YORP Effect on Asteroid 162173 Ryugu: Implications for the Dynamical History

Masanori Kanamaru¹, Sho Sasaki², Tomokatsu Morota³, Yuichiro Cho³, Eri Tatsumi⁴, Masatoshi Hirabayashi⁵, Naru Hirata⁶, Hiroki Senshu⁷, Yuri Shimaki¹, Naoya Sakatani⁸, Satoshi Tanaka⁹, Tatsuaki Okada¹⁰, Tomohiro Usui¹¹, Seiji Sugita¹², and Sei-ichiro Watanabe¹³

¹Institute of Space and Astronautical Science (ISAS), Japan Aerospace Exploration Agency (JAXA)
²Osaka University
³The University of Tokyo
⁴Instituto de Astrofisica de Canarias
⁵Auburn University
⁶University of Aizu
⁷Chiba Institute of Technology
⁸Rikkyo University
⁹JAXA ISAS
¹⁰JAXA
¹¹Institute of Space and Astronautical Science, Japan Aerospace Exploration Agency
¹²University of Tokyo
¹³Nagoya University

November 22, 2022

Abstract

Asteroid 162173 (Ryugu) is a carbonaceous asteroid that was visited by Japan's Hayabusa2 spacecraft in 2018. The formation mechanism of spinning-top shape of Ryugu is an essential clue to the dynamical history of the near-Earth asteroid. In this study, we address the spin-state evolution of Ryugu induced by the Yarkovsky–O'Keefe–Radzievskii–Paddack (YORP) effect, i.e., the thermal recoil torque that changes the rotation period and spin-pole direction.

Given the current orbit, spin state, and three-dimensional shape observed by Hayabusa2, we computed the YORP torque exerted on Ryugu using a simplified thermal model approximating zero thermal conductivity. Despite differences in meter-scaled topography, all 20 shape models that we examined indicate that the spin velocity of Ryugu is currently decreasing at a rate of $(-0.42-6.3)*10^{-6} \text{ deg/day}^2$. Our findings also suggest that the thermal torque on the asteroid is responsible for maintaining the spin pole upright with respect to the orbital plane.

Therefore, the YORP effect could explain the significant spin-down from a period of 3.5 h initially to 7.6 h currently. The corresponding time scale of the rotational deceleration is estimated to be 0.58–8.7 million years, depending on the input shape models. This time scale is comparable to e.g., the formation period of the largest crater, Urashima (5–12 Ma) or the western bulge (2–9 Ma) as derived from previous studies on crater statistics in Ryugu. It is considered that the rotation of the asteroid started to decelerate in the wake of the major crater formation or the resurfacing event on the western hemisphere.

YORP Effect on Asteroid 162173 Ryugu: Implications for the Dynamical History

M. Kanamaru¹, S. Sasaki², T. Morota³, Y. Cho³, E. Tatsumi⁴, M.
Hirabayashi⁵, N. Hirata⁶, H. Senshu⁷, Y. Shimaki¹, N. Sakatani⁸, S. Tanaka¹,
T. Okada¹, T. Usui¹, S. Sugita³, S. Watanabe⁹.

¹Institute of Space and Astronautical Science (ISAS), Japan Aerospace Exploration Agency (JAXA),

3-3-1 Yoshinodai, Sagamihara 252-5210, Japan.

²Osaka University, 1-1 Machikaneyama, Toyonaka, Osaka 560-0043, Japan.

³The University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 1130033, Japan.

⁴Instituto de Astrofísica de Canarias, C/Vía Láctea, 38205 La Laguna - Tenerife - España.

⁵Auburn University, 211 Davis Hall, Auburn, AL 36849-5338, United States

 6 University of Aizu, Tsuruga, Ikkimachi, Aizu Wakamatsu, Fukushima 965-8580, Japan.

⁷Chiba Institute of Technology, 2-17-1 Tsudanuma, Narashino, Chiba 275-0016, Japan.

⁸Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima, Tokyo 171-8501, Japan.

 $^9\mathrm{Nagoya}$ University, Furo-cho, Chikusa-ku, Nagoya, Aichi 464-8601 Japan.

Key Points:

1	• Thermal recoil torque (i.e., the YORP effect) plays a dominant role in the spin-
2	down of asteroid 162173 Ryugu.
3	- The estimated spin-down time scale (0.58 – 8.7 million years) indicates a period
4	of major change in the topography of Ryugu.
5	• The YORP effect is responsible for keeping the spin-pole of Ryugu perpendicu-
6	lar to the orbital plane.

Corresponding author: Masanori Kanamaru, kanamaru.masanori@jaxa.jp

Abstract

Asteroid 162173 (Ryugu) is a carbonaceous asteroid that was visited by Japan's Hayabusa2 spacecraft in 2018. The formation mechanism of spinning-top shape of Ryugu is an essential clue to the dynamical history of the near-Earth asteroid. In this study, we address the longterm evolution of the spin state of Ryugu induced by the Yarkovsky–O'Keefe–Radzievskii– Paddack (YORP) effect, i.e., the thermal recoil torque that changes the rotation period and spin-pole direction.

Given the current orbit, spin state, and three-dimensional shape observed by Hayabusa2, we computed the YORP torque exerted on Ryugu using a simplified thermal model approximating zero thermal conductivity. Despite differences in meter-scaled topography, all 20 shape models that we examined indicate that the spin velocity of Ryugu is currently decreasing at a rate of $(-0.42 - -6.3) \times 10^{-6} \text{ deg/day}^2$. Our findings also suggest that the thermal torque on the asteroid is responsible for maintaining the spin pole upright with respect to the orbital plane.

Therefore, the YORP effect could explain the significant spin-down from a period of 3.5 h initially to 7.6 h currently. The corresponding time scale of the rotational deceleration is estimated to be 0.58 - 8.7 million years, depending on the input shape models. This time scale is comparable to e.g., the formation period of the largest crater, *Urashima* (5 - 12 Ma) or the western bulge (2 - 9 Ma) as derived from previous studies on crater statistics in Ryugu. It is considered that the rotation of the asteroid started to decelerate in the wake of the major crater formation or the resurfacing event on the western hemisphere.

Plain Language Summary

The Japanese spacecraft Hayabusa2 visited the kilometer-sized asteroid, Ryugu, and 27 found it to have a spinning-top shape with a diamond-like cross section. For an aggregate 28 of rock fragments to deform in this way, fast rotation is required. The rotation period of 29 Ryugu is 7.6 h, and its rotational speed is not sufficiently fast to deform the entire body. 30 It is proposed that Ryugu initially spun rapidly and has since slowed down. Light has no 31 mass, but it does have momentum and produces a faint pressure. As the asteroid is heated 32 from the Sun, radiation is emitted from the asteroid surface, resulting in a breaking effect 33 and changing the rotational speed of the asteroid over millions of years. We found that the 34

- $_{35}$ $\,$ radiation pressure is a reasonable mechanism for the spin-down of the asteroid and thus
- ³⁶ provides a clue to Ryugu's history.

1 Introduction

Japan's Hayabusa2 was a sample return mission from the C-type near-Earth asteroid, 37 162173 (1999 JU₃) Ryugu (Tachibana et al., 2014; Watanabe et al., 2017; Tsuda et al., 38 2019). The Hayabusa2 spacecraft arrived at the target asteroid in June 2018 and started its 39 homeward journey to Earth in November 2019 after an approximately 17-month asteroid-40 proximity phase. The mission included two successful touchdowns to sample the surface ma-41 terial, an artificial cratering experiment, and deployment of a lander and rovers. Hayabusa2 42 revealed the nature of the rocky surface and its spinning-top shape (Watanabe et al., 2019). 43 The spinning-top-shaped body has an elevated ridge in the equatorial region and a flat cross 44 section in the mid-latitude region, unlike spherical or ellipsoidal objects. Ryugu's shape is 45 considered to be the result of deformation induced by fast rotation in the past (Watanabe 46 et al., 2019). According to finite-element-method analysis Hirabayashi et al. (2019), a fast 47 rotation at a period of approximately 3.0 - 3.5 h is sufficient to induce interior structural 48 failure or surface mass wasting due to centrifugal force. However, the spin-down process 49 from the past rapid rotation to the current milder state (7.6 h period) remains unknown. 50 The goal of this study is to explore the Yarkovsky–O'Keefe–Radzievskii–Paddack (YORP) 51 effect on Ryugu, i.e., thermally induced spin alteration (Rubincam, 2000), which is one 52 of the greatest contributors to the spin dynamics of the asteroid. We propose a new ap-53 proach to reveal its evolutionary history by combining a dynamical simulation and analyses 54 of geologic features. The dynamical process sensitive to a topographic change enables us to 55 integrate the two perspectives. 56

1.1 Asteroid Ryugu revealed by Hayabusa2

We present a brief review of the scientific achievements of Hayabusa2 at the time of 57 writing. Watanabe et al. (2019) is a flagship report on the first impression of Ryugu, 58 including the spinning-top shape as mentioned above. The spinning-top shape and rocky 59 surface strongly suggested that Ryugu is a rubble pile formed by the catastrophic disruption 60 of a parent body and reaccumulation of the fragments. For our later simulations, we utilized 61 the orbital elements, rotation period, spin-pole orientation, and other physical properties 62 of Ryugu reported in this study (see Table 1). Ryugu is a retrograde rotator with a pole 63 almost perpendicular to its orbital plane, for which the obliquity ε (i.e., tilt angle of the 64 spin axis with respect to the normal vector of a body's orbital plane) corresponds to 171.6°. 65

Table 1. Properties of asteroid 162173 Ryugu in the J2000.0 frame at the epoch of 2018 July 1.0TDB (See the supplementary material of Watanabe et al. (2019)).

