# Estimation of absolute stress in the hypocentral region of the 2019 Ridgecrest, California, earthquakes

Yuri Fialko<sup>1</sup>

 $^{1}\text{UCSD}$ 

November 21, 2022

#### Abstract

Strength of the upper brittle part of the Earth's lithosphere controls deformation styles in tectonically active regions, surface topography, seismicity, and the occurrence of plate tectonics, yet it remains one of the most debated quantities in geophysics. Direct measurements of stresses acting at seismogenic depths are largely lacking. Seismic data (in particular, earthquake focal mechanisms) have been used to infer orientation of the principal stress axes. I show that the focal mechanism data can be combined with information from precise earthquake locations to place constraints not only on the orientation, but also on the magnitude of absolute stress at depth. The proposed method uses relative attitudes of conjugate faults to evaluate the amplitude and spatial heterogeneity of the deviatoric stress and frictional strength in the seismogenic zone. Relative fault orientations. (dihedral angles) and sense of slip are determined using quasi-planar clusters of seismicity and their composite focal mechanisms. The observed distribution of dihedral angles between active conjugate faults in the area of Ridgecrest (California, USA) that hosted a recent sequence of strong earthquakes suggests in situ coefficient of friction of 0.4-0.6, and depth-averaged shear stress on the order of 25-40 MPa, intermediate between predictions of the "strong" and "weak" fault theories.

# Estimation of absolute stress in the hypocentral region of the 2019 Ridgecrest, California, earthquakes

Y.  $Fialko^1$ 

Y. Fialko, Scripps Institution of Oceanography, UCSD, 9500 Gilman Dr. 0225, La Jolla, CA 92093-0225, USA. (yfialko@ucsd.edu)

<sup>1</sup>Institute of Geophysics and Planetary

Physics, Scripps Institution of

Oceanography, University of California, San

Diego, La Jolla, California, USA.

Abstract. Strength of the upper brittle part of the Earth's lithosphere 3 controls deformation styles in tectonically active regions, surface topogra-4 phy, seismicity, and the occurrence of plate tectonics, yet it remains one of 5 the most debated quantities in geophysics. Direct measurements of stresses 6 acting at seismogenic depths are largely lacking. Seismic data (in particu-7 lar, earthquake focal mechanisms) have been used to infer orientation of the 8 principal stress axes. I show that the focal mechanism data can be combined q with information from precise earthquake locations to place constraints not 10 only on the orientation, but also on the magnitude of absolute stress at depth. 11 The proposed method uses relative attitudes of conjugate faults to evaluate 12 the amplitude and spatial heterogeneity of the deviatoric stress and frictional 13 strength in the seismogenic zone. Relative fault orientations (dihedral an-14 gles) and sense of slip are determined using quasi-planar clusters of seismic-15 ity and their composite focal mechanisms. The observed distribution of di-16 hedral angles between active conjugate faults in the area of Ridgecrest (Cal-17 ifornia, USA) that hosted a recent sequence of strong earthquakes suggests 18 in situ coefficient of friction of 0.4-0.6, and depth-averaged shear stress on 19 the order of 25-40 MPa, intermediate between predictions of the "strong" 20 and "weak" fault theories. 21

DRAFT

March 3, 2021, 12:57pm

DRAFT

Х - 2

## 1. Introduction

There is a long-standing debate regarding the level of average shear stress in the Earth's 22 crust [Rice, 1992; Hardebeck and Hauksson, 2001; Scholz, 2000]. Estimates of earthquake 23 stress drops place a lower bound on shear stress resolved on seismogenic faults on the 24 order of 1 - 10 MPa [Choy and Boatwright, 1995; Allmann and Shearer, 2009]. Laboratory 25 measurements of quasi-static rock friction [Byerlee, 1978; Dieterich, 1981; Marone, 1998; 26 Mitchell et al., 2013, 2015], orientation of young faults with respect to the inferred principal 27 stress axes [Walsh and Watterson, 1988; Collectini and Sibson, 2001], and measurements 28 in deep boreholes in stable intraplate interiors [Zoback et al., 1993; Townend and Zoback, 29 2000 suggest that the brittle upper crust should be able to support much higher deviatoric 30 stresses on the order of the lithostatic pressure (> 100 MPa for  $\sim$ 15 km thick seismogenic 31 zone), provided that the pore fluid pressure is approximately hydrostatic. Extrapolation of 32 laboratory measurements of quasi-static friction to in situ rock failure, and the assumption 33 of hydrostatic pore pressure constitute the so-called "strong fault" theory [Byerlee, 1978; 34 Scholz, 2000]. 35

In contrast, unfavorable orientation of some mature faults with respect to the principal stress axes [Mount and Suppe, 1987; Wernicke, 1995; Wang and Fialko, 2018], the "heat flow paradox" of the San Andreas Fault [Lachenbruch and Sass, 1980], high degree of slip localization on exhumed faults [Chester et al., 2005; Fialko, 2015], a possibility of fluid over-pressurization [Sibson, 2004], low frictional strength of some parts of mature faults suggested by scientific drilling experiments [Lockner et al., 2011], and strong dynamic weakening observed in laboratory friction experiments at slip rates in excess of  $\sim 0.1$ 

DRAFT

March 3, 2021, 12:57pm

<sup>43</sup> m/s [*Han et al.*, 2007; *Di Toro et al.*, 2011; *Goldsby and Tullis*, 2011; *Brown and Fialko*, <sup>44</sup> 2012] lend support to the "weak fault" theory according to which faults may operate at <sup>45</sup> background deviatoric stresses well below the failure envelope predicted by the Byerlee's <sup>46</sup> law [e.g., *Sibson*, 1990; *Noda et al.*, 2009; *Thomas et al.*, 2014]. Low effective friction <sup>47</sup> on major plate boundary faults is also warranted by geodynamic models of large-scale <sup>48</sup> tectonic phenomena such as subduction and orogeny [e.g., *Toth and Gurnis*, 1998; *Sobolev* <sup>49</sup> *and Babeyko*, 2005; *Stern and Gerya*, 2018].

One possible explanation reconciling disparate views on the magnitude of deviatoric 50 stresses in the lithosphere is that the effective fault strength may depend on the fault 51 "age", or total offset: young developing faults may be relatively strong while mature well-52 slipped faults may be weak, possibly because of activation of various weakening mech-53 anisms with an increasing cumulative slip [Fialko and Khazan, 2005; Rice, 2006; Noda 54 et al., 2009; Thomas et al., 2014; Fialko, 2015]. However, conditions that govern such a 55 transition, and the evolution of fault strength as a function of a cumulative offset are still 56 poorly known. 57

<sup>58</sup> Our understanding of the fault strength problem is severely limited by the lack of mea-<sup>59</sup> surements of deviatoric stress at seismogenic depths. Apart from a scarce set of point <sup>60</sup> measurements in deep boreholes [*Plumb and Hickman*, 1985; *Zoback et al.*, 1993; *Lockner* <sup>61</sup> *et al.*, 2011], most of the available information is derived from analyses of seismic data. <sup>62</sup> The most commonly used method of "stress inversion" relies on earthquake focal mecha-<sup>63</sup> nisms to solve for the orientations of principal stress axes that are most consistent with <sup>64</sup> all of the focal mechanisms in a specified volume [*Gephart and Forsyth*, 1984; *Michael*,

DRAFT

<sup>65</sup> 1987; *Hardebeck and Hauksson*, 2001]. This method however is unable to determine the <sup>66</sup> magnitude of deviatoric stress.

In this paper I show that under certain conditions the magnitude of deviatoric stress 67 can be estimated using a distribution of fault orientations with respect to one of the 68 principle stress axes, or between sets of conjugate faults activated by a given ambient 69 stress. One location where the respective conditions appear to be met is a Ridgecrest 70 area in the northern part of the Eastern California Shear Zone that hosted a sequence of 71 strong earthquakes in 2019 [Ross et al., 2019; Hauksson and Jones, 2020; Jin and Fialko, 72 2020]. I use microseismicity data to identify active faults in the Ridgecrest area and 73 quantify their orientations, and use the latter to evaluate the magnitude of shear stress 74 acting in the seismogenic zone. 75

#### 2. Conjugate faults as stress meters

Laboratory experiments and geological observations indicate that failure of relatively 76 intact rocks is well described by the Mohr-Coulomb theory [Lockner et al., 1992; Walsh 77 and Watterson, 1988; Collectini and Sibson, 2001; Scholz, 2019]. The latter predicts that 78 the failure criterion is independent of the intermediate principal stress (i.e., is intrinsi-79 cally two-dimensional), and failure can equally likely occur on mutually antithetic sets of 80 planes that are parallel to the intermediate principal stress axis, and make an acute angle 81 with the maximum compressive stress axis. The antithetic failure planes are referred to 82 as conjugate faults [Anderson, 1951; Twiss and Moores, 1992, p. 173]. A dihedral angle 83 between the newly formed conjugate faults is a measure of internal friction, and can be 84 used to infer the state of stress at the time of failure [Barton, 1976; Angelier, 1994]. In 85 practice, available data rarely allow one to discriminate between slip on newly formed vs 86

DRAFT

pre-existing faults, and/or faults that experienced a finite rotation since their inception 87 [e.g., Nur et al., 1986; Fialko and Jin, 2021]. Seismic focal mechanisms that are widely 88 used to infer orientations of the principal stress axes in the seismogenic zone [Gephart 89 and Forsyth, 1984; Michael, 1987; Hardebeck and Hauksson, 2001] are not suitable for 90 studying the relationships between active conjugate faults because because of two fun-91 damental limitations. First, uncertainties in the fault plane solutions are typically too 92 large, especially for small to intermediate-size events [Hardebeck and Shearer, 2002; Yang 03 et al., 2012; Duputel et al., 2012, to be useful for evaluation of dihedral angles. Second, 94 an intrinsic ambiguity between the two nodal planes in a focal mechanism does not allow 95 one to isolate sets of synthetic vs antithetic faults, required to define a dihedral angle 96 between the respective fault planes. 97

