

Deep learning classification of potentially severe convective storms in a changing climate

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Abstract

This is a test-case study assessing the ability of deep learning methods to generalize to a future climate (end of 21st century) when trained to classify thunderstorms in model output representative of the present-day climate. A convolutional neural network (CNN) was trained to classify strongly-rotating thunderstorms from a current climate created using the Weather Research and Forecasting (WRF) model at high-resolution, then evaluated against thunderstorms from a future climate, and found to perform with skill and comparatively in both climates. Despite training with labels derived from a threshold value of a severe thunderstorm diagnostic (updraft helicity), which was not used as an input attribute, the CNN learned physical characteristics of organized convection and environments that are not captured by the diagnostic heuristic. Physical features were not prescribed but rather learned from the data, such as the importance of dry air at mid-levels for intense thunderstorm development when low-level moisture is present (i.e., convective available potential energy). Explanation techniques also revealed that thunderstorms classified as strongly rotating are associated with learned rotation signatures. Results show that the creation of synthetic data with ground truth is a viable alternative to human-labeled data and that a CNN is able to generalize a target using learned features that would be difficult to encode due to spatial complexity. Most importantly, results from this study show that deep learning is capable of generalizing to future climate extremes and can exhibit out-of-sample robustness with hyperparameter tuning in certain applications.

1 **A benchmark to test generalization capabilities of deep**
2 **learning methods to classify severe convective storms in**
3 **a changing climate**

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6 **Key Points:**

- 7 • A convolutional neural network can robustly classify convection in current and fu-
8 ture climates.
9 • Skillful classifications are based on learned thermodynamic and kinematic char-
10 acteristics of thunderstorms.
11 • Creating synthetic data with ground truth is demonstrated to be a good alterna-
12 tive to creation of human labeled data.

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Abstract

This is a test-case study assessing the ability of deep learning methods to generalize to a future climate (end of 21st century) when trained to classify thunderstorms in model output representative of the present-day climate. A convolutional neural network (CNN) was trained to classify strongly-rotating thunderstorms from a current climate created using the Weather Research and Forecasting (WRF) model at high-resolution, then evaluated against thunderstorms from a future climate, and found to perform with skill and comparatively in both climates. Despite training with labels derived from a threshold value of a severe thunderstorm diagnostic (updraft helicity), which was not used as an input attribute, the CNN learned physical characteristics of organized convection and environments that are not captured by the diagnostic heuristic. Physical features were not prescribed but rather learned from the data, such as the importance of dry air at mid-levels for intense thunderstorm development when low-level moisture is present (i.e., convective available potential energy). Explanation techniques also revealed that thunderstorms classified as strongly rotating are associated with learned rotation signatures. Results show that the creation of synthetic data with ground truth is a viable alternative to human-labeled data and that a CNN is able to generalize a target using learned features that would be difficult to encode due to spatial complexity. Most importantly, results from this study show that deep learning is capable of generalizing to future climate extremes and can exhibit out-of-sample robustness with hyperparameter tuning in certain applications.

Plain Language Summary

As temperatures and water vapor continue increasing due to climate change, models that were trained using past data may no longer perform with skill. Here we explored whether the performance of a machine learning model was sensitive to a changing climate. The purpose of the machine learning model was to classify thunderstorms that were created using a high-resolution numerical model into two groups: potentially severe thunderstorms and potentially non-severe thunderstorms. Potentially severe thunderstorms were of interest because they have a greater likelihood of producing tornadoes and large hail, which cause billions of losses and dozens of fatalities every year. Results show that the machine learning model was able to classify thunderstorms with skill in both the present day and future climates partly due to the architecture of the machine learning model. We also explored the reasons behind the machine learning model's skill and found that it was able to learn thunderstorm characteristics and weather information from data. These results provide us with added confidence that machine learning models can learn physical relationships from weather and climate data and perform with skill in a changing climate in certain applications.