Parameters	Notation	Value	Unit		
Orbital elements					
Semi-major axis	a	1.190	AU		
Eccentricity	e	0.1903	_		
Inclination	Ι	5.884	deg		
Longitude of ascending node	Ω	251.6	deg		
Argument of perihelion	ω	211.4	deg		
Mean anomaly	Φ	21.94	\deg		
Rotation pole and period					
Right ascension (RA)	α	96.40	deg		
Declination (Dec)	δ	-66.40	deg		
Ecliptic longitude	λ	179.3	deg		
Ecliptic latitude	β	-87.44	deg		
Obliquity	ε	171.6	deg		
Rotation period	P	7.633	h		
Physical properties					
GM	GM	30.0	$\mathrm{m}^3/\mathrm{s}^2$		
Mass	M	4.50×10^{11}	kg		
Volume	V	0.377 ± 0.005	${\rm km}^3$		
Mean density	ho	$1{,}190\pm20$	$\rm kg/m^3$		

Three-dimensional (3D) shape models of Ryugu were constructed from images captured 66 by the onboard optical navigation camera (ONC) and have been updated until the time of 67 writing. In the Hayabusa2 project, two different methods are used for 3D shape reconstruc-68 tion: stereo-photoclinometry (SPC) (R. Gaskell et al., 2006; R. W. Gaskell et al., 2008) and 69 structure-from-motion (SfM) (Szeliski, 2011). Ryugu's volume, as derived from the shape 70 model and mass from spacecraft tracking data during a descent operation onto the asteroid, 71 yielded a bulk density of $1190 \pm 20 \text{ kg/m}^3$ (Watanabe et al., 2019). The average reflectance 72 spectrum of Ryugu is very flat from visible to near-infrared wavelengths, and its geometric 73 albedo is very low, i.e., $4.0 \pm 0.5\%$ at the 0.55 µm band (Tatsumi et al., 2020). The re-74 flectance spectrum can be classified as Cb-type in the Bus and Binzel taxonomy (Sugita et 75 al., 2019) and C/F-type in the Tholen taxonomy (Tatsumi et al., 2020). A weak but sharp 76 absorption feature at 2.72 µm was detected across the entire surface. These features suggest 77 that, similar to the heated Ivuna meteorite, Ryugu is composed of CM- or CI-like materials 78 (Kitazato et al., 2019). Because the bulk density of Ryugu is smaller than that of many 79 types of carbonaceous chondrites, the porosity of Ryugu could exceed 50% (Watanabe et 80 al., 2019). 81

Global ONC observations of Ryugu revealed many of its geologic properties, including 82 an east-west dichotomy, an equatorial ridge, numerous impact craters, and a high abundance 83 of large boulders (Sugita et al., 2019). Closer examinations of surface features on Ryugu 84 show evidence of mass motion from the equatorial ridges toward mid-latitude regions, such 85 as imbricated boulders and regolith run-ups on the ridge sides of boulders. Such direction of 86 mass motion is consistent with geopotential changes due to the spin deceleration of Ryugu; 87 a decrease in centrifugal force increases the geopotential of the equatorial ridge and lowers 88 that of mid-latitude regions (Sugita et al., 2019; Morota et al., 2020). Global mapping 89 also revealed that the surface of Ryugu exhibits distinctive latitudinal color variation that 90 supports the deceleration-induced mass motion. The most prominent color variation in 91 visible wavelengths is observed in the spectral slope between the b- and x-bands (0.48-0.86)92 µm) (Sugita et al., 2019; Tatsumi et al., 2020). The variation in the b-x spectral slope 93 is correlated with the geopotential (or elevation measured from an equipotential surface). 94 Areas of high potential, such as the polar and equatorial regions, tend to have smaller 95 or negative b-x slopes (i.e., bluer spectra). In contrast, the mid-latitude areas of Ryugu 96 have positive b-x slopes (i.e., redder spectra). This color variation suggests that materials 97 weathered on the surface migrate from highlands to lowlands in response to the current shape 98

and gravity field of Ryugu; this is likely caused by the most recent major mass motion on
 Ryugu (Sugita et al., 2019). Thus, both morphological and spectral surface features on
 Ryugu support the recent deceleration in spin rate.

Further, crater statistics can serve as indicators for the surface age of a solid objects and 102 the mechanical properties of the surface layer. Hirata et al. (2020) provided a comprehensive 103 list of impact craters larger than 20 m on Ryugu and discussed their spatial distribution. 104 More detailed morphological studies of the craters are reported in Noguchi et al. (2021). A 105 statistical randomness analysis by Hirata et al. (2020) confirmed that those craters are con-106 centrated in the equatorial region $(30^{\circ}S-30^{\circ}N)$ rather than follow a random distribution. 107 Moreover, the number density of the craters varies longitudinally. The so-called western 108 bulge $(160^{\circ}\text{E}-290^{\circ}\text{E})$ has fewer craters than regions around the prime meridian of Ryugu 109 $(300^{\circ}\text{E} - 30^{\circ}\text{E})$. Additionally, Michikami et al. (2019) reported a difference in boulder abun-110 dance (> 5 m) between the eastern and western hemispheres. In fact, the number density 111 of the boulders is relatively lower in the western hemisphere. The origin of the western 112 bulge is proposed to be a past deformation process of Ryugu during a period of fast ro-113 tation (Hirabayashi et al., 2019) or regolith landslides toward the western side at a rapid 114 spin (Scheeres, 2015). These processes could resurface in the western hemisphere of Ryugu 115 and result in an east-west dichotomy in the crater and boulder densities. Ryugu's craters 116 were also found to possess morphological features, such as raised rims and wall slumping, 117 consistent with unconsolidated surface materials. Based on this observation, Sugita et al. 118 (2019) estimated the residence time of Ryugu in the main asteroid belt since the formation 119 of the current topography to be 8.9 ± 2.5 Ma using the gravity scaling rule for coarse-grain 120 targets (Tatsumi & Sugita, 2018). The use of gravity-scaling was subsequently validated by 121 the artificial impact experiment conducted by Hayabusa2 (Arakawa et al., 2020). 122

Based on detailed crater observations using close-up images, Morota et al. (2020) found 123 that Ryugu experienced orbital excursion toward the Sun after leaving a stable orbit in 124 the main belt. This sunward orbital excursion likely reddened the surface layer (< 1 m)125 through solar heating and/or solar wind irradiation. Crater counting indicates that the 126 surface reddening event was terminated at 0.3 to 8.1 Ma. Because the erosion of the red 127 surface layer through the despinning-induced mass motion postdates the reddening event, 128 it can be deduced that the rotational deceleration of Ryugu has likely occurred in the last 129 0.3 - 8.1 Ma. 130

1.2 Observational and theoretical studies on YORP

Spin parameters of asteroids have been actively investigated through light curve and 131 radar observation. However, to detect a secular change in the rotation period, multiple 132 observation sessions over several years are required. The YORP effect was initially detected 133 by the increase in the spin velocity of asteroid 54509 YORP (2000 PH5) (Lowry et al., 134 2007; Taylor et al., 2007). Since then, YORP-induced spin-up has been observed in several 135 sub-kilometer-sized asteroids: 1862 Apollo (Kaasalainen et al., 2007; Ďurech, Vokrouhlický, 136 Kaasalainen, Weissman, et al., 2008), 1620 Geographos (Durech, Vokrouhlický, Kaasalainen, 137 Higgins, et al., 2008), 3103 Eger (Durech et al., 2012, 2018), 25143 Itokawa (Lowry et al., 138 2014), 1685 Toro (Durech et al., 2018), and 161989 Cacus (Durech et al., 2018). Most 139 recently, asteroid 101955 Bennu was observed to be spinning up at a rate of $(3.63 \pm 0.52) \times$ 140 $10^{-6} \text{ deg/day}^2$ by ground-based observations and NASA's OSIRIS-REx spacecraft (Nolan 141 et al., 2019; Hergenrother et al., 2019). Although the rotation period of asteroid 162173 142 Ryugu was monitored during the proximity phase of Hayabusa2, no significant change in 143 period was confirmed. To compare the results of observations and numerical simulations in 144 terms of the YORP effect on Ryugu, we have to wait for the next opportunity of light curve 145 acquisition. 146

Since the YORP modeling by Rubincam (2000), many numerical studies based on three-147 dimensional shapes of real asteroids have been performed. The computational models of the 148 YORP effect have been developed to incorporate non-zero thermal conductivity (Čapek & 149 Vokrouhlický, 2004) and projected shadows (Vokrouhlický & Čapek, 2002). The advanced 150 thermophysical model (ATPM) proposed by Rozitis and Green (2011, 2012) completely 151 implemented both the reabsorption of thermal emission due to uneven terrain and the 152 surface roughness effect to deflect radiation in the direction of the Sun. Moreover, it has 153 been found that lateral heat conduction is likely to significantly impact the thermal torque 154 (Golubov et al., 2014; Ševeček et al., 2016), which has been neglected in most YORP models 155 that solve the one-dimensional heat conduction problem. However, an all-in-one simulation 156 method is computationally costly and difficult to apply to highly accurate shape models 157 acquired by spacecrafts. 158

In this study, we aim to demonstrate the YORP-induced spin evolution of Ryugu and compare its time scale with the surface age of the asteroid. Although a simplified computational model is used herein (Section 2), we compared various types of Ryugu's

- shape models (Section 3) to overcome the inherent problem of numerical YORP modeling,
- ¹⁶³ in which the net torque is highly dependent on input shape models (Statler, 2009). In
- ¹⁶⁴ Section 4, we evaluate the model sensitivity to shape and compare our numerical model
- ¹⁶⁵ with another thermophysical model. In Section 5, we associate the spin alteration of Ryugu
- with geological events that have occurred on the asteroid.

