

Forcing of the MJO-related Indian Ocean Heating on the Intraseasonal Lagged NAO

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Abstract

Based on the experiments with the Coupled Forecast System version 2 (CFSv2), the mechanism by which the Madden-Julian Oscillation (MJO) modulates the North Atlantic Oscillation (NAO) is investigated. To isolate the cyclic MJO heating with an eastward propagation over the Indian Ocean and western Pacific, three sets of experiments are conducted with spatio-temporal varying heating added to the model's internally generated heating. The results suggest that the anomalous MJO heating over the Indian Ocean, rather than the western Pacific, dominates the formation of the NAO anomaly in the following 10-20 days. The MJO heating triggers a westward propagation of the storm track that influences Europe, complementing the eastward pathway of influence via the North Pacific. Both pathways contribute to an enhanced storm track over the North Atlantic and the positive NAO anomaly. The Eurasian pathway is less important for the formation of the negative NAO anomaly.

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3 **NAO**

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15
16 **Key Points:**

- 17
- 18 • The lagged connection of the NAO with the MJO is reproduced well in the CFSv2 model
with prescribed cyclic MJO heating forcings
 - 19 • The MJO-related heating (cooling) over the Indian Ocean alone plays a dominant role in
20 the formation of the positive (negative) NAO anomaly
 - 21 • The MJO affects the NAO via a secondary Eurasian (westward oriented) pathway, and
22 the primary North Pacific (eastward oriented) pathway
- 23

24 **Abstract**

25 Based on the experiments with the Coupled Forecast System version 2 (CFSv2), the mechanism
26 by which the Madden–Julian Oscillation (MJO) modulates the North Atlantic Oscillation (NAO)
27 is investigated. To isolate the cyclic MJO heating with an eastward propagation over the Indian
28 Ocean and western Pacific, three sets of experiments are conducted with spatio-temporal varying
29 heating added to the model’s internally generated heating. The results suggest that the anomalous
30 MJO heating over the Indian Ocean, rather than the western Pacific, dominates the formation of
31 the NAO anomaly in the following 10–20 days. The MJO heating triggers a westward
32 propagation of the storm track that influences Europe, complementing the eastward pathway of
33 influence via the North Pacific. Both pathways contribute to an enhanced storm track over the
34 North Atlantic and the positive NAO anomaly. The Eurasian pathway is less important for the
35 formation of the negative NAO anomaly.

36 **Plain Language Summary**

37 As the dominant source of predictability for subseasonal forecasts, the Madden–Julian
38 Oscillation (MJO) has a great impact on the leading winter extratropical mode, the North
39 Atlantic Oscillation (NAO). Previous studies suggested that the impact is through the
40 downstream propagation of the MJO-excited Rossby wave across the North Pacific and its
41 interaction with synoptic eddies over the North Atlantic. In addition to the traditional Pacific
42 pathway, here we find another pathway by which the MJO convection over the Indian Ocean
43 triggers a westward propagation of the Asian storm track that penetrates Eurasia and influence
44 the wave–eddy interaction related to the NAO.

45 **1 Introduction**

46 The North Atlantic Oscillation (NAO), one of the dominant mode of the extratropical
47 atmospheric variability, has a significant influence on weather and climate over the wide
48 northern hemisphere (Hurrell et al., 2003). The NAO varies temporally with periods spanning a
49 broad spectrum from synoptic to decadal, and its activity at intraseasonal timescale is one
50 substantial source of extended-range weather forecasting. To predict NAO activity at
51 intraseasonal timescales is thus of substantial importance.

52 The Madden–Julian Oscillation (MJO), the prominent mode of tropical intraseasonal
53 variability, is characterized with large-scale convection propagating eastward through the Indian
54 Ocean and the western Pacific along with baroclinic atmospheric circulation anomalies (Madden
55 & Julian, 1994; Zhang, 2005). Since the associated heating drives atmospheric teleconnections,
56 the MJO has a great impact on the extratropical atmospheric circulations (Garfinkel et al., 2014;
57 Matthews et al., 2004; Seo & Son, 2012; Stan et al., 2017; Zheng & Chang, 2019).

58 Previous studies have revealed a lagged connection of the NAO with preceding MJO
59 events (Cassou, 2008; Jiang et al., 2017; Lin et al., 2009). The positive (negative) NAO tends to
60 follow the enhanced (reduced) convection over the Indian Ocean at a lag of 10–15 days, which
61 corresponds to the MJO phase 3 (phase 6). Such a lagged connection is reproduced well both in
62 simplified general circulation models (GCMs) forced with the fixed MJO heating (Lin & Brunet,
63 2018; Shao et al., 2019) and in fully coupled atmosphere-ocean models forced with the eastward-
64 moving MJO heating (Straus et al., 2015; Yadav et al., 2019). This suggests that the MJO’s
65 leading impact on the NAO is a robust intrinsic feature of the atmosphere. Thus it provides an
66 important source for subseasonal predictability of the NAO (Lin et al., 2010; Tseng et al., 2018).

67 Physically, the MJO’s impact on the NAO may originate from the MJO-excited Rossby
68 wave propagation toward the North Atlantic and its subsequent interaction with synoptic eddies
69 locally (Cassou, 2008; Lin et al., 2009). An initiation of Rossby wave trains in the Pacific and
70 the interactions among the transient eddies from the eastern Pacific during the MJO phase 3
71 (phase 6) are considered to be responsible for setting the positive (negative) NAO phase (Rivière
72 & Drouard, 2015; Fromang & Rivière, 2020). Another pathway of influence was suggested by
73 Lin et al. (2015), who indicated that the MJO convection anomaly over the Indian Ocean may
74 induce a disturbance in the South Asian jet that propagates along the midlatitude waveguide
75 (e.g., Branstator, 2002) and affects the NAO. In addition to the wave train across the North
76 Pacific, Shao et al. (2019) found that the MJO heating initiates an upstream and westward
77 propagation of disturbances to western Asia-Europe along the Asian subtropical jet. Lin and
78 Brunet (2018) also revealed an early influence of a westward propagating Rossby wave excited
79 by the MJO. This suggests the possibility of multiple pathways for the mechanism of the MJO’s
80 influence on the NAO.

81 To further explore the possible pathways and understand the mechanism for the MJO–NAO
82 connection, it is helpful to isolate the individual contribution of the MJO-related regional and
83 moving heating over the Indian Ocean and the western Pacific. On one hand, the positive heating
84 anomaly over the western Pacific tends to induce a negative-phased NAO (Li et al., 2006b; Lin
85 et al., 2005; Yadav and Straus, 2017), and this influence is sensitively dependent on the
86 longitudinal position of the heating. On the other hand, the tropical Indian Ocean heating induces
87 an NAO tendency toward its positive phase (Hoerling et al., 2004; Li et al., 2006a; Lin et al.,
88 2015; Yu & Lin, 2016). Note that there is potential interference between the effects of the MJO’s
89 Indian Ocean and western Pacific heating, because one excited Rossby wave can alter the
90 background flow and affect the route of a Rossby wave excited by its counterpart.

91 In order to isolate the individual and combined roles of the MJO-linked regional heating,
92 we use a coupled ocean–atmosphere–land model, CFSv2, to conduct sensitivity experiments.
93 Since the initial state is still important for the extended-range weather forecasting, we use
94 observed initial conditions, but add idealized, temporally evolving heating, designed to mimic
95 realistic propagating MJO heating, to the full coupled model. Such a scheme preserves the
96 information embedded in the initial state containing the preceding MJO’s signal, and thus has
97 advantages over that with fixed heating forcing (Fromang & Rivière, 2020).

