

# Tropical free-tropospheric humidity differences and their effect on the clear-sky radiation budget in global storm-resolving models

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## Abstract

Reducing the model spread in free-tropospheric relative humidity (RH) and its response to warming is a crucial step towards reducing the uncertainty in clear-sky climate sensitivity, a step that is hoped to be taken with recently developed global storm-resolving models (GSRMs). In this study we quantify the inter-model differences in tropical present-day RH across GSRMs, making use of DYAMOND, a first 40-day intercomparison. We find that the inter-model spread in tropical mean free-tropospheric RH is reduced compared to conventional atmospheric models, except from the the tropopause region and the transition to the boundary layer. We estimate the reduction to approximately 50-70% in the upper troposphere and 25-50% in the mid troposphere. However, the remaining RH differences still result in a spread of 1.2 Wm<sup>-2</sup> in tropical mean clear-sky outgoing longwave radiation (OLR). This spread is mainly caused by RH differences in the lower and mid free troposphere, whereas RH differences in the upper troposphere have a minor impact. By examining model differences in moisture space we identify two regimes with a particularly large contribution to the spread in tropical mean clear-sky OLR: rather moist regimes at the transition from deep convective to subsidence regimes and very dry subsidence regimes. Particularly for these regimes a better understanding of the processes controlling the RH biases is needed.

1           **Tropical free-tropospheric humidity differences and**  
2           **their effect on the clear-sky radiation budget in global**  
3           **storm-resolving models**

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11           **Key Points:**

- 12           • A 40-day comparison of storm-resolving models indicates that free-tropospheric  
13           relative humidity differs less than among conventional models
- 14           • The remaining relative humidity differences still cause a non-negligible (approx-  
15           imately  $1.2 \text{ Wm}^{-2}$ ) spread in tropical mean clear-sky OLR
- 16           • Reducing humidity biases is most beneficial in the lower and mid free troposphere  
17           of dry subsidence regimes and near deep convective regimes

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**Abstract**

Reducing the model spread in free-tropospheric relative humidity (RH) and its response to warming is a crucial step towards reducing the uncertainty in clear-sky climate sensitivity, a step that is hoped to be taken with recently developed global storm-resolving models (GSRMs). In this study we quantify the inter-model differences in tropical present-day RH across GSRMs, making use of DYAMOND, a first 40-day intercomparison. We find that the inter-model spread in tropical mean free-tropospheric RH is reduced compared to conventional atmospheric models, except from the the tropopause region and the transition to the boundary layer. We estimate the reduction to approximately 50-70% in the upper troposphere and 25-50% in the mid troposphere. However, the remaining RH differences still result in a spread of  $1.2 \text{ Wm}^{-2}$  in tropical mean clear-sky outgoing longwave radiation (OLR). This spread is mainly caused by RH differences in the lower and mid free troposphere, whereas RH differences in the upper troposphere have a minor impact. By examining model differences in moisture space we identify two regimes with a particularly large contribution to the spread in tropical mean clear-sky OLR: rather moist regimes at the transition from deep convective to subsidence regimes and very dry subsidence regimes. Particularly for these regimes a better understanding of the processes controlling the RH biases is needed.

**Plain Language Summary**

Errors in the humidity and its change with global warming simulated by climate models limit our ability to predict how the climate system responds to an increase in greenhouse gas concentrations. In this study we investigate how large these humidity errors are in recently developed high-resolution models. We focus on the relative humidity, which measures the amount of moisture in the air compared to what air can hold at a given temperature. We find that the disagreement in the tropics is reduced compared to conventional climate models, but the relative humidity errors still have a considerable effect on the radiation budget. We also investigate in which regions of the tropics a further reduction of errors would be most beneficial. In the vertical, it is the altitude region between about 1 km and 10 km. In the horizontal, we find two tropical regimes that are particularly important: Dry regimes with very strong subsidence and moister regimes at the edge of deep convective regimes. Particularly for those regimes a better understanding of the processes that cause the model errors is needed.

**1 Introduction**

Free-tropospheric water vapor strongly impacts the Earth's outgoing longwave radiation (OLR) and therefore plays a key role in controlling the clear-sky response of the climate system to an increase in greenhouse gases. It is now widely accepted that this response is described by a warming and moistening of the atmosphere that is implied if the relative humidity (RH) and lapse rate were to depend on temperature alone, which corresponds to a warming at approximately constant RH (e.g. Held & Soden, 2000; Romps, 2014; Po-Chedley et al., 2019). This reduces the radiative response compared to a warming at constant absolute humidity, and can be described as a positive water-vapor-lapse-rate feedback. While general circulation models (GCMs) agree on this basic response (e.g. Soden & Held, 2006; Bony et al., 2006), there is still an appreciable inter-model spread in the magnitude of the water-vapor-lapse-rate feedback. This spread, which primarily originates from the tropics, contributes a non-negligible (about 30%) uncertainty to the climate sensitivity (Vial et al., 2013).

The RH is an important detail. Even small deviations from its assumed constancy with warming have a strong impact on the radiative response. RH changes alter the radiative compensation between water-vapor and lapse-rate feedback in the saturated re-

68 regions of the emission spectrum (Bony et al., 2006) and differences in the RH response  
 69 control the spread in tropical water-vapor–lapse-rate feedback across GCMs (Vial et al.,  
 70 2013; Po-Chedley et al., 2018). Even if RH does not change with warming, the RH pro-  
 71 file in the present climate may influence the feedback. While a correlation between global  
 72 mean present-day humidity and water vapor feedback has not been found for GCMs (John  
 73 & Soden, 2007), Bourdin et al. (2021) have argued that especially at warmer, tropical  
 74 temperatures the rapid closing of the atmospheric window by water vapor continuum  
 75 absorption makes the feedback dependent on the RH profile. There are other reasons to  
 76 care about present-day free-tropospheric RH (e.g. Derbyshire et al., 2004; Luo & Rossow,  
 77 2004; Stevens et al., 2017), but independent of whether these (or the proposed direct ef-  
 78 fect of present-day RH on the feedback) end up being important, confidence in an abil-  
 79 ity of models to correctly represent the present-day RH is essential for building trust in  
 80 model-based estimates of the subtle changes in RH under warming that influence the wa-  
 81 ter vapor feedback.

82  
 83 Sherwood et al. (2010) found that certain aspects of the tropical RH distribution  
 84 show signs of convergence in GCMs once horizontal resolutions fall below about 100km.  
 85 It is also known from previous studies that free-tropospheric RH is primarily controlled  
 86 by the circulation on scales resolved by typical GCMs, and parameterized processes like  
 87 convection only matter by influencing the circulation (e.g. Sherwood, 1996; Pierrehum-  
 88 bert & Roca, 1998; Dessler & Sherwood, 2000). On the one hand, the convergence of RH  
 89 in GCMs with different convective parameterizations might indicate that convective pro-  
 90 cesses play a minor role in affecting the circulation. On the other hand, for simulations  
 91 on an aquaplanet Retsch et al. (2019) found that allowing convection to be resolved ex-  
 92 plicitly has a larger impact on free-tropospheric RH than increasing resolution in sim-  
 93 ulations with parameterized convection. This suggests that the circulation changes more  
 94 significantly once convection is resolved explicitly and calls into question whether the RH  
 95 in GCMs converges for physical reasons.

96  
 97 A milestone in climate modelling has been made with the emergence of global storm-  
 98 resolving models (GSRMs; Satoh et al., 2019), also called global cloud-resolving or convection-  
 99 permitting models. While the development of the first GSRM already goes back more  
 100 than 15 years (Tomita et al., 2005), only recently the increase in computational capac-  
 101 ities has allowed several modelling groups to follow, enabling first intercomparisons. GSRMs  
 102 solve the non-hydrostatic equations on global grids with kilometre-scale resolution. At  
 103 such resolutions the models begin to resolve precipitating convective systems and there-  
 104 fore forgo the need to parameterize deep convection, which is hoped to eradicate some  
 105 long-standing biases (e.g. Miura et al., 2007; Stevens et al., 2020). Whether the spread  
 106 in free-tropospheric RH is reduced in GSRMs is, however, not obvious. This depends on  
 107 how strongly the behavior of convection depends on model formulation. If this depen-  
 108 dence is weak, RH differences should be small among GSRMs. However, there are also  
 109 reasons to expect the opposite. Bourdin et al. (2021) found that RH differences across  
 110 cloud-resolving models in radiative-convective equilibrium (RCE) are substantially larger  
 111 than across GCMs. The large spread in RCE models is likely related to different degrees  
 112 of convective organization (Becker & Wing, 2020). Although these differences are expected  
 113 to be smaller in simulations with more realistic setups, in which large-scale circulations  
 114 impose constraints on convective organization (Wing et al., 2020), they likely still play  
 115 a role. Therefore, it cannot be ruled out that the RH spread across GSRMs is similar  
 116 or even larger than across GCMs.

117  
 118 In this study we quantify differences in tropical free-tropospheric RH across GSRMs  
 119 for the first time, making use of the model intercomparison DYNAMICS of the Atmospheric  
 120 general circulation Modeled On Nonhydrostatic Domains (DYAMOND Stevens et al.,

121 2019). To assess how relevant the RH differences are from a radiative point of view, we  
 122 translate them into differences in clear-sky outgoing longwave radiation (OLR) using a  
 123 radiative transfer scheme. The latter is also used to compute radiative kernels, which  
 124 allow us to identify those regions in the tropical atmosphere, in which a future reduction  
 125 of RH differences would be most effective in reducing differences in clear-sky OLR.  
 126

127 We perform the comparison of the DYAMOND models in moisture space, i.e. we  
 128 sort the atmospheric state from dry to moist. On the one hand, humidity fields in mois-  
 129 ture space are highly aggregated, which ensures robust statistics. On the other hand, the  
 130 moisture space representation allows us to distinguish between different dynamic regimes  
 131 of the tropics, which is useful for identifying regions of large inter-model spread as well  
 132 as for the OLR calculations. The representation of the atmosphere in moisture space is  
 133 inspired by Bretherton et al. (2005), who used it to study the energy balance of convec-  
 134 tive self-aggregation in radiative-convective equilibrium simulations. Later, the depic-  
 135 tion in moisture space has also proven useful for analysing observational data (Schulz  
 136 & Stevens, 2018) and to bypass the issue of co-location when comparing observations  
 137 and model simulations (Naumann & Kiemle, 2020).  
 138

139 This paper is organized as follows: In Section 2 we introduce the DYAMOND sim-  
 140 ulations and describe our post-processing of the model output. In Section 3 we quan-  
 141 tify inter-model RH differences in the tropical mean and in moisture space. The impact  
 142 of the RH differences on the clear-sky radiation budget is examined in Section 4.  
 143