Symbol	Description
A	Geometric albedo
s_i	Shadowing factor of the i th surface element (1 for shadow or 0 for insolation)
Φ	Solar irradiation per unit area on a body's orbit
$oldsymbol{\hat{n}}_i$	Normal vector to the i th surface element
\hat{r}_{sun}	Direction of the Sun
ϵ	Emissivity of the body's surface
σ	Stefan-Boltzmann constant
T_i	Temperature of the i th surface element
K	Thermal conductivity of the material
$doldsymbol{f}_i$	Thermally induced force on the i th element
c	Speed of light
dS_i	Area of the i th element
au	YORP torque on the body
$oldsymbol{r}_i$	Centroid position of the i th element
$N_{\rm S}$	Number of surface elements
L	Angular momentum of rotation
C	Moment of inertia around the shortest axis
ω	Angular velocity of rotation

 Table 2.
 Notation in this paper.

Direction of the spin pole

Obliquity of the spin pole

Longitude of precession

2 Method of YORP Simulation

167

 \hat{s}

 ε

 ψ

To calculate the thermally induced torque on an asteroid, we need to evaluate the surface temperature or radiation energy flux of the body's surface based on its orbit, spin 168 state, and irregular shape. Subsequently, we simply have to integrate the equation of motion 169 for the asteroid's rotation. All symbols used in this section are listed in Table 2. 170

2.1 Thermal model

175

178

We begin with the energy conservation law at each surface element of a small body's shape. The following equation presents the balance between the incident energy from sunlight (left-hand side) and the sum of energy derived from thermal re-radiation from the surface element and heat conduction into the ground (right-hand side).

$$(1-A)(1-s_i)\Phi(\hat{\boldsymbol{n}}_i\cdot\hat{\boldsymbol{r}}_{sun}) = \epsilon\sigma T_i^4 + K\hat{\boldsymbol{n}}_i\cdot\nabla T_i$$
(1)

In this study, we calculated the energy flux $\Phi(t)$ in each time step based on the Kepler motion of the asteroid around the Sun.

$$\Phi(t) = \Phi_{\text{Earth}} \left(\frac{r_{\text{Earth}}}{r_{\text{body}}(t)} \right)^2 \tag{2}$$

The solar irradiation at the Earth's orbit $r_{Earth} = 1$ AU is called the solar constant Φ_{Earth} , and it is inversely proportional to the square of the body's distance from the Sun. It greatly influences the strength or time scale of the YORP effect depending on the orbital semi-major axis. For example, there is a difference in the energy flux by a factor of approximately six between the near-Earth orbit (~ 1 AU) and inner main belt (~ 2.5 AU). Asteroid Ryugu exhibits seasonal variation in solar irradiation by a few times because of its eccentric orbit. We used 1366.0 W/m² for the solar constant in our simulations.

The left-hand side of Equation 1 expresses the amount of solar energy absorbed by the 186 *i*th surface element of the shape model. Therefore, the factor $(\hat{n}_i \cdot \hat{r}_{sun})$ decreases the solar 187 irradiation per unit area depending on the tilt of the element. On the night-side of the body, 188 this factor becomes negative, and solar irradiation is supposedly turned off. In addition, we 189 implemented a ray-trace algorithm to check whether each element is illuminated or not at 190 a certain time, as implemented in, e.g., Breiter et al. (2009) and Rozitis and Green (2012). 191 The shadowing factor, s_i , returns an integer of 1 or 0, depending on whether solar rays 192 towards the *i*th element are blocked by other elements or not, respectively. To reduce the 193 computation time, we sometimes ignore the shadowing effect in our later simulations and 194 perform the so-called "pseudo-convex" model, originally implemented in Rubincam (2000). 195

The right-hand side of Equation 1 represents the energy released from each surface element, which includes the thermal radiation and heat flux of the body's interior. Some authors implemented one-dimensional thermophysical modeling to evaluate the surface temperature (e.g., Čapek & Vokrouhlický, 2004). This study simplified the computation of thermal radiation using the Rubincam (2000) approximation Rubincam (2000), which assumed (1) zero-conductivity and (2) Lambert radiation from each surface element. According to assumption (1), we can neglect the conduction term in Equation 1 as follows:

$$(1-A)(1-s_i)\Phi(\hat{\boldsymbol{n}}_i\cdot\hat{\boldsymbol{r}}_{sun})\approx\epsilon\sigma T_i^4\tag{3}$$

This equation holds that the incident energy from sunlight is immediately emitted from the surface with no time lag. The second assumes that each surface element isotropically radiates energy, with the same intensity of infrared radiation observed from any angle. The Lambert radiation assumption results in a simple formula for the force exerted on each surface element (Rubincam, 2000; Vokrouhlický & Čapek, 2002):

$$d\boldsymbol{f}_i = -\frac{2}{3} \frac{\epsilon \sigma T^4}{c} \hat{\boldsymbol{n}}_i dS_i \tag{4}$$

$$= -\frac{2\Phi}{3c}(1-s_i)(\hat{\boldsymbol{n}}_i \cdot \hat{\boldsymbol{r}}_{sun})\hat{\boldsymbol{n}}_i dS_i$$
(5)

The thermal "kick-back" force, $d\mathbf{f}_i$, is directed opposite of the facet normal, $\hat{\mathbf{n}}_i$, and its magnitude is proportional to the area of the element dS_i . The thermal radiation, $\epsilon\sigma T^4$, can be replaced by the incident energy based on the assumption in Equation 3. We convert the factor (1 - A) to 1 to combine the effects of scattering on the surface. If the scattered light reflects isotropically, like thermal radiation, we can add its contribution to the factor (1 - A).

We can then compute the net torque, τ , of the YORP effect by integrating the above force over the entire surface of the asteroid. Given a polyhedral shape model covered with $N_{\rm S}$ triangular meshes, one simply has to sum the torque on every surface element as a cross product of the element's position, r_i , and thermal kick-back, df_i , as follows:

$$\tau = \int_{S} \boldsymbol{r} \times d\boldsymbol{f} = \sum_{i=1}^{NS} \boldsymbol{r}_{i} \times d\boldsymbol{f}_{i}$$
(6)

2.2 Equation of motion

Given uniform rotation around the shortest axis, the angular momentum L of a spinning body is simply expressed as follows:

225

203

209

$$\boldsymbol{L} = C\omega \boldsymbol{\hat{s}} \tag{7}$$

Here, the direction of L always matches that of the spin pole \hat{s} by neglecting small components of the angular velocity about the other axes. Contrarily to a typical YORP time scale (~ millions of years), the rotation pole is considered to be quickly relaxed to the shortest axis by energy dissipation associated with inelastic distortion (Efroimsky, 2001; Mysen, 230 2006). The YORP-induced torque, τ , in Equation 6 changes the angular momentum of the 231 asteroid, and the equation of motion is expressed as follows:

232

237

238

239 240

24 24

$$\frac{d\boldsymbol{L}}{dt} = \boldsymbol{\tau} \tag{8}$$

Some authors decompose the above equation into three essential parameters to describe the spin state of the body. According to the expression given by Bottke et al. (2006), the equation of motion is expressed by time derivatives of angular velocity ω , obliquity ε , and longitude of precession ψ :

$$\frac{d\omega}{dt} = \frac{\tau_{\omega}}{C} \equiv \frac{\boldsymbol{\tau} \cdot \hat{\boldsymbol{s}}}{C} \tag{9}$$

$$\frac{d\varepsilon}{dt} = \frac{\tau_{\varepsilon}}{C\omega} \equiv \frac{\tau \cdot \hat{\boldsymbol{e}}_{\perp 1}}{C\omega}$$
(10)

$$\frac{d\psi}{dt} = \frac{\tau_{\psi}}{C\omega} \equiv \frac{\boldsymbol{\tau} \cdot \hat{\boldsymbol{e}}_{\perp 2}}{C\omega} \tag{11}$$

The first term, τ_{ω} , is a component of the YORP toque parallel to the spin pole and changes the angular velocity of rotation or the period. The other two components, τ_{ε} and τ_{ψ} , are components along the basis vectors perpendicular to the pole, as shown in the following equations and Figure 1:

$$\hat{\boldsymbol{e}}_{\perp 1} \equiv \frac{(\hat{\boldsymbol{N}} \cdot \hat{\boldsymbol{s}})\hat{\boldsymbol{s}} - \hat{\boldsymbol{N}}}{\sin \varepsilon}$$
(12)

$$\hat{\boldsymbol{e}}_{\perp 2} \equiv \frac{\hat{\boldsymbol{s}} \times \hat{\boldsymbol{N}}}{\sin \varepsilon}$$
(13)

Thus, in Equations 10 and 11, the torque components τ_{ε} and τ_{ψ} change the obliquity of the spin pole and induce precession of rotation, respectively. The obliquity, ε , is defined as the axial tilt angle between the spin normal vector \hat{s} and a normal vector \hat{N} to the body's orbital plane. In fact, although the torque component along $\hat{e}_{\perp 2}$ may excite wobbling rotation, we assume that the spin pole is quickly relaxed toward uniform rotation around the shortest axis by energy dissipation, and thus we focus on changes in ω and ε .



Figure 1. Basis vectors for a spinning body.