1 Introduction

The recent success of convolutional neural networks (CNNs; Fukushima & Miyake, 1982) in Earth science applications is largely due to their ability to capture nonlinear and translation invariant details among input variables. This class of deep learning models (LeCun et al., 2015) has proven skillful in various atmospheric science tasks, including detection of weather and climate features (Y. Liu et al., 2016; Lagerquist et al., 2019; Biard & Kunkel, 2019; Toms et al., 2019), emulation of complex model processes (Rasp et al., 2018), and prediction of extreme weather and climate phenomena (Gagne II et al., 2019; Zhou et al., 2019; Ham et al., 2019; Jergensen et al., 2020; Sobash et al., 2020; Lagerquist et al., 2020). This study focuses on convection over the central and eastern contiguous United States (CONUS), which at extremes can produce severe hazards (e.g., hail and tornadoes) that pose societal danger. CNNs have already shown skill in classification and prediction of convective storms in the present climate (Gagne II et al., 2019),

63 modeled using the Weather Research and Forecasting model (WRF; Skamarock & Klemp,
64 2008) at high-resolution (4 km). However, as the climate continues to warm, some fu-
65 ture thunderstorms may be outliers in the baseline climate used for training (Trapp &
66 Hoogewind, 2016), and these extreme events may be more difficult for CNNs to iden-
67 tify. This article explores the ability of CNNs to classify convection of a future climate
68 modeled with WRF, along with the physical reasons for the resultant performance.

69 Climate change is altering the large-scale atmospheric landscape over North Amer-
70 ica, resulting in changes to the frequency and intensity of organized convection (K. L. Ras-
71 mussen et al., 2017; Prein et al., 2017). Future changes to thermodynamic and kinematic
72 fields can impact climatological distributions of convection morphology and associated
73 severe hazards (e.g., tornadoes and large hail; Trapp et al., 2007, 2009; Diffenbaugh et
74 al., 2013). Studies have shown a climate change imprint on various aspects of severe thun-
75 derstorms and associated environments (Allen, 2018), including increases in thermody-
76 namic buoyancy and thunderstorm frequency (Brooks, 2013; Hoogewind et al., 2017),
77 increases in convective inhibition (Taszarek et al., 2020), more societal exposure (Ashley
78 & Strader, 2016), and an eastward geographic shift of environments over the U.S. favor-
79 able for severe hazards (Gensini & Brooks, 2018). However, discerning the interplay be-
80 tween thermodynamic and kinematic components on future convection has been more
81 challenging (Brooks, 2013), given that subtle changes to either field can alter the poten-
82 tial of a thunderstorm to produce severe hazards (Doswell et al., 1996). This complex
83 interplay, and varying seasonal and geographical trends, limit the broader conclusions
84 that can be derived from climate studies of severe convective storms.

85 In current forecasting applications, advancements in delineating thunderstorms ca-
86 pable of producing specific hazards have included the development of environmental prox-
87 ies and composite indices that take kinematic and thermodynamic factors into account
88 (E. N. Rasmussen, 2003; R. L. Thompson et al., 2003, 2007, 2012; Gropp & Davenport,
89 2018). Updraft helicity (UH) is an example of a diagnostic parameter, which estimates
90 the magnitude of rotation within a thunderstorm’s updraft using vertical wind speeds
91 and vorticity (Kain et al., 2008). Strongly-rotating thunderstorms with high magnitudes
92 of UH (e.g., $\geq 75 \text{ m}^2 \text{ s}^{-2}$) have a greater likelihood to be of supercell morphology (Clark
93 et al., 2013; Sobash et al., 2016), a type of thunderstorm that observations have shown
94 to be more likely to produce severe hazards (Bunkers et al., 2006; Duda & Gallus Jr, 2010).
95 Scalar thresholds for UH have been used to classify model simulated convection, with
96 thunderstorms that exceed the predetermined threshold classified as severe (Sobash et
97 al., 2011; Molina, Allen, & Prein, 2020). These dichotomous assignments derived from
98 UH have been used in kilometer-scale climate simulations to estimate changes to severe
99 hazards in a future climate (Trapp et al., 2011; Gensini & Mote, 2015). However, the
100 use of a heuristic to delineate non-severe and severe convection can result in incorrect
101 categorizations of thunderstorms that fall near the predetermined threshold. UH values
102 representative of severe convection also vary seasonally and regionally, based on the cli-
103 matological environments that drive severe convection activity (Sobash & Kain, 2017;
104 Molina, Allen, & Prein, 2020). Recently, Sobash et al. (2020) trained a CNN to forecast
105 severe hazard potential using severe thunderstorm parameters derived from WRF, show-
106 ing that a CNN can learn from diagnostics. The focus herein lies on evaluating a CNN’s
107 ability to classify convection and its out-of-sample robustness to a future climate.

