

Can Machine Learning Extract Useful Information about Energy Dissipation and Effective Hydraulic Conductivity from Gridded Conductivity Fields?

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Abstract

We confirm that energy dissipation weighting provides the most accurate approach to determining the effective hydraulic conductivity (K_{eff}) of a binary K grid. Machine learning and deep learning algorithms of varying complexity (decision tree, vanilla CNN, UNET) can infer K_{eff} with extremely high accuracy ($R^2 > 0.99$), even given only the fraction of the grid occupied by the high K medium. Adding information derived from the energy dissipation distribution improved each algorithm. However, all methods failed to infer K_{eff} accurately for outlier cases, all of which were inferred accurately using energy dissipation weighting directly. The UNET architecture could be trained to infer the energy dissipation weighting pattern from an image of the K distribution with high fidelity, although it was less accurate for cases with highly localized structures that controlled flow. Furthermore, the UNET architecture learned to infer the energy dissipation weighting even if it was not trained on this information. However, the weights were represented within the UNET in a way that was not immediately interpretable by a human user. This reiterates the idea that even if ML/DL algorithms are trained to make some hydrologic predictions accurately, they must be designed and trained to provide each user-required output if their results are to be used to improve our understanding of hydrologic systems most effectively.

1 **Can Machine Learning Extract Useful Information about Energy**
2 **Dissipation and Effective Hydraulic Conductivity from Gridded**
3 **Conductivity Fields?**

4

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9 **Abstract**

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24 our understanding of hydrologic systems most effectively.

25

26 **1- Introduction**

27 Numerical modeling is fundamental to understanding hydrologic systems, and to predicting
28 outcomes to be used for water resources management and groundwater contaminant remediation
29 [\[Ahuja et al., 2010; Chan & Elsheikh, 2017; Aliyari et al., 2019; Shamsudduha et al., 2019\]](#). Water

30 movement through the subsurface is controlled largely by the hydraulic conductivity of the region,
31 which can vary over orders of magnitude across multiple scales [*Green et al., 2009*].

32 Recent advances in hydrogeophysics increasingly suggest that the spatial pattern of hydraulic
33 conductivity can be mapped effectively [*Slater, 2007a; Hertrich, 2008; Dlubac et al., 2013*].
34 Coupled with carefully selected point measurements of hydraulic conductivity, these methods
35 offer the promise of real improvements in our ability to accurately model water flow and associated
36 solute transport in the subsurface. However, it is less clear whether “indirect methods” can be
37 used to infer upscaled effective values for hydraulic conductivity in a heterogeneous medium; i.e.,
38 it is unclear whether such methods can be used to infer the same effective conductivity value that
39 would be obtained via detailed modeling using the highly resolved conductivity field. One major
40 challenge to achieving this goal is the current lack of understanding of how spatial structure
41 (patterns in the conductivity field) affect the overall hydraulic conductivity of the medium. In this
42 study, we examine whether machine learning tools can provide insight into the problem of
43 hydraulic conductivity upscaling.

44 There is a rich body of literature on the upscaling of hydraulic conductivity. *Wen & Gómez-*
45 *Hernández [1996]* categorized upscaling techniques as being either local or non-local. Local
46 techniques, which include simple averaging, power averaging, renormalization, and percolation
47 theory, are based on the assumption that effective upscaled conductivity depends only on the
48 statistical distribution of media of different conductivities contained within the medium. Non-
49 local techniques, which include inverse modeling and energy dissipation, also consider how
50 boundary conditions affect flow.

51 Local methods based on simple or power averaging [*Journel et al., 1986; Matheron, 1965;*
52 *Desbarats & Srivastava, 1991; Zhu & Mohanty, 2002; Masihi et al., 2016*] typically represent the

53 domain in terms of fractions, each having a single conductivity, and exponentially weight the
54 conductivity of each fraction by the percent area or volume that it occupies. The extreme cases of
55 arithmetic weighting (exponent of 1, conceptually representing flows in parallel) and harmonic
56 weighting (exponent of -1, conceptually representing flows in series,) bound these approaches
57 [*Cardwell & Parsons, 1945*]. In general, local approaches work well provided that the medium is
58 approximately homogeneous; i.e., the spatial distributions of the fractions are not organized into
59 patterns, giving rise to structure [*Durlafsky, 1992*]. For any specific case, the value of the exponent
60 can be estimated by running a flow model [*Wen & Gómez-Hernández, 1996; Colecchio et al.,*
61 *2020*], but this requires the extra step of running the flow model to determine the effective
62 conductivity, which is often counter to the intended purpose of the upscaling effort.

63 The renormalization method to compute block conductivity (K_{eff}) is based on upscaling by a
64 recursive calculation whereby the extent of each grid unit is doubled along each direction at each
65 step [*King, 1989; King & Neuweiler, 2002*]. This approach essentially allows for the use of
66 arithmetic and harmonic averaging at the local scale, thereby simplifying the computation of
67 effective conductivity. However, while the method is very fast and efficient, severe errors can
68 occur in the final estimates at the scale of the largest blocks due to unrealistic boundary
69 representations during the recursive upscaling process [*Malick, 1995*]. Further, as with the
70 exponential approach, the renormalization method is only applicable to statistically isotropic,
71 lognormal conductivity fields having no clear structure [*Sánchez - Vila et al., 1995; Wen &*
72 *Gómez-Hernández, 1996*].

73 A significant advancement in the upscaling of K for binary media was achieved by the introduction
74 of percolation theory, proposed by *Vinay Ambegaokar [1971]* to model electron hopping in
75 semiconductors. The percolation concept was applied to hydrogeology by *Katz & Thompson*

76 [1985] to compute the K_{eff} of a medium characterized by a strong contrast between low and high
77 conductivities, with the assumption that the upscaled value of conductivity is primarily a
78 consequence of flows through connected high permeability pathways when they exist [Slater,
79 2007b; Ambegaokar et al., 1971]. Subsequent studies in which percolation theory was used to
80 assess K_{eff} [Berkowitz & Balberg, 1993; Hunt, Allen, Robert Ewing, 2014; Hunt & Sahimi, 2017]
81 have generally found that percolation theory is appropriate when the proportion of the high
82 conductivity medium is close to the percolation transition threshold [Colecchio et al., 2020].

83 Non-local methods can be used to infer effective values for system parameters via inverse
84 modeling, wherein the parameter field is constrained to be homogenous and the corresponding
85 best-fit equivalent upscaled parameter value is determined; several recent studies [Hassanzadegan
86 et al., 2016; Kotlar et al., 2019; Cheng et al., 2019; Coutinho de Oliveira et al., 2020] have used
87 this technique for vadose zone parameter estimation. However, this approach requires solving the
88 flow problem, including the boundary conditions, which requires that many observations are
89 available to properly constrain the parameter estimation problem. This can be very
90 computationally demanding [Vrugt et al., 2008], further, Lai & Ren [2016] have shown that this
91 approach can provide imperfect results; e.g., they showed that three different inverse approaches
92 applied to a one-dimensional situation resulted in models that were unable to reproduce the average
93 soil water content profile.

94 The most direct approach to determining how spatially variable averaging of hydraulic
95 conductivities occurs during flow is through energy dissipation analysis. This approach is largely
96 limited to steady-state problems, and also requires solving the flow problem to determine the
97 effective, upscaled parameter value. In essence, the energy dissipation approach defines the
98 energy per unit time required to force the fluid through each block of the porous medium; this

99 value is normalized for the shape of the domain and the boundary conditions, and then can be used
100 to define the spatial distribution of weights to be applied to the local conductivity values when
101 upscaling to determine K_{eff} . In this regard, [Knight \[1992\]](#) and [Indelman & Dagan \[1993\]](#)
102 suggested that K_{eff} can be determined from a grid of cells by assuming that dissipated energy must
103 be preserved during the equivalent block conductivity computation.

104 Although the energy dissipation approach is computationally demanding and requires that the flow
105 problem be solved for both the homogeneous and heterogeneous case, it has been found to be the
106 most accurate and mathematically rigorous way to upscale conductivity for steady state problems
107 [[Colecchio et al., 2020](#)]. Further, it can provide significant insight into the specific locations that
108 contribute most to the upscaled value of K_{eff} . Borrowing on the approach to defining the sample
109 area of time domain reflectometry probes using this approach ([Ferre et al., 1998](#)), it is possible to
110 identify relatively small areas of the domain that contribute disproportionately to the value of K_{eff} ,
111 thereby identifying key structures in the subsurface that may be controlling flow.

112 In recent years, due to advances in storage, computation, and graphic processing power, machine
113 learning (ML) and deep learning (DL) have gained popularity in different research areas, including
114 in natural language processing [[Allison Marier et al., 2016](#); [Yadav & Bethard, 2019](#); [Zhao &](#)
115 [Bethard, 2020](#)], computer vision [[O'Mahony et al., 2020](#); [Ronneberger et al., 2015](#); [Voulodimos](#)
116 [et al., 2018](#); [Liu et al., 2020](#)], economy [[Luo et al., 2017](#); [Mai et al., 2019](#)], and hydrology [[Assem](#)
117 [et al., 2017](#); [Nearing et al., n.d.](#); [Kratzert et al., 2019](#); [Demiray et al., 2020](#)]. In hydrogeology,
118 several attempts have been made to use deep learning to infer the forms of the equations governing
119 flow through porous media [[Afzaal et al., 2019](#); [Mo et al., 2020](#); [Tartakovsky et al., 2020](#); [Wang](#)
120 [et al., 2020](#)].

121 In particular, the architecture underlying convolutional neural networks (CNNs) allows for the
122 preservation of spatial structure and correlation information, and we might therefore expect that
123 the CNN approach is particularly suitable for problems involving gridded inputs, such as hydraulic
124 conductivity fields [Chan & Elsheikh, 2017; Canchumuni et al., 2018; Mo et al., 2020; Zhou et
125 al., 2020]. For example, Zhou et al. [2020] used a CNN to map conductivity fields to macro-
126 dispersivity, Wu et al. [2018] combined images of porous media with integral quantities of
127 porosity and specific surface area to estimate pore-scale permeability, and Mo et al. [2020]
128 parameterized a non-Gaussian conductivity field using a convolutional adversarial autoencoder as
129 well as proposing a deep residual dense CNN to map spatially distributed conductivity to head and
130 solute concentration for 2D and 3D media.

