

Catchment processes can amplify the effect of increasing rainfall variability

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Abstract

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ABSTRACT

By filtering the incoming climate signal when producing streamflow, river basins can attenuate – or amplify – projected increases in rainfall variability. A common perception is that river systems dampen rainfall variability by averaging spatial and temporal variations in their watersheds. However, by analyzing 671 watersheds throughout the United States, we find that many catchments actually amplify the coefficient of variation of rainfall, and that these catchments also likely amplify *changes* in rainfall variability. Based on catchment-scale water balance principles, we relate that faculty to the interplay between two fundamental hydrological processes: water uptake by vegetation and the storage and subsequent release of water as discharge. By increasing plant water uptake, warmer temperatures might exacerbate the amplifying effect of catchments. More variable precipitations associated with a warmer climate are therefore expected to lead to even more variable river flows – a significant potential challenge for river transportation, ecosystem sustainability and water supply reliability.

The temporal variability of stream flow mediates a variety of social and ecological outcomes. For example, daily flow variability determines the suitability of aquatic habitats¹, whereas variations over longer time scales affect the resilience of water supply², river transportation³, local economic development⁴ and the potential for violent conflicts⁵. The coefficient of variation of stream flow (CV_Q , defined as the ratio between the standard deviation of flow and its mean) plays a particularly important role, demarcating whether riverine processes are variance-dominated, with long periods of little to no flow interspersed with erratic bursts of high discharge, or mean-dominated, with flow rates persistently at or near their long-term mean. This distinction has implications for the form, function and resilience of river-dependent systems⁶.

Although driven by the variability of incoming precipitation, stream flow variability is ultimately determined by physical processes that take place throughout (and below) the land surface. Through these processes, catchments regulate stochastic weather fluctuations to sustain stream-dependent social and ecological systems, and to potentially buffer these systems against changes in these fluctuations^{7,8}. This buffering of water variability is commonly deemed an ecosystem service provided by the catchment⁹, and emerges from a long-term co-evolution between the landscapes and the systems that depend on them, against the backdrop of a continually changing climate^{10–14}. Yet today's climate is changing at an unprecedented rate. The temporal variability of rainfall is projected to increase in most regions of the world, where increased temperatures will be associated with more intense and less frequent precipitation events¹⁵. The standard deviation of daily rainfall is projected to be more sensitive than rainfall averages to changing temperatures ($4–5\%$ per $^{\circ}C$ versus $\leq 1–2\%$ per $^{\circ}C$)^{15,16}. The coefficient of variation of both rainfall and stream flow has increased significantly in most regions of the United States over the last four decades (Figure 1a). The ability of social and ecological systems to adapt to these changes is determined by the capacity of river catchments to buffer the effect of rapidly changing rainfall variability as they generate flow.

Using daily stream flow and precipitation data from 671 catchments located across the contiguous United States for the 1980–2015 period (see Methods), we show that many catchments in fact *amplify* the variability (as quantified by CV) of incoming precipitation (Figure 1 a–c). These catchments might also amplify projected changes in rainfall variability, which has potentially troubling implications for stream-dependant social and ecological systems. We build on a widely used model of catchment-scale water balance dynamics^{17–19}, to relate the amplifying effect of catchments to the interplay between two fundamental hydrological processes: the *partitioning* of rainfall into runoff and evapo-transpiration, and the *retention* of non-evapotranspired water as storage prior to its release as stream flow. We show that an increase in the proportion of precipitation lost to evapo-transpiration (e.g., due to higher temperatures²⁰) will exacerbate the amplifying effect of catchments and ultimately increase the variability of stream flow, even if rainfall variability is held constant. This suggests that projected increases in rainfall variability and evapotranspirative losses might both contribute to increasingly variable stream flows. We

show that these two mechanisms had a driving influence on observed historical changes in CV_Q .

Results

The ratio $r = \frac{CV_Q}{CV_P}$ between the coefficients of variation of stream flow and precipitation spans several orders of magnitude across the conterminous United States. For about a third of the 671×4 considered combinations of catchments and seasons, daily stream flow has a higher coefficient of variation than the incoming daily precipitation (Figure 1b). However, the analysis also reveals a persistent patterns of variations in the r ratio across seasons, observation time scales and geographic regions, as shown on Figure 1c. Catchments in seasons (summer) or locations (Great Plains and Southwest) where temperature and precipitation peaks are in phase see a larger share of their precipitation 'lost' as evapo-transpiration²¹ and tend to amplify the variability of rainfall ($r > 1$). In contrast, catchments where flow generation is governed by long term (seasonal) water storage, either as snow pack (Rocky Mountains and High Plains) or in the subsurface (West Coast summers), tend to dampen the variability of daily rainfall. However, a majority (83%) of catchments and seasons amplify the variability of *monthly* rainfall (obtained from daily observations using a 30-day moving average, Figure 1d). Based on these results, we hypothesize that the partitioning and retention of rainfall by catchments, along with the considered observation time scale, play an important role in determining whether catchments amplify or attenuate incoming rainfall variability.