These limitations can be mitigated by combining information provided by focal mecha-98 nisms with geometric constraints from the well-determined earthquake hypocenters. Pre-99 cisely relocated seismicity catalogs reveal ubiquitous lineated clusters of earthquakes that 100 illuminate faults or fault segments of various sizes and strikes (e.g., see Figure S1 in Sup-101 plementary Materials). Such clusters of earthquakes can be used to map the distribution 102 and attitude of active faults throughout the seismogenic layer. Fault strikes can be deter-103 mined with accuracy up to several degrees, an order of magnitude improvement over the 104 individual focal mechanism solutions. Also, fault orientations (well defined by seismicity 105 lineations) along with the polarity of focal mechanisms uniquely constrain the sense of 106 fault slip. I illustrate the method using data from the Ridgecrest area in Eastern California 107 Shear Zone (ECSZ) that hosted a sequence of strong earthquakes in 2019 (Figure 1). 108

DRAFT

March 3, 2021, 12:57pm

### 3. Data and methods

The ECSZ is an emergent plate boundary that accommodates an increasing fraction of 109 the relative motion between the Pacific and North American plates since its inception 6-10 110 Ma [Dokka and Travis, 1990; Nur et al., 1993; McClusky et al., 2001; Tymofyeyeva and 111 Fialko, 2015; Floyd et al., 2020]. As such, the ECSZ is a natural laboratory for studying the 112 development and evolution of new as well as re-activation of old fault systems. The ECSZ 113 is currently the most seismically active region in California, with 3 major earthquakes 114 occurring over the last 30 years [Sieh et al., 1993; Hauksson et al., 2002; DuRoss et al., 115 2020]. The most recent major event with magnitude 7.1 occurred in July 2019 near the 116 town of Ridgecrest in the northern part of the ECSZ (Figure 1), and involved rupture of 117 a system of right and left-lateral strike-slip faults [Ross et al., 2019; Hauksson and Jones, 118 2020; Jin and Fialko, 2020]. 119

The nearly perpendicular orientation of conjugate faults ruptured by the Ridgecrest 120 earthquakes (Figure 1b) is distinctly different from optimal orientations predicted by the 121 strong fault theory (dihedral angles of 50-60 degrees for the coefficient of friction of 0.6-0.8) 122 [Sibson, 1990; Scholz, 2019]. This prompted suggestions that in situ coefficient of friction 123 is close to zero [Ross et al., 2019]. Alternatively, high-angle conjugate faults could result 124 from rotation away from the optimal orientation since the initiation of the ECSZ [Fialko 125 and Jin, 2021]. As noted by Fialko and Jin [2021], a pattern of high-angle faulting similar 126 to that involved in the 2019 earthquake sequence is prevalent in a broader region around 127 the 2019 ruptures (Figure 1a). I start by quantifying the distribution of fault strikes and 128 relative orientations between conjugate faults expressed in microseismicity (Figure 1a). 129

DRAFT

X - 8

### 3.1. Analysis of fault orientations

To identify a population of active faults in the Ridgecrest area, I use a refined catalog 130 of earthquake focal mechanisms for southern California with earthquake locations derived 131 from waveform cross-correlation [Yang et al., 2012], updated to include data up to year 132 2020 (see Section "Data availability" in Supplementary Materials). The catalog data 133 for the area of interest include around  $3.2 \times 10^4$  focal mechanisms for earthquakes that 134 occurred between January 1981 and July 2019 (Figure 1a). The orientation of seismically 135 active faults is evaluated using the following procedure. Seismicity on sub-vertical strike-136 slip faults is manifested by lineated clusters of epicenters in the map view (Figure 1). I use 137 an unsupervised learning algorithm OPTICS (Ordering Points To Identify the Clustering 138 Structure) to select clusters of events that satisfy prescribed criteria of proximity and 139 density [Ankerst et al., 1999]. An event epicenter is selected as a core point of a cluster if 140 it has a number of geometrically defined neighbors equal to or greater than 10. The search 141 algorithm is executed iteratively, with an increasing distance that defines neighbors within 142 a cluster, from 0.5 to 1.5 km. At the end of each iteration selected clusters are removed 143 from the catalog and the search continues. Clusters chosen by the OPTICS algorithm 144 can have diverse geometries that are not necessarily linear. To select clusters that have 145 a quasi-linear shape, and estimate the best-fit linear trends, I use RANSAC (Random 146 Sample Consensus) [Schnabel et al., 2007] and robust linear regression algorithms. This 147 method is similar to that used by Skoumal et al. [2019] to analyze induced seismicity 148 in central Oklahoma, although the two approaches were developed independently. One 149 advantage of the clustering algorithm used in this study is that it allows for identification 150 of relatively small faults in the neighborhood of large clusters of earthquakes. In addition, 151

DRAFT

I interrogate a three-dimensional (3-D) distribution of earthquake hypocenters to identify 152 quasi-planar surfaces using a robust statistics algorithm for plane detection in unorganized 153 point clouds [Araújo and Oliveira, 2020]. To maximize the likelihood of feature detection 154 in three dimensions, I use the full waveform-relocated catalog [Hauksson et al., 2012] which 155 has  $\sim 3$  times more events than the focal mechanism catalog [Yang et al., 2012]. Planar 156 features that were not associated with a sufficient number of clustered hypocenters in 157 the focal mechanism catalog were excluded from the subsequent analysis. The 3-D plane 158 detection and the 2-D line clustering methods produced a number of spatially overlapping 159 features that likely represented the same fault structures. In such cases only one best-160 fitting fault segment was retained. 161

Examples of selected event clusters are shown in Figure 2. For each of the linear fits to the scattered epicenter locations (see red lines and black dots in Figure 2), I estimate errors in the best-fit strike angle by computing deviation of the least-square linear fits treating northing and easting coordinates as independent variables [*Fialko*, 2004]. The respective errors are shown as red numbers for each cluster (see Figure 2). On average the estimated uncertainties in fault strikes are on the order of several degrees.

#### 3.2. Analysis of slip direction

To determine the sense of slip on the identified fault segments, I use focal mechanisms of events in the respective clusters. For each event I compute components of the seismic moment tensor  $M_{ij}$  from the magnitude  $(M_w)$ , strike, dip, and rake angles provided in the focal mechanism catalog,  $M_{ij} = M_0(u_i n_j + u_j n_i)$ , where  $M_0 = 10^{1.5M_w+9.1}$  is the scalar seismic moment in newton meters,  $n_i$  is the normal to a slip plane (defined by the strike and dip angles), and  $u_i$  is the unit slip vector (defined by  $n_i$  and the rake angle).

DRAFT

I then compute a tensorial sum  $\Sigma_k M_{ij}$ , where k is the number of events in a cluster. To 174 investigate the effect of diversity of focal mechanisms (e.g., to avoid a possible dominance 175 of a largest event in a cluster), I also use moment tensors normalized by their scalar 176 moments,  $\bar{M}_{ij} = M_{ij}/\sqrt{M_{mn}M_{mn}/2}$  (repeated indices imply summation). I find that 177 using original and normalized moment tensors gives rise to essentially the same results. 178 The composite moment tensors may have an appreciable non-double-couple component 179 if focal mechanisms of events in a cluster are highly diverse. Yet orientations of the P 180 and T axes (that determine the average sense of slip on a plane defined by a seismicity 181 lineation) are well resolved. The focal mechanisms shown in Figure 2 represent the best-fit 182 double couple solutions for composite moment tensors  $\Sigma_k M_{ij}$ . For some event clusters, the 183 composite focal mechanisms revealed a nearly vertical plunge of the P axis, suggestive of 184 a predominantly dip-slip motion. The respective clusters were removed from the dataset. 185 Application of the algorithm described in this Section to the background (prior to July 186 2019) seismicity data (Figure 1a) resulted in selection of 70 quasi-linear clusters of micro-187 earthquakes. The respective clusters are shown in Figure 3, and individually in Figures 2 188 and S1-S2. The composite focal mechanisms of the identified clusters are predominantly 189 strike-slip, with approximately north-south P-axis, consistent with results of inversions for 190 the principle stress and strain rate axes [Yang and Hauksson, 2013; Hauksson and Jones, 191 2020; Fialko and Jin, 2021]. 192

#### 4. Distribution of dihedral angles

<sup>193</sup> Using information from both the fault strike (constrained by seismicity lineations) and <sup>194</sup> rake (constrained by the composite focal mechanisms) data, one can identify right- and <sup>195</sup> left-lateral faults in the total fault population without any assumptions about the sense

of shear stress resolved on the respective faults due to regional tectonic loading. The 196 observed distribution of orientations of active faults in the Ridgecrest area prior to the 197 2019 earthquake sequence is shown in Figure 4. The two sets of conjugate faults form 198 distinct clusters in a polar histogram (red and blue sectors in Figure 4). Left-lateral faults 199 are well aligned with those ruptured during the July 4 2019 M6.4 foreshock [Fialko and 200 Jin, 2021. Right-lateral faults trend somewhat more northerly compared to the main 201 rupture of the July 5 2019 mainshock, but similar to the initial rupture at the hypocenter 202 of the mainshock suggested by the first motion data [Jin and Fialko, 2020]. The axis of 203 the principal shortening rate [Fialko and Jin, 2021] approximately bisects the dihedral 204 angle formed by the conjugate fault planes (Figure 4). The principal compression axis is 205 oriented similar to the principal shortening rate axis ( $\sim 5$  degrees east of north) around 206 the hypocentral area of the M7.1 mainshock [Hauksson and Jones, 2020; Fialko and Jin, 207 2021]. 208

To quantify the range of admissible relative orientations of conjugate faults, I calculate 209 a dihedral angle between every pair of the identified conjugate faults. Figure 5 shows 210 a histogram of dihedral angles  $2\theta$ , where  $\theta$  is an angle between either fault plane and a 211 bisect. Uncertainties in the distribution of dihedral angles of conjugate faults (Figure 5) 212 are estimated using uncertainties in individual fault strikes. Suppose  $e_i$  is uncertainty in 213 the slope of a best linear fit for a cluster i, and m is a number of clusters in a given bin j214 of dihedral angles,  $a < 2\theta < b$ , where a and b are the minimum and maximum values of 215 samples in a given bin. The standard error of the mean of m angles is  $\epsilon_j = s/\sqrt{m}$ , where 216 s is the standard deviation of  $e_1, e_2, ..., e_m$  samples [Hogg et al., 2005]. 217