131 Reviews of several studies (e.g., Tartakovsky et al., 2020; Mo et al., 2020) indicate that data-driven
132 approaches are efficient, and can even outperform stochastic modeling or local (i.e., structure-
133 based) techniques. In particular, in the context of estimating effective parameter values, the
134 accuracy of CNN-based approaches can be attributed to the fact that, unlike classic stochastic
135 approaches that only consider the first and second statistical moments of a highly spatially variant
136 media, the machine learning approaches can account for spatial patterns that are not explicitly
137 characterized by those statistical moments [Zhou et al., 2020] or by classical structure-based
138 models.

139 Despite their impressive predictive power, ML-based models can suffer from a lack of
140 interpretability [Chakraborty et al., 2018; Apley & Zhu, 2016]. Most studies [Srisutthiyakorn,
141 2016; Mosser et al., 2017; Wu et al., 2018; Zhou et al., 2020] have mapped from measured inputs
142 to outputs without due consideration of the underlying physical processes involved. Consequently,
143 several studies [Raissi et al., 2019; Tartakovsky et al., 2020; Wang et al., 2020], have attempted

144 to incorporate physical constraints into DL algorithms. For example, [Wang et al. \[2020\]](#) used a
145 knowledge-based neural network to estimate head distribution by taking into consideration the
146 residuals of the governing equations, boundary conditions, and expert knowledge when
147 formulating the loss function used to train the model. [Tartakovsky et al. \[2020\]](#) incorporated
148 governing flow partial differential equation constraints (the Darcy and Richards equations) along
149 with training data into a DL algorithm to infer the hydraulic conductivity map based on sparse
150 observations of head and conductivity during saturated flow through a heterogeneous medium and
151 to infer the constitutive pressure-conductivity relationship from observations of capillary pressures
152 during unsaturated flow.

153 The aforementioned studies represent clear advances in the use of ML/DL for the upscaling of K_{eff} .
154 However, to date, little attention has been paid to the design of the underlying ML/DL architecture.
155 Further, we found no publications addressing the problem of how the ML/DL approach extracts
156 and uses information from the heterogeneous field in the process of inferring K_{eff} . Here, we make
157 use of recently developed approaches that facilitate comparing the activation patterns of different
158 DL models [[Kornblith et al., 2019a](#)] to examine how these ML tools extract and use the knowledge
159 that is relevant to the process of upscaling (i.e. energy dissipation weighting).

160 This study has three primary objectives. The first is to examine the potential for using ML/DL to
161 infer effective the hydraulic conductivities of two-dimensional binary conductivity fields; these
162 represent the simplest fields that display different levels of importance of K field structure (spatial
163 organization) on effective conductivity value K_{eff} . Conceptually, these binary fields can be viewed
164 as simplifications of bimodal K fields that can result from coastal depositional processes and
165 fracturing in low permeability media [[Knudby et al., 2006](#)]. The second is to evaluate the
166 performance of a specific type of CNN, an image to image translation algorithm known as UNET,

167 to infer the structure of energy dissipation weighting directly from binary K grids. The third is to
168 compare the ability of a UNET to infer K_{eff} from a binary K grid when trained on the energy
169 dissipation weighting to that when trained only on the K grid. In this regard, we examine how
170 information is processed by the UNET, to examine whether it is accounting for energy dissipation
171 ‘naturally’, even when it is not explicitly trained using such information.

172

173 **2- Methodology**

174 We examined the effect of the structure of a binary medium on the effective hydraulic conductivity,
175 K_{eff} , using the MODFLOW numerical 2-D groundwater model to produce the steady-state head
176 distribution over a square grid with a 1-D applied gradient. We computed K_{eff} from the geometry
177 of the grid, the applied Type I boundary conditions, and the steady-state flow through the system
178 for different random distributions of two media with different K values. We also computed the
179 energy dissipation in every cell to examine whether this information can provide insight into the
180 spatial weighting of the K values used to determine K_{eff} [*Indelman & Dagan, 1993*]. Further, we
181 examined a range of approaches to infer K_{eff} from the K grid, with and without information about
182 the energy dissipation distribution, including simple tree-based and more complex, CNN-based,

183 machine learning algorithms. Finally, we
184 used central kernel alignment similarity
185 *Kornblith et al., [2019b]* to infer the hidden
186 layer representation for K_{eff} estimation in
187 an attempt to understand how and whether
188 the deep learning algorithm considers
189 energy dissipation during K_{eff} estimation.

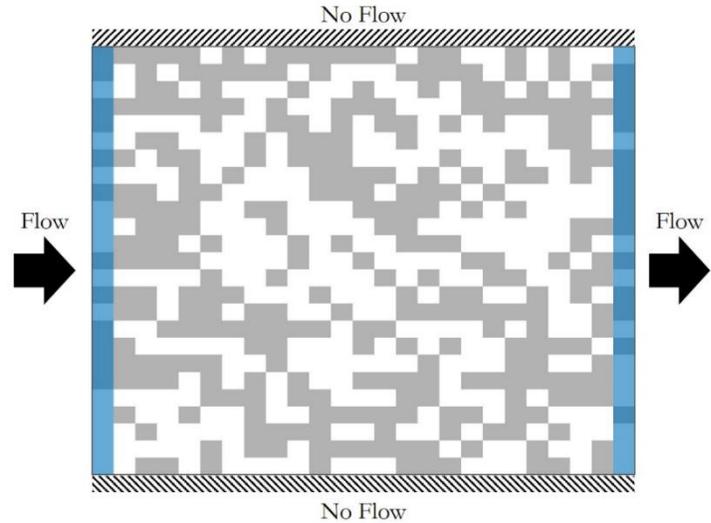


Figure 1. Sample 25x25 cell grid with 50% high K (white) and 50% low K (grey) cells, constant head boundaries (blue), and no flow boundaries (diagonal lines). The left boundary has a constant head of 2 and right boundary has a constant head of 1, with flow occurring from left to right.

190

191 **2-1- Flow through Heterogeneous**

192 **Binary Grids (Dataset Generation)**

193 We defined 25 by 25 grid domains with no flow boundaries at the top and bottom and constant
194 head boundaries of 2 m and 1 m on the left and right boundaries, respectively. Each cell has a
195 length of 1 m on a side. Two media populated the grid, with K values of 1 and 0.001 cm/s.
196 Different percentages of the prevalence of the high K material were considered, ranging from 1%
197 to 99%. For each high K percent, 3000 random distributions of the media were modeled. Figure
198 1 shows one example of a grid with 50% high K material.

199 For each grid, the effective hydraulic conductivity was computed based on Darcy's Law, the global
200 gradient applied over the domain, and the steady-state flow through the system. The convergence
201 criterion on the head used in MODFLOW was 0.01 m. To account for small errors that persisted
202 when the convergence criterion was met, the value of K_{eff} was calculated based on the flow into
203 the left boundary and the flow out of the right boundary. The resulting K_{eff} values calculated at
204 both boundaries agreed within 1%, and the average value was used for all analyses.

205

206 **2-1-1- Energy Dissipation Weighting Method**

207 Conceptually, energy dissipation is defined as the energy per unit time necessary to force the fluid
208 through the porous medium [Indelman & Dagan, 1993]. The value of K_{eff} can be thought of as a
209 weighted average of the spatially distributed values of K . Energy dissipation can be used to define
210 the spatial distribution of weighting factors based on the square of the gradient of the potential at
211 each location normalized by the sum of the square of the gradient of the potential for the same
212 boundary conditions for a domain filled with a homogeneous medium [Knight, 1992]. The
213 weighting factor at a point at (x,y) can be expressed as:

214

$$215 \quad W(x,y) = \frac{[\nabla\phi(x,y)]^2}{\iint [\nabla\phi_0(x,y)]^2 dx dy} \quad \text{Eq. 1}$$

216

217 where $w(x,y)$ is the weighting factor at point (x,y) , $\phi(x,y)$ is the potential at each location, and ϕ_0
218 is the potential distribution for the equivalent homogenous field. Knight [1992] showed that
219 spatially variable properties (e.g. for K) can be weighted to determine an upscaled property (here
220 K_{eff}) as the sum of the local K weighted by the energy dissipation weighting factor over the domain,
221 as:

$$222 \quad K_{eff} = \iint W(x,y)K(x,y) dx dy \quad \text{Eq. 2}$$

223

224 In this study, the steady-state head values were used to compute the energy dissipation distribution.
225 Because MODFLOW determines head values at the nodes and the K values are defined over the

226 cells, the gradient and K values are not aligned. There are two approaches to compute K_{eff} with
227 the energy dissipation approach for these conditions. First, the gradient can be computed at each
228 cell edge and the value of K_{eff} at the edge can be determined based on the K value in the two
229 neighboring cells. Second, the head values can be interpolated to the edges, allowing for gradients
230 to be computed at the nodes, matching the locations of the K grid. Both of these approaches were
231 tested and were found to agree within 1%; accordingly, the average of these two estimates of K_{eff}
232 was used for each grid for further analyses. Hereafter, the energy dissipation weights are referred
233 to as ED weights, or simply as weights.

234

235 **2-1-2- Estimating K_{eff} with a Regression Tree with and without ED Weights**

236 For a given percent of high K material, the energy dissipation distribution depends on the structure
237 and arrangement of high K and low K cells in the domain. As a result, the K distribution and the
238 ED weight distribution are related (but not identical) sources of information for inferring K_{eff} .
239 Throughout this study, we examine whether added knowledge of the ED weight distribution
240 improves the estimation of K_{eff} by machine learning and deep learning algorithms. First, we
241 compare the performance of simple regression tree (RT) models with and without the inclusion of
242 energy distribution information. We use a regression tree as a very simple ML to provide a baseline
243 of comparison for more advanced machine learning algorithms. For completeness, a gradient
244 boosting algorithm was also applied, but its performance was not significantly different than the
245 RT, so we opted for the simpler version of the tree-based ML.

246 Because RT models are not well-suited to considering spatial relationships among inputs, rather
247 than providing the RT models with the K grid and spatially distributed weights, we provided only

248 the following summary statistics: the percent of high K grids within the domain, and the fraction
249 of the cells that contain high spatial weights. To label the high ED weight cells in a grid, we
250 followed the procedure suggested by [Ferré et al., 1998]. We first computed the energy
251 distribution (Eqns. 1 & 2) after solving the steady-state head distribution with MODFLOW. The
252 weights were sorted in descending order, and the cells that contributed 95% of the total weight
253 were identified as high energy cells, thereby defining the smallest area contributing 95% of the
254 total weight in determining K_{eff} .