We formalize this hypothesis by deriving the r ratio of catchments based on four common, albeit extremely simplifying, assumptions about the underlying hydroclimatic processes. First, rainfall is assumed to follow a stationary marked Poisson process with exponentially distributed event depths¹⁷. Second, instantaneous evapo-transpirative losses from the unsaturated zone are assumed proportional to its volumetric water content. Under these conditions, pulses of deep infiltration from the unsaturated zone to the saturated zone (here designated as 'recharge events') themselves follow a stationary marked Poisson process with a lower event frequency than rainfall, but with identically distributed event depths¹⁸. Third, stream flow generation by the saturated subsurface is assumed proportional to the volume of stored water (with proportionality constant, or inverse mean hydraulic response time, k [T^{-1}]), implying an exponential decrease in stream flow through time between recharge events¹⁹. Lastly, the mean and variance of stream flow are dominated by base flow – the river discharge component associated with groundwater – at the considered (daily to monthly) time scales. Under these assumptions, the (squared) r ratio of catchments can be expressed as (see Methods):

$$r^2 = \frac{CV_Q}{CV_P} = \frac{f(\psi)}{\phi}, \quad (1)$$

where $f(\psi) = \frac{\psi - 1 + e^{-\psi}}{\psi} < 1$ is a strictly increasing function. Parameter $\phi \in [0, 1]$ represents the water yield, that is the proportion of the incoming rainfall that leaves the catchment as stream flow. Parameter $\psi \geq 0$ is the ratio between the observation time scale (e.g. monthly versus daily flows) and the mean hydraulic response time of the catchment (see Methods). Equation (1) allows isovalues of r to be mapped on the $\phi \times \psi$ plane (Figure 2a). Of particular interest is the isovalue line $r = 1$, which separates catchments that amplify (above the line on Figure 2a) or attenuate precipitation variability. The four assumptions that underpin Equation (1) are restrictive and likely fail to capture some of the processes that dominate flow generation in individual catchments. For example, the model is parametrized independently for each season, which allows it to capture seasonal changes in rainfall and temperature: a different water yield value is estimated for each season. However, carryover water storage between wet and dry seasons (both as soil moisture and groundwater) might violate the model's stationarity assumption²³. In addition, non-baseflow components of discharge may be non-negligible in many catchments, where the stream flow recession is better-approximated as a nonlinear power-law relationship, rather than the linear storage-discharge relationship assumed in Equation (1). However, these processes are unlikely dominant controls on stream flow variability at the daily to monthly time scales that we consider, as suggested by the numerical simulations presented in the Supplementary Discussion.

Applied to the 671×4 combinations of catchments and seasons of the dataset at daily, weekly, and monthly observation time scales, the model predicted observed values of r with a mean absolute percentage error (MAPE) of 49%. As expected, predictions are substantially better in small catchments that are well aligned with the lumped nature of the model, and in regions and seasons where dominant hydrologic processes are expected to align with the theoretical assumptions of the model (Figure 2c). For example, snow-dominated hydrology throughout the winter season in the Rocky Mountain region violates the assumption that catchment storage occurs in the subsurface and is proportional to discharge at the outlet. In many of the seasonally dry western regions, wet season onset during the Fall months of September, October, and November violate the assumption that rainfall statistics within a given season are stationary²³. In the summer months of the desert Southwest, monsoonal rainfall likely arrives in short, intense bursts that trigger overland flow²⁴, which is not strictly accounted for by the underlying runoff generation model¹⁹. Removing the 15% of catchments in region-seasons, where hydrology is likely dominated by snow (Fall and Winter in the Rockies, High Plains, Great Plains, Great Basin and Sierra Nevada) or overland flow

