier on Mount Eiger, Switzerland was recorded by a small aperture array as a broadband (0.1-10 Hz) infrasond signal. Array analysis reveals that the high ( $\sim 3$  Hz) frequency signal is infrasond produced by the moving ice mass, and its back-azimuth variation with time tracks the ice mass trajectory and provides a mean velocity estimate. Infrasond frequency is used to estimate a radius, that is in good agreement with the volume estimate from field observations. The low ( $\sim 0.1$  Hz) frequency oscillation is modeled in terms of the velocity field (wind), which the moving ice mass induces on the surrounding air, producing pressure variations at the different elements. These results show how infrasond array observations may provide quantitative information of glacier collapse and ice avalanche volume. This opens new perspectives for monitoring avalanching glaciers and providing warning for break-off events.

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## Key Points:

- Glacier collapse is recorded as a broadband infrasonnd signal.
- Array analysis allows to detect the high ( $>1\text{Hz}$ ) frequency component and derive velocity and trajectory.
- The low ( $<1\text{ Hz}$ ) frequency component is interpreted as air flow around the moving ice mass.

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## Abstract

A major ice collapse ( $\approx 20,000 \text{ m}^3$ ) from a hanging glacier on Mount Eiger, Switzerland was recorded by a small aperture array as a broadband (0.1-10 Hz) infrasound signal. Array analysis reveals that the high ( $\approx 3 \text{ Hz}$ ) frequency signal is infrasound produced by the moving ice mass, and its back-azimuth variation with time tracks the ice mass trajectory and provides a mean velocity estimate. Infrasound frequency is used to estimate a radius, that is in good agreement with the volume estimate from field observations. The low ( $\approx 0.1 \text{ Hz}$ ) frequency oscillation is modeled in terms of the velocity field (wind), which the moving ice mass induces on the surrounding air, producing pressure variations at the different elements. These results show how infrasound array observations may provide quantitative information of glacier collapse and ice avalanche volume. This opens new perspectives for monitoring avalanching glaciers and providing warning for break-off events.

## 1 Introduction

Rapid alpine mass movements such as ice or rock avalanches, rock falls and debris flows constitute severe natural hazards. They threaten human lives and infrastructure and are expected to increase with ongoing climate change and population pressure forcing settlements into exposed terrain [Field *et al.*, 2014]. Consequently, monitoring and early warning systems, which help mitigate the threat and impact of mass movements are a key component of hazard management in mountainous regions worldwide.

Recently, glacier collapses have caught particular attention of scientists and stakeholders. The twin collapses of two Tibetan glaciers in 2017 were a sudden reminder that climate change may produce glacial hazards in new places and with unexpected dimension [Kääb *et al.*, 2018]. In Europe, costly monitoring programs have also highlighted changing glacial hazards: Glacial retreat produces new and potentially unstable ice geometries, and warming atmosphere and mountain faces change the thermal regime of already unstable ice [Raymond *et al.*, 2003; Faillettaz *et al.*, 2011b, 2015; Preiswerk *et al.*, 2016]. The latter mechanism implies that hitherto cold based ice cover frozen to steep mountain faces (“hanging glaciers”) may warm towards a temperate basal regime leading to sliding instabilities [Preiswerk *et al.*, 2016]. With most unstable ice collapses happening unnoticed, the number of well documented events is small, which complicates systematic studies of break-off activity in relation to climatic factors. Instead, successful

44 early warning still relies on experienced observers identifying unstable ice and subsequent  
45 monitoring.

46 Several studies showed that failure time of unstable ice can often be predicted be-  
47 cause major break-off events are typically preceded by an acceleration of the ice surface  
48 [*Faillietaz et al.*, 2015]. High resolution photogrammetry and ground based interferom-  
49 etry (GBInSAR) [*Meier et al.*, 2016] reliably capture such acceleration, albeit at the cost  
50 of sophisticated and expensive instrument deployment, targeting only a small and pre-  
51 defined glacier region. In search of more affordable monitoring methods, researchers have  
52 turned to seismic techniques, which detect ground unrest in response to ice failure, avalanche  
53 propagation and even precursory englacial damage growth [*Dalban Canassy et al.*, 2012,  
54 2013; *Faillietaz et al.*, 2011a; *Pralong et al.*, 2003; *Faillietaz et al.*, 2015]. Unfortunately,  
55 microseismicity near glaciers tends to mask signals related to ice break-off and to date  
56 volumes of unstable or detaching ice seracs cannot be estimated from seismic data alone.

