Storm Time Data Assimilation in the Thermosphere Ionosphere with TIDA

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Abstract

Data assimilation schemes with empirical background models of the ionosphere are already in operational use. However such methods suffer during disturbed conditions when large gradients are present and are moving relatively fast through the modeled domain. Also, such schemes have limited forecasting capabilities. In order to improve disturbed conditions modeling, more sophisticated assimilation schemes based on sparse measurements for the coupled thermosphere ionosphere system are needed. We have implemented an ensemble Kalman Filter (enKF) for the Thermosphere-Ionosphere (TI) system. We used the Coupled Thermosphere Ionosphere Plasmasphere electrodynamics (CTIPe) model as the background for an assimilation scheme and created the Thermosphere Ionosphere Data Assimilation (TIDA) software package. We published our first paper discussing neutral mass density assimilation during quiet geomagnetic conditions in Space Weather in 2018. In this paper we present results from experiments during the 2003 Halloween Storm, 27-31 October 2003, under very disturbed (K\$-p\$ = 9) conditions while assimilating GRACE-A and B, and CHAMP neutral density measurements. TIDA was able to simulate this disturbed period without using the L1 solar wind measurements which were contaminated by solar energetic protons, by estimating the model inputs from the density measurements. TIDA is being prepared to offer specification and short term forecasts of neutral density for satellite drag and debris collision avoidance for space traffic management. We also plan to offer long term (solar cycle length), average neutral density estimation for satellite fleet management.

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Key Points:

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8	• This study demonstrates the data assimilation potential improvement for the TI
9	system modeling during severe geomagnetic storms
10	• The estimation of the neutral density covariance matrix with a 75 member ensem-
11	ble of CTIPe runs does not require covariance localization
12	• TIDA can produce neutral density model results even in the absence of L1 sys-
13	tem forcing measurements

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14 Abstract

Data assimilation schemes with empirical background models of the ionosphere are al-15 ready in operational use. However such methods suffer during disturbed conditions when 16 large gradients are present and are moving relatively fast through the modeled domain. 17 Also, such schemes have limited forecasting capabilities. In order to improve disturbed 18 conditions modeling, more sophisticated assimilation schemes based on sparse measure-19 ments for the coupled thermosphere ionosphere system are needed. We have implemented 20 an ensemble Kalman Filter (enKF) for the Thermosphere-Ionosphere (TI) system. We 21 used the Coupled Thermosphere Ionosphere Plasmasphere electrodynamics (CTIPe) model 22 as the background for an assimilation scheme and created the Thermosphere Ionosphere 23 Data Assimilation (TIDA) software package. We published our first paper discussing neu-24 tral mass density assimilation during quiet geomagnetic conditions in Space Weather in 25 2018. In this paper we present results from experiments during the 2003 Halloween Storm. 26 27-31 October 2003, under very disturbed ($K_p = 9$) conditions while assimilating GRACE-27 A and B, and CHAMP neutral density measurements. TIDA was able to simulate this 28 disturbed period without using the L1 solar wind measurements which were contami-29 nated by solar energetic protons, by estimating the model inputs from the density mea-30 surements. TIDA is being prepared to offer specification and short term forecasts of neu-31 tral density for satellite drag and debris collision avoidance for space traffic management. 32 We also plan to offer long term (solar cycle length), average neutral density estimation 33 for satellite fleet management. 34

³⁵ Plain Language Summary

Data assimilation schemes with empirical background models are already in operational use. Here we present an assimilation scheme using an ensemble Kalman filter with a physics based numerical background model. We show simulations for October 27 - 31, 2003, a period that includes several large geomagnetic disturbances known as the Halloween storms. This assimilation exercise is in preparation for testing future neutral density data products.

