A near-global climatology of oceanic coherent eddies

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Abstract

Ocean eddies influence regional and global climate through mixing and transport of heat and properties. One of the most recognizable and ubiquitous feature of oceanic eddies are coherent vortices with spatial scales of tens to hundreds of kilometers, frequently referred as "mesoscale eddies". Coherent mesoscale eddies are known to transport properties across the ocean and to locally affect near-surface wind, cloud properties, and rainfall patterns. Although coherent eddies are ubiquitous, their climatology, seasonality, and long-term temporal evolution remains poorly understood. Here, we examine the kinetic energy contained by coherent eddies and present the seasonal, interannual and long-term variability using satellite observations between 1993 to 2019. A total of $\scriptstyle \$ million coherent eddies. Additionally, a strong seasonal cycle is observed, with a 3-6 months lag between the wind forcing and the response of the coherent eddy field. The seasonality of the number of coherent eddies and their amplitude reveals that the number of coherent eddies responds faster to the forcing ($\scriptstyle \$ months), than the coherent eddy amplitude (which lags by $\scriptstyle \$ miss months). This seasonal cycle is spatially variable, so we also analyze their climatology in key oceanic regions. Our analysis highlights the relative importance of the coherent eddy field in the ocean kinetic energy budget, implies a strong response of the eddy number and eddy amplitude to forcing at different time-scales, and showcases the seasonality, and multidecadal trends of coherent eddy properties.

A near-global climatology of oceanic coherent eddies

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6 Key Points:

7	- Coherent eddies contain around 50% of the total surface ocean kinetic energy bud-
8	get.
9	• Seasonal cycle of the number of coherent eddies and the coherent eddy amplitude
10	reveals a 3-6 month lag to wind forcing.

• The seasonal lag between the number and the amplitude of coherent eddies suggests a role for the inverse cascade.

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13 Abstract

Ocean eddies influence regional and global climate through mixing and transport of heat 14 and properties. One of the most recognizable and ubiquitous feature of oceanic eddies 15 are coherent vortices with spatial scales of tens to hundreds of kilometers, frequently re-16 ferred as "mesoscale eddies". Coherent mesoscale eddies are known to transport prop-17 erties across the ocean and to locally affect near-surface wind, cloud properties, and rain-18 fall patterns. Although coherent eddies are ubiquitous, their climatology, seasonality, and 19 long-term temporal evolution remains poorly understood. Here, we examine the kinetic 20 energy contained by coherent eddies and present the seasonal, interannual and long-term 21 variability using satellite observations between 1993 to 2019. A total of ~ 37 million co-22 herent eddies are detected in this analysis. Around 50% of the kinetic energy contained 23 by ocean eddies corresponds to coherent eddies. Additionally, a strong seasonal cycle is 24 observed, with a 3–6 months lag between the wind forcing and the response of the co-25 herent eddy field. The seasonality of the number of coherent eddies and their amplitude 26 reveals that the number of coherent eddies responds faster to the forcing (~ 3 months), 27 than the coherent eddy amplitude (which lags by ~ 6 months). This seasonal cycle is spa-28 tially variable, so we also analyze their climatology in key oceanic regions. Our analy-29 sis highlights the relative importance of the coherent eddy field in the ocean kinetic en-30 ergy budget, implies a strong response of the eddy number and eddy amplitude to forc-31 ing at different time-scales, and showcases the seasonality, and multidecadal trends of 32 coherent eddy properties. 33

³⁴ Plain language summary

Coherent eddies are the most common feature of ocean variability observable from 35 satellites. They are crucial in ocean dynamics as they can transport properties over long 36 distances and interact with the atmosphere. Our study investigates the seasonal, inter-37 annual, and long-term changes in the abundance and intensity of coherent eddies, by au-38 tomatically identifying individual eddies over the available satellite altimeter record. The 39 seasonal cycle suggests a transition from numerous, smaller, and weaker coherent eddies, 40 to fewer and larger, and stronger coherent eddies over the season. In addition, a long-41 term adjustment of the coherent eddy field is identified with possible links to long-term 42 changes in the climate system. 43