## 144 2 DYAMOND simulations

### 145 2.1 Models and experimental protocol

146 DYAMOND is the first intercomparison project for GSRMs, comparing 40-day sim-  
 147 ulations of nine models (only acronyms are given here): ICON, NICAM, ARPEGE-NH,  
 148 FV3, GEOS, MPAS, UM, SAM and IFS. In the following we provide a brief overview  
 149 of the models and the experimental protocol of DYAMOND. A more detailed descrip-  
 150 tion is given by Stevens et al. (2019).  
 151

152 Most of the DYAMOND models solve the fully compressible non-hydrostatic Navier-  
 153 Stokes equations. Two exceptions are SAM, which uses the anelastic form of the non-  
 154 hydrostatic equations, and IFS, which solves the primitive equations and is hence a hy-  
 155 drostatic model. The models solve their governing equations on a variety of different nu-  
 156 merical grids. The horizontal grid spacing is between 2.5 km and 5 km in eight of the nine  
 157 models. The only exception is UM, which uses a latitude-longitude grid with a some-  
 158 what coarser resolution at low latitudes (7.8 km at the equator). The number of verti-  
 159 cal levels and the vertical extent of the model grid also vary among the models. The mod-  
 160 els were not specifically calibrated for the DYAMOND simulations. Some models even  
 161 ran for the first time in this configuration and at storm-resolving resolutions.  
 162

163 The models also differ in the parameterizations used to represent unresolved pro-  
 164 cesses. In particular, there are different approaches to handle convection, reflecting some  
 165 disagreement about which motions are adequately resolved at kilometre-resolution. While  
 166 in some models convection is not parameterized at all, in others shallow convection is  
 167 parameterized. GEOS and MPAS even employ scale-aware parameterizations for deep  
 168 convection. There is also diversity in the parameterizations for boundary layer turbu-  
 169 lence and microphysics.  
 170

171 The DYAMOND simulations were run for 40 days from 1 August to 10 September  
 172 2016. They were initialized with common atmospheric fields from the ECMWF global  
 173 (9 km) meteorological analysis. Daily sea surface temperatures (SSTs) and sea ice con-  
 174 centrations from the ECMWF analysis were used as boundary conditions. The initial-  
 175 ization of the land surface was left to the practices of the individual modelling groups.  
 176 After the initialization each simulation was allowed to evolve freely without further forc-  
 177 ing.

## 178 2.2 Post-processing and profile selection

179 We use the 3-hourly output of atmospheric pressure  $p$ , temperature  $T$ , specific hu-  
 180 midity  $q$  as well as vertical velocity  $W$ . Following Stevens et al. (2019) we exclude the  
 181 first ten days of the simulations and only use the last 30 days to minimize the effects of  
 182 biases from differences in the model spin-up as well as constraints from the common ini-  
 183 tialization.  
 184

185 The size of the model output represents a challenge for the analysis. 30 days of one  
 186 3-hourly 3D field (corresponding to 240 timesteps) on the native model grid covering the  
 187 tropics have a size on the order of 2 TB. For nine models and four variables this adds  
 188 up to more than 60 TB. Developing strategies for dealing effectively with the massive amounts  
 189 of data produced by GSRMs is one of the purposes of DYAMOND. Our approach is the  
 190 following: In a first step all fields are horizontally interpolated from each model's native  
 191 grid to a common regular latitude-longitude grid covering the tropics (30° S to 30° N)  
 192 with a resolution of 0.1°. This is done using a conservative remapping via the remap func-  
 193 tion of the Climate Data Operators (CDO) version 1.9.5 (Schulzweida, 2019). The remap-  
 194 ping reduces the data volume by about a factor of ten without noticeable loss of infor-  
 195 mation in the region of interest. In a second step we perform a subsampling of grid points.  
 196 From each of the 240 output timesteps about 42,000 oceanic profiles are selected ran-  
 197 domly, resulting in a total of 10 million selected profiles for each model. This reduces  
 198 the amount of data by another factor of 100. We estimated the sampling uncertainty by  
 199 repeating the random sampling several times for the same model. For tropical mean RH,  
 200 the quantity we focus on, the sampling uncertainty is about 0.01% RH and hence two  
 201 magnitudes smaller than inter-model differences, which are on the order of 1% RH (Sec-  
 202 tion 3.1). In the same manner we estimated the sampling uncertainty for each block in  
 203 moisture space (Section 3.2) to be at least one order of magnitude smaller than the inter-  
 204 model spread in the respective block. Hence, the random subsampling of profiles intro-  
 205 duces only a small error, but reduces the data volume to 0.1% of its original size. This  
 206 result shows that although GSRMs work with tremendous data volumes, most of the in-  
 207 formation is necessary for predicting their dynamic evolution, and for many analyses there  
 208 exists considerable opportunities to compress their output with relatively little loss of  
 209 information.  
 210

211 We exclude land areas to avoid complications from topography and more strongly  
 212 varying boundary layer depths and hence to simplify the interpretation. The inhomog-  
 213 eneity of land regions would also colour our analysis in moisture space. Vertically in-  
 214 tegrated water vapor (IWV), which is used to span moisture space (Section 3.2), is strongly  
 215 influenced by local surface characteristics over land. It can be very low in regions with  
 216 little soil moisture or in regions with high elevation. Consequently, if moisture space was  
 217 spanned from both oceanic and continental grid points, profiles associated with very dif-  
 218 ferent regimes would be mixed in the same IWV blocks. Therefore, we focus on the more  
 219 homogeneous ocean regions.  
 220

221 The fifth generation of the ECMWF atmospheric reanalysis (ERA5; Hersbach et  
 222 al., 2020) serves as an observationally constrained reference data set in our comparison.  
 223 It should be pointed out that potential biases with respect to observations exist in the  
 224 ERA5 water vapor fields. Xue et al. (2020) found a wet bias with respect to satellite ob-  
 225 servations in the free troposphere, which is most pronounced in regions of large-scale sub-  
 226 sidence. Nevertheless, the dataset provides a valuable constraint of the humidity distri-  
 227 bution and can be used to estimate its natural variability. Gridded atmospheric variables  
 228 are provided at a spatial resolution of 31 km. We use 3-hourly output corresponding to  
 229 the output times of the DYAMOND models and post-process it in the same way as the  
 230 model output.  
 231

### 232 3 RH differences in DYAMOND models

233 In this section we quantify the differences in free-tropospheric RH in the DYAMOND  
 234 models, first in the tropical mean and subsequently in moisture space.

#### 235 3.1 Tropical mean

236 Since the focus of this study is on the radiative impact of humidity differences we  
 237 concentrate on relative humidity (RH) rather than absolute humidity (measured by  $q$ ).  
 238 The atmospheric temperature and water vapor concentration are decisive parameters for  
 239 clear-sky radiative transfer. The RH is a valuable proxy that links their competing ef-  
 240 fects on longwave emission. This will be discussed in more detail in the second part of  
 241 this paper. Another reason to look at RH is that it is RH rather than  $q$  that is effectively  
 242 constrained by model processes (in particular, condensation and evaporation). There-  
 243 fore, any model errors in temperature are expected to alter  $q$  but not necessarily RH.  
 244

245 RH is calculated for each of the randomly selected profiles and their associated val-  
 246 ues of  $q$ ,  $p$  and  $T$  as  $\text{RH} = \frac{e}{e_s(T)}$ , where  $e$  is the water vapor pressure and  $e_s(T)$  is its  
 247 saturation value at temperature  $T$ . For  $e_s(T)$  we take the value over water for  $T$  above  
 248 the triple point  $T_t$  and the value over ice for  $T$  below  $T_t - 23$  K. For intermediate  $T$  a  
 249 a combination of both is used following the IFS documentation (ECMWF, 2018). It should  
 250 be noted here that the RH computed in this way can deviate from the RH calculated  
 251 internally in the microphysics schemes of the models because they use different meth-  
 252 ods to compute RH above the freezing level. The deviations are relevant when the re-  
 253 lation between RH and clouds or precipitation is investigated. However, as explained above  
 254 our focus is on the radiative impact of the humidity differences. We regard RH primar-  
 255 ily as a quantity that links temperature and absolute humidity, which are the quanti-  
 256 ties that ultimately enter the models' radiation schemes. Therefore, it is reasonable to  
 257 compare RH computed in a uniform way for all models.  
 258

259 Overall, the models all capture the typical C-shape of the tropical mean RH pro-  
 260 file with two maxima, one atop the boundary layer and one at the tropopause, and a min-  
 261 imum in the mid troposphere (Figure 1). The models' RH distributions also agree re-  
 262 markably well with the ERA5 distribution. In fact, the multi-model mean RH (not shown)  
 263 differs from ERA5 by less than 2% RH throughout the troposphere, except from the al-  
 264 titude region above 15 km.  
 265

266 Nevertheless, there are considerable differences among the models. The inter-model  
 267 standard deviation  $\sigma(\text{RH})$  (Figure 1c) has a distinct maximum around the top of the bound-  
 268 ary layer (BL). The transition from the BL to the free troposphere is marked by a steep  
 269 gradient in RH. Therefore, differences in the depth of the BL cause a large inter-model

270 spread in RH. In IFS the RH gradient at the top of the BL is particularly steep and the  
 271 lower free troposphere is significantly dryer than in other models. Generally, in most mod-  
 272 els the BL is deeper than in ERA5. The inter-model spread is smallest in the mid tro-  
 273 posphere between 4 and 10 km altitude. In that region  $\sigma(\text{RH})$  is 2-3% RH and approx-  
 274 imately constant with height. RH is lower than in ERA5 in the majority of models, ex-  
 275 cept ICON and NICAM. Above 10 km  $\sigma(\text{RH})$  increases with altitude and exceeds 8% RH  
 276 at 100 hPa.  
 277

278 To the extent one thinks of RH anomalies as linking  $q$  and  $T$  anomalies, it is in-  
 279 formative to consider  $q$  and  $T$  separately. In the DYAMOND models,  $T$  anomalies are  
 280 smallest in the lower troposphere, where they are constrained by identical SSTs, and in-  
 281 crease with height throughout the free troposphere, where the temperature profile is set  
 282 by convection and radiation (Figure 2a,b). At lower levels, where  $T$  anomalies are small,  
 283  $q$  and RH anomalies are correlated (Figure 1b, Figure 2d). In the upper troposphere, where  
 284  $T$  anomalies are large,  $T$  and  $q$  anomalies are correlated (Figure 2b,d), consistent with  
 285 the idea that model errors in  $T$  cause errors in  $q$ . Although RH anomalies are also large  
 286 there (Figure 1), they play a minor role in determining whether a model's  $q$  is small or  
 287 large as compared to another model's  $q$ .  
 288