255 To apply the RT analysis, we considered paired values of targets (K_{eff}) and features (percent of
256 high K material with or without the fraction of high energy cells). These were divided randomly
257 into 65% training, 15% validation, and 20% testing. The models were trained using the training
258 set and tuned using the validation set. We chose to use a binary split at each node, such that the
259 RT sequentially divided the training set of K_{eff} samples at each node into two subsets. The split
260 was based on the choice of a feature and a threshold value such that every sample was identified
261 as being above or below that threshold. At each point of division, the tree maximized the reduction
262 in overall variance such that the sum of the population-weighted variability of the K_{eff} values in
263 the two subsets was less than that of the parent set. Because each feature and threshold
264 identification is made without regard to any future or past selections, RT is known as a “greedy”
265 algorithm and is not guaranteed to be optimally efficient. Furthermore, RT results in binned
266 outputs, with a single value applied to all samples that fall into the final node along each branch.

267 The performance of the RT was based on its ability to predict K_{eff} for the testing set. This
268 procedure was then repeated with only the percent high K material provided to the RT (i.e., without
269 also providing the fraction of high energy cells). A comparison of the performance of these two

270 RT models provides an estimate of the value of the information contained in the fraction of high
271 weight cells for inferring K_{eff} with RT.

272

273 **2-1-3- Estimating K_{eff} with a Vanilla CNN with and without ED Weights**

274 The estimation of K_{eff} can be viewed as an image mapping problem: i.e., our goal is to map a grid
275 of 25x25 K values onto a single value of K_{eff} . From this perspective, together with the expectation
276 that the spatial patterns of K within the domain are important to predicting K_{eff} , a convolutional
277 neural network (CNN) is a natural choice for a deep learning method to apply to this problem.

278 CNN is a class of supervised learning algorithms that is suitable for processing image-based
279 datasets. It consists of two main types of components, a convolutional kernel, and a pooling layer.

280 A kernel is a sliding window of weights used to extract “features” from the inputs by convolution
281 of the inputs using the kernels, and propagation of the result to the next layer of the network.
282 Application of an activation function provides nonlinear elementwise transformation. Pooling
283 layers are optional blocks of a network that reduce the size of the hidden layers.

284 Herein, a ‘vanilla’ CNN refers to a common architecture comprising several convolutional layers
285 that are fully-connected to a dense output layer to perform predictions (see structure presented in
286 Table A1-A of the appendices). The number of layers and filters were selected via hyperparameter
287 tuning using the validation dataset. Dropout regularization was not included. For the cost function,
288 we used the mean squared error between the observed and predicted K_{eff} in the training samples.
289 The Adam algorithm [*Kingma & Ba, 2015*] was used to optimize the model parameters and
290 weights.

291 As for the RT analyses, the CNN was trained both with and without providing the ED weights as
292 input information. As shown previously by *Knight [1992]*, knowledge of the K field and the ED
293 weights provides a near-exact definition of K_{eff} . Therefore, we provided a degraded metric related
294 to the ED weights; specifically, a 25x25 0/1 masking matrix with 1 indicating high energy cells
295 was used as a surrogate for the ED weights.

296

297 **2-1-4- Estimating K_{eff} with and without ED Weights**

298 Recent advances in the application of deep learning to image processing have led to the
299 development of powerful machine learning architectures. In particular, given that the knowledge
300 of energy dissipation has been shown to provide valuable information regarding the weighting
301 required to define K_{eff} , the problem of estimating K_{eff} from a grid of K values can be seen as a
302 problem that has two stages. The first is to estimate the energy dissipation weighting at each cell,
303 and the second is to use the estimates of the spatially distributed ED weights to estimate K_{eff} . The
304 UNET architecture [*Ronneberger et al., 2015*] was developed to address problems that require
305 consideration of multiple scales by including skip connections, which recombine information from
306 earlier hidden layers with that of later hidden layers. Here, we propose a modified UNET
307 architecture that estimates the spatial weight distribution and then combines this estimate with the
308 K grid to estimate K_{eff} (Figure 2).

309 We applied the UNET in two different ways to understand if and how ED weighting is used in the
310 estimation of K_{eff} . In the first implementation, referred to as ‘informed’, the model is trained using
311 the freeze-training technique [*Zoph et al., 2016; Brock et al., 2017*], in which the lower branch of
312 the model, Figure (2), up to the point that the K grid information is reintroduced, is first trained to

313 estimate the spatially distributed ED weights. This is achieved by providing the ED weights during
314 training. Once trained, the informed UNET is then used to predict K_{eff} *without* being provided ED
315 weights. This is possible because UNET models are a variation of encoder-decoder algorithms,
316 which include a contracting path (like the vanilla CNN) followed by an expanding path. The
317 contracting path (i.e., encoder) is responsible for capturing the context while the expanding path
318 (i.e., decoder) enables localization. Through the use of encoder-decoder paths, the UNET can
319 provide an output that has the same dimensions as the input. In our application, this property is
320 necessary to obtain ED weights on a grid having the same size as the K grid. Making use of this
321 structure, we trained UNET to infer the ED weights and then used those inferred weights to predict
322 K_{eff} . In other words, for the informed UNET, the weights of the lower branch were frozen after
323 training, and training was then continued by feeding only the K grid into the UNET. The algorithm
324 then provided estimates of the ED weights, which were concatenated with the K grid and fed into
325 the final fully-connected layer. This model was trained to estimate K_{eff} .

326 The second implementation of UNET is referred to as ‘uninformed’. The model structure was
327 identical to the informed UNET, but was only provided K grid information; it was not trained
328 using any information about the actual ED weights. Rather, all weights in the model were fitted
329 simultaneously during training to fit K_{eff} .

330 The details of our UNET structure are provided in the Appendices (Table A1-B). Briefly, the
331 contracting path is comprised of repeated blocks of two consecutive 3x3 convolutional kernels
332 with rectified linear activation functions (Relu) followed by a 2 x 2 max-pooling layer with a stride
333 of 2 to reduce the number of parameters and diminish the next layer input size. On the contracting
334 path, multilevel decomposition is applied to each layer, doubling the number of feature maps (i.e.,
335 filters) at each step. The expanding path consists of repeated blocks of transposed convolution

336 layers with a kernel size of 2×2 and a stride of 2. In each block, the output of the transposed
337 convolution layer is concatenated with the cropped feature map of the corresponding step from the
338 encoding procedure (a skip connection). The concatenated values are subjected to two consecutive
339 3×3 convolutional kernels with Relu activation functions. The skip connections help to recover
340 information that may be lost by down-sampling during decoding. The cropping procedure in the
341 concatenation ensures that the tensor extracted from the encoder will have the same size as the
342 corresponding layer in the decoder. During decoding, the convolutional layer halves the number
343 of channels. A final convolution layer with a kernel size of 1×1 and linear activation maps the
344 current number of channels to a single layer. A skip connection was introduced to recover
345 information of the original grid, like the percent of high K, that may be lost by when inferring the
346 ED weights. Specifically, the inferred ED weights were concatenated with the K grid and fed
347 through a convolutional layer and a dense, fully-connected layer to estimate K_{eff} . It should be
348 noted that as part of preprocessing, we padded the input image to 32×32 to make the final output
349 of the UNET the same as the original image.

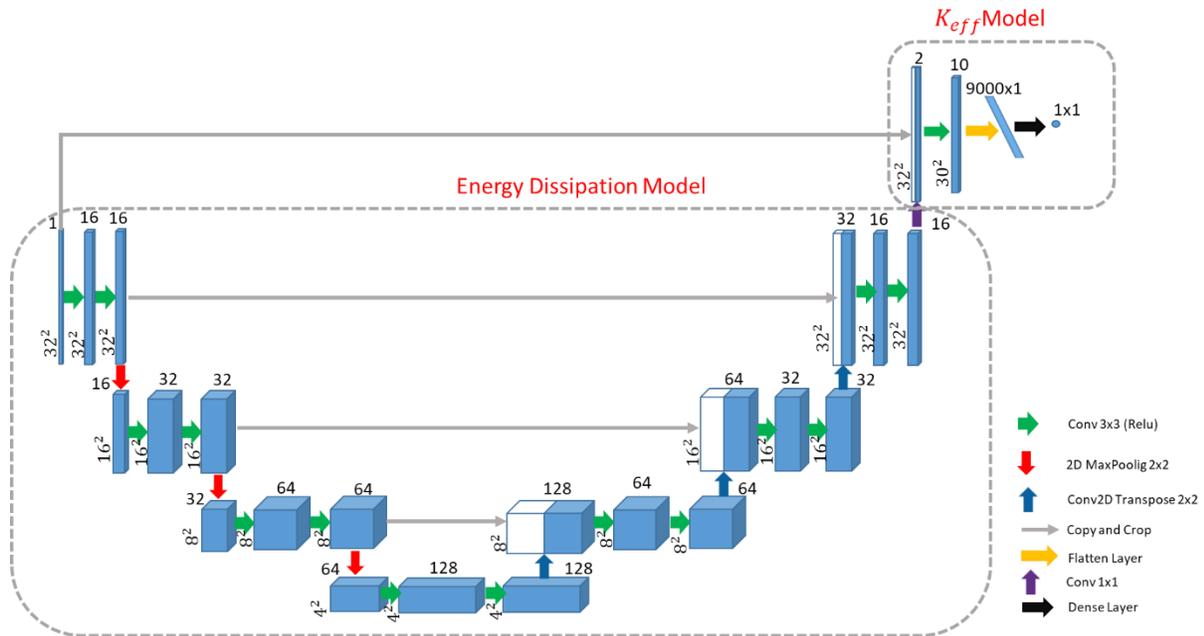


Figure2) Proposed U-net architecture. The architecture is composed of two submodel. Energy dissipation model has a UNET shape structure followed by a CNN model to map output of UNET to K_{eff} . Blue box corresponds to a multi-channel feature map. The number of channels is denoted on top of the box. The x-y-size is provided at the lower left edge of the box. White boxes represent skipped connection. The arrows are operations performed on feature maps described in the legend.

350

351 2-2- Model Evaluation

352 Identical data were provided to all of the methods; specifically, the K grids (dimension 3000*99)

353 MODFLOW-determined K_{eff} values, and (where applicable) ED weights. The inputs and targets

354 were divided into training, validation, and testing subsets. A random selection of 65% of these

355 inputs was used for training and 15 % were used as a validation dataset for hyperparameter tuning.

356 The same training/validation/testing sets were used for all of the analyses reported herein (e.g.

357 Regression Tree, vanilla CNN, etc.). Model performance is reported using the testing data set,

358 comprising the remaining 20% of the data. Before training, the inputs were standardized by

359 subtracting the mean value and dividing by the standard deviation. All hyper-parameters were

360 tuned using a grid search approach. The root mean squared error (RMSE) between the observed

361 and model-calculated values (of K_{eff} or ED weight) is used to assess the prediction quality of each
362 model. The R^2 value was also calculated but is only used to further illustrate the quality of the
363 predictions.