42 **1** Introduction

Tools for ensemble modeling and data assimilation in the terrestrial weather and 43 ocean science have been developed (Hoar et al., 2009) and are in operational use. The 44 use of an enKF in space weather is also not new. M. V. Codrescu et al. (2004) published 45 a paper for neutral composition enKF assimilation in 2004. Although neutral compo-46 sition was recognized to be one of the most important factors in ionospheric simulations 47 during storms (Chartier et al., 2013), the lack of neutral composition measurements has 48 prevented the operational implementation of enKFs in space weather products and ser-49 vices. However the importance of enKF for space weather research has been recognized, 50 enKFs have been used in research, and papers have been published (Solomentsev et al., 51 2012; Morozov et al., 2013; Hsu et al., 2014; Chartier et al., 2016), and references therein. 52

Today, other kinds of assimilation models based on Gauss Markov (GM) Kalman 53 Filter (KF) processes are more popular in operational settings (Spencer et al., 2004; Schunk 54 et al., 2004; T. Fuller-Rowell et al., 2006; Jee et al., 2010; Jakowski et al., 2011; Borries 55 et al., 2015). GM KF assimilation schemes are based on stationary predefined covari-56 ance matrixes that work best if large amounts of data are available to overwhelm the em-57 pirical background model. The sudden availability of large amounts of Total Electron 58 Content (TEC) measurements from Global Navigation Satellite Systems (GNSS) signals 59 made the ionosphere GM KF assimilation schemes feasible to implement. GM KF based 60 assimilation schemes can be very good at ionosphere specification for past events, espe-61 cially during quiet or moderately disturbed geomagnetic conditions when large amounts 62 of data are available. However, in real-time environments they can suffer from data star-63

vation and do not have forecasting capabilities beyond persistence with a predefined evolution toward climatology.

During disturbed conditions, GM KF schemes have difficulty because their prede-66 fined, quiet-time covariance matrices do not keep pace with the changing system. To ob-67 tain the appropriate covariance matrix during disturbed conditions it would be neces-68 sary to perform variational analysis (Rockafellar & Wets, 1998) during every assimila-69 tion time step. However, for assimilation schemes with hundreds of thousands to mil-70 lions of state elements, performing variational analysis every assimilation time step (15 71 72 - 30 minutes) is not practical and the covariance matrix needs to be estimated in some other way. An estimation of the covariance matrix using Monte Carlo methods was first 73 proposed by Evensen (1994) as the ensemble Kalman Filter (enKF). 74

In a previous paper (S. M. Codrescu et al., 2018), we discussed assimilation results 75 for total mass density and showed that assimilating measurements from one satellite im-76 proves the model results globally, during quiet conditions. In this paper, in Section 2, 77 we discuss the dominant processes that make the TI covariance matrix non-stationary 78 during disturbed geomagnetic conditions. The paper continues with an experiment us-79 ing TIDA to assimilate GRACE-A, GRACE-B, and CHAMP neutral density measure-80 ments during the extreme geomagnetic 2003 Halloween storms. Section 3 gives an overview 81 of the TIDA software and setup of the experiment. The measurement sources are de-82 scribed in Section 4, results presented in Section 5, and finally we conclude in Section 6. 83

⁸⁴ 2 The Thermosphere Ionosphere System

The global neutral density and composition of the thermosphere depend on sys-85 tem forcing and the interaction with the ionosphere (FullerRowell et al., 1994). The global 86 electron and ion density structure, roughly from 50 to 1000 km altitude, are at any given 87 time the result of a dynamic equilibrium between plasma production, loss, and trans-88 port, processes controlled to a large extent by neutral composition and neutral winds (T. J. Fuller-89 Rowell et al., 1997). The processes that affect neutral composition, density, and winds 90 and the production, loss, and transport of plasma are highly variable on timescales of 91 minutes to years and their relative importance can change as a function of location on 92 the globe, Universal Time, storm commencement time, season, solar cycle, waves prop-93 agating from below, and the previous state of the ionosphere-thermosphere-magnetosphere 94 system (Sarris, 2019). On short time-scales, the variations are controlled by a set of external energy inputs that include solar radiation absorption at a variety of wave lengths. 96 solar energetic proton deposition, solar wind energy transfer through the magnetosphere 97 that depends on the density and speed of the solar wind and the magnitude and orien-98 tation of the interplanetary magnetic field (IMF) (M. V. Codrescu et al., 2012), and waves 99 propagating from below (Heelis & Maute, 2020). The influence of waves propagating from 100 below will not be discussed further in this paper as their amplitudes and phases change 101 slowly relative to the duration of a geomagnetic storm and their influence can be taken 102 into account by an appropriate lower boundary condition in the assimilation background 103 model. 104

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2.1 The system During Quiet Geomagnetic Conditions

While the Thermosphere Ionosphere (TI) is never in a true steady state, it can reach quasi-steady state conditions if the system inputs are quasi-constant over some period of time (days), as it happens during prolonged quiet geomagnetic conditions (M. V. Codrescu et al., 2008). Under steady state conditions the system energy input is balanced by cooling through CO₂ and NO infrared emissions and diurnally reproducible patterns can be observed in most system state variables.