98 **2 Model and Methods**

99 2.1 Model Experiments

100 The coupled model, Climate Forecast System model version 2 (CFSv2) of the National
101 Centers for Environmental Prediction (NCEP), is used. Its atmospheric component model (the
102 Global Forecast System) has a T126 horizontal resolution with 64 vertical levels. The outputs are
103 interpolated to $1^\circ \times 1^\circ$ resolution and 11 pressure levels. The oceanic component is the Modular
104 Ocean Model version 4 (MOM4) from the Geophysical Fluid Dynamics Laboratory (GFDL).
105 The details of the CFSv2 are described in Saha et al. (2014).

106 The Control runs consist of four-month reforecasts (1 December to 31 March) beginning
107 from three sets of perturbed initial conditions (ICs) on 1 December of each year over the 31-yr
108 period (1980–2010), thus yielding a total of 93 simulations of 121 days. The ICs for atmosphere,
109 ocean, sea-ice, and land surface are obtained from the CFS Reanalysis (CFSR) (Saha et al.,

110 2010), of which the atmosphere ICs are perturbed by blending different atmospheric states
111 through a weighted average (e.g., Yadav et al., 2019).

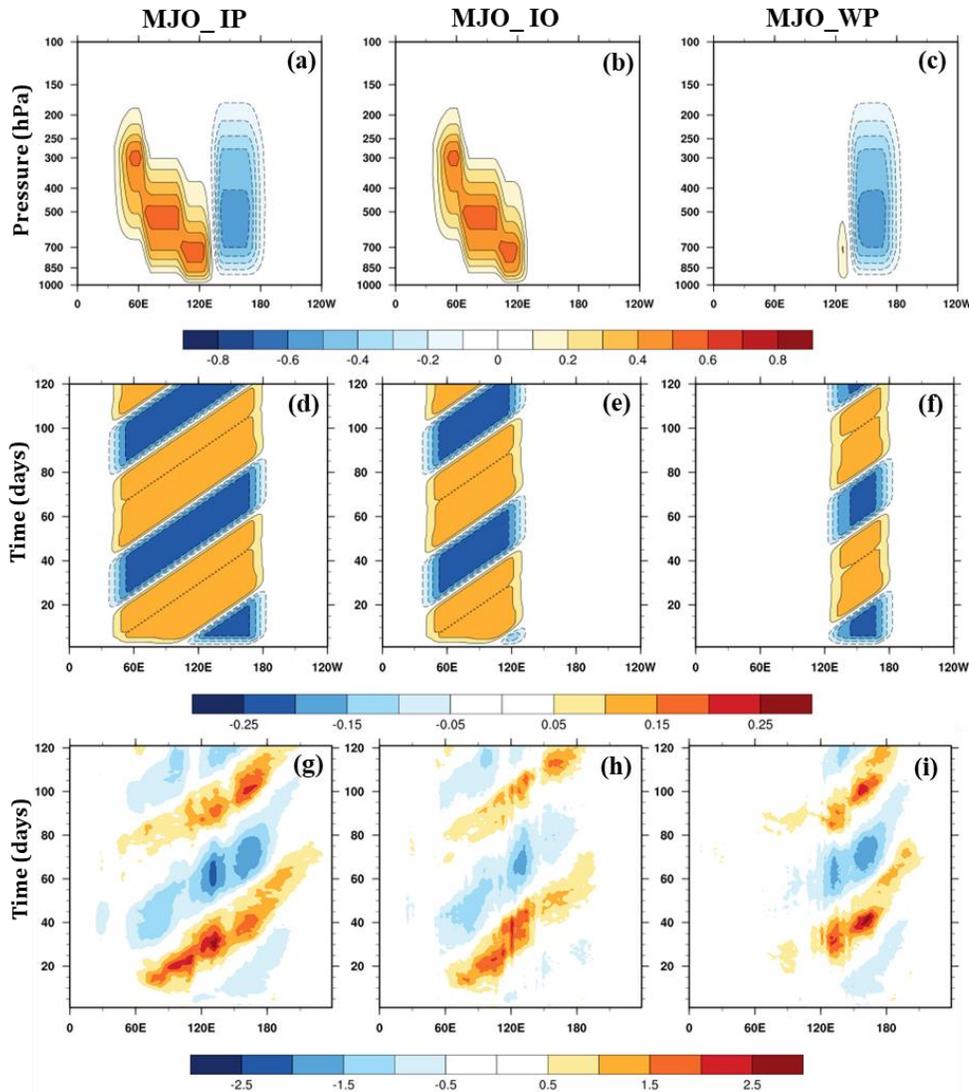
112 An idealized MJO evolving heating is added to model generated temperature tendency to
113 mimic realistic MJO cycles. Here the idealized MJO heating is prescribed with the spatial pattern
114 and propagating features by combining the technique developed by Jang and Straus (2012) and
115 Straus et al. (2015), and with the vertical profile based on estimates of the total diabatic heating
116 from the tropical rainfall measuring mission (TRMM) as Straus et al. (2015). The technique was
117 also recently applied for model heating bias correction by Swenson et al. (2019). The magnitude
118 and temporal structure of the idealized heating are overall based on observations of Yadav and
119 Straus (2017). Such an added heating, even with a relatively small magnitude, can effectively
120 organize the evolution of tropical diabatic heating in the model to give a robust MJO (Straus et
121 al., 2015).

122 To understand the model response to isolated MJO cycles, three sets of MJO-heating
123 experiments with heating forcing over different regions are conducted, including the Indo–
124 western Pacific Ocean (MJO_IP) runs, Indian Ocean (MJO_IO) runs, and western Pacific
125 (MJO_WP) runs. All these experiments are listed in Table S1 in the supporting information.
126 Note that the MJO_IP runs represent the typical MJO cycles, similar to the Slow Repeated
127 Cycles runs in Yadav et al. (2019), except for a smaller ensemble size. A maximum added
128 heating rate of 0.8 K d^{-1} was chosen with the overall magnitude scaled, so that the *total* (model
129 generated plus added) heating was roughly close to the observations. A fixed phase speed of 3°
130 longitudes per day was adapted to match the slow cases, yielding a period of 60 days.

131 Figures 1a–1f display the spatial structure and temporal evolution of the idealized heating
132 for these experiments. The vertical structure of the heating (Figures 1a–1c) indicates an evolution
133 from shallow to deep gradually (Yadav et al., 2019), accompanied by an eastward propagation
134 with two complete MJO cycles (Figures 1d–1f). The added heating decays off the equator as a
135 Gaussian form with an e-folding scale of 15° latitudes (Figure S1). The vertically averaged *total*
136 diabatic heating anomalies are shown in Figures 1g–1i. The diabatic heating in the MJO_IP runs
137 matches the observational slow MJO cases of Yadav and Straus (2017), except for an
138 amplification by a factor of two. The heating in the MJO_WP runs is additionally induced over
139 the eastern Indian Ocean centering around 90°E , lagging that in MJO_IO runs by about 10 days.
140 This may be caused by the feedback of the mid-latitude waves to tropical convective heating

141 (Frederiksen & Lin, 2013; Moore et al., 2010). Overall, the prescribed heating mirrors the
 142 horizontal structure of the MJO diabatic heating reasonably well (Figure S2).

143



144

145 **Figure 1.** The pressure-longitude cross-section of added heating anomalies on day 12 (a–c), vertically
 146 averaged (over 1000–50 hPa) added heating anomalies (d–f) and total diabatic heating anomalies (g–i) at
 147 each reforecast day. Displayed is the value averaged over latitudes 15°S–15°N. From left to right, it
 148 corresponds to MJO_IP, MJO_IO, and MJO_WP runs, respectively. Units are K day⁻¹.

