## Moment Tensors of Ring-Faulting at Active Volcanoes: Insights into Vertical-CLVD Earthquakes at the Sierra Negra Caldera, Galápagos Islands

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#### Abstract

Moderate earthquakes (Mw > 5) with moment tensors (MTs) dominated by a vertical compensated-linear-vector-dipole (vertical-CLVD) component are often generated by dip slip along a curved ring-fault system at active volcanoes. However, relating their MTs to ring-fault parameters has been proved difficult. The objective of this study is to find a robust way of estimating some ring-fault parameters based on their MT solutions obtained from long-period seismic records. We first model the MTs of idealized ring-faulting and show that MT components representing the vertical-CLVD and vertical strike-slip mechanisms are resolvable by the deviatoric MT inversion using long-period seismic waves, whereas a component representing the vertical dip-slip mechanism is indeterminate owing to a shallow source depth. We then propose a new method for estimating the arc angle and orientation of ring-faulting using the two resolvable MT components. For validation, we study a vertical-CLVD earthquake that occurred during the 2005 volcanic activity at the Sierra Negra caldera, Galápagos Islands. The resolvable MT components are stably determined with long-period seismic waves, and our estimation of the ring-fault parameters is consistent with the ring-fault geometry identified by previous geodetic studies and field surveys. We also estimate ring-fault parameters of two earthquakes that took place during the 2018 activity at the caldera, revealing significant differences between the two earthquakes in terms of slip direction and location. These results show the usefulness of our method for estimating ring-fault globally.

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| 12 | Key points:  |
| 13 | • Dip slip along curved ring faults at volcanoes generates $M_w > 5$ earthquakes dominated by a  |
| 14 | compensated-linear-vector-dipole component.  |
| 15 | • We propose a method for estimating ring-fault parameters by moment tensor inversion using long-period  |

16 seismic data.

- Our estimation of ring-fault parameters of earthquakes at the Sierra Negra caldera yields results consistent
- 18 with geodetic observations.

#### 19 Abstract

20 Moderate earthquakes  $(M_w > 5)$  with moment tensors (MTs) dominated by a vertical 21 compensated-linear-vector-dipole (vertical-CLVD) component are often generated by dip slip along a 22 curved ring-fault system at active volcanoes. However, relating their MTs to ring-fault parameters has been 23 proved difficult. The objective of this study is to find a robust way of estimating some ring-fault parameters 24 based on their MT solutions obtained from long-period seismic records. We first model the MTs of 25 idealized ring-faulting and show that MT components representing the vertical-CLVD and vertical 26 strike-slip mechanisms are resolvable by the deviatoric MT inversion using long-period seismic waves, 27 whereas a component representing the vertical dip-slip mechanism is indeterminate owing to a shallow 28 source depth. We then propose a new method for estimating the arc angle and orientation of ring-faulting 29 using the two resolvable MT components. For validation, we study a vertical-CLVD earthquake that 30 occurred during the 2005 volcanic activity at the Sierra Negra caldera, Galápagos Islands. The resolvable 31 MT components are stably determined with long-period seismic waves, and our estimation of the ring-fault 32 parameters is consistent with the ring-fault geometry identified by previous geodetic studies and field 33 surveys. We also estimate ring-fault parameters of two earthquakes that took place during the 2018 activity 34 at the caldera, revealing significant differences between the two earthquakes in terms of slip direction and 35 location. These results show the usefulness of our method for estimating ring-fault parameters, enabling us 36 to examine the kinematics and structures below active volcanoes with ring faults that are distributed 37 globally.

## **1 Introduction**

| 39 | Seismological methods can be used for the study of active volcanoes to investigate geometries of             |
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| 40 | subsurface structures and the physics of fluid transport into the magma plumbing system. Observations and    |
| 41 | analyses of shallow earthquakes with volcanic origins provide information on stress levels in volcanic       |
| 42 | edifices caused by magmatic pressures ascending from depth. This information is important for predicting     |
| 43 | eruptions and assessing hazards related to volcanic activity (e.g., McNutt, 2002; Chouet, 2003; Kawakatsu    |
| 44 | and Yamamoto, 2015). In most cases, small earthquakes are analyzed with in situ or near-field observations   |
| 45 | to infer detailed dynamics of magma transport or brittle fractures of volcanoes; for example, Kilauea in     |
| 46 | Hawaii (e.g., Neal et al., 2019; Shelly and Thelen, 2019) or Bárdarbunga in Iceland (e.g., Gudmundsson et    |
| 47 | al., 2016; Parks et al., 2017). In contrast, moderate volcanic earthquakes are sometimes recorded by         |
| 48 | regional and global seismic networks (e.g., Kanamori and Given, 1982; Kanamori et al., 1984; Kanamori        |
| 49 | and Mori, 1992; Ekström, 1994; Shuler et al., 2013a). If seismic signals radiated by such earthquakes can be |
| 50 | utilized, it is possible to study volcanoes distributed globally, including those on remote islands or       |
| 51 | underwater without local observation systems. These include submarine volcanoes near Torishima Island,       |
| 52 | south of Japan (e.g., Kanamori et al., 1993; Fukao et al., 2018; Sandanbata et al., 2018), and near Curtis   |
| 53 | Island, north of New Zealand (Gusman et al., 2020), which caused earthquakes with seismic magnitudes of      |
| 54 | > 5, and submarine volcanic areas near Mayotte Island in the Comoro Islands, which showed significant        |
| 55 | seismicity during 2018–2019 (Cesca et al., 2020; Darnet et al., 2020).                                       |

| 56 | One of the most notable types of volcanic earthquake observed at regional or global scales are those            |
|----|---|
| 57 | with seismic magnitudes of $M_w > 5$ that are characterized by deviatoric moment tensors (MTs) having a         |
| 58 | dominant vertical compensated-linear-vector-dipole (vertical-CLVD) component (e.g., Frohlich, 1994;             |
| 59 | Kanamori et al., 1993; Ekström, 1994; Shuler et al., 2013a; 2013b). There are two types of vertical-CLVD        |
| 60 | earthquake: one contains a dominant tension axis (vertical-T CLVD earthquakes), and the other contains a        |
| 61 | dominant pressure axis (vertical-P CLVD earthquakes) (e.g., Ekström, 1994; Shuler et al., 2013a) (Figure 1).    |
| 62 | Vertical-CLVD earthquakes cannot be explained by shear rupture on a planar fault, indicating that their         |
| 63 | anomalous mechanisms are associated with complex source structures or magmatic processes. For                   |
| 64 | vertical-CLVD earthquakes at volcanoes, several models have been proposed, including ring-faulting (e.g.,       |
| 65 | Ekström, 1994), rapid water-magma interaction initiated by magma intrusion into shallow crust (Kanamori         |
| 66 | et al., 1993), and opening or closing of a horizontal crack (e.g., Riel et al., 2015; Fukao et al., 2018).      |
| 67 | Among the different proposed source models, the ring-faulting mechanism explains many features                  |
| 68 | of vertical-CLVD earthquakes (e.g., Ekström, 1994; Shuler et al., 2013a; 2013b). Ekström (1994) showed          |
| 69 | that deviatoric MT analyses of long-period seismic signals radiated by pure dip slips on a curved ring fault    |
| 70 | result in vertical-CLVD focal mechanisms. Shuler et al. (2013a, 2013b) surveyed vertical-CLVD                   |
| 71 | earthquakes near volcanoes from 1976 to 2009 and located their centroids within the top 10 km of the crust,     |
| 72 | which is consistent with the formation process of ring faults during caldera collapse (e.g., Cole et al., 2005; |
| 73 | Acocella, 2007; Geyer and Martí, 2014). Shuler et al. (2013a) showed that most vertical-CLVD earthquakes        |
| 74 | were temporally associated with activity at nearby volcanoes with caldera structures. Vertical-CLVD             |

| 75 | earthquakes near Bárdarbunga in Iceland and Nyragongo in the Democratic Republic of the Congo have             |
|----|--|
| 76 | also been attributed to slips on non-planar ring faults (e.g., Gudmundsson et al., 2016; Parks et al., 2017;   |
| 77 | Nettles and Ekström, 1998; Shuler and Ekström, 2009). The recurrence of vertical-CLVD earthquakes at           |
| 78 | two shield volcanoes showing pronounced surface deformation or micro-seismicity along well-documented          |
| 79 | ring-fault structures has indicted their origins related to ring-faulting at the Rabaul caldera in Papua New   |
| 80 | Guinea (e.g., McKee et al., 1984; Mori and McKee, 1987; Mori et al., 1989; Shuler et al., 2013b) and the       |
| 81 | Sierra Negra caldera in the Galápagos Islands (e.g., Amelung et al., 2000; Yun et al., 2006; Yun, 2007;        |
| 82 | Jónsson, 2009; Bell et al., 2021).   |
| 83 | MT inversion using long-period seismic waves has been applied to study the sources of                          |
| 84 | vertical-CLVD earthquakes from far-field observations (e.g., Shuler et al., 2013b; Duputel and Rivera,         |
| 85 | 2019; Fontaine et al., 2019). Because of long-period properties, detailed 3D velocity structures of the        |
| 86 | volcanic edifices are not required. MT solutions of ring-faulting are known to reflect the properties of       |
| 87 | earthquake sources, such as the kinematics of a central block and the dip directions of a ring fault (Ekström, |
| 88 | 1994). When the central block moves upward on the inward-dipping ring fault (Figure 1a), or downward on        |
| 89 | the outward-dipping ring fault (Figure 1b), vertical-T CLVD earthquakes are produced; in contrast, if the      |
| 90 | kinematics of the block are reversed, vertical-P CLVD earthquakes are produced (Figure 1c and d). Hence,       |
| 91 | the polarity of the MT solutions (vertical-T or -P) helps to determine either the kinematics of the central    |
| 92 | block (upward or downward) or the dip direction of the ring fault (inward or downward), once either of the     |
| 93 | two is constrained from other observations such as crustal deformation or micro-seismicity (e.g., Shuler and   |

