Joint inversion of receiver functions and apparent incidence angles for sparse seismic data

Rakshit Joshi¹, Brigitte Knapmeyer-Endrun², Klaus Mosegaard³, Heiner Igel⁴, and Ulrich Christensen⁵

¹Max Planck Institute for Solar System Research
²Erdbebenstation Bensberg
³Niels Bohr Institute, University of Copenhagen
⁴Ludwig-Maximilians University, Munich
⁵Max-Planck-Institut für Sonnensystemforschung

November 24, 2022

Abstract

The estimation of crustal structure and thickness is instrumental in understanding the formation and evolution of terrestrial planets. Initial planetary missions with seismic instrumentation on board face the additional challenge of dealing with seismic activity levels that are only poorly constrained a priori. For example, the lack of plate tectonics on Mars leads to low seismicity which could in turn hinder the application of many terrestrial data analysis techniques. Here we propose using a joint inversion of receiver functions and apparent incidence angles, which contain information on absolute S-wave velocities of the subsurface. Since receiver function inversions suffer from a velocity depth trade-off, we in addition exploit a simple relation which defines apparent S-wave velocity as a function of observed apparent P-wave incidence angles to constrain the parameter space. We then use the Neighbourhood Algorithm for the inversion of a suitable joint objective function. The resulting ensemble of models is then used to derive uncertainty estimates for each model parameter. In preparation for analysis of data from the InSight mission, we show the application of our proposed method on Mars synthetics and sparse terrestrial data sets from different geological settings using both single and multiple events. We use information theoretic statistical tests as a model selection criteria and discuss their relevance and implications in a seismological framework.

Joint inversion of receiver functions and apparent incidence angles for sparse seismic data

Rakshit Joshi^{1,4}, Brigitte Knapmeyer-Endrun², Klaus Mosegaard³, Heiner Igel⁴, Ulrich R. Christensen¹

¹Max-Planck-Institute for Solar System Research, Göttingen, Germany ²Bensberg Observatory, University of Cologne, Cologne, Germany ³Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark ⁴Ludwig-Maximilians-Universitt, Munich, Germany

Key Points:

1

2

3

9

15

10	• We propose the joint inversion of receiver functions and apparent S-wave velocity
11	curves to estimate crustal thickness
12	• Using the Neighbourhood Algorithm, we show how a full uncertainty estimate can be
13	computed from an ensemble solution
14	• The method is applied to Martian synthetics and terrestrial data sets comprising
15	single and multiple events

Corresponding author: Rakshit Joshi, joshir@mps.mpg.de

16 Abstract

The estimation of crustal structure and thickness is instrumental in understanding 17 the formation and evolution of terrestrial planets. Initial planetary missions with seismic 18 instrumentation on board face the additional challenge of dealing with seismic activity levels 19 that are only poorly constrained a priori. For example, the lack of plate tectonics on 20 Mars leads to low seismicity which could in turn hinder the application of many terrestrial 21 data analysis techniques. Here we propose using a joint inversion of receiver functions 22 and apparent incidence angles, which contain information on absolute S-wave velocities 23 24 of the subsurface. Since receiver function inversions suffer from a velocity depth tradeoff, we in addition exploit a simple relation which defines apparent S-wave velocity as a 25 function of observed apparent P-wave incidence angles to constrain the parameter space. 26 We then use the Neighbourhood Algorithm for the inversion of a suitable joint objective 27 function. The resulting ensemble of models is then used to derive uncertainty estimates 28 for each model parameter. In preparation for analysis of data from the InSight mission, 29 we show the application of our proposed method on Mars synthetics and sparse terrestrial 30 data sets from different geological settings using both single and multiple events. We use 31 information theoretic statistical tests as a model selection criteria and discuss their relevance 32 and implications in a seismological framework. 33

³⁴ 1 Introduction

Receiver function (RF) analysis is a powerful technique to gain information about the 35 discontinuities in the crust and upper mantle beneath a single three-component seismic 36 station. RFs are essentially time series that are sensitive to the structure near the receiver. 37 The basic principle behind this method is that when a seismic wave is incident upon a 38 discontinuity, mode conversion between the compressional (P) and shear (S) waves will 39 take place in addition to the generation of reflected and transmitted waves. The resulting 40 converted wave (Ps or Sp) will have a time offset with respect to its parent wave, and this 41 time offset is directly proportional to the depth of the discontinuity and the velocity of 42 the layers above. In addition to the direct converted waves, the multiples resulting from 43 reflections and conversions between the discontinuity and the free surface can provide further 44 constraints on the layer thickness and help to resolve the depth-velocity trade-off. The RF 45 can be obtained by deconvolving the vertical component from the radial component of a 46 teleseismic event recorded on a three-component seismometer (Langston, 1979; Owens et al., 47 1987; Ammon, 1991). Since only a small percentage of the incident energy is converted at a 48 discontinuity, it is difficult to observe these conversions in a single seismogram. A number of 49 RFs can instead be used to measure the crustal thickness and average v_P/v_S ratios by H-k 50 (crustal thickness - average v_P/v_S) stacking for individual stations (Zhu & Kanamori, 2000; 51 Helffrich & Thompson, 2010) or imaging by CCP (Common Conversion Point) stacking of 52 data from many stations (Dueker & Sheehan, 1997). This, however, requires assumptions 53 on the velocity structure. 54

One method to obtain a detailed velocity structure is to directly invert the calculated 55 RFs using linearised iterative procedures, but Ammon et al. (1990) showed that such in-56 versions of RF contain an inherent trade-off between the depth to a discontinuity and the 57 velocity above. The primary sensitivity of the RF inversion is to velocity contrasts and rela-58 tive travel time, not to absolute velocity. This lack of sensitivity to absolute velocity results 59 from the relative S - P travel time constraints along with the limited range of horizontal 60 slowness contained in the data (Ammon et al., 1990). Thus RF data sets are generally 61 inverted jointly with other independent data sets that provide additional constraints on ab-62 solute shear wave velocities like surface wave dispersion curves (e.g. Du & Foulger (1999); 63 Julia et al. (2000)), or Rayleigh wave ellipticity (Chong et al., 2016). One such relation 64 which has not been heavily exploited is between apparent S-wave velocities and P-wave 65 polarisation. The polarisation of body waves has been traditionally used in seismology to 66

study the anisotropy of crustal and upper mantle structures (Schulte-Pelkum et al., 2001; 67 Fontaine et al., 2009). But the P-wave polarisation can also be used to constrain the near 68 surface shear wave speed. Svenningsen & Jacobsen (2007) showed that the amplitudes of 69 the vertical (Z) and radial (R) components of the P-receiver function at zero time is directly 70 related to the polarisation of P-waves. Deconvolution removes the complex waveform of the 71 incoming P-waves, which dominate the Z component. Hence the Z RF is an approximate 72 zero-phase spike with arrival instant at exactly t=0, where the time is measured relative to 73 the P-wave arrival. This can be used to estimate the apparent P-wave incidence without 74 influences from the P-wave coda. Further, filtering at successively long periods, a frequency 75 dependent apparent shear wave velocity profile can be obtained (Svenningsen & Jacobsen, 76 2007; Knapmeyer-Endrun et al., 2018) which can be used as an effective independent data 77 set to be jointly inverted with the RFs. 78