DRAFT

March 3, 2021, 12:57pm

Uncertainties on a number of conjugate pairs for a given bin of dihedral angles are 218 estimated assuming a normal distribution of measured values of  $2\theta_j$  with known mean 219 and standard deviation. A probability  $p_i(j)$  that a data point  $\theta_i$  belongs to bin j is:

$$p_i(j) = \int_a^b \frac{1}{\sqrt{2\pi}s_i} \exp\left[-\frac{(\theta_i - z)^2}{2s_i^2}\right] dz.$$
 (1)

The expected value of data points in a bin is given by a sum of the respective probabilities, 221

$$E_j = \Sigma_i p_i(j), \tag{2}$$

with the Bernoulli variance given by 222

$$V_j = \Sigma_i p_i(j)(1 - p_i(j)). \tag{3}$$

The standard deviation is the square root of variance [Hogg et al., 2005], 223

$$s_j = \sqrt{V_j}.\tag{4}$$

The ratio of the standard deviation to the expected value,  $\rho_j = s_j/E_j$ , is a proxy for 224 a relative error of the "unobserved count" of samples in each data bin. In Figure 5, 225 uncertainties in the number of dihedral angles per bin are estimated by multiplying the 226 actual bin counts by the respective values of  $\rho_j$  calculated using equations 1, 2, 3, and 4. 227 The distribution of dihedral angles shown in Figure 5 has a peak around 70 degrees, 228 and lower and upper bounds around 30 and 100 degrees, respectively. Assuming a ho-229 mogeneous background stress, some of the conjugate faults are optimally oriented for 230 failure given the laboratory values of the quasi-static coefficient of friction  $\mu \sim 0.6 - 0.8$ , 231 while others are not optimally oriented for any reasonable value of  $\mu$ . It follows that 232 the observed fault orientations require some heterogeneity in the effective fault strength, 233 ambient stress, or both. 234

DRAFT March 3, 2021, 12:57pm DRAFT

220

### 5. Role of stress heterogeneity

A locally homogeneous background stress is commonly assumed in inversions for the 235 principal stress orientations [Gephart and Forsyth, 1984; Michael, 1987]. There is no 236 physically justified length scale behind this assumption as rock volumes thought to satisfy 237 the assumption of stress homogeneity are chosen based on the density of seismic events 238 (number of events per unit volume) [e.g., Hardebeck and Hauksson, 2001]. In the presence 239 of multiple faults and fractures, the assumption of a homogeneous stress is likely violated 240 at small scales ranging from micro-asperities on a fault surface to the macroscopic fault 241 roughness, as predicted by numerical models [Mitchell et al., 2013; Dieterich and Smith, 242 2009] and observed in deep boreholes intersecting natural faults [e.g., Brudy et al., 1997]. 243 Stresses are also known to vary on spatial scales on the order of hundreds of kilometers, 244 as evidenced by regional inversions of the earthquake focal mechanisms [e.g., Yang and 245 Hauksson, 2013, presumably indicating transitions between different tectonic domains. 246 Other factors that may affect stress heterogeneity include e.g. 3-D variations in mechanical 247 properties of the host rocks [Fialko et al., 2002; Barbot et al., 2009]. 248

It is not obvious if the assumption of a constant background stress might be applicable 249 at spatial scales on the order of  $10^3 - 10^4$  m [*Iio et al.*, 2017; Alt and Zoback, 2017] 250 that are sampled by faults considered in this study (Figures 3, 2, and S1-S2). To check 251 whether results presented in Figures 4 and 5 could be attributed to stress heterogeneity, I 252 perform several tests. In particular, I examine the distribution of angles between synthetic 253 faults (i.e., faults that have the same sense of slip) as a function of distance between the 254 respective faults. If a relatively broad distribution of dihedral angles (Figure 5) results 255 from spatial variations in the orientation of the principal stress axes, strikes of closely 256

DRAFT

March 3, 2021, 12:57pm

spaced faults should be more similar to each other compared to strikes of more distant 257 faults having the same sense of slip. This would be expected e.g. if faults were optimally 258 oriented with respect to a local stress, but not necessarily to a regional stress. The 259 observed distribution of orientations of synthetic faults as a function of distance between 260 the faults is shown in the Supplementary Figure S3. The data indicate that (i) there is a 261 notable diversity in fault orientations at short (< 10 km) distances, (ii) there is little, if 262 any, systematic increase in the diversity of fault orientations with distance, and (iii) fault 263 orientations exhibit coherence at large (> 30 km) distances. 264

Previous studies suggested a local rotation of the principal stress axes around the Coso 265 region (northings N > 40 km in a local coordinate system used in Figure 3) [Hauksson 266 and Jones, 2020]. To investigate the respective possibility, I divided the data into the 267 northern (N > 40 km) and southern (N < 40 km) sub-sets, and repeated the analysis for 268 each sub-set. Figures S4-S5 show variability in fault strikes vs distance between pairs of 269 synthetic faults, and Figures S6-S7 show the distribution of fault strikes. The northern 270 sub-set shows some correlation between the diversity of fault strikes and distance between 271 synthetic faults, suggesting a possible effect of stress heterogeneity (Figure S4). In part 272 such heterogeneity could be attributed to a long-term fluid pumping at the Coso geother-273 mal plant [Fialko and Simons, 2000; Tymofyeyeva and Fialko, 2015]. Also, conjugate 274 faults in the northern sub-set exhibit smaller dihedral angles that are closer to optimal 275 orientations compared to faults in the southern sub-set (cf. Figures S6 and S7). However, 276 the mean of the left- and right-lateral fault strikes (i.e., the bisect) is not resolvably differ-277 ent between the northern and southern sub-sets, suggesting that a constant regional stress 278 is a viable first-order approximation. The spatial resolution of stress inversions depends 279

DRAFT

<sup>280</sup> on the distribution of seismicity; in areas with enough data (including the epicentral area <sup>281</sup> of the 2019 Ridgecrest earthquakes) the observed variations in the orientation of the prin-<sup>282</sup> cipal stress axes are smaller than 10-20 degrees [*Fialko and Jin*, 2021, see their figure 2], <sup>283</sup> insufficient to explain the observed distribution of dihedral angles (Figure 5) in terms of <sup>284</sup> regional variations in the stress field.

Given that the background tectonic loading is relatively uniform [*Floyd et al.*, 2020; *Fialko and Jin*, 2021], most of the local stress heterogeneity in the upper crust is likely associated with brittle failure. To quantify effects of stress heterogeneity due to a complex network of randomly oriented faults, I performed numerical simulations in which I varied the fault distribution, the ambient stress, and the effective fault strength.

# 5.1. Rotation of the principal stress axes due to a complex system of interacting faults

Slip on faults ultimately reduces stress imposed by tectonic loading, but also results in a 290 re-distribution of stress within the brittle crust, with largest stress perturbations typically 291 concentrated around the fault edges [e.g., Martel and Pollard, 1989]. To quantify the 292 effects of stress heterogeneity (specifically, the amount of rotation of the principle stress 293 axes) due to a complex fault system, I simulate a network of randomly oriented two-294 dimensional (plane strain) faults subject to a prescribed remotely applied stress (Figure 6). 295 Each fault is approximated by a linear array of dislocations. The boundary condition on 296 each dislocation is  $\tau \leq \mu \sigma'_n$ , where  $\tau$  and  $\sigma'_n$  are respectively the shear and the effective 297 normal stress (normal stress minus the pore fluid pressure) resolved on a dislocation plane. 298 and  $\mu$  is the local coefficient of friction. Both  $\tau$  and  $\sigma'_n$  are total stresses that result from 299 the remotely applied stress as well as slip on faults in response to the remotely applied 300

DRAFT

stress. The boundary condition ensures that each fault locally does not violate the Mohr-301 Coulomb failure criterion. Numerical simulations are performed using a boundary element 302 code TwoDD modified to handle non-linear stress-controlled boundary conditions [Crouch 303 and Starfield, 1983; Fialko and Rubin, 1997]. Fault lengths randomly vary in the interval 304 1-11 km, chosen to approximate the observed distribution of active faults in the Ridgecrest 305 area (Figures 1a and 3). Figure 6 shows an example of a modeled fault distribution. The 306 remotely applied stress has eigenvectors  $\sigma_{E,N}$  aligned with the coordinate axes, "east" (E) 307 and "north" (N), such that  $\sigma_E$ =-40 MPa, and  $\sigma_N$ =-160 MPa, similar to the background 308 stress inferred from the observed fault orientations in Ridgecrest (see Discussion section). 309 The maximum compressive stress  $\sigma_N$  is somewhat increased compared to an equilibrium 310 principal stress at which the optimally oriented faults are on the verge of failure, to allow 311 for finite slip on the modeled faults. 312

Two sets of simulations were performed for each random realization of the fault system, 313 one assuming a constant coefficient of friction ( $\mu = 0.6$ , Figure 6a,c), and another assuming 314 a variable coefficient of friction  $(0.3 < \mu < 0.6, \text{ Figure 6b,d})$ . The top panels in Figure 315 6 show the slip magnitude and the bottom panels show the orientation of the principal 316 compression axis (tick marks) and its rotation due to slip on faults (color). The modeled 317 faults essentially approximate shear cracks with a constant stress drop. In case of spatially 318 constant friction, only the faults that happened to be nearly optimally oriented for failure 319 become activated by the applied remote stress field, as expected (Figure 6a). In case of 320 variable friction, a more diverse population of faults is brought to failure (Figure 6b). 321 For the same remote stress, reductions in  $\mu$  give rise to larger static stress drops and slip 322 magnitudes on pre-existing faults. Faults with a constant stress drop produce a weak stress 323

DRAFT

singularity at the fault tips [e.g., Pollard and Segall, 1987; Fialko, 2015]. Despite such a 324 singularity, only limited rotation of the principal stress axis is observed in the surrounding 325 medium. In case of constant friction, the stress rotation is essentially negligible (Figure 326 6c). In case of heterogeneous friction, the stress rotation on average does not exceed 327  $\sim 10$  degrees, and is limited to relatively small areas around the fault tips (Figure 6d). 328 Increases in the magnitude of the remotely applied deviatoric and mean stresses result in 329 stress rotations that are smaller still, as the ratio of stress perturbations due to fault slip 330 to the absolute background stress decreases. 331

Results presented above suggest that the observed distribution of orientations of active faults in the Ridgecrest area (Figures 1a, 3, and 5) is unlikely explained in terms of spatial heterogeneity of stresses acting in the seismogenic zone.