149 **2.2 Analysis Methods**

150 The NAO pattern is defined as the first empirical orthogonal function (EOF) mode of the
 151 daily 500-hPa geopotential height fields (Z500) over the North Atlantic region (20°N–85°N,

152 90°W–30°E). The daily NAO indices are calculated as the projection of the daily Z500
153 anomalies onto the NAO pattern; this time series of projections is subsequently normalized. The
154 occurrence probabilities of the positive (negative) phase of the NAO at each reforecast day are
155 obtained by counting the number of days with the daily NAO index greater (less) than 0.5 (-0.5)
156 and then dividing by the total ensemble size of 93. When comparing the contribution of the MJO
157 heating imposed over different regions, the identical NAO pattern in Control runs is used for
158 calculating the NAO index. For each experiment, anomalies are defined as departures from the
159 annual cycle in the Control runs. This model annual cycle is estimated by projecting the daily
160 time series of each winter separately onto the first three Legendre polynomials in time as
161 described in Straus et al. (2003), and then averaging over all winters. We use Fourier
162 decomposition as a spatial filter method to isolate the synoptic-scale (zonal waves 5–12) eddies.

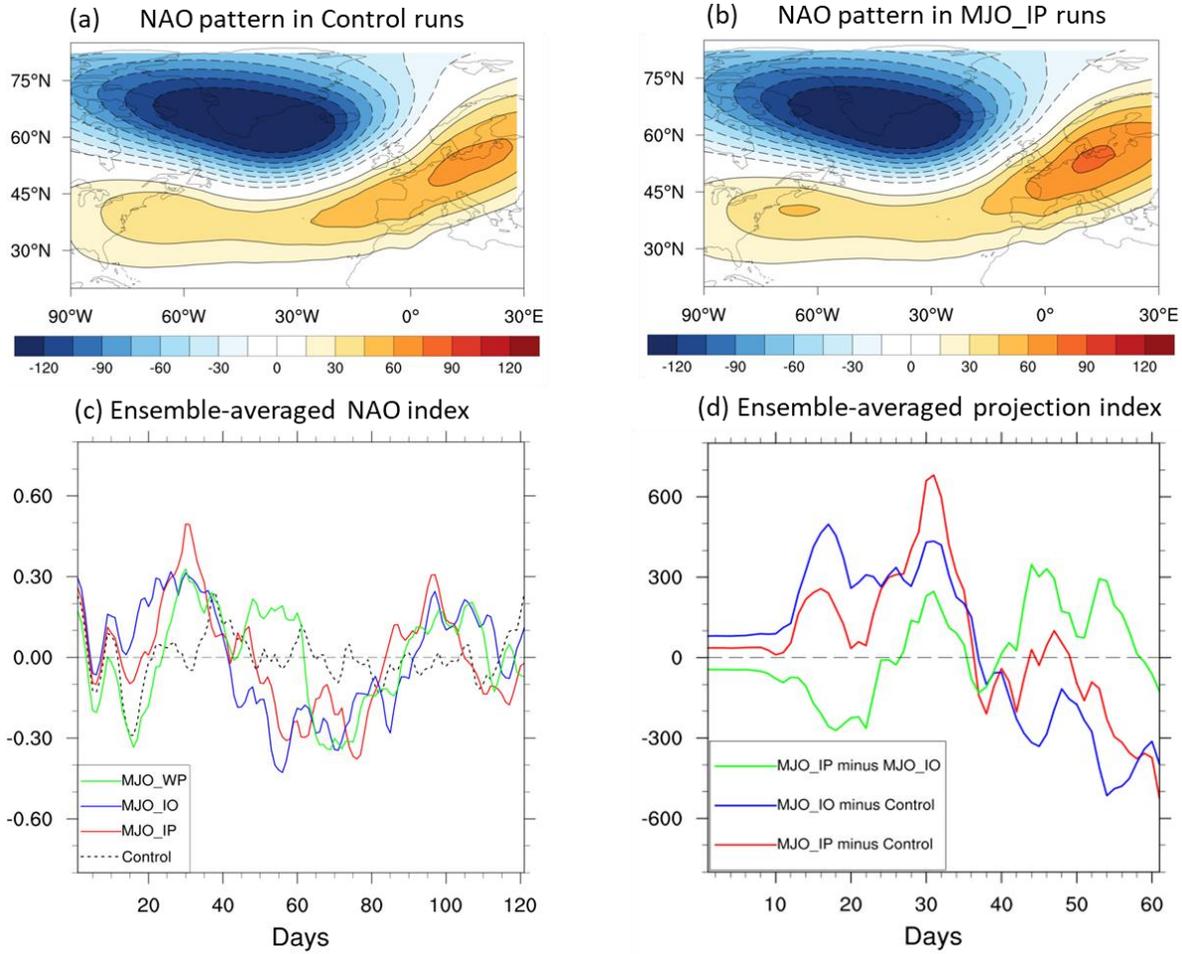
163 **3 Results**

164 The NAO pattern in Control runs (Figure 2a) agrees well with that in the ERA-Interim
165 reanalysis (Dee et al., 2011) as shown in Yadav et al. (2019). For the MJO_IP runs, the NAO
166 pattern is similar to that in Control runs, with a slightly stronger amplitude over the positive
167 sector (Figure 2b). As the model simulates both the evolving MJO cycles and the NAO pattern
168 well, we first investigate whether the observed MJO–NAO linkage can be reproduced in the
169 MJO_IP runs. Figure S3 illustrates the occurrence probabilities of the NAO at each reforecast
170 day in the MJO_IP runs. For the first (second) cycle, the occurrence probabilities of the positive
171 NAO are increased about 10–15 days after the MJO heating reaches roughly the 90°E longitude
172 at around day 15 (80). Conversely, the increase of the negative NAO occurs 15–20 days
173 following the MJO heating (cooling) over the western Pacific (Indian Ocean) at around day 40.
174 This suggests that the MJO–NAO connection can be captured well by forcing this coupled model
175 with the anomalous heating associated with the MJO cycles.

176 In order to compare the contribution of the MJO heating over different regions, the
177 evolution of NAO index from day 1 to 121 in each experiment is displayed (Figure 2c). Similar
178 to the occurrence probabilities, the averaged NAO indices show fluctuations of roughly two
179 cycles. During the first 10 days, the NAO indices in each MJO-heating runs are close to that in
180 Control runs. After day 15, the NAO index in MJO_IO runs begins to increase until around day
181 30. Generally, the increase of the NAO index in MJO_IO runs leads that in MJO_WP runs for

182 about 10 days during the first cycle. This indicates that the positive NAO anomaly may be firstly
183 initiated by the Indian Ocean heating of the MJO. Note that the NAO indices in the second
184 cycles display relatively weaker amplitudes to those in the first cycles, in coincidence with the
185 somewhat weaker MJO heating anomalies over the Indian Ocean. As complex tropical-
186 extratropical interactions are involved in the second cycle, we mainly focus on the NAO-like
187 response in the first cycle.

188 It is difficult to directly interpret the NAO-like response to the MJO-related regional
189 forcing because the additional heating over the Indian Ocean (western Pacific) are induced in the
190 MJO_WP (MJO_IO) runs. To isolate the contribution of the MJO forcing over the western
191 Pacific, we examine the differences in the heating (see Figure S4a) and response between the
192 MJO_IP and MJO_IO runs. The differences of Z500 over the North Atlantic between the
193 MJO_IP and MJO_IO runs, and between the MJO_IP (MJO_IO) and Control runs, are projected
194 onto the NAO pattern in Control runs. Figure 2d displays the projection indices of the Z500
195 differences for the MJO_IP minus MJO_IO runs (green curve), MJO_IP minus Control runs (red
196 curve), and MJO_IO minus Control runs (blue curve). The green curve shows that the MJO
197 heating over the western Pacific only contributes at a later stage. In contrast, the blue curve
198 indicates a dominant role of the anomalous Indian Ocean heating on the NAO anomaly. The 200-
199 hpa streamfunction together with wave activity vectors for the raw MJO_IP runs demonstrate
200 that the MJO-initiated Rossby waves originate mostly from the Indian Ocean heating/cooling
201 region (Figure S5). Seo and Son (2012) showed that the Indian Ocean heating can generate a
202 much broader and stronger Rossby wave source because of its position relative to the subtropical
203 jet, where the relative vorticity is large. This further verifies the crucial role the anomalous MJO
204 heating over the Indian Ocean. Thus, we will concentrate on the response to the heating forcing
205 in the MJO_IO runs.



