

# Shocklet structure of very high-beta Earth bow shocks

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November 23, 2022

## Abstract

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However, such shocks are supposed to be ubiquitous in astrophysical plasmas.

We present statistics of several tens  $\beta > 10$  shocks for MMS, Cluster and Geotail,

26 of which have  $\beta > 30$ . For the latter subset the most of

crossings reveal very complex structure with quasi periodic shocklets,

gradually thermalising the solar wind ion flow. One fortuitous MMS shock event

allowed to study this phenomenon with unprecedented details. Each shocklet, in turn, consists

of very high-amplitude magnetic oscillations with the period about 1 sec, coupled with the pulses of the plasma flow. These variations have wavelength about 150 km and are almost standing in the plasma rest frame, consistent with the expectation for Weibel mode.

All together, the transition interval may last 5–10 min, but corresponds to a proton cyclotron scale in the solar wind, due to very low magnetic field and very slow shock motion.

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## Key Points:

- 26 Earth bow shock crossings with extreme solar wind  $\beta > 30$  are catalogued during 1995–2020.
- Many crossings have peculiar layout with many periodic (5–20 sec) shocklets.
- Shocklets are filled with partially thermalised plasma, bunched in one-second flow pulses coupled with strong magnetic variations.

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**Abstract**

Observations of Earth's bow shock with very high  $\beta \geq 10$  (ratio of thermal to magnetic pressure) are extremely rare. However, such shocks are supposed to be ubiquitous in astrophysical plasmas. We present statistics of several tens  $\beta > 10$  shocks for MMS, Cluster and Geotail, 26 of which have  $\beta > 30$ . For the latter subset the most of crossings reveal very complex structure with quasi periodic shocklets, gradually thermalising the solar wind ion flow. One fortuitous MMS shock event allowed to study this phenomenon with unprecedented details. Each shocklet, in turn, consists of very high-amplitude magnetic oscillations with the period about 1 sec, coupled with the pulses of the plasma flow. These variations have wavelength about 150 km and are almost standing in the plasma rest frame, consistent with the expectation for Weibel mode. All together, the transition interval may last 5–10 min, but corresponds to a proton cyclotron scale in the solar wind, due to very low magnetic field and very slow shock motion.

**Plain Language Summary**

Collisionless shocks are very frequent and important objects in astrophysical plasmas. Earth's bow shock allow to study them in detail with in-situ experiments. However not all shock types are readily available in the solar wind. We present the detailed analysis of very rare shock with very low magnetic field.

**1 Introduction**

Earth's bow shock is the only readily accessible for in-situ measurements example of space collisionless shocks. In the rarefied magnetised plasmas a wide variety of shock types exists with quite differing structure (Kennel et al., 1985). The magnetic field vector is a key parameter in the Rankine-Hugoniot equations, governing the relation between upstream and downstream conditions. However, in the absence of collisions, specific kinetic mechanisms of field-particle interactions govern bulk flow slow-down and acceleration of some particles (Sagdeev, 1966; V. Krasnoselskikh et al., 2013). In the quasi-perpendicular shock geometry (when the angle between the shock normal and the upstream magnetic field is closer to  $90^\circ$ ) ions cannot escape upstream and a step-like shock transition forms with the overall width of several thousand km. In the quasi-parallel geometry (the angle is closer to  $0^\circ$ ) ions are capable to escape upstream along the magnetic field, a shock transition smears to the scales around several Earth radii, ions are efficiently accelerated locally, downstream flow becomes very structured (Scudder et al., 1986; Burgess et al., 2005; Turner et al., 2018; Plaschke et al., 2018).

Kinetic mechanisms evoke at a shock front low frequency (from one tenth to few Hz) and high-amplitude magnetic variations, actually dissipating ions. The specific unstable wavemode depends on magnetic geometry,  $\beta$ , Mach number, etc. In a supercritical quasi-perpendicular shock, the oblique whistler waves ( $\sim 5$  Hz) form the magnetic jump (V. V. Krasnoselskikh et al., 2002). In quasi-parallel shocks, series of substructures, known as SLAMS or shocklets, are formed, which gradually thermalise plasma flow (Lefebvre et al., 2009).

However, solar wind plasmas do not exhibit the whole range of parameters, defining the shock types. In particular, shocks in a weak magnetic field environment (high- $\beta$  shocks) are common in interstellar and intergalaxy space (Markevitch & Vikhlinin, 2007; Donnert et al., 2018).  $\beta$  is a dimensionless parameter, the ratio of plasma thermal to magnetic energy density. Typical  $\beta$  in solar wind is around unity, shocks with  $\beta > 10$  are rather rare, and only several dozens of cases with  $\beta$  closer to a hundred are potentially available.

Only very few examples of high- $\beta$  events have been investigated. Formisano et al. (1975) presented three cases of OGO-5 spacecraft observations with  $\beta$  equal to 8, 170, 49, mentioning large magnetic field excursions. Winterhalter and Kivelson (1988) stated that shock appearance with high-amplitude magnetic variations is typical for the cases with higher  $\beta$ . Farris et al. (1992) investigated one shock with  $\beta$  equal to 18, checking the validity of Rankine-Hugoniot conditions and also mentioning high-amplitude magnetic variations.

In our previous investigation (Petrukovich et al., 2019) (hereafter cited as PCS19) we conducted a thorough analysis  $\beta > 10$  occurrence in solar wind and of shocks in such conditions. A verified dataset of 22 shock crossings, observed by Cluster multispacecraft mission with the minimal spacecraft separation from several tens to couple hundred km, was presented. Intervals with  $\beta > 10$  are related with the low speed, high density solar wind flow and very low interplanetary magnetic field 1–2 nT and are often quite transient. Discovered relatively compact large-scale structure of the observed shock transitions (about couple of minutes) is similar to that earlier reported for oblique and quasi-perpendicular shocks. It is distinctly different from the structure of quasi-parallel shocks, which are extended up to several Earth radii (Burgess et al., 2005). The apparent increased width of the magnetic jump (up to about 30 seconds) is mostly related with the slow shock motion and increased cyclotron radius. Observed magnetic variations are different from that for supercritical shocks with  $\beta \sim 1$ . Dominating magnetic variations in the shock transition have amplitudes much larger than the background field and frequency of  $\sim 0.3$ – $0.5$  Hz (in some events — 1–2 Hz). The wave polarisation has no stable phase and is closer to linear, complicating determination of the wave propagation direction. The spatial scales (wavelengths) of variations are within several tens to couple hundred km.

In this publication we continue investigation of high  $\beta$  shocks with the substantial increase of statistics of verified crossings, including almost the full list for  $\beta > 30$ . This latter set is specially screened for any possible peculiarity of the shock structure. And, in fact, a novel type of shock profiles is found, rather typical for  $\beta > 30$  and almost not observed in lower  $\beta$  events (10–30). It is in a sense, intermediate between quasi-parallel and quasi-perpendicular profiles. The crossing is quite compact (about ten min between undisturbed solar wind and magnetosheath), but consists of quasi periodic enhancements (shocklets), gradually thermalising the flow and merging in the downstream state. Using a fortuitous event, registered by MMS, we are able to trace ion dynamics down to the subsecond range, revealing stunning periodicities. We also discuss statistics of other observations.

## 2 Assembling the shock statistics

High- $\beta$  shocks crossings are not frequent and usually clustered at the occasions of the specific solar wind with low bulk speed, high number density and low IMF (see PCS19 for the detailed solar wind statistics and details of the search procedure). We used 1-hour OMNI data set to automatically find hours with  $\beta > 10$  and a spacecraft within  $5 R_E$  from the model bow shock (Farris et al., 1991). All observations during 1995–2020 with Geotail, Interball, THEMIS, Cluster, MMS spacecraft are checked. For this initial look-out we take OMNI, ephemeris and spin-averaged magnetic field from CDAWeb archive.  $\beta$  values are precalculated in OMNI-2, assuming constant electron temperature (140000 K), He++ fraction (0.05) and He++ temperature (four times larger than proton temperature).

For each selected hour (in OMNI), the 5-hour window around it is reviewed visually. We pick up only crossings with the clear jumps in magnetic field and ion moments, as well as located within the stable high  $\beta > 10$  intervals (here 1-min OMNI was used). Such a criterion may result in missing some quasi-parallel shocks, which have very smeared

107 profiles, but the expected proportion of such events should be rather small, assuming uni-  
108 form distribution of IMF direction relative to shock normals.

109 This preliminary list contains several hundred candidate events. They, however,  
110 need further confirmation, regarding local upstream  $\beta$  value, data availability etc. We  
111 also excluded partial crossings, and crossings that occurred at a sharp  $\beta$  (mostly ion den-  
112 sity) change. In PCS19 we selected and verified 22 Cluster project events for 2003–2012  
113 with the relatively small separation (few tens or couple hundred km) between at least  
114 two spacecraft. This criterion was chosen in PCS19 to estimate the spatial scale of high-  
115 amplitude magnetic variations, forming the shock transition. Hereafter, for the sake of  
116 completeness, it is listed in Table S4 in Supplement.