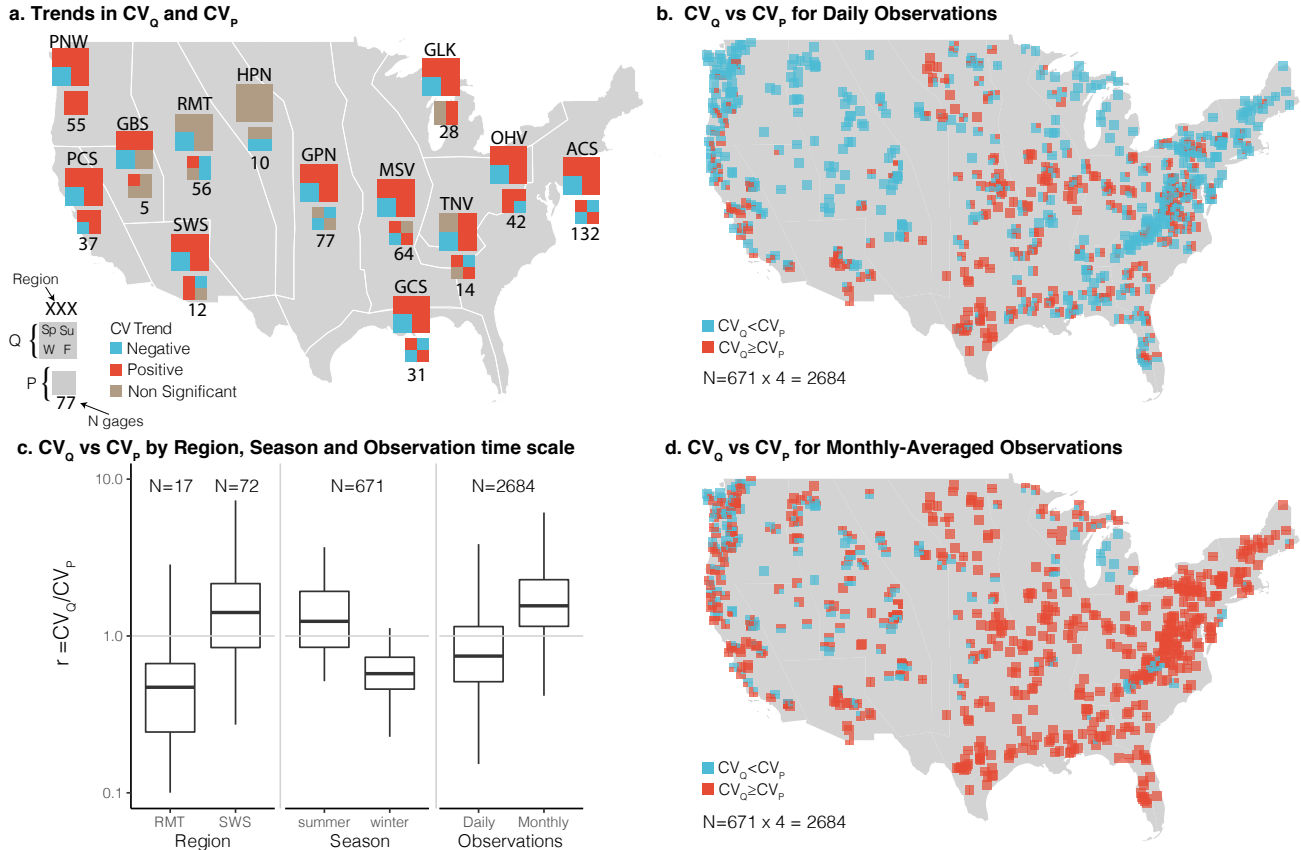


Figure 1. a. Changes in the coefficient of variation of daily streamflow (CV_Q , large symbols) and precipitation (CV_P , small symbols) by season (symbol quadrants) and region of the conterminous United States. Colors indicate statistically significant ($p < 0.05$) increases (red) or decreases (blue) between 1980 and 2015, as indicated by student t-tests on CV values computed over successive periods of 5 years for 563 of the 671 considered catchments with uninterrupted time series of observations (see Methods). Geographical Regions²² correspond to the Pacific Northwest (PNW), Pacific Coast (PCS), Great Basin (GBS), Southwest (SWS), Rockies (RMT), High Plains (HPN), Great Plains (GPN), Mississippi Valley (MSV), Great Lakes (GLK), Tennessee Valley (TNV), Gulf Coast (GCS), Ohio Valley (OHV) and Atlantic Coast (ACS). Numbers below the symbols indicate the number of catchments per region. **b.** Gage locations of the 671 catchments of the dataset²², with symbols split into seasonal quadrants. Colors indicate whether the CV of daily streamflow in the 1980–2015 period is larger (red) or smaller (blue) than rainfall. **c.** Ratio between CV_Q and CV_P for different regions (RMT vs. SWS, all seasons), seasons (summer vs. winter, all regions) and observation time scales (daily vs. monthly-averaged observations, all seasons and regions). **d.** Comparison between CV_Q and CV_P for monthly-averaged observations. The proportion of catchment-season combinations with $CV_Q > CV_P$ increased from 33% to 83%, compared to the equivalent map for daily observations in Panel b.

(Summer and Fall Monsoon in the Southwest) reduces the MAPE to 33%. Notably, despite its shortcomings in predicting the actual value of r in some catchments, the model predicted whether catchments amplify ($r > 1$) or attenuate ($r < 1$) rainfall with an accuracy above 80% for the full sample of catchments and seasons (Figure 2b).

These results suggest that the amplifying effect of catchments is ultimately determined by a competition between two fundamental processes captured by the model, precipitation partitioning and storage retention, which appear to transcend the complex and highly local nature of stream flow generating processes in individual catchments. On the one hand, the water yield ϕ quantifies how infiltrated precipitation is *partitioned* between river discharge and evapo-transpiration. If all other conditions remain the same, an increase in water yield increases the mean value of stream flow and therefore decreases its coefficient of variation and r ratio. On the other hand, the parameter ψ quantifies how non-evaporated water is *retained* between precipitation events and gradually released into the stream. Catchment retention affects stream flow variability differently for different observation time scales. If the observation time scale exceeds the average response time of the catchment ($\psi > 1$), the serial correlation introduced by catchment retention is ‘averaged out in the observed stream flow time series and will have little effect on r . In contrast, stream flow observations taken at a short enough time scale ($\psi < 1$) will capture the serial correlation introduced by catchment retention. These correlations attenuate the variance of stream flow and therefore decrease r .

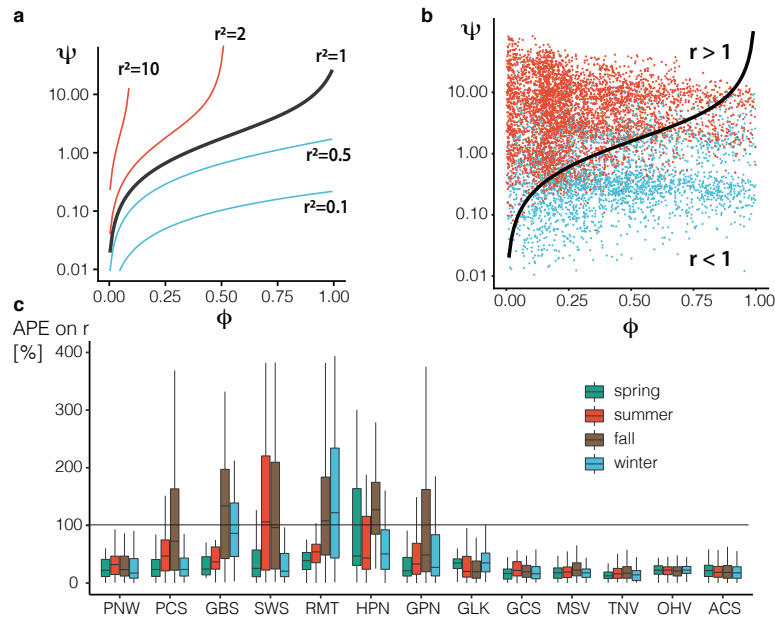


Figure 2. a. Theoretical (squared) r ratio as a function of the water yield ϕ and the ratio ψ between the observation time scale and the mean response time of the catchment. Partitioning (ϕ) and retention (ψ) processes interact non-linearly to determine the r ratio of catchments. **b.** Empirical validation of catchment types ($r > 1$ vs $r < 1$). Colored dots represent 671 catchments $\times$ 4 seasons $\times$ 3 observation time scales (1,7 and 30 days). Catchments with empirical r above (below) the unit are represented in red (blue) and are located above (below) the theoretical separation line with an accuracy above 80%. **c.** Absolute percentage error (APE) between observed and predicted r ratios by geographical region and season. The mean APE across all catchments, seasons and time scales (daily, weekly and monthly) is 49%, $N=8,004$. Removing 1,616 observations in regions and seasons dominated by snow (Fall and Winter in the Rockies, High Plains, Great Plains, Great Basin and Sierra Nevada) or desert monsoon (Summer and Fall in the Southwest) reduces the mean APE to 33%.