108 CNNs are a class of deep learning models canonically used for computer vision tasks
109 because of the capability of processing multiple layers of information to detect nonlin-
110 earities and translation invariant details of features (LeCun et al., 1998; Krizhevsky et
111 al., 2012). Various techniques have been developed to prevent deep learning models from
112 overfitting and to improve training stability, such as dropout and batch normalization
113 (Srivastava et al., 2014; Ioffe & Szegedy, 2015), which help CNNs generalize relationships
114 among input features and increase prediction accuracy. However, explaining the reasons
115 for model skill has been challenging, due to the complex architecture of CNNs that in-

116 clude many trained weights and biases within hidden layers and feature maps. Various
 117 CNN techniques have been recently developed to create and improve explanations of ma-
 118 chine learning predictions and classifications (Barnes et al., 2019; McGovern et al., 2019).
 119 These explanation techniques include saliency maps (Simonyan et al., 2013) and permu-
 120 tation feature importance (Breiman, 2001; Lakshmanan et al., 2015), which have been
 121 shown to help explain skillful CNN predictions of convective hazards (Gagne II et al.,
 122 2019). Identifying reliable reasons for model performance can increase the trust of at-
 123 mospheric scientists in machine learning and foster further discovery of the physical pro-
 124 cesses driving societally impactful weather and climate extremes.

125 Using deep learning and explanation techniques, the following questions will be an-
 126 alyzed in this paper:

- 127 1. Are future strongly-rotating thunderstorms classified skillfully by a CNN that was
- 128 trained under current climate conditions?
- 129 2. Which input features and spatial patterns are identified to be most important by
- 130 the deep CNN for classification?
- 131 3. What are the reasons (explanations) for incorrect classifications?

132 2 Data and Methods

133 2.1 Thunderstorm Identification in Climate Simulations

134 A set of two convection-permitting model simulations created by the Water Sys-
 135 tem Program of the National Center for Atmospheric Research were used to extract thun-
 136 derstorm objects for this study (C. Liu et al., 2017). The two simulations were created
 137 using WRF at 4 km grid spacing over the CONUS. The WRF simulations cover 13 years
 138 each and represent a retrospective climate period (October 2000–September 2013) and
 139 a future climate period (end of the 21st century). Initial and boundary conditions for
 140 both simulations were driven by the 6-hourly and 0.7° ERA-Interim (Dee et al., 2011),
 141 which is a global climate reanalysis data set produced by the European Centre for Medium-
 142 Range Weather Forecasts. A pseudo-global warming (PGW) perturbation signal (Schär
 143 et al., 1996), representative of an end of the 21st century business as usual climate sce-
 144 nario, was added to state variables of the future climate simulation. The PGW signal
 145 was derived from a set of 19 Coupled Model Intercomparison Project Phase 5 (CMIP5)
 146 models (Taylor et al., 2012) generated with a Representative Concentration Pathway of
 147 8.5 W m⁻² (RCP8.5) radiative forcing, which is a very high greenhouse gas concentra-
 148 tion pathway (Moss et al., 2010). To prevent drifting of the 4 km regional simulation from
 149 the reanalysis boundary conditions, large-scale spectral nudging of moderate strength
 150 was applied above the planetary boundary layer (von Storch et al., 2000), which provided
 151 synoptic-scale fidelity to past weather events yet allowed the mesoscale to evolve with
 152 some freedom. These model simulations allow us to isolate thermodynamic signals from
 153 kinematic influences on the future climate. Simulation details are available in Table 1
 154 and additional specifications can be found in C. Liu et al. (2017).

155 The watershed transform (Lakshmanan et al., 2009) was used to identify high-intensity
 156 updrafts that constitute thunderstorms from the convection-permitting climate simula-
 157 tions. The watershed transform, as employed herein, identified thunderstorms using a
 158 simulated radar reflectivity minimum threshold of 40 dBZ, which is a quantity propor-
 159 tional to the number of drops per unit volume and provides an estimate of convective
 160 precipitation (Trapp et al., 2011). Grid cells adjacent to the detected local maxima that
 161 also exceeded a minimum threshold of 20 dBZ were then treated as a part of the thun-
 162 derstorm object. This process was repeated iteratively and surrounding grid cells were
 163 continually associated with a thunderstorm until values were either below a minimum
 164 threshold of 20 dBZ or exceeded a predetermined thunderstorm object spatial extent of
 165 128 km (32 grid cells x 4 km grid spacing). Each thunderstorm was saved as a object

Table 1. WRF simulation parameterization schemes^a and settings, as detailed in C. Liu et al. (2017).