3 Results

3.1 Year-averaged torque on Ryugu

For the YORP modeling of asteroid Ryugu, we utilized the orbital elements, spin-pole 254 orientation, and rotation period published by Watanabe et al. (2019) (see Table 1). As a 255 nominal shape model for this study, we chose the 49152-mesh SPC model released on August 256 2, 2019. The mean mesh size of the shape model (i.e., mean diameter of circles of equivalent 257 areas) was 8.4 m. Herein, we present the results of this nominal model and later compare 258 the resultant YORP effects between shape models of different resolutions, release dates, and 259 3D reconstruction methods. We divided the cycle of Ryugu's rotation into 72 equal parts 260 (every 5 degrees of the rotation angle) and computed the YORP torque, τ , at each time 261 step. For a rotation period of 7.6 h, the interval of time steps was 382 s. The simulation 262 was stopped when the asteroid completed one orbit (474 days; 107 288 time steps). 263

Figure 2 illustrates the time variations of each torque component over the cycles of 264 Ryugu's rotation (left panels) and revolution (right panels). As the torque variation is 265 not completely cancelled over the cycles because of Ryugu's irregular shape, the residual 266 induces a secular change in the spin parameters. A net torque, $\bar{\tau}$, can be obtained by 267 averaging the diurnal and seasonal variations. In the nominal case of the SPC-based 49k-268 mesh model with the self-shadowing effect, the year-averaged torque results in $(\bar{\tau}_{\omega}, \bar{\tau}_{\varepsilon}, \bar{\tau}_{\psi}) =$ 269 (-0.161, 0.161, 4.05) N·m. The negative value of the ω -related component implies that 270 the angular velocity of Ryugu is currently decreasing. According to Equation 9 and the 271



Figure 2. Diurnal and seasonal variations of YORP torque components.

moment of inertia of $4.04 \times 10^{16} \text{ kg} \cdot \text{m}^2$, the change in the spin rate of Ryugu corresponds 272 to $\dot{\omega} = -1.71 \times 10^{-6} \text{ deg/day}^2$. The strength of the YORP effect is often characterized by 273 the YORP time scale (Rubincam, 2000), which corresponds to the time required to double 274 or halve the angular velocity ω . For Ryugu, the YORP time scale for doubling the current 275 rotation period corresponds to $t_{7.6h\rightarrow 15.2h} = 0.909$ million years. Note that this time scale 276 is computed assuming that the rotation decelerates at a constant rate. To investigate the 277 detailed process of spin evolution and its time scale, the reorientation of the spin axis must 278 be considered. 279

In addition, the resultant rate of deceleration may vary depending on the meter-scaled differences of an input shape model (Statler, 2009). Although the highest-resolution models described in Watanabe et al. (2019) are well matched regardless of the two different techniques of reconstruction, they may contain artifacts in the polar region where fewer images are obtained, and/or there are slight differences when reducing the resolution of the shape

models. Therefore, we surveyed various versions of shape models to determine the sensitivity 285 of the input model. Table 3 lists the year-averaged torque on each shape model considering 286 the self-shadowing effect. A shape model ID consists of the reconstruction technique (SFM 287 or SPC), number of surface meshes, and release date (in YYYYMMDD format). The YORP 288 simulations are performed only for the low-resolution models of ~ 49 k meshes because de-289 tection of locally generated shadows at every time step is computationally expensive. In all 290 cases, the net torque yields a negative rate of change for angular velocity ω and a positive 291 one for obliquity ε , indicating that Ryugu is currently spinning down and increasing its 292 obliquity toward 180°. The torque component that causes precession is difficult to cancel 293 during a cycle of revolution and yields greater net torque. The deceleration of Ryugu's 294 rotation is consistent with its fast rotation in the past. The spin-down time scales are esti-295 mated assuming that the spin rate has been decreasing at a constant rate from a 3.5-h to 296 a 7.633-h period. The estimated time scales of deceleration vary from 0.58 to 8.7 million 297 years. The cases can be classified into two types: type II, which yields more rapid deceler-298 ation $(t_{3.5h\rightarrow7.6h} < 1 \text{ Myr})$, and type IV, which yields slower deceleration (predominantly 299 $t_{3.5h\rightarrow7.6h} > 1$ Myr). The classification criteria are detailed in Section 3.2. 300

3.2 Obliquity dependence of YORP

The spin rate ω and obliquity ε are essential parameters for simulating the long-term 301 evolution of a rotating body. As the spin-pole direction and obliquity change, the solar irra-302 diation conditions of the body vary. In this section, we demonstrate the dependence of the 303 YORP effect on obliquity and predict Ryugu's spin evolution in millions of years. To achieve 304 this, we calculate the thermal net torque on the asteroid, as in the previous section, but for 305 various obliquities from 0° to 180°. Figure 3 shows the rates of change in ω (dashed) and ε 306 (solid) as functions of ε , as derived from the nominal model (SHAPE_SPC_49k_v20190802) 307 in a similar manner to previous studies (Rubincam, 2000; Vokrouhlický & Čapek, 2002; 308 Čapek & Vokrouhlický, 2004; Bottke et al., 2006). It should be noted that the solid curve 309 τ_{ε}/C (= $\omega\dot{\varepsilon}$) has three "asymptotic" nodes at $\varepsilon = 0^{\circ}$, 90°, and 180°. The thermal torque 310 tends asymptotically toward one of these nodes depending on the initial obliquity ε_0 . For 311 the nominal shape model, the boundaries at $\varepsilon = 37^{\circ}$ and 143° dominate the destiny of the 312 spin evolution and whether the spin pole finally stands upright ($\varepsilon \to 0^\circ$ or 180°) or falls on 313 the orbital plane ($\varepsilon \to 90^{\circ}$). On the other hand, the dashed curve τ_{ω}/C (= $\dot{\omega}$) in Figure 3 314 shows that the rotation of Ryugu decelerates at every obliquity. In this case, Ryugu should 315

Table 3. Thermal net torque and deceleration time scales derived from different shape models. According to Equations 9 to 11, the torque components divided based on the moment of inertia are shown as $\dot{\omega} = \tau_{\omega}/C$, $\omega \dot{\varepsilon} = \tau_{\varepsilon}/C$, and $\omega \dot{\psi} = \tau_{\psi}/C$. The self-shadowing effect is considered.

Model ID	$\dot{\omega}$	$\omega \dot{\varepsilon}$	$\omega \dot{\psi}$	$t_{3.5h \rightarrow 7.6h}$	Classification
$\mathrm{SHAPE}_{-} \dots$	$\times 10^{-6} [\text{deg}/\text{day}^2]$			[Myr]	
SFM 49k v20180705	-5 207	2 282	38 34	0 7032	
SFM_49k_v20180714	-5.834	2.523	39.82	0.6277	
SFM_47k_v20190130	-6.261	2.691	43.28	0.5849	
SPC_49k_v20180705	-5.065	3.410	46.07	0.7230	II
SPC_49k_v20180710	-5.010	2.973	43.03	0.7310	
SPC_49k_v20180717	-4.781	2.785	40.81	0.7660	
$SPC_{49k_v20180719_2}$	-3.647	2.367	39.12	1.004	
SFM_49k_v20180725_2	-4.560	1.775	40.38	0.8030	
$SFM_{49k_v20180804}$	-3.531	1.667	39.73	1.037	
SPC_49k_v20180731	-0.5352	1.561	41.35	6.842	
SPC_49k_v20180810	-0.6878	1.434	39.71	5.324	
SPC_49k_v20180816	-0.4212	1.362	39.81	8.693	
$SPC_{49k_v20180829}$	-0.6152	1.586	42.25	5.952	
$SPC_{49k_v20181014}$	-1.706	1.735	43.17	2.147	117
SPC_49k_v20181109	-1.368	1.719	43.03	2.676	1 V
SPC_49k_v20181204	-0.6796	1.477	42.91	5.388	
SPC_49k_v20190308	-1.207	1.607	43.35	3.035	
SPC_49k_v20190328	-1.069	1.548	42.99	3.426	
$SPC_{49k_v20190802^*}$	-1.705	1.701	42.86	2.148	
$SPC_{49k_v20200323}$	-1.406	1.245	42.22	2.604	

*Nominal shape model in this study



Figure 3. Obliquity dependence of the thermal torque derived from the nominal shape model. The self-shadowing effect is considered. Rates of change in obliquity ε (solid) and spin rate ω (dashed) as functions of the obliquity. The vertical dashed line at $\varepsilon = 171.6^{\circ}$ represents the nominal obliquity observed by Hayabusa2.

reach a permanent spin-down phase at one of the three asymptotic obliquities. The vertical dashed line in Figure 3 represents the current obliquity of Ryugu ($\varepsilon = 171.64^{\circ}$), which was observed by Hayabusa2 (Watanabe et al., 2019). As already mentioned in 3.1, Ryugu is currently considered to be spinning down with the obliquity of the spin pole increasing toward 180°. In contrast, the spin of asteroid 101955 Bennu (a target body of NASA's OSIRIS-REx mission) is accelerating with an obliquity of nearly 180° (Nolan et al., 2019; Hergenrother et al., 2019).

Vokrouhlický and Čapek (2002) performed YORP simulations using randomly generated shapes of virtual asteroids and classified hundreds of the cases according to the obliquity they would settle into after sufficient time. For types I and II, the spin axes will eventually fall ($\varepsilon \rightarrow 90^{\circ}$) and rise ($\varepsilon \rightarrow 0^{\circ}$ or 180°), respectively. These two types account for 80% of the 500 cases. A further 10% of the cases are classified as type III, which have different asymptotic obliquities from the above two types (e.g., $\varepsilon = 30^{\circ}$ and 150° in the shape of asteroid 2063 Bacchus). Type IV is the remaining minority, which has three asymptotic obliquities at $\varepsilon = 0^{\circ}$, 90°, and 180° depending on the initial obliquity. The nominal case plotted in Figure 3 is classified as this type.