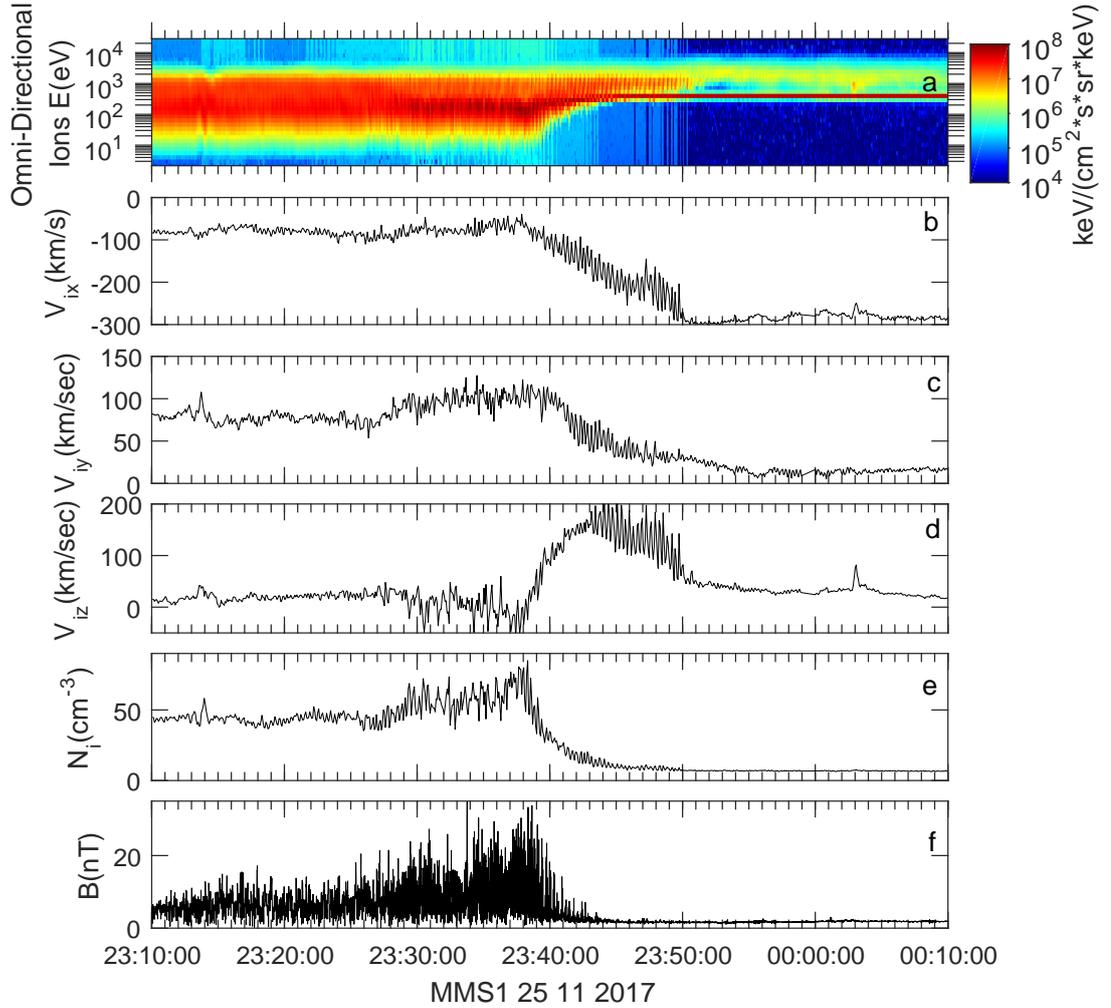
117 In the current publication we add several new verified subsets. Table S2 contains  
118 20 crossings of MMS spacecraft for 2017–2020, optimal to study plasma dynamics with  
119 high temporal resolution and to determine spatial scales. Several cases with actual  $\beta <$   
120 10 were left in this dataset to facilitate any comparisons in future. Table S3 contains 20  
121 crossings of Geotail spacecraft with  $\beta > 10$ . We also checked Interball and THEMIS  
122 crossings, but mostly they occurred with no high-resolution (16 Hz) magnetic field data,  
123 which are necessary to identify some important details of shock crossings (see PCS19 and  
124 below). Therefore, we do not provide separate tables for these spacecraft.

125 The main topic of this investigation, a collection of shocks with very high  $\beta > 30$   
126 is listed in Table S1 with 26 events for 1995–2020 years. The scope of Table S1 is wider,  
127 then just a subset of Tables S2,S3,S4. Geotail and MMS Tables S2 and S3 indeed have  
128 the almost full coverage (events were excluded only basing on quality requirements). The  
129  $\beta > 30$  events from Tables S2 and S3 are just copied to Table S1. Besides that, for Ta-  
130 ble S1 we additionally looked through THEMIS and Interball crossings, as well as through  
131 Cluster crossings, not covered by the Table S4 (which has the additional strongly restrict-  
132 ing criterion on spacecraft separation distance). The threshold  $\beta = 30$  as a character-  
133 istic of extreme cases was selected to keep the list substantial, but short enough, and is  
134 justified with further investigation.

135 Finally for the Table S1 we rechecked variability of upstream  $\beta$ . The main  $\beta$  vari-  
136 ant, used in all tables, is the OMNI value, taken at 1-min point nearest to the shock cross-  
137 ing. Additionally we provide in Table S1 OMNI  $\beta$  and total magnetic field averaged within  
138 12 min intervals, centred at the shock crossings. We also compute the local  $\beta$  estimate  
139 at some unperturbed solar wind interval, nearest to the shock. Since plasma measure-  
140 ments by MMS, Cluster, Geotail, Interball, THEMIS, are not exactly comparable with  
141 that of the interplanetary spacecraft, we use only local magnetic field for our estimate.  
142 We adjust OMNI  $\beta$  with the squared ratio of local upstream magnetic field and OMNI  
143 IMF. Since IMF is more variable, than the solar wind ion moments, and affects  $\beta$  strongly  
144 with a square law, such an approach looks quite reasonable.

145 Though three variants of  $\beta$  values (columns I,J,K in Table S1) are sometimes very  
146 different, there is no definite systematic change (e.g., overestimate in OMNI), except some  
147 extreme large OMNI  $\beta > 100$  are actually smaller locally. It is quite reasonable, since  
148 extreme  $\beta$  appear, when IMF is occasionally very close to zero. Such dropouts could be  
149 relatively small structures, which may evolve between L1 point and a bow shock. The  
150 detailed discussion of OMNI  $\beta$  variability and reliability is in PCS19.

151 For analysis we used full-resolution Cluster FGM magnetic field (here with the sam-  
152 pling  $\sim 20$  Hz) (Balogh et al., 2001) and HIA/CODIF ion data (sampling once in 4–12  
153 s, depending on a parameter) (Rème et al., 2001) from Cluster Science Archive, Geotail  
154 MGF (Kokubun et al., 1994) (16 Hz) and LEP (Mukai et al., 1994) (12 sec) data from  
155 DARTS ISAS archive, Interball magnetic field (Nozdrachev et al., 1998) (16 Hz), Level  
156 2 THEMIS FGM (16 Hz) and ESA (3 sec) (Angelopoulos, 2008; Auster et al., 2008; Mc-  
157 Fadden et al., 2008), MMS MGF (Russell et al., 2016) (128 Hz) and FPI (Pollock et al.,



**Figure 1.** Overview of MMS crossing for event 25 November 2017. (a) ion omnidirectional spectrogram, (b-e) ion velocity and density, (f) magnetic field magnitude.