94 Ekström, 2009; Gudmundsson et al., 2016).

| 95  | However, it has been proved challenging to relate MT solutions obtained from long-period seismic              |
|-----|---|
| 96  | waves directly to ring-fault parameters such as arc angle, dip angle, and the location of slip along the ring |
| 97  | fault. One of the reasons for the difficulty is that amplitudes of radiated long-period seismic waves are     |
| 98  | reduced owing to partial cancellations of long-period seismic waves from different portions of a ring fault   |
| 99  | (Ekström, 1994). Another reason is the instability of MT inversion for shallow earthquakes (e.g.,             |
| 100 | Dziewonski et al., 1981; Kanamori and Given, 1981). Although Shuler et al. (2013b) related MT solutions       |
| 101 | obtained from long-period seismic records to ring-fault parameters using the plunge of the tension or         |
| 102 | pressure axis and a parameter representing the dominance of the non-double-couple component, their            |
| 103 | estimations were not always consistent with those observed in nature or in analog models.                     |
| 104 | Contreras-Arratia and Neuberg (2020) showed that detailed ring-fault parameters can be recovered from         |
| 105 | near-field seismic stations with good azimuth coverage. Once reliable relationships between ring-fault        |
| 106 | parameters and MT solutions obtained from long-period seismic records are established, MT inversion will      |
| 107 | be a more powerful tool to remotely study the kinematics and subsurface structures of active volcanoes        |
| 108 | distributed globally that cause ring-faulting.  |

109 The objective of this study is to find a robust way of estimating ring-fault parameters using the MT 110 solutions of vertical-CLVD earthquakes. We first model theoretical MTs of idealized ring-faulting with 111 variable ring-fault parameters and decompose them into MT components. Although the MT component

| 112 | representing the vertical dip-slip mechanism is difficult to determine with long-period seismic waves, we                        |
|-----|--|
| 113 | show that the remaining MT components can be used to estimate some ring-fault parameters. To validate                            |
| 114 | the theoretical argument, we estimate the ring-fault parameters of vertical-CLVD earthquakes at the Sierra                       |
| 115 | Negra caldera by investigating their resolvable components of MT solutions determined with long-period                           |
| 116 | seismic waves and then compare the estimated parameters with those identified in previous studies using                          |
| 117 | geodetic observations and field surveys. We also discuss possible bias in MT inversion caused by a seismic                       |
| 118 | source with a volume change close to the ring-faulting.  |
| 119 | 2 Analysis   |
| 120 | 2.1 Modeling and decomposition of moment tensors of ring-faulting  |
| 121 | In this section, we theoretically explore robust relationships between MTs and ring-fault parameters.                            |
| 122 | We consider ring-faulting along a uniformly inward-dipping fault system that traces the circumference of a                       |
| 123 | circle. We define several ring-fault parameters as follows (Figure 2). The ring-faulting has a dip angle $\delta$                |
| 124 | that is constant along the fault system. The arc angle $\theta$ is the central angle that measures the ruptured                  |
| 125 | segment along the circumference. The ring-fault azimuth is defined by the azimuth (from the north) of the                        |
| 126 | vector $\overrightarrow{OM}$ , where O is the center of the circle and M is the midpoint of the ruptured segment. The ring-fault |
| 127 | azimuth indicates the ring fault's location along the circumference. The ring-fault orientation is the                           |
| 128 | geometrical orientation, measured clockwise from the north, of the tangent to the circle at $M$ , and is normal                  |
| 129 | to $\overrightarrow{OM}$ . The ring-fault azimuth can vary from 0° to 360°, whereas the ring-fault orientation can vary only     |

130 from  $0^{\circ}$  to  $180^{\circ}$ .

| 131 | Here we consider idealized ring-faulting for a vertical-T CLVD mechanism: a pure reverse slip of 1                  |
|-----|---|
| 132 | m along a circular inward-dipping ring fault (5 km radius at the surface) that extends from the surface to a        |
| 133 | depth of 2 km. We model the theoretical MT of ring-faulting in a similar way to Ekström (1994) and Shuler           |
| 134 | et al. (2013b); we discretize the ring fault into planar rhomboidal subfaults with a central angle of 1° for        |
| 135 | each, compute the MT of each subfault (Box 4.4 in Aki and Richards, 2002), and sum up the MTs of the                |
| 136 | subfaults. A ring fault is smaller than the wavelength, and the typical source time duration of vertical-CLVD       |
| 137 | earthquakes is ~10 s (Shuler et al., 2013b), which is shorter than the wave period of the long-period seismic       |
| 138 | waves that we use; hence, we can ignore the rupture propagation along the ring fault and assume the                 |
| 139 | point-source approximation. While fixing the ring-fault azimuth as 0° (i.e., the midpoint on the north), we         |
| 140 | vary two ring-fault parameters, that is, the dip angle $\delta$ ranging from 45° to 90°, and the arc angle $\theta$ |
| 141 | ranging from 0° to 360°. Only vertical-T earthquakes are discussed here because MTs of vertical-P                   |
| 142 | earthquakes can be examined by changing the signs of the MTs.   |

143 The scalar moment of the theoretical MTs is computed by following the definition given by Silver144 and Jordan (1982) and Dahlen and Tromp (1998):

145 
$$M_0 = \sqrt{\Sigma_{ij} M_{ij} M_{ij}/2},$$
 (1)

146 where  $M_{ij}$  are the *ij* elements of an MT in spherical coordinates (r,  $\theta$ , and  $\phi$ ) representing up, south, and 147 east, respectively. The moment magnitude is computed as:

148 
$$M_w = \frac{2}{3} (\log_{10} M_0 - 9.10).$$
 (2)

149 with  $M_0$  being measured in N m (e.g., Kanamori, 1977; Hanks and Kanamori, 1979).

We next decompose the theoretical MTs in a similar way to Kawakatsu (1996). For the decomposition, we define three moment scales corresponding to isotropic (*ISO*), vertical-CLVD (*CLVD*), and difference (*D*) components with the three diagonal elements ( $M_{rr}$ ,  $M_{\theta\theta}$ , and  $M_{\phi\phi}$ ):

153 
$$M_{ISO} = \frac{1}{3} \left( M_{rr} + M_{\theta\theta} + M_{\phi\phi} \right), \qquad (3)$$

154 
$$M_{CLVD} = \frac{1}{3} \left( 2M_{rr} - M_{\theta\theta} - M_{\phi\phi} \right), \qquad (4)$$

155 and

156 
$$M_D = \frac{1}{2} \left( M_{\theta\theta} - M_{\phi\phi} \right). \tag{5}$$

Note that the MT of ring-faulting contains no isotropic component ( $M_{ISO} = 0$ ). Hence, using the two moment scales ( $M_{CLVD}$  and  $M_D$ ) and the non-diagonal elements ( $M_{r\theta}$ ,  $M_{r\phi}$ , and  $M_{\theta\phi}$ ), the MT of ring-faulting can be uniquely decomposed into three deviatoric MT components in the following form:

$$M = M_{CLVD} + M_{SS} + M_{DS}, \quad (6)$$

161 where

162 
$$\boldsymbol{M}_{CLVD} = \boldsymbol{M}_{CLVD} \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix},$$
(7)

163 
$$\boldsymbol{M}_{SS} = \boldsymbol{M}_{D} + \boldsymbol{M}_{\theta\phi} = \boldsymbol{M}_{D} \begin{bmatrix} 0 & & \\ 0 & 1 & \\ 0 & 0 & -1 \end{bmatrix} + \boldsymbol{M}_{\theta\phi} \begin{bmatrix} 0 & & \\ 0 & 0 & \\ 0 & 1 & 0 \end{bmatrix},$$
(8)

164 and

165 
$$\boldsymbol{M}_{DS} = \boldsymbol{M}_{r\theta} + \boldsymbol{M}_{r\phi} = M_{r\theta} \begin{bmatrix} 0 & & \\ 1 & 0 & \\ 0 & 0 & 0 \end{bmatrix} + M_{r\phi} \begin{bmatrix} 0 & & \\ 0 & 0 & \\ 1 & 0 & 0 \end{bmatrix}.$$
(9)

166 Note that the moment scales (Equations 3–5) are scalars, whereas the MT components (Equations 7–9) are
167 tensors.

The three MT components  $M_{CLVD}$ ,  $M_{SS}$ , and  $M_{DS}$  represent different source types, i.e., the vertical-CLVD (*CLVD*), vertical strike-slip (*SS*), and vertical dip-slip (*DS*) mechanisms, respectively (Figure 2b). The sign of  $M_{CLVD}$  in Equation (7) depends on the type of vertical-CLVD earthquake:  $M_{CLVD} > 0$  for vertical-T earthquakes, and  $M_{CLVD} < 0$  for vertical-P earthquakes.

172 Using absolute values defined by 
$$|M_{CLVD}|$$
,  $M_{SS} = \sqrt{M_D^2 + M_{\theta\phi}^2}$ , and  $M_{DS} = \sqrt{M_{r\theta}^2 + M_{r\phi}^2}$ , we

173 can quantify the ratios of the *CLVD*, *SS*, and *DS* components in the MT of ring-faulting as:

174 
$$\frac{|M_i|}{|M_{CLVD}| + M_{SS} + M_{DS}} \times 100 \, [\%], \ (10)$$

175 where *i* represents *CLVD*, *SS*, or *DS*.

Figures 2c and 2d show the theoretical MTs and components for reverse slips on ring faults with dip
angles of 60° and 75°, respectively, which have arc angles of 90°, 180°, 270°, and 360° (2nd–5th rows,

| 178 | respectively). The ring-fault azimuths are 0°, and the ring-fault orientations are 90° (i.e., the midpoint of the      |
|-----|--|
| 179 | ring fault is located on the north along the circumference of the circle). For comparison, MTs of slip on              |
| 180 | planar faults with the same dip angles that are parallel to the ring-fault orientation are shown (1st row).            |
| 181 | Ring-faulting has a vertical-CLVD mechanism, as long-period seismic contributions from different                       |
| 182 | segments along the curved ring fault partially cancel out (Ekström, 1994). Because the azimuths of                     |
| 183 | principal axes of the two double-couple components, $M_{SS}$ and $M_{DS}$ , are determined by the strike angle of      |
| 184 | a planar fault (1st row), the double-couple components from different portions of the ring fault cause the             |
| 185 | geometric cancellation. In contrast, as the <i>CLVD</i> component, $M_{CLVD}$ , of a planar fault does not change with |
| 186 | its strike angle, the component of the ring fault accumulates and becomes more dominant in the moment                  |
| 187 | tensor as the arc angle increases.   |
| 188 | 2.2 Indeterminate DS component at a shallow source depth   |
| 189 | Once the MT solution of ring-faulting is determined, the ring-fault parameters, namely, dip angle,                     |

arc angle, and ring-fault azimuth (Figure 2a), can be estimated from the ratios of the three MT components and azimuths of the principal axes of the *SS* and *DS* components. However, the *DS* component of such shallow earthquakes is indeterminate from long-period seismic waves, because the component near the solid surface has little contribution to long-period seismic waves (e.g., Dziewonski et al., 1981; Kanamori and Given, 1981). The indeterminacy of the *DS* component makes it difficult to estimate the dip angle and 195 seismic magnitude of ring-faulting from long-period seismic waves. In addition, we cannot determine the

196 ring-fault azimuth, which is reflected in the azimuth of the tension axis of the DS component.