364

365 **2-3 Deep Learning Implementation**

366 All deep learning architectures were implemented in Python 3.6.9 with Tensorflow V. 2.2.0 and
367 CUDA version 10.1. Training and predictions were done on a P100 NVIDIA GPU. For both the
368 “informed” and “uninformed” models, we used Adamax with a learning rate of $5e-4$ as the
369 optimizer. For the vanilla CNN, the Adam optimizer with a learning rate of $1e-4$ was used. For all
370 cases, training was stopped when performance on the validation dataset stopped improving within
371 a patience value equals to 50.

372

373 **2-4- CKA and Similarity Analysis**

374 In addition to investigating whether machine learning algorithms can be trained to predict K_{eff}
375 using gridded binary K information, we also wanted to determine whether these tools can infer the
376 underlying pattern of energy-dissipation in the process of inferring K_{eff} . If it can be shown that the
377 deep learning procedure naturally infers the spatial distribution of energy dissipation, then it would
378 provide an example of how DL tools can “learn” underlying concepts. Further, because the
379 distribution of energy dissipation indicates which parts of the medium are having the largest impact
380 on steady-state flow, the ability to make inferences regarding these patterns would also enable an
381 understanding of the relationship between K_{eff} and the structure of the K distribution. Such

382 knowledge would also be valuable for understanding soil property distributions that may impact
383 dispersion, colloid trapping/mobilization, and erosion/piping.

384 To investigate the ability of deep learning tools to make inferences regarding the underlying
385 pattern of energy dissipation, we applied the UNET methodology in both informed and uninformed
386 modes, as described above. To compare how information flowed through the UNET in informed
387 and uninformed modes, we examined the intermediate representations (i.e., hidden layer outputs)
388 of each trained model. Specifically, the hidden layer outputs, known as hidden representations,
389 characterize the “features” learned by a hidden layer of a neural network from an input (i.e, K
390 grid), represented in a machine-readable format. Similarity measurements can be used to compare
391 these intermediate representations between networks.

392 *Kornblith et al. [2019]* showed that for a similarity index to be suitable, it should be invariant to
393 orthogonal transformation and isotropic scaling, and not be an invertible linear transformation.
394 We use the Hilbert-Schmidt independence criterion (HSIC) [*Gretton et al., 2005*], which is a
395 kernel-based statistical measure of the independence between two sets of variables:

396

$$397 \quad HSIC(K, L) = \frac{1}{(n - 1)^2} tr(KHLH) \quad \text{Eq. 3}$$

398 where:

399

$$400 \quad K, H, L \in R^{n \times n}$$

401

402 in which H is the centering matrix $H = I - \frac{1}{n}11^T$, and $K=k(X^{(i)}, X^{(j)})$, $L = l(Y^{(i)}, Y^{(j)})$ are
403 positive semidefinite kernel functions. For linear kernels, $K=k(X, Y) = XY^T$. An HSIC value of 0
404 implies independence. Other researchers [*Cristianini et al., 2006; Cortes et al., 2012; Kornblith*
405 *et al., 2019a*] showed that HSIC can be made to be invariant to isotropic scaling by normalization.
406 This normalized HSIC index is known as centered kernel alignment (CKA):

407

$$408 \quad CKA(K, L) = \frac{HSIC(K, L)}{\sqrt{HSIC(K, K)HSIC(L, L)}} \quad \text{Eq. 4}$$

409 In this study, we used the Centered Kernel Alignment (CKA) metric proposed by *Kornblith et al.,*
410 *[2019b]* with linear kernels to evaluate the similarities of layer representations in our trained
411 networks. Specifically, we calculated the CKA between corresponding intermediate
412 representations of the informed and uninformed networks. To assess the similarity between
413 corresponding intermediate representations of model 1 and model 2 at layer i and j , we flattened
414 the representations and let $X \in R^{n \times m_1}$ and $Y \in R^{n \times m_2}$ be the matrix of intermediate
415 representations of model 1 and model 2 with m_1 and m_2 neurons for n examples. Then, we
416 constructed the linear kernel matrices: $K= XX^T$ and $L= YY^T$. Finally, we used equation [4] to
417 compute the CKA metric. We compared similarities for all paired combinations of layers to
418 explore how information flowed through both networks.

419

420

421

422

423 **3- Results**

424 The main goal of this study was to investigate the impact that “structure” has on the effective value
425 of hydraulic conductivity (K_{eff}) of a binary heterogeneous medium. We examined this for multiple
426 realizations of random fields that contain different percentages of the higher K material.

427 A key insight regarding this was presented by *Knight, [1992]* and *Indelman & Dagan [1993]*, who
428 showed that the spatial distribution of energy dissipation during steady-state flow can be used to
429 define spatially distributed weights on K that can be used to compute K_{eff} . We first confirm this
430 finding for the set of binary grids examined. Then, we show that the performance of a regression
431 tree, trained to predict K_{eff} based only on the percent high K material, is improved by providing
432 (reduced) information about the ED weights. Finally, we examine whether deep learning
433 algorithms can predict K_{eff} with and without information regarding the ED weights. By comparing
434 DL algorithms trained with and without access to energy dissipation information, we seek to
435 understand the mechanism by which K_{eff} is inferred by the DL.

436 **3-1- Analysis of the Effective Hydraulic Conductivity (K_{eff}) and High K** 437 **Percentage**

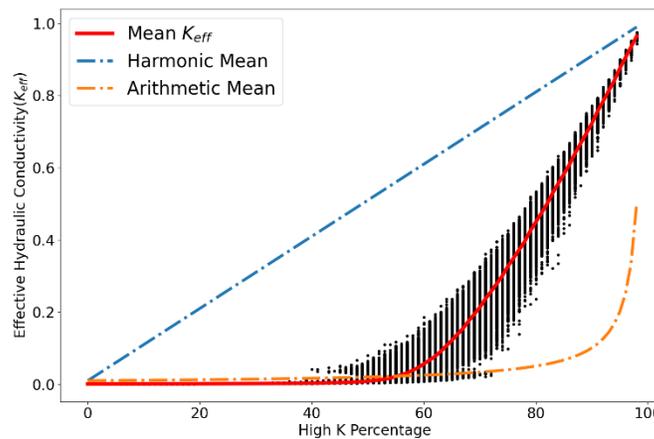
438 The steady-state flow problem, Figure (1), was solved for 3000 random realizations of a binary
439 flow field for high conductivity mixtures ranging from 1 to 99%. K_{eff} was computed from the
440 overall gradient applied over the domain and the steady-state flow through the domain. Figure 3
441 indicates how K_{eff} varies as a function of the percent high K material present in the realization.
442 The parallel and series arrangements for each percent high K realization were calculated
443 analytically and are seen to place limits on the ranges that K_{eff} values can take. The mean value
444 of K_{eff} for each high K percentage is shown in the figure.

445 The plot demonstrates the nonlinear dependence of K_{eff} on percent high conductivity. At low
446 percentages of high conductivity, K_{eff} is only minimally affected by the addition of more high K
447 material and remains approximately equal to the conductivity of the lower K material. A nonlinear
448 transition zone is seen to occur at approximately 40 to 70% high K, and the relationship becomes
449 approximately linear above 70%. For a given percentage of high K, the maximum variance of K_{eff}
450 occurs in the central transition zone.

451 These results illustrate the two related but different challenges for inferring K_{eff} from a binary grid:
452 predicting mean K_{eff} as a function of the percent high K material; and predicting K_{eff} for a specific
453 grid given knowledge regarding the percentage of high K material present.

454

455



459

Figure 3 K_{eff} distribution as a function of percent high K for medium K contrast condition

460

461

462 3-2- Analysis of the Energy-Dissipation Weighting Method to Explain the K_{eff}

463 *Knight [1992]* showed that the pattern of energy dissipation, calculated from the square of the
464 gradient of the potential, can be used to determine an upscaled property like K_{eff} . This fact is

465 confirmed by our study (Figure 4). The energy dissipation approach can be thought of as
466 computing a weighted average of the local K values on the grid that perfectly recovers the flow-
467 based K_{eff} .

468 Despite the power of the energy dissipation approach, the weights are very difficult to identify
469 visually. For example, the two grids are shown in Figures 5a and 5b both have 80% high
470 conductivity material but have strikingly different K_{eff} values (0.53 and 0.24 respectively). The
471 corresponding maps of the ED weights are shown in Figures 5c and 5d, illustrating that the grid
472 with the lower K_{eff} has a much more localized pattern of ED weighing. While it might be tempting
473 to attribute this localized weighting to the connected pattern of low K cells running vertically
474 through Figure 5b, beyond this qualitative assessment it is essentially impossible to visually infer
475 the values of the ED weights from the knowledge of the spatial organization of K . Of course, both
476 the pattern of ED weights and their values can be computed readily by solving the steady-state
477 flow problem, but then the value of K_{eff} can be determined directly and knowledge of the ED
478 weights is superfluous. Accordingly, the ED weighting approach is best seen as a method for
479 understanding spatial organization (e.g. [Ferre et al., 1998](#)), rather than a practical approach for
480 inferring K_{eff} from a K grid.

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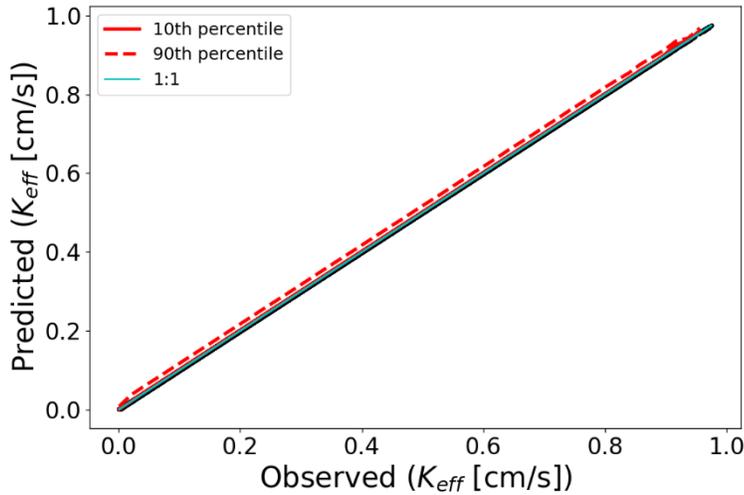


Figure 4) K_{eff} estimation using energy dissipation method

By classifying the domain into high and low weight areas, we can see that the spatial structure of high-weight areas varies systematically with the percent high conductivity material. The paired images in Figure 6a show how the fractions of high energy cell relate to the corresponding ED maps for several K grids with different percentages of high K material. Figure 6b shows the expected fraction of high energy cells as a function of the threshold used to define high weight areas. There are two clear conclusions. First, the high energy area is restricted in a relatively small area for percent high conductivity conditions between approximately 50 and 80%. Second, the results are not highly sensitive to the choice of threshold. Finally, Figure 6c indicates a strong relationship between K_{eff} and the fraction of high energy dissipation cells (defined with a threshold of 95%), but with some interesting complications to that relationship in the range of 50 to 60% high conductivity material. These results suggest that information regarding the fraction of high energy cells may be informative for inferring K_{eff} for a given percent high conductivity material fraction, but that the relationship is likely to be complex.