Next, we examine the ε -dependence of the net torque on the various shape models in 332 Table 3. The self-shadowing effect is considered in this survey. It is found that the YORP 333 effect on Ryugu results in either type II or IV. The seven cases in type II and 13 cases 334 in type IV are shown separately in Figure 4. Considering the symmetry of the even/odd 335 functions, half of each is omitted from display. The rates of change in the spin rate on the left 336 and obliquity on the right can be observed. In the high-obliquity area around the nominal 337 obliquity ($\varepsilon = 171.6^{\circ}$; marked by the gray dashed line), both types tend toward the state 338 of the upright spin pole. If Ryugu follows type IV evolution, it is necessary for the body to 339 start with an obliquity of over $\sim 140^{\circ}$ to reach the current value. Otherwise, Ryugu's spin 340 axis will become parallel to the orbital plane. When the axis of rotation becomes upright (at 341 an obliquity of 0°, equivalent to 180°), type II shapes tend to yield greater deceleration than 342 type IV shapes. Thus far, the time scale of deceleration depends on subtle differences in the 343 shape models to be entered and the indeterminacy of approximation in our numerical model, 344 but Ryugu is likely to be spinning down with the pole rising toward $\varepsilon = 180^{\circ}$. Changes in 345 Ryugu's spin state over time based on the obliquity dependence is discussed in Section 5.1. 346



Figure 4. Obliquity dependence surveyed for 20 shape models in Table 3. The self-shadowing effect is considered. The left half of each panel shows the thermal torque component required to change the spin rate as a function of obliquity. The right half shows the torque component required to change the obliquity. The 20 models are classified into types II (seven cases in the upper panel) and IV (13 cases in the lower panel) according to Vokrouhlický's criteria.

4 Validity of YORP Simulations

In general, a numerical simulation of the YORP effect strongly depends on small-scale 347 topographic features of the shape model (Statler, 2009; Breiter et al., 2009). To evaluate this 348 uncertainty, we prepared "perturbed" shape models from the nominal model used in Section 349 3 and repeated the YORP simulations (following the numerical experiments by Nolan et 350 al. (2019)). The perturbed models were created by applying noise to the nominal model 351 on a scale similar to the facet size. Each vertex of the original shape model was randomly 352 shifted in the radial direction, for example, within a range of ± 1 m. We demonstrated 1000 353 perturbed models for each noise of ± 1 m and ± 2 m by ignoring the self-shadowing effect. 354 The upper panels in Figure 5 illustrate the nominal shape model and perturbed models with 355 different noise levels. The mean mesh size $\bar{D}_{\rm S}$ of the nominal shape model is 8.4 m, which 356 is hereby defined as the mean diameter of circles of equivalent areas. As the noise increases, 357 more artificial bumps appear on the surface. The histograms show the distributions of 358 the rates of year-averaged acceleration, $\dot{\omega}$. Given the noise within ± 1 m (orange), $\dot{\omega}$ is 359 distributed around the nominal value of $-1.32 \times 10^{-6} \, [rad/day^2]$ with a 1σ uncertainty of 360 $\pm 19\%$. For larger-scale noise in the shape model, the distribution of the YORP acceleration 361 spreads, and some of the cases change to spinning up ($\dot{\omega} > 0$). According to Watanabe et al. 362 (2019), the shape models of 3 million meshes derived from SPC and SfM are well matched 363 within a standard deviation of elevation of ~ 1.5 m. The lower-resolution model used in 364 this study was created by downsizing the 3M-mesh model. Random artifacts on the shape 365 model at the meter scale affect the magnitude of the resultant YORP effect to some extent; 366 however, they are unlikely to change the sign of the acceleration rate. 367

We also provide an overview of the YORP acceleration dependence on the resolution 368 of an input shape model in the case of Ryugu. Ignoring the self-shadowing effect, we 369 performed YORP simulations up to the highest-resolution models. The SPC-based models 370 of each version have four different resolutions (i.e., numbers of surface facets): $N_{\rm S} = 49$ 152, 371 196 608, 786 432, and 3 145 728. The SfM models are also released with approximately the 372 same resolutions. Figure 6 represents the YORP acceleration rates derived from the various 373 shape models as functions of their resolutions. The SPC and SfM models are plotted as 374 blue circles and orange triangles, respectively. Shape models released on the same date are 375 connected with each other. A lower-resolution model was created by reducing the highest-376 resolution model released on the same date. Except for the five shape families (the SPC 377 models released on 2018-07-31, 2018-08-10, 2018-08-16, 2018-08-29, and 2020-03-23), the 378



Figure 5. YORP acceleration/deceleration derived from perturbed shape models. The self-shadowing effect is neglected in this survey.



Figure 6. Rotational acceleration as a function of the resolution of the input shape models. The self-shadowing effect is neglected.

remaining models yielded negative rates of rotational acceleration. In the low-resolution 379 models of \sim 49k meshes, however, we confirmed that all cases resulted in deceleration of 380 rotation when considering the self-shadowing effect (see Table 3). As reported by Breiter et 381 al. (2009), some shape families tend to yield greater rates of acceleration/deceleration as the 382 resolution of the shape models increases without converging to a certain value. The higher 383 resolution model has a larger variance in the slopes of the surface facets, and the magnitude 384 of the resultant acceleration can increase. A detailed thermal model, as described below, 385 is computationally costly, and its convergence to the resolution of the shape model has not 386 yet been confirmed. 387

In this study, we approximated the balance of incoming and outgoing radiation using a simple model based on Rubincam (2000). We examined the extent to which this model works for the YORP simulation on asteroid Ryugu. Rugged topography can block direct sunlight and cast a shadow on the surface. This self-shadowing effect could generate a significant bias in the radiation emitted from the body (Breiter et al., 2009). Herein, we turned self-shadowing on and off depending on the computation time. In addition, reabsorp-

tion of thermal emission from the surrounding ground ("self-heating") and nonzero thermal 394 conductivity could alter the thermal torque exerted on the asteroid (Čapek & Vokrouh-395 lický, 2004). A thermophysical model (TPM) was developed for simulating the distribution 396 of the surface temperature on Ryugu and comparing its results with mid-infrared images 397 obtained from the thermal infrared imager (TIR) on the Hayabusa2 spacecraft (Takita et 398 al., 2017). We performed the TPM simulation using Ryugu's ephemeris and obtained the 300 net torque component required to change the spin rate of Ryugu on August 1, 2018. The 400 200k-mesh SfM model (SHAPE_SFM_200k_v20180804) and a constant thermal inertia of 401 $300 \text{ J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-0.5}$ (tiu) were used for the simulation. Figure 7 compares the diurnal 402 variation of the thermal torque obtained for different thermal models. The blue curve in 403 the lower panel considers the total irradiation energy accounting for the self-shadowing and 404 self-heating effects (upper left panel), but zero conductivity is assumed in accordance with 405 Equation 3. The orange curve represents the time variation of the thermal torque based 406 on the distribution of surface temperature considering nonzero conductivity (upper right 407 panel). The TPM simulation solves the one-dimensional heat conduction equation in the 408 depth direction on each facet with the surface boundary condition according to Equation 1. 409 The gray dashed curve is derived from our implementation of Rubincam's model with the 410 spin phase fitted to the TPM simulation. 411

The blue curve indicates that the local shadows on the surface generate a fine irregular-412 ity in the time variation in the thermal torque. By averaging its ω -related component, the 413 shadowing effect is shown to increase the magnitude of the YORP deceleration compared to 414 the simplest model in this period of time. The daily averaged torque was (1) $\bar{\tau}_{\omega} = -0.365$ 415 $N \cdot m$ in Rubincam's model and (2) $\bar{\tau}_{\omega} = -0.407 N \cdot m$ in the shadowing model. In one 416 revolution cycle, we confirmed that the shadows increased or decreased the magnitude of 417 deceleration randomly. As shown by the orange curve, thermal inertia lowered the contrast 418 of radiation between the hemispheres of daytime and nighttime and lowered the peak of 419 the thermal torque. In addition, a phase delay of approximately 15 min can be observed 420 between the nonzero conductivity model and the others. Nonzero conductivity, however, 421 does not change the total amount of radiation throughout one rotational cycle. Therefore, 422 the phase lag of the thermal torque variation was insignificant to the net acceleration or 423 deceleration, as established previously (Capek & Vokrouhlický, 2004). On the other hand, 424 the delayed radiation due to thermal inertia is considered to be more effective in altering 425 the spin pole direction (Čapek & Vokrouhlický, 2004; Breiter et al., 2007; Mysen, 2008; 426



Figure 7. (Upper) Spatial distribution of the total radiation input to each facet and the surface temperature obtained using the TPM (Takita et al., 2017). (Lower) Time variation of the thermal torque component required to change the spin rate of Ryugu over a diurnal cycle. The blue curve considers the self-shadowing and self-heating effects in addition to our implementation of Rubincam's model (gray curve). Thermal inertia ($\Gamma = 300$ tiu) is also accounted for in the orange curve.

- 427 Scheeres, 2007). As revealed by the infrared observations of TIR and the Mobile Asteroid
- 428 Surface Scout (MASCOT) lander, the thermal inertia of Ryugu's surface material was esti-
- mated as approximately 300 tiu (Okada et al., 2020) or 225 ± 45 tiu (Shimaki et al., 2020),
- $_{430}$ corresponding to a thermal conductivity of ~ 0.1 W/(m · K) (Grott et al., 2019). Although
- 431 Ryugu is spinning at a relatively mild spin rate and is covered with porous boulders of low
- 432 conductivity, the dependence of the net torque on thermal inertia should be investigated in
- 433 the future.