197 To confirm the indeterminacy of the DS component at a shallow depth, we synthetize long-period 198 (0.005–0.0125 Hz) seismic waveforms, including all the relevant phases (e.g., P, S, and surface waves), at a virtual station from five hypothetical sources representing elementary components,  $M_{CLVD}$ ,  $M_D$ ,  $M_{\theta\phi}$ , 199  $M_{r\theta}$ , and  $M_{r\phi}$ . We assume the same scalar moment  $M_0 = 1.0 \times 10^{18}$  N m ( $M_w$  5.9) using Equation (1) for 200 201 the sources (Figure 3). Details of the numerical method are described in the caption of Figure 3. For a 202 source at 2.5 km depth in the crust, amplitudes of long-period seismic waves radiated from the DS 203 component  $(M_{r\theta}, M_{r\phi})$  are much smaller than those from the CLVD component  $(M_{CLVD})$  and the SS 204 component  $(M_D, M_{\theta\phi})$  (Figure 3a). Because of the inefficient seismic excitation, estimation of the DS 205 component is unstable. Also, small errors in the depth of the source result in large uncertainties in the DS 206 components owing to large variations in the amplitudes of synthetic long-period seismic waves. If the 207 source is at 10.5 km depth, the DS component radiates larger seismic waves (Figure 3b).

#### 208 2.3 Resolvable MTs of ring-faulting

Given the indeterminacy of the *DS* component, we propose a method for estimating two ring-fault parameters using only the *CLVD* and *SS* components, which are resolvable with long-period seismic waves. Here we define the resolvable MT ( $M_{res}$ ) by:

212 
$$\boldsymbol{M}_{res} = \boldsymbol{M}_{CLVD} + \boldsymbol{M}_{SS}. \tag{11}$$

213  $M_{res}$  for the idealized ring-faulting is shown in the 6th column in Figures 2c and 2d. Here, we introduce 214 two new dimensionless physical parameters extracted from  $M_{res}$ , as follows. The first parameter,  $k_{CLVD}$ , 215 is the ratio of  $|M_{CLVD}|$  to  $|M_{CLVD}| + M_{SS}$  of  $M_{res}$  defined by:

216 
$$k_{CLVD} = \frac{|M_{CLVD}|}{|M_{CLVD}| + M_{SS}} \times 100 \, [\%], \qquad (12)$$

which we call the *CLVD ratio*. This parameter can be used to estimate the ring-fault arc angle  $\Theta$  (Figure 217 4a). As  $\theta$  increases from 0° (i.e., a planar fault) to 180°,  $k_{CLVD}$  increases from 66.7% to 100%. From 218  $\Theta = 180^{\circ}$ ,  $k_{CLVD}$  decreases to a local minimum of 90% at ~255°, and then increases to 100% at 360°. 219  $k_{CLVD}$  reaches 100% when  $\Theta$  is 180° or 360°, where the SS component vanishes. When the dip angle is 220 221 constant along the ring fault, the relationship between  $k_{CLVD}$  and  $\Theta$  does not depend on the dip angle 222 because pure dip slip on a planar fault with any dip angle in all cases results in the same CLVD-to-SS component ratio of 2:1 (top row in Figures 2c and 2d). Thus, we can use  $k_{CLVD}$  to estimate some values of 223 224  $\Theta$  even if the DS component is indeterminate.

The second parameter,  $\psi$ , is defined as follows. The resolvable moment tensor  $M_{res}$  discussed here is expressed by three orthogonal dipoles. We use the orientation of the dipole with the smallest absolute moment to estimate the orientation of the ring fault. As shown in Figures 2c and 2d (6th column), this dipole determines the elongation direction of the nodal-line pattern of the mechanism diagrams of  $M_{res}$ . It can also be shown that this orientation is the same as the orientation of the Null (N) axis of the *best-fitting*  230 double-couple moment tensor (pp. 248-251 of Shearer, 2009) shown by thin curves on the mechanism 231 diagrams (6th column of Figures 2c and 2d). We refer to the dipole axis as the N-axis and denote its 232 orientation by  $\psi$ , which is measured from the north, eastward-reckoned positive,  $0 \le \psi < 180^\circ$ . Figures 4b and 4c show the relationships between the ring-fault orientation and the N-axis for vertical-T and 233 234 vertical-P CLVD earthquakes. The ring-fault orientation is parallel or perpendicular to the N-axis 235 depending on  $\Theta < 180^\circ$  or  $\Theta > 180^\circ$ , respectively. Because  $\psi$  is independent of the dip angle, this 236 parameter can be used to estimate the ring-fault orientation without knowing the DS component. We note 237 that what can be estimated from  $\psi$  is not the ring-fault azimuth but the orientation (Figure 2a); we cannot distinguish two different ring faults with the same arc angle but rotated by 180° to each other. 238

239 Thus,  $M_{res}$  for shallow ring-faulting is useful for estimating ring-fault parameters by using 240  $k_{CLVD}$  and  $\psi$  together. If  $k_{CLVD}$  is less than ~90%,  $\Theta$  can be uniquely determined by  $k_{CLVD}$ 241 because  $\Theta$  is a single-valued function of  $k_{CLVD}$  (Figure 4a). In this case, the ring-fault orientation is 242 parallel to the N-axis (Figures 4b and 4c). In contrast, if  $k_{CLVD}$  is larger than ~90%,  $\Theta$  cannot be 243 determined uniquely and three values of  $\Theta$  are possible for a given  $k_{CLVD}$  (Figure 4a); there also remain 244 two possibilities for the ring-fault orientation, parallel or perpendicular to the N-axis, depending on  $\theta$ 245 (Figures 4b and 4c). When  $\theta = 180^{\circ}$ , the N-axis orientation is indeterminate (Figures 2c and 2d), and 246 the ring-fault orientation cannot be determined. When  $\theta = 360^{\circ}$ , the ring-fault orientation is irrelevant.

## **3** Case study: Vertical-CLVD earthquakes at the Sierra Negra caldera, Galápagos Islands

| 248 | In the previous section, we showed that the resolvable MT, $M_{res}$ , which is composed of the <i>CLVD</i>         |
|-----|---|
| 249 | and SS components, of ring-faulting is useful for estimating the arc angle $\theta$ and the orientation of the ring |
| 250 | fault. Here, we investigate the relationships for a vertical-CLVD earthquake that occurred at the Sierra            |
| 251 | Negra caldera prior to the 2005 volcanic activity. We first test the stability of $M_{res}$ obtained from MT        |
| 252 | inversion using long-period seismic records at far field. Then, we analyze $M_{res}$ to estimate the ring-fault     |
| 253 | parameters and compare them with other observations. We also investigate two vertical-CLVD earthquakes              |
| 254 | at the caldera during volcanic activity in 2018.  |
| 255 | 3.1 $M_w$ 5.5 vertical-T CLVD earthquake prior to the 2005 eruption   |
| 256 | The Sierra Negra is a shield volcano located at the southern end of Isabella Island, in the Galápagos               |
| 257 | Islands (Figure 5a). A shallow 7 km $\times$ 10.5 km caldera structure is formed at the summit of the 1124-m-high   |
| 258 | volcano (Figure 5b; Reynolds et al., 1995). On 22 October 2005, the Sierra Negra caldera started eruption           |
| 259 | activity at ~23:30 in UTC (e.g., Global Volcanism Project, 2005; Geist et al., 2008). At 20:34 on the same          |
| 260 | day, about 3 h before initiation of the eruption, a vertical-T CLVD earthquake with $M_w$ 5.5 occurred              |
| 261 | (Chadwick et al., 2006; Jónsson, 2009). Clear long-period seismic signals from this earthquake were                 |
| 262 | observed at far-field stations (black kines in Figure 6). Geodetic observations with Global Positioning             |
| 263 | System (GPS) and Interferometric Synthetic Aperture Radar (InSAR) suggested reverse slip along a                    |
| 264 | sinuous fault system with an inward dip angle on the western to southern parts of the caldera caused by a           |

| 265 | pressurized sill-like magma chamber; this fault-motion mechanism is termed <i>trapdoor faulting</i> (e.g.,      |
|-----|---|
| 266 | Amelung et al., 2000; Jónsson, 2009). The occurrence of ring-faulting was indicated by a fresh fault scarp      |
| 267 | on the southwestern part of the caldera (black dotted and solid curves in Figure 5b) identified by Geist et al. |
| 268 | (2008), who conducted field surveys at the caldera after the 2005 eruption. The shallow sill-like magma         |
| 269 | chamber estimated from geodetic data (Jónsson, 2009) suggests that the earthquake occurred in the top $\sim$ 2  |
| 270 | km of the crust. For this geometry at such a shallow depth, the indeterminacy of the DS component is an         |
| 271 | issue. Thus, this is a good example for investigating how the MT solution of a vertical-CLVD earthquake         |
| 272 | caused by ring-faulting is related to the geometry of the ring fault identified by geodetic studies and field   |
| 273 | surveys.  |
| 274 | 3.2 Data & methods  |
| 275 | We perform MT inversion for the $M_w$ 5.5 vertical-T earthquake near the Sierra Negra caldera. We               |
| 276 | use the W-phase code for the inversion, including filtering, data screening, and convolution of Green's         |
| 277 | functions (Kanamori and Rivera, 2008; Hayes et al., 2009; Duputel et al., 2012). We use the normal mode         |
| 278 | method (e.g., Takeuchi and Saito, 1972) to compute Green's functions for the 1-D Preliminary Reference          |
| 279 | Earth Model (PREM; Dziewonski and Anderson, 1981), in the same way as we did for the synthetic test in          |
| 280 | Section 2.2. Long-period seismic waves are extracted from synthetic and observed waveforms by applying          |
| 281 | a one-pass and fourth-order Butterworth bandpass filter with corner frequencies at 0.005 and 0.0125 Hz.         |
| 282 | The inversion time window is set to include P, S, and surface waves. We assume zero contribution by a           |

volume change to the long-period seismic waves by imposing the zero-trace constraint,  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ . This means that the seismic waves are entirely attributed to ring-faulting. Possible bias caused by a volume change is discussed later in Section 4.2.