-2-

44 1 Introduction

Mesoscale ocean variability with spatial scales of tens to hundreds of kilometers is 45 comprised of processes such as vortices, waves, and jets (Ferrari & Wunsch, 2009; Fu et 46 al., 2010). These mesoscale processes are highly energetic, and they play a crucial role 47 in the transport of heat, salt, momentum, and other tracers through the ocean (Wun-48 sch & Ferrari, 2004; Wyrtki et al., 1976; Gill et al., 1974). One of the most recognizable 49 and abundant ocean processes observable from space are mesoscale vortices. Although 50 mesoscale vortices are commonly referred to in the literature as "mesoscale eddies", this 51 term is also often used to describe the total mesoscale ocean variability (the time-varying 52 component of the mesoscale flow), thus, to avoid ambiguity we will refer to mesoscale 53 vortices as *coherent eddies*. Coherent eddies are abundant and energetic; they are essen-54 tial to ocean dynamics as concluded by many previous studies (Hogg & Blundell, 2006; 55 Siegel et al., 2011; Beron-Vera et al., 2013; Frenger et al., 2013, 2015; Pilo et al., 2015; 56 Schubert et al., 2019; Patel et al., 2020). 57

Coherent eddies are quasi-circular geostrophic currents. According to their rota-58 tional direction and the sign of the Coriolis parameter, the sea surface height anomaly 59 within a coherent eddy can have a negative or positive sea surface height anomaly (cold-60 core and warm-core coherent eddies, respectively). This characteristic sea surface height 61 signature of coherent eddies has been utilized to identify and track coherent eddies from 62 satellite altimetry (e.g., Chelton et al., 2007; Faghmous et al., 2015; Ashkezari et al., 2016; 63 Martínez-Moreno et al., 2019; Cui et al., 2020). Automated identification algorithms of 64 coherent eddies have revealed their ubiquity in the oceans, with a predominant influence 65 at hotspots of eddy activity such as in boundary current extensions and the Antarctic 66 Circumpolar Current. In these regions, it has been estimated that coherent eddies con-67 tribute around 40-50% of the net mesoscale kinetic energy (Chelton et al., 2011) and thus 68 a significant fraction of the total kinetic energy (Ferrari & Wunsch, 2009). Although this 69 estimate showcases the importance of the mesoscale coherent eddy field, the energy con-70 tained by coherent eddies was estimated by extracting the total geostrophic velocity within 71 the radius of each detected coherent eddy; thus, it is possible that this estimate may con-72 tain energy from other processes. Here we extend on this past work by reconstructing 73 the surface imprint of coherent eddies using a new eddy tracking algorithm and using 74 the latest available satellite record. 75

-3-

There is broad consensus that mesoscale eddy kinetic energy has a pronounced sea-76 sonal variability (Qiu, 1999; Qiu & Chen, 2004; Kang & Curchitser, 2017; Uchida et al., 77 2017). Several hypotheses have been proposed to explain this seasonality including: sea-78 sonal variations of atmospheric forcing (Sasaki et al., 2014), seasonality of the mixed layer 79 depth (Qiu et al., 2014; Callies et al., 2015), seasonality of the intensity of barotropic in-80 stability (Qiu & Chen, 2004), the variability of the baroclinic instability due to the sea-81 sonality of the vertical shear (Qiu, 1999), and a seasonal lag of the inverse energy cas-82 cade (i.e. energy is transported between scales, from small to large; Arbic et al., 2013) 83 in combination with the presence of a front in the mixed layer, which can lead to a sea-84 sonal cycle of the baroclinic instability (Qiu et al., 2014). On one hand, processes such 85 as barotropic and baroclinic instabilities control the seasonality of coherent eddies in the 86 ocean. On the other hand, recent studies using observations and eddy-permitting climate 87 models suggest slower adjustments of the global ocean that create long-term changes in 88 the coherent eddy field. Such readjustments include a multidecadal increase in the ocean 89 stratification resulting from temperature and salinity changes (Li et al., 2020), a hori-90 zontal readjustment of sea surface temperature gradients (Cane et al., 1997; Bouali et 91 al., 2017; Ruela et al., 2020), and an intensification of the kinetic energy, eddy kinetic 92 energy, and mesoscale eddy kinetic energy over the last 3 decades as a consequence of 93 an increase in wind forcing (Hu et al., 2020; Wunsch, 2020; Martínez-Moreno et al., 2021). 94 All of these seasonal factors and long-term readjustments directly influence the annual 95 and decadal response of the coherent eddy field, however, the seasonality of the coher-96 ent component of the eddy kinetic energy, as well as the seasonal cycle and trends of the 97 coherent eddy statistics, remain unknown. 98