#### 6. Role of strength heterogeneity

It may be argued that small earthquakes that comprise quasi-linear clusters (Figures 1a, 335 2, 3, and S1-S2) are primarily governed by the rate and state friction [Dieterich, 2015] and 336 are not subject to strong dynamic weakening, so that the peak yield stress is comparable 337 to the background stress [Fialko, 2015]. In this case, one can interpret the observed range 338 of fault orientations (Figure 5) in terms of activation ( $\theta > \theta_1$ ) and de-activation ( $\theta > \theta_2$ ) of 339 pre-existing or newly created faults. It is generally recognized that the continental Earth's 340 crust is pervasively faulted and contains cracks, fractures and other structural defects that 341 can serve as potential slip surfaces over a broad range of sizes and orientations [Sykes, 342 1978; Sibson, 1990]. 343

DRAFT

### 6.1. Slip on immature sub-optimally oriented faults: Theory

Given a stress field with axes of the effective principal stresses  $\sigma'_1$  and  $\sigma'_3$  parallel to the Earth's surface, a condition for activation of pre-existing strike-slip faults is [*Sibson*, 1985, 1990]:

$$R = \frac{\sigma_1'}{\sigma_3'} = \frac{1 + \mu \cot \theta}{1 - \mu \tan \theta},\tag{5}$$

<sup>347</sup> where *R* is the effective stress ratio,  $\sigma'_1$  is the effective maximum compressive stress (max-<sup>348</sup> imum compressive stress minus the pore pressure *P*),  $\sigma'_3$  is the effective minimum com-<sup>349</sup> pressive stress,  $\mu$  is the coefficient of friction, and  $\theta$  is the angle between a fault plane <sup>350</sup> and the maximum compression axis. Equation 5 assumes the Mohr-Coulomb failure cri-<sup>351</sup> terion, vertical orientation of the intermediate principal stress, and negligible (compared <sup>352</sup> to friction) cohesion on a potential slip plane.

Equation 5 is typically under-determined as the number of unknowns (e.g.,  $\sigma'_1$ ,  $\sigma'_3$  and 353  $\mu$ ) is greater than the number of observables (such as angles between conjugate faults or 354 between faults and the principal stress axes). In case of the Ridgecrest seismicity, several 355 unique conditions may allow one to resolve this uncertainty. First, a transfersional stress 356 regime manifested by a mix of strike-slip and normal focal mechanisms [Hauksson and 357 Jones, 2020, including spatially overlapping strike-slip and normal earthquake ruptures 358 [Jin and Fialko, 2020] indicates that the maximum compressive  $(\sigma'_1)$  and intermediate 359  $(\sigma'_2)$  principle stresses are essentially of the same magnitude. In this case, both should 360 approximately equal the effective lithostatic stress,  $\rho_c g z - P$ , where  $\rho_c$  is the average 361 density of the upper crust, g is the gravitational acceleration, and z is depth. Second, 362 assuming that the lower and upper bounds of the observed distribution of dihedral angles 363 (Figure 5) correspond to activation  $(\theta_1)$  and de-activation  $(\theta_2)$  of pre-existing faults, one 364

DRAFT

X - 19

can estimate a possible range of variations in the coefficient of friction on activated faults,  $\mu_1 < \mu < \mu_0$ . The lower bound on  $\mu$  is given by

$$\mu_1 = \frac{1}{\tan(\theta_1 + \theta_2)}.\tag{6}$$

The minimum failure envelope  $\tau = \mu_1 \sigma'_n$ , where  $\sigma'_n$  and  $\tau$  are respectively the effective normal and shear stresses resolved on a fault, intersects the Mohr circle [*Twiss and Moores*, 1992, p. 141] at points corresponding to fault orientations  $2\theta_1$  and  $2\theta_2$ . A fault orientation that maximizes an excursion beyond the minimum failure envelope is given by an average of the activation and de-activation angles  $\theta_1$  and  $\theta_2$ . Substituting equation 6 into equation 5, and taking  $\theta$  to be equal to either  $\theta_1$  or  $\theta_2$ , one obtains expressions for the critical stress ratio  $R^*$  and the effective minimum compressive stress  $\sigma'_3$ :

$$R^* = \frac{1 + \mu_1 \cot \theta_1}{1 - \mu_1 \tan \theta_1} = \frac{1 + \mu_1 \cot \theta_2}{1 - \mu_1 \tan \theta_2},\tag{7}$$

374

(

$$\sigma_3' = \sigma_1'/R^*. \tag{8}$$

The coefficient of friction  $\mu_1$  provides a lower bound on the frictional strength of activated sub-optimally oriented faults. Faults that are oriented at more acute angles with respect to the principal compression axis can be on the verge of failure if they have a higher coefficient of friction, with an upper bound  $\mu_0$  that corresponds to an optimal fault orientation. The upper bound on  $\mu$  can be found from the following relationship between the stress ratio R and the coefficient of friction that corresponds to an optimal orientation [Sibson, 1985]:

$$R = \left(\sqrt{1 + \mu_0^2} + \mu_0\right)^2.$$
(9)

Solving for real non-negative values of  $\mu_0$  gives rise to

$$\mu_0 = \frac{R - 1}{2\sqrt{R^*}}.$$
(10)

DRAFT March 3, 2021, 12:57pm DRAFT

Figure 7 shows a Mohr circle diagram for the state of stress that satisfies the above 382 constraints as well as the assumption of a hydrostatic pore pressure [Townend and Zoback, 383 2000]  $(P = \rho_w gz)$ , where  $\rho_w$  is the density of water), at a reference depth of 7 km. The latter 384 is within the estimated range of the hypocentral depth of the M7.1 Ridgecrest earthquake 385 (3-8 km) [Hauksson and Jones, 2020]. It also approximately corresponds to the middle of 386 the seismogenic layer, so that the absolute stresses shown in Figure 7 represent stresses 387 averaged over the thickness of the seismogenic layer. As one can see from Figure 7, the 388 estimated stress ratio is  $R^* \approx 3$ , the depth-averaged shear stresses resolved on seismically 389 active faults are 25-40 MPa, and the inferred range of in situ coefficient of friction is 390  $0.4 < \mu < 0.6.$ 391

### 7. Discussion

High-end values of the estimated coefficient of friction are in agreement with labora-392 tory measurements of quasi-static friction of most rock types [Byerlee, 1978], and may 393 correspond to the formation of new faults or activation of pre-existing suitably oriented 394 faults in the ECSZ (Figure 7). The value of  $\mu \sim 0.6$  is also consistent with models sug-395 gesting that faults ruptured in the 2019 sequence were initiated at or near to an optimal 396 orientation of  $\sim 30^{\circ}$  with respect to the principal compression axis at the inception of 397 the ECSZ, and subsequently rotated to their current (sub-optimal) orientations [Fialko 398 and Jin, 2021]. The model of Fialko and Jin [2021] implies that the newly formed or 399 activated faults progressively weakened as they continued to accumulate slip and rotate 400 away from their optimal orientation due to the long-term tectonic motion. Hauksson and 401 Jones [2020] proposed that the orientation of the 2019 earthquake ruptures with respect 402 to the present-day principal compression axis might be explained assuming higher values 403

DRAFT

March 3, 2021, 12:57pm

of the stress ratio (R > 5) and the coefficient of friction  $(\mu = 0.75)$ . Such high values 404 however appear to be inconsistent with the observed transfermional stress regime in the 405 Ridgecrest-Coso area, and would require pore fluid pressures close to the least compressive 406 stress. Also, a high coefficient of friction would imply a peak in dihedral angles of the 407 regional fault population around the respective optimal value (~ 55 degrees for  $\mu = 0.75$ ) 408 which is not observed (Figure 5). Note that orientations of the 2019 ruptures (Figures 1b) 409 and 4) are within the documented range of a regional data set (Figure 5), so that results 410 presented in this study apply to the observed geometry of the 2019 earthquakes. 411

The inferred value of  $\mu_0$  (Figure 7) is also in agreement with observations of injection-412 induced seismicity in the central US that reveal ubiquitous dihedral angles of  $\sim 60^{\circ}$ 413 [Schoenball and Ellsworth, 2017; Alt and Zoback, 2017; Skoumal et al., 2019]. Such obser-414 vations are consistent with the idea that stable continental interiors can support stresses 415 on the order of hundreds of megapascals predicted by the strong fault theory. A relatively 416 broad distribution of dihedral angles in the Ridge crest area with a peak around  $\sim 70-75^\circ$ 417 (Figure 5) is however markedly different from a highly clustered distribution observed in 418 the central US [Schoenball and Ellsworth, 2017; Skoumal et al., 2019], suggesting differ-419 ences in the stress regime and the effective strength of the bulk of the seismogenic crust. 420 In part such differences could be attributed to different tectonic settings and loading con-421 ditions. Specifically, seismicity in the central US exemplifies a stable continental interior 422 responding to the anthropogenically induced increases in pore fluid pressure [e.g., Wein-423 garten et al., 2015]. In contrast, seismicity in the Ridgecrest area (Figure 1) is associated 424 with a nascent plate boundary responding to increases in tectonic strain [Nur et al., 1993; 425 Fialko and Jin, 2021]. The "developing plate boundary" environment is arguably more 426

DRAFT

March 3, 2021, 12:57pm

relevant for investigating the evolution of fault strength as a function of fault maturity,
and may provide useful insights into a poorly understood transition from "strong" to
"weak" faults.