286 We use long-period seismic records at far-field stations for the inversion. We download seismic 287 records at stations within 5°-60° of the epicentral distance from the Data Management Center of the 288 Incorporated Research Institutions for Seismology (IRIS). For data screening (i.e., to remove bad data with 289 glitch, or low signal-to-noise ratio), we conduct a trial MT inversion using a source placed at 2.5 km depth 290 in the crust (i.e., 5.5 km depth of PREM including a 3-km oceanic layer) just below the Sierra Negra caldera 291 (0.83°S, 91.14°W). We assume a half duration and a centroid time shift reported in the Global Centroid 292 Moment Tensor (GCMT) Catalog. As a result of the trial inversion, we remove clearly bad data yielding a normalized root mean square (NRMS) misfit > 0.9; the NRMS is defined by  $\rho_i = \sqrt{\|s_i - d_i\|^2 / \|s_i\|^2}$ , 293 294 where  $s_i$  and  $d_i$  are synthetic and observed data in the inversion time window at the *i*-th station, 295 respectively, and  $\|s\|$  represents the L2 norm of data vector s. The selected dataset is composed of 25 296 seismic records at stations for the epicentral distance range from  $12.4^{\circ}$  to  $46.6^{\circ}$  and has a good azimuthal 297 coverage (Figure 6). The stations are from different seismic networks: the Global Seismograph Network (II, 298 IU), Broadband Tomography Under Costa Rica and Nicaragua (YO, 2003–2006), GEOSCOPE (G), and the 299 United States National Seismic Network (US).

300

To examine the stability of the MT solutions, we repeat MT inversion while moving the centroid

301 location in a 3D space around the Sierra Negra caldera. By examining the variation in the MT solutions, we 302 can assess the sensitivity of the solutions to small variations in estimated centroid location. For MT 303 inversion in the 3D space, centroid locations are distributed on two planes: the x-y (longitude-latitude) plane at a depth of 2.5 km in the crust (Figure 7a), and the x-z (longitude-depth) plane along a latitude of 304 305 0.83°S across the caldera (Figure 7b). The centroid location intervals are 0.1° in the horizontal direction and 2.0 km in the vertical direction. At each centroid location, we try the inversion with different values for the 306 half duration  $t_h$  of the source time function and the centroid time shift  $t_c$ , assuming  $t_h = t_c$ , and then 307 308 determine an optimal value by a grid search minimizing the waveform misfit. The waveform fit for the MT solution is measured with a global version of the NRMS misfit,  $\rho = \sqrt{\sum_i ||s_i - d_i||^2 / \sum_i ||s_i||^2}$ , where each 309 310 sum goes over the number of seismic records. Then, from the solution, we obtain  $M_{res}$  defined by 311 Equation (11). Strictly speaking, to estimate  $M_{res}$  exactly with the constraint of  $M_{r\theta} = M_{r\phi} = 0$ , we need 312 to perform three-element MT inversions with the three constraints,  $M_{r\theta} = M_{r\phi} = 0$ , and  $M_{rr} + M_{\theta\theta} + M_{r\theta}$  $M_{\phi\phi} = 0$ . However, to compare our solutions with the GCMT solutions which were obtained for the five 313 MT elements with the only constraint  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ , we here perform five-element MT 314 inversions only with the constraint  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ , and after the solution was obtained we set 315  $M_{r\theta} = M_{r\phi} = 0$ . In Supporting Information, we compare  $M_{res}$  obtained with these two methods and 316 show that the results are very similar when the datasets are good. 317

#### 318 3.3 Results

#### 319 3.3.1 Indeterminate *DS* component and stability of the resolvable MT

| 320 | Figure 7a shows the global NRMS values for the MT solutions at locations on the x-y plane at a                                   |
|-----|--|
| 321 | depth of 2.5 km in the crust. In the area around the Sierra Negra caldera (white rectangle in Figure 7a), the                    |
| 322 | NRMS values are small. Figure 7b shows the global NRMS values for the MT solutions on the x-z plane                              |
| 323 | along latitude 0.83°S (dashed line in Figure 7a). Similarly, small NRMS values are given by most MT                              |
| 324 | solutions in the top ~15 km of the crust. For example, the MT solution at the caldera ( $0.83^{\circ}$ S, $91.14^{\circ}$ W; red |
| 325 | circle in Figure 7a) at a depth of 2.5 km reproduces the observed records well with an NRMS value of 0.365                       |
| 326 | (Figure 6). From the MT solutions in the 3D space, 53 solutions at different centroid grids yield NRMS                           |
| 327 | values of $\leq 0.365$ , which we refer to as <i>acceptable solutions</i> hereafter.   |

328 Figure 7c shows the MT solutions on the x-y plane at a depth of 2.5 km in the area around the 329 caldera (white rectangle in Figure 7a), and Figure 7d shows the solutions on the x-z plane along a latitude 330 of  $0.83^{\circ}$ S (white dashed line in Figure 7a) in the top ~10 km of the crust. The solutions on the two planes 331 differ significantly depending on centroid locations in the 3D space, although they yield similar small NRMS values. Notably, at shallower depths in the crust, estimated  $M_w$  values and ratios of the DS 332 component are larger (Figure 7d). For the 53 acceptable solutions,  $M_W$  values are distributed widely from 333 5.50 to 6.49 (Figure 8a), and the ratio of the DS component, computed with Equation (10), ranges from 334 335 44.8% to 97.7% (Figure 8b). These results demonstrate the instability of MT inversion caused by the indeterminate *DS* component, as discussed in Section 2.2.

| 337 | From the MT solutions at centroid locations on the x-y and x-z planes, we extract $M_{res}$ defined by               |
|-----|--|
| 338 | Equation (11) (Figures 7e and 7f). $M_{res}$ on the two planes have similar focal mechanisms and $M_W$ . $M_W$       |
| 339 | values of $M_{res}$ are in a narrow range (5.33 ± 0.04) for the 53 acceptable solutions (Figure 8c). Also, $M_{res}$ |
| 340 | for the acceptable solutions contain stable values of the CLVD ratio $k_{CLVD}$ (73.0% ± 3.0%; Figure 8d) and        |
| 341 | the N-axis azimuth $\psi$ (102.7° ± 3.0°; Figure 8e). These results confirm that $M_{res}$ is stably obtained for    |
| 342 | vertical-CLVD earthquakes, even in the cases where centroid locations are not accurately determined                  |
| 343 | indicating its stability under the presence of noise in observed data. Thus, the two physical parameters (i.e.       |
| 344 | $k_{CLVD}$ and $\psi$ ) obtained from $M_{res}$ can be used to reliably estimate ring-fault parameters.              |
| 345 | In Figure 9 and Table 1, we compare the MT solution obtained for the centroid location at a depth of                 |
| 346 | 2.5 km just below the caldera (0.83°S, 91.14°W) with the solution from the GCMT Catalog. The centroid                |
|     |  |

depth of the GCMT solution is 9.0 km in the crust (i.e., 12 km of PREM including a 3-km oceanic layer).

- 348 The two MT solutions, including the indeterminate DS component, have very different focal mechanisms,
- 349  $M_W$  values, and ratios of the DS component (Figures 9a and 9b). In contrast,  $M_{res}$  extracted from the two
- different solutions show similar values for  $M_w$  (5.31 and 5.31),  $k_{CLVD}$  (73.4% and 77.3%), and  $\psi$  (101.9°
- and 96.3°; Figures 9c and 9d). These results demonstrate that  $M_{res}$  can be reliably estimated from various
- 352 available catalogs such as the GCMT, even if the centroid depth and the complete MT are not accurately
- determined for the shallow earthquakes (e.g., Chu et al., 2009; Wimpenny and Watson, 2020).

#### 354 3.3.2 Ring-fault parameters inferred from the resolvable MT

| 355 | We next estimate ring-fault parameters for the 2005 vertical-T CLVD earthquake at the Sierra Negra                               |
|-----|--|
| 356 | caldera from $M_{res}$ of the MT solution (Figure 9c). If we assume that the seismic waves are generated                         |
| 357 | entirely from idealized ring-faulting (uniform slip along a circular ring fault with a constant dip angle),                      |
| 358 | $M_{res}$ with a value of $k_{CLVD}$ of 73.4% indicates a ring fault with an arc angle $\Theta$ of ~80° (Figure 4a). In          |
| 359 | such a case of $\theta < 180^{\circ}$ , the N-axis with $\psi$ of 101.9° suggests that the ring-fault orientation is a direction |
| 360 | rotated slightly clockwise from the E-W direction. Similarly, the intra-caldera fault (black curve in Figure                     |
| 361 | 5b), which was attributed to the earthquake source by geodetic observations and field surveys (Amelung et                        |
| 362 | al., 2000; Jónsson, 2009; Geist et al., 2008), has an arc angle a little smaller than 90° and its orientation is                 |
| 363 | slightly rotated clockwise from the E-W direction, if we approximate the fault as a circular arc. Although                       |
| 364 | here we do not consider complexities of the actual fault geometry and slip distributions, the overall                            |
| 365 | agreement of the ring-fault parameters with the well-documented intra-caldera fault geometry strongly                            |
| 366 | suggests that we can study geometries of ring faults at volcanoes by analyzing the $M_{res}$ of MT solutions                     |
| 367 | obtained from long-period seismic records at far field.  |