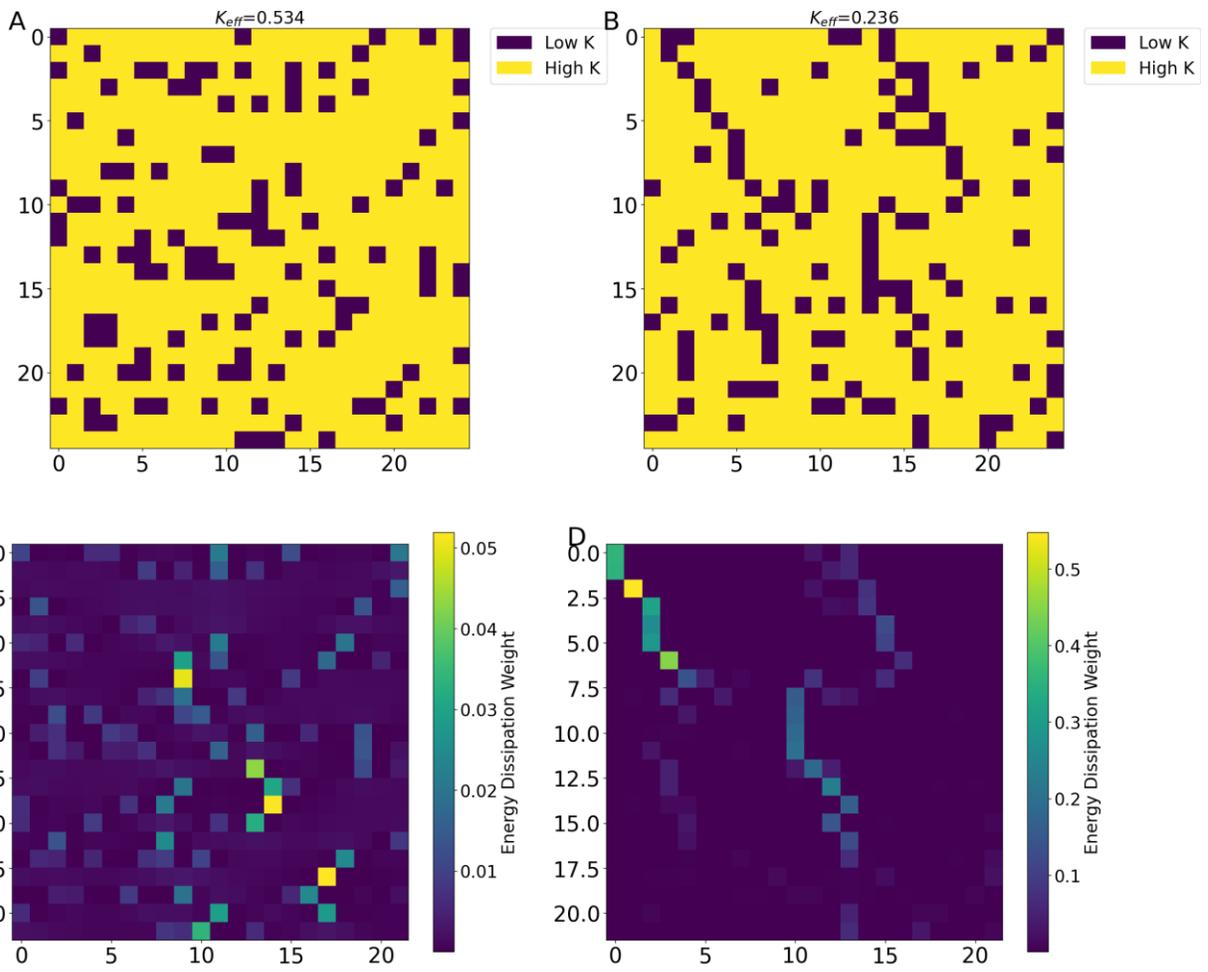


Figure 5) Effects of structure on K_{eff} for the structures with the same percent high conductivity. A,B: Grid samples with percent high conductivity values of 80.

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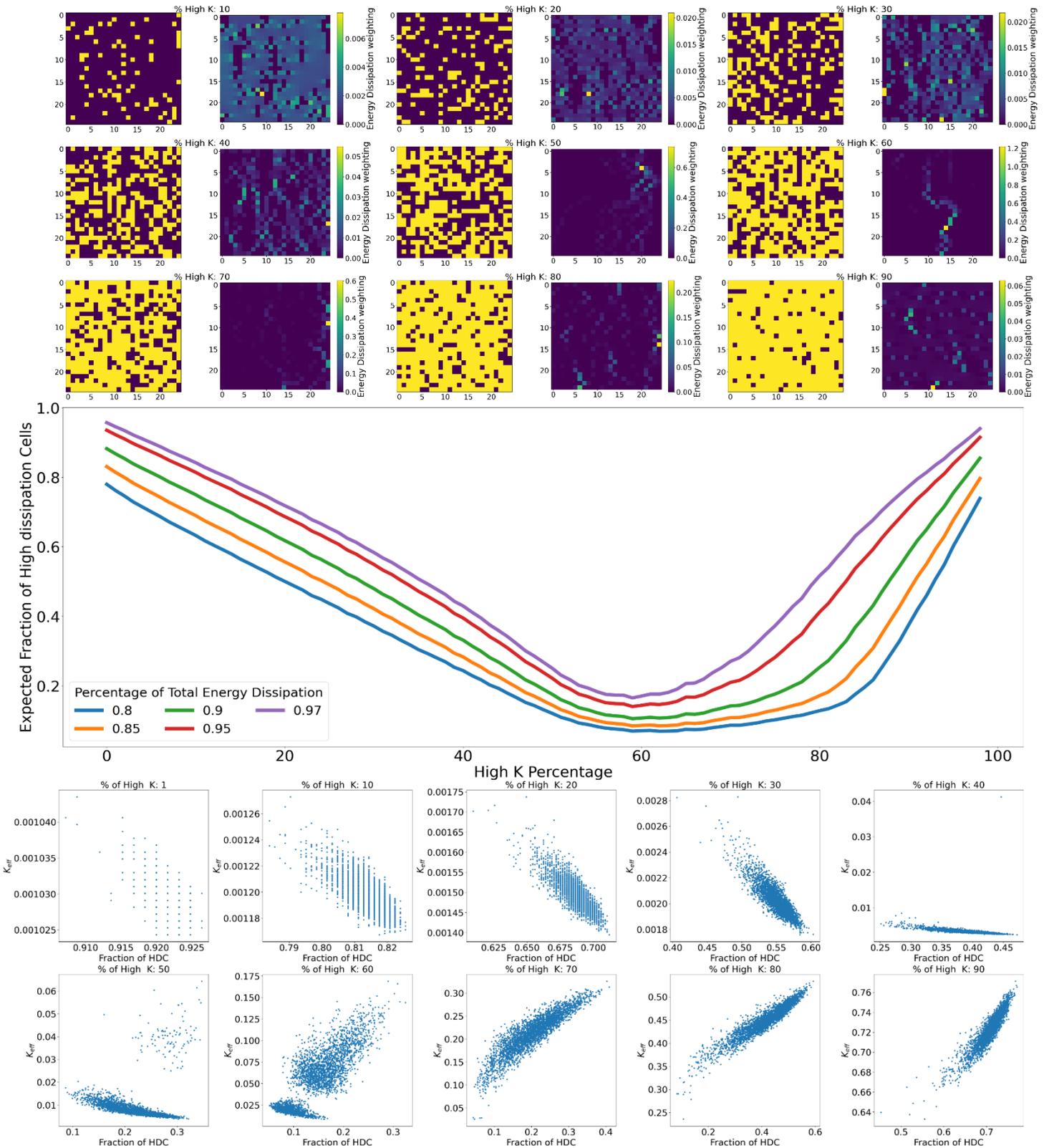


Figure 6) The energy dissipation pattern for different percent of high K materials. A: Grid samples and their corresponding energy dissipation weightings of high contributing cells as a function of percent of high K material. B: Average fraction of high energy dissipation cells as a function of the percent high K material, shown for definitions of "high energy dissipation". C: relationship between high energy cells and K_{eff} for different ranges of high k percentage.

506 **3-3- Inferring K_{eff} with a Regression Tree Given Information on Energy**

507 **Dissipation**

508 Given only the gridded K values, it is a simple matter to determine the fraction of high conductivity
509 cells. This property was used to infer K_{eff} by training a simple regression tree machine learning
510 algorithm (Figure 7a), which achieved an RMSE of 0.0213 and R2 of 0.9942 when evaluated using
511 the testing data. Note that this essentially finds only the *mean* value of K_{eff} at each percent high K
512 [red line in Figure 3]. Further providing the number of high-weight cells (based on a threshold of
513 95%) to the regression tree algorithm improves the estimation of K_{eff} , achieving an RMSE of
514 0.0133 and an R2 of 0.9978 (Figure 7b). While the improvement in R2 may seem unimportant,
515 there is a reduction in the error of K_{eff} prediction for outliers, for which structure is more important
516 (compare Figures 7a and 7b).

