Seismic and Episodic Slip Characteristics of Frictional-Viscous Subduction Megathrust Shear Zones

Whitney M. Behr¹, Taras V. Gerya², Claudio Cannizzaro³, and Robert Blass³

¹Department of Earth Sciences, ETH Zürich ²Swiss Federal Institute of Technology (ETH-Zurich) ³ETH Zurich

November 24, 2022

Abstract

The deep roots of subduction megathrusts exhibit aseismic slow slip events, commonly accompanied by tectonic tremor. Observations from exhumed rocks suggest this region of the subduction interface is a shear zone with frictional lenses embedded in a viscous matrix. Here we use numerical models to explore the transient slip characteristics of finite-width frictional-viscous megathrust shear zones. Our model utilizes an invariant, continuum-based, regularized form of rate- and state-dependent friction (RSF) and simulates earthquakes along spontaneously evolving faults embedded in a 2D heterogeneous continuum. The setup includes two elastic plates bounding a viscoelastoplastic shear zone (subduction interface melange) with inclusions (clasts) of varying distributions and viscosity contrasts with respect to the surrounding weaker matrix. The entire shear zone exhibits the same velocity-weakening RSF parameters, but the lower viscosity matrix has the capacity to switch between RSF and viscous creep as a function of local stress state. Results show that for a range of matrix viscosities near the frictional-viscous transition, viscous damping and stress heterogeneity in these shear zones both 1) sets the 'speed limit' for earthquake ruptures that nucleate in clasts such that they propagate at slow velocities; and 2) permits the transmission of slow slip from clast to clast, allowing slow ruptures to propagate substantial distances over the model domain. For reasonable input parameters, modeled events have moment-duration statistics, stress drops, and rupture propagation rates that match natural slow slip events. These results provide new insights into how geologic observations from ancient analogs of the slow slip source may scale up to match geophysical constraints on modern slow slip phenomena.

Seismic and Episodic Slip Characteristics of Frictional-Viscous Subduction Megathrust Shear Zones

Behr, Whitney Maria¹, Gerya, Taras¹, Cannizzaro, C.², Blass, R.²

¹Department of Earth Sciences, Swiss Federal Institute of Technology (ETH), Zurich, Switzlerand ²Department of Mathematics, Swiss Federal Institute of Technology (ETH), Zurich, Switzlerand

Key Points:

3

5

6

10

- Models of frictional-viscous megathrust melanges predict a wide range of transient slip styles.
 Viscous damping and stress heterogeneity in a melange matrix sets the speed limit.
 - Viscous damping and stress heterogeneity in a melange matrix sets the speed limit for slip.
- Ruptures in melange belts can propagate long distances and link up heterogeneities
 at slow speeds

Corresponding author: Whitney Behr, wbehr@ethz.ch

13 Abstract

The deep roots of subduction megathrusts exhibit aseismic slow slip events, commonly ac-14 companied by tectonic tremor. Observations from exhumed rocks suggest this region of the 15 subduction interface is a shear zone with frictional lenses embedded in a viscous matrix. 16 Here we use numerical models to explore the transient slip characteristics of finite-width 17 frictional-viscous megathrust shear zones. Our model utilizes an invariant, continuum-18 based, regularized form of rate- and state-dependent friction (RSF) and simulates earth-19 quakes along spontaneously evolving faults embedded in a 2D heterogeneous continuum. 20 The setup includes two elastic plates bounding a viscoelastoplastic shear zone (subduction 21 interface melange) with inclusions (clasts) of varying distributions and viscosity contrasts 22 with respect to the surrounding weaker matrix. The entire shear zone exhibits the same 23 velocity-weakening RSF parameters, but the lower viscosity matrix has the capacity to 24 switch between RSF and viscous creep as a function of local stress state. Results show that 25 for a range of matrix viscosities near the frictional-viscous transition, viscous damping and 26 stress heterogeneity in these shear zones both 1) sets the 'speed limit' for earthquake rup-27 tures that nucleate in clasts such that they propagate at slow velocities; and 2) permits the 28 transmission of slow slip from clast to clast, allowing slow ruptures to propagate substantial 29 distances over the model domain. For reasonable input parameters, modeled events have 30 moment-duration statistics, stress drops, and rupture propagation rates that match natural 31 slow slip events. These results provide new insights into how geologic observations from 32 ancient analogs of the slow slip source may scale up to match geophysical constraints on 33 modern slow slip phenomena. 34

³⁵ Plain Language Summary

Subduction megathrusts represent the largest and most hazardous seismogenic faults 36 on Earth and exhibit a wide range of earthquake slip patterns. An especially perplex-37 ing form of slip on subduction megathrusts are 'slow earthquakes', which are slip events 38 that release similar amounts of energy as regular earthquakes, but do so over months to 39 years, rather than seconds. These events most commonly occur at deeper levels of the sub-40 duction megathrust where rocks are thought to transition from brittle and strong— with 41 deformation dominated by fracture and cracking— to smoother, continuous, and weak-42 with deformation dominated by flow. In this work, we use numerical models to explore 43 the seismic slip characteristics of megathrust faults that are mixtures of weak and strong 44 materials. We simulate a wide megathrust fault zone with embedded weak and strong sec-45 tions, and we systematically vary the strength contrasts between, and relative proportions 46 of, weak to strong material. Our results suggest that three regimes of slip behaviors can 47 be defined as a function of these strength contrasts and proportions of weak-to-strong ma-48 terials: an aseismic regime with no earthquake slip, a slow-slip dominated regime, and a 49 regular earthquake-dominated regime. These results help to reconcile some of the features 50 that geologists find in rock outcrops brought to the surface from deep subduction environ-51 ments, with the modern-day geophysical record of subduction zone earthquakes and surface 52 deformation patterns. 53

54 **1** Introduction

Deep episodic slow slip events (SSEs), commonly accompanied by non-volcanic tremor 55 and low-frequency earthquakes, are increasingly recognized as essential processes of strain 56 release in subduction zones (Beroza & Ide, 2011; Lay et al., 2012; Z. Peng & Gomberg, 2010; 57 Rousset et al., 2019; Shelly et al., 2007) and continental plate boundary faults (Chen et al., 58 2018; Shelly, 2017; Thomas et al., 2009; Wech et al., 2012). In subduction environments, 59 SSEs typically occur at and around the mantle wedge corner, down-dip of the seismogenic 60 megathrust in what is thought to be an environment rich in metamorphic reactions and 61 associated fluids, and high fluid pressures (Audet & Bürgmann, 2014; Audet & Kim, 2016; 62

Behr & Bürgmann, 2021; Condit et al., 2020; Peacock, 2009). SSEs can reach similar 63 magnitudes to 'regular' megathrust earthquakes, but they exhibit much slower slip rates 64 (~1-2 mm/day), smaller displacements (mm to a few cm), longer durations (days to years), 65 more frequent recurrence (months to years), and lower stress drops (\sim 1-100 kPa) (Bletery & 66 Nocquet, 2020; Michel et al., 2019; Obara & Sekine, 2009; Schmidt & Gao, 2010; Wallace & 67 Eberhart-Phillips, 2013; Wech & Bartlow, 2014). Understanding the physical mechanisms 68 controlling SSEs, their similarities and differences compared to high-frequency earthquakes, 69 and their role in priming or directly triggering megathrust slip is a fundamental challenge 70 in geodynamics. 71

Since the original detection of slow slip events, a wide range of numerical simulations 72 have been used to explore potential source mechanisms. Several aspects of SSEs can be 73 reproduced using numerical models of frictional sliding on a discrete, planar fault within a 74 rate-and-state-friction framework (J. H. Dieterich, 1979; Marone, 1998; Rubin, 2008; Ru-75 ina, 1983). Liu & Rice (2005), for example, demonstrated that aseismic slip transients 76 arise where faults transition with depth/temperature from velocity-weakening to velocity-77 strengthening frictional properties. Skarbek et al. (2012) similarly showed that mixtures 78 of velocity-weakening and -strengthening materials on a fault could control the sliding be-79 havior, with slow slip favored by velocity-weakening to -strengthening material ratios of 80 40-70%. Several models have also coupled rate-and-state friction and dilatancy with elastic-81 ity and pore-fluid-pressure diffusion, suggesting that dilatant strengthening competes with 82 fault thermal or poro-plasto-elastic pressurization to modulate fault slip rates over a range 83 comparable to natural faults (Liu & Rubin, 2010; Petrini et al., 2020; Segall & Bradley, 84 2012; Segall et al., 2010; Suzuki & Yamashita, 2009). Other model types that invoke a 85 velocity-dependent friction law, e.g. faults that transition from rate-weakening at low slip 86 rates to neutral or rate-strengthening at higher slip rates, expand the range of parameter-87 space over which slow slip-type behavior can be produced (e.g. Beeler, 2009; Hawthorne & 88 Rubin, 2013; Im et al., 2020; Shibazaki, 2003). 89

Although planar megathrust fault models with varying frictional and/or poroelastic 90 properties are successful at reproducing a spectrum of fault slip behaviors, the model frame-91 work of a discrete fault surface or thin gouge layer is challenging to reconcile with geophysical 92 imaging of modern SSE environments, and with geologic observations of rocks exhumed from 93 SSE source depths. Seismic reflection, tomography, and receiver function images, for ex-94 ample, show that the deep SSE source region coincides with a seismic low velocity and low 95 V_p - V_s ratio zone that is up to several kilometers in thickness, interpreted to represent a 'sub-96 duction channel' or wide subduction shear zone composed of underplated, heterogeneous, 97 subduction melange material (Audet & Schaeffer, 2018; Calvert, 1996; Calvert et al., 2020; 98 Delph et al., 2018; Hansen et al., 2012; Li et al., 2015; Nedimović et al., 2003). Geological 99 observations from exhumed rocks support this notion of a finite-width subduction shear zone 100 on the deep interface (e.g. Behr & Platt, 2013; Cloos & Shreve, 1988; Festa et al., 2010; 101 Grigull et al., 2012; Xia & Platt, 2017), and furthermore suggest that deformation within it 102 proceeds by coupled frictional sliding and viscous creep (Angiboust et al., 2011a; Fagereng & 103 Den Hartog, 2017; Fagereng & Sibson, 2010; Hayman & Lavier, 2014; Ujiie et al., 2018). Ob-104 servations from the outcrop scale, for example, commonly include block-in-matrix melanges 105 in which rigid, cm- to m-scale lenses concentrate brittle slip along geometrically complex, 106 interconnected fault networks hosted within a ductile matrix (Cowan, 1985; Fagereng, 2011; 107 Fagereng et al., 2014; Fisher & Byrne, 1987; Kotowski & Behr, 2019; Phillips et al., 2020). 108 These outcrop-scale features are mimicked at the multi-kilometric scale with map patterns 109 of exhumed subduction complexes containing underplated mafic or ultramafic lineaments 110 mantled by high-strain, viscous melange belts (Agard et al., 2018; Tewksbury-Christle et 111 al., 2021). These finite-width, heterogeneous shear zones are so commonly preserved in the 112 rock record that understanding their potential for seismic or transient slip on the deep in-113 terface seems essential to understanding the processes occurring within the SSE zone (cf. 114 Beall et al., 2019; Behr & Bürgmann, 2021; Fagereng & Sibson, 2010; Hayman & Lavier, 115 2014; Lavier et al., 2021; Skarbek et al., 2012). 116



Figure 1. A) Schematic sketch of the subduction interface and associated transitions in structural style and seismic behavior with depth. The subduction interface has been suggested to transition downdip near the depth of slow slip and tremor from a discrete frictional megathrust fault to a more distributed frictional-viscous shear zone, which is the basis for the model setup shown in b). B) Model setup investigated here with high viscosity inclusions (clasts) embedded in a lower viscosity matrix and sheared at a constant boundary velocity.