57 Analogous to seismic waves, mass movements induce elastic waves in the atmosphere,  
58 which can be recorded in the infrasonic range typically taken as frequencies below 20 Hz.  
59 Snow avalanches [*Naugolnykh and Bedard*, 1990], rockfalls [*Johnson and Ronan*, 2015]  
60 and debris flows [*Allstadt et al.*, 2018; *Marchetti et al.*, 2019] have thus been studied with  
61 infrasound measurements. Although infrasound sensors are less sensitive to failure pre-  
62 cursors, rapid detection for hazard mitigation is in principle possible. For example, in-  
63 frasound detections could be used to monitor snow avalanches and debris flows in order  
64 to alert people in affected terrain and trigger road closures [*Marchetti et al.*, 2015; *Schim-*  
65 *mel et al.*, 2018; *Marchetti et al.*, 2019].

66 So far, relatively little research has focused on infrasound monitoring of glacier break-  
67 off events and resulting ice avalanches. With the help of standard array methods, even  
68 weak and distant infrasound recordings can detect and locate ice break-off events [*Preiswerk*  
69 *et al.*, 2016]. However, it is not clear which other types of information are contained in  
70 the infrasound signature of glacier break-off events and resulting ice avalanches. In par-  
71 ticular, volume estimates and flow velocities of ice avalanches which are key for early warn-  
72 ing or rapid response measures have yet to be extracted from infrasound recordings of  
73 glacier break-off events.

74 In this study we present an infrasound analysis of a break-off from the hanging glacier  
75 at Mount Eiger, Switzerland. We show that the infrasound signature is surprisingly broad-

76 band containing low-frequency (0.1 Hz) pressure oscillations in addition to signals around  
77 3 Hz, which are of the kind that has been used in previous mass movement studies. We  
78 model the low-frequency signals as pressure variations, induced by the flow of air around  
79 the moving avalanche mass. The combination of the various signal components provides  
80 good constraints on ice avalanche location, trajectory, velocity and volume.

## 81 **2 Hanging Glacier on Mount Eiger, Switzerland**

82 The hanging glacier is located at an elevation of around 3400 m above sea level on  
83 the west face of Mount Eiger in the Swiss Alps. The glacier is partly frozen to its bedrock  
84 with the presence of temperate zones [Margreth *et al.*, 2017; Faillettaz *et al.*, 2015]. Lo-  
85 cated above steep slopes, the glacier produces periodic break-off events in form of ice serac  
86 collapses from the 200 m wide and 30 m thick front, leading to ice avalanches that are typ-  
87 ically  $<10,000\text{ m}^3$  [Margreth *et al.*, 2017]. The collapses are driven by gravity and oc-  
88 cur upon significant englacial damage growth at a point when the ice can no longer sus-  
89 tain its weight [Faillettaz *et al.*, 2015]. Glacier front stability is controlled mostly by an  
90 average ice velocity at the glacier front of 7 m/y producing a yearly ice flux of 40,000  
91  $\text{m}^3$  through the frontal flux gate whose area is  $6,000\text{ m}^2$  [Margreth *et al.*, 2017].

92 Given negligible surface melt, collapse events balance the ice flux, resulting in ice  
93 release events with volumes ranging between 1,000 and  $100,000\text{ m}^3$ . An ice collapse of  
94  $100,000\text{ m}^3$  occurred on 20 August 1990 [Pralong and Funk, 2006]. If the basal thermal  
95 regime of the hanging glacier changes in response to bedrock warming and latent heat  
96 transfer, break-off failures significantly larger than  $100,000\text{ m}^3$  [Margreth *et al.*, 2017] may  
97 occur without any clear precursor events [Faillettaz *et al.*, 2011b].

98 Ice avalanches detaching from the hanging glacier front flow over 400 meters through  
99 a steep gully before entering a wider area covered with snow and ice debris produced by  
100 avalanches and previous ice collapses. Depending on this pre-existing snow cover, entrain-  
101 ment may enhance runout and the destructive potential of break-off events. At lower el-  
102 evations, the rocky Rotstock Ridge emerges 55-110 m above its surrounding terrain, break-  
103 ing and deflecting the avalanche flow southwest. This counter clockwise deflection of the  
104 flow to some extent shields the Eigerletscher train station (Figure 1). However, the train  
105 station is likely exposed to larger events that include substantial entrainment of pow-  
106 der snow [Margreth *et al.*, 2017].