Here we present a new global climatology of the coherent eddy kinetic energy by 99 reconstructing the coherent eddy signature from satellite observations. Our study doc-100 uments the seasonal cycle of the coherent eddy kinetic energy, and the seasonal cycle and 101 long-term trends of the coherent eddy properties over the satellite record. Moreover, we 102 conduct more detailed analyses in regions where coherent eddies dominate the eddy ki-103 netic energy field. The rest of this paper is structured as follows: the data sources and 104 methodology are described in Section 2. Then, we present the climatology, energy ra-105 tios, and global seasonality of the coherent eddy kinetic energy in Section 3. Section 4 106 outlines the global climatology and seasonality of coherent eddy properties, followed by 107 long-term changes of the coherent eddy properties (Section 5). Then we focus our at-108

-4-

tention on the seasonal cycle and coherent eddy properties in regions dominated by co-

herent eddies (Section 6). Finally, Section 7 summarizes the main results and discusses

the implications of this study.

112 2 Methods

We use daily sea surface height (SSH) data made available by the Copernicus Ma-113 rine Environment Monitoring Service in near real time (CMEMS, 2017). This gridded 114 product contains the sea surface height and geostrophic velocities with daily 0.25° res-115 olution from January 1993 to 2019. The daily geostrophic velocities allow us to compute 116 the kinetic energy (KE) and eddy kinetic energy (EKE) over the satellite record. The 117 main source of EKE is the time-varying wind (Ferrari & Wunsch, 2009); thus, we also 118 compute the seasonal cycle of the wind magnitude from the JRA55 reanalysis (Japan 119 Meteorological Agency, Japan, 2013) using wind velocities at 10m above the ocean's sur-120 face. 121

Over the same record, coherent eddy statistics from Martínez-Moreno et al. (2019), 122 hereafter MM19, are analyzed and compared with those released by Chelton & Schlax 123 (2013), hereafter CS13. Both datasets are gridded in a 1° resolution and are produced 124 via automated eddy identification algorithms using closed contours of SSH. However, these 125 datasets have important differences in the criteria they use to identify and record coher-126 ent eddies statistics. The major differences include: (i) MM19's algorithm requires an 127 adjustment between a 2D Gaussian and the SSH anomaly (SSHa) surface within the iden-128 tified closed contour, while CS13's only uses the outermost closed contour of SSH; (ii) 129 MM19's dataset reports the maximum SSHa within the identified coherent eddy, while 130 CS13's algorithm reports the maximum SSH value minus the discrete level in which the 131 coherent eddy was identified; and (iii) MM19's dataset includes all detected coherent ed-132 dies, while CS13's dataset excludes coherent eddies with lifetimes shorter than four weeks 133 and coherent eddy amplitudes smaller than 1cm. Moreover, MM19's algorithm allows 134 the reconstruction of the coherent eddy field under the assumption that coherent eddies 135 have a 2D Gaussian imprint in the sea surface height. This Gaussian reconstruction of 136 the coherent eddy field then allows us to estimate the coherent geostrophic eddy veloc-137 ities and thus the kinetic energy contained only by coherent eddies. 138

-5-

¹³⁹ 2.1 Kinetic Energy decomposition

Kinetic energy is commonly divided into the mean and time-varying components through a Reynolds decomposition. At a given time, the surface velocity field $\mathbf{u} = (u, v)$ is split into the time mean ($\overline{\mathbf{u}}$) and time varying components (\mathbf{u}'). Moreover, MM19 proposed to further decompose the eddy kinetic energy into the energy contained by coherent features (\mathbf{u}'_{e}) and non-coherent features (\mathbf{u}'_{n}). Therefore the KE equation can be written as:

$$KE = \underbrace{\overline{u}^2 + \overline{v}^2}_{MKE} + \underbrace{u'_e^2 + v'_e^2}_{CEKE} + \underbrace{u'_n^2 + v'_n^2}_{nCEKE} + \underbrace{\mathcal{O}_c^2}_{EKE} + \underbrace{\mathcal{O}^2}_{EKE}$$
(1)

Due to the properties of this decomposition, the second order term \mathcal{O}^2 is zero when 146 averaged over the same period as $\overline{\mathbf{u}}$. However, \mathcal{O}_c^2 is not necessarily negligible, unless it 147 is averaged over time and space. More information about the decomposition of the field 148 into coherent features and non-coherent features is explained in Martínez-Moreno et al. 149 (2019). A global snapshot of each component of kinetic energy decomposition is shown 150 in Figure 1, where the KE and EKE are comprised of rings and filaments. As expected, 151 the decomposition of EKE into CEKE and nCEKE components exhibits only the ring-152 like signatures expected of coherent eddies, while the non-coherent component primar-153 ily shows filaments, with some mis-identified coherent eddies. 154