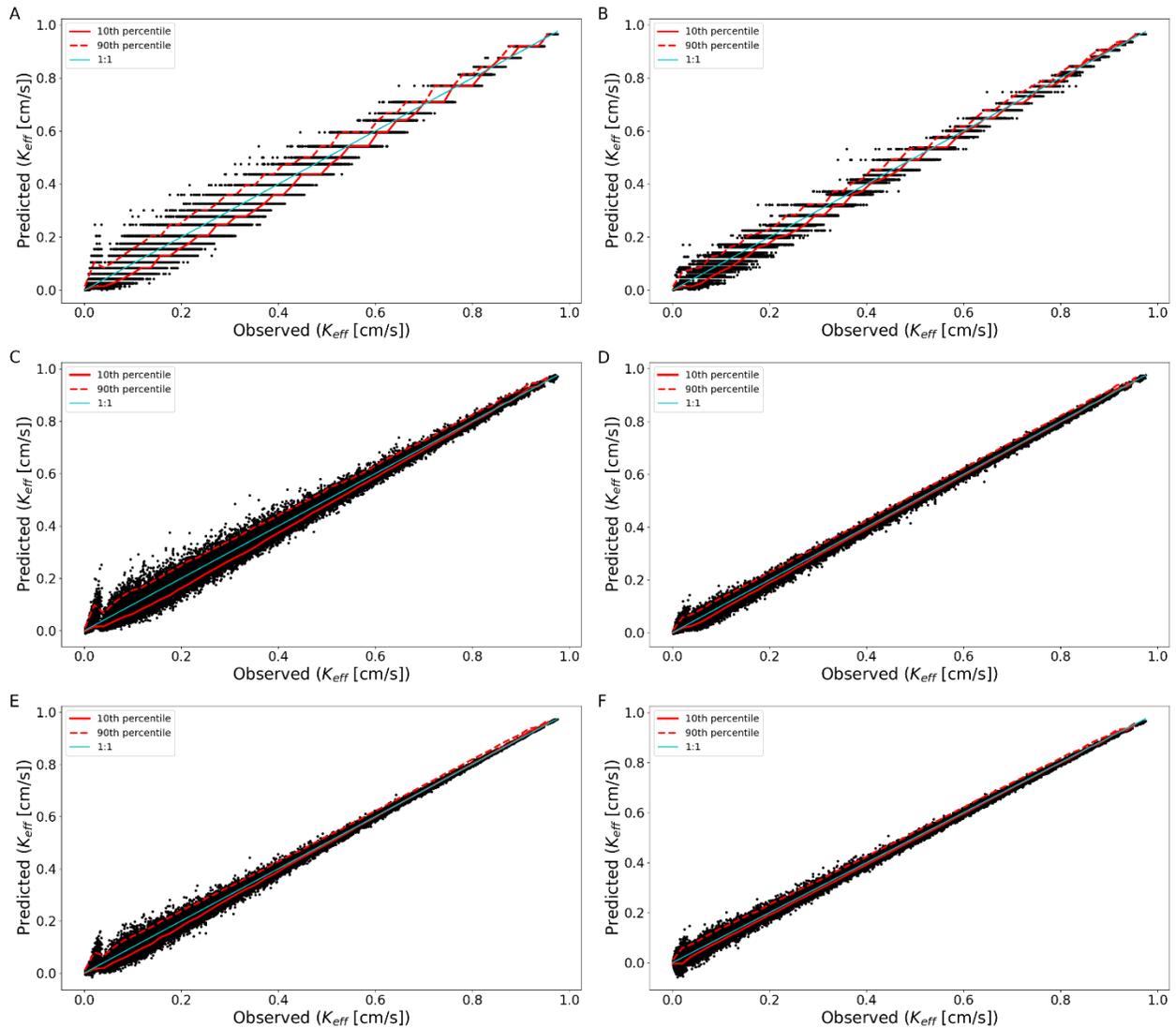


Figure 7) the testing performance of K_{eff} estimation using different methods. A: K_{eff} estimation using regression tree and only percent high K as input. B: K_{eff} estimation using regression tree and percent high K and fraction of high energy dissipation as inputs. C: K_{eff} estimation using vanilla CNN using only K grid as input. D: K_{eff} estimation using vanilla CNN using K grid and high energy dissipation cells mask as inputs. E: K_{eff} estimation using energy dissipation Uninformed UNET model. F: K_{eff} estimation using Informed UNET model with pre-training on energy dissipation.

517

518 **3-4- Use of a Vanilla CNN to infer K_{eff} with and without ED Weights**

519 For this part of the study, the binary K grid and a 0/1 map of high energy cells was provided as
 520 inputs to the CNN, and the target to be learned was K_{eff} . The vanilla CNN, provided with only the

521 K grid as input, performed as well (RMSE= 0.0171 and R2=0.9962) as the regression tree model
522 that had been provided both the percent high conductivity material and the fraction of high energy
523 cells (compare Figures 7c and 7b). Providing the binary high energy cell location map along with
524 the K grid improves the performance (RMSE=0.0087 and R2=0.999); see Figure 7d.
525 Note that, unlike the RT, the CNN method provides estimates for K_{eff} on a continuum (not binned).
526 Qualitatively, however, the CNN models provide relatively poor performance for low percent high
527 conductivity material when given only the K grid as input (Figure 7c).

528

529 **3-5- Inferring K_{eff} with UNET with and without ED weights**

530 The uninformed UNET performs better (RMSE=0.0113 and R2 =0.9984) than the vanilla CNN
531 when given only the K grid (compare Figures 7e and 7c). This indicates that the structure of the
532 UNET enables it to learn something that allows it to achieve improved performance.

533 The results of the informed UNET (Figure 7f) are interesting. On the one hand, while it shows
534 further improvement (RMSE=0.0106 and an R2=0.9986) over the uninformed UNET, it does not
535 outperform the corresponding CNN where the high energy map was provided. So, the UNET
536 structure seems to improve K_{eff} estimation while direct training on the ED weights only offers
537 marginal performance improvement. On the other hand, although the informed UNET was
538 provided information regarding the ED weights during training, its predictions of K_{eff} are made
539 *based solely on the K grid*. In other words, training with knowledge of the ED distribution mainly
540 affects the internal structure of the UNET. The result is that the “uninformed” and “informed”
541 versions of UNET exhibit similar predictive performance (indicating equally informative

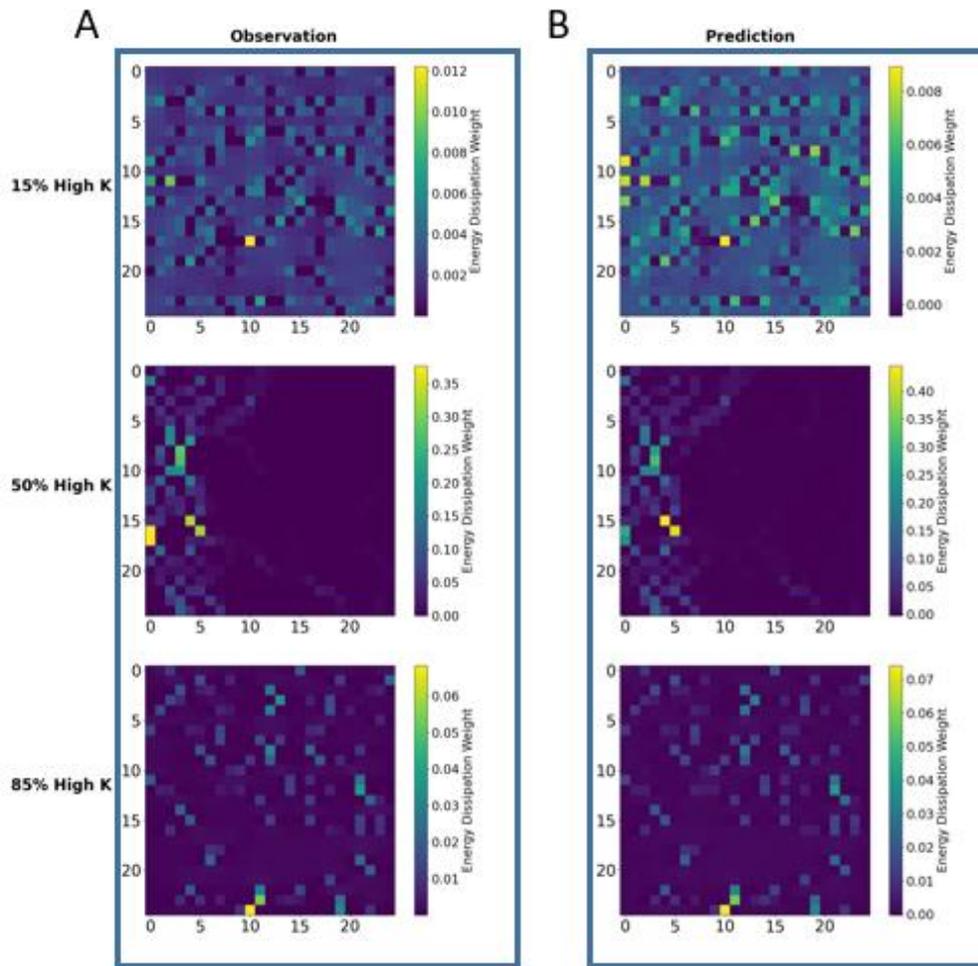
542 representations of the overall input-output mapping) while learning different internal
543 representations of the mapping from gridded K to K_{eff} .

544

545 **3-6- Inferring ED weights with UNET**

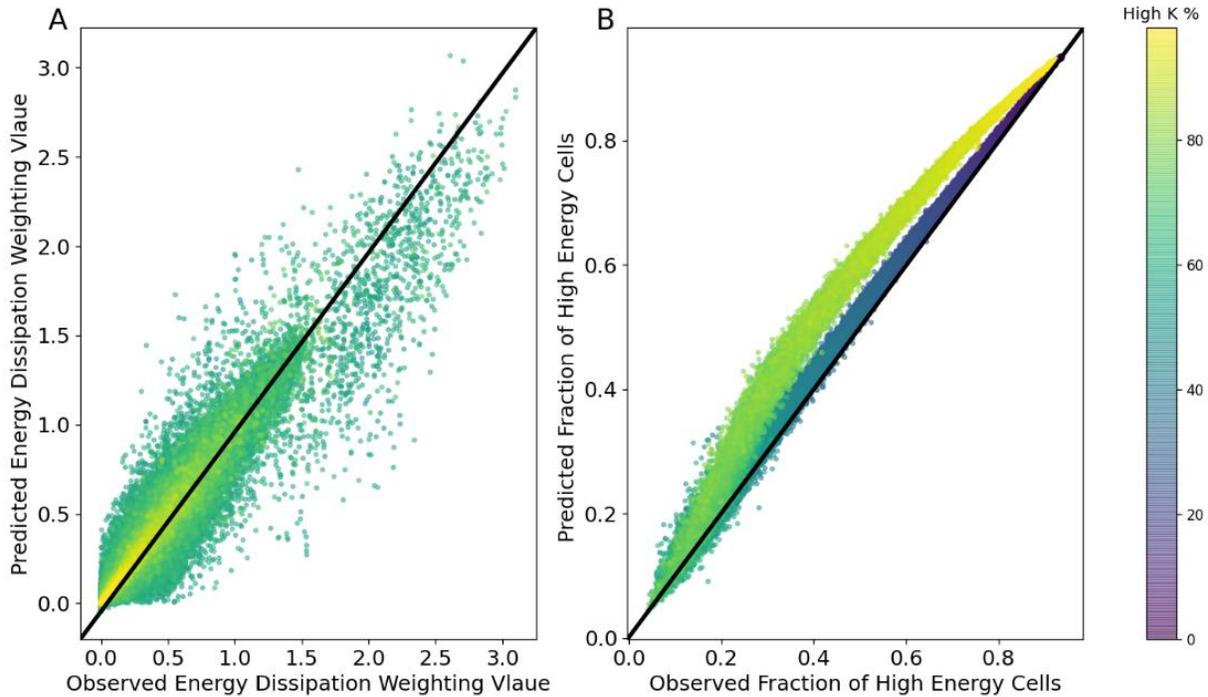
546 The performance of the informed UNET for inferring EC is illustrated for some example grids in
547 Figure 8. The correspondence between the ED weights predicted by the informed UNET and the
548 value calculated directly from the flow model shows low RMSE (0.0069) and high R2 (0.9549)
549 and the ability of the UNET to infer the fraction of high energy cells is likewise good
550 (RMSE=0.04876 and R2=0.9832). However, there is still a considerable mismatch (Figure 9A).
551 In particular, UNET consistently under-predicts the ED weights for cells that have very high actual
552 weight, while consistent over-predicting the fraction of high energy cells for cases with
553 intermediate percent high K (Figure 9B). From Figure 5b, these are the conditions that give rise
554 to the most concentrated weighting. Taken together, these results suggest that the UNET has
555 difficulty in inferring the ED weights when they are concentrated in highly localized areas (e.g.
556 60% high K material in Figure 5b).