Svenningsen & Jacobsen (2007) used a linearised inversion of apparent S-wave velocity 79 curves and demonstrated its independence of the starting model. Hannemann et al. (2016) 80 applied the method to an OBS data set and used a grid search method concluding that 81 the method is usable for single station estimates of the local S-wave velocity structure 82 beneath the ocean bottom. Schiffer et al. (2016) used an iterative least squares method 83 to jointly invert apparent velocity curves and RFs utilising a minimum number of layers 84 (6-8). Knapmeyer-Endrun et al. (2018) used a grid search over parameter space to invert 85 the S-wave velocity curve for crustal structure at several Earth stations with varying geology 86 and synthetic Mars data. It has also been shown that a priori S-wave velocity information 87 deduced from P-wave polarisations can be useful when inverting RF waveforms (Peng et 88 al., 2012). Park & Ishii (2018) further showed that the S-wave polarisation is sensitive to 89 both the compressional and shear wave speeds, and successfully combined P- and S-wave 90 polarisation directions measured by principal component analysis to derive the distribution 91 of near-surface P- and S-wave speeds in Japan. 92

In this paper, we use a modified version of the Neighbourhood Algorithm (Sambridge, 03 1999a; Wathelet, 2008) for the joint inversion of receiver functions and apparent S-wave velocity profile. The Neighbourhood Algorithm (NA) is a derivative-free optimisation method 95 which uses a pseudo-random trajectory in exploring the parameter space. Rather than 96 making inferences on model parameters using only the lowest-misfit model, it provides the 97 option of using the suite of all generated models for this purpose. With a well sampled 98 parameter space, an ensemble algorithm also benefits from the possibility of a probabilistic 99 solution with full uncertainty estimates. In contrast with earlier studies on this topic which 100 are predominantly based on large amounts of available data, we show how this method can 101 be used with limited data sets comprising only a few events. This becomes crucial in the 102 context of planetary seismology where the amount of data may be limited. For example, 103 it can be used to study the crustal structure of Mars using data from the InSight mission 104 (Lognonné et al., 2019). Another problem associated with determining the crustal structure 105 is the number of inter-crustal layers to be inverted for. We address this problem using a two-106 fold approach: we start by inverting for a model of low complexity and gradually increase it 107 till no significant velocity contrast along with misfit reduction is observed, with major dis-108 continuities being adequately represented by the model. We then use Akaike weights derived 109 from AIC (Akaike Information Criterion) values (Akaike et al., 1973) for all of these models 110 as a selection criteria. We apply this joint inversion scheme on synthetic seismograms for 111 Mars and selected terrestrial data. 112

113 2 Datasets

114 2.1 Mars Synthetics

In order to demonstrate and verify our proposed method, we first use synthetic seismograms for Mars that are generated using Greens Function (GF) databases prepared for a suite of apriori 1D velocity models with varying crustal thicknesses, seismic wave speeds,

densities, mantle compositions and aerotherms. These apriori models are obtained by the 118 inversion of bulk chemistry, mineralogy and geotherm, following the approach described in 119 Khan & Connolly (2008), Connolly (2009), and Khan et al. (2016). The GF databases are 120 computed using a 2.5D axis-symmetrical spectral element code, AxiSEM (Nissen-Meyer et 121 al. 2014), and are publicly available within the Marsquake Service (MQS) at ETH Zurich 122 ((Ceylan et al., 2017), http://instaseis.ethz.ch/marssynthetics/). Synthetic broadband seis-123 mograms can be calculated from these GF databases for arbitrary moment tensors and 124 source receiver combinations using the Instase package (van Driel, Krischer, et al., 2015). 125 These simulations are based on full numerical solutions of the visco-elastic wave equation 126 and include the effects of attenuation, are accurate down to a period of 1 s, and allow for a 127 total simulation duration of 30 minutes. 128

Since a large variation in crustal thickness is expected across Mars, a thin (30 km) 129 and thick (80 km) crust is employed to create the initial models, both with a 10 km thick 130 upper crustal layer. Further details of these models can be found in Ceylan et al. (2017). 131 The thin and thick crusts with different velocity contrasts at the Moho represent 1-D global 132 end-member models, rather than what is expected beneath the InSight landing site. In 133 this paper we have used two thin crust models (C30VH_AKSNL, C30VL_AKSNL) and one 134 thick crust model (C80VL_AKSNL) for the purpose of demonstrating the method. For all 135 of these models, we calculated synthetic seismograms and receiver functions at epicentral 136 distances between between 15° and 180° in 1° increments. Assuming normal faulting, a dip 137 slip source at an angle of 45° and at a depth of 5 km due north of the seismometer was used 138 to generate the synthetic waveforms. Since the synthetics do not have any added noise, we 139 assume a reasonable 25% standard deviation on mean absolute values of RFs and $V_{S,app}$ 140 whenever appropriate for likelihood calculations. We demonstrate the results of applying 141 our method first on a single event and then multiple events together. 142

2.2 Terrestrial Data

143

To verify how the algorithm works in a real setting, we analysed data from two sta-144 tions in Central Europe - BFO in Germany (Federal Institute for Geosciences and Natural 145 Resources, 1976) and SUW in Poland (GEOFON Data Centre, 1993). Reference values of 146 crustal thickness for these stations were taken from the Moho depth map of the European 147 plate (Grad et al., 2009) and Knapmeyer-Endrun et al. (2014). Because these sites have 148 known differences in crustal structure, this gives us the opportunity to test how the method 149 works in a range of possible scenarios and in the presence of noise. Station BFO is located on 150 the thinned crust of the Upper Rhine Graben which is a part of the European Cenozoic Rift 151 system (Ziegler, 1992). In contrast to this, station SUW is situated on the relatively thick 152 East European Craton which is the core of the Baltica proto-plate and occupies the north-153 eastern half of Europe. It is characterized by a thick three-layer crust with an additional 154 fast lower crustal layer (Grad et al., 2003). The East European Craton is of Precambrian 155 origin and overlain by a young thin sedimentary cover (Bogdanova et al., 2006) which leads 156 to strong reverberations in the P-receiver function for SUW (Wilde-Piórko et al., 2017) 157

3 Method 158

159

3.1 Calculation of Receiver Functions

The teleseismic P-wave receiver function represents the structural response near a 160 recording station to the incoming teleseismic P-wave. It can be obtained by removing the 161 source wavelet, propagation effects and the instrument response from the vertical, radial and 162 transverse waveforms. This is generally done by deconvolving the vertical component from 163 the radial and transverse components in a process called source equalisation (Vinnik, 1977; 164 Phinney, 1964). Several methods have been described in the literature for this deconvolu-165 tion process (e.g., see Vinnik (1977), Phinney (1964), Langston (1979), Owens et al. (1987), 166 Kind et al. (1995)) Here we use a time-domain Wiener filter for deconvolution as described 167

by Hannemann et al. (2017). The synthetic seismograms do not require the removal of any 168 instrument response, but they are filtered between 1 Hz and 50 s, 1 Hz being the upper 169 frequency limit of the synthetics. Additionally, due to the alignment of source and receiver, 170 these data are already in the ZRT system. For the terrestrial data, we first remove the 171 instrument response from all components and then filter the seismograms between 5 Hz and 172 50 s. The ZNE coordinate system is then rotated into ZRT using back-azimuths determined 173 by polarization analysis (Jurkevics, 1988) to obtain radial and transverse components. The 174 Wiener filter is determined such that it transforms the P-wave signal on the vertical com-175 ponent into a band-limited spike. This filter is then applied to all components of the signal 176 to finally obtain the RF with the spike positioned at the centroid of the signal. 177

3.2 Apparent S-wave velocity

Following the relationship between true and apparent incidence angles (Wiechert, 1907), it can be shown that the apparent incidence angle is sensitive to absolute shear wave velocity