### 3 Instrumentation and data

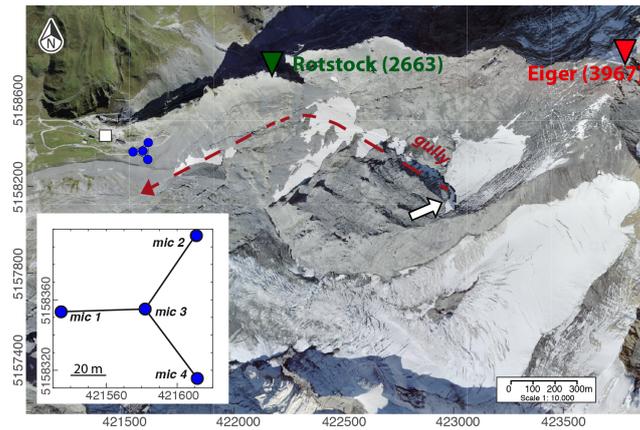
An infrasound array was deployed at an elevation of  $\approx 2300$  m, near the station Eigergletscher of the Jungfrauoch Railway (Figure 1). The main front of the hanging glacier locates  $\approx 1.4$  km East of and 900 m above the array.

The infrasound array was equipped with four PRS0100a pressure sensors by Item s.r.l., with a sensitivity of 25 mV/Pa in the pressure range of  $\pm 100$  Pa and frequency response between 0.02 and 100 Hz. The four sensors of the array were deployed with a triangular geometry (Figure 1), with one sensor in the center co-located with a Guralp CMG/DM24 digitizer. Maximum distance between two elements of the array was  $\approx 60$  m. Infrasound data provided by each array element were digitized at 24 bits and 100 Hz, GPS time stamped, recorded locally and made available through TCP/IP with a 3G modem. The pressure sensors were installed in plastic containers that were buried in the ground and covered with stones to reduce wind noise and increase the signal to noise ratio. Near the infrasound array, an interferometric radar was installed to predict break-off events via detection of unusual ice front velocities [Margreth *et al.*, 2017].

### 4 Serac Collapse on 29 May 2017

On May 29, 2017, a substantial serac collapse occurred from the hanging glacier at 03:45 UTC (Figure 2). The collapse was preceded by an acceleration of parts of the ice front to nearly 200 mm per day. The radar image showed that the unstable serac covered an area about 10% larger than the equivalent  $200\text{ m}^2$  surface area of the 12 April 2016 break-off documented in Margreth *et al.* [2017] (Figure S1). Assuming that pervasive crevasses leading to serac separation develop 40-50 m behind the ice front [Pralong *et al.*, 2003] yields a volume estimate of  $8'800\text{--}11'000\text{ m}^3$ . Direct ground-based and airborne field observations estimated a volume between  $20'000$  and  $30'000\text{ m}^3$ . Whereas the field observations cannot be reproduced, they were likely more accurate than volume estimate based on radar-derived serac area and expected crevasse location. We therefore conclude that the collapse volume was around  $20'000\text{ m}^3$ .

The collapsing serac fell nearly vertically for  $\approx 600$  m within the east-west gully and eventually turned counter-clockwise behind Rotstock Ridge before it continued moving downhill in a more or less straight line (red dashed line in Figure 1). The powder cloud reached the buildings of the Eigergletscher train station next to the infrasound an-