557



558

559 Figure 8) Samples of energy dissipation weight distributions prediction for different ranges of percent of high K material. Panel A: Observation. Panel B: Predicted values.



560 Figure 9) Performance of informed UNET model in energy dissipation estimation A: Energy dissipation
 561 weighting prediction for all grids. B: Fraction of high energy dissipation cells prediction performance as function
 of percent of high K material.

562

563 4- Discussion

564 Based on the results presented above, we discuss three issues. First, can ML/DL learn relationships
 565 that can predict both the trend and grid-specific variation of K_{eff} as a function of percent high K
 566 material? Second, does the use of increasingly more complex architectures lead to the improved
 567 inference of K_{eff} ? Finally, can the DL algorithms make effective use of reduced information
 568 provided regarding ED weighting (here, the number of high energy cells), and can they use such
 569 information during training to infer patterns associated with ED weighting?

570

571

572 **4-1- Dependence of the ED Weighting Distribution on the K Field**

573 The K_{eff} associated with binary grids shows a highly nonlinear dependence on the percentage of
574 high K material (Figure 3). Specifically, K_{eff} is closer to the arithmetic mean for materials with
575 low to medium percentage of high K, while being approximately halfway between the arithmetic
576 and harmonic means for materials with a higher percentage of high K. The variation in this trend
577 is due to the influence of specific structural patterns in the spatial distribution of high and low K
578 cells among grid realizations. The maximum degree of variability occurs for materials with
579 intermediate percentages of high K values. In general, both the trend and the specific variations in
580 K_{eff} are very well explained by ED-weighted averaging (Figure 4).

581 Given that the energy dissipation weights carry information regarding the impact of structure on
582 the effective conductivity of a binary K field, we examined the nature of this weighting as a
583 function of the percentage of high K material present in the medium. Specifically, we defined the
584 minimum area that contains 95% of all of the ED weight, and classified the cells within this region
585 as being ‘high energy cells’.

586 At high and low percent high K conditions, the medium is nearly homogeneous, but the energy is
587 distributed over ~75% of the domain (Figure 6b). The ED weighting is more highly constricted,
588 residing in a smaller number of high energy cells, for 60% high K material grids. The restricted
589 high K areas centered around 60% high K material tend to form localized regions within which
590 most of the energy dissipation occurs, indicating the influence of structures that force the flow to
591 occur through regions of relatively low K, leading to high energy loss. However, as the percentage
592 of high K increases to 80%, the high weight areas become concentrated in a small number of
593 unconnected regions, suggesting a different structural mechanism whereby flow is forced through
594 a small number of low K cells, rather than being channeled through a continuous structure.

595

596 **4-2- Comparison of Performance**

597 By considering the ML/DL algorithms in order of increasing architectural complexity (DT, vanilla
598 CNN, UNET) we can assess the value of increased algorithmic complexity and the value of
599 providing reduced information about the ED weights. In summary (Table 1), performance
600 improves with architectural complexity and when ED information is provided. In terms of RMSE
601 and R^2 , all of the ML/DL algorithms, including a simple decision tree provided with only the
602 percent high K material, performed extremely well. So, the differences in performance are mainly
603 due to their abilities to make case-specific use of structural (pattern) information, which manifests
604 as variations in K_{eff} at any given percentage of high K material (Figure 7).

605

606 Table 1) Training, validation, and testing performance of all models

	Energy Dissipation Weight	DT (Only High K%)	DT (Only High K% + Number of High Energy Dissipation Cells)	Vanilla CNN	Vanilla CNN with High Energy Disispaition Zones	No Knowledge	Knowledge
K_{eff} RMSE (Train)	0	0.0213869	0.01332592	0.0171827	0.00864406	0.00626774	0.00964671
K_{eff} RMSE (Val)	0	0.0215940	0.01367984	0.0172679	0.00866852	0.01129849	0.01077667
K_{eff} RMSE (Test)	0	0.0213212	0.01334975	0.0171188	0.00873331	0.01129849	0.01064088
K_{eff} R (Train)	1	0.9970817	0.99886803	0.9981229	0.99952405	0.99975328	0.99941291
K_{eff} R (Val)	1	0.9970250	0.99880711	0.9981039	0.99952134	0.99920198	0.99926396
K_{eff} R (Test)	1	0.9971003	0.99886423	0.9981378	0.99951423	0.99918991	0.99928351
Energy Dissipation RMSE (Train)	NaN	NaN	NaN	NaN	NaN	0.02693278	0.00248980
Energy Dissipation RMSE (Val)	NaN	NaN	NaN	NaN	NaN	0.02703661	0.00548620
Energy Dissipation RMSE (Test)	NaN	NaN	NaN	NaN	NaN	0.03300000	0.00695936
Energy Dissipation R (Train)	NaN	NaN	NaN	NaN	NaN	-0.04757823	0.99531359
Energy Dissipation R (Val)	NaN	NaN	NaN	NaN	NaN	-0.04673303	0.97724645
Energy Dissipation R (Test)	NaN	NaN	NaN	NaN	NaN	-0.05657500	0.97722907

607

608 For all methods, the performance was poorest when K_{eff} values are low (Figure 7). The
 609 performance was also relatively poor for intermediate percentage levels of high K (Figure 10).
 610 That is, the methods had the most difficulty when localized structures act to impede flow, whether
 611 those structures are organized as a continuous region (intermediate high K percentage) or as
 612 isolated blocks of low K material (low K_{eff}).

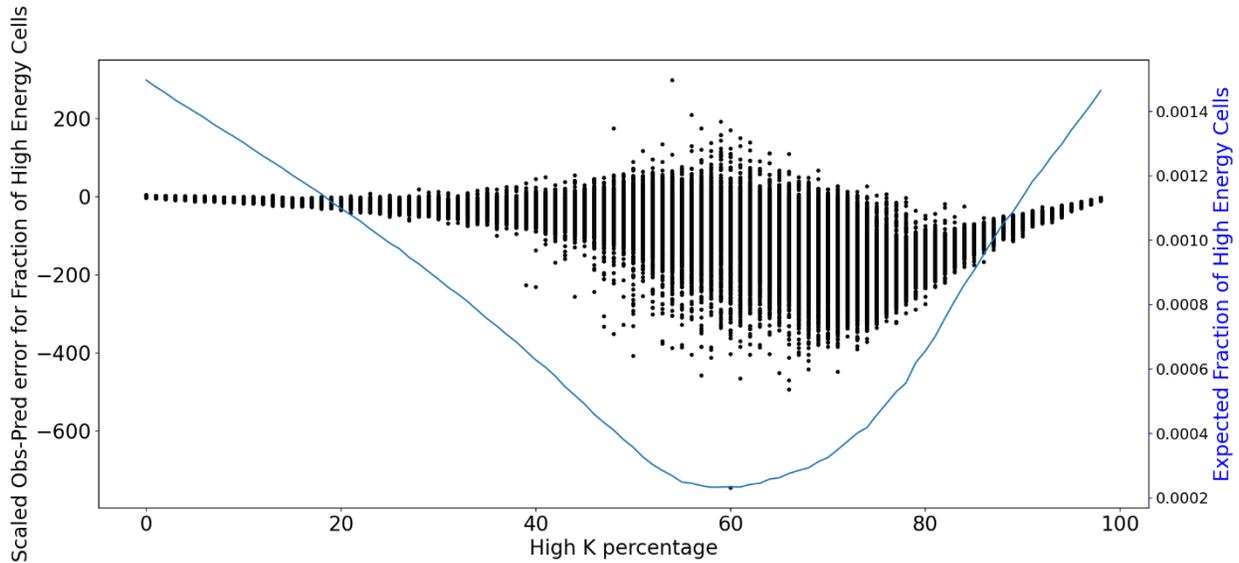


Figure 10) Difference between inferred and actual fraction of high K cells for each grid. To compare the errors of grids at each high k percentage, the values of left y axis is scaled by average of actual number of high k cells at each k percentage. The fraction of high K cells for a 95% threshold is presented by blue line.

613

614 **4-3- Hidden Layer Representation Analysis**

615 The superior performance of the informed UNET is notable because it does not require that the
 616 flow problem be solved to make predictions for the testing set. Specifically, once trained with ED
 617 weight information (requiring solving the flow problem during testing and validation), the UNET
 618 algorithm uses the learned relationships to infer the values of the ED weights for the test samples
 619 and combines this with the K grid to infer K_{eff} .

620 The performance of the uninformed UNET, for which ED weight information was never presented,
 621 so the flow problem never had to be solved, is comparable to that of the trained UNET. Given that
 622 the ED weights are thought to represent a key mechanism linking the K grid to the value of K_{eff} ,
 623 this raises the question of whether the uninformed UNET is somehow inferring information
 624 regarding the distribution of ED without being explicitly provided with such information during
 625 training.