Here we use numerical models, inspired by geophysical and geological observations 117 of the SSE source region, to investigate the transient slip characteristics of distributed 118 frictional-viscous shear zones. We build upon previous rate-and-state-friction-based models, 119 but combine this model framework with visco-elasto-plastic deformation of a heterogeneous 120 continuum to explore the interplay between viscous shear zone loading, brittle-plastic yield-121 ing, and rate-dependent frictional sliding on spontaneously generated slip surfaces embedded 122 within a finite-width shear zone representative of subduction "mega-melange". We exam-123 ine qualitative and quantitative similarities between modeled events and natural fast and 124 slow-slip and discuss implications for slow slip source mechanisms. Our results can poten-125 tially reconcile geophysical constraints on slow slip phenomena with the exhumed geological 126 record of the slow slip environment. 127

¹²⁸ 2 Model Setup and Approach

¹²⁹ Our model setup consists of a 4-km-wide by 20-km-long, visco-elasto-plastic shear ¹³⁰ zone (representing a cross-section through the subduction interface) bounded by two elastic ¹³¹ plates that impose right-lateral shear at constant velocity (Figure 1). The low viscosity

shear zone contains inclusions of varying sizes, aspect ratios, and distributions, intended 132 to represent heterogeneous higher viscosity lenses (e.g. underplated mafic fragments). The 133 model builds upon the approach outlined by Herrendörfer et al. (2018), which combines 134 earthquake cycle simulations using a regularised Rate and State Friction (RSF) formulation 135 (cf. Lapusta et al., 2000) with seismo-(thermo)-mechanical (STM) approaches developed by 136 van Dinther et al. (2013). The STM component of the code is a continuum-based approach 137 that simulates visco-elasto-plastic deformation in response to applied forces. The STM 138 component is combined with an invariant form of rate-and-state-friction, including dynamic 139 rupture propagation and seismic wave generation, applied to spontaneously-generated and 140 evolving faults. An adaptive time-stepping routine allows fault slip velocities to be resolved 141 over ~ 9 orders of magnitude (Herrendörfer et al., 2018). 142

Our primary interest is in the interplay between the lower viscosity matrix and higherviscosity inclusions, and how their interactions modulate simulated event characteristics such as nucleation sites, fault plane geometries, slip velocities, moment-duration relationships, rupture propagation rates, recurrence intervals, and stress drops. To investigate this, our reference model implements a threshold shear zone viscosity (η_t) representing the frictionalviscous transition, with the static frictional yield strength defined as:

$$\tau_s = \mu \sigma_n,\tag{1}$$

and the threshold viscosity as:

149

151

155

16

$$=\frac{\tau_s}{2\dot{\epsilon}} = \frac{\mu\sigma_n}{2\dot{\epsilon}}.$$
(2)

With the implementation of rate-and-state friction, the static stress (τ_s) is replaced with a regularized (Lapusta et al., 2000; Rice et al., 2001) and invariant (Herrendörfer et al., 2018) form of the velocity-dependent RSF formulation:

 η_t

$$\tau_{\rm n} = a \ P \ \operatorname{arcsinh}\left[\frac{V_p}{2V_0} \exp\left(\frac{\mu_0 + b \ \ln\left(\frac{\theta V_0}{L}\right)}{a}\right)\right] \tag{3}$$

where τ_s is replaced by the second invariant of the stress tensor (τ_n) , σ_n is replaced by the effective pressure P, $V_p = \epsilon_n 2D$ (where D is the grid cell size) is the plastic slip velocity, V_0 is the reference slip velocity, μ_0 is the reference friction coefficient, L is the characteristic slip distance, a is the RSF direct effect, and b is the RSF evolution effect. b is described by the aging evolution law (e.g. J. Dieterich, 1994; Lapusta et al., 2000; Liu & Rice, 2005):

$$\dot{\theta} = 1 - \frac{V\theta}{L}.$$
(4)

¹⁶² An approximate nucleation size (h^*) is defined, above which simulated events start to prop-¹⁶³ agate dynamically (cf. Rubin & Ampuero (2005)):

164
$$h^* = \frac{2}{\pi} \frac{GbL}{(b-a)^2 P_b (1-v)},$$
 (5)

where P_b is the effective pressure, G is the shear modulus and ν is Poisson's ratio.

The input model parameters are shown in Table 1. We assume a small effective pressure 166 of 3.75 MPa, consistent with inferences of high fluid pressures and low effective normal 167 stresses in subduction shear zones (e.g. Audet et al., 2009; Peacock et al., 2011; Taetz et al., 168 2018; Ujiie et al., 2018; Warren-Smith et al., 2019). The entire shear zone (inclusions and 169 matrix) are implemented with the same elastic properties, velocity-weakening (a - b) and 170 reference RSF parameters, and initial state. The forcing blocks outside the shear zone are 171 set up with velocity strengthening conditions and high initial state. For these conditions, 172 the threshold matrix viscosity is 10^{18} Pa·s and h^* is equal to 3.2 km. We assume the matrix 173 deforms via linear viscous mechanisms, consistent with microstructural observations from 174 rocks suggesting pressure-solution or diffusion-creep mechanisms are active in subduction 175 shear zones (Behr & Platt, 2013; Fagereng & Den Hartog, 2017; Platt et al., 2018; Stöckhert, 176

Parameter	\mathbf{Symbol}	Value
Shear modulus	G	30 GPa
Bulk Modulus	K	50 GPa
Poisson ratio	u	0.25
Density	ρ	2700 kg/m^3
Shear wave speed	C_s	$3.3 \mathrm{~km/s}$
Shear zone width	W_s	4 km
Bulk shear zone strain rate	$\dot{\epsilon}$	$1.5 \times 10^{-12} / s$
Initial mean stress	P_B	4 MPa
Gravity	g	$9.8 \mathrm{m/s}$
Reference friction	μ_0	0.5
Reference slip velocity	V_0	$4 \times 10^{-9} \text{ m/s}$
Characteristic slip distance	L	.001 m
RSF direct effect	a	0.011
RSF evolution effect	b	0.017
Initial state	$ heta_i$	Forcing block: $\frac{L}{V_0} \exp(40)$ s
		Shear zone: $\frac{L}{V_0} \exp(-1)$ s
Forcing block viscosity	η_b	1×10^{23} Pa·s
Clast viscosity	η_c	1×10^{22} Pa·s
Threshold viscosity	η_t	1×10^{18} Pa·s
Shear zone matrix viscosity	η_{sz}	$.001-2000 \times \eta_t$
Clast spatial density	$ ho_c$	20-90%

Table 1. Model Parameters

2002; Wassmann & Stoeckhert, 2013). A viscosity gradient is implemented at the horizontal
shear zone margins in an effort to limit interactions between propagating ruptures and model
boundaries. Inclusions are implemented with a random size distribution such that their long
dimensions can be close to, but are always less than the nucleation size. The location and
aspect ratios of inclusions are varied randomly about a narrow distribution and inclusions
are permitted to slightly overlap.

Model outputs include all physical parameters such as stress, strain rate, viscosity 183 and velocity. For tracking transient slip events, we record the maximum velocity within 184 the model domain for every timestep. Due to the gradual change of the slip velocity during 185 seismic events, their durations were computed using a variable velocity threshold $(V_{threshold})$ 186 defined as a function of the maximal slip velocity (V_{max}) recorded during each individual 187 event. Since the maximum slip velocity is unknown *a-priori*, we integrated characteristics of 188 all events for 14 different pre-defined thresholds (V_i) ranging from 10^{-8} to 10^{-1} m/s with 0.5 189 increment in the power exponent. The characteristic velocity threshold for each recorded 190 event was then defined a *a-posteriori* as $V_{threshold} = V_i$ when $10^3 V_i < V_{max} < 10^{3.5} V_i$. Moments for each event were integrated for each V_i by accounting for all grid nodes slipping with slip rate $V_n > V_i$ as $M = \sum^t \left(dt \sum_{n,(V_n > V_i)}^{n,(V_n > V_i)} (V_n G) \sum_{n,(V_n > V_i)}^{n,(V_n > V_i)} (dx)^2 \right)$ where dt is the 191 192 193 current time step, dx is the horizontal grid step and G is the shear modulus. 194

¹⁹⁵ **3 Model Results**

196

3.1 Summary of General Model Behaviors

All models begin with a stage of shear zone loading in which strain rates progressively 197 increase in the shear zone matrix and elastic strain accumulates in the higher viscosity clasts, 198 with the timescale of this stage controlled by the Maxwell relaxation time (η/G) . The visco-199 elastic deviatoric stress distributions that are set up in this initial stage are heterogeneous. 200 with concentrations and shadows developed as a function of clast distribution and spatial 201 density. Where stress concentrations exceed the frictional yield strength, plastic slip begins 202 accumulating on localized slip zones that develop on both the margins and in the interior of 203 clasts. For all model runs conducted near the threshold viscosity, the initial orientations of 204 these failure planes are conjugate sets controlled by the static friction coefficient, consistent 205 with Coulomb theory, with low values of μ_i generating planes oriented at lower angles to the 206 shear zone walls (Fig. 2d-g). Local deflections of slip plane orientations do occur in some 207 models near stress rotations adjacent to inclusions, however, leading to non-planar rupture 208 geometries (e.g. Fig. 2e) (cf. Preuss et al., 2019). 209