We turn to investigating whether catchments that amplify the variability of incoming precipitation also amplify *changes* in that variability. This may not be the case, for instance, if changing rainfall variability affects catchments’ ability to partition or retain water through changes in vegetation cover or snow pack. To estimate these effects, we use a linear regression framework, where the r ratio is taken to be a function of relative rainfall variability (CV_p) and time, and where CV_p is a function of time.

Taking the full time-derivative of the coefficient of variation of stream flow, CV_Q , then yields a linear function of $\frac{\partial CV_P}{\partial t}$ and CV_P :

$$\underbrace{\frac{dCV_Q}{dt}}_{\text{Total}} = \frac{d(r \cdot CV_P)}{dt} \quad (2)$$

$$= \underbrace{r \frac{\partial CV_P}{\partial t}}_{\text{Direct}} + \underbrace{\frac{\partial r}{\partial CV_P} \frac{\partial CV_P}{\partial t} CV_P}_{\text{Indirect}} + \underbrace{\frac{\partial r}{\partial t} CV_P + r \frac{\partial CV_P}{\partial r} \frac{\partial r}{\partial t}}_{\text{Exogenous}}$$

The first term of the derivative represents the direct (linear) response of the catchment to changing rainfall variability, as described by the ratio r . This term demonstrates that catchments that amplify rainfall variability may also amplify changes in rainfall variability. The second term represents the indirect (non linear) effect of changing rain regimes, where the r ratio is itself a function of rainfall variability. For example, more variable precipitation might affect vegetation cover in a way that decreases the proportion of rainfall lost to evapo-transpiration²⁵. This increase in water yield would lower the r ratio (per Equation 1), in which case $\partial r / \partial CV_P$ would be negative. The last terms represent the effects of an exogenous change in the r ratio that is not elicited by a change in rainfall variability. For example, warmer temperatures will cause less precipitation to fall as snow, which has been linked to lower water yields²⁰. This would increase r (per Equation 1) irrespective of changing precipitation variability, in which case $\frac{\partial r}{\partial t}$ would be positive. Such changes in catchment processes will directly influence streamflow variability (third term of Equation 2) but might also feed back to affect the variability of precipitation (last term of Equation 2), for instance by affecting precipitation recycling processes²⁶.

We use linear regressions to estimate the four terms of Equation 2 based on historical changes in rain and flow variability (see Methods). We focus on a subset of 563 catchments that have 35 years of continuous daily observations available, as shown in Supplementary Table S1. Regression results are shown in supplementary Table S2 and used to construct the graphs on Figure 3. Figure 3a shows a general historical increase in CV_Q ($p < 0.01$) for daily, weekly and monthly observations in all seasons, except winter when CV_Q decreased ($p < 0.01$). Changes in CV_Q appear dominated by exogenous changes in r (Figure 3a, red) and, to a lesser extent, by the direct effect of changes in CV_P (blue). The indirect effect of changes in CV_P (green) generally operates in the opposite direction to the two other components. This suggests that, on average across our dataset, catchments tend to ‘adapt’ their response to increasing rainfall variability so as to attenuate its overall effect on the variability of river flow – a negative feedback that has been associated with hydrologic resilience in past studies²⁷. Of note is that the indirect effect of CV_P on changes in CV_Q is also substantially smaller in magnitude than the direct effect. The ratio between the two effects is significantly smaller in absolute value than 0.55 ($p < 0.01$) for all seasons and observation time scales (dots on Figure 3b). It is important to keep in mind that the above results are based on regression estimates that represent *average* effects across catchments. Historical changes in CV_Q , and their underlying components, vary substantially across regions (Figure 1a) and individual catchments. A Monte Carlo analysis (see Methods) carried out to account for this variability revealed that the direct effect remains larger than the indirect effect for nearly all (>95%) simulations (box plots on Figure 3b). Together, these results suggest that catchments that currently amplify rainfall variability are also likely to amplify changes in rainfall variability.