626 For the informed UNET, the output layer of the lower branch, which is concatenated with the K
627 grid before the final step of inferring K_{eff} , represents the ED weight distribution. Examining the
628 corresponding layer of the uninformed UNET shows no correlation with the true ED weights.
629 However, a more advanced analysis, based on computing the centered kernel alignment similarity
630 (CKA) [Kornblith et al., 2019], provides a more complete picture of the information flows through
631 the informed and uninformed UNETs. These results are visualized as a similarity matrix (Figure
632 11). The output of each layer of the informed model is compared to other layers of the uninformed
633 model to examine the degree of similarity between them while accounting for the presence of
634 invertible linear transformations. A similarity value of zero between two layers indicates that their
635 representations are *not* invertible linear transformations of each other while a similarity value of 1
636 indicates that the two layers are equivalent up to a linear transformation.

637 We first compared the results for the informed UNET with that of an untrained network with
638 random initial weights and the same architecture (Figure 11a). The values on the diagonal
639 (representing the same layer in the two networks) have high CKA similarity for the first three
640 layers; this makes sense given that both networks are being fed the same inputs. However, the
641 similarity begins to diminish beyond that point; they show very strong dissimilarity at the output
642 layer, where the informed UNET is constrained to predict values that correspond to the ED
643 weights. They also differ strongly at the final dense layer because the untrained network did a
644 poor job of inferring K_{eff} .

645 Comparing the informed and uninformed UNETs gave striking results (Figure 11b). Namely,
646 layer similarity remains high for all layers *except* the output layer, where the informed UNET is
647 required to predict values that correspond to the ED weights. Further, the final dense layer is also

648 highly similar, reflecting the near-identical skill in predicting K_{eff} achieved by both the informed
649 and uninformed UNET.

650 In general, these results and patterns of similarity are consistent with the findings of *Kornblith et*
651 *al.*, [2019b] and *Thompson et al.* [2019]. They show that there can be many possible intermediate
652 architectural solutions to achieve the same task, but that the representations learned for the layers
653 closer to the inputs and the outputs tend to be similar. We interpret this to mean that the untrained
654 UNET can “learn” some useful information that is related to the ED weights directly from the K
655 grids. This information is not a direct map of actual ED weights. So, when required to produce
656 such a map (training under-informed conditions), the UNET learns an intermediate relationship
657 that can provide this map and to the user. It then uses the ED distribution to infer K_{eff} . However,
658 when not required to produce an ED map (training under uninformed conditions), the UNET does
659 not develop a layer to translate the information to a user-readable ED map. Rather, the latent
660 information about the ED weights propagates through the UNET, with an associated change in the
661 final dense layer to produce high-quality inferences of K_{eff} .

662

676 output of the mixed structure model and that of the informed model. This pattern is consistent with
677 the high CKA value observed in Figure 12 and suggests that an orthogonal transformation between
678 the weights was necessary to overcome the changes applied in the deeper layers and recover the
679 correct K_{eff} values. This analysis suggests that both the informed and uninformed UNET are
680 implementing similar computational processes, ostensibly extracting information corresponding
681 to the ED distribution from the K grid, but representing it differently in n-d dimensional space.
682 Further, that the user-imposed requirement to produce a readable ED map results in a nonlinear
683 transformation that must be compensated in later layers to produce accurate inferred K_{eff} values.

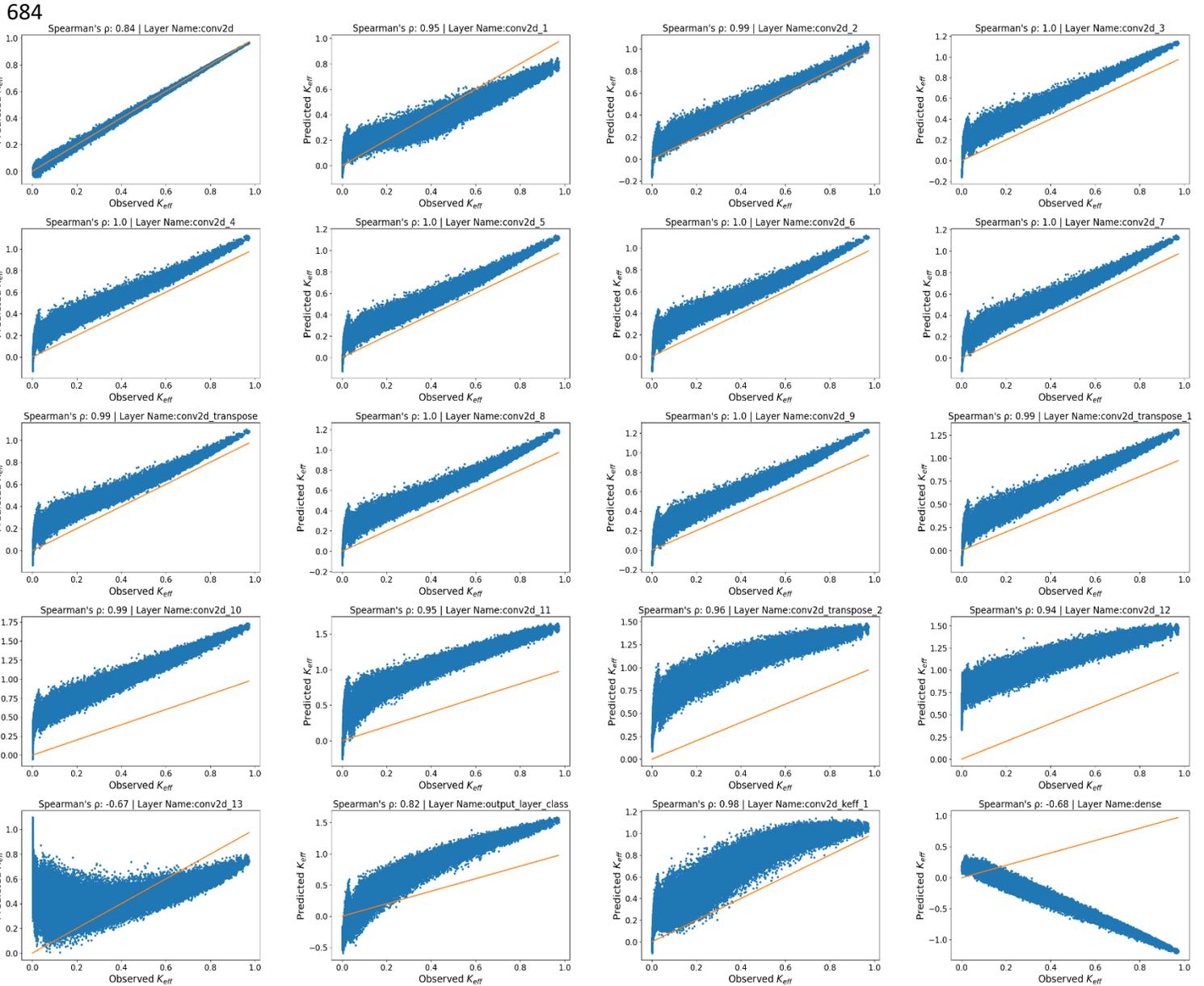


Figure 13) Correlation between True K_{eff} and the output of Unet model built up by sequential substitution of Informed model weights with Uninformed Unet collectively.

685

686 5-Conclusions

687 We have investigated the ability of ML and DL algorithms to infer the effective hydraulic

688 conductivity of binary K grids. All of the ML/DL methods were able to infer K_{eff} with extremely

689 high accuracy ($R^2 > 0.99$) when provided with only the binary grid. But, there was some
690 improvement in identifying the K_{eff} of outlier realizations, those most strongly affected by
691 structure, with increasing algorithmic complexity, progressing from a decision tree, to a vanilla
692 CNN, to a UNET.

693 Relying on previous work that showed the value of energy dissipation weighting for understanding
694 and inferring K_{eff} , we examined whether providing such information improved the ML/DL
695 performance. While adding information derived from the ED distribution improved the
696 performance of each algorithm, the improvement was similar to that realized by increasing the
697 algorithmic complexity.

698 The UNET architecture could be trained to infer the ED weighting from the K grid. This finding
699 was supported by a similarity analysis of the hidden layers of UNETs with and without ED
700 information provided. The accuracy of the inferred ED weights was lower when the energy
701 dissipation weights were concentrated into small areas; i.e., the UNET was better able to infer the
702 impacts of diffuse structures than highly localized structures. This finding may be due to the
703 relatively small number of realizations that showed strong structural control in our sample set,
704 suggesting that future work should examine this possibility.

705 While the UNET extracted the relevant ED weight information from the K grids, it only translated
706 this information to a user-readable map if forced to do so. This may have other implications for
707 the use of ML/DL techniques in subsurface hydrology. For example, ML/DL algorithms may be
708 able to implicitly infer head distribution information ‘naturally’ if they are trained to predict
709 streamflow; but the head distributions may not be available to the user unless the algorithms are
710 specifically designed to produce them. This may be an important consideration if ML/DL

711 algorithms are applied to models with multiple calibration data types or if the models will be used
712 for multi-objective decision support.

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714 **6-References**

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883 7-Data Availability

- 884 The data that supports the findings of this study are openly available in the University of Arizona
885 research data repository at [10.25422/azu.data.13324796](https://doi.org/10.25422/azu.data.13324796).

886 Appendix

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Vanilla CNN	Modified Unet Model
3*3 conv. 8-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	3*3 conv. 16-same padding-stride 1-Relu *2 2*2 Maxpooling stride 2
3*3 conv. 16-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	3*3 conv. 32-same padding-stride 1-Relu *2 2*2 Maxpooling stride 2
3*3 conv. 32-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	3*3 conv. 64-same padding-stride 1-Relu *2 2*2 Maxpooling stride 2 Dropout 0.64
3*3 conv. 16-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	3*3 conv. 128-same padding-stride 1-Relu *2
3*3 conv. 8-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	2*2 Conv2DTranspose. 64-same padding-stride 2-No activation *1 Cropping Concatenation 3*3 conv. 64-same padding-stride 1-Relu *2
3*3 conv. 4-same padding-stride 1-Relu *2 2*2 Maxpooling stride 1	2*2 Conv2DTranspose. 32-same padding-stride 2-No activation *1 Cropping Concatenation 3*3 conv. 32-same padding-stride 1-Relu *2
Flatten 1 Dense-Linear	2*2 Conv2DTranspose. 16-same padding-stride 2-No activation *1 Cropping Concatenation 3*3 conv. 16-same padding-stride 1-Relu *2
	1*1 conv. 1-same padding-stride 1-No activation *1
	Concatenation 3*3 conv. 10-same padding-stride 1-Tanh *1 Flatten 1 Dense-Linear

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Table A1 Deep learning structure parameters. A: vanilla CNN Structure.B: UNET model structure.