The low-end values of the estimated range of the coefficient of friction ( $\mu_1$ , see equa-430 tion 6 and Figures 5 and 7) provide some quantitative measure of the degree of weakening 431 associated with fault evolution as a function of tectonic strain. The average shear strain  $\varepsilon$ 432 accommodated by the ECSZ since its inception 6-10 Ma is on the order of 10-20% [Fialko 433 and Jin, 2021]. In a continuum representation of brittle failure such as "seismic flow" 434 of rocks [*Riznichenko*, 1965], one can define an average rate of tectonic strain softening, 435  $\partial \mu / \partial \varepsilon$ . Taking  $\partial \mu \approx \mu_0 - \mu_1$ ,  $\partial \mu / \partial \varepsilon$  is estimated to be on the order of unity. A moderate 436 reduction in the coefficient of friction suggested by the analysis of fault orientations (Fig-437 ures 4, 5 and 7) may be indicative of an onset of various weakening mechanisms with an 438 increasing cumulative fault slip, such as mineral alteration, ultra-comminution, pressur-439 ization of fault zone fluids, etc. [e.g., Imber et al., 1997; Reches and Lockner, 2010; Lacroix 440 et al., 2015]. Largest faults in the system might also experience dynamic weakening [Jin441 and Fialko, 2020]. 442

<sup>443</sup> Note that some variability in the coefficient of friction that could contribute to the <sup>444</sup> observed diversity of fault orientations (Figures 3 and 5) is naturally expected due to <sup>445</sup> dependence of friction on composition, normal stress, temperature, and other environ-<sup>446</sup> mental variables [*Stesky et al.*, 1974; *Byerlee*, 1978; *Mitchell et al.*, 2013, 2015, 2016]. A <sup>447</sup> key distinction with the "cumulative slip-weakening" model is that the latter predicts a <sup>448</sup> systematic dependence of the effective fault strength on fault maturity. In particular, <sup>449</sup> faults in the ECSZ that are currently less optimally oriented for slip were likely acti-

DRAFT

vated before faults that are currently well oriented with respect to the present-day stress field. While it may be difficult to determine the fault age or a cumulative offset, especially for small faults that are only expressed in micro-seismicity and don't yet have a surface expression (Figure 1a), we note that faults that produced the 2019 sequence are on the "long/less well-oriented" end of the distribution of active faults in the study area (Figures 1b and 5), consistent with a notion that for developing faults, the fault length correlates with the fault age [e.g., *Cowie and Scholz*, 1992].

Estimates of deviatoric stress based on the Mohr-Coulomb theory are upper bounds in 457 that they define the maximum shear stress the upper crust can support before new faults 458 are formed. In the presence of mature well-slipped faults, the average shear stress resolved 459 on the respective faults can be well below the static Mohr-Coulomb failure envelope due to 460 the effects of dynamic rupture [e.g., Noda et al., 2009; Thomas et al., 2014; Fialko, 2015]. 461 The long-term reduction in strength depends on the magnitude of stress concentration 462 ahead of the rupture front, and dynamic weakening behind the rupture front during 463 individual seismic events [Kirkpatrick and Shipton, 2009; Di Toro et al., 2011; Rubino 464 et al., 2017]. Both factors are expected to scale with the rupture size. Over geologic time, 465 mature faults localize tectonic strain and may not be oriented with respect to the principal 466 stress axes in any predictable fashion, other that the sense of shear stress resolved on a 467 fault should be the same as the sense of fault slip. 468

The method proposed in this study relies on relative orientations of small developing immature faults distributed throughout the seismogenic layer, so that the effects of stress concentration and dynamic weakening, if any, should be minimal. It should be mentioned that dihedral angles between conjugate faults are uniquely related to the coefficient of

DRAFT

friction only in case of newly formed faults; a re-activation of pre-existing faults depends 473 on other factors that affect the effective fault strength, such as e.g. the pore fluid pressure. 474 The lower bound on the coefficient of friction  $\mu_1$  (Figures 5 and 7) should therefore be 475 considered an effective residual friction that accounts for all relevant weakening mecha-476 nisms. Estimation of the magnitude of deviatoric stress further requires special conditions 477 such as a 2-D state of stress (equal magnitudes of two of the principal stress components). 478 The above conditions appear to be met in the area around Ridgecrest (Figures 1 and 3), 479 allowing a unique estimate of the magnitude of absolute stresses in the seismogenic crust. 480 The depth-averaged shear stress S is on the order of a few tens of megapascals (see 481 Figure 7). This is well below the values of shear stress measured in deep boreholes 482 and suggested by seismic observations in the stable continental crust [e.g., Brudy et al., 483 1997; Townend and Zoback, 2000; Schoenball and Ellsworth, 2017], but similar to values 484 suggested for the San Andreas Fault (SAF) based on the borehole measurements [Lockner] 485 et al., 2011] and independent constraints such as the heat flow data [Lachenbruch and Sass, 486 1980] and stress perturbations due to topography [Fialko et al., 2005]. Despite similar 487 values of the driving shear stress, active faults in the Ridgecrest area may be considered 488 to be relatively strong compared to the SAF because of the transfermional stress regime in 489 the ECSZ versus transpressional regime on the SAF. The magnitude of deviatoric stress 490 in the study area thus falls in between predictions of the strong and weak fault theories. 491

### 8. Conclusions

<sup>492</sup> Precisely determined relative locations of small and intermediate size earthquakes often
 <sup>493</sup> reveal lineated structures likely illuminating active faults at depth. Quasi-linear clusters
 <sup>494</sup> of earthquakes can be used to constrain fault orientations (e.g., strike and dip angles),

DRAFT

which, in combination with information provided by the composite focal mechanisms, 495 may allow one to quantify relative orientations of active conjugate faults. Dihedral an-496 gles formed by the conjugate fault planes carry information about the heterogeneity in 497 the ambient stress field and the fault strength, as well as the orientation and (under 498 certain conditions) the magnitude of the principal stresses. I demonstrate the proposed 499 method using data from the Eastern California Shear Zone near the town of Ridgecrest 500 that hosted a series of strong earthquakes in July of 2019. The data analysis indicates 501 that the attitudes of small- to medium-sized faults (that sample in situ stresses on spatial 502 wavelengths on the order of kilometers) are essentially the same as those of the M6-M7 503 earthquakes of the 2019 Ridgecrest sequence that ruptured the entire seismogenic layer 504 (thereby sampling stresses on spatial wavelengths on the order of tens of kilometers). I 505 use statistics of dihedral angles between active faults expressed in the background (prior 506 to July 2019) seismicity to estimate the effective fault strength and the absolute shear 507 stress acting at seismogenic depths. The inferred range of the coefficient of friction is 508  $0.4 < \mu < 0.6$ , and the depth-average shear stress is 25-40 MPa. A possible interpreta-509 tion of the observed distribution of dihedral angles is that the new faults are formed (or 510 existing faults are activated) at optimal angles with respect to the maximum compression 511 axis, and are progressively weakened as they continue to accumulate slip and rotate away 512 from the optimal orientation due to a long-term tectonic motion. Results presented in 513 this study suggest that a transition from "strong" to "weak" faults may initiate at the 514 early stages of formation of a plate boundary, and involve relatively low total offsets. The 515 proposed method can be used to assess the magnitude of deviatoric stress acting at seis-516 mogenic depths in other actively deforming areas expressed in abundant microseismicity. 517

DRAFT

March 3, 2021, 12:57pm

<sup>518</sup> but lacking well-developed mature faults. Quasi-linear clusters of earthquakes and their <sup>519</sup> composite focal mechanisms can also be used to improve robustness of inversions for the <sup>520</sup> orientation of the principal stress axes.

Acknowledgments. I thank reviewers... This study was supported by NSF (grant EAR-1841273) and NASA (grant 80NSSC18K0466). Figures were produced using Generic Mapping Tools (GMT) [Wessel et al., 2013] and Matlab.

#### **Data Availability Statement**

The data that support the findings of this study are openly available in the Southern California Earthquake Data Center (SCEDC) repository (doi: 10.7909/C3WD3xH1) at https://scedc.caltech.edu/data/alt-2011-yang-hauksson-shearer.html and https://scedc.caltech.edu/data/alt-2011-dd-hauksson-yang-shearer.html. Data are available through Yang et al. [2012] and Hauksson et al. [2012].

### References

- <sup>529</sup> Allmann, B. P., and P. M. Shearer (2009), Global variations of stress drop for moderate
   <sup>530</sup> to large earthquakes, J. Geophys. Res., 114, B01,310.
- <sup>531</sup> Alt, R. C., and M. D. Zoback (2017), In situ stress and active faulting in Oklahoma, Bull.
  <sup>532</sup> Seism. Soc. Am., 107(1), 216–228.
- <sup>533</sup> Anderson, E. M. (1951), *The dynamics of faulting*, 206 pp., Oliver and Boyd, Edinburgh.
- Angelier, J. (1994), Fault slip analysis and palaeostress reconstruction, in *Continental deformation*, pp. 53–100.
- <sup>536</sup> Ankerst, M., M. M. Breunig, H.-P. Kriegel, and J. Sander (1999), OPTICS: ordering <sup>537</sup> points to identify the clustering structure, *ACM Sigmod record*, 28(2), 49–60.