289 That the DYAMOND simulations were run just over one month (August/ September  
 290 2016) represents a potential limitation for the intercomparison, especially for vari-  
 291 ables that are subject to high internal variability on longer time scales. To estimate the  
 292 internal variability of RH, we calculate the interannual variability in the mean August/  
 293 September RH distribution based on five years (2014-2019) of the ERA5 reanalysis, shown  
 294 as the dotted line in Figure 1c. Given that interannual variations in free-tropospheric  
 295 water vapor are primarily driven by SST variations (Chuang et al., 2010) and the five  
 296 years include a strong El Niño event in 2015/2016, the interannual variability rather rep-  
 297 represents an upper bound for the internal variability one could expect in the DYAMOND  
 298 runs with fixed SST. Despite this, the inter-model standard deviation is significantly larger  
 299 than the ERA5 interannual variability throughout the troposphere, suggesting that the  
 300 inter-model differences are mostly systematic model biases rather than a result of poorly  
 301 sampled internal variability. The region where the inter-model differences are expected  
 302 to be colored most strongly by internal variability is the upper troposphere, where the  
 303 inter-model spread is only two to three times larger than the estimated internal variabil-  
 304 ity.  
 305

306 Another potential limitation arises from the common initialization of the models,  
 307 which might constrain the RH profiles even after the first ten days of the simulation that  
 308 were excluded (Section 2.2). To test this, we divided the analyzed 30-day period into three  
 309 consecutive 10-day periods and repeated the spread analysis. We did not find a system-  
 310 atic increase of the inter-model spread over time, except from the altitude region above  
 311 14 km. For a second analysis we made use of a coupled atmosphere-ocean simulation per-  
 312 formed with the ICON model at storm-resolving resolution (5 km grid spacing). The sim-  
 313 ulation was run for two years, starting on 20th January 2020. The length of the simu-  
 314 lation allows us to examine how the RH profile evolves after the first 40 days. In Fig-  
 315 ure 3 we compare tropical mean RH profiles for February 2020 and February 2021. Febru-  
 316 ary 2020 corresponds to days 13 to 40 after the initialization and is hence comparable  
 317 to the time period we analyze in the DYAMOND simulations. If the RH profile was still  
 318 in the transition from the initial conditions during that month, we would expect it to  
 319 be very different one year later. However, the RH differences between February 2020 and  
 320 February 2021 are small compared to the inter-model differences (cf. Figure 1). Through-  
 321 out the lower and mid troposphere, the difference is smaller than 1% RH. The largest  
 322 differences of up to 3% RH occur in the upper troposphere above 12 km. It has to be kept

323 in mind that SST changes from February 2020 to February 2021 in the coupled simu-  
 324 lation, so the RH differences we find are most likely related to SST changes rather than  
 325 to constraints from initialization in February 2020. The size of the differences and the  
 326 increase in the upper troposphere are in accordance to what we found for the inter-annual  
 327 variations in ERA5 (Figure 1c). It is very unlikely that the RH in February 2020 was  
 328 still in its transition from initialization, but SST and/or model drift changed in a way  
 329 to keep RH almost constant in February 2021. Hence, both analyses indicate that the  
 330 transition from the initial conditions is already largely completed after the first ten days.  
 331 The upper troposphere (above 12 km) might be an exception, but as we will see in Sec-  
 332 tion 4 the RH differences in this region do not significantly affect the clear-sky radiation  
 333 budget.

335 To examine how the RH spread in DYAMOND compares to that in conventional,  
 336 coarser atmospheric GCMs, we compare the DYAMOND ensemble to 29 GCMs that par-  
 337 ticipated in the Atmospheric Model Intercomparison Project (AMIP) experiments of the  
 338 Coupled Model Intercomparison Project phase five (CMIP5) (Taylor et al., 2012). The  
 339 AMIP simulations have a total length of 30 years (1979-2008) and were run with pre-  
 340 scribed (identical) SST. An exact quantitative comparison of the RH spread in GSRMs  
 341 and GCMs will not be possible until longer, multi-year storm-resolving simulations are  
 342 available. Nevertheless, a comparison to the AMIP GCMs is valuable to put the DYA-  
 343 MOND spread into perspective. The inter-model spread in AMIP is quantified both based  
 344 on 30-year averages and based on monthly averages of RH. This allows us to estimate  
 345 how much the inter-model spread in a single month can differ from the spread on clima-  
 346 tological timescales. The inter-model standard deviation of 30-year mean RH is denoted  
 347 by the black dashed line in Figure 1c. It lies within the range of monthly standard de-  
 348 viations, which is shown as gray shading. In most parts of the free troposphere, the most  
 349 extreme monthly standard deviations differ between 5-25% from the 30-year value. Only  
 350 in the tropopause region the deviations are larger (up to 40%). Overall, the AMIP ex-  
 351 periment confirms that the inter-model spread in a single month provides a good first  
 352 estimate of the inter-model spread on climatological timescales. However, the the vari-  
 353 ability in the monthly standard-deviation should be kept in mind when the (monthly)  
 354 DYAMOND spread is compared to the (climatological) AMIP spread in the following.

356 The inter-model spread in DYAMOND is smaller than the spread in AMIP through-  
 357 out most of the free troposphere. The largest reduction is found between 8 km and 14 km  
 358 altitude, where the RH spread in DYAMOND is reduced by approximately 50-70% com-  
 359 pared to AMIP. At lower altitudes, between 3 km and 8 km altitude, the DYAMOND spread  
 360 is smaller by approximately 25-50%. The lower free troposphere is an exception: the peak  
 361 in  $\sigma(\text{RH})$  at the top of the BL is less pronounced in CMIP5 AMIP than in DYAMOND,  
 362 indicating that variations in the depth of the BL are smaller in the AMIP models. How-  
 363 ever, part of the smaller spread in the AMIP models can be explained by the fact that  
 364 the hydrolapse in these models is generally less steep, which is evident from the AMIP  
 365 multi-model mean RH profile (Figure 1a). RH differences caused by a shift in the height  
 366 of the hydrolapse are therefore smaller, but dispersed over a broader layer.

368 As mentioned in Section 1, Sherwood et al. (2010) found that certain aspects of  
 369 the RH distribution converge in GCMs once horizontal grid spacings fall below a cer-  
 370 tain scale. A question arising from this is whether the agreement across GSRMs is bet-  
 371 ter than across the CMIP5 AMIP models with rather high resolutions. To test this we  
 372 repeated the spread analysis for only those nine AMIP models with grid resolutions ex-  
 373 ceeding T85 (128x256 grid points), corresponding to the scale suggested by Sherwood  
 374 et al. (2010). While the RH spread across these high-resolution GCMs is somewhat re-  
 375 duced in the upper and lower troposphere, the spread in the mid troposphere seems to

376 be unaffected (not shown). As we will show in Section 4.4, it is particularly the spread  
 377 in the mid troposphere that matters for the outgoing longwave radiation. Hence, there  
 378 is still a valuable improvement in GSRMs compared to the high-resolution GCMs.  
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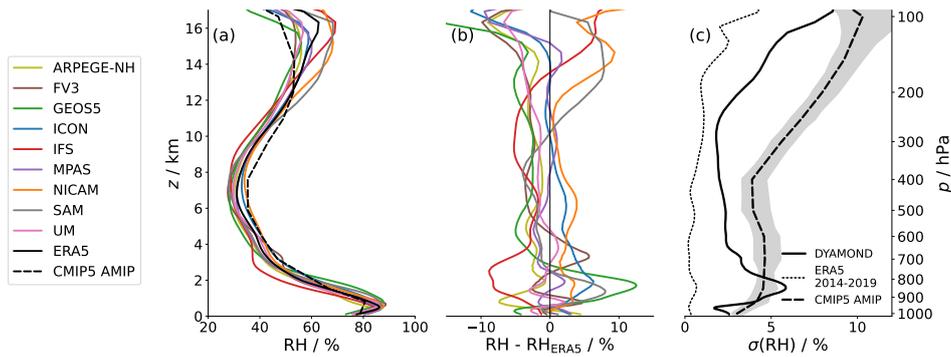
380 An additional series of DYAMOND runs with the ICON model allowed us to in-  
 381 vestigate how RH changes with increasing horizontal resolution beyond the convergence  
 382 scale suggested by Sherwood et al. (2010). We compared tropical mean (ocean only) RH  
 383 from runs at 80 km, 40 km and 20 km grid spacing with parameterized convection as well  
 384 as runs at 20 km, 10 km, 5 km and 2.5 km grid spacing with explicit convection (not shown).  
 385 In the parameterized runs RH hardly changes with increasing horizontal resolution. RH  
 386 strongly depends on resolution for the explicit runs at 20 km and 10 km, for which us-  
 387 ing explicit convection might not be adequate. At 5 km grid spacing RH has converged.  
 388 In some altitude regions, particularly in the mid troposphere, the RH difference between  
 389 the converged explicit runs and the parameterized runs is significantly larger than the  
 390 differences between the parameterized runs at different resolutions. These findings sug-  
 391 gest that resolving convection impacts RH although it seemed to have already converged  
 392 at coarser resolutions when convection was parameterized.  
 393

394 In summary, despite the shortness of the DYAMOND simulations we can say with  
 395 a high degree of certainty that the spread in free-tropospheric RH in the DYAMOND  
 396 GSRMs is reduced compared to the AMIP GCMs throughout most of the free troposphere,  
 397 except from the region at the transition to the BL and the tropopause region. We es-  
 398 timate the reduction to approximately 50-70% in the upper troposphere (8-14 km) and  
 399 25-50% in the mid troposphere (3-8 km). For an exact quantification longer storm-resolving  
 400 simulations are required. The reduction in the spread is even more remarkable consid-  
 401 ering that the DYAMOND models were not specifically calibrated for this experiment.  
 402 Many of them were even run in the storm-resolving configuration for the first time. How-  
 403 ever, as we will show in Section 4, the remaining RH differences still have a non-negligible  
 404 impact on the clear-sky radiation budget.  
 405

### 406 3.2 Moisture space

407 To distinguish between different dynamic regimes of the tropics, namely subsidence  
 408 and deep convective regimes, which are not necessarily co-located in different models,  
 409 we compare RH statistics in moisture space (Bretherton et al., 2005; Schulz & Stevens,  
 410 2018; Naumann & Kiemle, 2020). To span the moisture space, the randomly selected at-  
 411 mospheric profiles (Section 2.2) are ranked by their vertically integrated water vapor (IWV).  
 412 The integration is performed from the surface to an altitude of 20 km for all models.  
 413

414 Inter-model differences in the distribution of IWV are most pronounced at high IWV  
 415 values (Figure 4). This is apparent when comparing different percentiles of IWV. While  
 416 the 25th percentiles of all models lie within a range of  $2.2 \text{ kg m}^{-2}$ , the 75th percentiles  
 417 differ by more than  $10 \text{ kg m}^{-2}$  between the two most extreme models IFS and NICAM.  
 418 The overall shape of the IWV distribution differs among models. For IFS and NICAM  
 419 distributions are approximately uniform over a large range of IWV values, whereas the  
 420 distribution of ARPEGE-NH has a pronounced peak at IWV values of about  $50 \text{ kg m}^{-2}$ .  
 421 For the remaining models (including ERA5) distributions are more bimodal with a first  
 422 peak at  $25\text{--}30 \text{ kg m}^{-2}$  and a second peak at  $50\text{--}55 \text{ kg m}^{-2}$ . The exact position and the  
 423 relative strengths of the two peaks differ among the models. In SAM the first peak is  
 424 particularly pronounced, whereas in ICON the second peak is comparably strong. Bi-  
 425 modality is a known feature of the IWV distribution over tropical oceans, which is not  
 426 reliably reproduced by GCMs (Mapes et al., 2018). Our results indicate that this prob-



**Figure 1.** Tropical mean RH profiles and inter-model spread in the DYAMOND ensemble. (a) Tropical mean vertical profiles of RH over ocean regions from all DYAMOND models (colours), the ERA5 reanalysis (black solid) and the CMIP5 AMIP 30-year multi-model mean (black dashed). (b) Vertical RH profiles for the DYAMOND models shown as deviation from the ERA5 profile. (c) Inter-model standard deviation of tropical mean RH in DYAMOND (solid line). For comparison, the inter-annual RH spread in five years of ERA5 (2014-2019; dotted line) as well as the inter-model spread of the 30-year mean RH in the CMIP5 AMIP ensemble (dashed line) are shown. Grey shading indicates the range of inter-model standard deviations in individual months of the AMIP experiment.