Model specifications	
Domain grid points	1,360 x 1,016 grid points
Domain size (East-West, North-South)	5,440-km, 4,064-km
Vertical levels	51 stretched vertical levels, topped at 50-hPa
Microphysics scheme	Thompson aerosol-aware (G. Thompson & Eidhammer, 2014)
Planetary boundary layer scheme	Yonsei University (Hong et al., 2006)
Shortwave and longwave radiation scheme	RRTMG (Iacono et al., 2008)
Land surface scheme	Improved Noah-MP land-surface model (Niu et al., 2011)

^aNo sub-grid cloud cover, shallow, or deep cumulus parameterizations were employed.

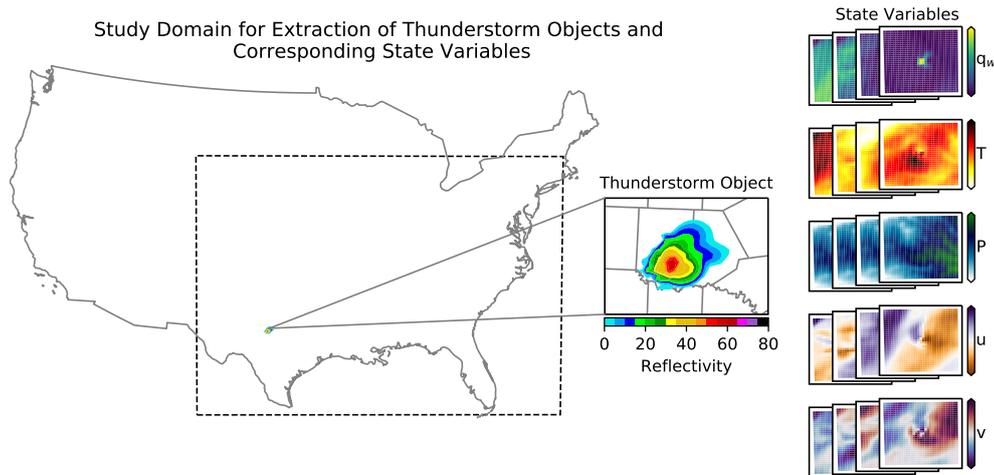


Figure 1. Thunderstorm objects for this study were extracted from areas east of the Rocky Mountains (over land) within the dashed-line polygon. An example thunderstorm object is shown over the CONUS for scale, with the inset displaying a larger version, and corresponding state variables are shown on the right. State variables listed from top-to-bottom are water vapor mixing ratio (q_w ; g kg^{-1}), temperature (T ; K), pressure (P ; hPa), and zonal (u) and meridional (v) winds (m s^{-1}). The four layers for each state variable indicate the four levels (1, 3, 5, and 7 km above ground) at which variables were derived.

166 spanning 128 x 128 km containing the thunderstorm and the adjacent environment, which
 167 influences thunderstorm characteristics (R. L. Thompson et al., 2012). Thunderstorms
 168 were extracted over land and east of the Rocky Mountains (Fig. 1), where severe thun-
 169 derstorms have a greater climatological likelihood of occurrence (Brooks et al., 2003).
 170 The temporal focus of this study was limited to winter (December, January, and Febru-
 171 ary; DJF) and spring months (March, April, May; MAM). Other seasons were omitted
 172 due to a simulated dry bias during summer months across the central CONUS, which
 173 was partly associated with land-surface feedbacks (Barlage et al., 2018).

174 Similar to Gagne II et al. (2019), meteorological state variables were extracted from
 175 the WRF simulations to train a CNN after creating the thunderstorm objects. Five vari-
 176 ables were extracted and interpolated onto four different vertical levels, resulting in a
 177 total of 20 input attributes used for training the CNN (Fig. 2). The five variables are
 178 pressure (P ; hPa), temperature (T ; K), water vapor mixing ratio (q_w ; g kg^{-1}), and zonal