$v_{S_{app}} = \sin(0.5\overline{i_p})/p$

where $\overline{i_p}$ denotes the apparent P-wave incidence angle and p denotes ray parameter. Svenningsen & Jacobsen (2007) proposed a method to directly estimate the apparent incidence angle using RFs instead of the raw waveform data which in turn emphasised the true S-wave velocity information contained in them. We follow a similar procedure and estimate the apparent P-wave incidence angle from the amplitudes of vertical and radial receiver functions at time t=0 using the relation

$$\tan \overline{i_p} = \frac{RRF(t=0)}{ZRF(t=0)}$$

Now estimating i_p as a function of low pass Butterworth filter period (T) results in a $v_S(T)$ 181 curve which emphasises the absolute S-wave velocity variation with depth. Larger T implies 182 more smoothening and thus more multiples at later times influence the values of the filtered 183 receiver functions at t=0. In contrast with the squared cosine filters used by Svenningsen & 184 Jacobsen (2007), we use a Butterworth filter which has twice the corner period as a cosine 185 filter. For each trace we measure the dominant period of the spike in the ZRF and discard 186 the values of filter periods smaller than that. We show cases with both single and multiple 187 events. When multiple events are used at varying epicentral distances, we calculate the 188 median of the apparent S-wave velocity curve at each sample period. 189

¹⁹⁰ 3.3 Inversion

For the purpose of this study, we have employed a modified version of the Neighbour-191 hood Algorithm (NA) (Wathelet, 2008) for the joint inversions of RF and apparent S velocity 192 curves. Being a derivative free optimisation algorithm and taking into account the low di-193 mensionality of our problem, NA seems to be a good choice because of its simplicity (two 194 tuning parameter scheme) and lack of dependence on starting models (Sambridge, 1999a). 195 Moreover, an ensemble of models rather than a single model can be used to make robust 196 statistical inferences about the model parameters. The modifications by Wathelet (2008) 197 further implement dynamic scaling of model parameters and allows to define irregular limits 198 to the searchable parameter space. The idea behind the NA is to start with an initial coarse 199 sampling of the parameter space, then select the regions with lowest misfits and continue 200 to resample these regions such that the heaviest sampled regions correspond to the models 201 which best fit the data. In each iteration, the NA uses nearest-neighbour regions defined by 202 Voronoi cells to partition and search the parameter space. The misfit is assumed to be con-203 stant within each of these Voronoi cells, and with each iteration, sampling is concentrated 204 on the cells with lower misfit relative to the rest of the cells. The algorithm relies on only 205 two control parameters : Ns - number of new samples to generate at each iteration and 206

Nr - number of promising models to select for further sampling. The ratio Ns/Nr controls whether the algorithm behaves exploratively or exploitatively (Sambridge, 1999a,b).

We use the L2 norm in order to measure how well a given model with a particular set of parameters can reproduce the given data quantitatively

$$\Phi(m) = \left\|\frac{g(\mathbf{m}) - d_{obs}}{\sigma_d}\right\|^2$$

where $g(\mathbf{m})$ is the estimated data and σ_d^2 is the estimated variance of the data noise. In this study, the noise has been assumed uncorrelated for simplicity and thus a simple Euclidean distance can be used. For a joint inversion of receiver function and apparent S-wave velocity, the objective function is defined by the linear combination of misfits of the weighted receiver functions Φ_{RF} and the apparent velocity curve Φ_{Vapp} , using the L2 norm, thus takes the form

$$\Phi(m) = \alpha \Phi_{RF} + \Phi_{V_{app}} \tag{1}$$

The weighting constant α is tuned manually by sample forward runs prior to the inversion 209 process such that both the individual misfits are of the same order of magnitude. As 210 mentioned before, the two parameters that control the NA need to be tuned depending on 211 the problem and the style of sampling needed. For a more explorative search that is robust 212 against local minima, we perform 1200 iterations in each inversion run with 300 models 213 produced at each iteration (n_s) and 100 cells re-sampled at each iteration (n_r) , resulting 214 in an ensemble of ~ 360000 models per run. Each inversion was repeated several times to 215 test the stability of the results. High n_s/n_r ratio ensures faster convergence while a high 216 number of initial models $(n_{s_0} = 3000)$ ensures highly explorative behaviour. 217

Knapmeyer-Endrun et al. (2018) compared several algorithms used in literature for the 218 computation of receiver functions before choosing the forward calculation implemented by 219 Shibutani et al. (1996). The algorithm calculates the impulse response of a layer stack in the 220 P-SV system. We then convolved the resulting synthetic Z- and RRFs with the observed 221 ZRFs to account for the observed complexity and waveform widths. Once the RFs are 222 obtained, we can straight away calculate the apparent S wave velocities using the procedure 223 described in the last section. Density was not considered to be a parameter to be inverted 224 for and was calculated using Birch's law (Birch, 1961), while the S-wave velocity and the 225 v_P/v_S ratio were allowed to vary. Furthermore, the S-wave velocity was constrained to 226 increase with increasing depth. The fact that a single forward calculation can be performed 227 in a matter of seconds and the waveform complexity matches that of real data makes this 228 algorithm suitable for the propose of this study. 229

3.4 Bayesian Formulation

The Bayesian formulation allows to account for prior knowledge of the parameters of our model, provided that this information can be expressed as a probability distribution $\rho(\mathbf{m})$. The prior corresponds to the knowledge that we have about our system, for example from previous studies. As new data is available, often in the form of likelihoods, this prior information can then be updated using Bayes' rule. This results in what is known as the posterior distribution for these unknowns - a distribution over the full range of these parameters.

238

3.4.1 Computing average Likelihoods

The likelihood $\rho(\mathbf{d_{obs}}|\mathbf{m})$ is a function of the model parameters that describes the goodness of fit of a model to the observed data. Assuming a Gaussian error distribution

for a given misfit measure, $\mathbf{\Phi}(\mathbf{m})$, the likelihood function is defined as :

$$\rho(\mathbf{d_{obs}}|\mathbf{m}) \propto exp\left(\frac{-\Phi(m)}{2}\right)$$

As mentioned before, the NA initially starts with a coarse sampling of the parameter 239 space, and eventually the algorithm guides the sampling such that the best fitting regions of 240 the parameter space are also the most heavily sampled regions. This therefore introduces a 241 bias in the sampling of the parameter space which otherwise could be used to compute the 242 full uncertainty from the ensemble of acceptable solutions. Sambridge (1999b) demonstrates 243 that this could be achieved by a Gibbs re-sampling of the output ensemble which essentially 244 concentrates on the low misfit regions and approximates the true posterior density by an ap-245 proximate one. Here we show a simple alternative method to compute marginal histograms 246 from the biased samples based on binning model parameters. In essence, each model in the 247 ensemble has a pair-wise distance to every other model which can be calculated using multi-248 dimensional scaling. Binning model parameters within a small distance and computing 249 average likelihoods then approximates the true posterior density as a histogram. 250

²⁵¹ Consider N sample models $\mathbf{m}^{(1)}, ..., \mathbf{m}^{(N)}$ in a K-dimensional space, distributed accord-²⁵² ing to an (everywhere positive) unknown distribution $\nu(\mathbf{m})$. Assume that $\nu(\mathbf{m})$ is close to ²⁵³ the distribution, $f(\mathbf{m})$, and that we wish to compute the marginal histograms $f_k(m_k)$ from ²⁵⁴ the samples.