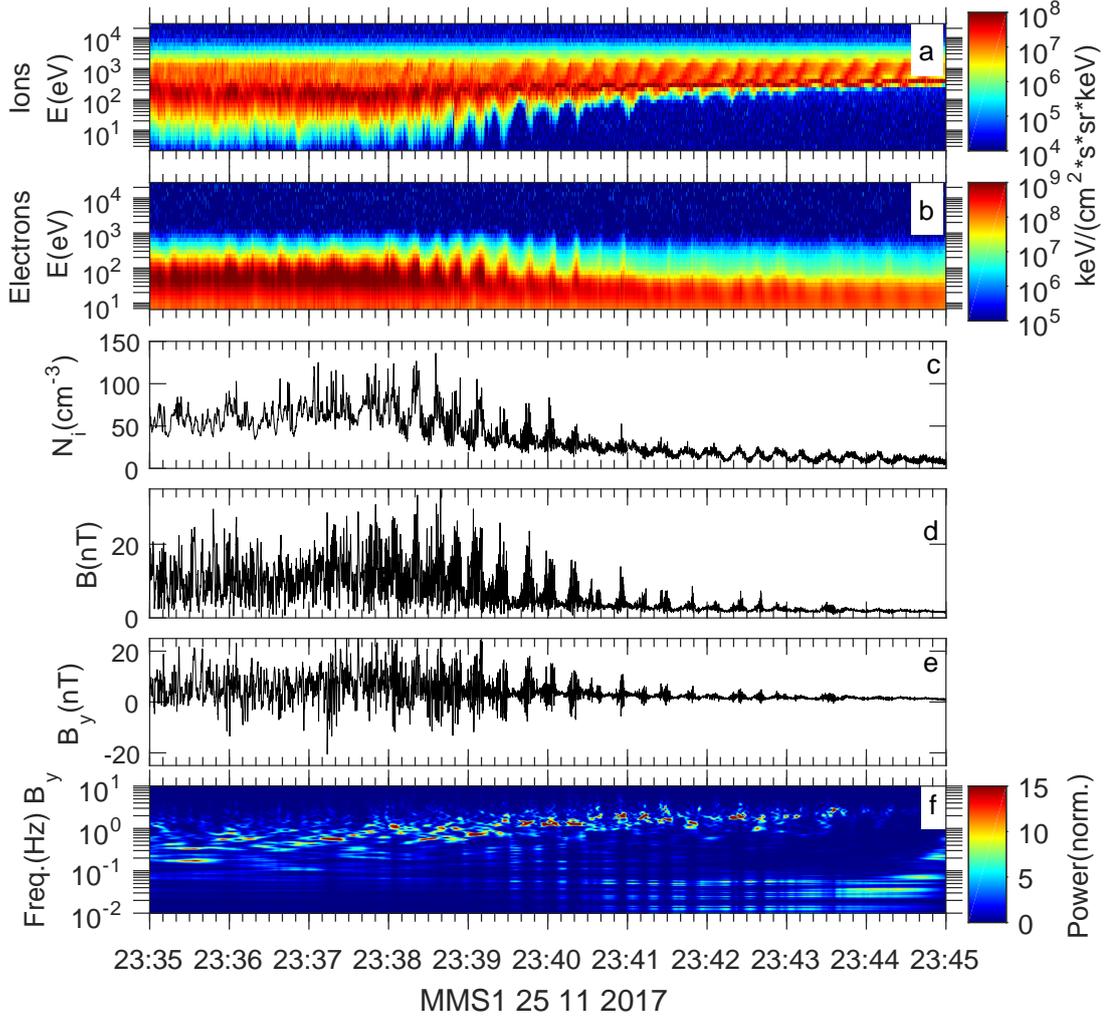
158 2016) (0.1 Hz in Burst mode) data from CDAWeb archive. All vectors in this paper are  
 159 in GSE frame of reference. In the next section MMS1 data are used, if not explicitly men-  
 160 tioned otherwise.

### 161 3 Shock example

#### 162 3.1 General structure

163 The shock crossing of interest occurred on 25 November 2017 around 23:40 UT.  
 164 It is the only MMS event with the described phenomenon, but, fortunately, it is also a  
 165 brightest example. The interval 23:10–00:10 UT covers the large-scale view (Figure 1).  
 166 MMS Fast mode data are used in this figure. The shorter interval 23:35–23:45 UT of the  
 167 Burst mode is in Figure 2.

168 MMS spacecraft are sunward and somewhat duskward from Earth with the space-  
 169 craft separation about 30 km. OMNI solar wind speed is small  $\sim 335$ – $340$  km/s, density



**Figure 2.** Overview of MMS crossing for event 25 November 2017, for the burst mode interval. (a) ion omnidirectional spectrogram, (b) electron omnidirectional spectrogram, (c) ion density, (d) magnetic field magnitude, (e)  $B_y$  magnetic field, (f) wavelet dynamic spectrum of magnetic field  $B_y$ .

170 is moderately high  $\sim 9 \text{ cm}^{-3}$  (all characteristics are in Table S1 or S2). According to 1-  
 171 min OMNI data, IMF magnitude is 0.9 nT, resulting in very high  $\beta = 66$  and Alfvén  
 172 Mach number  $\sim 60$ . Magnetosonic Mach number is 7. These values are stable on a scale  
 173 of one hour. Local (measured by MMS) solar wind ion bulk speed is somewhat less than  
 174 300 km/s, but one should note, that FPI is not a dedicated solar wind instrument. Up-  
 175 stream electron bulk velocity (not shown here) is closer to the OMNI value. Local IMF  
 176 (e.g., at 23:50 UT) is about twice larger than that in OMNI, resulting in local upstream  
 177  $\beta$  only about 16. However, this crossing has substantial amount of reflected ions, which  
 178 may lead to some increase of magnetic field in the foreshock.

179 The model shock normal (Farris et al., 1991) is almost sunward, and the resulting  
 180  $\theta_{Bn}$  angle is  $68^\circ$  for OMNI magnetic field and  $59^\circ$  for local magnetic field, so the shock  
 181 geometry is determined reliably and is close to quasi perpendicular. The compression  
 182 ratios of magnetic field and ion density are close to four, typical for supercritical shocks.

183 However, for about of couple of minutes 2335–2340 UT the ion density is up to 2–3 time  
 184 higher than the final downstream value. We place the main shock transition at 23:38–  
 185 23:39 UT, when magnetic field and ion density stably reach the downstream level.

186 The plasma flow completely relaxes well behind the shock front, approximately at  
 187 2325 UT (Figure 1), when oscillations in ion density and bulk velocity subside. The fi-  
 188 nal downstream bulk velocity is  $\approx$ –80, 80, 10 km/s both for ions and electrons. The mag-  
 189 netosheath plasma flow here is close to stagnation, because of proximity to the magne-  
 190 topause.

191 Substantial suprathermal ion population is also present upstream. The transition  
 192 zone can be identified qualitatively as 23:38–23:50 UT, basing on the substantial pres-  
 193 ence of reflected ions, affecting the ion bulk velocity components. Taking into account  
 194 very low magnetic field, as well as, very low (expected, see Sec. 5) speed of the shock  
 195 motion, the spatial length of this 12-min interval is actually of the order of a proton cy-  
 196 clotron radius in solar wind.

197 The main peculiar feature of this shock transition is rich variability (Fig.2). The  
 198 dominating upstream signature are the periodic enhancements of ion density and mag-  
 199 netic field with the stable frequency 0.05–0.06 Hz (period slightly smaller than 20 sec-  
 200 onds, Fig. 2f). We name such enhancements as shocklets, similar to a quasi-parallel shock.  
 201 Amplitudes of shock lets grow towards downstream, and finally these enhancements merge  
 202 in a continuous downstream state. Electron spectrogram (Fig. 2b) reveals periodic en-  
 203 ergy and density increases, following magnetic field changes. Ion spectrogram (Fig. 2a)  
 204 reveals substantial changes of ion populations also inside shocklets, which are described  
 205 in detail in the next subsection. Each such shocklet, being formally located upstream,  
 206 actually contributes to thermalisation of the ion flow. Another characteristic oscillation  
 207 of magnetic field and ion density is embedded inside shocklets. It has the frequency about  
 208 0.5–2 Hz, decreasing towards downstream (Fig. 2f).

209 In the following we concentrate on the interval 23:38–23:45 UT with the most pro-  
 210 nounced periodic structures and select three characteristic shocklets. However, it is al-  
 211 most impossible to describe all observed details in a single investigation. In particular,  
 212 we leave the reconstruction of the full 3D ion kinetics to the future studies.