206

207 **Figure 2.** The 500-hpa geopotential height (Z500) anomalies (unit: gpm) regressed onto the NAO index in (a)

208 Control runs and (b) MJO_IP runs, together with (c) ensemble-averaged NAO index at each reforecast day for

209 the MJO_IP (red curve), MJO_IO (blue curve), MJO_WP (green curve) and Control runs (black curve), and (d)

210 projection indices of the Z500 differences for the MJO_IP minus MJO_IO runs (green curve), the MJO_IP

211 minus Control runs (red curve), and the MJO_IO minus Control runs (blue curve), respectively.

212

213 The differences of the Z500 between the MJO_IO and Control runs from day 7 to day 21

214 are shown in Figure 3, which illustrates the evolution of the extratropical response to the MJO

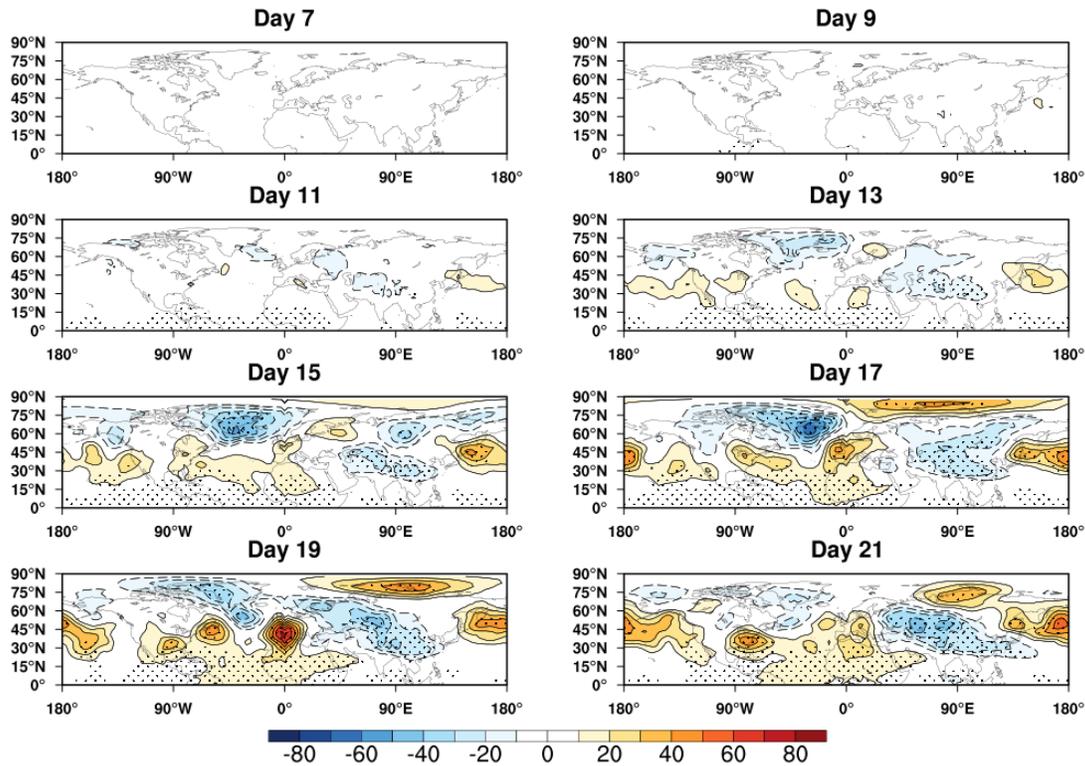
215 heating. Since the diabatic heating anomaly over the Indian Ocean does not appear until around

216 day 7 (see Figure S4b), there is no evident response before day 11. From day 13 to day 15,

217 negative anomalies of the geopotential height are built up over the subtropical Asia and extend

218 northwestward. There is also formation of an anomalous anticyclone over the western North

219 Pacific, along with a north–south dipole over the eastern North Pacific. Over the high latitudes of
 220 the North Atlantic, a negative height anomaly is formed, which deepens over the Greenland
 221 region until day 17. Meanwhile, a positive height anomaly to the northwest of the Indian Ocean
 222 extends westward, merging with the one over the subtropical North Atlantic, together forming
 223 the southern part of the NAO-like pattern. Thus, a positive NAO-like pattern is developed.
 224 Delayed by 15–20 days from the cooling over the Indian Ocean (see Figure S4b), a strong
 225 negative NAO-like response is developed at around days 55–61 (Figure S6). Prior to the
 226 formation of negative NAO anomaly, the positive height anomalies over the Eurasia and negative
 227 height anomalies over the North Pacific are established respectively, which are generally
 228 reversed to the situation following the heating over the Indian Ocean.



229
 230 **Figure 3.** Composite differences of the 500-hPa geopotential height (unit: gpm) between the MJO_IO and
 231 Control runs from day 7 to day 21. Dotted is significant at the 90% confidence level according to a Student's t
 232 test.

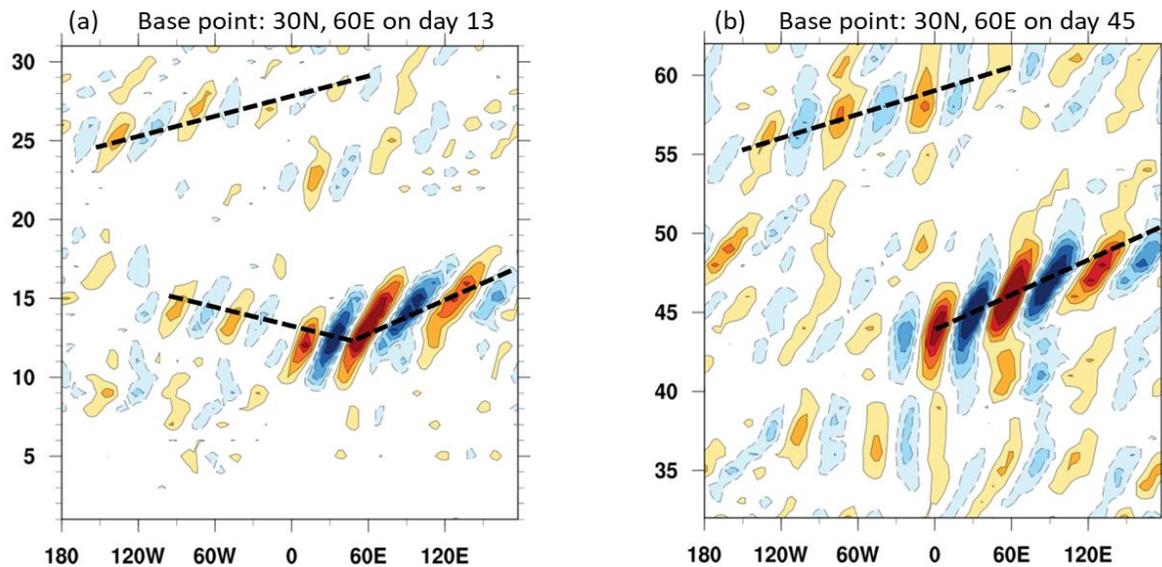
233
 234 Because the subtropical jet can act as a waveguide to modulate the wave/eddy propagation
 235 (Lee et al., 2019; Zheng & Chang, 2020), we further investigate the differences of the zonal wind
 236 at 300 hpa between the MJO_IO and Control runs (Figure S7). At the initial stage (days 7–12), a

237 positive zonal wind anomaly is induced over the subtropical Asian region and enhances with
238 both westward and eastward extension. At days 13–15, a positive zonal wind anomaly is formed
239 over the mid-latitudes of North Atlantic. Then it strengthens and exhibits a poleward shift at days
240 16–18, along with a negative anomaly built up to its south. This suggests that the North Atlantic
241 mid-latitude jet is pushing northward, in favor of the formation of the positive NAO anomaly.