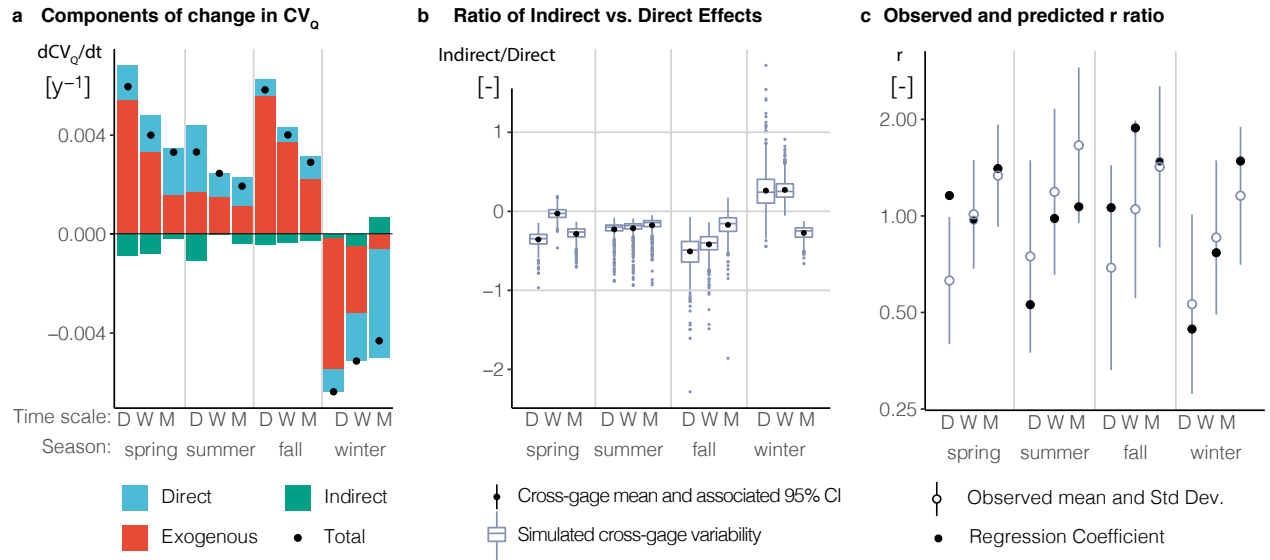


Figure 3. a. Components of changes in historical CV_Q . Dots represent the average annual change in CV_Q across all gages ($N=563$) by season and for daily (D), weekly (W) and monthly (M) observations. Colored bars represent the direct (blue) and indirect (green) contributions of changes in CV_P , and the contribution of exogenous changes in r (red) estimated through linear regression. **b.** Ratio between the indirect and direct effects of CV_P on historical changes in CV_Q . Dots indicate the ratios between $\alpha_{12} \cdot E[CV_P]$ and α_1 , where α_1 and α_{12} are linear regression coefficients (see methods) and $E[CV_P]$ is the observed CV_P averaged across gages. Bootstrapped 95% confidence intervals are smaller than symbol sizes so not displayed. Purple boxplots represent simulated variations across catchments: α_{12} and α_1 are drawn from independent normal distributions with mean and standard deviation given by the linear regression, and CV_P s are observed individually at each gage. The ratio between average indirect and direct effects is smaller than 0.55 for all seasons and time scales ($p < 0.01$). The direct effect is larger than the indirect effect for $>95\%$ of the simulations. **c.** Comparison between the regression coefficient α_2 (black) and empirically estimated r ratios (purple), see Methods. Most regression coefficient lie within one standard deviation (error bar) of the mean empirical observation of r (empty symbol).

Implications

River catchments filter incoming climate signals, and therefore determine the extent to which changing rain regimes ultimately translate into changing water availability for stream-dependent social and ecological systems. Whether a catchment amplifies or attenuates changes in rainfall variability emerges from the competition between two fundamental hydrologic functions – partitioning and retention – that are active in all watersheds. The universal nature of these drivers can facilitate the assessment of climate vulnerability in data-scarce basins, which is an enduring global challenge²⁸. The two parameters that describe this competition – water yield and the mean catchment response time – can be directly estimated if (even sparse) rainfall and stream flow records are available^{29,30}.

These findings have three important implications in the context of climate change. First, by decreasing the water yield (for instance by decreasing the fraction of precipitation falling as snow²⁰), increased temperatures will likely increase catchments' propensity to amplify the relative variability of incoming rainfall. The model associates any relative decrease in ϕ with an equivalent relative increase in r^2 , per the inverse proportional relation between ϕ and r^2 in Equation 1. This implies that, by affecting water yield, increasing temperatures will increase the coefficient of variation of stream flow, even if rainfall variability remains constant. Second, partitioning (ϕ) and retention (ψ) interact non-linearly to determine the r -ratio of the catchment. By capturing this relation, the model may be used to evaluate the effect of catchment alterations – land cover changes, for instance – on the amplification or attenuation of changing rainfall variability. For example, an increase in water yield from $\phi = 0.36$ to $\phi = 0.4$ (perhaps associated with deforestation³¹) will have a disproportionately large bearing on r^2 for catchments with short response times, where a large value of ψ maps to steep isovalues of r in the $\phi \times \psi$ plane on Figure 2a. Third, the theory elucidates the relation between observation time scales and catchments ability to filter incoming rainfall variability. A catchment that attenuates rainfall variability for short (e.g., daily) observation time scales will nonetheless amplify rainfall variability for sufficiently long (e.g., monthly) time scales. The appropriate time scale of observation is determined by the considered application. This implies that a given catchment can both attenuate changes in rainfall variability for some applications (e.g., fish habitat driven by daily variability), while amplifying it for others (e.g., agricultural yields driven by seasonal variability). Therefore, the application context, not only the underlying hydrologic processes, determines the vulnerability of watersheds to changing rain regimes³².

Methods

Data and pre-processing

Stream flow data were obtained from the Catchment Attributes and Meteorology for Large Sample Studies (CAMELS) dataset compiled by the United States Geological Survey²². We used precipitation data from the North America Land Data Assimilation data preprocessed to match the catchments of the CAMELS dataset²². The combined stream flow and precipitation dataset is publicly available at <https://ral.ucar.edu/solutions/products/camels> and provides daily rainfall and stream discharge observations from 671 gaged catchments with minimal human impact in the lower 48 US states between 1980 and 2015. Observations from 16 season-catchment combinations, most of them in winter, (Supplementary Table S1) were removed because we were unable to identify suitable recessions to determine k (see below), likely due to snow-dominated runoff processes. Separately, we removed 108 gauges from the regression analysis due to incomplete (interrupted) time series of observations (Table S1). Our sample sizes were therefore 2668 and 2252 catchment-season combinations for the validation and regression analyses, respectively. All data used in both analyses are freely available at <https://curate.nd.edu/show/bc386h47534>. As seen on Supplementary Figure S1, the dataset covers a very wide range of catchment sizes, topography, vegetation and hydroclimatic characteristics²².