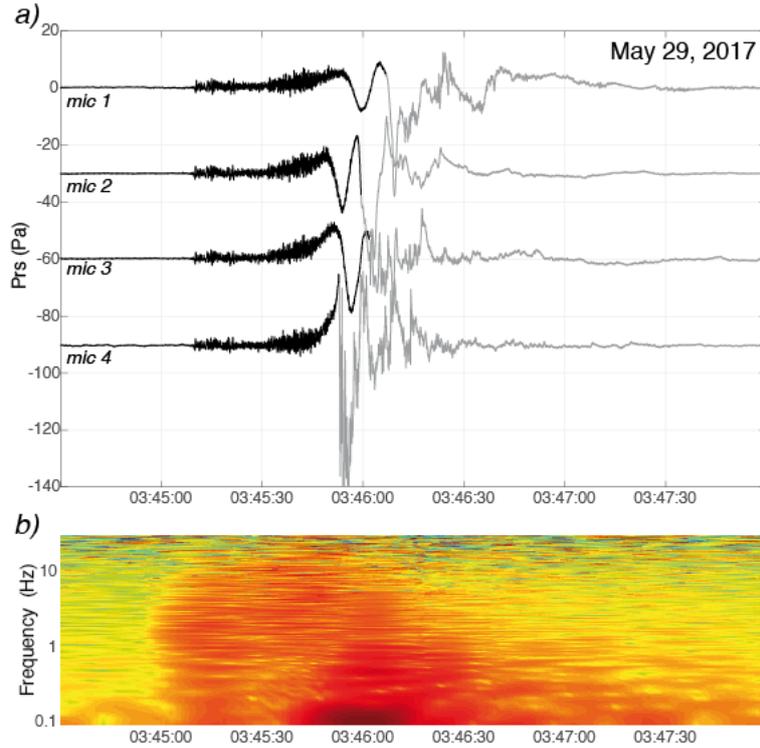


122 **Figure 1.** Location of the infrasound array (blue dots), positioned nearby the Eigergletscher  
 123 train station (white square), and of the avalanching front (with arrow) of the hanging glacier on  
 124 Mount Eiger. The location of Mount Eiger (reversed red triangle) and the Rotstock Ridge (re-  
 125 versed green triangle) peaks is marked for reference. Detached ice lamellas typically flow within a  
 126 narrow gully before being deflated anti-clockwise by the Rotstock Ridge (red dashed arrow). The  
 127 geometry of the four elements of the array is shown in the inset. Spot image reproduced by  
 128 ©/with permission/2020 swisstopo (JD100042).

145 tenna and material partly covered the infrasound array. Sensor four (Figure 1, inset), in  
 146 particular, was covered by snow and ice blocks.

150 The event was clearly recorded by the infrasound array at 03:45:10 UT, as a long-  
 151 lasting ( $\approx 150$  sec), large amplitude ( $> 70$  Pa peak-to-peak), broadband signal (Figure  
 152 2). Higher frequency signals, peaking around 2.5-3 Hz extend to well above 10 Hz. These  
 153 signals are super-imposed on a low-frequency oscillation, peaking around 0.1 Hz (Fig-  
 154 ure 2b).

155 The high frequency energy is most visible during the first part of the signal, until  
 156 03:45:55. The low frequency signal starts as a smooth pressure increase around 03:45:35,  
 157  $\approx 25$  seconds after the high frequency signal onset was recorded at the array and within  
 158 a few seconds it begins to dominate the entire spectrum. The low frequency oscillations  
 159 reach a first positive peak of  $\approx 10-15$  Pa, within 18-23 seconds of their onset (Figure 2a).  
 160 This low frequency oscillation is dispersive, showing a different frequency content at the  
 161 different elements of the array. Peak frequency, measured as the inverse of the time dif-



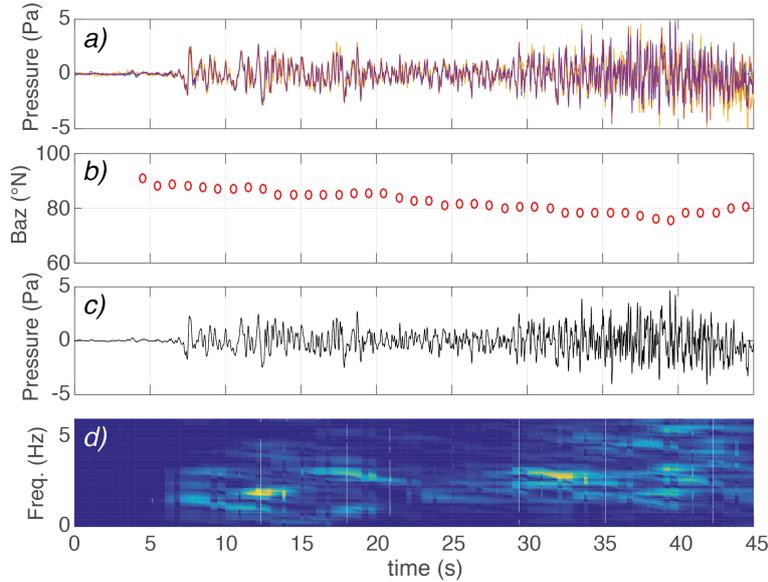
147 **Figure 2.** Infrasonic record of the collapse at the 4 elements of the array (a). The signal is  
 148 colored in gray once the spurious phase is recorded. (c) Spectrogram of the signal recorded by  
 149 sensor 2 showing a main peak around 0.1 Hz preceded by a higher frequency (3 Hz) phase.