179 (u) and meridional (v) winds (m s^{-1}). Variables were then interpolated onto the follow-
 180 ing heights above ground level (AGL): 1, 3, 5, and 7 km. AGL heights were preferred
 181 over constant pressure surfaces because pressure surfaces might be below ground across
 182 portions of the High Plains and AGL heights are more likely to sample similar parts of
 183 a thunderstorm updraft. UH ($\text{m}^2 \text{s}^{-2}$) was also extracted and is quantified as

$$\text{UH} = \int_{2\text{km}}^{5\text{km}} w \zeta dz,$$

184 where the integral of the product of vertical velocity (w) and vertical vorticity (ζ) is com-
 185 puted from 2 km to 5 km AGL (Kain et al., 2008). UH was used as ground truth to cre-
 186 ate the training labels, but was not used as an input attribute (i.e., variable) for the CNN.
 187 A high-magnitude UH threshold (e.g., $75 \text{ m}^2 \text{ s}^{-2}$) was used to delineate convection more
 188 likely to be of supercell morphology (Sobash et al., 2011). The 1D vector containing labels
 189 for CNN training and testing was created using binary assignment (i.e., integer en-
 190 coding) derived from UH and encoded as 0 or 1. Values exceeding the UH threshold (the
 191 potentially severe category) were assigned a label of 1, whereas values below the thresh-
 192 old were assigned a label of 0. Thunderstorm objects were then split into two subsets
 193 prior to CNN training: 60% for training and 40% for testing. Stratified sampling of thun-
 194 derstorm objects that exceeded or did not exceed the delineated UH threshold was con-
 195 ducted to ensure that training and testing data contained the same percentage of ma-
 196 jority and minority classes. Since the meteorological variables contain different dynamic
 197 ranges, the training data was standardized by subtracting the training set variable’s mean
 198 and then dividing by its standard deviation. The testing data was also standardized for
 199 model evaluation using the mean and standard deviation values extracted from the cur-
 200 rent climate training data.

201 2.2 CNN Architecture and Explanations

202 The deep learning model used in this study was a CNN (LeCun et al., 1990) that
 203 consisted of three convolutional layers (similar to Gagne II et al., 2019). The 20 input
 204 attributes described in the previous sub-section were fed into the first convolutional layer
 205 (Fig. 2). A stride length of 1 was used for the filter windows, which consisted of 5×5
 206 grid cells, with zero padding also applied to the edges of each feature map. The recti-
 207 fied linear unit (ReLU; $\max(0, x)$) activation function was used for each feature map (ex-
 208 cept for the last dense layer), which preserved the magnitude of positive signals and negated
 209 negative signals when propagated forward through the network (LeCun et al., 2015). Max
 210 pooling was performed after each convolutional layer by extracting maximum values of
 211 the feature maps within a sliding 2×2 filter window with stride length of 1. Max pool-
 212 ing added translation invariance and allowed the model to learn higher-level features (i.e.,
 213 increase in kilometers) in deeper layers. After the three convolution and pooling oper-
 214 ations, the resultant data was flattened into a 1D vector, passed through a dense layer
 215 (Fig. 2), and a ReLU activation function was applied to its output. The 1D vector was
 216 then passed through a final dense layer, with a sigmoid activation function applied to
 217 produce the model’s output as a value between 0 and 1, which was interpreted as the
 218 probability that the input attributes contained a strongly rotating thunderstorm.

219 The weights of the CNN were trained to minimize mean squared error (MSE) us-
 220 ing the Adam optimization algorithm (Kingma & Ba, 2014) via backpropagation with
 221 a learning rate of 0.0001. Glorot uniform was used as the layer weight initializer (Glorot
 222 & Bengio, 2010). Sensitivity to random weight initialization was assessed by training sev-
 223 eral models using different random initializations and skill was comparable across mod-
 224 els, potentially due to the large training sample size or the large number of input attributes
 225 used during training. During training, a batch size of 128 was used, randomly pulled from
 226 the training data population and passed forward through the CNN. To prevent overfit-