5 Discussion

5.1 YORP-induced spin evolution of Ryugu

We explored the effect of the obliquity of Ryugu's spin pole on the thermally induced 434 torque in Section 3.2. This enables us to predict the long-term evolution of the spin state 435 over millions of years. The top panels in Figure 8 demonstrate representative examples 436 of the ε -dependence of the YORP effect for type II and IV cases. The latest SFM model 437 (SHAPE_SFM_47k_v20190130) and our nominal model (SHAPE_SPC_49k_v20190802) were 438 chosen from each group. Again, the self-shadowing effect was considered, and the current 439 orbit of Ryugu was used (a = 1.19 AU). The middle and bottom panels represent the rotation 440 period and obliquity of the asteroid, respectively, as functions of time after providing initial 441 conditions. The initial rotation period is set to 3.5 h, obliquities range from 100° to 170° . 442 The evolution paths follow the ε -dependence on the corresponding upper panels and the 443 equations of motion in Equations 9 and 10. The currently observed spin parameters of 444 Ryugu are marked at P = 7.632 h and $\varepsilon = 171.6^{\circ}$ by gray dashed lines in each panel. The 445 nominal case of type IV clearly shows that an initial obliquity smaller than 143° cannot 446 achieve an upright spin pole. For the type II example, an upright spin pole can be achieved 447 for any initial obliquity exceeding 90°. The time scale for the spin axis to rise ($\varepsilon \to 180^\circ$) is 448 within a few million years for the nominal case. For a type II case starting with a smaller 449 obliquity, the spin pole can take nearly 5 million years to rise. 450

Moreover, we also surveyed for various initial rotation periods. The contour plots in 451 Figure 9 show the time required for the rotation period to reach 7.632 h as a function of the 452 initial obliquity and period. The same shape models as Figure 8 were used. In the nominal 453 case of type IV, the time scale of rotational deceleration is within a few million years. Note 454 that the possible obliquity must equal or exceed 143° to prevent the spin pole from collapsing 455 onto the orbital plane. For the type II case, the spin-down time scale could be up to 6.5456 million years if the body enters a collapsed spin-pole state with a small deceleration rate. 457 Although the time scale varies depending on the input shape models, the path of the spin 458 evolution is as described above. 459

As mentioned above, the YORP-induced torque is responsible for keeping the spin pole perpendicular to the orbital plane. However, the current obliquity of Ryugu is 172°, and it does not perfectly match 180°. Considering the relatively short time scale of change in the spin-pole direction, Ryugu is likely to have experienced a spin-related disturbance event



Figure 8. Paths of spin evolution according to representative examples of obliquity dependence on the YORP effect for type II (left) and type IV (right) cases. The top panels show the dependence of the thermal torque on obliquity. The middle and bottom panels plot the temporal evolution of the rotation period P and obliquity ε , respectively, assuming an initial period of 3.5 h and obliquities in the range of 100° – 170°. The horizontal gray dashed lines indicate the current period and obliquity of Ryugu.



Figure 9. Time required to decelerate to the current rotation period of Ryugu as a function of the initial obliquity, ε_0 , and period, P_0 for a type II (left) and type IV evolution (right).

within the last several million years. As a single event, a close encounter with a planet 464 could potentially alter radically the angular momentum of a near-Earth asteroid (Scheeres 465 et al., 2000; Benson et al., 2019). The spin modification due to the gravitational torque of 466 a planet strongly depends on the hyperbolic orbit and spin-pole direction of the asteroid 467 with respect to the planet. The kinetic energy of an impactor could also directly alter the 468 angular momentum of an asteroid. The effect of an impact event on Ryugu is estimated 469 in Section 5.2. A topographic change caused by crater formation could have altered the 470 YORP effect on the body over its geological time scale. According to the list of craters on 471 Ryugu compiled by Noguchi et al. (2021), the total area of all these craters is 3.65×10^5 m², 472 which corresponds to approximately 13% of the total surface area of the body. In addition, 473 prediction of non-uniform rotation is left for future work because the thermal torque can 474 cause precession of the spin pole. 475

5.2 Effect of an impact event

482

The Hayabusa2 mission conducted an artificial cratering experiment using a small carryon impactor (SCI), which revealed that the artificial crater on Ryugu was formed in the gravity-dominated regime owing to the significantly small cohesion of its surface materials (Arakawa et al., 2020). According to the conventional scaling law in this regime and other parameters from the impact conditions of the SCI experiment, Arakawa et al. (2020) provided the scaling law for the cohesionless surface of Ryugu as follows:

$$\pi_{\rm R} = 0.62 \times \pi_2^{-0.17} \pi_4^{0.0014} \tag{14}$$

where $\pi_{\rm R}$, π_2 , and π_4 are the conventional dimensionless parameters (Housen & Holsapple, 483 2011). Using this scaling law and the size of the largest crater observed on Ryugu, the 484 maximum change in the rotation parameters owing to an impact can be estimated. The 485 largest crater, Urashima, is 246.9 ± 7.0 m in diameter and is located near the equator 486 (Noguchi et al., 2021). The other collision parameters are listed in Table 4. Therefore, we 487 considered a chondritic meteorite of radius ~ 1 m that collided with a rotating spherical 488 body similar to Ryugu at the mean impact velocity in the main belt. Assuming that the 489 target body acquired all the kinetic energy of the impactor without any loss, the maximum 490 change in the angular momentum was calculated to be $\Delta L = 4.1 \times 10^{10} \text{ kg} \cdot \text{m}^2/\text{s}$ when 491 the impactor collided in a tangential direction to the spherical target. This increase is less 492 than 1% of the original angular momentum of Ryugu, $L = 9.2 \times 10^{12} \text{ kg} \cdot \text{m}^2/\text{s}$. Even if 493 the impactor collided in the east-west direction at the equator, the change in the rotation 494 period would be limited to approximately 120 s in both the acceleration and deceleration 495 cases. In the event of a north-south collision, the direction of the spin pole would change 496 by a maximum of only 0.25° . In reality, the change would be significantly smaller because 497 of energy dissipation, etc. It can be concluded that even the formation of the largest crater 498 on Ryugu would not have been able to disturb its rotation to such an extent. 499

5.3 Implications for geologic history of Ryugu

⁵⁰⁰ Despite the uncertainty in the numerical YORP modeling, this study strongly suggests ⁵⁰¹ that the YORP effect could have been a major factor in the rotational deceleration of Ryugu ⁵⁰² since its currently observed shape was formed. Our YORP simulation based on Ryugu's ⁵⁰³ shape model yielded rates of change in angular velocity of $(-0.42 - -6.3) \times 10^{-6} \text{ deg/day}^2$ ⁵⁰⁴ (see Table 3). In most cases, the spin pole of Ryugu was maintained for obliquities of nearly

Parameters	Notation	Value	Unit
Radius of Urashima crater	R	123	m
Impact velocity [*]	u	5300	m/s
Target density	ρ	1190	$\rm kg/m^3$
Target gravity ^{**}	g	1.2×10^{-4}	m/s^2
Projectile radius	a	1.07	m
Projectile density	δ	3000	$\rm kg/m^3$

Table 4. Impact parameters used to estimate the maximum change in the rotation of Ryugu.

*Equal to mean impact velocity in the main belt (Bottke et al., 1994). **Corresponding to a spherical body with a GM of 30 m³/s² and an equatorial radius of 502 m (Watanabe et al., 2019).

⁵⁰⁵ 180°. In this obliquity range, the deceleration rate can be considered to be approximately ⁵⁰⁶ constant in all cases (see the left side of Figure 4). Assuming a constant deceleration at ⁵⁰⁷ these rates, it would have taken 0.58 - 8.7 million years to alter the rotation period from 3.5 ⁵⁰⁸ to 7.6 h. This is consistent with the time scales (0.3–8.1 Ma) of spin deceleration estimated ⁵⁰⁹ by Morota et al. (2020) based on crater counting, as previously discussed in Section 1.1.

As the YORP effect depends on the body's shape, the deceleration time scale corre-510 sponds to the time that has passed since the occurrence of a major change in topography 511 during the fast rotation phase. Statistical analysis of fresher craters with bluer spectra on 512 Ryugu indicated that the asteroid experienced surface reddening due to solar heating when 513 it migrated from the inner main belt to the near-Earth orbit 0.3–8 million years ago (Morota 514 et al., 2020). Hence, our estimated time scale of the rotational deceleration is comparable 515 to the time that Ryugu has spent in the near-Earth orbit. A recent paper by Cho et al. 516 (2021) estimated the surface age of each geological unit on the asteroid. According to these 517 crater statistics, the equatorial ridge is the oldest terrain on Ryugu, thought to have formed 518 23 - 30 million years ago. This early deformation is consistent with the direct formation of 519 the top shape during the accumulation of the rubble pile (Michel et al., 2020). However, 520 the YORP deceleration time scale is much shorter than the formation age of the equatorial 521 ridge. Therefore, a more recent resurfacing event may have impacted the YORP effect on 522 Ryugu, becoming a tipping point in its dynamical history in terms of spin. A corresponding 523

geological event could be the formation of the largest crater, *Urashima*, or the formation of the western bulge, which is considered to be a younger unit with fewer craters than the eastern hemisphere (Hirata et al., 2020). The formation ages of these units are estimated to be 5 - 12 and 2 - 9 Ma, respectively, depending on the timing of the orbital migration of Ryugu from the main belt to its near-Earth orbit (Cho et al., 2021). Our estimate of the deceleration time scale is comparable with the ages of these events, and it is possible that Ryugu had been spinning at a fast rate until the event time.