DRAFT March 3, 2021, 12:57pm DRAFT

- Araújo, A. M., and M. M. Oliveira (2020), A robust statistics approach for plane detection in unorganized point clouds, *Pattern Recognition*, 100, 107–115.
- Barbot, S., Y. Fialko, and D. Sandwell (2009), Three-dimensional models of elasto-static 540 deformation in heterogeneous media, with applications to the Eastern California Shear 541
- Zone, Geophys. J. Int., 179, 500–520. 542

538

539

549

- Barton, N. (1976), The shear strength of rock and rock joints, International Journal of 543 rock mechanics and mining sciences & Geomechanics abstracts, 13, 255–279. 544
- Brown, K. M., and Y. Fialko (2012), "Melt welt" mechanism of extreme weakening of 545 gabbro at seismic slip rates, Nature, 488, 638–641. 546
- Brudy, M., M. Zoback, K. Fuchs, F. Rummel, and J. Baumgartner (1997), Estimation of 547 the complete stress tensor to 8 km depth in the KTB scientific drill holes: Implications 548 for crustal strength, J. Geophys. Res., 102, 18,435–18,475.
- Byerlee, J. (1978), Friction of rock, *Pure Appl. Geophys.*, 116, 615–626. 550
- Chester, J. S., F. M. Chester, and A. K. Kronenberg (2005), Fracture surface energy of 551 the Punchbowl fault, San Andreas system, Nature, 437, 133–136. 552
- Choy, G. L., and J. L. Boatwright (1995), Global patterns of radiated seismic energy and 553 apparent stress, J. Geophys. Res., 100, 18,205–18,228. 554
- Collettini, C., and R. H. Sibson (2001), Normal faults, normal friction?, Geology, 29, 555 927 - 930.556
- Cowie, P. A., and C. H. Scholz (1992), Growth of faults by accumulation of seismic slip, 557 J. Geophys. Res., 97, 11,085–11,095. 558
- Crouch, S. L., and A. M. Starfield (1983), Boundary element methods in solid mechanics, 559 322 pp pp., George Allen and Unwin, Boston. 560

DRAFT

568

- Di Toro, G., R. Han, T. Hirose, N. De Paola, S. Nielsen, K. Mizoguchi, F. Ferri, M. Cocco, 561
- and T. Shimamoto (2011), Fault lubrication during earthquakes, Nature, 471(7339), 562 494 - 498.563
- Dieterich, J. (2015), Applications of Rate- and State-Dependent Friction to Models of 564
- Fault Slip and Earthquake Occurrence, in Treatise on Geophysics, 2nd. Ed., Vol. 4, 565
- edited by G. Schubert, pp. 93–110, Elsevier Ltd., Oxford. 566
- Dieterich, J. H. (1981), Mechanical behavior of crustal rocks, in Mechanical behavior of 567 crustal rocks: the Handin volume, Geophysical Monograph, vol. 24, edited by N. L.
- Carter, M. Friedman, J. M. Logan, and D. W. Stearns, pp. 103–120, American Geo-569 physical Union, Washington, DC. 570
- Dieterich, J. H., and D. E. Smith (2009), Nonplanar faults: Mechanics of slip and off-fault 571 damage, in Mechanics, structure and evolution of fault zones, pp. 1799–1815, Springer. 572
- Dokka, R. K., and C. J. Travis (1990), Role of the Eastern California shear zone in 573 accommodating Pacific-North American plate motion, Geophys. Res. Lett., 17, 1323-574 1327. 575
- Duputel, Z., L. Rivera, Y. Fukahata, and H. Kanamori (2012), Uncertainty estimations 576 for seismic source inversions, Geophys. J. Int., 190, 1243–1256. 577
- DuRoss, C. B., R. D. Gold, T. E. Dawson, K. M. Scharer, K. J. Kendrick, S. O. Akciz, 578 S. J. Angster, J. Bachhuber, S. Bacon, S. E. Bennett, et al. (2020), Surface displacement 579 distributions for the July 2019 Ridgecrest, California, earthquake ruptures, Bull. Seism. 580
- Soc. Am., 110, 1400–1418. 581
- Fialko, Y. (2004), Evidence of fluid-filled upper crust from observations of post-seismic 582 deformation due to the 1992  $M_w$  7.3 Landers earthquake, J. Geophys. Res., 109, B08,401, 583

DRAFT

X - 28

- <sup>584</sup> 10.1029/2004JB002,985.
- <sup>565</sup> Fialko, Y. (2015), Fracture and Frictional Mechanics Theory, in *Treatise on Geophysics*,
- 2nd. Ed., Vol. 4, edited by G. Schubert, pp. 73–91, Elsevier Ltd., Oxford.
- Fialko, Y., and Z. Jin (2021), Simple shear origin of the cross-faults ruptured in the 2019 Ridgecrest earthquake sequence, *Nature Geoscience*, *in revision*.
- Fialko, Y., and Y. Khazan (2005), Fusion by earthquake fault friction: Stick or slip?, J.
   *Geophys. Res.*, 110, B12,407, doi:10.1029/2005JB003,869.
- <sup>591</sup> Fialko, Y., and M. Simons (2000), Deformation and seismicity in the Coso geothermal
   <sup>592</sup> area, Inyo County, California: Observations and modeling using satellite radar interfer <sup>593</sup> ometry, J. Geophys. Res., 105, 21,781–21,793.
- <sup>594</sup> Fialko, Y., D. Sandwell, D. Agnew, M. Simons, P. Shearer, and B. Minster (2002), De<sup>595</sup> formation on nearby faults induced by the 1999 Hector Mine earthquake, *Science*, 297,
  <sup>596</sup> 1858–1862.
- <sup>597</sup> Fialko, Y., L. Rivera, and H. Kanamori (2005), Estimate of differential stress in the upper
  <sup>598</sup> crust from variations in topography and strike along the San Andreas fault, *Geophys.*<sup>599</sup> J. Int., 160, 527–532.
- Fialko, Y. A., and A. M. Rubin (1997), Numerical simulation of high pressure rock tensile
   fracture experiments: Evidence of an increase in fracture energy with pressure?, J.
   *Geophys. Res.*, 102, 5231–5242.
- Floyd, M., G. Funning, Y. A. Fialko, R. L. Terry, and T. Herring (2020), Survey and
   Continuous GNSS in the vicinity of the July 2019 Ridgecrest earthquakes, *Seismol. Res. Lett.*, *91*, 2047–2054.

DRAFT

X - 30

- <sup>606</sup> Gephart, J. W., and D. W. Forsyth (1984), An improved method for determining the
- regional stress tensor using earthquake focal mechanism data: Application to the San
- <sup>608</sup> Fernando earthquake sequence, J. Geophys. Res., 89, 9305–9320.
- Goldsby, D., and T. Tullis (2011), Flash heating leads to low frictional strength of crustal
   rocks at earthquake slip rates, *Science*, *334*, 216–218.
- <sup>611</sup> Han, R., T. Shimamoto, T. Hirose, J.-H. Ree, and J. Ando (2007), Ultralow friction of <sup>612</sup> carbonate faults caused by thermal decomposition, *Science*, *316*, 878–881.
- <sup>613</sup> Hardebeck, J. L., and E. Hauksson (2001), Crustal stress field in southern California and <sup>614</sup> its implications for fault mechanics, *J. Geophys. Res.*, *106*, 21,859–21,882.
- Hardebeck, J. L., and P. M. Shearer (2002), A new method for determining first-motion
  focal mechanisms, *Bull. Seism. Soc. Am.*, *92*, 2264–2276.
- Hauksson, E., and L. Jones (2020), Seismicity, stress state, and style of faulting of the
  Ridgecrest-Coso region from the 1930s through 2019: Seismotectonics of an evolving plate boundary segment, *Bull. Seism. Soc. Am.*, 110, 1457–1473, doi:10.1785/
  0120200051.
- Hauksson, E., L. Jones, and K. Hutton (2002), The 1999  $M_w$  7.1 Hector Mine, California, earthquake sequence: Complex conjugate strike-slip faulting, *Bull. Seism. Soc. Am.*, *92*, 1154–1170.
- <sup>624</sup> Hauksson, E., W. Yang, and P. M. Shearer (2012), Waveform relocated earthquake catalog
- for Southern California (1981 to 2011), Bull. Seism. Soc. Am., 102(5), 2239–2244, doi:
   10.1785/0120120010.
- <sup>627</sup> Hogg, R. V., J. McKean, and A. T. Craig (2005), *Introduction to mathematical statistics*,
  <sup>628</sup> 6th edition, Pearson Education.

- Iio, Y., I. Yoneda, M. Sawada, T. Miura, H. Katao, Y. Takada, K. Omura, and S. Horiuchi 629 (2017), Which is heterogeneous, stress or strength? An estimation from high-density 630 seismic observations, Earth, Planets and Space, 69(1), 1–16.
- Imber, J., R. Holdsworth, C. Butler, and G. Lloyd (1997), Fault-zone weakening processes 632
- along the reactivated Outer Hebrides Fault Zone, Scotland, Journal of the Geological 633 Society, 154, 105–109. 634
- Jennings, C., and W. Bryant (2010), Fault Activity Map of California, California Division 635 of Mines and Geology, Geologic Data Map No. 6. 636
- Jin, Z., and Y. Fialko (2020), Finite slip models of the 2019 Ridgecrest earthquake se-637 quence constrained by space geodetic data and aftershock locations, Bull. Seism. Soc. 638 Am., 110, 1660–1679, doi:10.1785/0120200060. 639
- Kirkpatrick, J., and Z. Shipton (2009), Geologic evidence for multiple slip weakening 640 mechanisms during seismic slip in crystalline rock, J. Geophys. Res., 114, B12,401. 641
- Lachenbruch, A. H., and J. H. Sass (1980), Heat flow and energetics of the San Andreas 642 fault zone, J. Geophys. Res., 85, 6185–6222. 643
- Lacroix, B., T. Tesei, E. Oliot, A. Lahfid, and C. Collettini (2015), Early weakening 644 processes inside thrust fault, *Tectonics*, 34, 1396–1411. 645
- Lockner, D. A., J. Byerlee, V. Kuksenko, A. Ponomarev, and A. Sidorin (1992), Ob-646 servations of quasistatic fault growth from acoustic emissions, in Fault mechanics and 647
- transport properties of rocks, edited by B. Evans and T. Wong, pp. 3-31, Academic, 648
- San Diego, CA, USA. 649

631

Lockner, D. A., C. Morrow, D. Moore, and S. Hickman (2011), Low strength of deep San 650 Andreas fault gouge from SAFOD core, *Nature*, 472(7341), 82–85. 651