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2.2 Eddy statistics

The eddy statistics used in this study include (i) the eddy count $(cEddy_n)$ defined 159 as the number of coherent eddies per grid cell, (ii) the eddy diameter defined as the di-160 ameter of a circle with equal area to the closed contour of each identified eddy, and (iii) 161 the mean eddy amplitude defined as the mean amplitude of the coherent eddies within 162 the cell (cEddy_{*amp*}). The latter metric can be separated into positive (cEddy⁺_{*amp*}) and 163 negative $(cEddy_{amp}^{-})$ coherent eddy amplitudes, defined as the mean amplitude of warm 164 core and cold core coherent eddies, respectively, within the cell. The polarity indepen-165 dent eddy amplitude ($|cEddy_{amp}|$) is defined as: 166

$$|cEddy_{amp}| = \frac{1}{2} \left(cEddy_{amp}^{+} - cEddy_{amp}^{-} \right)$$
(2)



Figure 1. Snapshot of surface kinetic energy ($\overline{\text{KE}}$), surface eddy kinetic energy ($\overline{\text{EKE}}$), surface coherent eddy kinetic energy ($\overline{\text{CEKE}}$), and surface non-coherent eddy kinetic energy ($\overline{\text{nCEKE}}$) for the 1st of January 2017.

Note that the $cEddy_{amp}^+$ and $cEddy_{amp}^-$ are sign definite, thus the difference will always 167 be positive, whereas the gridded averaged $\operatorname{cEddy}_{amp}$ can be negative or positive noting 168 the dominant polarity of coherent eddies in the region, and the absolute value of $cEddy_{amp}$ 169 is denoted by $cEddy_{|amp|}$. We analyze the climatology and trends of the above eddy statis-170 tics over the available satellite record, namely between 1993 and 2019. We exclude the 171 equatorial region (10° S - 10° N) and regions poleward of 60° , because the geostrophic ap-172 proximation is invalid near the Equator and the satellite spatial coverage at high-latitudes 173 is unable to resolve the coherent eddy scales polewards of 60° . Note that the climatol-174 ogy of $cEddy_n$ is computed by adding all the identified eddies over the record, while all 175

other climatological statistics are computed as the time-average over the record. Seasonal climatologies are calculated for the monthly average of each coherent eddy statistic, while hemispheric time-series are filtered with a running average of 90 days. Trends of cEddy_n and |cEddy_{amp}| are calculated by coarsening the dataset to a 5° grid, and then linear trends are computed for each grid point. The statistical significance of trends is assessed by a modified Mann-Kendall test above the 95% confidence level (Yue & Wang, 2004).

Time averages are denoted by $\overline{}$, while area-weighted averages are denoted using $\langle \rangle$, where the area-weighted average of a function f is:

$$\langle f \rangle = \frac{\int f \xi dx dy}{\int \xi dx dy},\tag{3}$$

where ξ is a mask that is set to zero in grid cells where no coherent eddies were identified and one elsewhere.

¹⁸⁷ 3 Global Coherent Eddy Energetics

The kinetic energy decomposition estimated from sea surface height measured by 188 satellite altimeters averaged from 1993-2019 is shown in Figure 2. These maps show that 189 many regions of the global ocean are highly energetic in mean KE ($\overline{\text{KE}}$), mean EKE ($\overline{\text{EKE}}$). 190 mean coherent eddy kinetic energy (\overline{CEKE}) and mean non-coherent eddy kinetic energy 191 $(\overline{\text{nCEKE}})$. The spatial pattern highlights well-known regions of the ocean where mesoscale 192 processes are abundant, such as the western boundary current (WBC) extensions and 193 the Antarctic Circumpolar Current. The spatial distribution of the energy contained by 194 the reconstructed mesoscale coherent eddies and non-coherent components are similar 195 (Figures 2c,d). However, there are some regions where coherent eddies dominate over 196 non-coherent, and vice-versa. Overall, this decomposition suggests that boundary cur-197 rent extensions and other energetic regions of the ocean contain both coherent and non-198 coherent components of the kinetic energy. 199