The height $h_{[a,b]}$ of the histogram column for an interval [a,b] must (for $N \to \infty$) be proportional to the marginal probability $P_k(a < m_k < b)$. Hence,

$$h_{[a,b]}\approx \int_a^b f_k(m_k)dm_k$$

except for a normalization factor. This can be re-written as a mean value (expectation) of the ratio $\frac{f_k(m_k)}{\nu(m_k)}$ over the interval [a, b] with respect to $\nu(m_k)$:

$$h_{[a,b]} \approx \int_{a}^{b} \frac{f_k(m_k)}{\nu(m_k)} \nu(m_k) dm_k$$

and since the sample models $\mathbf{m}^{(1)}, ..., \mathbf{m}^{(N)}$ are distributed according to $\nu(\mathbf{m})$, we have the approximation:

$$h_{[a,b]} \approx \frac{1}{N} \sum_{\{i|a < m_k^{(i)} < b\}} \frac{f_k(\mathbf{m}^{(i)})}{\nu(\mathbf{m}^{(i)})}$$

This expression can be used when f_k can be evaluated in the sample points, and when we can evaluate $\nu(\mathbf{m}^{(i)})$ from the density of sample points. The density at $\mathbf{m}^{(i)}$ can, e.g., be evaluated over a cube C with edge length Δm , centered at $\mathbf{m}^{(i)}$:

$$\nu(\mathbf{m}^{(\mathbf{i})}) = \frac{1}{(\Delta m)^K} N_c$$

where N_C is the number of sample points in C

265 3.4.2 Priors

We impose a minimal prior knowledge on all the parameters by using the uniform distribution as our choice of priors. The prior for each parameter takes a constant value over a defined interval. For example, if X is a model parameter which can take values over the interval $\Delta X = (X_{max} - X_{min})$, we define the prior probability density as :

$$\rho(x_i) = \begin{cases} \frac{1}{\Delta X}, & \text{if } X_{min} \le x_i \le X_{max} \\ 0, & \text{otherwise} \end{cases}$$

We can now apply Bayes' rule (Bayes, 1763) to combine the likelihood of observing the data with the prior distribution and to give the posterior probability density function:

 $\rho(\mathbf{m}|\mathbf{d_{obs}}) \propto \rho(\mathbf{d_{obs}}|\mathbf{m})\rho(\mathbf{m})$

Note that the denominator in the Bayes' rule, $\rho(\mathbf{d_{obs}})$, which is a sum over all possible models has been treated as a constant in this work, leading to a proportionality sign in the equation.

3.5 Model Selection

We use Akaike's Information Criterion (AIC) (Akaike et al., 1973) as a model selection criterion, which essentially gives the Kullback-Leibler divergence between a candidate model and the true model as

AIC = 2k - 2ln(L)

where k and L denote the number of model parameters and the value of maximum likelihood of the model, assuming Gaussian errors. The first term in this equation is a measure of fit between the synthetic model and the true model representing the reality; the second term penalizes the order of complexity of this synthetic model. While raw AIC values themselves have no meaning, the quantity $exp\left(\frac{AIC_{min}-AIC_i}{2}\right)$ is an estimate of the relative likelihood of the *i*th model. These model likelihoods can then be normalized to obtain Akaike weights $w_i(AIC)$ (Burnham & Anderson, 2002; Wagenmakers & Farrell, 2004),

$$w_i(AIC) = \frac{exp\{-0.5\Delta_i(AIC)\}}{\sum_{k=1}^{K} exp\{-0.5\Delta_k(AIC)\}}$$

which can be interpreted as the probability that the *i*th model is the best (i.e., it minimizes the estimated information loss (Anderson & Burnham, 2004)). The strength of evidence in favour of one model over the other can then also be obtained by dividing their respective Akaike weights. When the number of samples is small, a correction factor is added to the above equation giving the corrected AIC (AICc) values

$$AICc = 2k - 2ln(L) + \frac{2kn}{n - k - 1}$$

Here k denoted the number of model parameters and n the number of independent samples. 276 Since the samples of a seismogram are generally correlated, with the correlation length being 277 proportional to sampling frequency, we instead use the product of the Nyquist rate and the 278 signal length as a measure of the number of independent samples (van Driel, Wassermann, 279 et al., 2015). For a band limited signal, the Nyquist rate is given by $2 * (f_{high} - f_{low})$ which 280 gives 1.96 Hz and 9.96 Hz for synthetics and terrestrial data, respectively $(f_{high}$ and f_{low} 281 denote the upper and lower frequency limits). Anderson & Burnham (2004) suggest using 282 AICc when the ratio between the sample size n and the number of model parameters k283 is low (< 40). We will therefore use AICc when dealing with synthetic data and AIC for 284 terrestrial data. 285

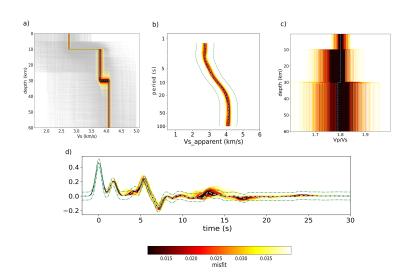


Figure 1. Result for thin crust model C30VH_AKSNL and event distance 70° (a) 1-D velocity profile. The light gray lines represent traversed models outside the maximum misfit range. The blue dashed line represents the true model. (b) Fit to $v_{S,app}$ (c) v_P/v_S ratio as a function of depth (d) Fit to receiver function waveforms. The blue dashed lines denote the observed data and the green dash-dotted lines represent the uncertainty in observations.

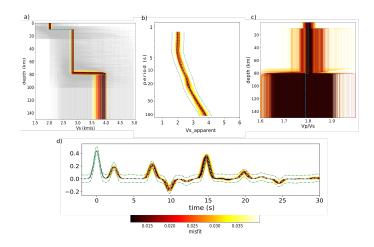


Figure 2. Same as Figure 1 for C80VL_AKSNL. Event distance is 40°.

286 4 Results

4.1 Mars Synthetics

Figures 1 and 2 show the result of applying the method on single events for a priori Mar-288 tian velocity models with a thin fast (C30VH_AKSNL) and a thick slow (C80VL_AKSNL) 289 crust, respectively. Since noise is not a limiting factor here, in both cases, the residual in-290 cludes the misfit for the complete waveform up to 30 s and apparent S wave velocity to 117 291 s. Each inversion was repeated 3 times to test the stability and the results were concate-292 nated. The plots include all models within a maximum misfit value, ranked and color coded 293 according to misfit with black models being the best fitting solutions. This maximum misfit 294 value is derived such that it encompasses the best 25% of all the models in the ensemble. 295

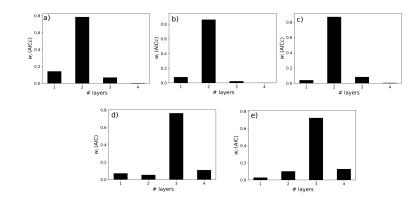


Figure 3. Model probabilities based on AICc values for (a) C30VH_AKSNL (b) C80VL_AKSNL (c) C30VL_AKSNL and AICc values for (d) BFO (e) SUW

Adding a third layer to the model parameterization did not produce any considerable 296 changes to the result. For C30VH_AKSNL the additional third layer produced a velocity 297 contrast of around 0.8~% against the layer adjacent to it with an insignificant misfit drop, 298 while C30VH_AKSNL produced a similar low velocity contrast of around 0.45 %. This shows 299 that an additional layer is not warranted by the data. This is also confirmed numerically by 300 our model selection criteria. Figures 3(a) and (b) show the respective probabilities obtained 301 from AICc values for 1, 2, 3 and 4 layer models with constant velocity over a half space for 302 C30VH_AKSNL and C80VL_AKSNL respectively. For C30VH_AKSNL, there is a higher 303 probability ($\sim 16\%$) of explaining the data with just a single layer than for C80VL_AKSNL. 304 This is consistent with a weak Moho signal produced by the small velocity contrast. Since 305 the 2 layer model has the highest probability (and thus minimum AIC), we conclude that 306 it is the optimum model that explains this data set. This is also in agreement with the true 307 models indicated by the blue dashed lines in figures 1 and 2. The apriori range for each 308 parameter for both 2 layer and 3 layer cases are shown in Figures 4 and 5. 309