427 lem is similarly pronounced in GSRMs.

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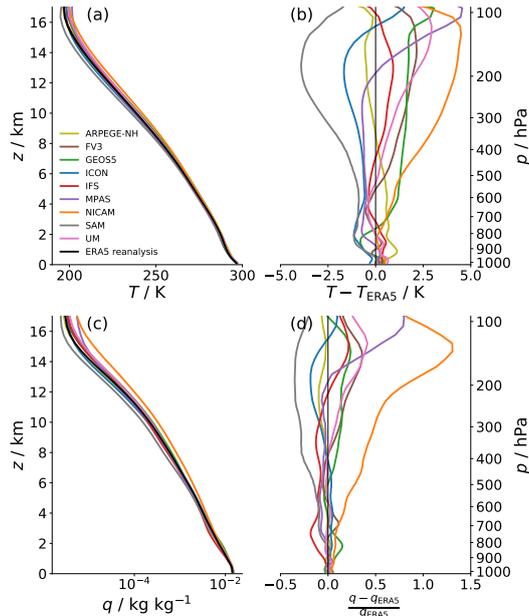
429 To display quantities in moisture space IWV-ranked profiles from each model are  
 430 split into 50 blocks, each containing an equal amount of profiles corresponding to two  
 431 percentiles of IWV. Quantities are then averaged over each block. This block-averaging  
 432 results in an  $x$ -axis that is linear in the percentile of IWV. Due to the non-uniform IWV  
 433 distributions (Figure 4) block-averaged IWV itself increases non-linearly as a function  
 434 of the IWV percentile. This is also visible in the multi-model mean (black line in Fig-  
 435 ure 5d), albeit very weakly: In the driest and moistest percentiles, respectively, the in-  
 436 crease in IWV is steeper than in the intermediate percentiles. Note that this also means  
 437 that the comparison of different models in moisture space is made at a certain IWV per-  
 438 centile rather than a certain IWV value.

439

440 SST increases from about 292 K in low IWV percentiles to about 302 K in high per-  
 441 centiles (Figure 5d). The SST gradient weakens from dry to moist regimes, similar to  
 442 how the meridional SST gradient weakens from the subtropics towards the inner tropics.  
 443 The inter-model standard deviation in block-averaged SSTs is around 0.15 K, imply-  
 444 ing that the the distribution of SST in moisture space is very similar among models.  
 445 The underlying PDF of SSTs is identical in all models, which, compared to other quan-  
 446 tities like IWV, puts an additional constraint on the SST distribution in moisture space.

447

448 Block-averaged vertical velocities (Figure 5c) indicate that the large-scale circula-  
 449 tion is directed upward in the highest 5–10 IWV percentiles and downward in drier re-  
 450 gions. The blocks with positive vertical velocities correspond to the regions of intense  
 451 rainfall in the Indo-Pacific Warm Pool and the Intertropical Convergence Zone (ITCZ),  
 452 where deep convection is concentrated. Note that block-averaged vertical velocities take  
 453 on values up to  $13 \text{ cm s}^{-1}$  in the deep convective regimes, but the color map in Figure  
 454 5c is truncated at  $1.2 \text{ cm s}^{-1}$ . The drier blocks correspond to trade wind regimes. There,

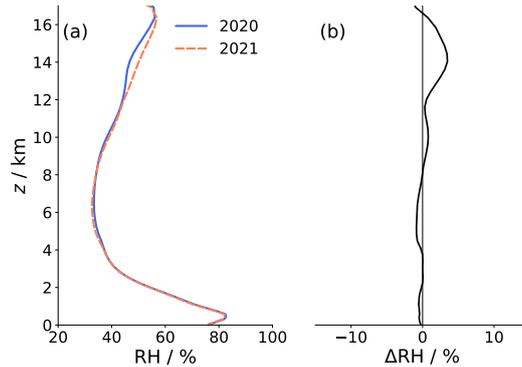


**Figure 2.** Tropical mean vertical profiles of temperature  $T$  and specific humidity  $q$  over ocean regions from all DYAMOND models. Vertical profiles of  $T$  (a, b) and  $q$  (c, d) are shown as absolute values together with the ERA5 profiles (a, c) and as deviation from the ERA5 profiles (b, d). Deviations in  $q$  are in fractional units, i.e. normalized by the ERA5 value ( $q_{\text{ERA5}}$ ).

455 the free troposphere is characterized by large-scale subsidence, which increases in strength  
 456 with decreasing IWV. At the transition from deep convective to subsidence regimes near  
 457 the 90th IWV percentile vertical velocities are negative in the lower free troposphere and  
 458 positive aloft. These blocks represent an advanced state in the life cycle of deep convec-  
 459 tion associated with upper-level anvil clouds. This state is characterized by ascent above  
 460 the freezing level (which is located around 5 km) and descent below, driven by conden-  
 461 sation and freezing above the freezing level, and melting and evaporation of precipita-  
 462 tion below (Betts, 1990). The increasing amount of high-level clouds from dry to moist  
 463 regimes is also reflected by a sharp decrease in all-sky OLR in the moist blocks (Figure  
 464 5d).

465

466 The largest RH values are found in the BL (5a), where moisture is provided by evap-  
 467 oration from the surface. The RH in the BL is relatively constant throughout moisture  
 468 space. Where air rises from the BL to the free troposphere in deep convective plumes  
 469 it cools and its RH increases until saturation is reached. Therefore, the highest RH val-  
 470 ues in the free troposphere are found in deep convective regions. Throughout the tropics,  
 471 particularly in the subsidence regions, the free-tropospheric RH profile takes on a  
 472 typical C-shape, which is known from observations (e.g. Jensen et al., 1999; Vömel et  
 473 al., 2002) and GCMs (Sherwood et al., 2010). With a simple analytical model Romps  
 474 (2014) showed that this shape of the RH profile can be understood from the balance be-  
 475 tween moistening by detrainment of saturated air from convective regions and drying by  
 476 subsidence. As the temperature lapse rate increases with height, the reduction in RH  
 477 for a given amount of subsidence also increases with height. This increase in subsidence  
 478 drying, together with a decrease in convective moistening, explains why RH decreases  
 479 with height in the lower free troposphere. In the upper troposphere, however, convec-  
 480 tive moistening dominates and causes RH to maximize at the tropopause. A plateau in



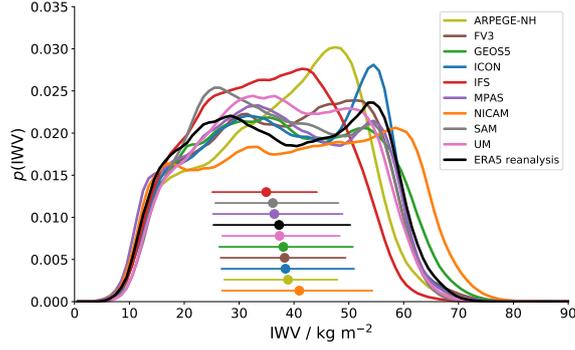
**Figure 3.** Comparison of RH in two subsequent Februaries of a coupled atmosphere-ocean simulation with the ICON model at storm-resolving resolution (5 km). (a) Tropical mean (ocean only) RH in February 2020 (blue) and February 2021 (orange). February 2020 corresponds to days 13 to 40 after initialization, which is comparable to the analyzed DYAMOND period. (b) RH difference between February 2020 and February 2021.

481 RH is apparent near the freezing level at around 5 km particularly in the high IWV per-  
 482 centiles. Latent heat release from ice formation enhances the stability at this level, which  
 483 causes deep convection to preferably detrain there (Stevens et al., 2017).  
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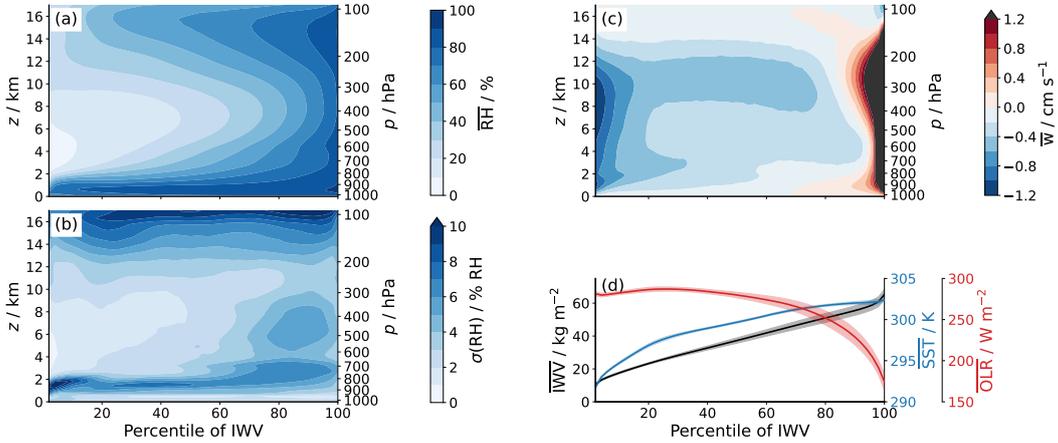
485 Displaying inter-model differences in moisture space reveals how they are distributed  
 486 over the different regimes of the tropics. RH anomalies for individual models are shown  
 487 in Figure A1 in Appendix A. Here we focus on the inter-model standard deviation  $\sigma(\text{RH})$ ,  
 488 shown in Figure 5b. First, it is apparent that the large inter-model spread in the upper  
 489 troposphere (Figure 1) prevails throughout the entire tropics. In the tropopause region  
 490  $\sigma(\text{RH})$  exceeds 10% RH everywhere except from the driest part of the subsidence regions.  
 491 Second, the local maximum in  $\sigma(\text{RH})$  at the top of the BL is most pronounced in the  
 492 driest regimes, where the RH gradient between the BL and the free troposphere is steep-  
 493 est (Figure 5a). In moister regions, where the RH gradient is less steep, the maximum  
 494 in  $\sigma(\text{RH})$  is weaker but broader. Third, in the mid troposphere  $\sigma(\text{RH})$  increases from  
 495 less than 1% RH in the lowest IWV percentiles to more than 5% RH near the 90th per-  
 496 centile. The largest part of the spread in tropical mean mid-tropospheric RH stems from  
 497 the region representing the transition from subsidence to deep convective regimes (cf.  
 498 Figure 5c). The large spread in this regime might be related to model differences in con-  
 499 vective behavior. In the moistest 5 percentiles of IWV the inter-model spread decreases  
 500 again. In these regimes deep convection keeps the RH close to 100% in all models.  
 501