Eddy kinetic energy is known to be more than an order of magnitude greater than kinetic energy of the mean flow (MKE; Gill et al., 1974); this result is clearly shown in Figure 3a, which indicates that $\overline{\text{EKE}}$ is responsible for almost all the $\overline{\text{KE}}$ across the ocean, except for regions with persistent currents over time. Such regions are located in the mean boundary extension locations, the equatorial Pacific currents and regions in the Antarctic Circumpolar Current, where the $\overline{\text{EKE}}$ explains around 40% of the $\overline{\text{KE}}$. In a previ-



Figure 2. a) Mean surface kinetic energy ($\overline{\text{KE}}$); b) surface eddy kinetic energy ($\overline{\text{EKE}}$); c) surface coherent eddy kinetic energy ($\overline{\text{CEKE}}$), and d) surface non-coherent eddy kinetic energy ($\overline{\text{nCEKE}}$) averaged between 1993-2018.

ous study, Chelton et al. (2011) estimated that the EKE within coherent eddies with life-218 times greater than 4 weeks contain between 40-60% of the $\overline{\text{EKE}}$. Our method to recon-219 struct the coherent eddy signature (Figure 3b) further corroborates that the coherent 220 eddy component ($\langle \overline{\text{CEKE}} \rangle$) has ~48% of the $\langle \overline{\text{KE}} \rangle$ (Figure 3d). Furthermore, global area 221 averages of the ratios show that $\langle \overline{\text{EKE}} \rangle$ explains $\sim 78\%$ of the ocean $\langle \overline{\text{KE}} \rangle$ field, while 222 non coherent eddy features contain $\sim 57\%$ percent of the $\langle \overline{\text{EKE}} \rangle$. Note that the globally 223 averaged coherent and non coherent components do not add to 100% as the cross terms 224 (\mathcal{O}_c^2) are non-zero. The spatial pattern reveals a dominance of the $\overline{\text{CEKE}}$ equatorward 225 from the boundary current extensions and in areas with large coherent eddy contribu-226 tions of around 80% of the region's eddy kinetic energy, such as south of Australia, in 227 the Tehuantepec Gulf, and in the tropical Atlantic. An evident signal is a reduction of 228 the energy contained by coherent eddies at high latitudes and an increase in the energy 229 explained by non-coherent eddies; this signal could be a consequence of the inability of 230 the 0.25° satellite resolution (~ 13 km at 60° latitude) to resolve coherent eddies with 231 scales smaller than ~ 10 km (first baroclinic Rossby radius at 60°; Chelton et al., 1998). 232

Figure 4 shows the seasonal cycle of the area-weighted EKE and CEKE for the Northern Hemisphere ($\langle EKE \rangle_{NH}$ and $\langle CEKE \rangle_{NH}$; 10°N - 60°N) and Southern Hemisphere ($\langle EKE \rangle_{SH}$ and $\langle CEKE \rangle_{SH}$; 60°S - 10°S). In both hemispheres, the $\langle EKE \rangle$ and $\langle CEKE \rangle_{NH}$ peak during summer. In the Northern Hemisphere, the largest $\langle EKE \rangle_{NH}$ and $\langle CEKE \rangle_{NH}$

Figure 3. Ratios of the kinetic energy components. a) Map of the proportion of mean eddy 203 kinetic energy (EKE) versus mean kinetic energy (KE); b) Map of the fraction of mean coherent 204 eddy kinetic energy (CEKE) versus mean eddy kinetic energy (EKE); c) Map of the fraction of 205 mean non-coherent eddy kinetic energy (NCEKE) versus mean eddy kinetic energy (EKE); d) 206 Global time and area averaged (represented by hi) fraction of mean eddy kinetic energy (EKE) 207 versus the global mean kinetic energy (KE), area averaged fraction of mean coherent eddy 208 kinetic energy (TEKE) and mean non coherent eddy kinetic energy (TEKE) versus global 209 mean eddy kinetic energy (EKE). Regions where the depth of the ocean is shallower than 210 1000m are removed from the ratio estimation. 211



Figure 7. Distribution of the identified eddy diameter $(cEddy_d; km)$ and hemispherical seasonality of the coherent eddy diameter. a) Distribution in percentage of identified eddy amplitude, solid bar below distribution represents 90% of the identified eddies. Seasonal cycle of the eddy diameter for the b) Northern Hemisphere and c) Southern Hemisphere. Dark solid line and area corresponds to coherent eddies with diameters larger than 120 km, while light gray dash-dotted line and area shows coherent eddies with diameters smaller than 120 km.