The slip velocities on rupture planes initially grow exponentially as ruptures propagate 210 due to the RSF direct effect. Once ruptures have initiated, they can propagate in either 211 direction along their length. Whether ruptures will continue to propagate through the model 212 domain depends on the local stresses at the rupture tip, which is the sum of the dynamic 213 stresses associated with the rupture front itself and the heterogeneous background stresses 214 set up within the shear zone. If a rupture tip migrates into a zone of relatively high stresses, 215 the slip velocity and propagation velocity increases; whereas if the rupture tip migrates 216 into regions of low stresses, the slip velocity decreases, and if stresses are low enough, the 217 rupture arrests. In cases where a rupture reaches the nucleation size (cf. Eq. 5), it begins 218 to propagate dynamically. Variations in rupture speed during dynamic rupture propagation 219 can lead to generation of shear and pressure waves that radiate away from the slipping zone. 220 The propagating ruptures produce regions of low state relative to the surrounding unslipped 221 regions. Due to the short timescale of our model runs and the comparatively slow aging 222 law, rupture planes persist as low state zones throughout the model duration such that 223 eventually the initially high-viscosity inclusions (and in some cases the shear zone matrix) 224 become cut by numerous low state fault planes. 225

226

3.2 Simplified two-inclusion models

To illustrate the general model behaviors in more detail, we first use simplified twoinclusion models. Figure 2 shows the initial conditions, model state, and maximum velocity as a function of timestep for two-inclusion models with different matrix viscosities and/or different friction coefficients. Figure 2c highlights the initial stress field in which, because of their higher viscosity with respect to the surrounding matrix, the inclusions are under compression and generate stress concentrations and shadows in the surrounding lower-viscosity matrix.

Figure 2d-g shows the rupture patterns for four different model runs after an arbitrary 234 number of timesteps (6500). For the threshold viscosity case (Fig. 2d), clasts are loaded 235 to failure by surrounding viscous shear, but ruptures are generally confined to the clasts 236 themselves, except where local stress concentrations around and between the clasts permit 237 ruptures to propagate short distances into the matrix. This behavior illustrates the viscous 238 damping (i.e. effectively velocity-strengthening) effect of the low viscosity matrix. Because 239 the stresses in the model are always near the frictional yield strength, the slip velocities of 240 intra-inclusion ruptures are slow (Fig. 2h) and all ruptures are quenched before they reach 241 the critical nucleation size. 242

Figure 2e shows a model run in which the matrix viscosity is 10 times larger than η_t . Ruptures nucleate at stress concentrations on the inclusion margins and begin to prop-



Figure 2. Initial conditions (a-c), model state (d-g), and velocity (h) as a function of timestep for simplified two-inclusion models with different matrix viscosities and/or different friction coefficients. See Section 3.2 for detailed description.

agate unhindered through the lower viscosity matrix. Although the rupture orientations
in this regime are influenced by the model stress field, the slip velocities are not affected
and velocities on these rupture planes grow exponentially toward the maximum of 0.1-1
m/s. This behavior ensues because the matrix viscosity, above the threshold value, sets up
higher stress magnitudes in the shear zone, thus favoring fast frictional slip and allowing
the ruptures to reach the nucleation size and propagate dynamically.

Figure 2f-g shows two model runs in which the matrix viscosity is slightly above the 251 threshold value, but with different coefficients of friction. In this regime, ruptures can prop-252 agate through the matrix in regions of stress concentration, but they slip at slow velocities 253 because the stress magnitudes ahead of the rupture tip are very close to the threshold value, 254 and because the rupture tips occasionally propagate into stress shadows that lead to veloc-255 ity decreases. The changes in μ_0 result in different orientations of ruptures, but the overall 256 event patterns are similar. These two model runs show the potential for near-threshold 257 models to develop ruptures of significant length that link multiple inclusions through the 258 matrix across the model domain, but that nonetheless maintain slow slip velocities (Fig. 259 2h) due to low overall stresses and stress heterogeneity. 260

261

3.3 Multi-Inclusion Models

Here we focus on more complex multi-inclusion models in which only the matrix viscos-262 ity and the average spatial density of inclusions were varied; all other parameters remained 263 constant as in Table 1. Figure 3 shows the initial viscosity, stress distributions at the on-264 set of plastic yielding, and state at the end of the model run, for six example model cases 265 with varying starting matrix viscosities and clast distributions. Figure 4 shows the event 266 velocities through time for the same six model cases. We bin the models into three gen-267 eral categories based on shear zone matrix viscosity: above-threshold, near-threshold, and 268 below-threshold models, and four categories of clast percentage (ρ_c): low ρ_c , medium ρ_c , 269 high ρ_c , and clast-free. 270

271

3.3.1 Above-Threshold Models

Above-threshold models are classified as those in which the matrix viscosity is 100-272 2000 times the threshold viscosity. Because the viscosities in these models are too high to 273 permit any significant viscous creep, the model behaviors are dominated by elastoplastic 274 interactions and are insensitive to clast distributions and densities. Stresses build at the 275 model corners near the imposed viscosity gradient as the clasts do not produce significant 276 stress heterogeneity (Fig. 3a) and ruptures propagate at rates of 0.1-1 km/s horizontally 277 along the shear zone boundary across the model domain (Fig. 4a). Model events approach 278 maximum slip velocities (0.1-1 m/s, Fig. 4a) because of the stress magnitudes well above 279 the frictional yield strength and the associated direct effect of RSF. Throughout the model 280 runs, only one fault plane is active at any particular time, so the event patterns shown in 281 Figure 4a reflect the true event recurrence interval. With time in the models, initial rupture 282 planes are repeatedly occupied by high-velocity events that generate seismic waves that 283 reverberate across the model domain. Because fast slip events dominate in these model runs, 284 the events themselves are sometimes affected by propagation to the model boundaries and 285 by interference from the propagating seismic waves as they reflect off of the non-absorbent 286 model boundaries; this is an artifact of the model setup that explains some secondary low-287 velocity events recorded in these models, but does not substantially affect the overall rupture 288 patterns. 289

290 3.3.2 Below-Threshold Models

Below-threshold models are those in which the viscosity of the shear zone matrix is 5- $100 \times$ less than the threshold viscosity. For low to intermediate clast densities, these models do not generate sufficient stress concentrations to produce significant plastic yielding in



Figure 3. Initial conditions, initial stress state, and state at the end of the model run for 6 models with different matrix viscosities and different clast concentrations. Event velocities over time are shown for these same model runs in Figure 4. a) High matrix viscosity well above η_t leads to fast (cf. Fig. 4) slip events that propagate along the shear zone boundaries. b) Clast-free model just above η_t yields dominantly fast slip events that nucleate in the shear zone matrix and eventually propagate along shear zone boundaries. c) Same viscosity as in b) but with a low concentration of clasts. This leads to dominant slow slip (cf. Fig. 4) with several slip planes rupturing through the shear zone matrix. d-e) Models with viscosities at η_t but with different clast concentrations. Low ρ_c leads to clast-limited slow slip events whereas an increase in ρ_c leads to slow slip with ruptures that extend through the shear zone matrix. f) Below threshold viscosity model with high clast concentration. Slow-to-moderate velocity slip events are generated but only at direct contacts between clasts, after which the shear zone deforms at a steady state rate.



Figure 4. Maximum velocity over time for the models shown in Figure 3.

clasts, so no frictional failure or transient deformation occurs and the shear zone deforms 294 at a constant steady-state strain rate. At high clast densities, however, some events are 295 generated in the model. Figure 3f, for example, shows a model with a matrix viscosity that 296 is 10x less than η_t , but with 70% clasts clustered to form a load-bearing framework. This 297 model shows the development of stress concentrations at clast-clast and clast-shear-zone-298 wall contacts. This produces an early phase of small events with slow- to intermediate- slip 299 velocities (Fig. 4f). The events only propagate along clast-clast or clast-shear zone interfaces 300 but are immediately quenched when they reach viscous matrix regions due to the damping 301 effect of the very low matrix viscosity. The high-stress contact points gradually become 302 regions of low viscosity and low state, after which transient events are no longer generated 303 as sufficient stress magnitudes are no longer attained. Unlike in the above-threshold models, 304 several events can occur simultaneously in the 2D model domain, so the event patterns in 305 Figure 4 represent only the maximum-velocity events occurring at any one time and therefore 306 reflect a minimum recurrence interval. 307

308

3.3.3 Near-Threshold Models

Near-threshold models are defined as those in which the viscosity of the shear zone 309 matrix is $1-10\times$ greater than the threshold viscosity. Models in which the viscosity is equal 310 to the threshold value and clast densities are low show nucleation of events in clasts and slow 311 slip (averaging $\sim 10^{-7}$ m/s, Fig. 4c) along these rupture planes, but as in Figure 2d, the rup-312 tures are quenched when they propagate into the surrounding matrix (Fig. 3c). Increasing 313 clast densities in threshold models, or increasing the matrix viscosity to slightly above the 314 threshold value (e.g. $1.1-1.4\times$), however, each have the effect of slightly elevating average 315 stresses in the shear zone matrix, thus promoting through-going ruptures in some parts of 316 the model domain. Figure 3d, for example, shows a model run in which the viscosity is still 317 at the threshold value, but because the clast density is higher, some through-going rupture 318 planes develop, linking the margins of multiple clasts, and at least one rupture surface prop-319 agates through most of the model domain at slow velocity. Similarly, Figure 3c shows a 320 model case in which ρ_c is low, but because of the slightly above-threshold viscosity, events 321 can propagate farther into the matrix, linking ruptures between high viscosity lenses, but 322 still slipping at slow average velocities $(<10^{-2} \text{ m/s})$ and never reaching normal earthquake 323 slip rates. 324

The maintenance of stress magnitudes very close to the frictional yield strength in 325 near-threshold models also produces some behaviors through time that are not observed 326 in other model types. For example, in many model runs, the propagation of ruptures into 327 regions of the matrix that are only slightly below the frictional yield stress leads to dynamic 328 triggering of nearby rupture surfaces that propagate in the same or the opposite direction 329 as the initial rupture front (Video 1). Additionally, as in the below-threshold models, many 330 events can occur simultaneously in the 2D model domain, so the event patterns in Figure 331 4 represent a minimum recurrence interval. Contrary to the above-threshold models, the 332 propagation rates of ruptures in near-threshold models are much slower, ranging from ~ 0.1 333 to 20 km/day. 334



335 336

337

338

339

340

341

342 343

Video 1. Video of a near-threshold model with low clast concentration. The sequence begins with ruptures developing throughout the model domain only in clasts. These rupture planes eventually coalesce and link up across the shear zone matrix. At 30 seconds, a moderate-to-fast-velocity event nucleates and generates seismic waves that propagate through the model domain until 57 seconds. The rest of the model run shows repeated slow slip events that link clasts and matrix on single rupture planes. In several instances propagating ruptures trigger slip on nearby rupture surfaces, in both forward- and reverse-propagation directions.