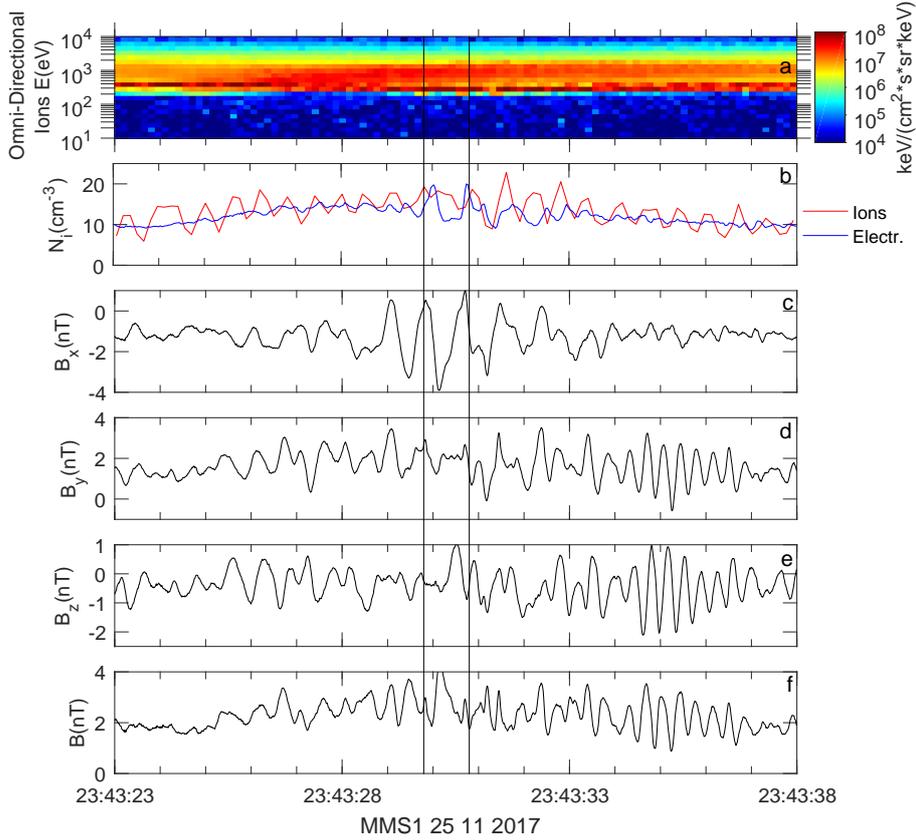
### 213 3.2 Shocklets

214 We choose three intervals, each including one "shocklet": #1 in the distant upstream  
 215 with 23:43:23–23:43:38 UT , #2 in more mature foreshock 23:40:14–23:40:26 UT, and  
 216 #3 almost at a shock front, but still upstream, 23:39:00–23:39:12 UT (Figures 3–8).

217 The upstream shocklet #1 occurs on the background of almost undisturbed solar  
 218 wind and IMF, mostly as an enhancement of the net magnetic field magnitude from 2  
 219 to 3 nT and of ion density from 10 to 15  $\text{cm}^{-3}$  (Fig.3).All specific shocklet signatures,  
 220 described here, are more developed and evident in shocklets #2 and #3). In a more de-  
 221 tailed view, the magnetic magnitude enhancement consists of the magnetic variations  
 222 with the amplitudes of the order of the background IMF. In the ion overview data (en-  
 223 ergy spectrograms, Fig. 3a, Fig. 4), this magnetic and density enhancement is accom-  
 224 panied by a slight slowdown and rotation of the solar wind flow towards the future down-  
 225 stream state, as well as by the appearance of the Earth-streaming high-energy compo-  
 226 nent (in  $-X$  spectrogram of Fig. 4).

227 The reflected ions in  $+X$  and  $+Z$  are present not only in shock lets, but also through-  
 228 out the foreshock.  $+X$  flow is more intense towards the shock-ward edge of the shock-  
 229 let, but their energy increases towards upstream.

230 There is also a stable ion density periodicity  $\leq$ 1 sec (Fig. 3b). It likely corresponds  
 231 to the known caveat of MMS measurements in the solar wind: the narrow solar wind ion

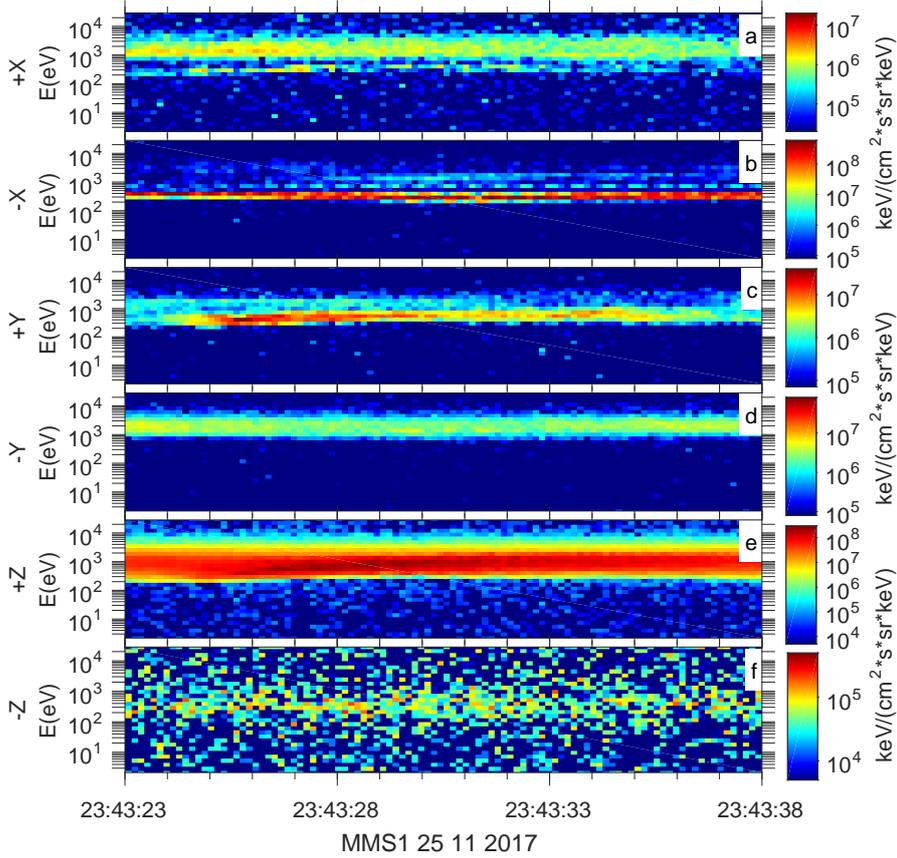


**Figure 3.** Overview of shocklet #1. (a) ion omnidirectional spectrogram, (b) ion and electron density, (c-f) magnetic field vector and magnitude. Vertical lines denote two plasma density peaks.

232 beam periodically falls in between the FPI sensors. The 20-sec spacecraft period and 32  
 233 FPI azimuthal sectors result in a  $20/32=0.65$  s period, close to the observed one. Simul-  
 234 taneous electron density data confirm only two substantial density spikes (23:43:30, 23:43:31),  
 235 which coincide with the maxima in  $B_x$ .

236 There are two clear wave packets. The first one at 23:43:34–23:43:37 UT is mostly  
 237 in  $B_y$  and  $B_z$  components and with frequency 2.75 Hz. Its main wave characteristics are  
 238 in Table 1. The temporal delays between MMS spacecraft are of the order of 0.1 sec, al-  
 239 lowing reliable multipoint analysis (not shown here in detail). It is an elliptically polarised  
 240 wave with the clear minimum variance direction, just  $10^\circ$  away from the timing normal.  
 241 The variance matrix was built using all four satellites to improve statistical accuracy.  
 242 The Doppler shift in frequency is approximately equal to the observed frequency, sug-  
 243 gesting the almost standing wave in the plasma rest frame. However, the timing veloc-  
 244 ity vector is not parallel to the nominal bulk flow velocity.

245 The second wave packet at 23:43:28–23:43:33 UT is mostly in  $B_x$ , has the linear  
 246 polarisation (Table 1) and lower frequency. The maximum variance vector is orthogo-  
 247 nal (within  $10^\circ$ ) to local magnetic field and the timing normal. The propagation direc-  
 248 tion (timing normal) is pointed closer to the final direction the downstream flow. As in  
 249 the previous case, the Doppler shift is of the order of the observed frequency.



**Figure 4.** Ion spectrograms for six directions for shocklet #1.

250 The second sample shocklet (23:40:14–23:40:26 UT) occurs already in a substan-  
 251 tially decelerated solar wind flow with the increased ion density ( $20\text{--}30\text{ cm}^{-3}$ ) and mag-  
 252 netic field ( $3\text{--}5\text{ nT}$ ) (Figure 5).

253 The magnetic field magnitude temporary enhancements are up to  $10\text{--}15\text{ nT}$ , mostly  
 254 in  $B_y$  and  $B_z$  components. Both ion and electron density peak up to  $50\text{ cm}^{-3}$ . The prop-  
 255 erties of the clear magnetic wave packet 23:40:15–23:40:21.5 UT with linear polarisation  
 256 are listed in Table 2 and are similar to that of the linearly polarised packet in the shock-  
 257 let #1 (23:43:28–23:43:33 UT), as concerns frequency, velocity, maxvar direction, wave-  
 258 length and Doppler shift. The peaks in magnetic field magnitude correspond to the ex-  
 259 trema of components. Peaks in ion and electron density often correspond to (almost) max-  
 260 ima of  $B_x$ , but this feature is not confirmed on statistics.