#### 502 4 Impact of RH anomalies on clear-sky OLR

503 To quantify the effect of the inter-model differences on the radiation balance, we  
 504 translate them into differences in clear-sky OLR ( $\text{OLR}_c$ ) using a radiative transfer model.  
 505 The differences are analyzed in moisture space to determine how much different tropi-  
 506 cal moisture regimes contribute to the inter-model spread in tropical mean  $\text{OLR}_c$ . Fur-  
 507 thermore, we use radiative kernels to examine in which altitude regions RH differences  
 508 have the strongest impact on  $\text{OLR}_c$ . This allows us to identify the regions of the tropi-  
 509 cal troposphere in which a further reduction of RH differences would be most benefi-  
 510 cial.  
 511



**Figure 4.** Probability density function of integrated water vapor (IWV) over tropical ocean regions in the DYAMOND models and ERA5. Percentiles of each model’s IWV distribution are shown below the curves: Coloured circles indicate the median, horizontal bars range from the 25th to the 75th percentile.



**Figure 5.** Distributions of different block-averaged quantities in moisture space: (a) multi-model mean RH, (b) multi-model standard deviation of RH, (c) multi-model mean vertical velocity and (d) multi-model mean IWV (black), SST (blue) and all-sky OLR (red). Note that the color map for vertical velocity in (c) is truncated at  $1.2 \text{ cm s}^{-1}$  and any larger values (up to  $13 \text{ cm s}^{-1}$  in the highest IWV block) are displayed in black. For the quantities in (d) the inter-model standard deviation is denoted by shaded areas around the multi-model mean values.

512 Fundamentally, clear-sky OLR is determined by surface temperature as well as at-  
 513 mospheric temperature and greenhouse gas concentrations. For the  $\text{OLR}_c$  anomalies in  
 514 the DYAMOND models we expect that anomalies in the surface temperature play a minor  
 515 role, since SST is prescribed and its distributions in moisture space is very similar  
 516 among models (Figure 5). Furthermore, compared to model differences in water vapor  
 517 we expect differences in other greenhouse gasses to have a small effect on  $\text{OLR}_c$ . There-  
 518 fore, we fix the concentrations of other greenhouse gasses in our radiative transfer sim-  
 519 ulations. Thus, we assume that  $\text{OLR}_c$  anomalies in the DYAMOND models are primar-  
 520 ily caused by anomalies in atmospheric temperature and absolute humidity.  
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#### 4.1 Radiative transfer simulations

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The radiative transfer simulations to obtain clear-sky OLR are performed with the Rapid Radiative Transfer Model for GCMs (RRTMG Mlawer et al., 1997). RRTMG is a well validated fast radiative transfer code used in various weather and climate models. For this study we use RRTMG through the Python package `konrad` (DOI: 10.5281/zenodo.3899702), which in turn uses the `CliMT` Python interface for RRTMG (Monteiro et al. 2018). Note that not all of the DYAMOND models employ RRTMG as their native radiation scheme. Differences in the radiation codes can cause errors on the order of  $2 \text{ Wm}^{-2}$  in the models' internally calculated clear-sky OLR (Pincus et al., 2015). By using the same radiation scheme for each model for our offline calculations we neglect this error source, but instead focus solely on the effect of RH differences on clear-sky OLR.

OLR<sub>c</sub> is calculated based on the block-averaged profiles of pressure, temperature, and specific humidity in moisture space (Section 3.2). We found that calculating OLR<sub>c</sub> from block-averaged profiles generally introduces a small negative error compared to OLR<sub>c</sub> calculated based on individual profiles. OLR is often thought to increase linearly with temperature, and does, increasingly so, as temperatures are reduced below their tropical mean (e.g. Koll & Cronin, 2018). Within the tropics, where temperature fluctuations are small, variability in clear-sky OLR is dominated by RH changes (e.g. John et al., 2006). Due to the approximately logarithmic dependence of OLR<sub>c</sub> on RH, averaging decreases OLR<sub>c</sub> (Pierrehumbert et al., 2007). However, the resulting bias is very similar for all models, so that the effect on inter-model differences in OLR<sub>c</sub> is negligible.

To characterize the surface we use model output of surface pressure and the prescribed SST fields and select the same points as for the 3D data (Section 2.2). The surface emissivity is assumed to be 1. For other gasses than water vapor we use fixed vertical profiles in accordance with those in Wing et al. (2017): The ozone volume mixing ratio follows a gamma distribution in pressure and vertically constant volume mixing ratios are assumed for O<sub>2</sub>, CO<sub>2</sub>, CH<sub>4</sub> and N<sub>2</sub>O.

For the radiative transfer simulations we interpolate profiles from all models on a uniform vertical grid ranging from the surface to an altitude of 20 km with a resolution of 100 m. The top at 20 km corresponds to the maximum altitude for which output is available from all models. For our purpose OLR<sub>c</sub> is defined as the longwave upward clear-sky radiative flux at this level. Due to this definition the inter-model differences in OLR<sub>c</sub> only reflect  $T$  and  $q$  differences in the troposphere, potential differences in the stratosphere are ignored. Note that due to the missing stratosphere the absolute value of the OLR<sub>c</sub> defined at 20 km has a positive offset compared to the "true" OLR<sub>c</sub> defined at a higher TOA. However, this is not relevant for our results since we are only interested in the effect of differences in the troposphere.

We focus only on the clear-sky case here, so any cloud condensate contained in the profiles is ignored. Clouds, particularly those at high altitudes, have a strong impact on OLR. Hence, model differences in cloud properties can cause significant differences in all-sky OLR, which are not considered here.

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#### 4.2 Model differences in clear-sky OLR

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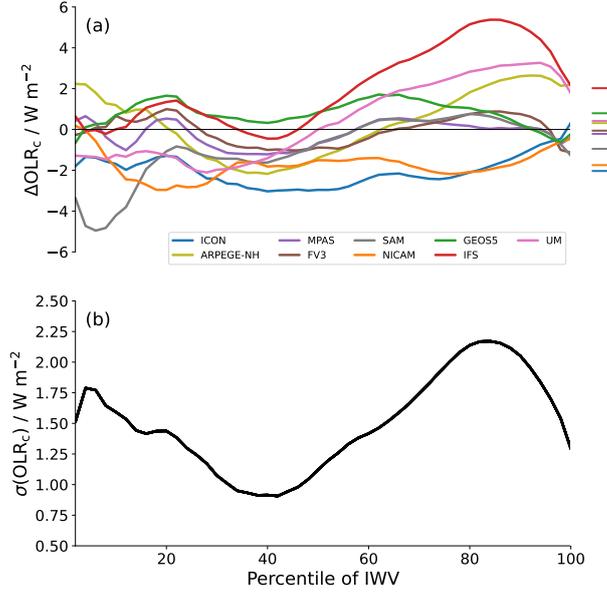
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Tropical mean OLR<sub>c</sub> differs by more than  $4 \text{ Wm}^{-2}$  between the two most extreme models IFS and ICON (Figure 6a). The multi-model standard deviation in tropical mean OLR<sub>c</sub> is  $1.2 \text{ Wm}^{-2}$ . This is small compared to cloud radiative effects, but still a third of the estimated radiative forcing due to a doubling of CO<sub>2</sub> (Collins et al., 2013). In some

572 models, e.g. UM and ARPEGE-NH, both positive and negative anomalies occur across  
 573 moisture space, which partly cancel in the tropical mean.  
 574

575 Two moisture regimes stand out due to a particularly large spread in clear-sky OLR  
 576 (Figure 6b): One local maximum in  $\sigma(\text{OLR})$  occurs in rather moist regimes around the  
 577 80th percentile of IWV. This corresponds to the region at the transition from deep con-  
 578 vective to subsidence regimes, where the inter-model RH spread in the mid troposphere  
 579 maximizes (Figure 5b). A second, slightly weaker maximum in  $\sigma(\text{OLR})$  is located at the  
 580 dry end of moisture space. In the next section we aim to better understand why the spread  
 581 in  $\text{OLR}_c$  maximizes in these two regimes and which altitude regions in the troposphere  
 582 contribute most.  
 583



**Figure 6.** Inter-model differences in clear-sky OLR in moisture space. (a) Anomalies in clear-sky OLR for each model, defined as the deviation from the ERA5 value and (b) inter-model standard deviation of clear-sky OLR.

### 584 4.3 Radiative kernels

585 To examine how different altitude regions in moisture space contribute to the spread  
 586 in tropical mean  $\text{OLR}_c$ , for each of the 50 blocks in moisture space we decompose each  
 587 model’s  $\text{OLR}_c$  anomaly into contributions from individual atmospheric layers using the  
 588 radiative kernel method (Soden et al., 2008).  
 589

590 Dividing the atmosphere into  $N$  vertical layers and linearising around the ERA5  
 591 state that we use as reference state, a model’s clear-sky OLR anomaly  $\Delta\text{OLR}_c$  can be  
 592 written as:

$$\Delta\text{OLR}_c \approx \sum_{i=1}^N (K_i^e \Delta e_i + K_i^T \Delta T_i) \approx \sum_{i=1}^N K_i^{\text{RH}} \Delta\text{RH}_i. \quad (1)$$

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Here, the index  $i$  denotes the vertical layer. The vectors  $\mathbf{K}^x$  are radiative kernels that describe the sensitivity of  $\text{OLR}_c$  to changes in a variable  $x$  in each layer:

$$K_i^x = \frac{\partial \text{OLR}_c}{\partial x_i}. \quad (2)$$

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The first approximation in Equation 1 assumes that anomalies in  $\text{OLR}_c$  are primarily caused by anomalies in atmospheric  $e$  and  $T$ , the effect of anomalies in surface temperature is assumed to be negligible. Moreover, it is assumed that contributions from each layer to the OLR response are independent, neglecting potential masking effects from perturbations above. Despite these assumptions the kernels  $\mathbf{K}^e$  and  $\mathbf{K}^T$  can be used to approximate the  $\text{OLR}_c$  anomalies of the DYAMOND models with good accuracy, which is shown in Figure B1 in Appendix B. The computation of the kernels is also described in Appendix B.