## 368 3.4 Insights into two vertical-CLVD earthquakes prior to and during the 2018 eruption

The Sierra Negra caldera renewed its eruption activity at ~19:40 on 26 June 2018 (UTC), which lasted until 23 August (Global Volcanism Program, 2018; Vasconez et al., 2018; Bell et al., 2021). The activity included eruptions from several fissure vents along the northern part of the caldera rim and on the

| 372  | northern side of the volcanic flank, and large surface deformation with increased seismicity along the  |
|--|---|
| 373  | intra-caldera fault system (Bell et al., 2021). Prior to and during the eruption, two vertical-CLVD   |
| 374  | earthquakes with $M_w > 5$ were reported near the Sierra Negra caldera: a vertical-T earthquake with $M_w 5.3$ at   |
| 375  | 9:15 on 26 June, about 10 h before the initiation of the eruption, and a vertical-P earthquake with $M_w$ 5.1 at  |
| 376  | 0:30 on 5 July. Bell et al. (2021) analyzed GPS records at the caldera and attributed the two earthquakes to  |
| 377  | trapdoor faulting events on the intra-caldera fault structure. This indicates the ring-faulting origin of the   |
| 378  | earthquakes.  |
|  |   |
| 379  | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by   |
| 379<br>380   | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by flipped kinematics of slips on inward-dipping ring faults. Bell et al. (2021) reported that the first   |
| 379<br>380<br>381  | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by flipped kinematics of slips on inward-dipping ring faults. Bell et al. (2021) reported that the first (vertical-T) earthquake took place during the inflation phase of the caldera, preceding the eruption, and   |
| <ul><li>379</li><li>380</li><li>381</li><li>382</li></ul>                                | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by<br>flipped kinematics of slips on inward-dipping ring faults. Bell et al. (2021) reported that the first<br>(vertical-T) earthquake took place during the inflation phase of the caldera, preceding the eruption, and<br>caused large uplift of the inner caldera floor; on the other hand, the second (vertical-P) earthquake occurred   |
| <ul><li>379</li><li>380</li><li>381</li><li>382</li><li>383</li></ul>                    | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by<br>flipped kinematics of slips on inward-dipping ring faults. Bell et al. (2021) reported that the first<br>(vertical-T) earthquake took place during the inflation phase of the caldera, preceding the eruption, and<br>caused large uplift of the inner caldera floor; on the other hand, the second (vertical-P) earthquake occurred<br>during a rapid deflation phase after the initiation of the eruption and the caldera floor subsided. Shuler et al.  |
| <ul> <li>379</li> <li>380</li> <li>381</li> <li>382</li> <li>383</li> <li>384</li> </ul> | The difference in the types of vertical-CLVD earthquake (vertical-T or P) can be explained by<br>flipped kinematics of slips on inward-dipping ring faults. Bell et al. (2021) reported that the first<br>(vertical-T) earthquake took place during the inflation phase of the caldera, preceding the eruption, and<br>caused large uplift of the inner caldera floor; on the other hand, the second (vertical-P) earthquake occurred<br>during a rapid deflation phase after the initiation of the eruption and the caldera floor subsided. Shuler et al.<br>(2013a) demonstrated similar temporal relationships between vertical-CLVD earthquakes and an eruption |

386 whereas most vertical-P earthquakes occurred after an eruption started. Considering the co-seismic 387 deformation patterns of the caldera, it is reasonable to attribute the vertical-T earthquake to upward motion 388 of the central block along an inward-dipping ring fault (Figure 1a), and the vertical-P earthquake to a drop 389 of the block slipping on an inward-dipping ring fault (Figure 1c).

| 390 | To provide insights into the source geometries of two vertical-CLVD earthquakes, we here analyze                                 |
|-----|--|
| 391 | their MT solutions from the GCMT Catalog (Table 1, Figures 10a and 10c). Focal mechanisms and the                                |
| 392 | parameters ( $k_{CLVD}$ and $\psi$ ) of $M_{res}$ extracted from the MT solutions of the vertical-T and P earthquakes            |
| 393 | are shown in Figures 10b and 10d, respectively. For the vertical-T earthquake, $k_{CLVD}$ is 72.2% and $\psi$ is                 |
| 394 | 86.4° (approximately E–W), and for the vertical-P earthquake, $k_{CLVD}$ is 71.9% and $\psi$ is 55.5°                            |
| 395 | (approximately NE–SW). The small values of $k_{CLVD}$ , 72.2% for the vertical-T earthquake and 71.9% for                        |
| 396 | the vertical-P earthquake, indicate that both earthquakes occurred along short ring faults with arc angles $\Theta$              |
| 397 | of ~80°, according to the relationship between $k_{CLVD}$ and $\Theta$ (Figure 4a). In contrast, the significant                 |
| 398 | difference in $\psi$ of ~31° implies that the earthquakes occurred at different locations along the intra-caldera                |
| 399 | fault system. Using the relationship between the N-axis of $M_{res}$ and the orientation of the ring fault with                  |
| 400 | $\Theta < 180^{\circ}$ (top row in Figure 4b), the N-axis of $M_{res}$ is expected to be parallel to the ring-fault orientation. |
| 401 | Therefore, we estimate that the vertical-T earthquake occurred on a ring-fault segment oriented in the E-                        |
| 402 | W direction, whereas the vertical-P earthquake occurred on a different segment oriented in the NE-SW                             |
| 403 | direction. Given the fault structures exposed on the caldera floor (Figure 5b), we suggest that the vertical-T                   |
| 404 | earthquake was generated by reverse slip on the southern intra-caldera fault, which may partially                                |
| 405 | correspond to the fault estimated as generating the 2005 earthquake (the eastern part of black curve in                          |
| 406 | Figure 5b). By contrast, we infer that the vertical-P earthquake occurred on another ring-fault segment on                       |
| 407 | the southeastern or northwestern portion, although we cannot determine which of the two segments from                            |
| 408 | M <sub>res</sub> .   |

| 409 | We compare our estimations with geodetic observations by Bell et al. (2021), who used GPS data                 |
|-----|--|
| 410 | recorded on the caldera floor. The authors reported that the vertical-T earthquake caused large co-seismic     |
| 411 | uplift of 1.8 m and 1.4 m at GPS stations GV09 and GV06, respectively (Figure 5b), which supports our          |
| 412 | estimation of the vertical-T earthquake along the southern fault. On the other hand, the second earthquake     |
| 413 | caused large subsidence of 71 cm at GV06, but only 15 cm at GV09. The larger displacement at GV06 than         |
| 414 | GV09 supports that the main rupture of the vertical-P earthquake was on the southeastern part of the           |
| 415 | intra-caldera fault, which is consistent with one of the two candidates that we estimate for the geometry of   |
| 416 | the vertical-P earthquake (i.e., southeastern or northwestern intra-caldera fault). For reference, we indicate |
| 417 | the more plausible ring-fault geometry of the vertical-P earthquake by a gray dotted curve in Figure 5b.       |
| 418 | Thus, we suggest that the clear differences between the parameters of $M_{res}$ for the two vertical-CLVD      |
| 419 | earthquakes offer information about significant differences in source locations along the intra-caldera fault  |
| 420 | system.  |
| 421 | 4 Discussion   |

#### 422 4.1 Efficiency of long-period seismic excitation from ring-faulting

423 As demonstrated above, the nature of seismic excitation from ring-faulting is very different from 424 that of regular tectonic earthquakes. In general, despite the spectacular surface expression of ring faults, the 425 seismic excitation, especially at long periods (greater than  $\sim 100$  s), is inefficient, which often causes 426 difficulty in interpretation. We have already discussed several specific cases above, and here we add some 427 general discussion to clarify the problem with the inefficient seismic excitation.

There are two aspects to this problem. First, as previously discussed by Ekström (1994) and Shuler et al. (2013b), the ring-fault geometry results in cancellation of the source strength, as measured by the scalar moment. As discussed in Section 2, we represent the MT of ring-faulting by the sum of MTs of planar rhomboidal subfaults under the point-source approximation. We then compute the scalar moment  $M_0$  of the ring-faulting using Equation (1). Figure 11a shows the ratio:

433 
$$\frac{M_0}{\sum_i \Delta M_0^i} \qquad (13)$$

434 as a function of the dip and arc angles, where  $\Delta M_0^i$  is the scalar moment of the *i*-th subfault along the ring 435 fault computed using Equation (1). This ratio is generally smaller than 1 owing to the geometrical 436 cancellation of the double-couple components (i.e.,  $M_{SS}$  and  $M_{DS}$ ).

In addition to this geometrical cancellation, the efficiency of seismic excitation of ring-faulting is reduced because of its shallow source property. As expressed by Equation (6), the MT of ring-faulting can be expressed by the sum of three components,  $M_{CLVD}$ ,  $M_{SS}$ , and  $M_{DS}$ . Because of the very shallow depth,  $M_{DS}$  does not contribute to long-period seismic excitation; by contrast, the other two components ( $M_{CLVD}$ ,  $M_{SS}$ ), which we referred to as resolvable components, have contributions. The effect of little seismic excitation from  $M_{DS}$  can be expressed by the following ratio of scalar moment of  $M_{res}$  to that of the theoretical MT (Figure 11b):

$$444 \qquad \qquad \frac{M_0^{res}}{M_0}, \qquad (14)$$

445 where  $M_0^{res}$  is the scalar moment based on Equation (1) for  $M_{res}$  (defined by Equation (11)).

446 Then, the combined effect can be given by the ratio (Figure 11c):

447 
$$\frac{M_0}{\sum_i \Delta M_0^i} \times \frac{M_0^{res}}{M_0} = \frac{M_0^{res}}{\sum_i \Delta M_0^i}.$$
 (15)

As shown in Figure 11c, the excitation efficiency of long-period seismic waves from ring-faulting at ashallow depth is generally low, being lower for ring faults dipping more steeply.

450 The inefficient excitation of long-period seismic waves explains many peculiar characteristics of 451 vertical-CLVD earthquakes. Ring-faulting may generate greater surface deformation than expected 452 empirically from their seismic magnitudes estimated with long-period seismic waves. This may explain that the moment magnitude of the slip model geodetically estimated for an intra-caldera earthquake at the Sierra 453 Negra caldera was much larger than that determined with seismic data independently (Jónsson, 2009). If 454 vertical-T CLVD earthquakes at the submarine volcanoes near Torishima Island and Curtis Island are 455 456 related to ring-faulting, the disproportionately large tsunamis for their seismic magnitudes may be partially a result of the inefficient seismic excitation. Kanamori et al. (1993) identified an azimuthally uniform 457 radiation pattern of Rayleigh waves and an absence of Love waves from a vertical-T earthquake. This 458 459 peculiarity can be explained by the inefficient excitation of the DS component, as well as the geometrical cancellation of the double-couple components (Ekström 1994; Shuler et al., 2013b). 460

- 461 4.2 Effect of volume change on the zero-trace estimate of the *CLVD* component
- In previous sections, we estimated the CLVD moment scale  $M_{CLVD}$  of ring-faulting, defined by Equation (4), at a very shallow depth, with the assumption of a vanishing isotropic component  $M_{ISO}$ , defined by Equation (3). If a volume change occurs near ring-faulting, the estimated  $M_{CLVD}$  might be biased. As the bias depends on the geometry of the magma reservoir, we discuss three cases below.