The top layer crustal S-wave velocity and transition depth is well resolved for both 310 the representative end member models. For C30VH_AKSNL, there is a high uncertainty in 311 the Moho depth which in turn escalates the uncertainty in the S-wave velocity in the lower 312 crust. This might be explained as the direct converted phase and the multiples produced 313 by the intra-crustal discontinuity at 10 km depth are clearly visible in the data while the 314 Moho conversion for the thin crust model is not readily recognizable. This is in contrast to 315 C80VL_AKSNL where the direct converted phase and the multiples produced at the Moho 316 are clearly visible. The mantle S-wave velocities on the other hand are better constrained 317 for C30VH_AKSNL than for C80VL_AKSNL. This is explained by the $v_{S_{,app}}$ curves for the 318 models. The $v_{S_{app}}$ curve for C80VL_AKSNL does not contain any information on the upper 319 mantle velocity within its period range whereas in the $v_{S_{,app}}$ curve for C30VH_AKSNL, the 320 velocities converge to the upper mantle velocity of 4.1 km/s for periods longer than ~ 50 s. 321 This clearly demonstrates the advantage of inverting receiver functions along with frequency 322 dependent apparent S-wave velocities. 323

In both cases, the v_P/v_S ratio is also fairly well constrained for the top two layers by the method, as can be seen in the sub-figures (d). This is in agreement with Sambridge (1999a), where it was shown that the v_P/v_S ratio from the NA inversion is better resolved in the top layers than for the deeper ones. The thickness of the layers and their corresponding S-velocities are also better constrained than the v_P/v_S ratio. For C80VL_AKSNL, the v_P/v_S ratio of the half-space is not well resolved and varies across the whole model range

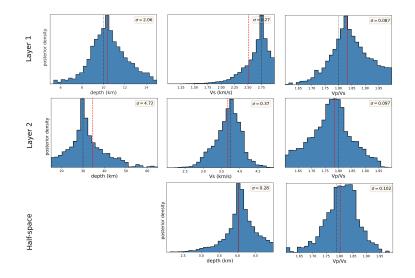


Figure 4. C30VH_AKSNL : 1D marginal posterior densities of depth, velocity and v_P/v_S ratio for each layer. The half-space has no depth parameter. The red dashed line denotes the mean value and the black dotted line represents the true parameter value.

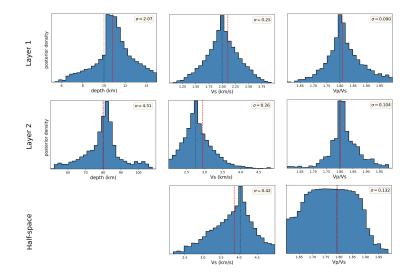


Figure 5. Same as Figure 4 for C80VL_AKSNL

investigated, whereas for C30VH_AKSNL, it is adequately resolved for all the layers even
 though the variance increases with depth.

To test how the method performs when multiple events are available, a median $v_{S_{,app}}$ 332 curve was calculated for model C30VL_AKSNL from the RFs between 40° to 90° where 333 the the $v_{S_{app}}$ curves are similar for each distance (Knapmeyer-Endrun et al., 2018). This 334 median $v_{S,app}$ curve was then jointly inverted with 6 receiver functions selected at epicentral 335 distances of 90° , 80° , 70° , 60° , 50° and 40° . The resulting profile along with the waveform 336 fit for each RF and $v_{S_{,app}}$ curve is shown in Figure 6. The velocity profile lies well within 337 the range of the uncertainty and the receiver function at each distance is also well modelled. 338 The variance in velocity again increases with depth and is maximum for the mantle. The 339

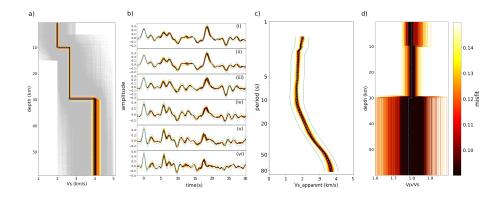


Figure 6. Example of multiple inversions for C30VL_AKSNL (a) 1-D velocity profiles. The light gray lines represent traversed models outside the maximum misfit range. (b) Fit to receiver function waveforms at epicentral distance of (i)90° (ii) 80° (iii) 70° (iv) 60° (v) 50° and (vi) 40° (c) Fit to the median $v_{S,app}$ (d) v_P/v_S ratio as a function of depth. The blue dashed curves denote the observed data and the green dash-dotted lines represent the data uncertainty.

median $v_{S_{app}}$ curves are also close to the observed curve, even though the kinks between 2 -340 3 s and 7 s appear to be slightly sharper than in the observed curve. Unlike C30VH_AKSNL, 341 C30VL_AKSNL has a shorter $v_{S_{app}}$ curve extending to 82 s. This restricts the retrieval of 342 S-wave velocity information from longer periods and has the effect of an increased variance 343 in the upper mantle velocity. The Moho on the other hand is well resolved due to a high 344 impedance contrast which results in a direct phase at around 6 s for RFs at 40° and 50° , 345 and a clear multiple at around 19 and 24 seconds for RFs at 90° , 80° and 70° . Looking at 346 the probability densities we see that using more data has the effect of an overall decrease in 347 uncertainty levels. From Figure 3(c), we see that the data is best explained by a 2 layer model 348 which has the highest value for w_i (AICc). To check whether there is a decrease in the depth 349 velocity trade off, we further compared the density plots of Moho depth and the velocity 350 above with the results from a direct receiver function inversion which did not employ $v_{S_{app}}$ 351 as an additional constraint. Here we used the best 25% models of the respective ensembles. 352 It is evident from the Figure 8 that along with a gain in accuracy, there is a considerable 353 reduction in trade-off between depth and velocity in the case of the joint inversion. For an 354 application of the method to synthetic data with added noise see Drilleau et al. (2020). 355

4.2 Terrestrial Data

356

The examples above from synthetic data show that in principle the joint inversion 357 of apparent S-wave velocity with receiver functions serves as a useful complement. This 358 section presents inversion results for terrestrial data where the inherent data noise becomes 359 an important consideration and has a strong influence on the resulting model parameters 360 and their associated uncertainties. Figure 9 (a) shows the noise levels computed for stations 361 BFO (green) and SUW (blue) using the pre-event noise of the radial component of the 362 receiver functions since they should ideally be independent and non-correlated. For each 363 station we calculate the mean of the pre-event noise of the radial component of each receiver 364 function from all the events considered here for multiple inversions and bin them according 365 to amplitude, creating a distribution from which noise parameters can be estimated. The 366 variance in the noise level was found to be the higher for SUW with each roughly following 367 a Gaussian distribution. Similarly Figure 9 (b) shows the noise characteristics for the $v_{S_{app}}$ 368 curve for both the stations calculated by binning of residuals from the median curve. 369

Selection of the model complexity that best describes the data is again done using the procedure described in the previous section. Starting at a low degree, we gradually increase

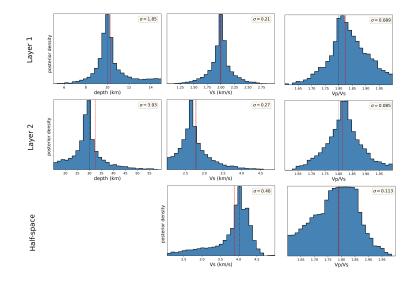


Figure 7. Same as Figure 4 for C30VL_AKSNL

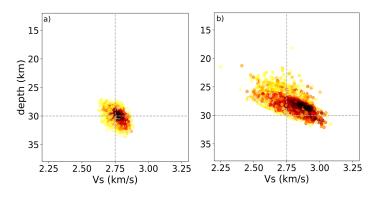


Figure 8. Comparison of depth velocity trade off for (a) Joint inversion of RF with $v_{S_{,app}}$ (b) RF inversion without $v_{S_{,app}}$. The grey dashed lines denote the true values of depth and velocity.

the complexity until the parameterization produces no significant deviation in profile and misfit reduction. We then compare the corresponding relative likelihood values and choose the maximum.