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Perturbations in  $e$  and  $T$  have opposite effects on  $\text{OLR}_c$ , which is evident from the different signs of the respective kernels (Figure B1). At constant RH perturbations in  $e$  and  $T$  are positively correlated, so their effects on  $\text{OLR}_c$  compensate to some degree. It is well known that in the water vapor bands, the spectral regions at which the water vapor optical depth is larger than 1, modulo foreign broadening, the emission from a layer to space depends only on RH (Nakajima et al., 1992; Ingram, 2010). This behavior is often referred to as "Simpsonian", as it has been recognized since the early work of Simpson (1928). Therefore, it can be assumed that anomalies in  $\text{OLR}_c$  in the DYAMOND models are primarily determined by RH anomalies. This corresponds to the second approximation in Equation 1.

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A perturbation in RH can be produced isothermally, i.e. by varying  $e$  and keeping  $T$  constant, or isobarically, i.e. by varying  $T$  and keeping  $e$  constant. Therefore, there are two ways to define a RH kernel, which we refer to as  $\mathbf{K}^{\text{RH},e}$  and  $\mathbf{K}^{\text{RH},T}$ , respectively:

$$\begin{aligned} K_i^{\text{RH},e} &= \left. \frac{\partial \text{OLR}_c}{\partial \text{RH}_i} \right|_{T=\text{const.}} = e_s K_i^e \\ K_i^{\text{RH},T} &= \left. \frac{\partial \text{OLR}_c}{\partial \text{RH}_i} \right|_{e=\text{const.}} = -\frac{e_s}{\text{RH}} \left( \frac{de_s}{dT} \right)^{-1} K_i^T. \end{aligned} \quad (3)$$

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To translate  $\mathbf{K}^e$  and  $\mathbf{K}^T$  into RH kernels they have to be weighted by a factor describing the change of RH for a change in  $e$  or  $T$ , respectively. For  $\mathbf{K}^{\text{RH},e}$  this factor is equal to the saturation water vapor pressure  $e_s$ . For  $\mathbf{K}^{\text{RH},T}$  the dependence of  $e_s$  on  $T$  given by the Clausius Clapeyron relation has to be taken into account.  $\mathbf{K}^{\text{RH},e}$  and  $\mathbf{K}^{\text{RH},T}$  are identical to the extent that the  $\text{OLR}_c$  response to a given change in RH is independent of whether this change is produced by a change in  $e$  or in  $T$ .

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$\text{OLR}_c$  anomalies approximated using  $\mathbf{K}^{\text{RH},e}$  (Figure 7c) are more accurate than those approximated using  $\mathbf{K}^{\text{RH},T}$  (Figure B2c). Therefore, for the further analysis we concentrate on  $\mathbf{K}^{\text{RH},e}$ . Overall,  $\text{OLR}_c$  anomalies approximated from RH anomalies agree well with true (directly calculated)  $\text{OLR}_c$  anomalies (Figure 7c) and the inter-model standard deviation  $\sigma(\text{OLR}_c)$  is well reproduced (Figure 7d). In Appendix B we elaborate more on the accuracy of the approximation for individual models as well as on the differences between  $\mathbf{K}^{\text{RH},e}$  and  $\mathbf{K}^{\text{RH},T}$ .

#### 4.4 Relative importance of different altitude regions

The impact of RH anomalies for the radiation budget is determined by the magnitude of the RH anomalies and the sensitivity of  $OLR_c$  to a given perturbation in RH. The latter is described by the radiative kernel  $\mathbf{K}^{RH,e}$  (Equation 1).  $\mathbf{K}^{RH,e}$  is negative throughout the tropical troposphere (Figure 7a), indicating that an increase in RH leads to a decrease in  $OLR_c$ . Its absolute value is largest in the mid troposphere in the dry subsidence regimes.

The overall distribution of the kernel can be understood based on the concept of an effective emission height for each wavenumber  $\nu$ , corresponding to the level at which the optical depth  $\tau_\nu$  reaches unity (e.g. Petty, 2006). A water vapor perturbation will generally have a strong impact on OLR if it is applied near or above a level for which  $\tau_\nu \approx 1$  in a large portion of the water vapor bands. Ultimately, the vertical distribution of  $\mathbf{K}^{RH,e}$  is determined by the distribution of effective emission heights. The distribution of effective emission heights depends on the distribution of spectral absorption coefficients and is generally broad (e.g. Clough et al., 1992; Jeevanjee & Fueglistaler, 2020), which is why  $\mathbf{K}^{RH,e}$  is significant throughout the troposphere. However, above a certain level (around 200 hPa) the emission from water vapor rapidly declines, which is well known from studies of radiative cooling (e.g. Hartmann & Larson, 2002). Due to the strong dependence of water vapor concentrations on temperature through Clausius-Clapeyron, the amount of water vapor at these upper levels is so small that even at the line centers  $\tau_\nu$  barely reaches unity. The emission to space also declines at the lowest levels, although water vapor is abundant, because there is only a limited part of the spectrum (on the wings of lines and very weak lines), where radiation can escape to space without being re-absorbed at upper levels. This "masking" by the optically thick atmosphere above increases with increasing IWV, which is why for a given altitude level the absolute value of  $\mathbf{K}^{RH,e}$  decreases towards moist regimes.

Note that in general the distribution of a water vapor kernel is very sensitive to how water vapor is perturbed (Held & Soden, 2000). We perturb RH by a constant value, similar to Spencer and Braswell (1997) or Allan et al. (1999). In this case the perturbation in  $e$  is proportional to  $e_s$  (Equation 3). Hence, it decreases with altitude, but is approximately constant throughout moisture space. Other studies apply equal fractional perturbations in  $e$  (Shine & Sinha, 1991) or keep RH constant under a uniform temperature perturbation (Held & Soden, 2000; Soden et al., 2008). In both cases the perturbation in  $e$  is proportional to  $e$  itself, resulting in a stronger weighting of moist compared to dry regimes.

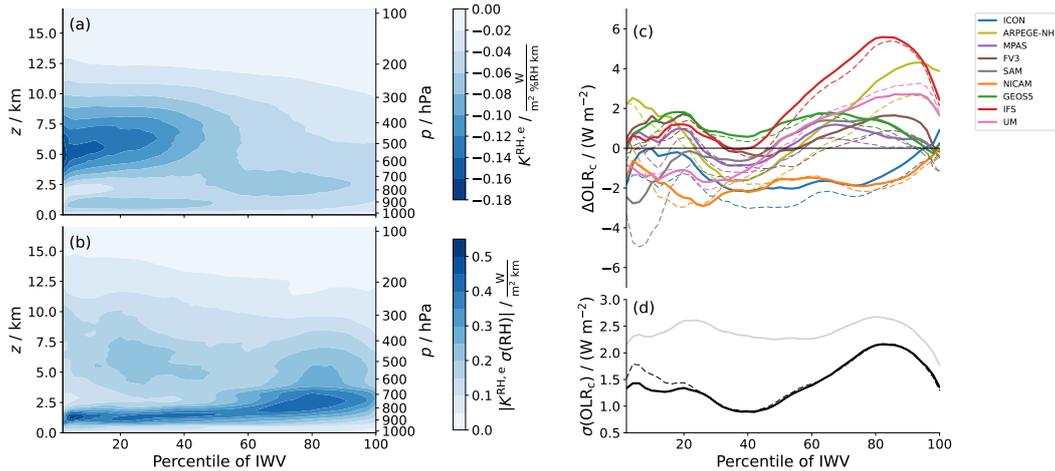
In low IWV percentiles  $\mathbf{K}^{RH,e}$  peaks at an altitude of around 6 km. The peak weakens from dry to moist regimes for the reasons named above. A very similar behavior was found by Spencer and Braswell (1997) for base states with RH values roughly corresponding to those in the dry half of moisture space. For the moist half of moisture space, however, we find that lower atmospheric layers (below 5 km) become relatively more important. A possible explanation for this could be the continuum absorption in the major atmospheric window region (approximately 800 to 1200  $\text{cm}^{-1}$ ), which acts to decrease the surface component of  $OLR_c$  as RH increases in the lower troposphere. In contrast to absorption in the water vapor bands, continuum absorption scales with the square of the water vapor pressure and therefore becomes relatively more important for high humidity base states.

The product of the RH response kernel  $\mathbf{K}^{RH,e}$  and the RH inter-model standard deviation  $\sigma(\text{RH})$  (Figure 7b) indicates where the actual inter-model differences have the

685 strongest effect on clear-sky OLR. First, the top of the BL stands out as a narrow re-  
 686 gion of strong impact.  $OLR_c$  is not particularly sensitive to RH perturbations there (Fig-  
 687 ure 7a), but the inter-model differences in RH are large (Figure 5b) because the mod-  
 688 els differ in the depth of the BL. RH differences in a broad layer in the mid troposphere  
 689 also significantly affect  $OLR_c$ . Integrated over its full width, the contribution from this  
 690 layer is larger than that from the BL top. The mid troposphere is characterized by an  
 691 increasing RH spread from dry to moist regimes with a pronounced maximum near the  
 692 80th IWV percentile (Figure 5b) and a decreasing sensitivity of  $OLR_c$  from dry to moist  
 693 regimes (Figure 7a). The combination of both results in a relatively uniform importance  
 694 of RH differences across moisture space, with two local maxima occurring near the 30th  
 695 and near the 80th IWV percentile. The layer over which RH differences have a consid-  
 696 erable impact on  $OLR_c$  generally extends to higher altitudes in the dry regimes than in  
 697 the moist regimes, which is again a consequence of the stronger masking effect in moist  
 698 regimes. Due to the low sensitivity of  $OLR_c$  to RH perturbations in the upper tropo-  
 699 sphere (above about 10–12 km) the large inter-model RH differences there (Figure 5b)  
 700 have virtually no effect on  $OLR_c$ .

702 Not considering clouds has an effect on the response kernels. Particularly high clouds  
 703 are important, because they mask some of the effect of  $T$  and  $q$  in lower atmospheric lev-  
 704 els (Soden et al., 2008). They are mainly present in moist regimes, starting around the  
 705 60th IWV percentile in most models (not shown). In these regimes we would expect the  
 706 sensitivity of  $OLR_c$  to RH perturbations to decrease, particularly in levels below the clouds,  
 707 which are most abundant at around 8-12 km height. This would dampen some of the ef-  
 708 fect of the large RH differences in the lower and mid free troposphere in the moist regimes.

710 An important point to note is that the vertical integration of the product of  $\mathbf{K}^{RH,e}$   
 711 and  $\sigma(RH)$ , shown as the grey line in Figure 7d, does not yield the inter-model standard  
 712 deviation in  $OLR_c$ , but a higher value, which is more uniform throughout moisture space.  
 713 In many models RH anomalies have different signs in different altitude regions (Figure  
 714 1 and Figure A1). This information is not contained in  $\sigma(RH)$ . The effects of such op-  
 715 posite RH anomalies on  $OLR_c$  compensate to some degree. Interestingly, such compen-  
 716 sating errors play a bigger role in the dry regimes, as indicated by the larger difference  
 717 between the grey and the black line in Figure 7d and evident from Figure A1. In fact,  
 718 it is only due to these compensating effects that dry regimes contribute less to tropical  
 719 mean differences in clear-sky OLR than moist regimes.