Time series of daily precipitation and stream flow observations were split into four seasons according to their observation month: December to February, March to May, June to August and September to November, respectively for Winter, Spring, Summer and Fall. Moving average window of seven and thirty days were then applied to aggregate the 35 years of daily precipitation and stream flow time series into weekly ($T_0 = 7$) and monthly ($T_0 = 30$) observation time scales, respectively. The coefficient of variation (CV) of precipitation and stream flow, and their ratio r , was then computed using the aggregated time series. Note that $CV_Q [-]$ is unit-less and represents the CV of both specific (i.e. area-normalized) and total discharge. Water yields ϕ were then computed for each season and catchment by taking the ratio between total seasonal stream flow volume and total seasonal precipitation volume, both taken over the whole period of data observation. Lastly, the linear recession constant k was estimated by identifying suitable recessions (at least 4 consecutive days with a decreasing, concave-up hydrograph) to be fitted with non-linear least squares, as detailed in³³. The recession constant was used to compute $\psi = k \cdot T_0$ for each combination of catchments, seasons, and observational time scales.

We estimated temporal changes in CV_P and CV_Q by assuming that long-term precipitation and stream flow dynamics emerge from stationary processes that take place within multiple juxtaposed periods^{6,34}. The 35 years of continuous daily observations available for 563 catchments of the data-set (see Supplementary Table S1) were split into seven non-overlapping

periods of five years. To ensure that our results are not driven by the arbitrary period length, we reproduced our analyses using period lengths of two and 10 years (see Supplementary Figures S2 and S3). The coefficients of variation of precipitation and river flows were then computed for each period, catchment, season and (daily, weekly and monthly) observation time scales. Pairs of successive periods ($t - 1$ and t) were then combined to estimate temporal changes in stream flow and precipitation variability ($\Delta CV_Q^{(t)} = CV_Q^{(t)} - CV_Q^{(t-1)}$ and $\Delta CV_P^{(t)} = CV_P^{(t)} - CV_P^{(t-1)}$) along with the average level of rainfall variability ($\overline{CV_P^{(t)}} = 0.5CV_P^{(t)} + 0.5CV_P^{(t-1)}$) across the pair.

Hydrological Model

The model assumes that precipitation is a marked Poisson process, with frequency λ_P [T^{-1}] and exponentially distributed event volumes with (area-normalized) mean α_P [L]¹⁷. Due to the assumed independence of rain events, the coefficient of variation (CV) of total rain volume, aggregated over T_0 days, is $CV_P = \sqrt{2/(T_0\lambda_P)}$ (see Supplementary Discussion for derivation details). All incoming water is assumed to infiltrate into a subsurface unsaturated zone, meaning that canopy interception processes are embedded in α_P .

Once infiltrated, water exits the unsaturated zone layer, either via evapo-transpiration (at a rate assumed proportional to current unsaturated zone water content¹⁸) or via percolation into the saturated zone. Such runoff generating recharge events are created when a contemporaneous rain event causes unsaturated zone moisture content to exceed an effective field-capacity, where water freely drains to the saturated zone. Under the above assumptions about the rainfall process and drainage from the unsaturated zone, it can be shown that the probability distribution of depths of recharge events is approximately equal¹⁹ to the probability distribution of rainfall depths (i.e., both distributions are exponential with mean α_P). Climate processes and water storage dynamics in the unsaturated zone therefore jointly determine the water delivered to the saturated zone, which generates discharge in the stream as water tables lower between recharge events. These recharge events can be described as a marked Poisson process with a censored frequency $\lambda < \lambda_P$. The censoring ratio ϕ provides a simple measure for quantifying the fraction of total rainfall that exits the catchment as stream flow over the long term²⁹, also known as the water yield:

$$\phi = \frac{\lambda}{\lambda_P} = \frac{\mu_Q}{\mu_P} \in [0, 1] \quad (3)$$

where μ_P and μ_Q are the long-term mean precipitated and discharged water volumes. Note that the above expression neglects contributions to total stream flow volume that are not associated with discharge generated by a subsurface saturated zone. This explains the relatively poorer performance of the model in catchments (e.g., SWS in summer, Figure 2c) where overland flow is likely substantial.

Discharge at the catchment outlet is assumed proportional to storage within the saturated zone, with a proportionality constant k [T^{-1}], implying an exponential flow recession between rainfall events with characteristic drainage timescale k^{-1} [T]. In contrast to the rainfall and recharge events, the stream flow time series is serially correlated due to retention and slow release of storage at a rate dependent on the hydraulic response time of the catchment k^{-1} ³⁵. This process affects the variance of stream flow as follows (see Supplementary Discussion for derivation details):

$$\sigma_Q^2 = 2\lambda\alpha_P^2k^{-1} \left(kT_0 - 1 + e^{-kT_0} \right) \quad (4)$$

Expressing mean cumulative stream flow over a period T_0 as $T_0\lambda\alpha_P$ leads to an expression for the coefficient of variation of stream flow (CV_Q) and the (squared) r ratio:

$$r^2 = \frac{CV_Q^2}{CV_P^2} = \frac{\lambda_P}{\lambda} \cdot \frac{kT_0 - 1 + e^{-kT_0}}{kT_0} = \frac{f(\psi)}{\phi} \quad (5)$$

where $\psi = kT_0 > 0$ is the ratio between the observation time scale (T_0) and the mean response time of the catchment (k^{-1}). The function $f(\psi) = \frac{\psi - 1 + e^{-\psi}}{\psi} < 1$ is strictly increasing and represents the serial correlation introduced by retention, and its attenuating effect on streamflow variability.

The model was validated by computing the absolute percentage error between the r^2 ratio predicted using Equation 5 based on estimated k and ϕ , and the $\hat{r}^2$ ratio obtained from empirical estimations of CV_Q and CV_P :

$$APE = 100 \times \frac{|r^2 - \hat{r}^2|}{\hat{r}^2}$$

We also evaluate the model based on the frequency of correct predictions of $r < 1$.

Regression analysis

We used linear regressions to analyse temporal changes in CV_Q and CV_P . We first determined whether differences in CV between subsequent periods were significantly different from zero by conducting student-t tests on ΔCV_Q and ΔCV_P for each season and geographical region (Figure 1a), with standard errors clustered by catchment³⁶.