The results for seismic station BFO are summarized in Figure 10. From the velocity 375 profile (subplot (a)) we can see that the data can be sufficiently described by a minimum 376 parameterisation comprising 3 layers with constant velocity over a half-space - a low velocity 377 top layer of sediments, an upper crustal layer extending from the base of the sediments 378 to a depth of \sim 7 km and a thick lower crust that extends from 7-8 km to the Moho 379 at ~ 25 km depth. Various studies found the Moho depth between 23.8 and 27 km for 380 station BFO (Geissler et al., 2008; Knapmeyer-Endrun et al., 2014; Grad et al., 2009). 381 The mantle velocities are also adequately constrained by the data showing a maximum 382 probability for mantle v_S velocity of 4.6 km/s. The results for the S-wave velocity model 383 also show close agreement with Svenningsen & Jacobsen (2007) (shown in blue dashed lines) 384 and Knapmeyer-Endrun et al. (2018) (shown in green dashed lines). Since Svenningsen & 385 Jacobsen (2007) used the apparent velocity curve up to 0.2 s in contrast to 1.3 s allowed by 386 our data-set, the top sediment layer could be better resolved to thickness values below 1km. 387

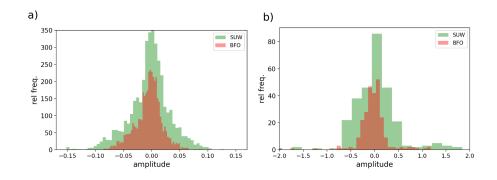


Figure 9. Noise characteristics of (a) RF shown as a frequency distribution of amplitude calculated from radial component of receiver functions for different stations (b) $v_{S,app}$ calculated as a frequency distribution of error from the median curve.

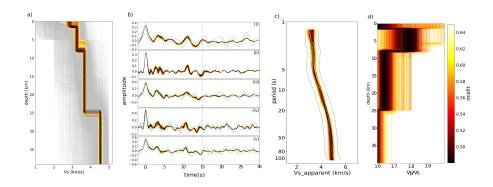


Figure 10. Example of joint inversions for terrestrial data from station BFO (a) 1-D velocity profiles. The blue and green dashed line represents the results from Svenningsen & Jacobsen (2007) and Knapmeyer-Endrun et al. (2018). The light gray lines represent traversed models outside the maximum misfit range.(b) Fit to receiver function waveforms at epicentral distance of (i) 82° (ii) 79° (iii) 70° (iv) 51° (v) 45°. The blue dashed curve denotes the observed radial RFs and green dashed lines represent the standard error. The dark blue dotted line at 15s shows the end of the misfit window. (c) Fit to the median $v_{S,app}$ (d) v_P/v_S ratio as a function of depth

Subplots (b) and (c) show the corresponding fits to the receiver function for each event and a median $v_{S,app}$ curve. Except for the RF waveform in event (i) where the phase at ~ 10 s is over-pronounced, the models fit the data from other events adequately well. The modelled $v_{S,app}$ curve also follows the data closely at all periods, including the sharp kink around ~ 2 s. At longer periods after ~ 50 s, the velocities seem to converge to ~ 4.8 km/s providing a tight constraint on the upper mantle which explains the low uncertainty seen in the the half space v_S .

Station SUW is located on the East European craton and sits on a relatively thicker 395 crust than BFO. Using a similar parameterization as before with 3 layers including a top 396 sedimentary layer results in a subsurface velocity profile shown in Figure 11 (a). The model 397 predicts the Moho to be located at a depth of ~ 45 km with the highest probability density 398 and an intra-crustal discontinuity at 15 km. Previous studies have estimated the Moho 399 depth to lie between 41 km and 46.8km for station SUW (Geissler et al., 2008; Knapmeyer-400 Endrun et al., 2014; Grad et al., 2009). The thickness and v_S of the sedimentary layer, 401 however, are not well constrained with the uncertainty for v_S being the highest amongst all 402 all layers. This is also evident from the modelled $v_{S_{app}}$ curves (subplot (c)) which show a 403

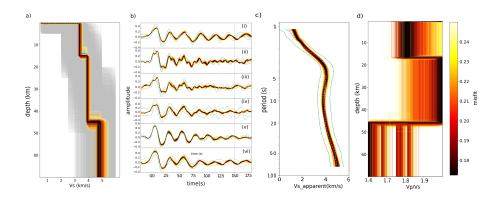


Figure 11. Same as Figure 10 for station SUW (b) shows the fit to receiver function waveforms at epicentral distances of (i) 82° (ii) 77° (iii) 72° (iv) 68° (v) 64° (vi) 60°

slight deviation from the observed curve at short periods. Such a deviation could indicate 404 that the sedimentary layer is more complex than our parameterization which models it 405 simply as layer with constant velocity. An increase in the model complexity (e.g., modelling 406 the sedimentary layer with a velocity gradient) could lead to a better fit here as suggested 407 by Knapmeyer-Endrun et al. (2018). Further, the missing v_S information at long periods in 408 the observation leads to an increase in uncertainty in the upper mantle velocity which shows 409 the highest probability density at a value of ~ 4.9 km/s. The modelled RFs shown in Figure 410 11 (b) clearly show the ringing effect with gradual decrease in amplitude with time caused 411 by the thin sediment layer. These strong reverberations produce high amplitude oscillations 412 in the early part of the signal and completely masks the direct Moho conversion at $\sim 6s$. 413 This example in particular shows that caution is needed to interpret receiver functions with 414 a sedimentary layer in terms of subsurface structures. 415

Figures 3(d) and 3(e) show the respective model probabilities obtained from AIC values. 416 We see that both the data can be best explained by 3 layer models with constant velocity 417 over a half space. However, there is still $\sim 9\%$ probability for a 4 layer model in both cases. 418 The resulting values for v_P/v_S for each layer are also shown in suplots (d) in Figures 10 and 419 11. Unlike the case for synthetics, a high variation is observed here between the layers. In 420 all the examples, the top sediment cover shows the highest uncertainty. The first and second 421 layers are better resolved. The average v_P/v_S values estimated from RF analysis in previous 422 studies are between 1.69 and 1.75 for BFO (Geissler et al., 2008; Knapmeyer-Endrun et al., 423 2014)) and between 1.81 and 1.84 for SUW. We find that the mean values from our results 424 are broadly similar with values of 1.67 and 1.82, respectively. 425

⁴²⁶ 5 Summary and Conclusion

In the context of the InSight mission, receiver function analysis has been envisioned 427 as a likely method to study the crustal structure of Mars (Panning et al., 2017). In order 428 to diminish the depth-velocity trade off inherent in travel time methods, we propose to 429 use the information provided by apparent P-wave incidence angles derived from P-receiver 430 functions as an additional constraint (Knapmeyer-Endrun et al., 2018). In this study, we 431 present a method for joint inversion of receiver functions and frequency dependent apparent 432 S-wave velocity curves using the Neighbourhood Algorithm. This results in an ensemble 433 of model solutions along with their respective misfit values which can in turn be used to 434 compute the full uncertainty of the model parameters. We then develop such a probabilistic 435 solution using the resultant ensemble and apply this method to various data sets. Further, 436 determining the sufficient number of layers for an optimal model presents another challenge 437 in waveform inversion. We tackle this by gradually increasing the number of layers till adding 438

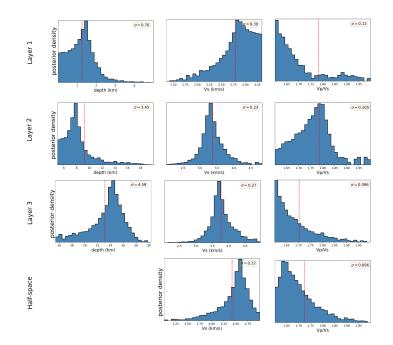


Figure 12. Same as Figure 4 for the inversion of data from station BFO

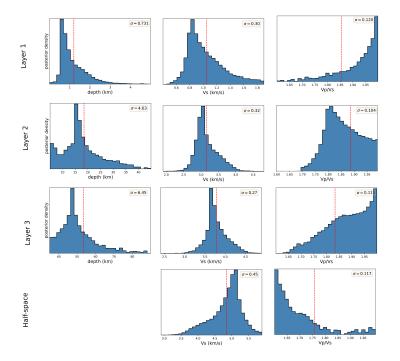


Figure 13. Same as Figure 4 for the inversion of data from station SUW

439 yet another produces no significant change, and then using AIC as a statistical inference440 test on all possible model families.