While in prolonged quiet periods, the TI system reaches a quasi-steady state that 112 can last many days (Roble, 1992). The state is said to be in a diurnally reproducible pat-113 tern. Under such conditions statistical models of high-latitude convection electric fields 114 (Weimer, 2005), particle precipitation (T. J. Fuller-Rowell & Evans, 1987), and solar EUV 115 fluxes based on correlation with the F10.7 measurements (Hinteregger et al., 1981) are 116 good enough to give acceptable model results when used in physics based numerical mod-117 els of the system. In addition, empirical, statistical models of the ionosphere (Bilitza, 118 2018; Nava et al., 2008) or thermosphere climatology (Picone et al., 2002) are also good 119 during quasi-steady state conditions. This means that during quiet conditions the sys-120 tem can be modeled with a high level of confidence. 121

During quasi-steady state conditions, a global equilibrium is established between 122 heating due to solar radiation absorption on the dayside, Joule Heating at high latitudes 123 and infrared cooling due to NO and CO₂. As a consequence, a diurnally reproducible 124 global neutral temperature structure and circulation are established and a relatively sta-125 ble global neutral composition structure is maintained (Killeen et al., 1997). This state 126 of the thermosphere produces a diurnally reproducible global dynamo electric field pat-127 tern (Richmond, 1989) which in association with the stable prompt penetration electric 128 field pattern of magnetospheric origin (Manoj & Maus, 2012) produce a diurnally repro-129 ducible ionosphere. During geomagnetically quiet conditions the energy input from so-130 lar radiation absorption dominates the system energy input (Mlynczak et al., 2016). 131

In the upper atmosphere around 300 km altitude where the peak electron density 132 normally occurs, the temperature structure establishes day-night pressure gradients that 133 drive the global circulation neutral winds (Hedin et al., 1991). The winds blow from the 134 135 dayside towards the nightside, both east and west and over the poles from the 14:00 local time sector. Mostly molecular species are present below 150 km altitude and atomic 136 species above. The difference between the Earth geographic and magnetic poles contributes 137 to the diurnal variation in the global temperature, winds, and composition structure both 138 in the sun-fixed reference frame and at any location on the globe. 139

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2.2 The system During Disturbed Geomagnetic Conditions

During geomagnetic storms, changes in external system forcing cause large increases 141 in the magnitude and distribution of Joule heating, in auroral particle precipitation to-142 tal energy and its distribution, and in momentum transfer to neutrals. The total energy 143 input into the TI system at high-latitudes increases dramatically and can become larger 144 than solar radiation heating. This has dramatic consequences for the global neutral winds 145 and composition. Furthermore, changes in neutral winds cause changes in the dynamo 146 electric field pattern. Due to the tight coupling between the ionosphere and thermosphere 147 the changes are then reflected in the ionosphere and feed-back to the neutral state through 148 ion drag, momentum transfer, heat transfer, and other mechanisms (FullerRowell et al., 149 1994, 1996). 150

Empirical models are not appropriate to represent the state of the TI system during severe geomagnetic storms. Numerical models of the system also suffer during disturbed conditions because the statistical models used for forcing have very large uncertainties and this results in unacceptable uncertainties in model simulation results. Although disturbed conditions may happen only during a small percentage of time, it is during disturbed conditions that accurate modeling is most important.

Storm Joule heating occurs at high-latitudes at about 110-115 km altitude where molecular species $(O_2 \text{ and } N_2)$ dominate. The additional heating changes the pressure gradients and drives a storm circulation, in addition to the quiet time winds. Strong vertical winds are driven above the auroral zone heating area and meridional winds away from the heating area at higher altitudes. Vertical winds will take molecular species up and change the neutral composition creating what is called the composition bulge. Merid ional winds will spread the bulge towards lower latitudes (Proelss & von Zahn, 1978).

During small disturbances the storm induced meridional winds are overwhelmed by the quiet time circulation on the dayside but add to it on the nightside resulting in a distortion of the composition bulge relative to the shape of the auroral zone. During large storms meridional winds can turn equatorward at mid-latitudes even on the dayside. The size, shape, and position of the auroral zone and the composition bulge are highly variable functions of solar wind density and speed, magnitude and orientation of the interplanetary magnetic field, and storm time.