The specific influence of stress heterogeneity, induced by the presence of clasts, on event 344 slip velocity in near-threshold models can also be examined by comparing near-threshold 345 models with and without clasts (Fig. 4b-c). Models in which the matrix viscosity is equal to 346 the threshold value, but where no clasts are implemented do not generate events because no 347 stress heterogeneity is present to push the model over the threshold stress toward frictional 348 failure. This is in contrast to threshold models with clasts, which generate slow slip events 349 due to failure within the clasts and subsequent quenching in the shear zone matrix (Fig. 350 4c-d). Models in which the matrix viscosity is slightly above the threshold value, with no 351 clasts present, are dominated by moderate- to fast-velocity, regularly-recurring events (Fig. 352 4b) that characteristically propagate across the whole model domain (Fig. 3b) – the lack 353 of stress heterogeneity prevents slip velocity perturbations from developing such that slip 354 velocities continue to grow exponentially with increasing slip. This contrasts with the event 355 patterns for models with the same matrix viscosity, but in which clasts are present, which 356 are dominated by slow slip events with shorter (and more irregular) minimum recurrence 357 times, and in which only some ruptures propagate as a single surface through the entire 358 model domain (Fig. 4c). 359



Figure 5. Normalized median moment and median event velocities as a function of matrix and bulk viscosity, with symbols representing clast distributions.

4 Model Event Statistics

Here we use the full suite of model runs to examine trends in transient event patterns as a function of shear zone viscosity and clast concentration, including median moments (normalized to the minimum model event size), and median event slip velocities (normalized to the imposed velocity across the shear zone) (Figure 5).

Figure 5a illustrates that there is a quasi-linear relationship i log-log space between 365 the median moment for modeled events as a function of shear zone matrix viscosity, with 366 higher moments associated with stronger shear zone matrices (Fig. 5a). This occurs because 367 ruptures nucleating in clasts can propagate farther into the shear zone matrix when the ma-368 trix viscosity (and stress) is higher on average, thus producing longer rupture surfaces (cf. 369 Section 3). The relationship appears to saturate at matrix viscosities $\sim 100x$ the thresh-370 old viscosity because the stress magnitudes in these models are nearly everywhere above 371 the frictional yield strength, so ruptures are never quenched in the matrix and therefore 372 propagate across the full model domain. 373

Figure 5b indicates that the correlation between moment and viscosity does not apply in the case of the *bulk* viscosity of the shear zone; i.e. the bulk viscosity for shear zones with very low matrix viscosity, but high clast content is 1-2 orders of magnitude larger
than threshold viscosity models with moderate clast contents, yet the median moment for
events is still small. This emphasizes the importance of the intervening weak viscous matrix
material in modulating slip behavior through its ability to damp nucleated ruptures, even
when clast concentrations and bulk viscosities are high.

Figure 5c shows the correlation between matrix viscosity and median event slip velocity. Events for models at and below the threshold viscosity exhibit similar event slip velocities of up to 3 orders of magnitude larger than the imposed shear zone loading rate, whereas above-threshold models show faster median slip velocities with increasing matrix viscosity, again saturating at ~100x the threshold viscosity.

We can also examine how our specific model parameters and associated transient event 386 patterns scale with natural slow slip phenomena, by examining moment release patterns, 387 stress drops, and moment-duration scaling (Fig. 6). Similar to what is shown in Figure 5a, 388 Figure 6a shows a clear correlation between cumulative moment release over time and shear 389 zone matrix viscosity. Furthermore, the plot demonstrates that above-threshold models (or 390 those near-threshold models with higher clast contents) show very regular moment release 391 over time, whereas near-threshold models with low clast contents exhibit an early phase of 392 moment release associated with ruptures generated only in clasts, followed by a later phase 393 of more regular moment release when ruptures coalescence to form planes that link up across 394 the model domain. A more detailed analysis or comparison of recurrence intervals among 395 model types is not appropriate here because the model setup tracks only the maximum 396 velocity within the 2D model domain, whereas as noted in Section 3, near-threshold and 397 below-threshold models commonly exhibit multiple events occurring simultaneously or in 398 close succession. Additionally, in reality, event recurrence intervals are not only sensitive 399 to plate boundary loading rates, but also to rates of fault healing (e.g. Fisher et al., 2019; 400 Marone et al., 1995; McLaskey et al., 2012; Sibson, 1992), a poorly understood process that 401 in our model framework would affect the time evolution of the state variable, but varying 402 this parameter was beyond the scope of this study. 403

Figure 6b demonstrates that there is an overall positive relationship between the stress drop of modeled events and their moment magnitude (M_w) , although the slope of this relationship appears to steepen for lower M_w . Stress drops for all modeled events range from less than ~4 kPa to 2 MPa, with higher viscosity models exhibiting higher moment magnitudes (cf. Fig 5a-b) and larger stress drops. For modeled slow slip events in particular, stress drops range from ~4-300 kPa, averaging ~100 kPa.

In Figure 6c, the model event statistics are compared to the scaling relationships for 410 slow slip versus regular earthquakes proposed by Ide et al. (2007). The majority of events 411 in the models are slow events that form a narrow swath with a $M \simeq 4.5 T$ scaling that in na-412 ture would be mostly seismically and geodetically undetectable. These are primarily events 413 generated within clasts or at clast margins that propagate until they are quenched in the 414 viscous matrix. As discussed in Section 3, below-threshold models with very high clast 415 densities generate point-like stress concentrations along clast-clast contacts— the failure of 416 these contacts produce small, but still slow slip events that extend downward in moment-417 duration space toward the region defined by very low frequency earthquakes (pink triangles 418 in Fig. 6b). Ruptures in near-threshold and above-threshold models that are able to prop-419 agate from clasts into the matrix increase in both slip velocity and fault slip area, and are 420 therefore drawn downward toward shorter durations and larger moments. Near-threshold 421 model events with low to intermediate clast contents cluster around the slow slip scaling 422 line, specifically overlapping with events characterized by Bletery et al. (2017), referred to 423 as 'secondary slip fronts'. With increasing matrix viscosity, model events are drawn even 424 farther toward shorter durations and greater moments such that they start to overlap with 425 regular earthquake phenomena. This transition between the slow-slip scaling and regular 426 earthquake scaling is a continuous transition as a function of matrix viscosity in our models; 427



Figure 6. a) Cumulative moment release over time, b) computed stress drops as a function of moment magnitude and c) moment-duration statistics for modeled events, colored by viscosity and with symbols representing ρ_c .

⁴²⁸ i.e. we do not observe any gap in moment-duration space between slow slip and regular ⁴²⁹ earthquakes (discussed further in Section 5).

Individual events in our models only partially overlap with the large seismic moments 430 but long durations estimated for several natural slow slip events based on geodetic inversions. 431 For example, our largest moment-longest duration events overlap significantly with slow slip 432 associated with ETS events documented for Cascadia during the time period 2007-2017 (cf. 433 Michel et al., 2019), but individual model events do not reach the larger moments and 434 longer durations that have been documented for some events in Cascadia, and several in 435 New Zealand, Mexico, Alaska and Japan (cf. Fig. 5 in Z. Peng & Gomberg, 2010). This is 436 partly because the maximum moment in our models is limited by our choice of nucleation 437 size (h^*) and model domain length (itself limited by computational expense). However, 438 model limitations aside, a growing body of observations from modern subduction zones 439 suggest that slow slip events may comprise an amalgamation of multiple shorter-duration 440 slip episodes (e.g. Bletery & Nocquet, 2020; Bletery et al., 2017; Frank et al., 2018). Our 441 models potentially capture this behavior in cases where multiple ruptures trigger each other 442 and are closely spaced in time (e.g. Video 1). To qualitatively examine this possibility 443 from the perspective of modeled events, we calculated the cumulative moment for events 444 sampled over random, 1-year intervals in one near-threshold model (grey diamonds in Fig. 445 6b). Events amalgamated in this way reach greater moments and longer durations that more 446 closely overlap with the moment-duration statistics recorded in several modern subduction 447 zones. 448

449 5 Discussion

450

5.1 Implications for Subduction Zone Transient Slip Patterns

In Figure 7 we plot the full suite of models as a regime diagram illustrating the ex-451 pected seismic and transient slip behaviors as a function of matrix viscosity and clast per-452 centage. The patterns of transient slip shown in this plot approximate the behavior of 453 velocity-weakening, frictional-viscous systems for any threshold viscosity and clast size near 454 the nucleation size, so are not strongly dependent on our specific choice of threshold vis-455 cosity, RSF parameters, or shear zone geometry or kinematics. The regime diagram thus 456 provides a useful general framework for understanding how transient deformation may oc-457 cur in heterogeneous frictional-viscous shear zones that define the deep roots of subduction 458 megathrusts and other major plate boundary fault zones. 459

Although temperature was not explicitly implemented in our models, the three model 460 types presented (above-threshold, near-threshold, and below-threshold) can be interpreted 461 as three temperature endmembers along the plate interface because of the strong temper-462 ature dependence of viscosity. Above-threshold models represent low-temperature regions 463 up-dip of the SSE zone, within the megathrust seismogenic region. Because the viscous yield 464 strength is much higher than the frictional yield strength, subduction megathrust seismic-465 ity patterns in this regime have little to do with rock viscous properties, and their source 466 physics are better captured by single-fault models in which frictional properties and/or ge-467 ometries vary, as in numerous previous elastodynamic modeling studies (e.g. Ampuero & 468 Rubin, 2008; J. H. Dieterich, 1992; Kaneko et al., 2008; Lapusta et al., 2000). 469