242 To understand how the anomalous subtropical Asian jet related to the MJO modulates the
243 North Atlantic jet, we examine the shift in the storm tracks. Figure S8 shows the evolution of the
244 300-hPa synoptic-scale $v'v'$ anomaly (the difference between the MJO_IO and Control runs). At
245 days 10–12, the positive $v'v'$ anomalies are established along the South Asia jet, which extend to
246 the western Europe at days 13–15, indicating an expanding of Asian storm track influencing the
247 western Europe directly. Subsequently, the storm tracks are enhanced over the eastern North
248 Atlantic. In addition, the strengthening storm tracks over the North Pacific exhibit an eastward
249 extension, which seem to influence the North Atlantic at days 22–24. Both eastward and
250 westward extension of the enhanced storm tracks are likely to contribute to the positive NAO
251 anomaly. On the contrary, the weakened subtropical Asian jet (at days 43–45) and the
252 subsequent weakening storm tracks (at around days 49–57) over the North Atlantic are
253 conducive to the negative NAO anomaly.

254 In order to detect the pathways via which the MJO-induced disturbances propagate into the
255 North Atlantic, we further calculate the one-point lead-lag correlation of the 300-hPa synoptic-
256 scale meridional wind anomaly (v'), where a base point is chosen nearby the subtropical Asian
257 jet at 60°E, 30°N. The lead-lag correlation coefficients are presented as a function of time and
258 longitude, averaged from 30°N to 40°N (Figure 4). Consistent with the westerly jet stream, the
259 synoptic eddies generally exhibit eastward movement. The westward propagation indicated by
260 the dashed line in Figure 4a suggests that the synoptic eddies over the North Atlantic at around
261 days 12–15 may be affected by those from the South Asia jet. From day 16 to 18, the synoptic
262 eddies over the North Atlantic in MJO_IO runs exhibit a faster eastward phase speed with
263 respect to those in Control runs, along with a northeast–southwest tilt (Figure S9), favoring the
264 development of the positive NAO phase (e.g., Ren et al., 2012; Song, 2016). As such, the
265 anomalies along the Asian subtropical jet may firstly influence the positive NAO through the
266 westward Asian-Europe pathway.

267 On the other hand, the disturbances induced along the subtropical Asian jet propagate
 268 across the North Pacific and downstream into the North Atlantic from day 12 to day 28. The
 269 increase of the projection index later at around days 22–30 (see Figure 2d) could be largely
 270 attributed to the Pacific pathway. This also suggests that it takes a longer time for the MJO
 271 heating over the Indian Ocean to affect the NAO via the Pacific pathway than the westward
 272 pathway. The eastward tilt of the lines in Figure 4b shows a more traditional Pacific pathway (at
 273 days 45–60) for the negative NAO-like responses at around days 55–60, while the westward
 274 pathway is much weaker. This indicates that the Eurasian pathway may play a secondary role.



275 **Figure 4.** One-point lead-lag correlation coefficients of 300-hpa synoptic-scale v' for a base point at 30°N,
 276 60°E on day 13 (a) and day 45 (b), averaged over the latitudes 30°N–40°N. Here, v' is the difference of the
 277 meridional wind (waves 5–12) between the MJO_IO and Control runs. The ordinate is reforecast time. The
 278 interval of the contours is 0.1.
 279

280 4 Summary and Discussions

281 The mechanism for the observed lagged-connection of the NAO with the MJO is
 282 investigated by forcing a coupled model (CFSv2) with idealized cyclic MJO heatings. Three sets
 283 of experiments, each having an integration of two eastward propagating MJO cycles with a
 284 period of about 60 days, are conducted to isolate the contribution of the MJO-related heating
 285 anomalies over the Indian Ocean and western Pacific, respectively. The results demonstrate an
 286 increase of the positive (negative) NAO occurrence following the MJO heating (cooling) over
 287 the Indian Ocean at a lag of 10–15 (15–20) days. Furthermore, the anomalous MJO heating over

288 the Indian Ocean, rather than that over the western Pacific, dominates the NAO-like response.
289 The MJO heating over the Indian Ocean can exert its influence via the traditional pathway across
290 the North Pacific, however part of the impact may be transmitted via the Eurasia, which takes a
291 shorter time (around 7–10 days). The shift of the strengthened subtropical Asian jet causes an
292 expanding Asian storm track to propagate westward, influencing the Europe and enhancing the
293 storm tracks over the eastern North Atlantic, thus favoring the development of the positive NAO.
294 On the other hand, the induced disturbances in the subtropical Asian jet propagate across the
295 North Pacific and downstream into the North Atlantic, enhancing the NAO after around 10–15
296 days. The situation is essentially reversed following the MJO's cooling over the Indian Ocean for
297 the negative NAO-like response, although the Eurasian pathway does not seem to play a role
298 here.

299 Since the MJO-related heating anomalies over the Indian Ocean and the western Pacific
300 are not independent, and presumably feed back on each other, the dominant effect of the
301 anomalous MJO heating over the Indian Ocean does not rule out the potential role of the heating
302 over the western Pacific. The western Pacific heating anomaly has minor contribution, probably
303 because the affected initial state of the portion of the subtropical jet is less effective in
304 transporting the disturbances along the jet waveguide to the North Atlantic (e.g., Lin & Brunet,
305 2018).

306 While we have shed light on the direct MJO-related tropical forcing of the North Atlantic
307 region, other mechanisms are likely to play a role, such as the possible stratosphere pathway (e.g.,
308 Barnes et al., 2019; Lee et al., 2019). There are also tropical–extratropical interactions of
309 intraseasonal oscillations (Frederiksen & Lin, 2013), which may play a role in the model
310 experiments. For example, the synoptic eddies from the North Atlantic jet may affect those along
311 the subtropical jet, which in turn have an influence on the North Atlantic jet through downstream
312 propagation. The mechanism for how the extratropics influence the tropical heating linked to the
313 MJO deserves further investigation.

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323 (<https://apps.ecmwf.int/datasets/data/interim-full-daily/levtype=pl/>). The NCEP Climate Forecast
324 System Reanalysis (CFSR) can be obtained from [https://climatedataguide.ucar.edu/climate-](https://climatedataguide.ucar.edu/climate-data/climate-forecast-system-reanalysis-cfsr)
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[Geophysical Research Letters]

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Supporting Information for

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[Forcing of the MJO-related Indian Ocean heating on the Intraseasonal Lagged NAO]

5

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Contents of this file

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Text S1

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Table S1

15

Introduction

16

This supporting information provides the method for calculating the horizontal components of

17

the wave activity flux (Text S1), and description of the model experiments (Table S1). Figures

18

S1–S9 are provided to support the analysis presented in the main text.

19

Text S1.