During a geomagnetic storm molecular species are transported up (upwelling) above 171 200 km where they displace lighter atomic species (mostly atomic Oxygen). The lighter 172 species are then forced equatorward by storm meridional winds. To balance the pres-173 174 sure gradients and close the storm circulation the lighter species are transported down (downwelling) by storm vertical winds at some distance equatorward of the heating area 175 and a return poleward flow of molecular species takes place at lower altitudes (FullerRowell 176 et al., 1994, 1996). The position of the upwelling area can vary in time but depends mostly 177 on the intensity of the storm while the position of the downwelling area is a more com-178 plicated function of storm intensity, duration, and storm time profile. 179

The changes in neutral dynamics and composition cause important changes in the 180 TI system (Proelss & von Zahn, 1978; FullerRowell et al., 1994; Burns et al., 1995; Fuller-181 Rowell et al., 1996). In the composition bulge, plasma production decreases due to the 182 decreased atomic Oxygen densities while the loss of plasma increases through charge ex-183 change with molecular species followed by recombination. Poleward meridional winds 184 and westward E-fields can also contribute to plasma loss. It is not uncommon to have 185 less than half the quiet time plasma peak density (NmF2) in an area covered by the com-186 position bulge following a geomagnetic storm. This is what is called the negative iono-187 sphere storm effect. The global neutral composition can take more than 36 hours to re-188 cover after a storm. 189

In the downwelling area the increased atomic Oxygen causes increased plasma production and reduced loss resulting in increased plasma density. This is the positive ionospheric storm. Equatorward meridional winds and eastward E-fields can also contribute to the positive phase.

At a given location, positive storm effects are seen first though not always, followed by negative storm effects (M. V. Codrescu et al., 1992). The ionospheric changes are most pronounced in the F2 layer but can be significant in the whole ionosphere especially during long geomagnetic storms. Meridional winds driven by storms can cross the equator and propagate in the opposite hemisphere.

The system forcing uncertainties are greatly amplified during geomagnetic storms. Small scale electric field variability can increase dramatically, change the spatial distribution of energy input, and more than double the Joule heating that results from the convection average electric fields (M. V. Codrescu et al., 2000). The thermosphere ionosphere coupling and the dynamic changes produced by storms in each of the thermosphere and ionosphere subsystems make the modeling difficult and lead to unacceptably large simulation uncertainties.

206 2.3 The path forward

There are two ways to mitigate the large forcing uncertainties during storms: measure the forcing, i.e. measure the electric fields and particle precipitation at the necessary grid points every few minutes, or use any available system measurements to estimate an appropriate forcing using a data assimilation scheme. As long as properly measuring the forcing is not possible the only practical solution is a sophisticated data assimilation process, that is, a data assimilation scheme that can take advantage of all available TI measurements to reduce the external forcing uncertainty while also improving
model data comparisons.

Developing an assimilation scheme that can take advantage of a variety of TI measurements is a major challenge because the external forcing acts in multiple ways with different time constants and because the system contains feed-back loops with stormtime dependent gains. These complications make the correlations between model variables non-stationary or in other words, state and time dependent. Since the covariance matrix depends on the present state of the system, it has to be calculated or estimated again during each assimilation time step.

One practical way to obtain the covariance is by Monte Carlo estimation methods (Evensen, 2003). An appropriate number of members of the background model (an ensemble) is run with representative forcing variations and statistics of their results are used to estimate a covariance matrix. The accuracy of the estimated covariance is a function of the number of members relative to the number of degrees of freedom of the system, the forcing distribution over the ensemble members, and the error of the system estimation, at the time of the estimation.

²²⁹ 3 The Thermosphere Ionosphere Data Assimilation (TIDA) Software

The Thermosphere Ionosphere Data Assimilation (TIDA) software implements an enKF for the TI system. Results from TIDA were first presented in (S. M. Codrescu et al., 2018), although the scheme was not called TIDA at the time. TIDA consists of three parts: the data assimilation code, the background Thermosphere Ionosphere general circulation model CTIPe (M. V. Codrescu et al., 2012), and supporting analysis routines in Python.