162 difference between the two positive peaks, decreases from 0.11 Hz (9 seconds time differ-  
 163 ence) for mic 2, down to 0.085 Hz (11.6 seconds time difference) for mic 1. Moreover,  
 164 the low frequency signal is marked by large time delays at the different array elements  
 165 ( $\approx 6$  seconds between mic1 and mic2 and  $\approx 2.5$  seconds between mic2 and mic3), with  
 166 the signal first recorded at sensor 2. Considering the small aperture ( $\approx 85$  m) of the ar-  
 167 ray, these delays are consistent with a propagation velocity of a few tens of m/s, well be-  
 168 low the propagation velocity of sound.

169 The waveforms show a third spurious phase (gray in Figure 2). The timing of this  
 170 phase varies across the array. It is first recorded at 03:45:52 UT, before the first posi-  
 171 tive peak of the low frequency oscillation was reached, at sensor 4, and eventually, 15 sec-  
 172 onds afterwards at 03:46:07 UT, at sensor 1. We attribute this spurious phase to avalanche  
 173 debris depositing on the sensors.

## 174 5 Array Analysis of High-Frequency (3 Hz) Signals

175 In order to interpret the initial, high-frequency (3 Hz) infrasonic signal generated  
 176 as the ice avalanche approaches the antenna, we perform coherence analysis of infrasound  
 177 data recorded at the 4 array elements (Figure 3a). We apply cross-correlation analysis  
 178 in discrete time windows of 5 second with 4 second overlap to 1-10 Hz band-pass filtered  
 179 infrasound data. Once coherent signals are observed throughout the array, we evaluate  
 180 time delays among the array elements following *Ulivieri et al.* [2011]. This gives prop-  
 181 agation back-azimuth (Figure 3b) of the infrasound ray and allows calculation of the stacked  
 182 signal along the beam (Figure 3c) as the sum of broadband (0.1-25 Hz) infrasound data  
 183 recorded at the 4 array elements and shifted according to calculated propagation back-  
 184 azimuth. In this way, we strongly reduce the noise and enhance the waveform charac-  
 185 teristics. Although the stacked waveform is obtained from the broadband infrasound record,  
 186 spectral analysis of stacked waveforms clearly points out a narrow frequency component  
 187 peaking between 2.5 and 3 Hz (Figure 3d).



188 **Figure 3.** Amplitude (Pa at the array) of the recorded signal band-pass filtered between .1  
 189 and 25 Hz, a). Back azimuth (b) of infrasound detections. Stacked waveform along the beam (c)  
 190 and corresponding PSD (d). Timing is expressed as seconds after 3:45 UTC.

191 Back-azimuth  $Baz$  identifies the direction of infrasound propagation and in our case  
 192 defines a vector pointing from the infrasound antenna towards the moving avalanche front.

193 Back-azimuth is marked by a constant decrease from 90 degrees north to 75 degrees north,  
 194 before the trend changes and a slight increase up to 82 degrees north is observed (Fig-  
 195 ure 3b). Considering the topography between the glacier front and the array, the observed  
 196 variation of the back-azimuth is consistent with the ice mass flowing downhill within the  
 197 gully to eventually turn anti-clockwise behind the Rotstock Ridge (Figure 1).

198 The temporal changes of back-azimuth can be used to obtain an estimate of the  
 199 downhill velocity of the ice/snow mass. We assume the first detection, pointing at 90 de-  
 200 grees North, to be consistent with the rupture time at the front of the glacier. We as-  
 201 sume the detection with the minimum back-azimuth of 75 degrees north, that is reached  
 202 35 seconds after the onset, to reflect the timing when the collapsing ice mass hits the Rot-  
 203 stock Ridge, where the direction of the gully changes from North-Westward ( $\approx 290$  de-  
 204 grees N) South-Westward ( $\approx 235$  degrees N). With this assumption, the avalanche trav-  
 205 els a distance of  $\approx 1$  km between the front and the deflection point (Figure 1) in ca. 35  
 206 seconds. This corresponds to a mean velocity of  $\approx 28$  m/s. During this phase, recorded  
 207 infrasound is characterized mostly by the high frequency component and by a smooth  
 208 increase of pressure at all the sensors before the ice mass reaches the array. Our anal-  
 209 ysis thus confirms that the recorded high frequency signal, that is highly coherent across  
 210 the four array elements and tracked clearly with a variable back-azimuth, is produced  
 211 by the collapsed mass rapidly moving downhill.