The method is successfully applied to synthetic seismograms generated for three aprori Mars subsurface models. Here we used both single and multiple events, and the uncertainty in the retrieved model parameters decreases with an increase in the size of the data set. We

then applied the method on terrestrial data from three different seismic stations located in 444 different geological settings. The resulting subsurface models were in good agreement with 445 the results obtained in previous studies using diverse approaches which corroborated the 446 efficacy of the method. Some aspects in applying this method to InSight data do warrant 447 attention. The effect of location uncertainties will considerably affect the calculation of 448 $v_{S_{app}}$. Knapmeyer-Endrun et al. (2018) showed that the biggest affect in $v_{S_{app}}$ can be 449 caused by an uncertainty in distance and back-azimuth. A $\pm 25\%$ uncertainty in distance 450 could yield an uncertainty of ± 1 s/deg of the ray parameter for the P phase, while an 451 erroneous back-azimuth will lead to a decrease in estimated v_S values at shorter periods. 452 The thickness and velocity of a thin regolith layer can also be quite difficult to resolve if 453 there is missing or erroneous information at short periods, as was the case in our study of 454 terrestrial data. Another factor that limits the information that can be obtained from v_{Sam} 455 on Mars is long period noise and effects of glitches (Scholz et al., 2020). Knapmeyer-Endrun 456 et al. (2018) suggests that long period noise will affect longer periods while it has been 457 observed that glitches can contaminate any part of the signal. Unlike the synthetics and 458 terrestrial data used in this study, the $v_{S_{,app}}$ curve obtained from actual Mars data could be 459 limited to much shorter periods. This would then increase the uncertainty in the retrieved 460 v_S values at larger depths. A similar situation was encountered in Drilleau et al. (2020). 461 In our previous study, Lognonné et al. (2020), we have been able to constrain the S-wave 462 velocity and depth for the first inter-crustal layer of Mars between 1.7 to 2.1 km/s and 8463 to 11 km, respectively, using such a limited $v_{S_{,app}}$ curve while further work involving the 464 entire crust is in preparation. It is therefore important that all these factors are correctly 465 accounted for. 466

467 Acknowledgments

R.J. acknowledges the funding provided by the IMPRS and the Emeritus group. The
MPSMPG SEIS team acknowledges funding for development of the SEIS leveling system
by the DLR German Space Agency. Seismic data for station BFO and SUW were obtained
from the Federal Institute for Geosciences and Natural Resources and GEOFON data centre
of the GFZ German Research Centre for Geosciences, respectively. This paper is InSight

473 Contribution Number 216.

474 **References**

- Akaike, H., Petrov, B. N., & Csaki, F. (1973). Second international symposium on information theory.
- Ammon, C. J. (1991). The isolation of receiver effects from teleseismic P waveforms. Bull.
 of the Seism. Soc. Am., 81, 2504-2510.
- Ammon, C. J., Randall, G. E., & Zandt, G. (1990). On the nonuniqueness of receiver function inversions. *Journal of Geophysical Research: Solid Earth*, 95(B10), 15303–15318.
- Anderson, D., & Burnham, K. (2004). Model selection and multi-model inference. Second.
 NY: Springer-Verlag, 63(2020), 10.
- Bayes, T. (1763). Lii. an essay towards solving a problem in the doctrine of chances. by the
 late Rev. Mr. Bayes, frs communicated by Mr. Price, in a letter to John Canton, amfr s. *Philosophical transactions of the Royal Society of London*(53), 370–418.
- Birch, F. (1961). The velocities of compressional waves in rocks to 10 kilobars, Part 2. J. *Geophys. Res.*, 66, 2199-2224.
- Bogdanova, S., Gorbatschev, R., Grad, M., Janik, T., Guterch, A., Kozlovskaya, E., ... others (2006). Eurobridge: new insight into the geodynamic evolution of the East European Craton. Geological Society, London, Memoirs, 32(1), 599–625.
- ⁴⁹¹ Burnham, K. P., & Anderson, D. R. (2002). Model selection and.
- Ceylan, S., van Driel, M., Euchner, F., Khan, A., Clinton, J., Krischer, L., ... Giardini, D.
 (2017). From initial models of seismicity, structure and noise to synthetic seismograms for Mars. Space Science Reviews, 211(1-4), 595–610.

- ⁴⁹⁵ Chong, J., Ni, S., Chu, R., & Somerville, P. (2016). Joint inversion of body-wave receiver
 ⁴⁹⁶ function and Rayleigh-wave ellipticity. Bulletin of the Seismological Society of America,
 ⁴⁹⁷ 106(2), 537-551.
- Connolly, J. A. D. (2009). The geodynamic equation of state: What and how.
 Geochemistry, Geophysics, Geosystems, 10(10). Retrieved from https://agupubs
 .onlinelibrary.wiley.com/doi/abs/10.1029/2009GC002540 doi: https://doi.org/
 10.1029/2009GC002540
- Drilleau, M., Beucler, ., Lognonn, P., Panning, M. P., Knapmeyer-Endrun, B., Banerdt,
 W. B., ... Tharimena, S. (2020). MSS/1: Single-Station and Single-event
 Marsquake Inversion. *Earth and Space Science*, 7(12), e2020EA001118. Retrieved
 from https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020EA001118
 (e2020EA001118 10.1029/2020EA001118) doi: https://doi.org/10.1029/2020EA001118
- ⁵⁰⁷ Du, Z., & Foulger, G. (1999). The crustal structure beneath the northwest fjords, Iceland, ⁵⁰⁸ from receiver functions and surface waves. *Geophysical Journal International*, 139(2), ⁵⁰⁹ 419–432.
- Dueker, K. G., & Sheehan, A. F. (1997). Mantle discontinuity structure from midpoint stacks
 of converted P to S waves across the Yellowstone hotspot track. Journal of Geophysical Research: Solid Earth, 102(B4), 8313–8327.
- Federal Institute for Geosciences and Natural Resources. (1976). German regional seis *mic network (grsn)*. Bundesanstalt fr Geowissenschaften und Rohstoffe. Retrieved from
 https://www.seismologie.bgr.de/doi/grsn/ doi: 10.25928/MBX6-HR74
- Fontaine, F. R., Barruol, G., Kennett, B. L., Bokelmann, G. H., & Reymond, D. (2009).
 Upper mantle anisotropy beneath Australia and Tahiti from P-wave polarization: Implications for real-time earthquake location. *Journal of Geophysical Research: Solid Earth*, 114(B3).
- Geissler, W. H., Kind, R., & Yuan, X. (2008). Upper mantle and lithospheric heterogeneities
 in central and Eastern Europe as observed by teleseismic receiver functions. *Geophysical Journal International*, 174(1), 351–376.
- GEOFON Data Centre. (1993). Geofon seismic network. Deutsches GeoForschungsZentrum
 GFZ. Retrieved from http://geofon.gfz-potsdam.de/doi/network/GE doi: 10.14470/
 TR560404
- Grad, M., Jensen, S. L., Keller, G. R., Guterch, A., Thybo, H., Janik, T., ... others (2003).
 Crustal structure of the Trans-European suture zone region along POLONAISE'97 seismic
 profile P4. Journal of Geophysical Research: Solid Earth, 108(B11).
- Grad, M., Tiira, T., & Group, E. W. (2009). The moho depth map of the European Plate.
 Geophysical Journal International, 176(1), 279–292.
- Hannemann, K., Krüger, F., Dahm, T., & Lange, D. (2016). Oceanic lithospheric S wave velocities from the analysis of P wave polarization at the ocean floor. *Geophys. J. Int.*, 207, 1796-1817. doi: 10.1093/gji/ggw342
- Hannemann, K., Krüger, F., Dahm, T., & Lange, D. (2017). Structure of the oceanic
 lithosphere and upper mantle north of the Gloria fault in the eastern mid-Atlantic by
 receiver function analysis. J. Geophys. Res., 122, 7927-7950. doi: 10.1002/2016JB013582
- Helffrich, G., & Thompson, D. (2010). A stacking approach to estimate vp/vs from receiver
 functions. *Geophysical Journal International*, 182(2), 899–902.
- Julia, J., Ammon, C. J., Herrmann, R., & Correig, A. M. (2000). Joint inversion of receiver function and surface wave dispersion observations. *Geophysical Journal International*, 143(1), 99–112.
- Jurkevics, A. (1988). Polarization analysis of three-component array data. Bull. seism. Soc. Am., 78(5), 1725-1743.
- Khan, A., & Connolly, J. (2008). Constraining the composition and thermal state of Mars
 from inversion of geophysical data. *Journal of Geophysical Research: Planets*, 113(E7).
- Khan, A., van Driel, M., Böse, M., Giardini, D., Ceylan, S., Yan, J., ... others (2016).
 Single-station and single-event marsquake location and inversion for structure using syn
 - thetic Martian waveforms. Physics of the Earth and Planetary Interiors, 258, 28–42.