**Figure 7.** Impact of RH differences on clear-sky OLR in moisture space. (a) RH response kernel  $K^{RH,e}$  showing the sensitivity of clear-sky OLR to a 1% RH change in a 1 km layer under constant temperature for 50 blocks in moisture space, (b) inter-model standard deviation  $\sigma(RH)$  weighted with  $K^{RH,e}$ , (c) Clear-sky OLR anomalies approximated from  $K^{RH,e}$  and the RH anomalies of each model and (d) inter-model standard deviation in the approximated clear-sky OLR. Thin dashed lines in (c) and (d) correspond to "true" clear-sky OLR calculated directly from temperature and specific humidity profiles (same as in Figure 6). The vertical integral of (b) is shown as the grey line in (c).

## 5 Summary and conclusions

In this study we quantified inter-model differences in tropical free-tropospheric humidity in an ensemble of nine different GSRMs, which took part in DYAMOND, a first 40-day intercomparison for models of this type. We focused on the effect of the humidity differences on the radiation budget and therefore concentrated on differences in RH rather than absolute humidity. The RH is most informative because in a large part of the spectrum the emission from a layer to space depends primarily on RH (Nakajima et al., 1992; Ingram, 2010).

A justified question that arises is how much one can learn about climatological RH biases from an intercomparison as short as 40 days. To address some major concerns associated with the shortness of the DYAMOND simulations, we performed additional analysis based on longer-term data sets. One potential limitation is that the models' RH might still be constrained by the common initial conditions. However, both a first two-year storm-resolving simulation with the ICON model as well as the evolution of the inter-model RH spread within the analyzed 30-day period suggest that the transition from the initial conditions is largely completed after the excluded ten-day spinup period. Another concern is that the RH biases identified in the analyzed 30-day period might result mainly from a poor sampling of internal variability. However, the DYAMOND inter-model spread in RH is significantly larger than what would be expected from internal variability, which was estimated from five years of ERA5 reanalysis data. This suggests that the inter-model differences we find in DYAMOND mostly represent systematic model biases. This applies least to the upper troposphere (above 12 km), where natural variability is comparably large. In accordance with that, the inter-model RH spread in each individual month of the CMIP5 AMIP intercomparison is within a 25% range of the spread in 30-year mean RH, only in the upper troposphere deviations are larger. We conclude from these results

746 that in a large part of the free-troposphere one month of intercomparison already pro-  
 747 vides a good first estimate for climatological RH biases.

749 The comparison to the CMIP5 AMIP ensemble also shows that the inter-model spread  
 750 in tropical mean RH in DYAMOND is reduced throughout the free troposphere, except  
 751 from the transition to the boundary layer and the tropopause region. This indicates that  
 752 free-tropospheric RH and hence clear-sky OLR are better constrained in GSRMs than  
 753 in GCMs. Based on this first month of intercomparison we estimate the reduction to ap-  
 754 proximately 50-70% in the upper troposphere (8-14 km) and 25-50% in the mid tropo-  
 755 sphere (3-8 km). For an exact quantification longer storm-resolving simulations will be  
 756 needed.

758 A question that cannot be answered from the relatively short DYAMOND simu-  
 759 lations is whether the spread in the water-vapor-lapse-rate feedback is also reduced in  
 760 GSRMs. However, there are some reasons to be optimistic about this. On the one hand,  
 761 to the extent that the feedback depends on the base-state RH as suggested by Bourdin  
 762 et al. (2021), reducing the inter-model spread in present-day RH should also reduce the  
 763 spread in the feedback. On the other hand, the water-vapor-lapse-rate feedback depends  
 764 on how much RH changes under warming. Given that the present-day RH is better con-  
 765 strained in GSRMs, it seems unlikely that the spread in the RH response is increased.  
 766 This is to be verified once model simulations at higher SSTs are available.

768 Although RH differences are reduced in the DYAMOND ensemble, they still cause  
 769 a spread of  $1.2 \text{ Wm}^{-2}$  in tropical mean clear-sky OLR. To better understand how dif-  
 770 ferent tropical moisture regimes contribute to this spread, it has proven useful to com-  
 771 pare model fields in moisture space, i.e. sorted from low to high IWV. Combining the  
 772 inter-model standard deviation  $\sigma(\text{RH})$  with radiative kernels (the sensitivity of clear-sky  
 773 OLR to RH perturbations) in moisture space allowed us to examine the radiative im-  
 774 pact of the RH differences in a given dynamic regime and altitude region and hence to  
 775 assess in which regions a further reduction would be most beneficial. Based on the re-  
 776 sults we can split the tropical free troposphere into four main regions:

- 777 1. The transition between the BL and the free troposphere. Throughout the tropics  
 778 this altitude region (around 2 to 3 km) is characterized by a local maximum  
 779 in the inter-model RH spread, with  $\sigma(\text{RH})$  exceeding 6% RH. These differences are  
 780 associated with differences in the depth of the BL. Due to their large magnitude  
 781 they contribute considerably to the spread in clear-sky OLR, although the sen-  
 782 sitivity of clear-sky OLR to a given RH perturbation is rather small in this alti-  
 783 tude region.
- 784 2. The mid troposphere of moist regimes. This region ranges from about 3 km to 10 km  
 785 in altitude and roughly covers the highest 50 percentiles of IWV in moisture space.  
 786 With  $\sigma(\text{RH})$  up to 6% RH the inter-model spread in these moist regimes is sub-  
 787 stantially larger than in the same altitude region of dry regimes. The spread max-  
 788 imizes at the transition from deep convective to subsidence regimes near the 90th  
 789 percentile of IWV, which might be indicative of model differences in convective  
 790 behavior. The large RH differences cause the inter-model OLR spread to maxi-  
 791 mize in this region, although the sensitivity of clear-sky OLR to RH perturbations  
 792 is moderate.
- 793 3. The mid troposphere of dry regimes. In this region the model agreement in RH  
 794 is remarkably good. The inter-model standard deviation  $\sigma(\text{RH})$  is 1-3% RH and  
 795 hence less than half of the standard deviation in moist regimes. However, the sen-  
 796 sitivity of clear-sky OLR to RH perturbations is moderate.
- 797

sensitivity of clear-sky OLR to RH perturbations is considerably larger. Therefore, the small RH differences in the dry regimes have a comparable effect on clear-sky OLR as the larger differences in the moist regimes. This is why the inter-model spread in clear-sky OLR has a second, albeit slightly weaker local maximum in the dry regimes. The maximum is weaker than the one in the moist regimes because compensating effects due to opposite RH anomalies at different altitude regions occur more frequently in the dry regimes. The reason for this is not obvious and needs further investigation.

4. The upper troposphere. In the altitude region above 10 km the inter-model spread is generally large, with  $\sigma(\text{RH})$  exceeding 8% near the tropopause. However, the sensitivity of clear-sky OLR to RH perturbations is so small that the impact of these differences on the clear-sky OLR is negligible.

Our results are limited to the clear-sky case. High clouds, which are most abundant in the moist regimes, mask some of the clear-sky effect (e.g. Soden et al., 2008) and hence reduce the radiative impact of the RH differences in the mid troposphere. This highlights even more the importance of the dry regimes, where high clouds are rare.

We conclude that to further constrain the radiation budget in GSRMs it is most crucial to reduce the RH differences at the top of the BL and in the mid troposphere. Reducing the former by adjusting the depth of the BL seems possible with the current level of knowledge. Also, one would expect clear benefits from increased vertical resolution when it comes to representing the BL depth. On the other hand, observational reference data are sparse because satellite capacities to probe the BL region are still limited. Reducing the differences in the mid troposphere seems more challenging and requires a detailed understanding of the processes controlling RH in these regions remote from deeper convection. An advantage is that this altitude region of the tropical atmosphere is extensively observed by satellites.

## Appendix A RH anomalies in individual models

In Section 3.2 we focused on the inter-model spread in RH expressed by the inter-model standard deviation  $\sigma(\text{RH})$ . Here we show how the RH deviates from ERA5 in moisture space for individual models (Figure A1). It is evident that for many models, particularly for ICON, NICAM and IFS, the largest part of the RH anomalies in the mid troposphere that are apparent in the tropical mean (Figure 1) stems from rather moist regimes. Furthermore, in all models RH anomalies of opposite sign exist at different altitude regions and across moisture space. As mentioned in Sections 4.2 and 4.4 their effects on tropical mean clear-sky OLR partly compensate. For example, the GEOS5 model has both an anomalously moist lower free troposphere (due to an anomalously deep BL) and an anomalously dry mid free troposphere in regions of intermediate IWV (Figure A1d). Due to the compensation of these opposite effects the  $\text{OLR}_c$  anomaly in these regions is rather small (Figure 6). In the UM model the lower and mid free troposphere are anomalously moist in dry regimes and anomalously dry in moist regimes (Figure A1j). The resulting  $\text{OLR}_c$  anomalies almost fully compensate in the tropical mean (Figure 6).

## Appendix B Radiative kernels for water vapor pressure, temperature and relative humidity

To obtain the radiative kernels  $\mathbf{K}^e$  and  $\mathbf{K}^T$  for a given block in moisture space,  $\text{OLR}_c$  is calculated for the averaged ERA5 profiles in this block using the setup described in Section 4.1. The calculation is repeated with a small perturbation applied to  $e$  or  $T$  in one atmospheric layer, yielding the element of  $\mathbf{K}^e$  of  $\mathbf{K}^T$ , respectively, for that layer. This

847 is done successively for all layers. We perturb  $e$  by 5% of its absolute value and  $T$  by 1 K.  
 848 The chosen perturbation sizes lie within the range for which the assumption of linear-  
 849 ity around the base state is valid. Within this range the calculated kernels are indepen-  
 850 dent of the exact perturbation size.

851  
 852 The kernels  $\mathbf{K}^e$  and  $\mathbf{K}^T$  can be used together with anomalies in  $e$  and  $T$  to approx-  
 853 imate anomalies in clear-sky OLR (Equation 1) in the DYAMOND models with good  
 854 accuracy (Figure B1e). The approximation is least accurate for the NICAM model. NICAM  
 855 is the model with the largest anomalies in absolute humidity (Figure 2), so it is likely  
 856 that the assumption of linearity around the reference state starts to lose validity. In other  
 857 models some smaller inaccuracies occur particularly in the dry half of moisture space.  
 858 Most of them can be explained by SST anomalies that are not considered in Equation  
 859 1. Such SST anomalies have a stronger impact in the dry regions because the surface com-  
 860 ponent of  $\text{OLR}_c$  is larger there than in moist regions. The largest deviations between true  
 861 and approximated  $\text{OLR}_c$  anomalies in dry regimes arise for SAM and ARPEGE-NH. These  
 862 are only partly explained by SST anomalies, so non-linearity or masking effects might  
 863 play a role.