212 In order to interpret the high-frequency (3 Hz) initial infrasonic signal generated  
 213 as the ice avalanche approaches the antenna we approximate the avalanche volume as  
 214 a moving sphere [*Naugolnykh and Bedard, 1990*]. Its kinetic energy is partially transferred  
 215 into infrasonic wave energy as the avalanche motion perturbs atmosphere pressure. The  
 216 dominant frequency of the sound wave scales with the inverse of the sphere size: [*Nau-*  
 217 *golnykh and Bedard, 1990*]:

$$218 \quad f = c/\pi D, \quad (1)$$

219 where  $c$  is the velocity of sound in the atmosphere while  $D$  is the diameter of the  
 220 sphere. For the 29 May 2017 collapse with a dominant infrasonic frequency of 2.5-3 Hz  
 221 (Figure 3 d) and an assumed sound propagation velocity of 330 m/s, eq 1 predicts a mov-  
 222 ing sphere diameter  $D$  of  $\approx 35$ -42 m corresponding to a sphere volume between 22,000

223 and  $38,000 m^3$ . This result is in good agreement with the value of  $20,000 m^3$  estimated  
 224 from the radar images and direct field observation described above.

## 225 **6 Modeling the Low Frequency (0.1 Hz) Oscillation**

226 Lack of coherence inhibits application of array techniques to the signal below 1 Hz  
 227 (Figure 2 b). We propose that the low frequency (0.1 Hz) pressure oscillations are a man-  
 228 ifestation of air streaming around the moving avalanche mass. Approximating the avalanche  
 229 mass again as a rigid sphere, the behavior of the fluid is controlled by the Reynolds num-  
 230 ber ( $\Re$ ), defined as:

$$231 \quad \Re = Dv\rho/\mu, \quad (2)$$

232 where  $D$  is the diameter of the sphere, estimated above from the dominant  $> 1$  Hz  
 233 frequency to be  $\approx 35$ - $42$  m,  $v$  is its velocity, inferred to be  $\approx 20$ - $40$  m/s, and  $\rho$  and  $\mu$  are  
 234 the density and viscosity of air, that we assume here as  $1.3 kg/m^3$  and  $1.7 \times 10^{-5} Pa \cdot$   
 235  $s$  for external temperature of 0 degree C. The corresponding  $\Re$  is on the order of  $10^7$ ,  
 236 thus satisfying the assumptions for an ideal fluid ( $\mu \rightarrow 0, \Re \rightarrow \infty$ ).

237 The problem can be described as an inviscid flow, with no boundary layer and no  
 238 viscous wake downstream the sphere. In this case, the air flow around the sphere is a  
 239 potential flow, where the velocity field ( $\mathbf{v}$ ) is a laminar field with no vorticity and is fully  
 240 described analytically by its radial ( $v_r$ ) and tangential ( $v_\theta$ ) components [*Landau and Lif-*  
 241 *shitz, 1959*]:

$$242 \quad v_r = v \left( \frac{R_S^3}{r^3} \right) \cos \theta \quad (3)$$

$$243 \quad v_\theta = v \left( \frac{R_S^3}{r^3} \right) \sin \theta \quad (4)$$

244 where  $v$  is the velocity of the sphere,  $R_S$  is the sphere radius,  $r$  is the radial coor-  
 245 dinate, with  $r=0$  at the barycenter of the sphere, and  $\theta$  represents the angular coordi-  
 246 nate, for which  $\theta=0$  in the direction of the motion of the sphere. Both equations are de-  
 247 fined only when  $r > R_S$ . Both radial (eq. 3) and tangential (eq. 4) velocity components  
 248  $\rightarrow 0$  with increasing distance ( $r$ ) from the sphere.

249 According to equations (3 and 4), air molecules located along the trajectory of the  
 250 sphere ( $\theta=0$ ) have only a radial velocity component, that is positive in front of the sphere  
 251 (i.e. air is pushed ahead by the sphere), while it is negative behind (i.e. air is pulled by  
 252 the moving sphere). For all other positions, the air velocity field is characterized by both  
 253 radial and tangential components, resulting in air flow streamlined around the sphere  
 254 (Figure 4).