CTIPe has a long history going back to the early 1980's (T. J. Fuller-Rowell & Rees, 1980). The model has been running in real time (M. V. Codrescu et al., 2012) for more than ten years and has been tested during both quiet and disturbed conditions (Fedrizzi et al., 2012; M. V. Codrescu et al., 2012; Negrea et al., 2012; Fernandez-Gomez et al., 2019). CTIPe was transitioned into operations at the Space Weather Prediction Center (SWPC) in November 2019. Results from the SWPC real-time operational run are available at: http://ccmc-swpc.s3-website-us-east-1.amazonaws.com/plots.html

TIDA uses an ensemble of CTIPe model realizations to obtain a Monte Carlo style approximation of the non-stationary covariance matrix for the TI system. In this paper we will further explore neutral mass density assimilation during the severely disturbed 246 2003 Halloween storms.

TIDA is unique among data assimilation schemes in targeting strongly forced systems due to its handling of the system forcing. The Kalman state vector is augmented with the external system forcing and consequently the forcing is modified or inferred by the assimilated measurements. This inference allows the scheme to run even in the absence of L1 measurements. The forcing changes resulting from one assimilation time step are used during the following assimilation time step.

In addition to the ensemble members, TIDA also conducts a special member and a reference member. The special member is forced with the best estimate of the external system forcing as inferred in the previous assimilation step. The reference run is forced using the measurements of solar wind from the ACE spacecraft at L1 and F10.7 that would have been available in real-time. For the results presented here, we have used an ensemble with 75 members. The assimilation time step is 30 minutes and the model time step is one minute. The Kalman state vector, in addition to the augmented forcing parameters discussed above, contains the following fields: neutral temperature, constituent mixing ratios, meridional and zonal neutral winds, and mean molecular mass. The state vector contains over 191 thousand elements while the covariance matrix has over 36 million elements.

TIDA is a research tool that has a very large number of configuration options. Our 264 goal in this paper is to show that the assimilation scheme responds to the measurements 265 and their uncertainty as expected during a significant geomagnetic disturbance and to 266 also highlight that the assimilation scheme is able to use the neutral density measure-267 ments to estimate the forcing even in the absence or degradation of L1 measurements. 268 We do not claim that our configuration choices result in the best estimate of the system 269 forcing or the best possible TI simulation for this time period. We plan to tune the scheme 270 and use more diverse measurements to further improve results in the future. 271

272 **4 Data**

The neutral density measurements assimilated in this experiment are derived from very sensitive accelerometers flown on the GRACE-A, GRACE-B, and CHAMP satellites (Sutton, 2011). No bias correction was applied before assimilating the data. Furthermore, the estimated uncertainty provided with the measurements was used directly.

The Advanced Composition Explorer (ACE) satellite monitors the solar wind from the first Lagrange point (L1). Unfortunately, due to a solar energetic particle event, significant portions of the ACE data are bad quality and not usable during the storm period. We have retrieved the available data from the NASA OMNI service (https://omniweb .gsfc.nasa.gov/form/sc_merge_min1.html), which provides solar wind values propagated to Earth's magnetopause. During data gaps and outages, the most recent valid solar wind driver value is repeated across the gap.

284 5 Results

We first discuss results from a run where neutral density measurements from all 285 three satellites, GRACE-A, GRACE-B, and CHAMP, were assimilated. During most as-286 similation time steps, about 30 measurement/satellite were available for assimilation. Given 287 that fewer than 100 measurements were assimilated in each 30 minute assimilation time 288 step and that normal input parameters are not available for many hours during this pe-289 riod, the results are surprisingly good for such an extreme space weather event. Later 290 in this paper we'll discuss model measurement comparisons when measurements from 291 only one satellite are assimilated at a time, to demonstrate that this is not a lucky co-292 incidence but a consequence of the strongly forced nature of the TI system and of the 293 large scale coherence of the neutral density features in both the real system and in the 294 CTIPe model. We note that all results presented in this paper are along the orbit of the 295 moving satellites and are not orbit averaged. 296