363 5 Trends

The results presented in Figures 4 and 6 suggest a long-term readjustment of the 364 coherent eddy field. The long-term trends of the number of coherent eddies, absolute co-365 herent eddy amplitude, and coherent eddy amplitude polarities are further explored in 366 Figure 8 contrasting the MM19 and CS13 methods. Both MM19 and CS13 datasets show 367 consistent spatial patterns in the trends and significance of the number of coherent ed-368 dies and the absolute coherent eddy amplitude. Several regions in the ocean, such as the 369 Southern Ocean, North Atlantic and North Pacific, show a decrease in the number of ed-370 dies. Those same regions also have a clear increase in the absolute coherent eddy am-371 plitude. These trends are similar to those observed in mesoscale eddy kinetic energy (Martínez-372 Moreno et al., 2021) and provide additional evidence of a readjustment of the mesoscale 373 eddy field over the last 3 decades. 374

The observed trends of $cEddy_{|amp|}$ in several oceanic regions have the same scale as sea level rise (~3cm per decade). By analyzing the positive and negative coherent eddy amplitude, we filter out the observed trends that come from a net increase in sea level.

-17-



Figure 8. Trends of coherent eddy statistics. a) and b) Trends of the number of identified coherent eddies from satellite observations identified using the TrackEddy scheme of MM19, and those reported in CS13's dataset. c) and d) Trends of the absolute value of identified coherent eddy amplitude (cEddy_{|amp|}) from satellite observations identified using TrackEddy (after MM19), and those reported by CS13. e) and f) Trends of the eddy amplitude polarity using TrackEddy (cEddy⁺_{amp} and cEddy⁻_{amp}). Gray stippling shows regions that are statistically significant above the 95% confidence level.

In fact, each coherent eddy polarity has intensified in the Southern Ocean and North East Pacific and Atlantic. In other words, the amplitude of each polarity has increased over time, and thus this strengthening is an intrinsic response of the coherent eddy field. Note that the negative coherent eddy amplitude dominates the global $|cEddy_{amp}|$ trends (Figure 8e, f). However, different trend patterns can be observed in both positive and negative coherent eddy amplitudes in the North Atlantic and North Pacific, where the negative coherent eddy amplitude in the Western Boundary Currents appears to decrease.

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6 Regional Climatology

For regions with relatively large proportions of CEKE located at WBC extensions and eastern boundary currents, we investigate the seasonal and long-term variability of the coherent eddy properties. The most energetic WBC include the Gulf Stream, the Kuroshio

-18-

Current, and the Agulhas Current (Figures 9, 10, and 11). Coherent eddy generation in boundary current extensions occurs through baroclinic and barotropic instabilities of the mean current, thus all these regions share similar generation dynamics. In all these regions without exception; (i) CEKE contains 50-80% of the EKE in regions equatorward from the mean WBC extensions, (ii) the number of eddies is consistently small over the mean WBC extensions, and (iii) the eddy amplitude is larger over the mean WBC extensions.

In the Gulf Stream, the energy ratio between CEKE and EKE is $\sim 56\%$ (Figure 9). 403 The highest energy ratio occurs in regions with numerous eddies, colocated with regions 404 where the largest $|cEddy_{amp}|$ gradients occur. The time series of $cEddy_n$ and $\langle |cEddy_{amp}| \rangle$ 405 are anti-correlated (-0.52), and they display interannual and seasonal variability. Although 406 Chaudhuri et al. (2009) observed that a positive phase of the North Atlantic Oscillation 407 (NAO) exhibits higher EKE, due to an increase in baroclinic instability, thus suggest-408 ing more coherent eddies, we do not find a correlation between the $cEddy_n$ or the $\langle |cEddy_{amp}| \rangle$ 409 in the Gulf Stream and the NAO index. Similar to the signal observed in the hemispheric 410 analysis, the eddy count seasonal cycle follows the wind maximum lagging by ~ 3 months, 411 while the amplitude of the coherent eddies lags by ~ 6 months. 412

The variability of the $cEddy_n$ and $\langle |cEddy_{amp}| \rangle$ in the Kuroshio Current are weakly anti-correlated (-0.41; Figure 10). However, on average 56% of the energy in the region corresponds to CEKE. As observed in the Gulf Stream, there is an important seasonal cycle in the boundary extension, where the eddy count seasonal cycle occurs in March, lagging the wind maximum by ~3 months (January). Meanwhile, the amplitude of the coherent eddies lags the wind maximum by ~ 6 months (June).