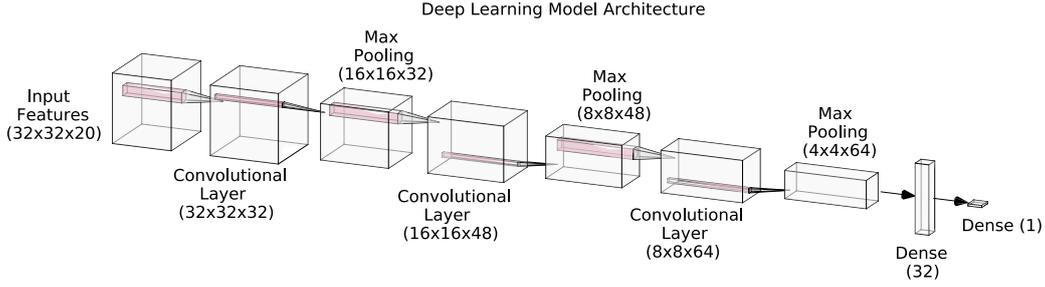


Figure 2. The architecture of the CNN. The model consists of three 2D convolutional layers and max pooling layers. The dimensions of the feature maps are shown in parentheses. 2D filter windows are depicted in pink, of dimension 5 x 5 for each convolutional layer and 2 x 2 for each max pooling layer. The km range of learned features grows in deeper layers of the CNN because of max pooling layers; the spatial extent learned is 20x20 km for the first convolutional layer (filter containing 5 filter pixels x 4 km per pixel), 40x40 km for the second convolutional layer, and 80x80 km for the third convolutional layer.

227 ting of weights during training, Ridge (L2 norm; 0.001) regularization was added as a
 228 penalty term to reduce the magnitude of the weights at each convolutional layer. Batch
 229 normalization was also applied after each convolutional layer and the first dense layer
 230 (i.e., before each pooling layer), which involved standardizing layer outputs by subtract-
 231 ing the batch mean and dividing by the batch standard deviation, in effect reducing co-
 232 variance shift (Ioffe & Szegedy, 2015). 2D spatial dropout (30% in this study; Srivas-
 233 tava et al., 2014) was also employed after batch normalization, which increased the ro-
 234 bustness of learned features. We note that numerous training iterations were run with
 235 the order of batch normalization and spatial dropout reversed, but results were more skill-
 236 ful with batch normalization preceding spatial dropout in this application. A validation
 237 data set was used during training, consisting of 10% of the available training data, which
 238 provided insight into the skill of the model during training. Cross-validation on 5 folds
 239 was also performed to assess result sensitivity to the underlying test data distribution
 240 and differences were minimal. The final model settings were selected based on the low-
 241 est resultant test data MSE from a hyperparameter grid search that resulted in over 128
 242 independently trained CNNs trained using 20 epochs. The classification output of the
 243 lowest MSE was evaluated using probabilistic and nonprobabilistic skill metrics that will
 244 be further detailed within the results. For more details about CNNs, see Goodfellow et
 245 al. (2016).

246 To explore the relative importance of specific meteorological variables on CNN clas-
 247 sification performance, we used the permutation feature importance (PFI; Breiman, 2001)
 248 analysis, specifically the single-pass forward test variant. PFI ranks variables based on
 249 how much randomizing them impacts error during testing, with larger magnitude decreases
 250 in skill associated with greater importance. Higher relative importance suggests that the
 251 respective variables have greater relevance to the classification due to the larger mag-
 252 nitude weights associated with them within the CNN architecture. 500 permutations were
 253 completed for each of the 20 variables to capture uncertainty associated with shuffling
 254 order in PFI. Permuted fields for a set of examples were also visualized to further ex-
 255 plain variable importance results. The chosen examples consist of cases that were origi-
 256 nally classified as one class by the CNN, but switched to another class due to PFI. Cer-
 257 tain classified thunderstorms that were switched to incorrect classifications (according
 258 to the ground truth label) also consistently appeared in larger skill reductions, and these

were used to narrow down the subset of thunderstorms for visualization. To explain model reasoning within a spatial context, image-specific saliency maps (Simonyan et al., 2013) and input*gradient (Shrikumar et al., 2016) were used. Input*gradients is computed as the product of the local gradient and input (Mamalakos et al., 2021), which provides the variable relevance.