261 The solar wind flow before and after Shocklet #2 is already substantially deceler-  
 262 ated and is further thermalised within the shocklet (Fig. 6). There is also significant amount  
 263 of high energy reflected ions. Sporadically low energy ions around 100 eV appear. The  
 264 large density peaks correspond to clear enhancements of the magnetosheath-like ion flow  
 265 ( $\sim(-160, 90, 50)\text{ km/s}$ ). The intervals between density peaks are almost void of the magnetosheath-  
 266 type flow, contain less low energy and more high energy ions, including downstream di-  
 267 rected ( $-X$ ) 1000–2000 eV ions (23:40:15–23:40:18 UT). This small-scale bunching of the  
 268 shocklet flow is barely visible in shocklet #1, is evident here, and is much more promi-  
 269 nent in shocklet #3.

**Table 1.** Wave analysis data for shocklet #1.

Parameter	23:43:34–23:43:37 UT	23:43:28–23:43:33 UT
magnetic field, nT	-1.18, 1.42, -0.36	-1.21, 1.84, -0.38
ion bulk flow, km/s	-220, 55, 120	-180, 60, 150
peak frequency, Hz	2.75	1.2
eigenvalues	0.068 0.47 0.57	0.26 0.34 1.67
min(max) var vector	0.997, -0.050, 0.055	-0.87, -,0.46, -0.21
spacecraft delays vs MMS1, s	0.078, 0.039, -0.047	0.117, 0.117, 0.094
multipoint timing normal	0.992, -0.0404, -0.119	0.603, -0.760, -0.243
timing velocity, km/s	200.4	196
wavelength, km	72	163
Doppler shift, Hz	~3	~1.3
$\theta_{kB}$	~40°	~35°

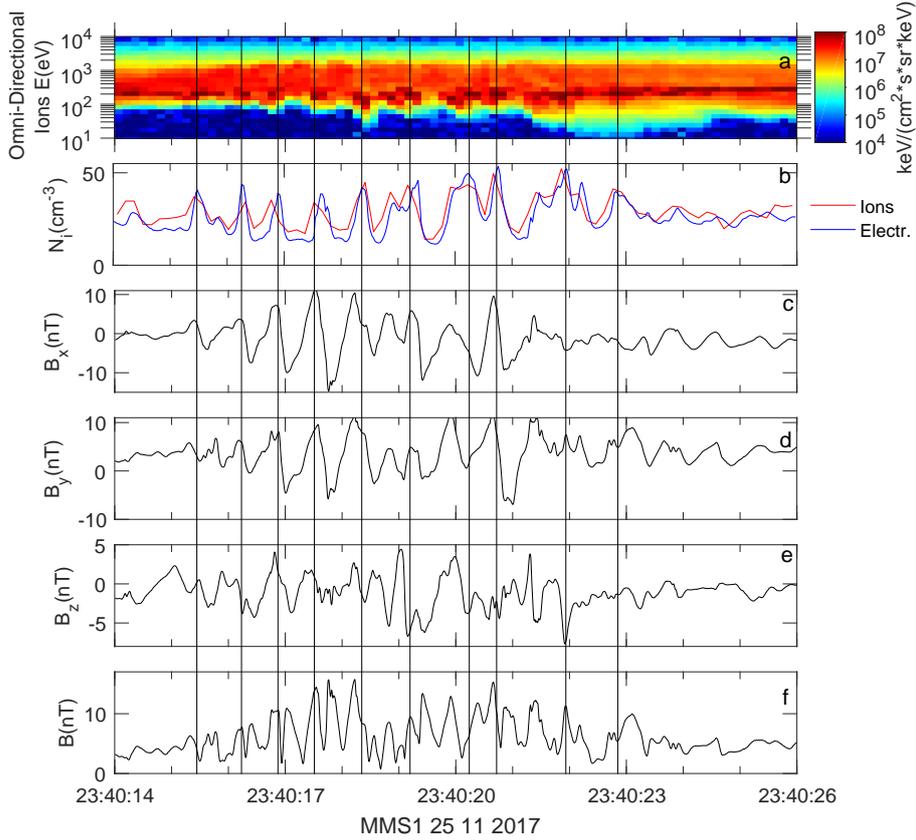
**Table 2.** Wave analysis data for shocklets 2 and 3.

Parameter	shocklet 2	shocklet 3
magnetic field, nT	-0.93, 3.63, -0.82	-1.67, 4.06, -1.17
ion bulk flow, km/s	-150, 90, 100	-100, 110, 70
peak observed frequency, Hz	1.25	0.8
eigenvalues	4.72, 5.78, 46.2	16.47, 19.49, 117.72
max var vector	0.8132, 0.5768, 0.0777	0.86, 0.47, 0.17
spacecraft delays vs MMS1, s	0.133, 0.133, 0.109	0.164, 0.171, 0.148
multipoint timing normal	0.591, -0.774, -0.230	0.539, -0.801, -0.262
timing velocity, km/s	173	139
wavelength, km	138	173
Doppler shift, Hz	~1.3	~0.9
$\theta_{kB}$	~35°	~35°

270 The third sample shocklet (23:39:00–23:39:12 UT, contains almost magnetosheath  
271 type plasma (Fig. 7,8), but still is attributed to foreshock, since it is enveloped in the  
272 less thermalised solar wind flow. It also contains a typical magnetic wave packet at 23:39:00–  
273 23:39:09 UT. The magnetic field oscillations (5–30 nT) are mostly in  $B_x$  and  $B_y$  com-  
274 ponents. The properties of the packet are listed in Table 2 and are similar to that in shock-  
275 let #2, but the frequency is somewhat lower and the wavelength longer.

276 At least six clear ion density bursts, of the order of 1-sec duration and amplitudes  
277 up to  $100 \text{ cm}^{-3}$ , are coupled with magnetic variations. The density variations are almost  
278 identical in electron and ion data and the delays between the spacecraft are almost the  
279 same for magnetic field and density (see Figure 9 for a detailed plot). It should be noted,  
280 however, that while the magnetic field sampling 128 Hz is sufficient to measure delays  
281 of the order of 0.15 s reliably, the density sampling is marginally sufficient only to con-  
282 firm delays equal to one sampling interval. Thus, it is not possible to make an indepen-  
283 dent timing of density peaks with the accuracy comparable with that for magnetic field  
284 time profiles. Also, there is no any clear correlation between density peaks and magnetic  
285 field magnitude and direction.

286 Ion spectrograms of shocklet #3 are similar to that of shocklet #2, but contain more  
287 thermalised plasma. The down-streaming hot ions are enhanced during the shocklet. The  
288 one-second flow periodicity is very well developed here. For example, during the ion den-



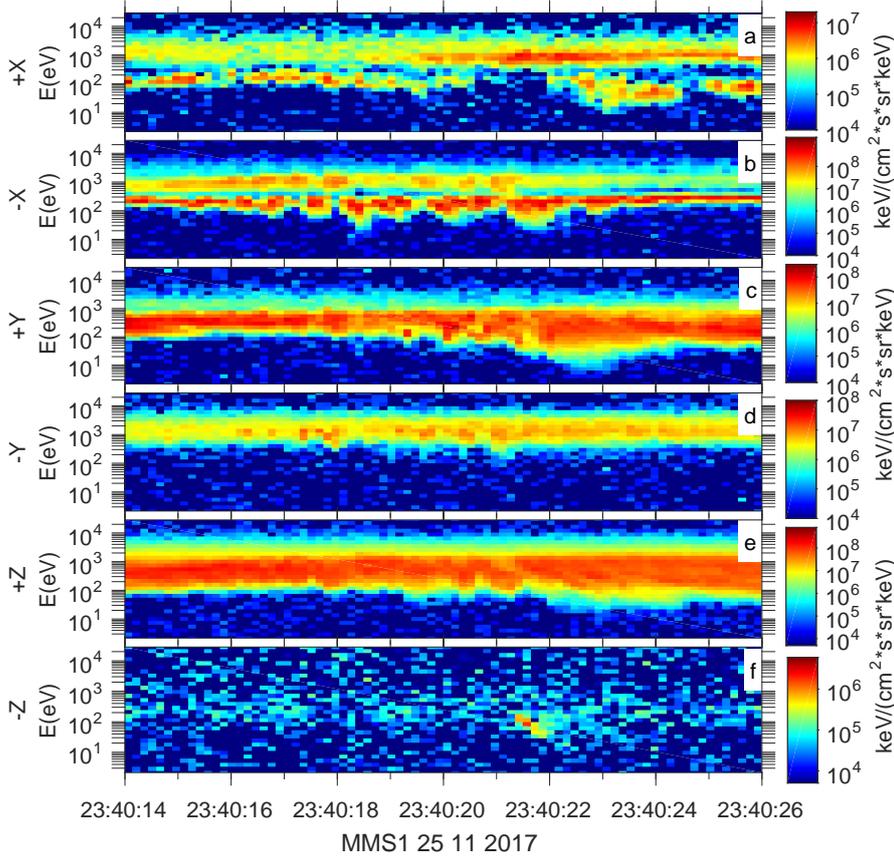
**Figure 5.** Overview of shocklet #2. (a) ion omnidirectional spectrogram, (b) ion and electron density, (c-f) magnetic field vector and magnitude. Vertical lines denote two plasma density peaks.