20

We calculate the horizontal components of the phase-independent wave activity

21

flux derived by the Takaya and Nakamura (2001), and assume that the group velocity

22

is zero. Using their equation (38), a two-dimensional (horizontal) wave activity flux is

23

expressed as follows:

$$W = \frac{p \cos \phi}{2|U|} (W_\lambda, W_\phi) + C_U M \quad (1)$$

24 with

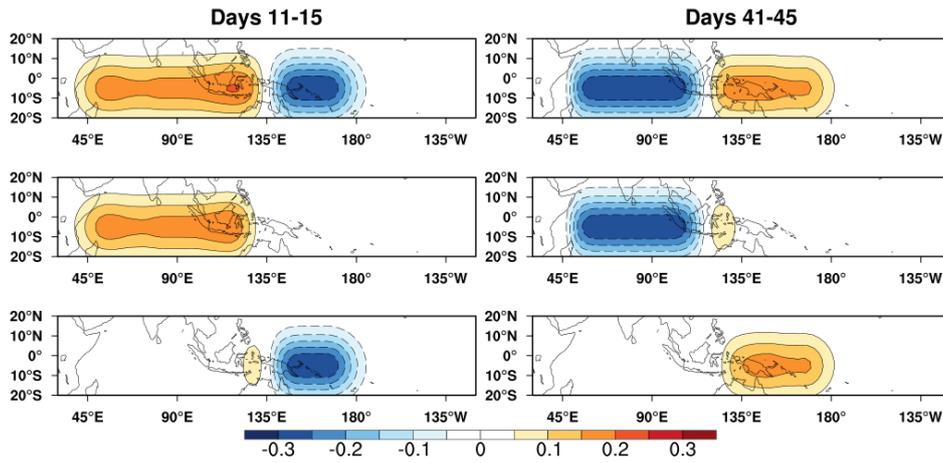
$$25 \quad W_\lambda = \frac{U}{a^2 \cos^2 \phi} \left[\left(\frac{\partial \psi'}{\partial \lambda} \right)^2 - \psi' \frac{\partial^2 \psi'}{\partial \lambda^2} \right] + \frac{V}{a^2 \cos \phi} \left[\frac{\partial \psi'}{\partial \lambda} \frac{\partial \psi'}{\partial \phi} - \psi' \frac{\partial^2 \psi'}{\partial \lambda \partial \phi} \right] \quad (2)$$

$$26 \quad W_\phi = \frac{U}{a^2 \cos \phi} \left[\frac{\partial \psi'}{\partial \lambda} \frac{\partial \psi'}{\partial \phi} - \psi' \frac{\partial^2 \psi'}{\partial \lambda \partial \phi} \right] + \frac{V}{a^2} \left[\left(\frac{\partial \psi'}{\partial \lambda} \right)^2 - \psi' \frac{\partial^2 \psi'}{\partial \phi^2} \right] \quad (3)$$

27 where ψ' is the perturbation streamfunction, (U, V) are the basic state zonal and
 28 meridional winds, (ϕ, λ) are latitude and longitude, a is the earth's radius, and p is
 29 pressure.

30

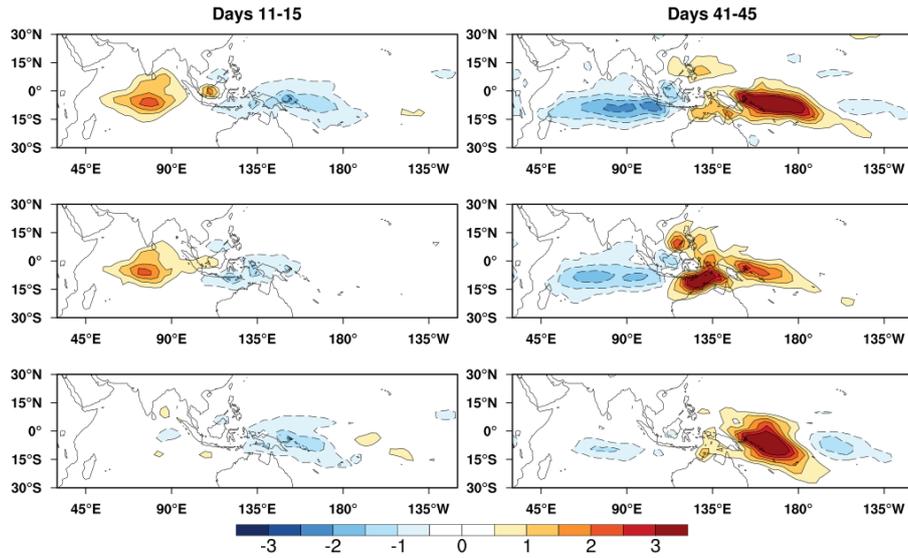
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32

33 **Figure S1.** The vertically averaged (over 1000–50 hPa) added heating anomalies (unit: K day^{-1})
 34 in the MJO_IP (top), MJO_IO (middle), and MJO_WP runs (bottom).

35



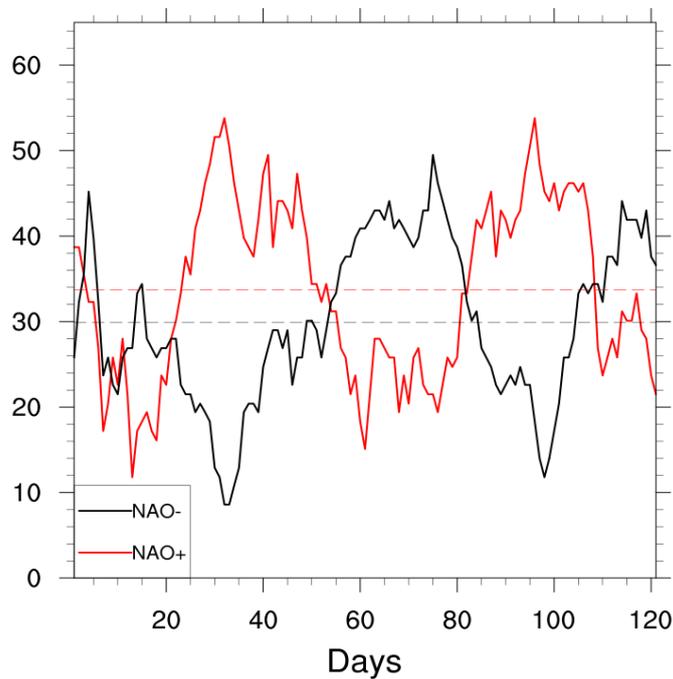
36

37 **Figure S2.** The vertically averaged (over 1000–50 hPa) diabatic heating anomalies (unit: K day^{-1})

38 in the MJO_IP (top), MJO_IO (middle), and MJO_WP runs (bottom).

39

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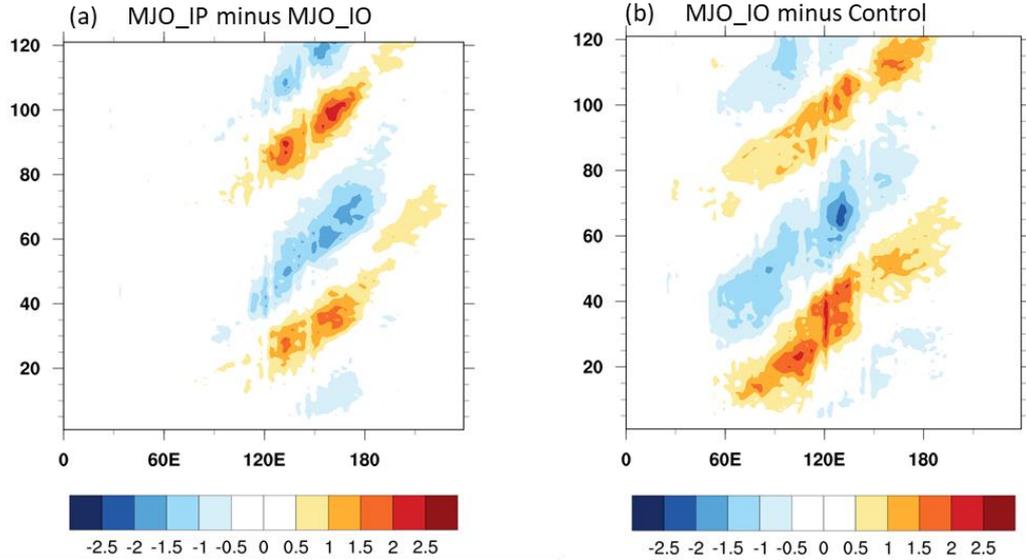
41