#### 466 <u>Horizontal tensile crack</u>

467 The moment tensor for a horizontal tensile (or compressional) crack with a volume change  $\Delta V$  is 468 given in the  $(r, \theta, \phi)$  coordinate system by (e.g., Kawakatsu and Yamamoto, 2015)

469 
$$\boldsymbol{M}_{Tensile} = \Delta V \begin{bmatrix} \lambda + 2\mu \\ 0 & \lambda \\ 0 & 0 & \lambda \end{bmatrix}. \quad (16)$$

As seismic excitation of a moment tensor M is determined by  $(M:\varepsilon)$ , where  $\varepsilon$  is the strain tensor at the source (Gilbert, 1971), the excitation by the horizontal tensile crack is proportional to  $(\lambda + 2\mu)\varepsilon_{rr} + \lambda\varepsilon_{\theta\theta} + \lambda\varepsilon_{\phi\phi}$ , which is equal to  $\sigma_{rr}$ , where  $\varepsilon_{rr}$ ,  $\varepsilon_{\theta\theta}$ , and  $\varepsilon_{\phi\phi}$  are the rr,  $\theta\theta$ , and  $\phi\phi$  elements of the strain tensor, respectively, and  $\sigma_{rr}$  is the rr element of the stress tensor. For a very shallow source,  $\sigma_{rr} \approx$ 0. This means that a very shallow horizontal tensile crack has little seismic excitation (pp. 180–183 of Dahlen and Tromp, 1998; Fukao et al., 2018).

476 Previous studies have suggested that the Sierra Negra caldera has a sill-like magma reservoir at a
477 depth of ~2 km (e.g., Amelung et al., 2000; Chadwick et al., 2006; Jónsson, 2009). Because a volume

- 478 change of such a shallow sill-like reservoir involves a moment tensor defined by Equation (16) and does not 479 contribute to long-period seismic waves, it is reasonable to attribute the seismic waves from the 480 vertical-CLVD earthquakes at the caldera only to ring-faulting, as done in Section 3.
- 481 The case for a horizontal tensile crack has an important implication for other types of volume
  482 change. *M<sub>Tensile</sub>* can be decomposed as:

483 
$$\Delta V \begin{bmatrix} \lambda + 2\mu & \\ 0 & \lambda \\ 0 & 0 & \lambda \end{bmatrix} = \left(\lambda + \frac{2}{3}\mu\right) \Delta V \begin{bmatrix} 1 & \\ 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} + \frac{4}{3}\mu \,\Delta V \begin{bmatrix} 1 & \\ 0 & -0.5 \\ 0 & 0 & -0.5 \end{bmatrix}.$$
(17)

484 The first and second terms on the right-hand side represent isotropic and CLVD sources, respectively. Thus, 485 the vanishing excitation by a horizontal tensile crack simply means that a unit isotropic tensor  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ 

486 is equivalent to a CLVD tensor 
$$-\frac{4\mu}{3\lambda+2\mu}\begin{bmatrix}1\\0\\-0.5\\0\\0\\-0.5\end{bmatrix}$$
 for seismic excitation at a very shallow depth.

#### 487 <u>Spherical source</u>

488 If the deformation below ring-faulting is represented by a spherical source given by a moment

489 tensor

490 
$$\boldsymbol{M}_{Sphere} = \Delta V \begin{bmatrix} \lambda + \frac{2}{3}\mu \\ 0 & \lambda + \frac{2}{3}\mu \\ 0 & 0 & \lambda + \frac{2}{3}\mu \end{bmatrix} = M_{ISO}^{Sphere} \begin{bmatrix} 1 \\ 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}, (18)$$

491 where

492 
$$M_{ISO}^{Sphere} = \left(\lambda + \frac{2}{3}\mu\right)\Delta V, \quad (19)$$

493 then, using the equivalence relation between the isotropic and CLVD tensors, the CLVD moment scale of

494 ring-faulting at a shallow depth is observed as a CLVD source with

495 
$$M'_{CLVD} = M_{CLVD} - \frac{4\mu}{3\lambda + 2\mu} M^{Sphere}_{ISO} = M_{CLVD} - \frac{4}{3}\mu \,\Delta V.$$
 (20)

496 Thus, to estimate  $M_{CLVD}$  for ring-faulting, we need to add  $\frac{4}{3}\mu \Delta V$  to the observed  $M'_{CLVD}$  estimated with 497 the assumption of  $\Delta V = 0$ .

#### 498 <u>Vertical cylindrical source</u>

499 If the deformation below ring-faulting is represented by a vertical cylindrical source given by a500 moment tensor

501 
$$M_{Cylinder} = \Delta V \begin{bmatrix} \lambda & \lambda + \mu \\ 0 & 0 & \lambda + \mu \end{bmatrix} = \left( -\frac{2}{3}\mu \,\Delta V \right) \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -0.5 \end{bmatrix} + \left( \lambda + \frac{2}{3}\mu \right) \Delta V \begin{bmatrix} 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

502 
$$= M_{CLVD}^{Cylinder} \begin{bmatrix} 1 \\ 0 & -0.5 \\ 0 & 0 & -0.5 \end{bmatrix} + M_{ISO}^{Cylinder} \begin{bmatrix} 1 \\ 0 & 1 \\ 0 & 0 & 1 \end{bmatrix},$$
(21)

503 where

504 
$$M_{CLVD}^{Cylinder} = -\frac{2}{3}\mu \,\Delta V \ (22)$$

505 and

506 
$$M_{ISO}^{Cylinder} = \left(\lambda + \frac{2}{3}\mu\right)\Delta V, \quad (23)$$

507 then, considering the additional isotropic and CLVD components from the vertical cylindrical source, the

508 CLVD moment scale of ring-faulting is equivalent to a CLVD source with

509 
$$M'_{CLVD} = M_{CLVD} + \left(M^{Cylinder}_{CLVD} - \frac{4\mu}{3\lambda + 2\mu}M^{Cylinder}_{ISO}\right)$$

510 
$$= M_{CLVD} + \left\{ -\frac{2}{3}\mu \,\Delta V - \frac{4\mu}{3\lambda + 2\mu} \left(\lambda + \frac{2}{3}\mu\right) \Delta V \right\}$$

$$511 \qquad \qquad = M_{CLVD} - 2\mu\,\Delta V. \tag{24}$$

512 Thus, we need to add  $2\mu \Delta V$  to the observed  $M'_{CLVD}$  to estimate  $M_{CLVD}$  for ring-faulting.

To illustrate the equivalence relation between the isotropic and CLVD tensors discussed above, we show synthetic long-period waveforms computed for a CLVD source, an isotropic source, and a horizontal tensile crack source (Figure 12). For this comparison, we use a common metric for  $M_{CLVD}$ ,  $M_{ISO}$ , and  $M_{Tensile}$ . If we use the definition of a scalar moment  $M_0$ , given by Equation (1), then a CLVD source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and isotropic source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 1$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and a horizontal tensile crack source,  $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = 0.5$ , and the box and th

519 
$$M_0 \begin{bmatrix} \sqrt{4/3} & & \\ 0 & -\sqrt{1/3} & \\ 0 & 0 & -\sqrt{1/3} \end{bmatrix}, \quad (25)$$

520 
$$M_0 \begin{bmatrix} \sqrt{2/3} & & \\ 0 & \sqrt{2/3} & \\ 0 & 0 & \sqrt{2/3} \end{bmatrix}, \quad (26)$$

521 and

522 
$$M_0 \sqrt{\frac{2}{(\lambda+2\mu)^2+2\lambda^2}} \begin{bmatrix} \lambda+2\mu & \\ 0 & \lambda \\ 0 & 0 & \lambda \end{bmatrix}.$$
(27)

Here, we use the same scalar moment of  $M_0 = 1.0 \times 10^{18}$  Nm ( $M_w$  5.9). The waveforms for the CLVD and isotropic sources are quite similar to each other, except for the polarity and amplitude (Figures 12a and 12b). Figure 12c shows waveforms for the horizontal tensile source. The amplitudes are very small, reflecting the cancellation effects of  $M_{CLVD}$  and  $M_{ISO}$ .

#### 527 4.3 Limitations in analysis of long-period seismic waves from ring-faulting

We demonstrated the usefulness of MT inversion using long-period seismic waveforms for 528 studying slip kinematics and geometries of ring faults at active volcanoes. However, limitations in the use 529 of long-period seismic waves remain. Some moment tensor elements of ring-faulting are inefficient for 530 generating long-period seismic waves, so that parts of source parameters cannot be determined only with 531 532 the records. The temporal-spatial history of rupture propagation along a ring fault may not be resolved owing to the long-period property. Additionally, our method assumes simple cases of ring-faulting, i.e., 533 534 pure dip-slip motion along a circular fault geometry with uniform slip; however, ring-faulting can contain slightly strike-slip motion, complex fault geometry, and nonuniform slip distribution. To recover such 535

| 536 | detailed information of ring-faulting, shorter-period seismic waves may be utilized with heterogeneous 3-D    |
|-----|---|
| 537 | velocity structures around the calderas (e.g., Contreras-Arratia and Neuberg, 2019; Hejrani and Tkalčić,      |
| 538 | 2020). Also, recent studies demonstrated that inversion analysis using a simple 1-D Earth model can affect    |
| 539 | the MT inversion results (Hjörleifsdóttir and Ekström, 2010; Hejrani et al., 2017); hence, effects of the 3-D |
| 540 | velocity structures on the resolvable moment tensors need to be further examined. It is also difficult to     |
| 541 | constrain a source with a volume change that may accompany ring-faulting by using long-period seismic         |
| 542 | waves alone. To constrain the mechanism of a source with a change in volume, geodetic observations of         |
| 543 | surface deformation using such as GPS, tiltmeters, or InSAR are useful (e.g., Yun, 2007; Anderson et al.,     |
| 544 | 2019; Segall et al., 2019, 2020). Combinations of seismic analyses with geodetic observations will provide    |
| 545 | more details about source processes of ring-faulting that involve volume change of a magma reservoir.         |
|     |   |