Near-threshold models, by definition, represent the frictional-viscous transition, and 470 are thus intended to capture temperatures intermediate between those expected up-dip along 471 the seismogenic megathrust and those expected down-dip in the zone of aseismic creep. The 472 events in these models have several features in common with natural SSEs. This includes 473 characteristically slow slip velocities that are \sim 1-3 orders of magnitude faster than the 474 background plate rate, and, for our chosen model input parameters, rupture propagation 475 rates of 0.1-20 km/day, and average stress drops in the range \sim 1-300 kPa. Events in near-476 threshold models also demonstrate that moment magnitudes approaching those derived 477



Figure 7. Regime diagram showing the expected slip behavior as a function of matrix viscosity and clast concentration.

geodetically from natural slow slip events can be produced through summation of multiple
slip events within the 2D model domain and/or through single rupture surfaces that fail
in close succession over time (Fig. 6). The interaction of ruptures within these models,
including triggered events that propagate away from the main rupture front, resembles
observations of tremor migrations in slow slip events (e.g. Bletery et al., 2017; Ghosh et al.,
2010; Hawthorne et al., 2016; Obara et al., 2012; Y. Peng et al., 2015; Rubin & Armbruster,
2013).

With increasing viscosity above the threshold viscosity, the models show a progres-485 sive transition toward faster slip events, with some exhibiting intermediate slip velocities or 486 mixed slow and fast slip. The models thus do not support a fundamental change in mecha-487 nism between fast and slow slip, but instead suggest a progressive decrease (updip)/increase 488 (downdip) in the velocity-strengthening effects of viscous creep. The models predict that 489 the region of the interface between the seismogenic megathrust and the dominantly slow 490 slip zone should exhibit intermediate-velocity slip events that are seismically detectable. 491 Very few natural events matching the moment-duration values expected for this viscosity 492 range have been documented, however, so this reflects a potential discrepancy between our 493 model predictions and natural observations. However, several studies have questioned the 494 idea that slow slip and regular earthquakes obey different scaling relationships, and suggest 495 a continuum between slow slip and regular earthquake fault slip modes (Frank & Brodsky, 496 2019; Gomberg et al., 2016; Hulbert et al., 2019; Leeman et al., 2016; Z. Peng & Gomberg, 497 2010), consistent with our model results. 498

Models in which the viscosity of the shear zone matrix is less than the threshold 499 viscosity are potentially representative of conditions of increasing temperature at the down-500 501 dip extent of the SSE zone and the transition to aseismic creep. Below-threshold models with very high clast contents are the only models to produce small-magnitude, moderately slow-502 velocity events that for our input model parameters resemble very low frequency earthquakes 503 (Figs. 6,7). VLFEs, along with low frequency earthquakes, are commonly interpreted to 504 compose the tectonic tremor signals that accompany slow slip (Ito et al., 2007; Katsumata 505 & Kamaya, 2003; Obara, 2002; Rogers & Dragert, 2003; Shelly et al., 2006). Tremor is 506 most commonly observed on the deeper sections of the subduction plate interface, whereas 507 several recent observations suggest that there is a gap, where only long-term slow slip 508 events are observed, located between the megathrust seismogenic zone and deeper zones of 509 episodic tremor and slow slip (e.g. Kato et al., 2010; Rousset et al., 2017; Takagi et al., 510 2016). This gap is consistent with the observation in our models that VLFE-like events are 511 only produced where the shear zone matrix viscosity is 1-2 orders of magnitude below the 512 threshold viscosity (e.g. at higher temperature conditions of the interface corresponding 513 to deeper depths). Although our models do not explicitly capture this, in the context 514 of our model framework, combined episodic tremor and slow slip may represent slow slip 515 events propagating from near-threshold-viscosity regions into clast-rich domains that contain 516 pockets of lower viscosity material and that are tremorgenic. 517

518

5.2 Comparisons to the Geologic Record

In addition to matching some of the measured geodetic and seismic characteristics of 519 slow slip events, several aspects of our models also resemble features preserved in exhumed 520 rocks. As discussed in Section 1, many exhumed subduction shear zones from the deep 521 interface show evidence for strong viscosity contrasts in the form of rigid blocks embedded 522 in a viscous matrix (e.g. Angiboust et al., 2013, 2011b; Bebout & Barton, 2002; Kotowski 523 & Behr, 2019; Marroni et al., 2009; Rad et al., 2005; Scarsi et al., 2018; Tarling et al., 524 2019; Ukar & Cloos, 2019). Experimental flow laws for subduction related materials sug-525 gest that viscosity contrasts can be up to 4 orders of magnitude for pressure-temperature 526 conditions representative of the downdip megathrust (cf. Fig. 2 in Behr & Becker, 2018). 527 Additionally, different spatial distributions of rigid clasts may be expected not only due to 528 differing amounts of subducted mafic components, but also (especially in the case of warm 529

subduction zones) different degrees of dehydration and metamorphism to form dry eclogite 530 or amphibolite, which are rheologically hardened metamorphic rocks that enhance viscosity 531 contrasts (Behr et al., 2018; Yamato et al., 2019). Several exhumed shear zones further-532 more show evidence that the frictional yield strength in clasts was locally exceeded even 533 near peak subduction depths, with clasts exhibiting both tensile and shear fractures that 534 preserve high pressure mineral assemblages (Angiboust et al., 2011b; Bukała et al., 2020; 535 Kotowski & Behr, 2019; Taetz et al., 2018). Some studies have also described evidence 536 for continuation of structures nucleated in clasts into the surrounding dominantly viscously 537 deformed matrix; whereas others highlight a cyclical interplay between brittle veining and 538 viscoplastic slip on weak matrix cleavage planes (Fagereng et al., 2010; Kotowski & Behr, 539 2019; Platt et al., 2018; Ujiie et al., 2018). 540

Geologic features described above closely resemble the fracture sets and weak slip 541 planes that develop as low state plastic slip zones within our models (Fig. 3). However, 542 block-in-matrix structures and associated faults sets in subduction melange belts are most 543 commonly documented at scales less than 10-100 meters due to limitations in the areas of 544 geologic exposure. Thus, a persistent open question has been whether these types of struc-545 tures could scale up to produce the large magnitudes characteristic of modern SSEs. Our 546 models indicate that this upscaling is very likely to occur at conditions near the frictional-547 viscous transition at moderate clast concentrations, and that it can occur not only through 548 linkages of single rupture surfaces from clast to clast through the matrix, but also through 549 simultaneous or cascading failure of multiple triggered rupture surfaces within a finite-width 550 shear zone (cf. Video 1). Our models thus support the idea that observations from individ-551 ual melange outcrops are one length-scale of an approximately fractal system, that mimic 552 the deformation processes occurring in multi-kilometer-scale (relevant to slow slip) 'mega-553 melange' belts consisting of rheologically heterogeneous underplated terranes (cf. Behr & 554 Bürgmann, 2021). 555

556

5.3 Similarities and Differences to Other Frictional-Viscous Models

Ando et al. (2012) and Nakata et al. (2011) explored rupture dynamics of LFEs and 557 VLFEs simulated for a 2D fault plane with a prescribed slow slip front propagating through 558 heterogeneous patches of contrasting viscous and frictional (velocity-weakening vs. strength-559 ening) properties. Rupture propagation in these models was governed by a viscous damping 560 term such that stress transmission between heterogeneous patches was stifled by low back-561 ground viscosities and/or low patch distributions. Skarbek et al. (2012) similarly exam-562 ined slip behaviors for RSF models with alternating velocity-weakening and strengthening 563 patches, varying both the a-b parameters and the patch distributions. More recently, 564 Lavier et al. (2021) explored the role of brittle-ductile interactions in finite-width shear 565 zones, simulating ductile regions by matching velocity-strengthening frictional properties to 566 variations in viscosity. Each of these model frameworks predicted a transition in rupture 567 behavior from elastodynamic to slow slip, similar to what we observe here. In the purely 568 elastic, one-dimensional model case of Skarbek et al. (2012), the transition from elastody-569 namic slip to slow slip was more abrupt and the range over which slow slip events could 570 be expected was comparatively narrow. In the case of Lavier et al. (2021), velocity-neutral 571 conditions in the ductile matrix are \sim equivalent to our threshold viscosity models, whereas 572 increasing velocity-strengthening conditions simulates decreasing matrix viscosity. Their 573 models produced behaviors similar to our below-threshold models shown in Figure 7, with 574 aseismic creep dominating at low clast concentrations, transitioning to transient slip events 575 when clast concentrations are increased to between 45 and 80% (cf. Figure 4c in Lavier 576 et al. (2021)). In the case of our models, however, these transitions in slip style can be 577 generated simply by varying matrix viscosity, with no variations in the velocity-dependent 578 frictional properties within the shear zone required. 579

Visco-plastic models conducted in a study by Beall et al. (2019) also have some aspects in common with our below-threshold, high-clast-distribution models. Similar to their

observations and previous work on granular materials (Daniels & Hayman, 2008; Hayman 582 et al., 2011; Reber et al., 2015), we see the development of force chains extending across 583 the model domain when clast densities are greater than $\sim 50\%$ (cf. Figure 3e-f). Beall et al. 584 (2019) suggested that the fracturing process in clast-rich shear zones may lead to switches 585 from subduction zone 'jamming', in which clasts control the bulk strain rate, to periods of 586 elevated strain rates localized in intervening weak viscous matrix regions after clast fracture, 587 perhaps consistent with slow slip velocities. Our models suggest that the fracture process 588 itself in jammed, high-viscosity-contrast shear zones may create seismicity that resembles 589 very low frequency earthquakes, but that once these fractures have been generated through-590 out the model domain, the shear zone accommodates the imposed plate velocity by viscous 591 creep at steady state. Incorporation of fracture healing processes could result in a regular 592 oscillation of this process, however, potentially supporting the model proposed by Beall et 593 al. (2019). However, our models also predict viscously-damped, yet still frictional slow slip, 594 even in cases where the matrix viscosity (and associated viscous strain rate) is not particu-595 larly low and where clast concentrations are not high enough for clasts to directly interact; 596 thus our models predict a wider range of conditions of both viscosity and clast concentration 597 where slow slip may be anticipated (Fig. 7). 598