255 For each array element and following equations 3 and 4, we calculate the velocity  
 256 field of air resulting from the avalanche motion (Figure 4a, b). We assumed a sphere of  
 257 radius ( $R_S$ ) of 20 m, in agreement with the diameter  $D$  of  $\approx 35$ -42 m estimated from the  
 258 frequency of recorded infrasound (eq 1). The sphere moves with a velocity ( $v$ ) of 28 m/s  
 259 and along the collapse trajectory shown by the red dashed arrow in Figure 1 and cal-  
 260 culated from temporal back-azimuth variations (Figure 2 c).

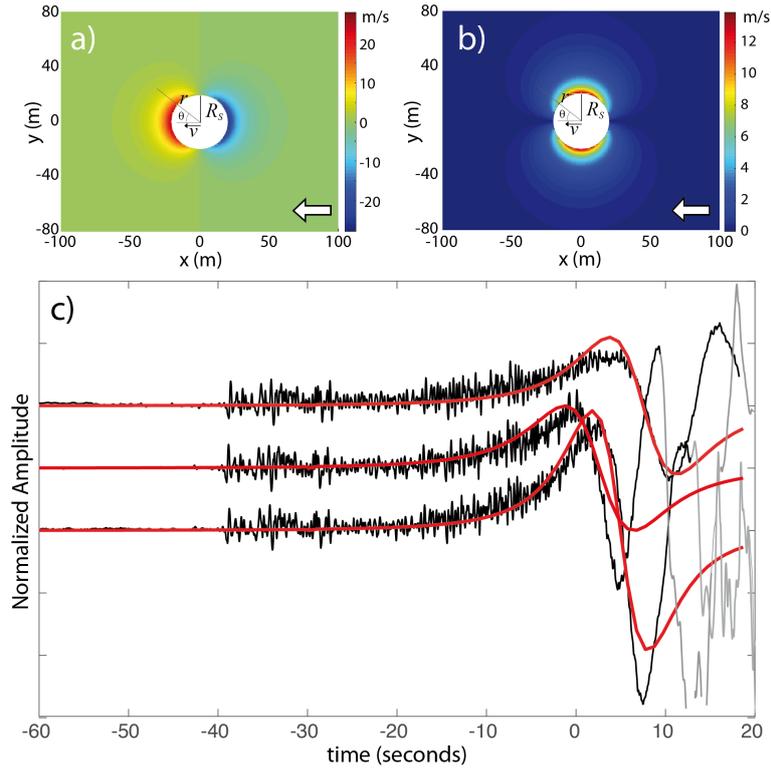
268 The velocity field  $\mathbf{v}$  (Figure 4a, b), given by equations 3 and 4, is characterized by  
 269 a non-zero gradient ( $\nabla\mathbf{v} \neq 0$ ), which means that the velocity is not constant around  
 270 the sphere. Therefore, considering a unit volume  $V$ , identified by the closed surface  $S$ ,  
 271 at a given position nearby the sphere, influx air velocity will differ from efflux air veloc-  
 272 ity, thus resulting in  $\Phi_S(\mathbf{v}) \neq 0$ . This will produce, within the unit volume and in a  
 273 unit time, a net air flux resulting in a change in the number ( $n$ ) of air moles and thus,  
 274 according to the ideal gas equation, in a change of pressure ( $P$ ):

$$275 \quad P = \frac{nRT}{V} \quad (5)$$

276 where  $V$  is the gas volume,  $R$  is ideal gas constant and  $T$  is the absolute temper-  
 277 ature, that are all assumed as constant. The flux of the velocity field ( $\Phi_S(\mathbf{v})$ ) is thus pro-  
 278 portional to the net air flux and, hence, to the pressure. A quantity, which is propor-  
 279 tional to the expected pressure  $P$  at each array element is therefore obtained from the  
 280 flux of the calculated velocity field ( $\Phi_S(\mathbf{v})$ ) via the volumetric integral of  $\nabla \cdot \mathbf{v}$  and by  
 281 applying the divergence theorem:

$$282 \quad \Phi(\mathbf{v}) = \int_V \nabla \cdot \mathbf{v} dV \quad (6)$$

283 Figure 4c shows the comparison of raw infrasound data and modeling results. Am-  
 284 plitudes are normalized as the velocity flux ( $\Phi_S(\mathbf{v})$ ) has been calculated with equation