During fast rotation at a period of ~ 3.6 h, the Coriolis force may accumulate impact 531 ejecta asymmetrically on a spinning body (Hirata et al., 2021). Some of the major craters 532 in the equatorial region (e.g., Urashima, Cendrillon, and Kolobok) have higher rims on the 533 west sides. These east-west asymmetric craters may bias the YORP effect on Ryugu. In 534 the future, we need to consider the possibility that the formation of multiple craters has 535 gradually altered the spin history of the body, or that the inward orbital migration decreased 536 the heliocentric distance and hastened the spin alteration. In addition, roughness smaller 537 than the size of the meshes (centimeter to decimeter) may have contributed to the increase 538 in spin rate caused by thermal torque, known as the tangential YORP effect (Golubov & 539 Krugly, 2012; Golubov et al., 2014; Golubov, 2017). The boulder-rich surface of Ryugu 540 tends to impede rotational deceleration caused by the normal YORP and extend the time 541 scale of the spin-down. As observed by the TIR on Hayabusa2, the surface roughness induces 542 thermal infrared beaming toward the Sun (Okada et al., 2020), which also could dampen 543 the magnitude of the YORP effect (Rozitis & Green, 2011, 2012). 544

The YORP simulation in this study also predicts the change in the direction of Ryugu's 545 rotation axis. The currently observed shape of Ryugu yields the stability of the spin pole at 546 an obliquity of 180°. For Ryugu, it is likely that the spin pole has remained perpendicular 547 to the orbital plane even if a spin disturbance event has occurred, as explained in Section 548 5.1. In addition to the mass-shedding process on the surface of Ryugu, the pole stability 549 may contribute to the formation of the latitudinal pattern in the visible and near-infrared 550 spectra (Sugita et al., 2019). This may have protected the polar regions from sunlight and 551 maintained their bluer spectra (Tatsumi et al., in prep.). 552

6 Conclusion

In this study, we investigated the YORP-induced spin evolution of asteroid Ryugu. 553 We also confirmed that a simplified thermal model assuming zero thermal conductivity can 554 compute the YORP torque exerted on Ryugu with sufficient accuracy. The approximation 555 reduced the computational time and allowed us to examine various versions of the shape 556 models. Regardless of the differences between the 3D construction methods and input 557 image datasets, it is suggested that Ryugu is currently spinning down at a rate of (-0.42)558 -6.3 × 10⁻⁶ deg/day², and a reasonable time scale of 0.58 - 8.7 million years is given 559 for the spin alteration that has occurred since the fast rotation in the past. Combined with 560 Hayabusa2 remote sensing data, our findings on the dynamical and geological history of 561 Ryugu will contribute to the interpretation of future analyses of samples returning to Earth 562 at the end of 2020. 563

564 Acknowledgments

We would like to thank all members of the Hayabusa2 mission team for their support of the data acquisition. All data will be available at the JAXA Data Archives and Transmission System (DARTS) at https://www.darts.isas.jaxa.jp/planet/project/hayabusa2/. This study is supported by the JSPS KAKENHI No. JP17H06459 ("Aqua Planetology") and the JSPS Core-to-Core Program "International Network of Planetary Sciences". We would like to thank Editage (www.editage.com) for English language editing.

References

- Arakawa, M., Saiki, T., Wada, K., Ogawa, K., Kadono, T., Shirai, K., ... Miura, A. (2020). An artificial impact on the asteroid (162173) Ryugu formed a crater in the gravitydominated regime. *Science*. doi: 10.1126/science.aaz1701
- Benson, C. J., Scheeres, D. J., & Moskovitz, N. A. (2019). Spin state evolution of asteroid (367943) Duende during its 2013 earth flyby. *Icarus*, 113518. Retrieved from http:// www.sciencedirect.com/science/article/pii/S0019103519304075 doi: https:// doi.org/10.1016/j.icarus.2019.113518
- Bottke, W. F., Nolan, M. C., Greenberg, R., & Kolvoord, R. A. (1994). Velocity Distributions among Colliding Asteroids. *Icarus*, 107(2), 255–268. doi: 10.1006/ icar.1994.1021
- Bottke, W. F., Vokrouhlický, D., Rubincam, D. P., & Nesvorný, D. (2006, may). THE

YARKOVSKY AND YORP EFFECTS: Implications for Asteroid Dynamics. Annual Review of Earth and Planetary Sciences, 34(1), 157–191. Retrieved from http:// www.annualreviews.org/doi/10.1146/annurev.earth.34.031405.125154 doi: 10 .1146/annurev.earth.34.031405.125154

- Breiter, S., Bartczak, P., Czekaj, M., Oczujda, B., & Vokrouhlický, D. (2009). The YORP effect on 25 143 Itokawa. Astronomy and Astrophysics, 507(2), 1073–1081. doi: 10.1051/0004-6361/200912543
- Breiter, S., Michalska, H., Vokrouhlický, D., & Borczyk, W. (2007). Radiation-induced torques on spheroids. Astronomy and Astrophysics, 471(1), 345–353. doi: 10.1051/ 0004-6361:20077313
- Čapek, D., & Vokrouhlický, D. (2004). The YORP effect with finite thermal conductivity. *Icarus*, 172(2), 526–536. doi: 10.1016/j.icarus.2004.07.003
- Cho, Y., Morota, T., Kanamaru, M., Takaki, N., Yumoto, K., Ernst, C. M., ... Sugita, S. (2021). Geologic History and Crater Morphology of Asteroid (162173) Ryugu. *Journal of Geophysical Research - Planets*. Retrieved from https://www.essoar.org/ action/showAuthorDashboard?state=submitted doi: 10.1002/essoar.10506689.1
- Efroimsky, M. (2001). Relaxation of wobbling asteroids and comets Theoretical problems, perspectives of experimental observation. *Planetary and Space Science*, 49(9), 937– 955. doi: 10.1016/S0032-0633(01)00051-4
- Gaskell, R., Barnouin-Jha, O., Scheeres, D., Mukai, T., Hirata, N., Abe, S., ... Kominato, T. (2006). Landmark Navigation Studies and Target Characterization in the Hayabusa Encounter with Itokawa. AIAA/AAS Astrodynamics Specialist Conference and Exhibit. doi: 10.2514/6.2006-6660
- Gaskell, R. W., Barnouin-Jha, O. S., Scheeres, D. J., Konopliv, A. S., Mukai, T., Abe, S.,
 ... Demura, H. (2008). Characterizing and navigating small bodies with imaging data. *Meteoritics & Planetary Science*, 43(6), 1049–1061. Retrieved from https://onlinelibrary.wiley.com/doi/abs/10.1111/j.1945-5100.2008.tb00692.x doi: 10.1111/j.1945-5100.2008.tb00692.x
- Golubov, O. (2017). Analytic Model for Tangential YORP. The Astronomical Journal, 154(6), 238. doi: 10.3847/1538-3881/aa88ba
- Golubov, O., & Krugly, Y. N. (2012). Tangential component of the YORP effect. Astrophysical Journal Letters, 752(1). doi: 10.1088/2041-8205/752/1/L11
- Golubov, O., Scheeres, D. J., & Krugly, Y. N. (2014). A three-dimensional model of

tangential yorp. Astrophysical Journal, 794(1). doi: 10.1088/0004-637X/794/1/22

- Grott, M., Knollenberg, J., Hamm, M., Ogawa, K., Jaumann, R., Otto, K. A., ... Moussi-Soffys, A. (2019). Low thermal conductivity boulder with high porosity identified on C-type asteroid (162173) Ryugu. doi: 10.1038/s41550-019-0832-x
- Hergenrother, C. W., Maleszewski, C. K., Nolan, M. C., Li, J. Y., Drouet d'Aubigny, C. Y., Shelly, F. C., ... Marty, B. (2019). The operational environment and rotational acceleration of asteroid (101955) Bennu from OSIRIS-REx observations. *Nature Communications*, 10(1). doi: 10.1038/s41467-019-09213-x
- Hirabayashi, M., Tatsumi, E., Miyamoto, H., Komatsu, G., Sugita, S., Watanabe, S.-i., ... Tsuda, Y. (2019). The Western Bulge of 162173 Ryugu Formed as a Result of a Rotationally Driven Deformation Process. *The Astrophysical Journal*, 874(1), L10. doi: 10.3847/2041-8213/ab0e8b
- Hirata, N., Morota, T., Cho, Y., Kanamaru, M., ichiro Watanabe, S., Sugita, S., ... ichi Iijima, Y. (2020). The spatial distribution of impact craters on Ryugu. *Icarus*, 338. doi: 10.1016/j.icarus.2019.113527
- Hirata, N., Namiki, N., Yoshida, F., Matsumoto, K., Noda, H., Senshu, H., ... ichiro Watanabe, S. (2021). Rotational effect as the possible cause of the east-west asymmetric crater rims on Ryugu observed by LIDAR data. *Icarus*. doi: 10.1016/ j.icarus.2020.114073
- Housen, K. R., & Holsapple, K. A. (2011). Ejecta from impact craters. *Icarus*, 211(1), 856–875. doi: 10.1016/j.icarus.2010.09.017
- Kaasalainen, M., Durech, J., Warner, B. D., Krugly, Y. N., & Gaftonyuk, N. M. (2007, mar). Acceleration of the rotation of asteroid 1862 Apollo by radiation torques. *Nature*, 446(7134), 420-422. Retrieved from http://www.nature.com/articles/ nature05614 doi: 10.1038/nature05614
- Kitazato, K., Milliken, R. E., Iwata, T., Abe, M., Ohtake, M., Matsuura, S., ... Tsuda, Y. (2019). The surface composition of asteroid 162173 Ryugu from Hayabusa2 nearinfrared spectroscopy. *Science*, 364 (6437), 272–275. doi: 10.1126/science.aav7432
- Lowry, S. C., Fitzsimmons, A., Pravec, P., Vokrouhlický, D., Boehnhardt, H., Taylor, P. A., ... Kusnirák, P. (2007). Direct detection of the asteroidal YORP effect. *Science*, 316(5822), 272–274. doi: 10.1126/science.1139040
- Lowry, S. C., Weissman, P. R., Duddy, S. R., Rozitis, B., Fitzsimmons, A., Green, S. F., ... van Oers, P. (2014). The internal structure of asteroid (25143) Itokawa as revealed

by detection of YORP spin-up. *Astronomy & Astrophysics*, 562, A48. Retrieved from https://doi.org/10.1051/0004-6361/201322602 doi: 10.1051/0004-6361/201322602