Our results are also consistent with previous models that emphasize the potential for 599 frictional-viscous interactions to modulate event slip velocities, and for slow slip events to 600 occur near the brittle-ductile or frictional-viscous transition in subduction environments (e.g. 601 Goswami & Barbot, 2018), even in the absence of discretely implemented heterogeneities. 602 Recent models by Petrini et al. (2020), for example, suggested predominant development of 603 slow slip events at the downdip limit of the megathrust in a zone of prescribed gradually 604 decreasing matrix viscosity. Above and below this transitional zone, respectively, seismic 605 ruptures and aseismic slip emerged; and the moment-duration distributions computed by 606 Petrini et al. (2020) bear several similarities with our results, despite implementation of 607 quite different constitutive relationships. 608

Overall, a primary advantage to our model framework is the incorporation of a finite-609 width shear zone, which allows analysis of how spontaneously-generated, geometrically com-610 plex, rupture surfaces (e.g. similar to those observed in the rock record) may interact with 611 each other, and how they may scale up to resemble a slow slip event (e.g. similar to those 612 recorded using geodetic methods in active fault zones). There are also several limitations 613 to the current model setup, however, that could pave the way for future developments, 614 including exploration of realistic temperature and pressure gradients and shear heating, dy-615 namic pressure and pore fluid pressure evolution, power law viscosity or viscous anisotropy 616 effects, time evolution of the state variable to simulate fault healing processes, and effects 617 of simultaneously varying frictional and viscous properties. 618

619 6 Conclusions

We show that models simulating earthquakes and transient slip events in heterogeneous 620 viscoelastoplastic shear zones resembling subduction 'mega-melange' belts can reproduce 621 several key aspects of natural slow slip and tremor phenomena, including matching slip 622 velocities, propagation rates, and stress drops. For conditions near the frictional-viscous 623 transition, the viscous component of these shear zones, and the stress heterogeneity set 624 up by the presence of rigid clasts, set a 'speed limit' for earthquake ruptures such that 625 they slip and propagate at velocities similar to natural slow slip events, despite constant 626 velocity-weakening frictional properties. The viscous component simultaneously permits the 627 transmission of slow slip from clast to clast, allowing slow ruptures to propagate substantial 628 distances, even in cases where clasts are widely spaced—this potentially reconciles how slip 629 planes observed at the outcrop scale by geologists may scale up to achieve hundred kilometer 630 scales implied by geodetic inversions of slow slip events. Additionally, the implementation of 631 a finite-width shear zone allows us to observe coalescence, triggering and reverse-propagation 632 among multiple rupture surfaces within a thicker elevated-slip-rate zone, also consistent 633

with emerging observations of slow slip as clusters of multiple slip transients. If our model framework of slow slip representing fault plane interactions within a finite-width shear zone is correct, it implies that estimated moments and recurrence intervals from natural slow slip and tremor events do not necessarily represent repeated failure of a single rupture plane, but instead may reflect multiple rupture planes slipping simultaneously or cascading through the width of a subduction interface shear zone.

640 Acknowledgments

This research was funded by an ERC Starting Grant (S-SIM, grant no. 947659) awarded to W.M.Behr and by an Swiss National Science Foundation grant awarded to T. Gerya (grant no. 200021-192296). WM Behr acknowledges several helpful discussions of the manuscript content with Thorsten Becker. All model images utilized the perceptually uniform colormaps from Crameri (2018). Data for model input parameters and videos of exemplary model runs will be made available on the ETH Research Collection data repository upon publication of this manuscript.

648 References

- Agard, P., Plunder, A., Angiboust, S., Bonnet, G., & Ruh, J. (2018). The subduction plate
 interface: rock record and mechanical coupling (from long to short timescales). *Lithos*,
 320, 537–566.
- Ampuero, J.-P., & Rubin, A. M. (2008). Earthquake nucleation on rate and state faults –
 aging and slip laws. *Journal of Geophysical Research*, 113(B1).
- Ando, R., Takeda, N., & Yamashita, T. (2012). Propagation dynamics of seismic and aseis mic slip governed by fault heterogeneity and newtonian rheology. *Journal of Geophysical Research: Solid Earth*, 117(B11).
- Angiboust, S., Agard, P., De Hoog, J., Omrani, J., & Plunder, A. (2013). Insights on
 deep, accretionary subduction processes from the sistan ophiolitic "mélange" (eastern
 iran). Lithos, 156, 139–158.
- Angiboust, S., Agard, P., Raimbourg, H., Yamato, P., & Huet, B. (2011a). Subduction
 interface processes recorded by eclogite-facies shear zones (monviso, w. alps). *Lithos*,
 127(1-2), 222–238.
- Angiboust, S., Agard, P., Raimbourg, H., Yamato, P., & Huet, B. (2011b). Subduction
 interface processes recorded by eclogite-facies shear zones (monviso, w. alps). Lithos,
 127(1-2), 222–238.
- Audet, P., Bostock, M. G., Christensen, N. I., & Peacock, S. M. (2009). Seismic evidence for
 overpressured subducted oceanic crust and megathrust fault sealing. *Nature*, 457(7225),
 76–78.
- Audet, P., & Bürgmann, R. (2014). Possible control of subduction zone slow-earthquake
 periodicity by silica enrichment. *Nature*, 510(7505), 389–392.
- Audet, P., & Kim, Y. (2016). Teleseismic constraints on the geological environment of deep
 episodic slow earthquakes in subduction zone forearcs: A review. *Tectonophysics*, 670, 1–15.
- Audet, P., & Schaeffer, A. J. (2018). Fluid pressure and shear zone development over the locked to slow slip region in cascadia. *Science Advances*, 4(3), eaar2982.
- Beall, A., Fagereng, Å., & Ellis, S. (2019). Fracture and weakening of jammed subduction
 shear zones, leading to the generation of slow slip events. *Geochemistry, Geophysics, Geosystems, 20*(11), 4869–4884.
- Bebout, G. E., & Barton, M. D. (2002). Tectonic and metasomatic mixing in a hight, subduction-zone mélange—insights into the geochemical evolution of the slab-mantle
 interface. Chemical Geology, 187(1-2), 79–106.
- Beeler, N. M. (2009). Constructing constitutive relationships for seismic and aseismic fault
- slip. Mechanics, Structure and Evolution of Fault Zones, 1775–1798.

- Behr, W., & Becker, T. W. (2018). Sediment control on subduction plate speeds. Earth
 and Planetary Science Letters, 502, 166–173.
- Behr, W., & Bürgmann, R. (2021). Whats down there? the structures, materials and environment of deep-seated slow slip and tremor. *Phil. Trans. Roy. Soc.*, 379.
- Behr, W., Kotowski, A. J., & Ashley, K. T. (2018). Dehydration-induced rheological heterogeneity and the deep tremor source in warm subduction zones. *Geology*, 46(5), 475-478.
- Behr, W., & Platt, J. (2013). Rheological evolution of a mediterranean subduction complex.
 Journal of Structural Geology, 54, 136–155.
- Beroza, G. C., & Ide, S. (2011). Slow earthquakes and nonvolcanic tremor. Annual Review of Earth and Planetary Sciences, 39(1), 271–296.
- ⁶⁹⁵ Bletery, Q., & Nocquet, J.-M. (2020). Slip bursts during coalescence of slow slip events in ⁶⁹⁶ cascadia. *Nature Communications*, 11(1).
- Bletery, Q., Thomas, A. M., Hawthorne, J. C., Skarbek, R. M., Rempel, A. W., & Krogstad,
 R. D. (2017). Characteristics of secondary slip fronts associated with slow earthquakes
 in cascadia. *Earth and Planetary Science Letters*, 463, 212–220.
- Bukała, M., Barnes, C., Jeanneret, P., Hidas, K., Mazur, S., & Almqvist, B. (2020). Ko smi
 nska k, klonowska i, šurka j and majka j (2020) brittle deformation during eclogitization
 of early paleozoic blueschist. front. Front. Earth Sci, 8, 594453.
- Calvert, A. J. (1996). Seismic reflection constraints on imbrication and underplating of
 the northern cascadia convergent margin. *Canadian Journal of Earth Sciences*, 33(9),
 1294–1307.
- Calvert, A. J., Bostock, M. G., Savard, G., & Unsworth, M. J. (2020). Cascadia low
 frequency earthquakes at the base of an overpressured subduction shear zone. *Nature Communications*, 11(1).
- Chen, K. H., Tai, H.-J., Ide, S., Byrne, T. B., & Johnson, C. W. (2018). Tidal modulation
 and tectonic implications of tremors in taiwan. *Journal of Geophysical Research: Solid Earth*, 123(7), 5945–5964.
- Cloos, M., & Shreve, R. L. (1988). Subduction-channel model of prism accretion, melange
 formation, sediment subduction, and subduction erosion at convergent plate margins: 2.
 implications and discussion. *Pure and Applied Geophysics*, 128(3), 501–545.
- Condit, C. B., Guevara, V. E., Delph, J. R., & French, M. E. (2020). Slab dehydration
 in warm subduction zones at depths of episodic slip and tremor. *Earth and Planetary Science Letters*, 552, 116601.
- ⁷¹⁸ Cowan, D. S. (1985). Structural styles in mesozoic and cenozoic mélanges in the western ⁷¹⁹ cordillera of north america. *Geological Society of America Bulletin*, 96(4), 451–462.
- Crameri, F. (2018). Geodynamic diagnostics, scientific visualisation and staglab 3.0. Geoscientific Model Development, 11(6), 2541–2562.
- Daniels, K. E., & Hayman, N. W. (2008). Force chains in seismogenic faults visualized with
 photoelastic granular shear experiments. Journal of Geophysical Research: Solid Earth,
 113(B11).
- Delph, J. R., Levander, A., & Niu, F. (2018). Fluid controls on the heterogeneous seismic characteristics of the cascadia margin. *Geophysical Research Letters*, 45(20).
- Dieterich, J. (1994). A constitutive law for rate of earthquake production and its application
 to earthquake clustering. Journal of Geophysical Research: Solid Earth, 99(B2), 2601–
 2618.
- Dieterich, J. H. (1979). Modeling of rock friction: 1. experimental results and constitutive equations. *Journal of Geophysical Research*, 84 (B5), 2161.
- Dieterich, J. H. (1992). Earthquake nucleation on faults with rate-and state-dependent
 strength. *Tectonophysics*, 211(1-4), 115–134.
- Fagereng, Å. (2011). Frequency-size distribution of competent lenses in a block-in-matrix
 mélange: Imposed length scales of brittle deformation? Journal of Geophysical Research,
 116(B5).
- Fagereng, Å., & Den Hartog, S. A. (2017). Subduction megathrust creep governed by