#### 546 **5.** Conclusions

In this study, we investigated how source parameters of ring-faulting are related with MTs of vertical-CLVD earthquakes determined with long-period seismic waves. Avoiding the indeterminate issue of the vertical dip-slip component for shallow earthquakes, we proposed a new method to estimate the arc angle and the orientation of the ring fault based on two physical parameters, namely, the CLVD ratio  $k_{CLVD}$ and the N-axis azimuth  $\psi$ , of the resolvable MT  $M_{res}$ , which is composed of the vertical-CLVD and vertical strike-slip components. Through a case study of the 2005 vertical-CLVD earthquake at the Sierra Negra caldera, we showed the stability of  $M_{res}$  obtained by MT inversion using long-period seismic

| 554 | records at far field. We also demonstrated that the ring-fault parameters estimated with $M_{res}$ were      |
|-----|--|
| 555 | consistent with the geometry of the ring fault identified by geodetic observations and field surveys. In     |
| 556 | addition, we pointed out clear differences between $M_{res}$ of two vertical-CLVD earthquakes during the     |
| 557 | 2018 activity at the caldera and suggested significant differences in the kinematics and source locations of |
| 558 | the two ring-faulting events. Analyses of long-period seismic waves from moderate vertical-CLVD              |
| 559 | earthquakes observed globally allow remote estimation of ring-fault parameters at active volcanoes even      |
| 560 | without local observation networks. A better understanding of ring-faulting will provide insights into       |
| 561 | interactions of fault systems at volcanoes with magmatic processes, potentially leading to assessments of    |
| 562 | volcanic hazards.  |

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#### 571 Data Availability Statement

- 572 We used topography and bathymetry data downloaded from the Advance Land Observation
- 573 Satellite (ALOS) World 3D–30 m DEM (AW3D30; available from
- 574 <u>https://www.eorc.jaxa.jp/ALOS/en/index.htm</u>) provided by the Japan Aerospace Exploration Agency
- 575 (JAXA), and from GEBCO\_2020 Grid (available from
- 576 <u>https://www.gebco.net/data\_and\_products/gridded\_bathymetry\_data/</u>). The W-phase code can be
- 577 downloaded from <u>http://wphase.unistra.fr/wiki/doku.php/wphase</u>. We obtained earthquake information
- 578 from the GCMT Catalog (<u>https://www.globalcmt.org/</u>). We plotted focal mechanisms representing moment
- 579 tensors with a MATLAB code developed by James Conder (available from MATLAB Central File
- 580 Exchange
- 581 (https://www.mathworks.com/matlabcentral/fileexchange/61227-focalmech-fm-centerx-centery-diam-var
- 582 <u>argin</u>). Datasets of MT solutions obtained in this study and used for Figures 7 and S1 are provided in an
- 583 open access repository, Zenodo (<u>https://doi.org/10.5281/zenodo.4414990</u>).

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#### 786 Figures and tables



788 Figure 1 Two types of vertical-CLVD earthquake caused by ring-faulting.



793



795 Figure 2 Modeling and decomposition of theoretical moment tensors of idealized ring-faulting.

| 796 | (a) Ring-fault parameters. Thick and thin arc curves represent up-dip and down-dip ends, respectively.                         |
|-----|--|
| 797 | Arc angle $\Theta$ , dip angle $\delta$ , and ring-fault azimuth $\overrightarrow{OM}$ are variable parameters. The ring-fault |
| 798 | <i>orientation</i> is perpendicular to the ring-fault azimuth. The dip angle is uniform along the ring fault. (b)              |
| 799 | Three decomposed moment tensor (MT) components. (c-d) Theoretical MTs of ring-faulting with arc                                |
| 800 | angles of 90°, 180°, 270°, and 360° and with dip angles of (c) $60^{\circ}$ and (d) $75^{\circ}$ . For reference, an MT of     |
| 801 | a planar faulting is also shown in the top row. Columns: (1) kinematics and geometry of ring-faulting,                         |
| 802 | (2-6) focal mechanism diagrams of (2) the theoretical MT, (3-5) decomposed MT components                                       |

| 803 | (CLVD, SS, and DS) with their ratios, and (6) resolvable MT. The orientation of the best double- | couple |
|-----|--|--------|
|-----|--|--------|

- 804 *solution* is shown by thin curves in columns 2 and 6. All focal mechanisms are shown by projection of
- 805 the lower focal hemisphere. The diameter of the focal mechanism diagram is proportional to its scalar
- 806 moment but slightly exaggerated for the component with percentages of < 10% for clear visualization.





808 Figure 3 Synthetic long-period seismic waves from five elementary moment tensor components.

| 809 | Synthetic long-period seismic waveforms from sources representing five elementary moment tensor   |
|-----|---|
| 810 | components. The centroid depth is (a) 2.5 km and (b) 10.5 km in the crust. $M_D$ and $M_{\theta\phi}$ determine                                 |
| 811 | the SS component, and $M_{r\theta}$ and $M_{r\phi}$ determine the DS component. The virtual station is located at                               |
| 812 | $(\varphi, \Delta) = (19.2^{\circ}, 17.8^{\circ})$ , where $\varphi$ is the station azimuth from north (eastward positive), and $\Delta$ is the |

| also distance from the source. We use the w-phase code (Kanamori and Kivera, 2008; Hayes et al., 20 | 813 | distance from the source. | We use the W- | phase code (Kanamori | and Rivera, | 2008; Hayes et al | ., 200 |
|---|-----|---------------------------|---------------|----------------------|-------------|-------------------|--------|
|---|-----|---------------------------|---------------|----------------------|-------------|-------------------|--------|

- 814 Duputel et al., 2012) for the convolution of Green's functions and filtering. Green's functions are
- 815 computed by the normal mode method (e.g., Takeuchi and Saito, 1972), with the 1-D Preliminary
- 816 Reference Earth Model (PREM; Dziewonski and Anderson, 1981). A one-pass and fourth-order
- 817 Butterworth bandpass filter with corner frequencies of 0.005 and 0.0125 Hz is applied.



819 Figure 4 Relationship between *M<sub>res</sub>* and ring-fault parameters.



| 824 | of the central block (up or down), and the ring-fault orientation (an arrow) are shown. In the 3rd        |
|-----|---|
| 825 | column, $M_{res}$ is shown with the orientation of its N-axis (arrow). In the 4th column, the SS          |
| 826 | component is shown with its T- or P-axis (arrow). Note that the N-axis of $M_{res}$ is the same as the T- |
| 827 | and P-axes of the SS component for vertical-T and vertical-P earthquakes, respectively.                   |



829 Figure 5 Maps of the Galápagos Islands and the Sierra Negra caldera.

| 830 | (a) Map of the Galápagos Islands. Topographic and bathymetric data is from GEBCO_2020. The             |
|-----|--|
| 831 | black rectangle in the inset panel indicates the area shown in (a). The black cross represents the     |
| 832 | centroid location of the vertical-T earthquake of 22 October 2005 reported in the GCMT Catalog. (b)    |
| 833 | Map of the Sierra Negra caldera. Topographic data is from the Advance Land Observation Satellite       |
| 834 | (ALOS) World 3D-30 m DEM (AW3D30) provided by the Japan Aerospace Exploration Agency                   |
| 835 | (JAXA) (e.g., Tadono et al., 2014). The black curve indicates the fresh vertical scarp identified by   |
| 836 | Geist et al. (2008) during a field survey in June 2006; the part represented by the solid curve was    |
| 837 | clearly identified, whereas those along the dotted curves were less clearly defined. The red circles   |
| 838 | represent locations of GPS stations used by Bell et al. (2021). The gray dotted curve indicates a      |
| 839 | possible geometry inferred in this study for the 2018 vertical-P earthquake (see text in Section 3.4). |



Figure 6 Model performance of MT inversion for the  $M_w$  5.5 vertical-T CLVD earthquake of 22

842 October 2005.

Red and black lines represent synthetic and observed waveforms, respectively. The start and end

- points of the inversion time window are indicated by red circles. In each inset map, the blue star and
- the large red circle represent locations of the epicenter (0.83°S, 91.14°W) and the station. The station
- 846 azimuth ( $\varphi$ ) and epicentral distance ( $\Delta$ ) are indicated at the top of each panel.



Figure 7 MT inversion for the vertical-T CLVD earthquake of 22 October 2005 at the Sierra Negra
caldera.

(a-b) Global NRMS misfits  $\rho$  of MT solutions at source locations distributed on (a) the x-y plane at a depth of 2.5 km in the crust and (b) the x-z plane along a latitude of 0.83° (dashed white line in (a)). The red circle in (a) and the red line in (b) represent the approximate locations of the Sierra Negra caldera. (c-d) MT solutions at different centroid locations on (c) the x-y plane around the caldera (in the area shown by the white rectangle in (a)) and (d) the x-z plane. (e-f) Resolvable MTs on (e) the xy plane around the caldera and (f) the x-z plane. All focal mechanisms are shown by projection of the lower focal hemisphere. In (b), (d), and (f), the vertical axis represents the centroid depth in the crust.



858 Figure 8 Histogram of the parameters of acceptable MT solutions.

(a)  $M_w$  and (b) the ratio of the DS component of the acceptable MT solutions. (c)  $M_w$ , (d) the CLVD

860 ratio  $k_{CLVD}$ , and (e) the N-axis azimuth  $\psi$  of  $M_{res}$  extracted from the acceptable MT solutions.

861



Figure 9 MT solutions and resolvable MTs of the  $M_w$  5.5 vertical-T CLVD earthquake of 22 October 2005. (a) MT solution with the ratios of the three MT components and (c) resolvable MT with the ratio of the *CLVD* component  $k_{CLVD}$  and the N-axis azimuth  $\psi$  obtained from our MT inversion at a depth of 2.5 km in the crust just below the caldera. (b) MT and (d) resolvable MT obtained from the GCMT Catalog. All focal mechanisms are shown by projection of the lower focal hemisphere.