Figure 1 is a scatter plot of model versus measurement results over the Halloween 297 storms (October 27 - 31, 2003). The left column labeled "Reference" illustrates the CTIPe 298 model results without data assimilation. This is what would have been produced by a 200 CTIPe real-time operational run. The middle column shows "Forecast" model results 300 from TIDA before the present assimilation time step measurements are assimilated, while 301 the right column shows the final "Analysis" TIDA neutral density results. The rows are 302 for the three satellite measurements used in this run: CHAMP (top row), GRACE-A (mid-303 dle row), and GRACE-B (bottom row). Forecast results can be thought of as assimila-304 tion results when only measurements older than 30 minutes are available while analy-305 sis means that measurements up to the simulation time are available. 306

p2/figures/scatter1.pdf

Figure 1. Scatter plot of model vs measurement when three satellite data sets are assimilated. Left column reference state (no assimilation), middle column forecast state, right column analysis state, over the 5 day Halloween 2003 storm period with all 3 satellite data sets assimilated.

The large overestimation of neutral density in the reference run (left column) is caused 307 by the loss of forcing measurements during October 30. The L1 measurements needed 308 for the convection and particle precipitation patterns were compromised by an ongoing 309 solar energetic proton event. Since the operational run must produce results even in the 310 absence of input measurements, the model reuses the last available forcing measurements 311 again and again until new forcing measurements become available. The last available L1 312 measurements for October 30 were such that they caused a large overestimation of the 313 Joule heating in the model, when repeated, resulting in much larger modeled neutral den-314 sity for corresponding measurements. 315

Figure 2 illustrates the forcing parameters for the sub-period 29 - 30 October, 2003. Both the reference forcing (blue) and TIDA forcing (yellow) are shown. The large magnitude of B in the YZ plane and the favorable angle together with the large solar wind velocity result in the large overestimation of Joule heating. The TIDA forcing parameters were inferred by the assimilation scheme from the neutral density measurements.

Neutral density measurements alone do not assure a unique solution for model forcing. The inferred forcing parameters presented in Figure 2 are a best estimate for the model forcing given the distribution of assimilated measurements and their uncertainties and the physics captured in the CTIPe model.

Changes in neutral density at the height of a satellite can result from a change in 325 temperature, a change in neutral composition, or a combination of both. Neutral den-326 sity measurements alone do not contain enough information to allow TIDA to uniquely 327 determine the cause of a model data discrepancy and properly correct for it during each 328 assimilation time step. This and the continuous change in the position of the satellite 329 measurements over the globe result in the ruggedness of the inferred system forcing. Ad-330 ditional measurements of temperature and/or neutral composition are expected to re-331 duce the variability of the inferred forcing and further improve model data comparisons 332 for neutral density. 333

Figure 3 shows the measured (yellow), reference (red), forecast (blue), and anal-334 ysis (black) neutral density values for October 29 and 30, 2003. The overestimation of 335 density by the reference run is again obvious on October 30. On the other hand, at times 336 TIDA slightly underestimates the neutral density. This is most obvious for CHAMP at 337 the end of October 30. We do not have a good explanation for this effect and plan to 338 investigate it further. We suspect the effect to be due to the arbitrary limits we imposed 339 on how much the forcing elements are allowed to change from one assimilation time step 340 to the next with a possible contribution from the non-optimal global coverage of the as-341 similation data sets. 342

Scatter plots like Figure 1 for the three single satellite assimilation cases are very similar, show only a little more spread than the 3 satellite assimilation case, are not discussed here but can be seen in Appendix A. The difference in forcing parameters inferred by TIDA for the four assimilation cases are minor, do not bring any revelations, and again are not presented here. The difference in TIDA results when assimilating all data sets at once or one at a time can best be seen in Table 1.

349 Table 1 summarizes the assimilation results over the 5 day period. The results of the wrong inputs forced upon the reference run by the absence of L1 measurements due 350 to the proton event contamination is obvious and totally unacceptable for an operational 351 run. Using previous neutral density measurements, i.e. measurements made before the 352 present 30 minute assimilation time step, TIDA can infer better system forcing param-353 eters and reduce the along the orbit RMSD from over 140% (CHAMP Reference) to be-354 low 21% (CHAMP Forecast) and from over 203% (GRACE-A and B Reference) to less 355 than 26% (GRACE-A and B Forecast). The assimilation of the measurements during 356

p2/figures/plot-forcings1.pdf

Figure 2. Forcing measured or assumed for the reference run (blue) and inferred by TIDA from neutral density measurements alone (yellow).

p2/figures/plot-density1.pdf

Figure 3. Neutral density observed (yellow), reference (red), forecast (blue) and analysis (black) for the three satellites during October 29 and 30, 2003

the assimilation time step further reduces the RMSD to less than 16.5% for CHAMP and to less than 15% for GRACE-A and B.