- pressure solution and frictional-viscous flow. Nature Geoscience, 10(1), 51-57.
- Fagereng, Å., Hillary, G. W., & Diener, J. F. (2014). Brittle-viscous deformation, slow slip,
 and tremor. *Geophysical Research Letters*, 41(12), 4159–4167.
- Fagereng, Å., Remitti, F., & Sibson, R. H. (2010). Shear veins observed within anisotropic
 fabric at high angles to the maximum compressive stress. *Nature Geoscience*, 3(7), 482–
 485.
- Fagereng, Å., & Sibson, R. H. (2010). Mélange rheology and seismic style. *Geology*, 38(8),
 751–754.
- Festa, A., Pini, G. A., Dilek, Y., & Codegone, G. (2010). Mélanges and mélange-forming
 processes: a historical overview and new concepts. *International Geology Review*, 52(10-12), 1040–1105.
- Fisher, D., & Byrne, T. (1987). Structural evolution of underthrusted sediments, kodiak
 islands, alaska. *Tectonics*, 6(6), 775–793.
- Fisher, D., Smye, A., Marone, C., van Keken, P., & Yamaguchi, A. (2019). Kinetic mod els for healing of the subduction interface based on observations of ancient accretionary
 complexes. *Geochemistry, Geophysics, Geosystems, 20*(7), 3431–3449.
- Frank, W. B., & Brodsky, E. E. (2019). Daily measurement of slow slip from low-frequency
 earthquakes is consistent with ordinary earthquake scaling. *Science advances*, 5(10),
 eaaw9386.
- Frank, W. B., Rousset, B., Lasserre, C., & Campillo, M. (2018). Revealing the cluster of
 slow transients behind a large slow slip event. *Science advances*, 4(5), eaat0661.
- ⁷⁵⁹ Ghosh, A., Vidale, J. E., Sweet, J. R., Creager, K. C., Wech, A. G., Houston, H., &
 ⁷⁶⁰ Brodsky, E. E. (2010). Rapid, continuous streaking of tremor in cascadia. *Geochemistry,* ⁷⁶¹ *Geophysics, Geosystems,* 11(12).
- Gomberg, J., Wech, A., Creager, K., Obara, K., & Agnew, D. (2016). Reconsidering
 earthquake scaling. *Geophysical Research Letters*, 43(12), 6243–6251.
- Goswami, A., & Barbot, S. (2018). Slow-slip events in semi-brittle serpentinite fault zones.
 Scientific reports, 8(1), 1–11.
- Grigull, S., Krohe, A., Moos, C., Wassmann, S., & Stöckhert, B. (2012). "order from chaos":
 a field-based estimate on bulk rheology of tectonic mélanges formed in subduction zones.
 Tectonophysics, 568, 86–101.
- Hansen, R. T. J., Bostock, M. G., & Christensen, N. I. (2012). Nature of the low velocity
 zone in cascadia from receiver function waveform inversion. *Earth and Planetary Science Letters*, 337-338, 25–38.
- Hawthorne, J. C., Bostock, M. G., Royer, A. A., & Thomas, A. M. (2016). Variations in slow slip moment rate associated with rapid tremor reversals in cascadia. *Geochemistry*, *Geophysics*, *Geosystems*, 17(12), 4899–4919.
- Hawthorne, J. C., & Rubin, A. M. (2013). Laterally propagating slow slip events in a rate and state friction model with a velocity-weakening to velocity-strengthening transition. *Journal of Geophysical Research: Solid Earth*, 118(7), 3785–3808.
- Hayman, N. W., Ducloué, L., Foco, K. L., & Daniels, K. E. (2011). Granular controls on periodicity of stick-slip events: kinematics and force-chains in an experimental fault. *Pure and applied geophysics*, 168(12), 2239–2257.
- Hayman, N. W., & Lavier, L. L. (2014). The geologic record of deep episodic tremor and slip. *Geology*, 42(3), 195–198.
- Herrendörfer, R., Gerya, T., & van Dinther, Y. (2018). An invariant rate- and State Dependent friction formulation for viscoeastoplastic earthquake cycle simulations. Journal
 of Geophysical Research: Solid Earth, 123(6), 5018–5051.
- Hulbert, C., Rouet-Leduc, B., Johnson, P. A., Ren, C. X., Rivière, J., Bolton, D. C., &
 Marone, C. (2019). Similarity of fast and slow earthquakes illuminated by machine
 learning. *Nature Geoscience*, 12(1), 69–74.
- Ide, S., Beroza, G. C., Shelly, D. R., & Uchide, T. (2007). A scaling law for slow earthquakes.
 Nature, 447(7140), 76–79.
- Im, K., Saffer, D., Marone, C., & Avouac, J.-P. (2020). Slip-rate-dependent friction as a

- ⁷⁹² universal mechanism for slow slip events. *Nature Geoscience*, 13(10), 705–710.
- Ito, Y., Obara, K., Shiomi, K., Sekine, S., & Hirose, H. (2007, January). Slow earthquakes
 coincident with episodic tremors and slow slip events. *Science*, 315(5811), 503–506.
- Kaneko, Y., Lapusta, N., & Ampuero, J.-P. (2008). Spectral element modeling of sponta neous earthquake rupture on rate and state faults: Effect of velocity-strengthening friction
 at shallow depths. Journal of Geophysical Research, 113(B9).
- Kato, A., Iidaka, T., Ikuta, R., Yoshida, Y., Katsumata, K., Iwasaki, T., ... Hirata, N.
 (2010). Variations of fluid pressure within the subducting oceanic crust and slow earthquakes. *Geophysical Research Letters*, 37(14).
- Katsumata, A., & Kamaya, N. (2003). Low-frequency continuous tremor around the moho discontinuity away from volcanoes in the southwest japan. *Geophysical Research Letters*, $3\theta(1)$, 20–21.
- Kotowski, A. J., & Behr, W. (2019). Length scales and types of heterogeneities along the
 deep subduction interface: Insights from exhumed rocks on syros island, greece. *Geosphere*, 15(4), 1038–1065.
- Lapusta, N., Rice, J. R., Ben-Zion, Y., & Zheng, G. (2000). Elastodynamic analysis for slow tectonic loading with spontaneous rupture episodes on faults with rate- and statedependent friction. *Journal of Geophysical Research: Solid Earth*, 105 (B10), 23765– 23789.
- Lavier, L. L., Tong, X., & Biemiller, J. (2021). The mechanics of creep, slow slip events and earthquakes in mixed brittle-ductile fault zones. *Journal of Geophysical Research: Solid Earth*, e2020JB020325.
- Lay, T., Kanamori, H., Ammon, C. J., Koper, K. D., Hutko, A. R., Ye, L., ... Rushing, T. M. (2012). Depth-varying rupture properties of subduction zone megathrust faults. *Journal of Geophysical Research: Solid Earth*, 117(B4).
- Leeman, J., Saffer, D., Scuderi, M., & Marone, C. (2016). Laboratory observations of slow earthquakes and the spectrum of tectonic fault slip modes. *Nature communications*, 7(1), 1-6.
- Li, J., Shillington, D. J., Bécel, A., Nedimović, M. R., Webb, S. C., Saffer, D. M., ... Kuehn,
 H. (2015). Downdip variations in seismic reflection character: Implications for fault
 structure and seismogenic behavior in the alaska subduction zone. *Journal of Geophysical Research: Solid Earth*, 120(11), 7883–7904.
- Liu, Y., & Rice, J. (2005). Aseismic slip transients emerge spontaneously in threedimensional rate and state modeling of subduction earthquake sequences. *Journal of Geophysical Research*, 110(B8).
- Liu, Y., & Rubin, A. M. (2010). Role of fault gouge dilatancy on aseismic deformation transients. *Journal of Geophysical Research*, 115(B10).
- Marone, C. (1998). Laboratory-derived friction laws and their application to seismic faulting. Annual Review of Earth and Planetary Sciences, 26(1), 643–696.
- Marone, C., Vidale, J. E., & Ellsworth, W. L. (1995). Fault healing inferred from time
 dependent variations in source properties of repeating earthquakes. *Geophysical Research Letters*, 22(22), 3095–3098.
- Marroni, M., Pandolfi, L., Principi, G., Malasoma, A., & Meneghini, F. (2009). Deformation history of the eclogite-and jadeitite-bearing mélange from north motagua fault zone, guatemala: insights in the processes of a fossil subduction channel. *Geological Journal*, 44(2), 167–190.
- McLaskey, G. C., Thomas, A. M., Glaser, S. D., & Nadeau, R. M. (2012). Fault healing
 promotes high-frequency earthquakes in laboratory experiments and on natural faults.
 Nature, 491(7422), 101–104.
- Michel, S., Gualandi, A., & Avouac, J.-P. (2019). Similar scaling laws for earthquakes and cascadia slow-slip events. *Nature*, 574 (7779), 522–526.
- Nakata, R., Ando, R., Hori, T., & Ide, S. (2011). Generation mechanism of slow earthquakes: Numerical analysis based on a dynamic model with brittle-ductile mixed fault heterogeneity. *Journal of Geophysical Research*, 116(B8).