To relate changes in CV_Q to changes in CV_P , Equation 2 is expressed as the following linear regression:

$$\underbrace{\Delta CV_Q}_{\text{Total}} = \underbrace{\alpha_0 + \alpha_1 \overline{CV_P}}_{\text{Exogenous}} + \underbrace{\alpha_2 \cdot \Delta CV_P}_{\text{Direct}} + \underbrace{\alpha_{12} \cdot \Delta CV_P \cdot \overline{CV_P}}_{\text{Indirect}} + \varepsilon. \quad (6)$$

where ε is a random error term assumed to have a mean value of zero and be independent across catchments. Variables ΔCV_Q , ΔCV_P and $\overline{CV_P}$ are obtained from CV_Q and CV_P estimated for successive 5-year periods of the observation record as described above. Assuming that these estimates are discrete approximations of the corresponding terms in Equation 2, regression coefficients can be interpreted as the exogenous ($\alpha_1 \equiv \partial r / \partial t$ and $\alpha_0 \equiv r \cdot \partial CV_P / \partial r \cdot \partial r / \partial t$), direct ($\alpha_2 \equiv r$) and indirect ($\alpha_{12} \equiv \partial r / \partial CV_P$) components of $\frac{\partial CV_Q}{\partial t}$. Regression coefficients were estimated for each season and observation time scale using ordinary least squares, with standard errors clustered by catchment³⁶.

Plugging regression estimates back into Equation 6 and omitting random errors allowed us to plot the average contributions of the direct, indirect and exogenous effects on the average temporal change in CV_Q across catchments, for each season and considered time scale (Figure 3a). The relative importance of the direct and indirect effects was estimated by taking the ratio between the corresponding terms of Equations 6 (Figure 3b, dots). The variability of this ratio across catchments was estimated through numerical simulations by (i) sampling $\overline{CV_P}$ from the set of 563 catchment-averaged observations; (ii) sampling α_2 and α_{12} from independent normal distributions with mean and standard deviations given by the relevant regression estimates; and (iii) computing the ratio of indirect vs. direct effects as $\overline{CV_P} \frac{\alpha_{12}}{\alpha_2}$. Box plots on Figure 3b represent the distribution of that ratio obtained from 1000 Monte Carlo repetitions.

We carried out two robustness checks to build confidence in our regression results. First, the analysis implies that the regression coefficient α_2 can be interpreted as the average value of r across all catchments, as seen by comparing Equations 2 and 6. Figure 3c compares regression coefficient α_2 (black) with r ratios obtained empirically from period-of-record stream flow and precipitation observations at each catchment (purple): α_0 remains within one standard deviation (error bar) of the mean empirical value of r (empty symbols) for nearly all seasons and time scales. Second, we replicated the analysis using changes in CV_Q and CV_P estimated over different periods lengths. Periods longer (10 years) or shorter (2 years) than the preferred duration (5 years) lead to increases in both the uncertainty of regression estimates and in errors on $r \equiv \alpha_2$ (Supplementary Figure S3). However, the mean contributions of the direct, indirect and exogenous effects and the spatial distribution of historical trends remain similar to those presented for periods of 5 years (Supplementary Figures S2 and S3). We interpret the errors and uncertainties for longer and shorter periods as likely caused by sample size limitations. Namely, there appears to be a tradeoff on the duration of periods between (i) having enough observations within each period to accurately estimate CV_P and CV_Q at daily to monthly time scales and (ii) having enough periods represented to implement the linear regression analysis over a large enough sample size. The sensitivity analysis in Supplementary Figure S3 points to the chosen period length of 5 years as optimal in regards to that tradeoff.

References

1. Fabris, L., Lazzaro, G., Buddendorf, W. B., Botter, G. & Soulsby, C. A general analytical approach for assessing the effects of hydroclimatic variability on fish habitat. *J. Hydrol.* **566**, 520–530 (2018).
2. Vogel, R. M. & Bolognese, R. A. Storage-reliability-resilience-yield relations for over-year water supply systems. *Water Resour. Res.* **31**, 645–654 (1995).
3. Marengo, J. A. *et al.* Recent extremes of drought and flooding in amazonia: vulnerabilities and human adaptation. (2013).
4. Brown, C. & Lall, U. Water and economic development: The role of variability and a framework for resilience. In *Natural resources forum*, vol. 30, 306–317 (Wiley Online Library, 2006).
5. Roche, K. R., Müller-Itten, M., Dralle, D. N., Bolster, D. & Müller, M. F. Climate change and the opportunity cost of conflict. *Proc. Natl. Acad. Sci.* (2020).
6. Botter, G., Basso, S., Rodriguez-Iturbe, I. & Rinaldo, A. Resilience of river flow regimes. *Proc. Natl. Acad. Sci.* **110**, 12925–12930 (2013).
7. Teutschbein, C., Grabs, T., Laudon, H., Karlsen, R. H. & Bishop, K. Simulating streamflow in ungauged basins under a changing climate: The importance of landscape characteristics. *J. Hydrol.* **561**, 160–178 (2018).