42 **Figure S3.** Occurrence probabilities (%) of the positive (red curve) and negative (black curve)

43 NAO from day 1 to day 121 in the MJO_IP runs. The red (black) reference line represents the

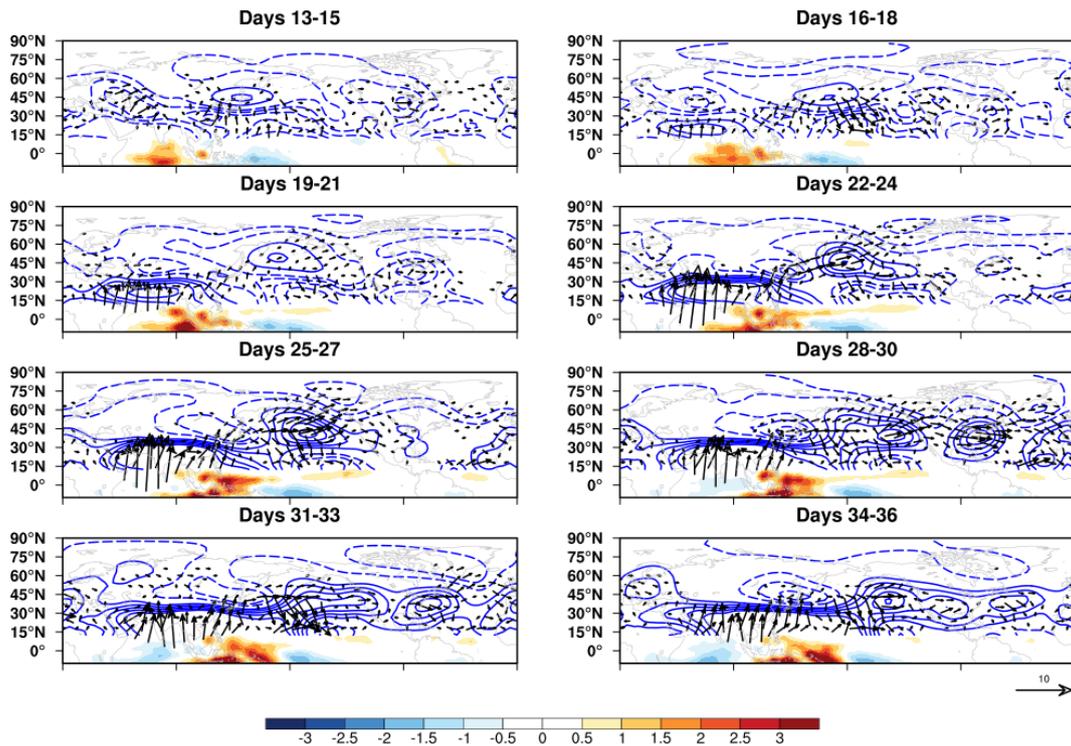
44 climatological mean of the positive (negative) NAO with value 33.7 (29.9).

45



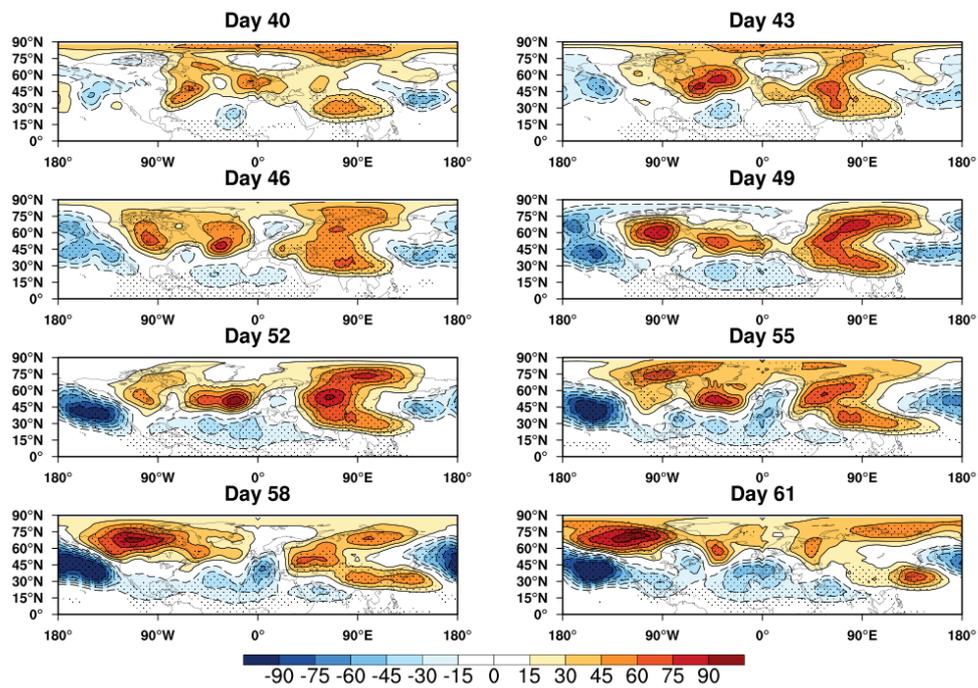
46

47 **Figure S4.** The differences of the vertically averaged (over 1000–50 hPa) diabatic heating (unit: K
 48 day⁻¹) averaged over latitudes 15°S–15°N between the MJO_IP and MJO_IO runs (a), and
 49 between the MJO_IO and Control runs (b).