DRAFT

March 3, 2021, 12:57pm

X - 32

- <sup>652</sup> Marone, C. (1998), Laboratory-derived friction laws and their application to seismic fault-<sup>653</sup> ing, Annu. Rev. Earth Planet. Sci., 26, 643–696.
- <sup>654</sup> Martel, S. J., and D. D. Pollard (1989), Mechanics of slip and fracture along small faults <sup>655</sup> and simple strike-slip fault zones in granitic rock, *J. Geophys. Res.*, *94*, 9417–9428.
- McClusky, S., S. Bjornstad, B. Hager, R. King, B. Meade, M. Miller, F. Monastero, and
   B. Souter (2001), Present day kinematics of the Eastern California Shear Zone from a
   geodetically constrained block model, *Geophys. Res. Lett.*, 28, 3369–3372.
- <sup>659</sup> Michael, A. J. (1987), Use of focal mechanisms to determine stress: a control study, J. <sup>660</sup> Geophys. Res., 92, 357–368.
- Mitchell, E., Y. Fialko, and K. M. Brown (2013), Temperature dependence of frictional
   healing of Westerly granite: experimental observations and numerical simulations, *Geo- chemistry, Geophysics, Geosystems, 14*, 567–582.
- Mitchell, E., Y. Fialko, and K. Brown (2015), Frictional properties of gabbro at condi tions corresponding to slow slip events in subduction zones, *Geochemistry, Geophysics*,
   *Geosystems*, 16(11), 4006–4020.
- <sup>667</sup> Mitchell, E., Y. Fialko, and K. M. Brown (2016), Velocity-weakening behavior of Westerly <sup>668</sup> granite at temperature up to 600° C, *J. Geophys. Res.*, *121*, 6932–6946.
- Mount, V., and J. Suppe (1987), State of stress near the San Andreas fault: Implications
   for wrench tectonics, *Geology*, 15, 1143–1146.
- Noda, H., E. Dunham, and J. R. Rice (2009), Earthquake ruptures with thermal weakening
  and the operation of major faults at low overall stress levels, *J. Geophys. Res.*, 114,
  B07,302.

DRAFT

March 3, 2021, 12:57pm

- <sup>674</sup> Nur, A., H. Ron, and O. Scotti (1986), Fault mechanics and the kinematics of block <sup>675</sup> rotations, *Geology*, 14, 746–749.
- <sup>676</sup> Nur, A., H. Ron, and G. Beroza (1993), The nature of the Landers-Mojave earthquake <sup>677</sup> line, *Science*, *261*, 201–203.
- Plumb, R. A., and S. H. Hickman (1985), Stress-induced borehole elongation: A comparison between the four-arm dipmeter and the borehole televiewer in the Auburn
  geothermal well, J. Geophys. Res., 90, 5513–5521.
- Pollard, D. D., and P. Segall (1987), Theoretical displacements and stresses near fractures in rock: With applications to faults, joints, veins, dikes, and solution surfaces, in
- Fracture Mechanics of Rock, edited by B. K. Atkinson, chap. 8, pp. 277–350, Academic
   Press, London.
- Reches, Z., and D. A. Lockner (2010), Fault weakening and earthquake instability by powder lubrication, *Nature*, 467(452-U102 DOI: 10.1038/nature09348).
- Rice, J. R. (1992), Fault stress states, pore pressure distribution, and the weakness of
   the San Andreas Fault, in *Fault mechanics and transport properties of rocks*, edited by
- B. Evans and T. Wong, pp. 475–503, Academic, San Diego, CA, USA.
- Rice, J. R. (2006), Heating and weakening of faults during earthquake slip, J. Geophys.
   *Res.*, 111, B05,311.
- <sup>692</sup> Riznichenko, Y. V. (1965), The flow of rocks as related to seismicity, *Dokl. Akad. Nauk* <sup>693</sup> SSSR, 161(1), 96–98.
- Ross, Z. E., B. Idini, Z. Jia, O. L. Stephenson, M. Zhong, X. Wang, Z. Zhan, M. Simons,
- E. J. Fielding, S.-H. Yun, et al. (2019), Hierarchical interlocked orthogonal faulting in the 2019 Ridgecrest earthquake sequence, *Science*, *366* (6463), 346–351.

DRAFT

X - 34

- <sup>697</sup> Rubino, V., A. Rosakis, and N. Lapusta (2017), Understanding dynamic friction through <sup>698</sup> spontaneously evolving laboratory earthquakes, *Nature communications*, 8(1), 1–13.
- Schnabel, R., R. Wahl, and R. Klein (2007), Efficient RANSAC for point-cloud shape
- detection, in *Computer graphics forum*, vol. 26, pp. 214–226, Wiley Online Library.
- <sup>701</sup> Schoenball, M., and W. L. Ellsworth (2017), A systematic assessment of the spatiotempo <sup>702</sup> ral evolution of fault activation through induced seismicity in Oklahoma and southern
- <sup>703</sup> Kansas, J. Geophys. Res., 122(12), 10–189.
- <sup>704</sup> Scholz, C. H. (2000), Evidence for a strong San Andreas fault, *Geology*, 28(2), 163–166.
- <sup>705</sup> Scholz, C. H. (2019), *The mechanics of earthquakes and faulting*, 3rd Ed., 493 pp., Cam-
- <sup>706</sup> bidge Univ. Press, New York, NY.
- <sup>707</sup> Sibson, R. H. (1985), A note on fault reactivation, J. Struct. Geol., 7(6), 751–754.
- Sibson, R. H. (1990), Rupture nucleation on unfavorably oriented faults, Bull. Seism. Soc.
   Am., 80, 1580–1604.
- <sup>710</sup> Sibson, R. H. (2004), Controls on maximum fluid overpressure defining conditions for <sup>711</sup> mesozonal mineralisation, J. Struct. Geol., 26(6-7), 1127–1136.
- <sup>712</sup> Sieh, K., L. Jones, E. Hauksson, K. Hudnut, D. Eberhart-Phillips, T. Heaton, S. Hough,
- K. Hutton, H. Kanamori, A. Lilje, et al. (1993), Near-field investigations of the Landers
  earthquake sequence, *Science*, *260*, 171–176.
- <sup>715</sup> Skoumal, R. J., J. O. Kaven, and J. I. Walter (2019), Characterizing seismogenic fault
- structures in Oklahoma using a relocated template-matched catalog, Seismol. Res. Lett., 90(4), 1535-1543.
- Sobolev, S. V., and A. Y. Babeyko (2005), What drives orogeny in the Andes?, *Geology*, 33(8), 617–620.

#### DRAFT

- Stern, R. J., and T. Gerya (2018), Subduction initiation in nature and models: A review, 720 Tectonophysics, 746, 173–198. 721
- Stesky, R., W. Brace, D. Riley, and P.-Y. Robin (1974), Friction in faulted rock at high 722 temperature and pressure, *Tectonophysics*, 23, 177–203. 723
- Sykes, L. R. (1978), Intraplate seismicity, reactivation of preexisting zones of weakness, al-724
- kaline magmatism, and other tectonism postdating continental fragmentation, *Reviews* 725 of Geophysics, 16(4), 621-688. 726
- Thomas, M. Y., N. Lapusta, H. Noda, and J.-P. Avouac (2014), Quasi-dynamic versus 727 fully dynamic simulations of earthquakes and aseismic slip with and without enhanced 728 coseismic weakening, J. Geophys. Res., 119, 1986–2004. 729
- Toth, J., and M. Gurnis (1998), Dynamics of subduction initiation at pre-existing fault 730 zones, J. Geophys. Res., 103, 18,053-18,067. 731
- Townend, J., and M. Zoback (2000), How faulting keeps the crust strong, *Geology*, 28, 732 399-402. 733
- Twiss, R., and E. Moores (1992), Structural Geology, W.H. Freeman, New York, NY. 734
- Tymofyeyeva, E., and Y. Fialko (2015), Mitigation of atmospheric phase delays in InSAR 735 data, with application to the Eastern California Shear Zone, J. Geophys. Res., 120, 736 5952-5963. 737
- Walsh, J., and J. Watterson (1988), Dips of normal faults in British Coal Measures and 738 other sedimentary sequences, Journal of the Geological Society, 145(5), 859–873. 739
- Wang, K., and Y. Fialko (2018), Observations and modeling of co- and postseismic defor-740 mation due to the 2015  $M_w$  7.8 Gorkha (Nepal) earthquake, J. Geophys. Res., 123(1), 741 761-779.

DRAFT

742

March 3, 2021, 12:57pm

- <sup>743</sup> Weingarten, M., S. Ge, J. W. Godt, B. A. Bekins, and J. L. Rubinstein (2015), High-rate
  <sup>744</sup> injection is associated with the increase in US mid-continent seismicity, *Science*, *348*,
  <sup>745</sup> 1336–1340.
- Wernicke, B. (1995), Low-angle normal faults and seismicity: A review, J. Geophys. Res.,
   100, 20,159–20,174.
- Wessel, P., W. H. F. Smith, R. Scharroo, J. Luis, and F. Wobbe (2013), Generic Mapping
   Tools: Improved Version Released, *Eos, Trans. AGU*, *94*(45), 409–410, doi:10.1002/
   2013EO450001.
- <sup>751</sup> Yang, W., and E. Hauksson (2013), The tectonic crustal stress field and style of faulting
- <sup>752</sup> along the Pacific North America Plate boundary in Southern California, *Geophys. J.*<sup>753</sup> Int., 194, 100–117.
- Yang, W., E. Hauksson, and P. M. Shearer (2012), Computing a large refined catalog of
  focal mechanisms for southern California (1981–2010): Temporal stability of the style
  of faulting, *Bull. Seism. Soc. Am.*, 102, 1179–1194.
- Zoback, M., R. Apel, J. Baumgartner, M. Brudy, R. Emmermann, B. Engeser, K. Fuchs,
  W. Kessels, H. Rischmuller, F. Rummel, and L. Vernik (1993), Upper-crustal strength
  inferred from stress measurements to 6 km depth in the KTB borehole, *Nature*, 365,
  633–635.