8. Chezick, K., Anderson, S. & Moore, J. River networks dampen long-term hydrological signals of climate change. *Geophys. Res. Lett.* **44**, 7256–7264 (2017).
9. Guswa, A. J., Hamel, P. & Dennedy-Frank, P. J. Potential effects of landscape change on water supplies in the presence of reservoir storage: LANDSCAPE EFFECTS ON WATER SUPPLIES. *Water Resour. Res.* **53**, 2679–2692, DOI: [10.1002/2016WR019691](https://doi.org/10.1002/2016WR019691) (2017).
10. Porder, S. Coevolution of life and landscapes. *Proc. Natl. Acad. Sci.* **111**, 3207–3208 (2014).
11. Sivapalan, M. Pattern, process and function: elements of a unified theory of hydrology at the catchment scale. *Encycl. hydrological sciences* (2006).
12. Fan, Y. *et al.* Hillslope hydrology in global change research and earth system modeling. *Water Resour. Res.* **55**, 1737–1772 (2019).
13. Troch, P. A. *et al.* Catchment coevolution: A useful framework for improving predictions of hydrological change? *Water Resour. Res.* **51**, 4903–4922, DOI: [10.1002/2015WR017032](https://doi.org/10.1002/2015WR017032) (2015).
14. Dietrich, W. E. & Perron, J. T. The search for a topographic signature of life. *Nature* **439**, 411–418 (2006).
15. Donat, M. G., Lowry, A. L., Alexander, L. V., O’Gorman, P. A. & Maher, N. More extreme precipitation in the world’s dry and wet regions. *Nat. Clim. Chang.* **6**, 508–513 (2016).
16. Pendergrass, A. G., Knutti, R., Lehner, F., Deser, C. & Sanderson, B. M. Precipitation variability increases in a warmer climate. *Sci. reports* **7**, 1–9 (2017).
17. Rodriguez-Iturbe, I., Porporato, A., Ridolfi, L., Isham, V. & Cox, D. Probabilistic modelling of water balance at a point: the role of climate, soil and vegetation. In *Proceedings of the Royal Society of London A: Mathematical, Physical and Engineering Sciences*, vol. 455, 3789–3805 (The Royal Society, 1999).
18. Porporato, A., Daly, E. & Rodriguez-Iturbe, I. Soil water balance and ecosystem response to climate change. *The Am. Nat.* **164**, 625–632 (2004).
19. Botter, G., Porporato, A., Rodriguez-Iturbe, I. & Rinaldo, A. Basin-scale soil moisture dynamics and the probabilistic characterization of carrier hydrologic flows: Slow, leaching-prone components of the hydrologic response. *Water resources research* **43** (2007).
20. Berghuijs, W., Woods, R. & Hrachowitz, M. A precipitation shift from snow towards rain leads to a decrease in streamflow. *Nat. Clim. Chang.* **4**, 583–586 (2014).
21. Berghuijs, W. R., Sivapalan, M., Woods, R. A. & Savenije, H. H. Patterns of similarity of seasonal water balances: A window into streamflow variability over a range of time scales. *Water Resour. Res.* **50**, 5638–5661 (2014).
22. Addor, N., Newman, A. J., Mizukami, N. & Clark, M. P. The camels data set: catchment attributes and meteorology for large-sample studies. *Hydrol. Earth Syst. Sci. (HESS)* **21**, 5293–5313 (2017).
23. Müller, M. F., Dralle, D. N. & Thompson, S. E. Analytical model for flow duration curves in seasonally dry climates. *Water Resour. Res.* **50**, 5510–5531 (2014).
24. Howes, D. A. & Abrahams, A. D. Modeling runoff and runoff in a desert shrubland ecosystem, Jornada Basin, New Mexico. *Geomorphology* **53**, 45–73, DOI: [10.1016/S0169-555X\(02\)00347-1](https://doi.org/10.1016/S0169-555X(02)00347-1) (2003).
25. Feng, X., Porporato, A. & Rodriguez-Iturbe, I. Stochastic soil water balance under seasonal climates. *Proc. Royal Soc. A: Math. Phys. Eng. Sci.* **471**, 20140623 (2015).
26. Spera, S. A., Galford, G. L., Coe, M. T., Macedo, M. N. & Mustard, J. F. Land-use change affects water recycling in Brazil’s last agricultural frontier. *Glob. change biology* **22**, 3405–3413 (2016).
27. Harder, P., Pomeroy, J. W. & Westbrook, C. J. Hydrological resilience of a Canadian Rockies headwaters basin subject to changing climate, extreme weather, and forest management. *Hydrol. Process.* **29**, 3905–3924 (2015).
28. Blöschl, G. *et al.* Twenty-three unsolved problems in hydrology (uph)—a community perspective. *Hydrol. Sci. J.* **64**, 1141–1158 (2019).
29. Doulatyari, B. *et al.* Predicting streamflow distributions and flow duration curves from landscape and climate. *Adv. water resources* **83**, 285–298 (2015).
30. Müller, M. & Thompson, S. Topreml: a topological restricted maximum likelihood approach to regionalize trended runoff signatures in stream networks. *Hydrol. Earth Syst. Sci.* **19**, 2925–2942 (2015).

31. Levy, M., Lopes, A., Cohn, A., Larsen, L. & Thompson, S. Land use change increases streamflow across the arc of deforestation in brazil. *Geophys. Res. Lett.* **45**, 3520–3530 (2018).
32. Müller, M. & Thompson, S. A value-based model selection approach for environmental random variables. *Water Resour. Res.* **55**, 270–283 (2019).
33. Dralle, D. N., Karst, N. J., Charalampous, K., Veenstra, A. & Thompson, S. E. Event-scale power law recession analysis: quantifying methodological uncertainty. *Hydrol. Earth Syst. Sci.* **21**, 65 (2017).
34. Porporato, A., Vico, G. & Fay, P. A. Superstatistics of hydro-climatic fluctuations and interannual ecosystem productivity. *Geophys. Res. Lett.* **33** (2006).
35. Dralle, D., Karst, N., Müller, M., Vico, G. & Thompson, S. E. Stochastic modelling of inter-annual variation of hydrologic variables. *Geophys. Res. Lett.* (2017).
36. Williams, R. L. A note on robust variance estimation for cluster-correlated data. *Biometrics* **56**, 645–646 (2000).

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Author contributions statement

M.F.M, K.R.R and D.N.D designed and performed the research. M.F.M wrote the paper.

Additional information

Competing interests Authors declare no conflict of interest.