289      sity burst (23:39:06.120–23:39:06.870 UT) the ion flow has clear magnetosheath like di-  
 290      rection  $\sim(-124, 95, 10)$  km/s, but still is different from the finally relaxed state  $\sim(-80,$   
 291      80, 10) km/s. In the "gap" interval 23:39:07.020–23:39:07.470 UT there is much less magnetosheath-  
 292      like flow and much more other ion populations, including upstreaming cold ions (100 eV)  
 293      and downstreaming hot ions (1000 eV).

#### 294      4 Other examples

295      The review of very high  $\beta$  crossings in Table S1 reveals that a quasi-periodic struc-  
 296      ture in the foreshock is present in 14 out of 26 cases. Column #2 contains a heuristic  
 297      estimate of the quality of shocklets. Marks 2-3 are given, when a structure has a clear  
 298      appearance, is filled with 1-Hz magnetic oscillations, but has some significant visual de-  
 299      ficiencies, such as unequal spacing or small number of shocklets (but not less than 3).  
 300      Marks 4-5 are given for very good examples. The shocklet period is in the range 5–20  
 301      s, and is provided in column 2 as, e.g., 'p15'.

302      Other 12 cases are considered with 'no shocklets'. Mark 1 is given for two events,  
 303      when only slight increases of magnetic field are observed, with no internal magnetic os-  
 304      cillations, but accompanied with the slight deceleration of solar wind. In our main ex-  
 305      ample, such enhancements are located in the upstream-most part 23:44–23:45 UT (Fig.  
 306      2). It is possible to identify such type mostly in the MMS cases, which have high cadence



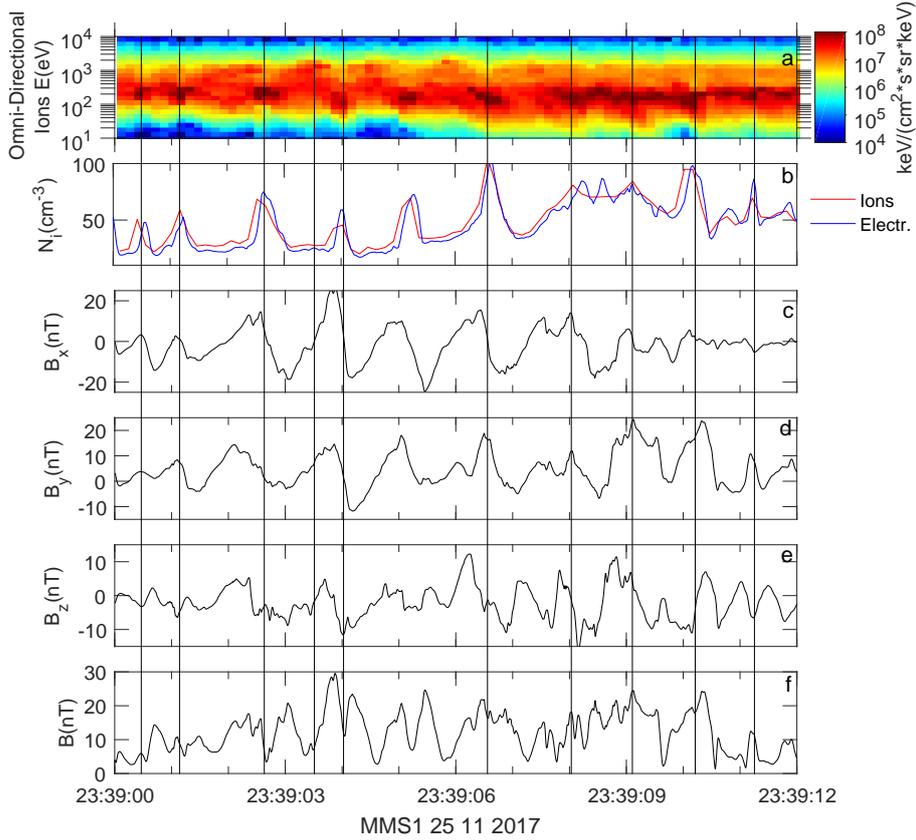
**Figure 6.** Ion spectrograms for six directions for shocklet #2.

307 ion measurements. Otherwise, it is difficult to interpret reliably magnetic variations. Fi-  
 308 nally, mark 0 denotes complete visual absence of the effect.

309 An initial attempt to determine statistically origins of these shocklet events failed.  
 310 There is no substantial difference in  $\beta$ , solar wind parameters and IMF between shock-  
 311 let and non-shocklet crossings. Moreover, in some Cluster examples (see below) the cross-  
 312 ings by different spacecraft may exhibit almost simultaneously absence and presence of  
 313 shocklets.

314 The criterion of 'very high- $\beta$ ' as  $\beta > 30$  was selected initially just to compile some  
 315 reasonable statistics of unique shocks. Later we recheck almost all available events with  
 316  $\beta > 10-30$ , to determine how important is indeed this specific  $\beta$  threshold for obser-  
 317 vation of periodic shocklets. Only one series of three shocks with shocklets was found  
 318 additionally (Geotail, 1996 Nov 07, 10-17 UT) with OMNI  $\beta = 11-17$ . However, the  
 319 local  $\beta$  was higher (15-43). It is marked in Table S3. Additionally four more events with  
 320 very weak signatures (denoted as '1' in Table S2) were found in MMS data (marked in  
 321 Table S2).

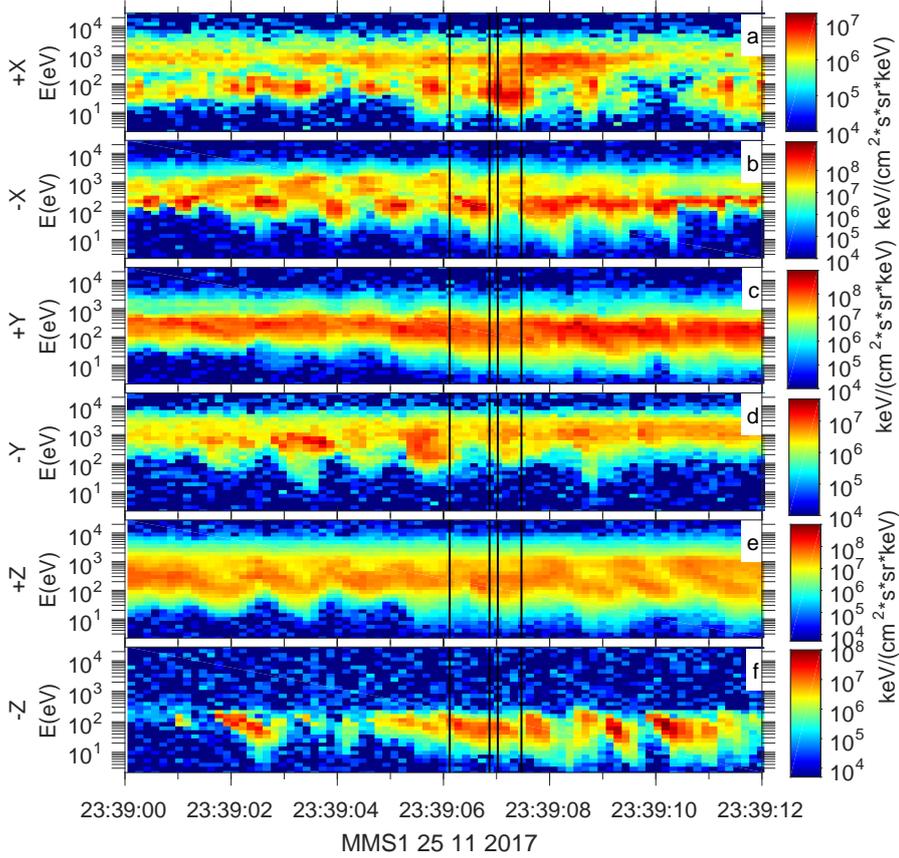
322 It should be mentioned that it is essential to have at least 16-Hz sampling of mag-  
 323 netic field to discover the event reliably in magnetic variations and about 1 Hz sampling  
 324 of plasma moments to confirm plasma deceleration. To reveal in detail the internal struc-  
 325 ture of shocklets, one needs full MMS resolution of 128 Hz for magnetic field and 10 Hz  
 326 for plasma.



**Figure 7.** Overview of shocklet #3. (a) ion omnidirectional spectrogram, (b) ion and electron density, (c-f) magnetic field vector and magnitude. Vertical lines denote two plasma density peaks.