261 **Figure 4.** Radial  $v_r$  (a) and tangential  $v_\theta$  (b) components of the inviscid flow induced by the  
 262 moving sphere in surrounding air. The white arrow shows the sphere movement direction. Com-  
 263 parison (c) between the recorded infrasound pressure (black) and the modeled pressure at the  
 264 array (red). Recorded waveforms are colored in gray after the spurious signal is recorded. Wave-  
 265 forms are normalized and aligned in time, according to the amplitude and timing of the positive  
 266 peak of the second element of the array (mic2). Comparison is limited to the first 3 elements of  
 267 the array were at least the first positive peak of the low frequency oscillation is fully recorded.

285 6 only on the plane passing through the barycenter of the sphere, whereas 3D contribu-  
 286 tions should be considered. Moreover, the relationship between  $\Phi_S(\mathbf{v})$  and the air quan-  
 287 tity was not quantified in our proposed framework.

288 The timing of maximum amplitude of the low frequency (0.1 Hz) oscillation at dif-  
 289 ferent array elements coincides with the instant when the axis connecting the sphere's  
 290 barycenter and the array element is at  $\theta=90$  degrees with respect to the sphere's mov-  
 291 ing direction (Figure 4c). At that point the radial velocity turns negative and the tan-  
 292 gential velocity starts to decrease (Figure 4c) leading to a decrease of the modeled ve-  
 293 locity flux.

## 7 Discussion and Conclusion

The infrasound array records of this major ice collapse ( $\approx 20.000 \text{ m}^3$ ) from the front of the hanging glacier on Mount Eiger, Switzerland, allowed to investigate the nature of infrasound energy radiation from a falling ice mass and to evaluate the potential of infrasound array analysis to monitor avalanching glaciers.

We confirmed that a glacier collapse is an efficient source of infrasound waves, that once tracked by an array allow to evaluate the trajectory of the falling ice mass, and whose peak frequency is proportional to the ice volume. Although a more careful calibration and additional data will be required, these results highlight the potential of infrasound records to remotely estimate collapse volumes and trajectories.

Presented results show also that in certain conditions a broadband signal can be recorded, being induced by the air flux induced by the moving ice mass. Modeled and real waveforms are normalized and aligned considering the positive peak at the second element of the array (Figure 4). This allows to compare the duration, the frequency content, the relative timing and the relative amplitude of the modeled and recorded waveform. The comparison is limited to the first 3 elements of the array, where the low frequency oscillation is recorded properly. Figure 4c shows a general agreement between the recorded and modeled waveforms. The modeling reproduces the dispersive nature of the wave, the timing of the positive peaks and relative amplitude ratios. The positive peak is first recorded at sensor 2 and eventually at sensor 1, that is furthest away along the trajectory. Misfits for the signal onset might be due to the wrong assumption on the dimension and velocity of the ice collapse, the trajectory as well as the assumption of the rigid sphere instead of a mass that is likely breaking into pieces along the trajectory.

The model fails to reproduce the tail of the signal. This might result from the fact that the velocity field ( $\mathbf{v}$ ) described by the equations (3) and (4) derived for inviscid flows typically fails to reproduce the velocity field behind the sphere, as it was experimentally observed that vortices develop and the flow decouples from the sphere (d’Alambert paradox [*Landau and Lifshitz, 1959*]). Nevertheless, our simple model explains the timing, the relative amplitude and the dispersive nature of the recorded low frequency ( $< 0.1 \text{ Hz}$ ) infrasonic wave field, and explains the broadband frequency characteristics of the recorded signal. Given the rapid decrease of the amplitude of the velocity field with dis-

326 tance from the source (eq. 3 and 4) such an effect is expected primarily for data recorded  
327 near the moving source.

328 Ahead of confirming and validating the array processing results, the presented mod-  
329 eling could be used to investigate the evolution of future collapses at the hanging glacier  
330 on Mount Eiger and to understand similar signals recorded elsewhere.

331 Given the short computing time of infrasound array processing, and its efficiency  
332 to identify signals related to moving sources [Marchetti *et al.*, 2015], this could be used  
333 as an additional system to provide quantitative real-time information of hanging glacier  
334 stability.

### 335 **Acknowledgments**

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