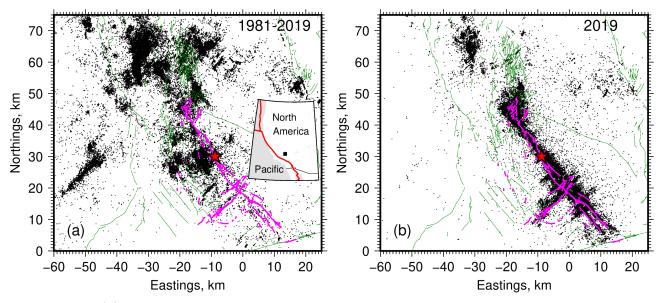
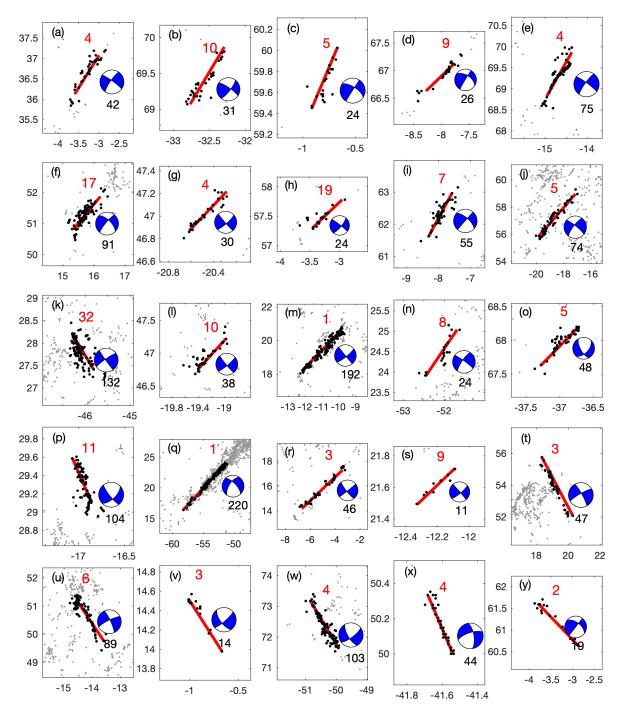


Figure 1. (a) Precisely relocated seismicity in the Ridgecrest-Coso area over a time period 1981-July 2019 [Hauksson et al., 2012]. Thin green lines denote Quaternary faults [Jennings and Bryant, 2010]. Magenta lines denote surface traces of the 2019 ruptures [DuRoss et al., 2020]. Red star denotes the epicenter of the 2019 M7.1 earthquake. Inset shows the location of the study area. (b) Precisely relocated seismicity over 6 months following the July 2019 M7.1 event [Ross et al., 2019]. Local origin is at 117.5°W, 35.5°N.

DRAFT

March 3, 2021, 12:57pm



**Figure 2.** Seismicity lineations identified by the clustering algorithm. Grey dots denote the background seismicity, black dots denote events included in a cluster. The local UTM coordinate system is the same as in Figure 1. Red lines denote the best linear fits. White and blue "beach balls" denote the composite focal mechanisms for the respective clusters. Black numerical labels below the beach balls indicate the number of events in a cluster. Red numerical labels above the beach balls indicate uncertainty in the estimated strike angle, in degrees. D R A F T D R A F T D R A F T D R A F T

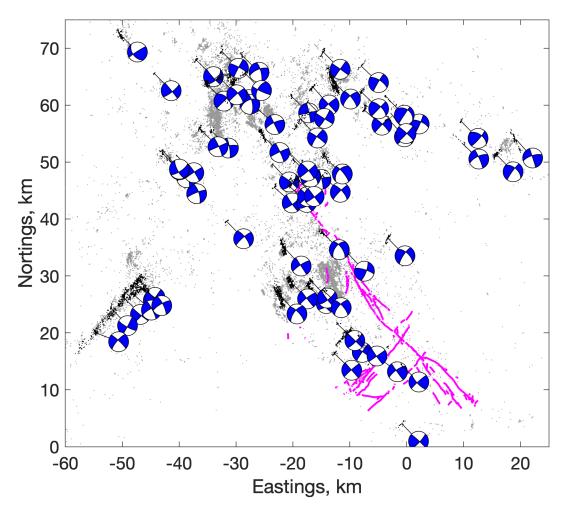
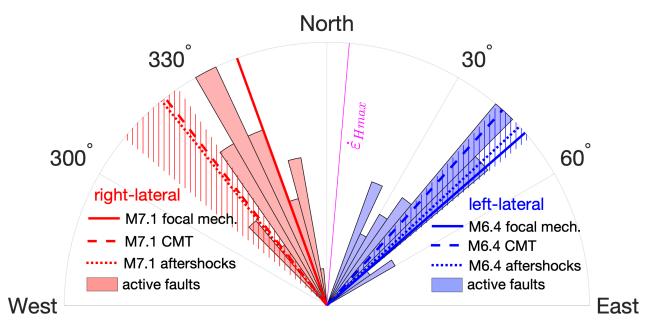


Figure 3. Map of the Ridgecrest-Coso area. Magenta wavy lines denote surface traces of the 2019 ruptures mapped by field surveys [*DuRoss et al.*, 2020]. Grey dots denote pre-earthquake (1981-2019) seismicity from the focal mechanism catalog [*Yang et al.*, 2012]. Black dots denote seismicity lineations selected by the clustering algorithm (see Supplementary Materials and Figures S2-S4 for details). White and blue "beach balls" denote the best-fitting double-couple composite focal mechanism for the respective linear clusters of earthquakes. Coordinates the same as in Figure 1.



**Figure 4.** A distribution of strikes of 70 active fault segments shown in Figure 3. Red histogram corresponds to right-lateral faults (total of 30 samples, maximum number of samples per bin: 7), and blue histogram corresponds to left-lateral faults (total of 40 samples, maximum number of samples per bin: 10). Hatched areas denote orientation of faults ruptured by the M6.4 foreshock and M7.1 mainshock of the 2019 sequence [*Jin and Fialko*, 2020; *Fialko and Jin*, 2021]. Thin magenta line denotes the principal shortening rate axis derived from geodetic data [*Fialko and Jin*, 2021].

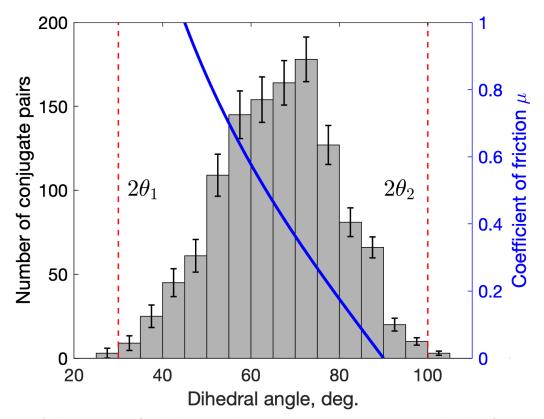


Figure 5. A histogram of dihedral angles between the conjugate strike-slip faults identified in Figure 3. Red vertical lines denote the lower  $(2\theta_1)$  and upper  $(2\theta_2)$  bounds on the observed distribution. Blue line (right axis) denotes the coefficient of friction corresponding to conjugate faults that are optimally oriented for failure according to the Mohr-Coulomb criterion,  $\mu = 1/\tan(2\theta)[Sibson, 1990]$ .

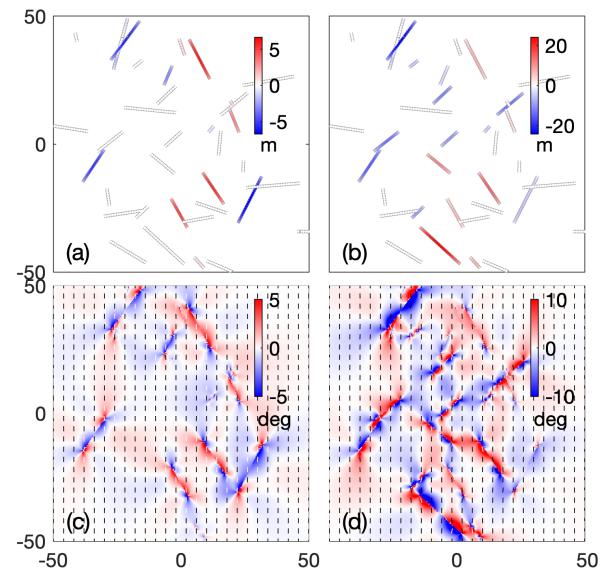


Figure 6. Numerical simulations of a system of randomly oriented faults activated by the applied remote stress field. (a,c) Geometry of the fault network. Color denotes the slip magnitude. Right-lateral slip is positive and left-lateral slip is negative. (b,d) Orientation of the maximum compression axis (tickmarks) and rotation caused by fault slip (color). Counterclockwise rotation is deemed positive. (a,c) Constant coefficient of friction,  $\mu = 0.6$ . (b,d) Variable coefficient of friction,  $0.3 < \mu < 0.6$ . Calculations assume the Young's modulus of 50 GPa, and the Poisson ratio of 0.25. Coordinate axes are in km.

DRAFT

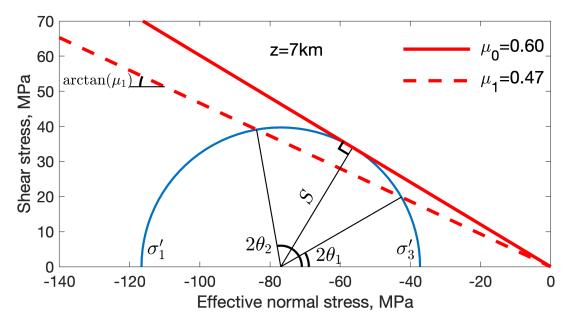


Figure 7. The estimated state of stress in the hypocentral region of the 2019 Ridgecrest earthquakes. Blue curve (the Mohr circle) denotes variations in shear stress on potential slip planes as a function of a dihedral angle  $2\theta$  between conjugate slip planes (or angle  $\theta$  between a slip plane and the maximum compression axis). Radius of the Mohr circle represents the maximum shear stress,  $S = |\sigma'_1 - \sigma'_3|/2$ . Red lines are the Mohr-Coulomb failure envelopes corresponding to activation of pre-existing faults ( $\mu_1$ , dashed line), and generation of new faults ( $\mu_0$ , solid line). Calculations assume  $\rho_c = 2.7 \times 10^3 \text{ kg/m}^3$ ,  $\rho_w = 10^3 \text{ kg/m}^3$ , and  $g = 9.8 \text{ m/s}^2$ .

DRAFT

March 3, 2021, 12:57pm