327 MMS spacecraft separation of several tens km allows to reveal the small-scale struc-  
 328 ture of shocklets (100–200 km), but the foreshock structure as a whole remains uncer-  
 329 tain. Variety of the Cluster crossings potentially allows to use the larger spacecraft sep-  
 330 arations to visualize the large-scale structure. During late Cluster years only the distance  
 331 between C3 and C4 was controlled, while the whole tetrahedron had the scale of several  
 332 thousand km.

333 For two Cluster multispacecraft events with quasi-periodic structure (2007 Feb 05  
 334 and 2007 Mar 21) we determine the shock speed along the normal, which is very low (7.2  
 335 and 3.5 km/s respectively). Such low speeds were also found in PCS19 and are rather  
 336 common for low speed solar wind (Kruparova et al., 2019) However, the distance between  
 337 C3 and C4 equal to 400–600 km turned out to be too large for these particular events  
 338 (Fig. 10 for 2007 Feb 05). The observed 1.5 min difference between crossings of C3 and  
 339 C4 corresponds to 600 km separation, but C3 foreshock contains only weak signatures  
 340 of shocklets, while C4 foreshock has many. Spacecraft C1 and C2, being several thou-  
 341 sand km away (separations are in Table S1), observed also very differing profiles.



**Figure 8.** Ion spectrograms for six directions for shocklet #3. Vertical lines denote one plasma flow pulse interval at 23:39:06 UT and one interval between the pulses 23:39:07 UT (see text for details).

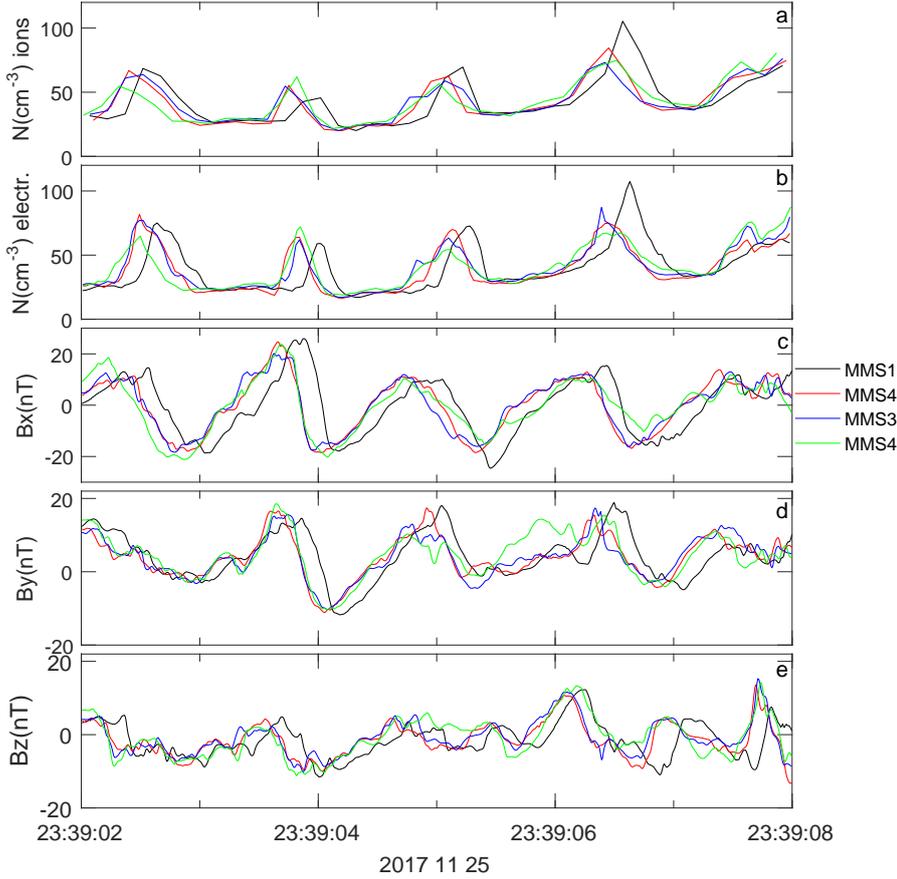
## 5 Discussion

### 5.1 General shock properties

Understanding the spatial structure of this new type of shock front with shocklets is of primary interest. Though MMS allows to reveal the scales about 10-s of km, unfortunately, the large-scale structure remains not fully clear. The Cluster project data only confirm strong differences on the scale of minutes and many hundred km.

First of all, one needs to keep in mind specifics of high  $\beta$  shocks related with the very low speed of proper shock motion (below 5–10 km/s) and the large kinetic scale due to the low magnetic field. Though our MMS case does not allow to determine the shock speed, assuming  $\sim 5$  km/s, one can get an estimate of 1500 km for a 5 min of observation. Therefore the reasonable foreshock length up to the most upstream shocklet is 1000–4000 km, of the order of proton gyroradius in low IMF.

The second important issue is remarkable stability of the shocklet periodicity. Their duration remains constant, and amplitude most often steadily grows, while one is approaching the shock front.



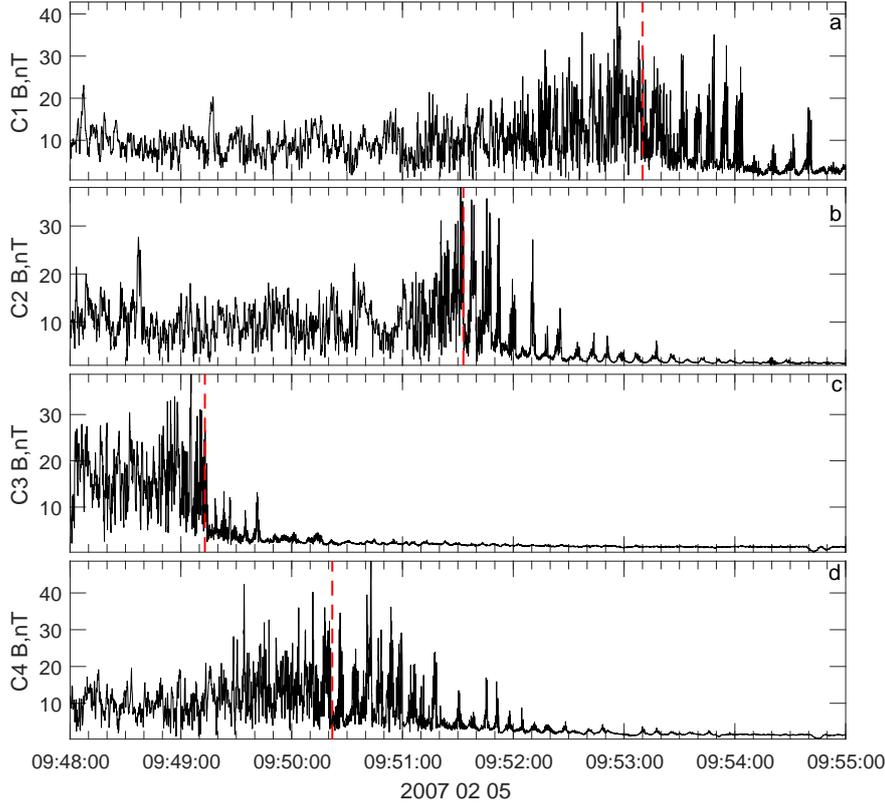
**Figure 9.** Multispacecraft time profiles of ion and electron density and magnetic field for the interval of the largest fluctuations in shocklet #3.

357 The frequency of the large-amplitude magnetic oscillations is steadily decreasing  
 358 ( from 3 to 0.5 Hz, Figure 2f), while the wavelength is increasing towards the shock front.  
 359 However, the geometry of the wave packets is very stable and the most of the observed  
 360 frequency is due to Doppler shift. These local structures are moving with  $\sim 100$  km/s.  
 361 Therefore the 1-Hz density peaks and magnetic field maxima have the spatial scale of  
 362 the order of 100–150 km along the local flow. The full wave packet in one shocklet (10  
 363 sec) likely has the length about 1000 km.

364 In the third place, this dynamic structure with shocklets is likely appearing on the  
 365 background of a standard high- $\beta$  shock (see PCS19 for examples and Fig. 10 with al-  
 366 most absent shocklets at Cluster 3 location).

367 Basing on these considerations one can suggest the following variants of the fore-  
 368 shock structure. The 'stationary' variant assumes, that shocklets are actually azimuthally-  
 369 moving undulations on a shock front. In the maxima of undulations the shock transi-  
 370 tion is strongly smeared in the upstream direction. The gaps between shocklets are then  
 371 'valleys' between undulations. This scenario explains strict periodicity, but lacks under-  
 372 standing, why the shock transition is suddenly smearing so strongly and uniformly in  
 373 many undulations to explain the ordering of shocklet amplitudes.