Figure 10 GCMT solutions for two vertical-CLVD earthquakes during the 2018 volcanic activity. (a) MT solution with the ratios of the three MT components and (b) resolvable MT of the  $M_w$  5.3 earthquake of 26 June 2018 with the ratio of the *CLVD* component  $k_{CLVD}$  and the N-axis azimuth  $\psi$ obtained from the GCMT Catalog. (c–d) The same as (a–b) but for the  $M_w$  5.1 earthquake of 5 July 2018. All focal mechanisms are shown by projection of the lower focal hemisphere. 876





Figure 11 Seismic excitation rate of ring-faulting at a shallow source depth.

879 (a) Geometrical cancellation of the scalar moment of idealized ring-faulting, calculated using Equation 880 (13). (b) The ratio of  $M_0^{res}$  to  $M_0$  of idealized ring-faulting, calculated using Equation (14). (c) The





883 Figure 12 Effects of an isotropic source on estimation of the CLVD source.

Synthetic long-period seismic waveforms of (a) a CLVD source (Equation 25), (b) an isotropic source (Equation 26), and (c) a horizontal tensile source (Equation 27). The MT of the horizontal tensile crack consists of *CLVD* and *ISO* components with a ratio of  $M_{ISO}$ :  $M_{CLVD} = \left(\lambda + \frac{2}{3}\mu\right):\frac{4}{3}\mu$ , as given in Equation (17). The centroid depth is assumed to be 2.5 km in the crust. The station location and filtering procedure are the same as those used for Figure 3.

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|   | Event date      | Source of  | Longitudo | Latitude<br>(°S) Depth<br>in the crust<br>(km) | Depth                | Elements of moment tensor (N m) |                 |                |               |             |                  |   |       |
|---|-----------------|------------|-----------|--|----------------------|---------------------------------|-----------------|----------------|---------------|-------------|------------------|---|-------|
|   |                 | solution   | (°W)      |  | in the crust<br>(km) | M <sub>rr</sub>                 | Μ <sub>θθ</sub> | $M_{\phi\phi}$ | $M_{r\theta}$ | $M_{r\phi}$ | $M_{\theta\phi}$ | Scale<br>factor<br>(10 <sup>exp</sup> ) | $M_w$ |
|   | 22 October 2005 | This study | 91.14     | 0.83   | 2.5                  | 1.246                           | -1.035          | -0.210         | -6.127        | -3.718      | 0.182            | 17                                      | 5.84  |
| _ | 22 October 2005 | GCMT       | 91.35     | 1.00   | 9.0                  | 1.260                           | -0.989          | -0.268         | 0.459         | -1.510      | 0.080            | 17                                      | 5.46  |
| _ | 26 June 2018    | GCMT       | 91.33     | 0.96   | 9.0                  | 1.230                           | -1.090          | -0.148         | 0.118         | -0.592      | -0.059           | 17                                      | 5.35  |
| _ | 5 July 2018     | GCMT       | 90.98     | 0.88   | 9.0                  | -3.880                          | 2.490           | 1.400          | 0.314         | -3.300      | 1.420            | 16                                      | 5.06  |

890

## 891 Table 1 Moment tensor solutions of vertical-CLVD earthquakes for the Sierra Negra caldera.

| 892 | Centroids and moment tensor solutions of vertical-CLVD earthquakes for the Sierra Negra caldera     |
|-----|---|
| 893 | obtained by MT inversion in this study or taken from the GCMT Catalog. Note that the centroid depth |
| 894 | of the GCMT Catalog may be determined at a greater depth of 9 km in the crust (i.e., 12 km of PREM  |
| 895 | including a 3-km oceanic layer) than the accrual centroid depth of the earthquakes to maintain the  |
| 896 | stability of the solutions (Ekström et al., 2012).  |
|     |   |

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#### Supporting Information for

### Moment Tensors of Ring-Faulting at Active Volcanoes: Insights into Vertical-CLVD Earthquakes at the Sierra Negra Caldera, Galápagos Islands

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#### Additional Supporting Information (Files uploaded separately)

Captions for Datasets S1 to S4

#### Introduction

In Text S1, we conduct three-element MT inversion for estimating the resolvable moment tensor ( $M_{res}$ ) of the vertical-T CLVD earthquake at the Sierra Negra caldera in 2005. In Data Sets S1–S4, we provide solutions of MT inversions for the earthquake obtained in Section 3 and Text S1. Data Sets are available in an open access repository, Zenodo (https://zenodo.org/record/4414990).

#### Text S1. Inversion with the constraint of zero DS component

In Main Text, we obtain  $M_{res}$ , defined by Equation (11), for the vertical-T CLVD earthquake at the Sierra Negra caldera in 2005 as follows: (1) estimate five independent MT elements by the inversion assuming the zero trace  $(M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0)$ , and then (2) remove the indeterminate *DS* component ( $M_{DS}$ ) by setting  $M_{r\theta} = M_{r\phi} = 0$ . On the other hand,  $M_{res}$ can be obtained directly by the inversion for only three independent MT elements with the constraints of zero *DS* component, or  $M_{r\theta} = M_{r\phi} = 0$ , as well as the zero trace (e.g., Kanamori and Given, 1981). Here, we estimate  $M_{res}$  of the vertical-T CLVD earthquake by the three-element MT inversion. For the inversion, we basically follow the five-element MT inversion method in the 3D space, as explained in Section 3.2, but with the additional constraint of  $M_{r\theta} = M_{r\phi} = 0$ . We use the same dataset composed of the 25 seismic records.

Figure S1a shows the global NRMS values for  $M_{res}$  solutions at locations on the x–y plane at a depth of 2.5 km below the solid surface that are obtained by the three-element MT inversion. In a small area around the Sierra Negra caldera (white rectangle in Figure S1a), the NRMS values are small. Figure S1b shows the global NRMS values for  $M_{res}$  solutions on the x–z plane along latitude 0.83°S (dashed line in Figure S1b). Similarly, small NRMS values are yielded by most of the solutions in the shallow crust. The solution at the caldera (0.83°S, 91.14°W; red circle in Figure S1a) at a depth of 2.5 km reproduces the observations well with an NRMS value of 0.394 (Figure S2). From the  $M_{res}$  solutions in the 3D space, 36 solutions at different centroid grids yield NRMS values of  $\leq$  0.394.

In Figures S1c and S1d, we show  $M_{res}$  estimated by the three-element MT inversion at centroid locations on the x–y and x–z planes, respectively.  $M_{res}$  on the two planes have very similar focal mechanisms and  $M_w$ . For the 36 solutions with small NRMS values of  $\leq 0.394$ ,  $M_w$  values are in a narrow range (5.33 ± 0.03) (Figure S3a); the solutions also contain stable values of the CLVD ratio  $k_{CLVD}$  (73.0% ± 2.2%; Figure S3b) and the N-axis azimuth  $\psi$  (102.8° ± 1.5°; Figure S3c). These values are almost the same as those of  $M_{res}$  obtained by the five-element MT inversion method in Main Text (See Section 3.3 and Figure 8c–e). Thus, the two different methods for estimating  $M_{res}$  yield almost equivalent results when using the good datasets.

We note that the  $M_{res}$  solutions obtained by the three-element MT inversion do not contain the *DS* component ( $M_{r\theta} = M_{r\phi} = 0$ ); however, the global NRMS values of  $\leq 0.394$  for the  $M_{res}$  solutions are almost comparable to the values of  $\leq 0.365$  for the solutions including the *DS* component estimated by the five-element MT inversion in Main Text (See Section 3.3 and Figure 6). This demonstrates that most of the long-period seismic waves of the earthquake are originated from the *CLVD* and *SS* components, whereas the *DS* component has little contribution to excitations of long-period seismic waves, as discussed in Section 4.1.



## Figure S1. Three-element MT inversion with the constraint of zero *DS* component for the vertical-T CLVD earthquake of 22 October 2005 at the Sierra Negra caldera.

(a–b) NRMS misfits of  $M_{res}$  solutions inverted by the three-element MT inversion at source locations distributed on (a) the x–y plane at a depth of 2.5 km in the crust and (b) the x–z plane along a latitude of 0.83° (dashed white line in (a)). The red circle in (a) and the red line in (b) represent the approximate locations of the Sierra Negra caldera. (c–d)  $M_{res}$  solutions at different centroid locations on (c) the x–y plane around the caldera (in the area shown by the white rectangle in (a)) and (d) the x–z plane. All focal mechanisms are shown by projection of the lower focal hemisphere. In (b) and (d), the vertical axis represents the centroid depth in the crust.



## Figure S2. Model performance of three-element MT inversion with the constraint zero *DS* component for the $M_w$ 5.5 vertical-T CLVD earthquake of 22 October 2005.

Red and black lines represent synthetic and observed waveforms, respectively. The start and end points of the inversion time window are indicated by red circles. In each inset map, the blue star and large red circle represent locations of the epicenter (0.83°S, 91.14°W) and the station. The station azimuth ( $\varphi$ ) and epicentral distance ( $\Delta$ ) are indicated at the top of each panel. Note that the observations are well-reproduced even without the *DS* component.



Figure S3. Histogram of the parameters of *M<sub>res</sub>* solutions with small NRMS values.

(a)  $M_W$ , (b) the CLVD ratio  $k_{CLVD}$ , and (c) the N-axis azimuth  $\psi$  of  $M_{res}$  solutions yielding small NRMS values of  $\leq$  0.394, which are estimated by the three-element MT inversion with the constraint of zero *DS* component.

#### Reference

Kanamori, H., & Given, J. W. (1981). Use of long-period surface waves for rapid determination of earthquake-source parameters. *Physics of the Earth and Planetary Interiors*, *27*(1), 8–31. <u>https://doi.org/10.1016/0031-9201(81)90083-2</u>

**Data Set S1.** MT solutions obtained by the five-element MT inversion on the x-y plane with the constraint of zero trace, which is conducted in Section 3. The solutions are used for Figures 7a, 7c and 7e.

**Data Set S2.** Same as Data Set S1, but on the x-z plane. The solutions are used for Figures 7b, 7d and 7f.

**Data Set S3.** *M*<sub>res</sub> solutions obtained by the three-element MT inversion on the x-y plane with the constraints of zero trace and zero *DS* component, which is conducted in Text S1. The solutions are used for Figures S1a, and S1c.

**Data Set S4.** Same as Data Set S3, but on the x-z plane. The solutions are used for Figures S1b, and S1d.