864  
 865 As explained in Section 4.3, anomalies in  $\text{OLR}_c$  can also be approximated from RH  
 866 anomalies and a RH kernel (Equation 1). There are two ways to define a RH kernel by  
 867 varying either  $e$  or  $T$  (Equation 3), which we refer to as  $\mathbf{K}^{\text{RH},e}$  and  $\mathbf{K}^{\text{RH},T}$ , respectively.  
 868 Our main analysis is based on  $\mathbf{K}^{\text{RH},e}$  because it approximates the anomalies in  $\text{OLR}_c$   
 869 more accurately. The largest deviations from true (directly calculated)  $\text{OLR}_c$  anom-  
 870 alies occur for SAM in the lowest IWV percentiles, for ARPEGE-NH in high percentiles  
 871 and for ICON in all percentiles (Figure 7c). The inter-model standard deviation  $\sigma(\text{OLR})$   
 872 is well reproduced with the approximated  $\text{OLR}_c$  (Figure 7d), except from the lowest IWV  
 873 percentiles, where it is slightly underestimated. This is mainly caused by the deviations  
 874 in SAM and ICON. For most models the approximation from RH anomalies is slightly  
 875 less accurate than the one from  $e$  and  $T$  anomalies (cf. Figure B1). An exception is NICAM,  
 876 for which  $\text{OLR}_c$  approximated from RH anomalies matches the true  $\text{OLR}_c$  much bet-  
 877 ter than the one approximated from  $e$  and  $T$  anomalies.

878  
 879 For completeness Figure B2 shows  $\mathbf{K}^{\text{RH},T}$  and the  $\text{OLR}_c$  anomalies approximated  
 880 using this version of the RH kernel.  $\mathbf{K}^{\text{RH},T}$  takes on larger absolute values than  $\mathbf{K}^{\text{RH},e}$   
 881 (cf. Figure 7a, note the different colour scales in Figures 7 and B2), i.e. a 1% increase  
 882 in RH causes a larger decrease in clear-sky OLR if it is produced by decreasing  $T$  rather  
 883 than increasing  $e$ . Furthermore, the peak altitude in  $\mathbf{K}^{\text{RH},T}$  is lower than in  $\mathbf{K}^{\text{RH},e}$ . These  
 884 differences indicate that for  $\text{OLR}_c$  it does matter to a certain degree whether a RH per-  
 885 turbation is caused by a perturbation in  $e$  or in  $T$ . Nevertheless, considering that the  
 886 physical mechanisms behind a change in  $\text{OLR}_c$  are very different for changes in  $e$  and  
 887  $T$ , the two kernels agree remarkably well, again demonstrating that the atmosphere be-  
 888 haves partly "Simpsonian" (see Section 4.3).

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Version v0.8.0 of konrad is available at <https://github.com/atmtools/konrad/tree/v0.8.0>

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The authors declare no conflict of interest.

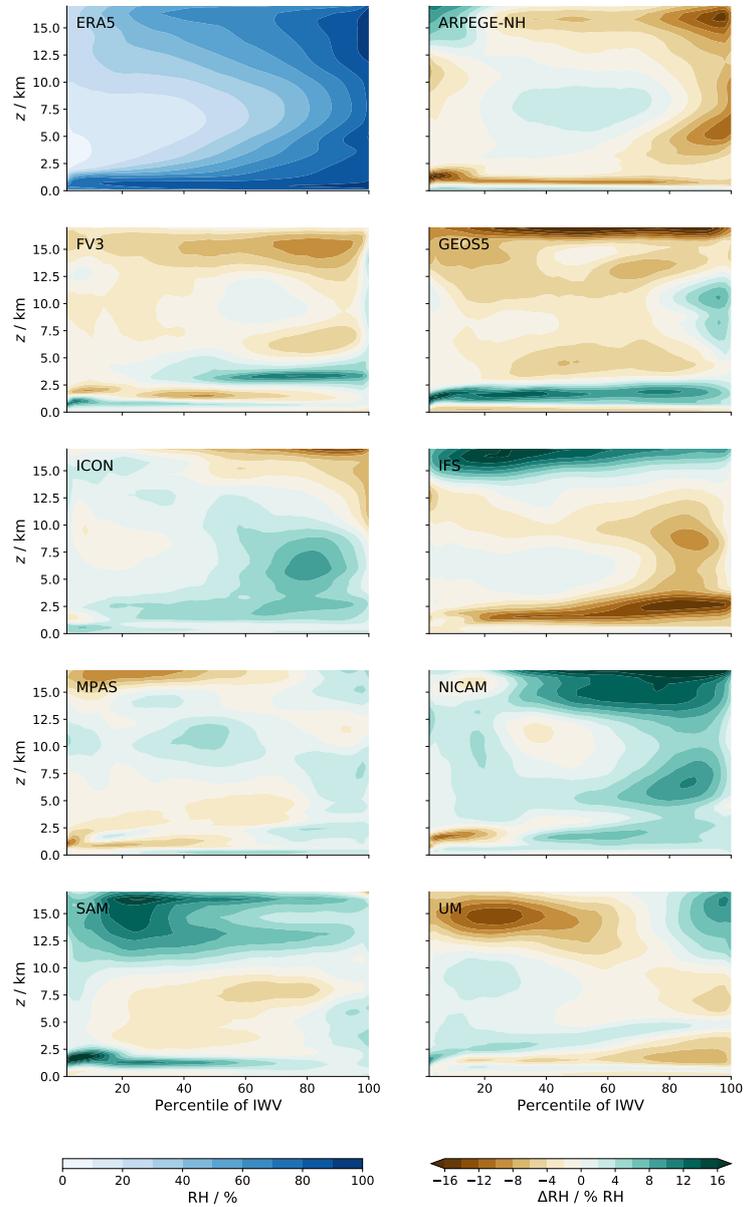
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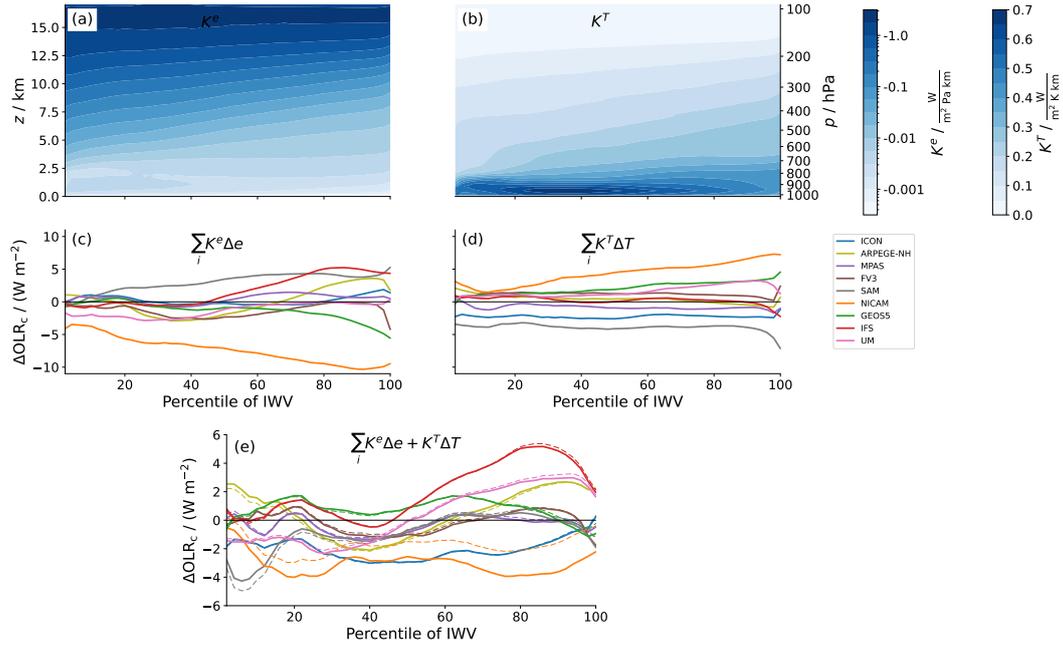
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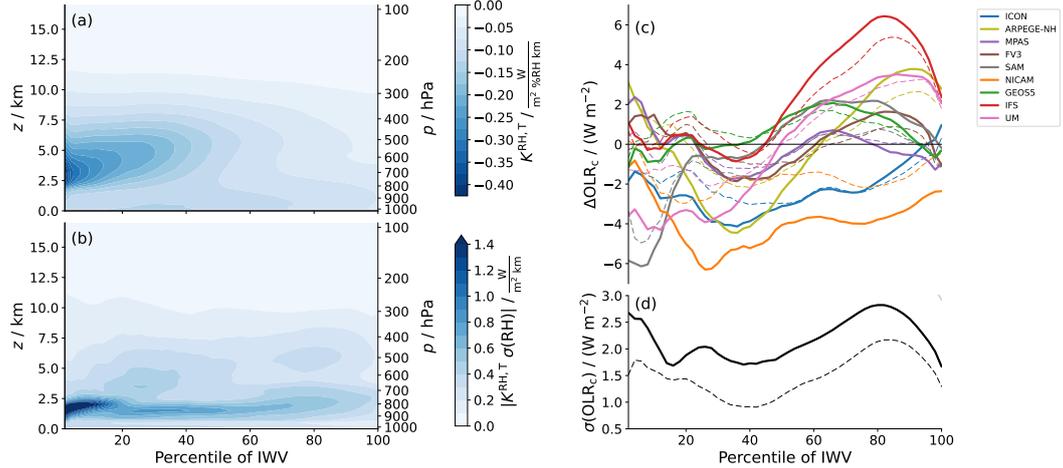
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**Figure A1.** RH anomalies of DYAMOND models in moisture space. The upper left panel shows the ERA5 RH distribution in moisture space, remaining panels show the deviation from the ERA5 RH for each model.



**Figure B1.** Clear-sky OLR anomalies in the DYAMOND models approximated with the kernel method. (a) Water vapor response kernel  $K^e$  showing the sensitivity of clear-sky OLR to a change of 1 Pa in water vapor pressure  $e$  in a 1 km layer. Note the logarithmic colour scale. (b) Temperature response kernel  $K^T$  showing the sensitivity of clear-sky OLR to a temperature change of 1 K in a 1 km layer. Also shown are clear-sky OLR anomalies calculated (c) solely from anomalies in  $e$  and the respective kernel  $K^e$  and (d) solely from anomalies in  $T$  and  $K^T$ . (e) shows clear-sky OLR anomalies calculated from both kernels. True (directly calculated) clear-sky OLR anomalies are shown as thin dashed lines for comparison.



**Figure B2.** As Figure 7 but based on  $K^{RH,T}$ . Note that the colour scale in (a) and (b) is different from Figure 7 since  $K^{RH,T}$  takes on more negative values than  $K^{RH,e}$ .