In the Southern Hemisphere the strongest boundary current, the Agulhas Current, 433 shows similar behavior to its counterparts in the Northern Hemisphere (Figure 11). On 434 average, coherent eddies in the Agulhas Current contain $\sim 56\%$ of the energy, meanwhile 435 the cEddy_n seasonal peak occurs in August, while the $\langle | cEddy_{amp} | \rangle$ peak occurs in January-436 February. The seasonal lag between the winds, eddy count, and eddy amplitude in each 437 of the WBC extensions is interpreted as being analogous to the lagged response of co-438 herent eddy properties (Figure 6) due to eddy-eddy interactions, consistent with the in-439 verse cascade of energy. 440

-19-

Figure 9. Climatology of the eddy eld and coherent eddy eld in the Gulf Stream. a) Ratio 413 of mean coherent eddy kinetic energy (CEKE) versus mean eddy kinetic energy (EKE); b) Thick 414 lines show the running average over 2 years and thin lines show the running average over 90 days 415 of the coherent eddy number sum and the average coherent eddy amplitude; c) Map of the num-416 ber of eddies; d) Map of the average coherent eddy amplitude; e) Seasonal cycle of the number 417 of eddies (cEddy_n); f) Seasonal cycle of the positive coherent eddy amplitude ($cEddy_{amp}^{+}$), 418 and g) Seasonal cycle of the negative coherent eddy amplitude ($\mathsf{cEddy}_{\mathsf{amp}}\;$). Contours in maps 419 correspond to mean sea surface height (m). 420

al., 2020; Wunsch, 2020; Martínez-Moreno et al., 2021). This long-term readjustment re veals an intensification of the coherent eddy field, possibly due to long-term readjust ments in the ocean baroclinic and barotropic instabilities, as well as the strength of the
 winds.

The reconstruction of the coherent eddies and their statistics has revealed regions 524 with important coherent eddy contributions and a distinct seasonal evolution of the co-525 herent eddies. Western boundary current (WBC) extensions generate eddies through the 526 instability of the main currents and the seasonal cycle of coherent eddies, CEKE, and 527 thus EKE could be associated with an inverse energy cascade observable through lagged 528 seasonal cycles in the coherent eddy statistics. In addition, the amplitude of the seasonal 529 cycle in WBC extensions is two times larger than any other region, thus the seasonal-530 ity of the coherent eddies in WBC extensions dominates the hemispheric seasonal cy-531 cle. Furthermore, the seasonal lag of the inverse energy cascade is coupled with the pres-532 ence of fronts (Qiu et al., 2014), such as the case for WBC extensions, and our results 533 are consistent with the notion of baroclinic instability generating eddies and, via eddy-534 eddy interactions, a lagged inverse energy cascade. 535

The use of satellite observations in this study limits our ability to quantify the im-536 portance of the inverse energy cascade seasonality in the control of the coherent eddy 537 seasonal cycle. As mentioned above, there is robust evidence of an increase in eddy-eddy 538 interactions, however we cannot discard important contributions from other processes 539 such as the seasonal cycle of forcing, stratification, and instabilities, which are crucial 540 in the generation of coherent eddies. Although this study can provide a descriptive re-541 sponse of the coherent eddy field, further work is needed to assess the role of eddy-eddy 542 interactions in our changing climate, ocean dynamics, and biogeochemical processes. Fur-543 thermore, the SWOT mission could allow us to advance our understanding of eddy-eddy 544 interactions and the seasonal cycle of scales smaller than mesoscale, which may provide 545 further evidence of the inverse energy cascade driving the coherent eddy seasonality. Cur-546 rent generation climate models have just started to resolve mesoscale dynamics, thus, 547 the presented estimate of energy in coherent eddies from satellite observations could be 548 used as a benchmark that facilitates the evaluation of such models, and to quantify the 549 energy contained by mesoscale and more specifically coherent eddies in future climate 550 projections. 551

-25-

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556	struction, coherent and non-coherent eddy kinetic energy datasets, in addition to grid-
557	ded coherent eddy tracking datasets are publicly available at (https://doi.org/10.5281/
558	zenodo.4646429). All analyses and figures in this manuscript are reproducible via Jupyter
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