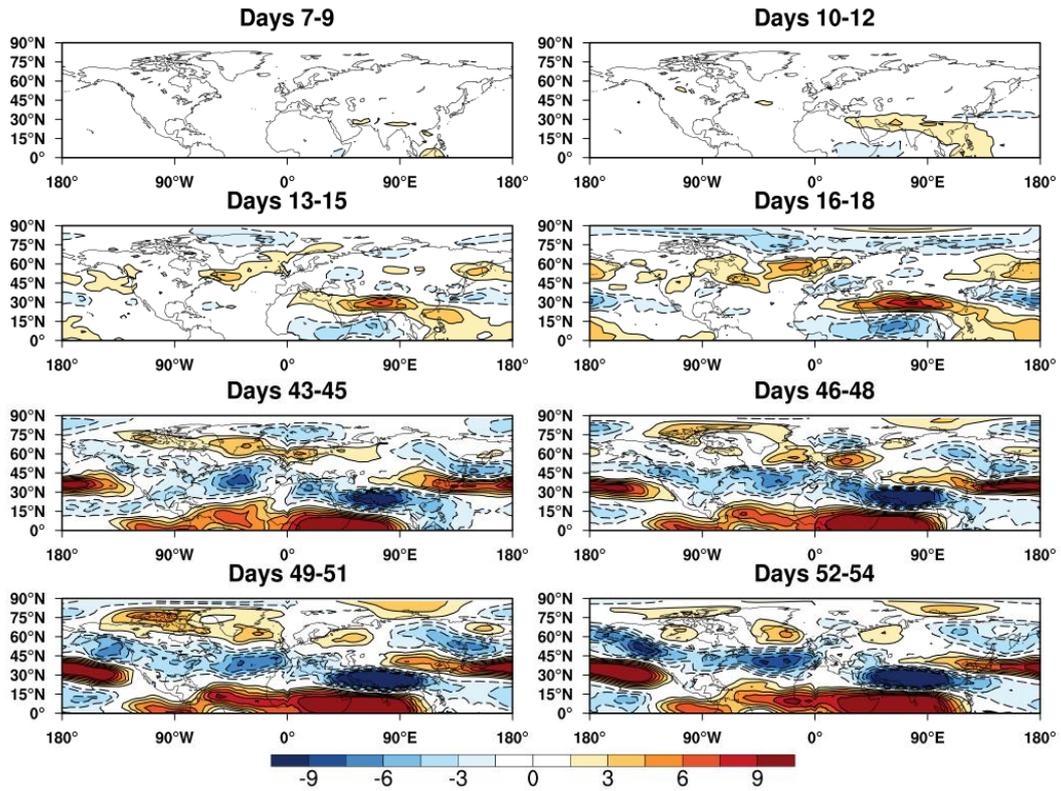
50

51 **Figure S5.** Composites of the 200-hPa streamfunction (contours), horizontal components of
 52 phase-independent wave activity flux (arrows) and diabatic heating anomalies (shaded) in the raw
 53 MJO_IP runs. Contour interval is $1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ for streamfunction, plotted north of 15°N. Units
 54 of wave activity flux are $\text{m}^2 \text{ s}^{-2}$, and only vectors larger than 0.5 are shown. Units of heating
 55 anomalies are K day^{-1} .

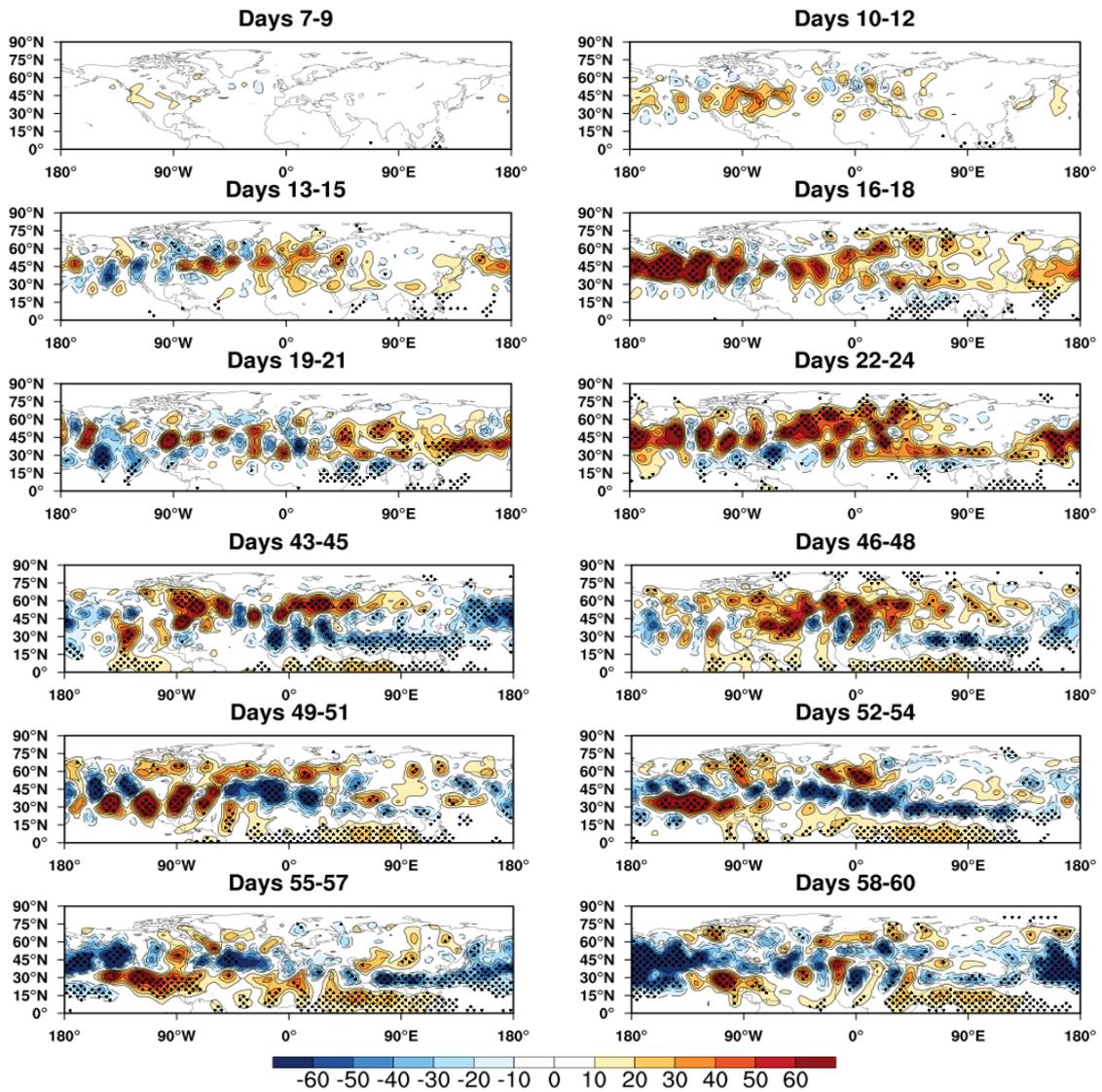


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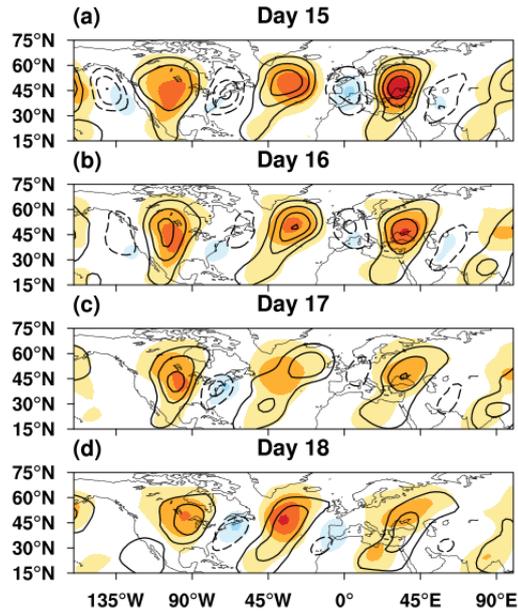
58 **Figure S6.** Composite differences of the 500-hPa geopotential height (unit: gpm) between the
 59 MJO_IO and Control runs from day 40 to day 61. The composite results at the 95% confidence
 60 level according to a Student's t test are dotted.



61 **Figure S7.** Composite differences of the 300-hPa zonal wind (unit: m s^{-1}) between the MJO_IO
 62 and Control runs averaged every 3 days.



63 **Figure S8.** Composite differences of the 300-hPa synoptic $v'v'$ (unit: $m^2 s^{-2}$) between the MJO_IO
 64 and Control runs averaged every 3 days. The composite results at the 90% confidence level
 65 according to a Student's t test are dotted.
 66



67

68 **Figure S9.** One-point lagged regression coefficients of the 300-hPa anomalous synoptic-scale
 69 streamfunction for the base point at 45°N, 30°E on day 15 in Control runs (shading) and MJO_IO
 70 runs (contours) respectively, from day 15 to day 18. The interval of the contours is 0.2.

71

72 **Table S1.** Description of Model Experiments

Experiments	Added heating region	Ensemble size	Duration	Simulations
Control	none	3	December to March in 1980–2010	93
MJO_IP	45°–180°E, 20°S–10°N	3	December to March in 1980–2010	93
MJO_IO	45°–130°E, 20°S–10°N	3	December to March in 1980–2010	93
MJO_WP	115°–180°E, 20°S–10°N	3	December to March in 1980–2010	93

73