- Michel, P., Ballouz, R.-L., Barnouin, O. S., Jutzi, M., Walsh, K. J., May, B. H., ... Lauretta, D. S. (2020, dec). Collisional formation of top-shaped asteroids and implications for the origins of Ryugu and Bennu. *Nature Communications*, 11(1), 2655. Retrieved from http://www.nature.com/articles/s41467-020-16433-z doi: 10.1038/s41467-020 -16433-z
- Michikami, T., Honda, C., Miyamoto, H., Hirabayashi, M., Hagermann, A., Irie, T., ... Sugita, S. (2019). Boulder size and shape distributions on asteroid Ryugu. *Icarus*, 331, 179–191. doi: 10.1016/j.icarus.2019.05.019
- Morota, T., Sugita, S., Cho, Y., Kanamaru, M., Tatsumi, E., Sakatani, N., ... Tsuda, Y. (2020). Sample collection from asteroid (162173) Ryugu by Hayabusa2: Implications for surface evolution. *Science*, 368(6491), 654–659. doi: 10.1126/science.aaz6306
- Mysen, E. (2006). Canonical rotation variables and non-Hamiltonian forces: Solar radiation pressure effects on asteroid rotation. *Monthly Notices of the Royal Astronomical Society*, 372(3), 1345–1350. doi: 10.1111/j.1365-2966.2006.10944.x
- Mysen, E. (2008). Dynamical effects of thermal emission on asteroids (Vol. 383) (No. 1). doi: 10.1111/j.1745-3933.2007.00405.x
- Noguchi, R., Hirata, N., Hirata, N., Shimaki, Y., Nishikawa, N., Tanaka, S., ... Watanabe, S.-i. (2021). Crater depth-to-diameter ratios on asteroid 162173 Ryugu d/D of craters on Ryugu. *Icarus*, 354, 114016. Retrieved from http://www.sciencedirect.com/ science/article/pii/S0019103520303791 doi: https://doi.org/10.1016/j.icarus .2020.114016
- Nolan, M. C., Howell, E. S., Scheeres, D. J., McMahon, J. W., Golubov, O., Hergenrother, C. W., ... Lauretta, D. S. (2019). Detection of Rotational Acceleration of Bennu Using HST Light Curve Observations. *Geophysical Research Letters*, 46(4), 1956–1962. doi: 10.1029/2018GL080658
- Okada, T., Fukuhara, T., Tanaka, S., Taguchi, M., Arai, T., Senshu, H., ... Tsuda, Y. (2020). Highly porous nature of a primitive asteroid revealed by thermal imaging. *Nature*, 579(7800), 518–522. doi: 10.1038/s41586-020-2102-6
- Rozitis, B., & Green, S. F. (2011). Directional characteristics of thermal-infrared beaming from atmosphereless planetary surfaces - a new thermophysical model. *Monthly Notices*

of the Royal Astronomical Society, 415(3), 2042–2062. doi: 10.1111/j.1365-2966.2011 .18718.x

- Rozitis, B., & Green, S. F. (2012). The influence of rough surface thermal-infrared beaming on the Yarkovsky and YORP effects. Monthly Notices of the Royal Astronomical Society, 423(1), 367–388. doi: 10.1111/j.1365-2966.2012.20882.x
- Rubincam, D. P. (2000). Radiative Spin-up and Spin-down of Small Asteroids. *Icarus*, 148(1), 2–11. doi: 10.1006/icar.2000.6485
- Scheeres, D. J. (2007). The dynamical evolution of uniformly rotating asteroids subject to YORP. *Icarus*, 188(2), 430–450. doi: 10.1016/j.icarus.2006.12.015
- Scheeres, D. J. (2015). Landslides and Mass shedding on spinning spheroidal asteroids. *Icarus*, 247, 1–17. doi: 10.1016/j.icarus.2014.09.017
- Scheeres, D. J., Ostro, S. J., Werner, R. A., Asphaug, E., & Hudson, R. S. (2000). Effects of Gravitational Interactions on Asteroid Spin States. *Icarus*, 147(1), 106–118. doi: 10.1006/icar.2000.6443
- Seveček, P., Golubov, O., Scheeres, D. J., & Krugly, Y. N. (2016, aug). Obliquity dependence of the tangential YORP. Astronomy & Astrophysics, 592, A115. Retrieved from http://www.aanda.org/10.1051/0004-6361/201628746 doi: 10.1051/0004-6361/ 201628746
- Shimaki, Y., Senshu, H., Sakatani, N., Okada, T., Fukuhara, T., Tanaka, S., ... ichiro Watanabe, S. (2020). Thermophysical properties of the surface of asteroid 162173 Ryugu: Infrared observations and thermal inertia mapping. *Icarus*, 348. doi: 10.1016/ j.icarus.2020.113835
- Statler, T. S. (2009). Extreme sensitivity of the YORP effect to small-scale topography. *Icarus*, 202(2), 502–513. doi: 10.1016/j.icarus.2009.03.003
- Sugita, S., Honda, R., Morota, T., Kameda, S., Sawada, H., Tatsumi, E., ... Tsuda, Y. (2019, mar). The geomorphology, color, and thermal properties of Ryugu: Implications for parent-body processes. *Science*, 364(6437), eaaw0422. Retrieved from https:// www.sciencemag.org/lookup/doi/10.1126/science.aaw0422 doi: 10.1126/science .aaw0422
- Szeliski, R. (2011). Computer vision: algorithms and applications. Choice Reviews Online, 48(09), 48–5140–48–5140. doi: 10.5860/choice.48-5140
- Tachibana, S., Abe, M., Arakawa, M., Fujimoto, M., Iijima, Y., Ishiguro, M., ... Kuninaka,H. (2014). Hayabusa2: Scientific importance of samples returned from C-type near-

Earth asteroid (162173) 1999 JU3. *Geochemical Journal*, 48(6), 571–581. doi: 10 .2343/geochemj.2.0350

- Takita, J., Senshu, H., & Tanaka, S. (2017). Feasibility and Accuracy of Thermophysical Estimation of Asteroid 162173 Ryugu (1999 JU3) from the Hayabusa2 Thermal Infrared Imager (Vol. 208) (No. 1-4). doi: 10.1007/s11214-017-0336-x
- Tatsumi, E., Domingue, D., Schröder, S., Yokota, Y., Kuroda, D., Ishiguro, M., ... Sugita, S. (2020). Global photometric properties of (162173) Ryugu. Astronomy and Astrophysics. doi: 10.1051/0004-6361/201937096
- Tatsumi, E., & Sugita, S. (2018). Cratering efficiency on coarse-grain targets: Implications for the dynamical evolution of asteroid 25143 Itokawa. *Icarus*. doi: 10.1016/j.icarus .2017.09.004
- Taylor, P. A., Margot, J. L., Vokrouhlický, D., Scheeres, D. J., Pravec, P., Lowry, S. C.,
 ... Magri, C. (2007). Spin rate of asteroid (54509) 2000 PH5 increasing due to the
 YORP effect. Science, 316(5822), 274–277. doi: 10.1126/science.1139038
- Tsuda, Y., Yoshikawa, M., Saiki, T., Nakazawa, S., & ichiro Watanabe, S. (2019). Hayabusa2 Sample return and kinetic impact mission to near-earth asteroid Ryugu. Acta Astronautica, 156, 387–393. doi: 10.1016/j.actaastro.2018.01.030
- Vokrouhlický, D., & Čapek, D. (2002). Yorp-induced long-term evolution of the spin state of small asteroids and meteoroids: Rubincam's approximation. *Icarus*, 159(2), 449–467. doi: 10.1006/icar.2002.6918
- Watanabe, S., Hirabayashi, M., Hirata, N., Hirata, N., Noguchi, R., Shimaki, Y., ... Tsuda,
 Y. (2019). Hayabusa2 arrives at the carbonaceous asteroid 162173 Ryugu-A spinning top-shaped rubble pile. *Science*, 364 (6437), 268–272. doi: 10.1126/science.aav8032
- Watanabe, S., Tsuda, Y., Yoshikawa, M., Tanaka, S., Saiki, T., & Nakazawa, S. (2017). *Hayabusa2 Mission Overview* (Vol. 208) (No. 1-4). doi: 10.1007/s11214-017-0377-1
- Durech, J., Vokrouhlický, D., Baransky, A. R., Breiter, S., Burkhonov, O. A., Cooney,
 W., ... Warner, B. D. (2012). Analysis of the rotation period of asteroids (1865)
 Cerberus, (2100) Ra-Shalom, and (3103) Eger-search for the YORP effect. Astronomy and Astrophysics. doi: 10.1051/0004-6361/201219396
- Durech, J., Vokrouhlický, D., Kaasalainen, M., Higgins, D., Krugly, Y. N., Gaftonyuk, N. M., ... Dyvig, R. R. (2008, oct). Detection of the YORP effect in asteroid (1620) Geographos. Astronomy and Astrophysics, 489(2), L25-L28. Retrieved from http://www.aanda.org/10.1051/0004-6361:200810672 doi: 10.1051/0004-6361:

200810672

- Ďurech, J., Vokrouhlický, D., Kaasalainen, M., Weissman, P., Lowry, S. C., Beshore, E., ...
 Kitazato, K. (2008, sep). New photometric observations of asteroids (1862) Apollo and (25143) Itokawa An analysis of YORP effect. Astronomy and Astrophysics, 488(1), 345–350. Retrieved from http://www.aanda.org/10.1051/0004-6361:200809663
- Ďurech, J., Vokrouhlický, D., Pravec, P., Hanuš, J., Farnocchia, D., Krugly, Y. N., ...
 Warner, B. D. (2018, jan). YORP and Yarkovsky effects in asteroids (1685) Toro, (2100) Ra-Shalom, (3103) Eger, and (161989) Cacus. Astronomy & Astrophysics, 609, A86. Retrieved from https://www.aanda.org/10.1051/0004-6361/201731465 doi: 10.1051/0004-6361/201731465