548

- Kind, R., Kosarev, G., & Petersen, N. (1995). Receiver Functions at the Stations of the
 German Regional Seismic Network (GRSN). *Geophys. J. Int.*, 121, 191-202.
- Knapmeyer-Endrun, B., Ceylan, S., & van Driel, M. (2018). Crustal S-wave velocity from
 apparent incidence angles: a case study in preparation for Insight. Space Science Reviews,
 214(5), 83.
- Knapmeyer-Endrun, B., Krüger, F., & Group, t. P. W. (2014). Moho depth across the
 Trans-European Suture zone from P-and S-receiver functions. *Geophysical Journal Inter- national*, 197(2), 1048–1075.
- Langston, C. A. (1979). Structure under Mount Rainier, Washington, inferred from teleseismic body waves. *Journal of Geophysical Research: Solid Earth*, 84 (B9), 4749–4762.
- Lognonné, P., Banerdt, W., Pike, W., Giardini, D., Christensen, U., Garcia, R. F., ...
 others (2020). Constraints on the shallow elastic and anelastic structure of mars from
 insight seismic data. *Nature Geoscience*, 13(3), 213–220.
- Lognonné, P., Banerdt, W. B., Giardini, D., Pike, W., Christensen, U., Laudet, P., ... others (2019). Seis: Insights seismic experiment for internal structure of Mars. Space Science Reviews, 215(1), 12.
- Owens, T. J., Taylor, S. R., & Zandt, G. (1987). Crustal structure at regional seismic
 test network stations determined from inversion of broadband teleseismic P waveforms.
 Bulletin of the Seismological Society of America, 77(2), 631–662.
- Panning, M. P., Lognonné, P., Bruce Banerdt, W., Garcia, R., Golombek, M., Kedar, S.,
 Wookey, J. (2017, Oct 01). Planned Products of the Mars Structure Service for
 the Insight Mission to Mars. *Space Science Reviews*, 211(1), 611–650. doi: 10.1007/ s11214-016-0317-5
- Park, S., & Ishii, M. (2018). Near-surface compressional and shear wave speeds constrained
 by body-wave polarization analysis. *Geophysical Journal International*, 213(3), 1559–1571.
- Phinney, R. A. (1964). Structure of the Earth's crust from spectral behavior of long-period
 body waves. Journal of Geophysical Research, 69(14), 2997–3017.
- Sambridge, M. (1999a). Geophysical inversion with a neighbourhood algorithm I. Searching a parameter space. *Geophys. J. Int.*, 138, 479-494. doi: 10.1046/j.1365-246X.1999
 .00876.x
- Sambridge, M. (1999b). Geophysical inversion with a neighbourhood algorithmii. appraising
 the ensemble. *Geophysical Journal International*, 138(3), 727–746.
- Schiffer, C., Stephenson, R., Oakey, G. N., & Jacobsen, B. H. (2016). The crustal structure of Ellesmere Island, Arctic Canadateleseismic mapping across a remote intraplate orogenic belt. *Geophysical Journal International*, 204(3), 1579–1600.
- Scholz, J.-R., Widmer-Schnidrig, R., Davis, P., Lognonné, P., Pinot, B., Garcia, R. F., ...
 others (2020). Detection, analysis, and removal of glitches from insight's seismic data
 from mars. *Earth and Space Science*, 7(11).
- Schulte-Pelkum, V., Masters, G., & Shearer, P. M. (2001). Upper mantle anisotropy from
 long-period P-wave polarization. *Journal of Geophysical Research: Solid Earth*, 106 (B10),
 21917–21934.
- Shibutani, T., Sambridge, M., & Kennett, B. (1996). Genetic algorithm inversion for
 receiver functions with application to crust and uppermost mantle structure beneath
 eastern Australia. *Geophysical Research Letters*, 23(14), 1829–1832.
- Svenningsen, L., & Jacobsen, B. (2007). Absolute S-velocity estimation from receiver
 functions. *Geophysical Journal International*, 170(3), 1089–1094.
- van Driel, M., Krischer, L., Stähler, S. C., Hosseini, K., & Nissen-Meyer, T. (2015). Instaseis:
 Instant global seismograms based on a broadband waveform database. Solid Earth, 6(2),
 701–717.
- van Driel, M., Wassermann, J., Pelties, C., Schiemenz, A., & Igel, H. (2015, 07). Tilt
 effects on moment tensor inversion in the near field of active volcances. *Geophysical Journal International*, 202(3), 1711-1721. Retrieved from https://doi.org/10.1093/
 gji/ggv209 doi: 10.1093/gji/ggv209

- Vinnik, L. (1977). Detection of waves converted from P to SV in the mantle. *Physics of the Earth and planetary interiors*, 15(1), 39–45.
- Wagenmakers, E.-J., & Farrell, S. (2004). AIC model selection using Akaike weights.
 Psychonomic bulletin & review, 11(1), 192–196.
- Wathelet, M. (2008). An improved neighborhood algorithm: Parameter conditions and dynamic scaling. *Geophys. Res. Lett.*, 35, L09301. doi: 10.1029/2008GL033256
- Wiechert, E. (1907). Über Erdbebenwellen. I. Theoretisches über die Ausbreitung der
 Erdbebenwellen. Nachrichten von der Gesellschaft der Wissenschaften zu Göttingen,
 Mathematisch-Physikalische Klasse, 415-429.
- Wilde-Piórko, M., Grycuk, M., Polkowski, M., & Grad, M. (2017). On the rotation of
 teleseismic seismograms based on the receiver function technique. *Journal of seismology*,
 21(4), 857–868.
- ⁶¹⁵ Zhu, L., & Kanamori, H. (2000). Moho Depth variations in southern California from ⁶¹⁶ teleseismic receiver functions. J. geophys. Res., 105(B2), 2969-2980.
- ⁶¹⁷ Ziegler, P. A. (1992). European Cenozoic rift system. *Geodynamics of rifting*, 1, 91–111.