374 Alternatively, a shocklet might be born upstream as an 'island', if certain condi-  
 375 tions are met with e.g., properties of the reflected ions. A shocklet gradually grows and



**Figure 10.** Magnitude of magnetic field for four Cluster spacecraft for the 2007 Feb 05 crossing. Vertical lines denote the presumed shock front positions.

376 deflects the solar wind flow. The growing magnetic variations break the solar wind flow  
 377 in 1-s pulses, which become more prominent closer to a shock front. Simultaneously a  
 378 shocklet is convected azimuthally and downstream with this flow. Then the lifespan of  
 379 a shocklet of the order of 10 s and 1000 km, is enough to develop, propagate and merge  
 380 with the shock front. In this scenario it is easy to explain amplitudes of shocklets, but  
 381 difficult to explain the strict periodicity along the spacecraft trajectory.

382 The local plasma conditions, facilitating growth of shocklets and controlling their  
 383 duration, remain unknown for now. One can, for example, underline downstreaming hot  
 384 ions, registered within the shocklets, as possible candidates.

385 A final reply to this problem will require the detailed analysis of the 3d ion kinet-  
 386 ics both in experiment and modeling. The multispacecraft mission will need a separa-  
 387 tion of the order of couple hundred km to observe the foreshock structure.

## 388 5.2 Magnetic variation properties

389 The properties of the dominating magnetic oscillations in the 2017-Nov-25 MMS  
 390 case are consistent with that previously found in PCS19. Additionally, MMS mission al-  
 391 lows full 3d linear reconstruction, rather than two-point estimates of the spatial char-  
 392 acteristics. The wavelength is of the order of 150 km, observed frequency is about 1 Hz,  
 393 polarisation is linear, the vector of maximal variation is stably orthogonal to the back-  
 394 ground magnetic field. The dominating frequency is decreasing towards downstream to

below 0.5 Hz also in consistency with PCS19 (in that examples oscillations were present only at and behind the shock front). The propagation direction is also orthogonal to the background magnetic field and is about  $20^\circ$  away from the local bulk flow. The latter angle slightly depends on the definition of the bulk flow (an average during the shocklet or a value during the density peak), but, in any case, it is small. The Doppler shift is almost equal to the observed frequency, thus the magnetic wave is almost standing in the plasma rest frame, having the frequency not more than 10–20% of the observed one.

The observed wave properties are quite stable for the three studied wave packets (except the upstream-most elliptically polarized wave, which is set aside here). The coplanarity conjecture (Hubert et al., 1998) for compressive waves (the vectors of magnetic field, wavevector and maximum variation are coplanar) is likely invalid. Other interpretation variants are discussed in PCS19.

The described properties are consistent with the alternative hypothesis of Weibel mode, frequently suggested for high- $\beta$  plasma and similar to drift mirror mode. With no seed magnetic field the Weibel mode has only imaginary frequency, that is, magnetic field variations are growing faster, than propagate. For a finite magnetic field, Pokhotelov and Balikhin (2012) suggested that the Weibel mode grows as a mix of two opposite circular polarisations, and has small real frequency. A more detailed analysis of additional plasma parameters such as electric field and electron distribution may help in the future identification of the wave mode. Another potentially interesting issue for the future study, is nonlinear coupling of these variations with the ion flow bursts, which helps to decelerate solar wind flow in the foreshock (Urbář et al., 2019).

## 6 Conclusions

The indepth study of very high  $\beta$  shocks ( $\beta > 30$ ) revealed the novel type of shock structure, consisting of shocklets — 5–20 s enhancements of magnetic variations, gradually heating and deflecting the solar wind flow. The shock, however is quasi-perpendicular or oblique and the whole shock transition remains comparable with the proton gyroscale.

It is also interesting to note, that besides the high-resolution particle measurements, the slow shock motion ( $\sim 5$  km/s) and large kinetic scale (due to low magnetic field) are also critical to reveal the proton dynamics within these shocklets. With more ordinary  $\beta$  and more typical faster shock motion (Kruparova et al., 2019) even MMS high measurement cadence would be likely insufficient.

## Acknowledgments

The data analysis was supported with Russian Science Fund project 19-12-00313. We are thankful for the public project archives: Cluster Science Archive (<https://csa.esac.esa.int/csa-web/>), DARTS (<http://darts.isas.jaxa.jp/>), CDAWeb (<https://cdaweb.gsfc.nasa.gov/>) and OMNI (<https://omniweb.gsfc.nasa.gov/>) for availability of spacecraft data. High-resolution magnetic field data for one Interball-Tail spacecraft crossing is included as electronic supplement and will be uploaded to public repository after acceptance.

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*[JGR Space Physics]*

Supporting Information for

**[Shocklet structure of very high- $\beta$  Earth bow shocks]**

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**Contents of this file**

1. Captions to Tables S1 to S4
2. Caption to Dataset

**Additional Supporting Information (Files uploaded separately)**

Tables S1 to S4 in a single TableS1234.xls file  
Dataset of Interball-tail data in a single Table\_IBT.xlsx file

**Introduction**

Supporting information includes

1. four tables with the lists of bow shock crossings. Tables are included as a single separate Excel file, with four sheets, named Table S1 to Table S4.
2. Dataset for Interball-Tail shock crossing (see table S1) as Table\_IBT.xlsx file. Dataset will be uploaded to public repository after acceptance.

**CAPTIONS**

**Table S1.**List of shock crossings with very high  $\beta > 30$ 

Table caption

A	Spacecraft name
B	Code of observation type (see sec 4)
C	year
D	month
E	date
F	UT interval
G	Crossing UT
H	Spacecraft coordinates, $R_E$
I	OMNI $\beta$ , var 1 (nearest to crossing time 1-min value)
J	OMNI $\beta$ , var 2 (12-min average around crossing time)
K	local $\beta$
L	OMNI magnetic magnitude, var 1
M	OMNI magnetic magnitude, var 2
N	local magnetic magnitude
O	OMNI magnetic vector, var 1
P	local magnetic vector
Q	UT interval for local values calculation
R	OMNI $V_x$ component of solar wind speed
S	OMNI ion density
T	OMNI ion temperature
U	Model shock normal
V	Angle between OMNI magnetic field and shock normal
W	Spacecraft separation vector for C2-C1 (MMS2-MMS1, THE-THD)
X	Spacecraft separation vector for C3-C1 (MMS3-MMS1, THA-THD)
Y	Spacecraft separation vector for C4-C1 (MMS4-MMS1)

**Table S2.**

List of shock crossings by MMS spacecraft

Table caption

A	Spacecraft name
B	Code of observation type (see sec 4)
C	year
D	month
E	date
F	UT interval
G	Crossing UT
H	Spacecraft coordinates, $R_E$
I	OMNI $\beta$ , var 1 (nearest to crossing time 1-min value)
J	OMNI magnetic magnitude, var 1
K	OMNI magnetic vector, var 1

L	OMNI V <sub>x</sub> component of solar wind speed
M	OMNI ion density
N	OMNI ion temperature
O	Model shock normal
P	Angle between OMNI magnetic field and shock normal
Q	Spacecraft separation vector for MMS2-MMS1
R	Spacecraft separation vector for MMS3-MMS1
S	Spacecraft separation vector for MMS4-MMS1

**Table S3.**

List of shock crossings by Geotail spacecraft

Table caption

A	Spacecraft name
B	Code of observation type (see sec 4)
C	year
D	month
E	date
F	UT interval
G	Crossing UT
H	Spacecraft coordinates, R <sub>E</sub>
I	OMNI $\beta$ , var 1 (nearest to crossing time 1-min value)
J	OMNI magnetic magnitude, var 1
K	OMNI magnetic vector, var 1
L	OMNI V <sub>x</sub> component of solar wind speed
M	OMNI ion density
N	OMNI ion temperature
O	Model shock normal
P	Angle between OMNI magnetic field and shock normal

Table S3.

List of shock crossings by Cluster spacecraft from PCS19

Table caption

A	Spacecraft name
B	Code of observation type (see sec 4)
C	year
D	month
E	date
F	UT interval
G	Crossing UT
H	Spacecraft coordinates, R <sub>E</sub>
I	OMNI $\beta$ , var 1 (nearest to crossing time 1-min value)
J	OMNI magnetic magnitude, var 1

K	OMNI magnetic vector, var 1
L	OMNI Vx component of solar wind speed
M	OMNI ion density
N	OMNI ion temperature
O	Model shock normal
P	Angle between OMNI magnetic field and shock normal
Q	Spacecraft separation vector for C2-C1
R	Spacecraft separation vector for C3-C1
S	Spacecraft separation vector for C4-C1

**Table IBT**

Magnetic field for Interball-Tail shock crossing

Table caption

A	year
B	month
C	date
D	hour
E	min
F	sec
G	Bx GSE , nT
H	By GSE , nT
I	Bz GSE , nT