It is obvious from Table 1 that the best TIDA neutral density results are obtained when all 3 satellite data sets are assimilated at the same time. The fact that the TIDA results are better for any satellite when assimilating all measurements than when assimilating only a particular satellite is evidence that the data sets are consistent with each other, have only small biases relative to each other, and that the model approximates the physics of the system well enough to be able to improve the results far away from the location of any given measurement.

6 Conclusions

We have developed TIDA, an enKF data assimilation software package adapted for strongly externally-forced systems. The strongly forced system requires the estimation of the system forcing parameters at each assimilation time step. This is because the forcing uncertainties are the largest source of uncertainty for model results. In addition, the non-stationary nature of the system encourages the estimation of the covariance matrix during each assimilation time step.

Including the external system forcing parameters in the Kalman state of TIDA allows their estimation based on all system measurements and results in considerable improvement in modeling results. Given enough system measurements, the forcing parameters can be inferred even in the absence of the regular forcing measurements (L1 solar wind and F10.7 values). This can assure uninterrupted modeling operations even when model inputs are not available.

TIDA, the implementation of the enKF used in this study, demonstrates the considerable improvement potential of data assimilation for the TI system modeling. A small number of measurements, fewer than 100 neutral density values assimilated during each 30 minute assimilation time steps over 5 days, can reduce the model data RMSD along the orbit be factors of 7 to 10 vs the reference with bad forcing. Furthermore, we have demonstrated that assimilation of the neutral density from a single satellite improves the specification globally.

The TIDA results further indicate that the estimation of the neutral density covariance matrix with a 75 member ensemble of CTIPe runs is good enough to eliminate the need for covariance localization. This is essential, given the sparse data coverage of neutral density available today.

³⁹⁰ Appendix A Individual satellite scatter plots

391 Acknowledgments

³⁹² The CTIPe model code is open source. A GitHub Docker version of CTIPe is available

³⁹³ upon request. Please email Mihail Codrescu (Mihail.Codrescu@noaa.gov) if interested.

³⁹⁴ The TIDA code is commercially available from Vector Space, LLC. Please Email Ste-

fan Codrescu (ssmmcc1@gmail.com) if interested. The CHAMP and GRACE-A and B

neutral density measurements were provided by Eric Sutton and are available at: https://

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		All sats		Only CHA	AMP	Only GR	ACE-A	$Only \ GRA$	ACE-B
ellite	Reference	Forecast	Analysis	Forecast	Analysis	Forecast	Analysis	Forecast	Analysis
AMP	140.25	20.67	16.37	21.82	18.06	21.87	20.37	21.90	20.24
ACE A	205.68	25.72	14.97	25.83	24.15	26.55	18.83	26.63	18.88
ACE B	203.71	25.61	14.98	25.65	23.95	26.50	18.93	26.48	18.85

Table 1. Root Mean Square % difference for Reference, Forecast, and Analysis over the 5 day Halloween 2003 storm period.

p2/figures/scatter2.pdf

Figure A1. Scatter plot of model vs measurement when only the CHAMP satellite data set is assimilated. Left column reference state (no assimilation), middle column forecast state, right column analysis state, over the 5 day Halloween 2003 storm period.

p2/figures/scatter3.pdf

Figure A2. Scatter plot of model vs measurement when only the GRACE-A satellite data set is assimilated. Left column reference state (no assimilation), middle column forecast state, right column analysis state, over the 5 day Halloween 2003 storm period.

p2/figures/scatter4.pdf

Figure A3. Scatter plot of model vs measurement when only the GRACE-B satellite data set is assimilated. Left column reference state (no assimilation), middle column forecast state, right column analysis state, over the 5 day Halloween 2003 storm period.

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Figure 1.

2003 Halloween Storm: neutral mass density: all satellites assimilated



Figure 2.



Figure 3.



Figure 4.

2003 Halloween Storm: neutral mass density: only CHAMP assimilated



Figure 5.

2003 Halloween Storm: neutral mass density: only GRACE-A assimilated



Figure 6.

2003 Halloween Storm: neutral mass density: only GRACE-B assimilated