- Nedimović, M. R., Hyndman, R. D., Ramachandran, K., & Spence, G. D. (2003). Reflection signature of seismic and aseismic slip on the northern cascadia subduction interface. *Nature*, 424 (6947), 416–420.
- Obara, K. (2002, May). Nonvolcanic deep tremor associated with subduction in southwest japan. *Science*, 296 (5573), 1679–1681.
- Obara, K., Matsuzawa, T., Tanaka, S., & Maeda, T. (2012). Depth-dependent mode of tremor migration beneath kii peninsula, nankai subduction zone. *Geophysical research letters*, 39(10).
- Obara, K., & Sekine, S. (2009). Characteristic activity and migration of episodic tremor and slow-slip events in central japan. *Earth, Planets and Space*, 61(7), 853–862.
- Peacock, S. M. (2009). Thermal and metamorphic environment of subduction zone episodic tremor and slip. *Journal of Geophysical Research*, 114.
- Peacock, S. M., Christensen, N. I., Bostock, M. G., & Audet, P. (2011). High pore pressures
 and porosity at 35 km depth in the cascadia subduction zone. *Geology*, 39(5), 471–474.
- Peng, Y., Rubin, A. M., Bostock, M. G., & Armbruster, J. G. (2015). High-resolution
 imaging of rapid tremor migrations beneath southern vancouver island using cross-station
 cross correlations. Journal of Geophysical Research: Solid Earth, 120(6), 4317–4332.
- Peng, Z., & Gomberg, J. (2010). An integrated perspective of the continuum between
 earthquakes and slow-slip phenomena. *Nature Geoscience*, 3(9), 599–607.
- Petrini, C., Gerya, T., Yarushina, V., van Dinther, Y., Connolly, J., & Madonna, C. (2020).
 Seismo-hydro-mechanical modelling of the seismic cycle: methodology and implications
 for subduction zone seismicity. *Tectonophysics*, 791, 228504.
- Phillips, N. J., Motohashi, G., Ujiie, K., & Rowe, C. D. (2020). Evidence of localized failure
 along altered basaltic blocks in tectonic mélange at the updip limit of the seismogenic
 zone: Implications for the shallow slow earthquake source. *Geochemistry, Geophysics, Geosystems*, 21(7), e2019GC008839.
- Platt, J. P., Xia, H., & Schmidt, W. L. (2018). Rheology and stress in subduction zones around the aseismic/seismic transition. *Progress in Earth and Planetary Science*, 5(1), 1–12.
- Preuss, S., Herrendörfer, R., Gerya, T., Ampuero, J.-P., & van Dinther, Y. (2019). Seismic and aseismic fault growth lead to different fault orientations. *Journal of Geophysical Research: Solid Earth*, 124(8), 8867–8889.
- Rad, G. F., Droop, G., Amini, S., & Moazzen, M. (2005). Eclogites and blueschists of
 the sistan suture zone, eastern iran: a comparison of P–T histories from a subduction
 mélange. Lithos, 84 (1-2), 1–24.
- Reber, J. E., Lavier, L. L., & Hayman, N. W. (2015). Experimental demonstration of a
 semi-brittle origin for crustal strain transients. *Nature Geoscience*, 8(9), 712–715.
- Rice, J. R., Lapusta, N., & Ranjith, K. (2001). Rate and state dependent friction and the
 stability of sliding between elastically deformable solids. *Journal of the Mechanics and Physics of Solids*, 49(9), 1865–1898.
- Rogers, G., & Dragert, H. (2003, June). Episodic tremor and slip on the cascadia subduction
 zone: the chatter of silent slip. *Science*, 300(5627), 1942–1943.
- Rousset, B., Campillo, M., Lasserre, C., Frank, W. B., Cotte, N., Walpersdorf, A., ...
 Kostoglodov, V. (2017). A geodetic matched filter search for slow slip with application to the mexico subduction zone. *Journal of Geophysical Research: Solid Earth*, 122(12), 10–498.
- Rousset, B., Fu, Y., Bartlow, N., & Bürgmann, R. (2019). Weeks-Long and Years-Long
 slow slip and tectonic tremor episodes on the south central alaska megathrust. *Journal*of Geophysical Research: Solid Earth, 124(12), 13392–13403.
- Rubin, A. M. (2008). Episodic slow slip events and rate-and-state friction. Journal of Geophysical Research, 113(B11).
- Rubin, A. M., & Ampuero, J.-P. (2005). Earthquake nucleation on (aging) rate and state
 faults. Journal of Geophysical Research: Solid Earth, 110(B11).
- Rubin, A. M., & Armbruster, J. G. (2013). Imaging slow slip fronts in cascadia with high

- precision cross-station tremor locations. Geochemistry, Geophysics, Geosystems, 14(12),
 5371–5392.
- Ruina, A. (1983). Slip instability and state variable friction laws. Journal of Geophysical Research: Solid Earth, 88(B12), 10359–10370.
- Scarsi, M., Malatesta, C., & Fornasaro, S. (2018). Lawsonite-bearing eclogite from a tectonic
 mélange in the ligurian alps: New constraints for the subduction plate-interface evolution.
 Geological Magazine, 155(2), 280–297.
- Schmidt, D. A., & Gao, H. (2010). Source parameters and time-dependent slip distribu tions of slow slip events on the cascadia subduction zone from 1998 to 2008. Journal of Geophysical Research, 115.
- Segall, P., & Bradley, A. M. (2012). The role of thermal pressurization and dilatancy in controlling the rate of fault slip. *Journal of Applied Mechanics*, 79(3).
- Segall, P., Rubin, A. M., Bradley, A. M., & Rice, J. R. (2010). Dilatant strengthening as a mechanism for slow slip events. *Journal of Geophysical Research*, 115(B12).
- Shelly, D. R. (2017). A 15 year catalog of more than 1 million low-frequency earthquakes:
 Tracking tremor and slip along the deep san andreas fault. Journal of Geophysical Research: Solid Earth, 122(5), 3739–3753.
- ⁹¹⁷ Shelly, D. R., Beroza, G. C., & Ide, S. (2007). Non-volcanic tremor and low-frequency ⁹¹⁸ earthquake swarms. *Nature*, 446(7133), 305–307.
- Shelly, D. R., Beroza, G. C., Ide, S., & Nakamula, S. (2006, July). Low-frequency earthquakes in shikoku, japan, and their relationship to episodic tremor and slip. *Nature*,
 442(7099), 188–191.
- Shibazaki, B. (2003). On the physical mechanism of silent slip events along the deeper part of the seismogenic zone. *Geophysical Research Letters*, 30(9).
- Sibson, R. (1992). Implications of fault-valve behaviour for rupture nucleation and recurrence. *Tectonophysics*, 211(1-4), 283–293.
- Skarbek, R. M., Rempel, A. W., & Schmidt, D. A. (2012). Geologic heterogeneity can
 produce aseismic slip transients. *Geophysical Research Letters*, 39(21).
- Stöckhert, B. (2002). Stress and deformation in subduction zones: insight from the record of exhumed metamorphic rocks. *Geological Society, London, Special Publications*, 200(1), 255–274.
- Suzuki, T., & Yamashita, T. (2009). Dynamic modeling of slow earthquakes based on ther moporoelastic effects and inelastic generation of pores. Journal of Geophysical Research, 114.
- Taetz, S., John, T., Bröcker, M., Spandler, C., & Stracke, A. (2018). Fast intraslab fluid-flow events linked to pulses of high pore fluid pressure at the subducted plate interface. *Earth and Planetary Science Letters*, 482, 33–43.
- Takagi, R., Obara, K., & Maeda, T. (2016). Slow slip event within a gap between tremor and locked zones in the nankai subduction zone. *Geophysical Research Letters*, 43(3), 1066–1074.
- Tarling, M. S., Smith, S. A., & Scott, J. M. (2019). Fluid overpressure from chemical reactions in serpentinite within the source region of deep episodic tremor. *Nature Geoscience*, 12(12), 1034–1042.
- Tewksbury-Christle, C., Behr, W., & Helper, M. (2021). Tracking deep sediment underplat ing in a fossil subduction margin: implications for interface rheology and mass and volatile
 recycling. *Geophysics, Geochemistry, Geosystems, in press.* doi: 10.1029/2020GC009463
- Thomas, A. M., Nadeau, R. M., & Bürgmann, R. (2009). Tremor-tide correlations and near-lithostatic pore pressure on the deep san andreas fault. *Nature*, 462(7276), 1048– 1051.
- ⁹⁴⁹ Ujiie, K., Saishu, H., Fagereng, Å., Nishiyama, N., Otsubo, M., Masuyama, H., & Kagi,
 ⁹⁵⁰ H. (2018). An explanation of episodic tremor and slow slip constrained by crack-seal
 ⁹⁵¹ veins and viscous shear in subduction mélange. *Geophysical Research Letters*, 45(11),
 ⁹⁵² 5371–5379.
- ⁹⁵³ Ukar, E., & Cloos, M. (2019). Cataclastic deformation and metasomatism in the subduction

zone of mafic blocks-in-mélange, san simeon, california. *Lithos*, 346, 105116.

- van Dinther, Y., Gerya, T., Dalguer, L., Mai, P. M., Morra, G., & Giardini, D. (2013). The seismic cycle at subduction thrusts: Insights from seismo-thermo-mechanical models.
- Journal of Geophysical Research: Solid Earth, 118(12), 6183–6202.
- Wallace, L. M., & Eberhart-Phillips, D. (2013). Newly observed, deep slow slip events at the
 central hikurangi margin, new zealand: Implications for downdip variability of slow slip
 and tremor, and relationship to seismic structure. *Geophysical Research Letters*, 40(20),
 5393–5398.
- Warren-Smith, E., Fry, B., Wallace, L., Chon, E., Henrys, S., Sheehan, A., ... Lebedev, S.
 (2019). Episodic stress and fluid pressure cycling in subducting oceanic crust during slow slip. *Nature Geoscience*, 12(6), 475–481.
- Wassmann, S., & Stoeckhert, B. (2013). Rheology of the plate interface—dissolution precipitation creep in high pressure metamorphic rocks. *Tectonophysics*, 608, 1–29.
- Wech, A. G., & Bartlow, N. M. (2014). Slip rate and tremor genesis in Cascadia. Geophysical Research Letters, 41(2), 392–398.
- Wech, A. G., Boese, C. M., Stern, T. A., & Townend, J. (2012). Tectonic tremor and deep slow slip on the alpine fault. *Geophysical Research Letters*, 39(10).
- Xia, H., & Platt, J. P. (2017). Structural and rheological evolution of the laramide subduction channel in southern california. *Solid Earth*, 8(2), 379–403.
- Yamato, P., Duretz, T., & Angiboust, S. (2019). Brittle/ductile deformation of eclogites:
- insights from numerical models. Geochemistry, Geophysics, Geosystems, 20(7), 3116–
 3133.