3 Results

3.1 Thunderstorm Classification in a Future Climate

Thunderstorms identified within the future climate model simulation contain warmer temperatures and higher moisture content than thunderstorms identified within the current climate model simulation at all vertical levels (1, 3, 5 and 7 km; Table 2), which is consistent with the applied PGW signal (C. Liu et al., 2017). Table 2 shows that future thunderstorms contain about 1.3 g kg^{-1} more low-level (at 1 km) water vapor mixing ratio and are about 2.4 K warmer at low levels (at 1 km) than thunderstorms of the current climate (both statistically significant at the 95th percentile confidence level). These results are also consistent with the Clausius-Clapeyron equation that estimates a 7% increase in saturation vapor pressure per $+1^\circ\text{C}$. Using the Clausius-Clapeyron equation, water vapor mixing ratio of future thunderstorms should be about 8.76 g kg^{-1} at 1 km, which is comparable to the 8.9 g kg^{-1} contained in thunderstorms extracted from the future climate model simulation (Table 2). Extremes within the future climate were also of interest. These extremes were classified as “outlier cases” and were selected as thunderstorms containing 1 km water vapor mixing ratio exceeding the 99th-percentile of thunderstorms from the future climate. The focus of outlier cases lies on 1 km water vapor mixing ratio because increased low-level moisture and thermodynamic buoyancy can result in more intense vertical winds related to stronger thunderstorm updrafts. Added low-level moisture and warmth provide additional thermodynamic buoyancy and vertical instability that could lead to more intense convection in the future (K. L. Rasmussen et al., 2017; Prein et al., 2017). The increased moisture and warmth could also pose the CNN with added difficulty in performing the thunderstorm classification task. Table 2 shows little change in zonal (u) and meridional (v) thunderstorm winds between the current and future climate model simulations. Since the classification task being performed by the CNN is related to winds, the relative consistency in wind magnitude may result in little change in classification skill between the current and future climate model simulations.

Here we evaluate probabilistic forecasts generated by the CNN, which are probabilities that the thunderstorm objects contain a strongly rotating or non-strongly rotating thunderstorm. Strongly rotating thunderstorms are associated with a higher probability magnitude and non-strongly rotating thunderstorms are associated with a lower probability magnitude. The large imbalance between the majority and minority classes was important to consider during evaluation of the CNN classification skill (Table 3). Therefore, the performance diagram and metrics that are more useful for evaluating forecasts of rare events were used (Roebber, 2009). The minority class in this case consists of strongly rotating thunderstorms, which are rare events that comprise approximately 3% of all thunderstorms in the convection-permitting model simulations. Performance diagrams summarize the probability of detection (POD; ratio of hits to the total of hits and false alarms), critical success index (CSI; ratio of hits to the total of hits, false alarms, and misses), and bias (ratio of false alarms to misses). Success ratio (SR) is also summarized, which is $1 - \text{false alarm ratio}$ (FAR; ratio of false alarms to the total of hits and false alarms). The curves shown on the performance diagrams were created by varying the probability threshold between 0 and 1 to convert probabilistic forecasts into binary forecasts and show how skill changes based on the probability threshold used (Fig. 3a,c,e).

Table 2. Median of thunderstorm variables extracted from the current and future climate simulations. Environments surrounding the thunderstorms were omitted for these statistics. Future thunderstorms with higher low-level moisture content than most cases in the future climate (i.e., outlier cases with $\geq 99^{th}$ percentile of 1 km water vapor mixing ratio in the future climate), are also shown. Statistically significant values of the future climate and future outliers are indicated in **boldface** and computed using confidence intervals of 2.5th and 97.5th percentile of a 1,000-member bootstrap from a total sample of 454,242 thunderstorm objects extracted from the current climate simulation.

Current Climate	1-km	3-km	5-km	7-km
Temperature (K)	283.7	272.7	261.0	247.4
v-winds (m s^{-1})	5.3	7.8	9.7	11.2
u-winds (m s^{-1})	3.1	9.9	14.1	17.2
Water vapor mixing ratio (g kg^{-1})	7.6	4.8	2.1	0.7
Pressure (hPa)	868.7	679.9	526.4	402.3
Future Climate	1-km	3-km	5-km	7-km
Temperature (K)	286.2	275.6	264.6	251.9
v-winds (m s^{-1})	5.1	7.4	9.5	11.3
u-winds (m s^{-1})	2.8	10.0	14.4	17.8
Water vapor mixing ratio (g kg^{-1})	8.9	5.7	2.8	1.0
Pressure (hPa)	869.0	681.7	529.5	406.3
Future Outliers	1-km	3-km	5-km	7-km
Temperature (K)	295.7	284.7	272.5	260.5
v-winds (m s^{-1})	4.8	4.0	3.8	4.2
u-winds (m s^{-1})	2.6	7.0	9.8	12.0
Water vapor mixing ratio (g kg^{-1})	17.2	8.0	3.5	1.4
Pressure (hPa)	889.2	704.1	551.5	427.0

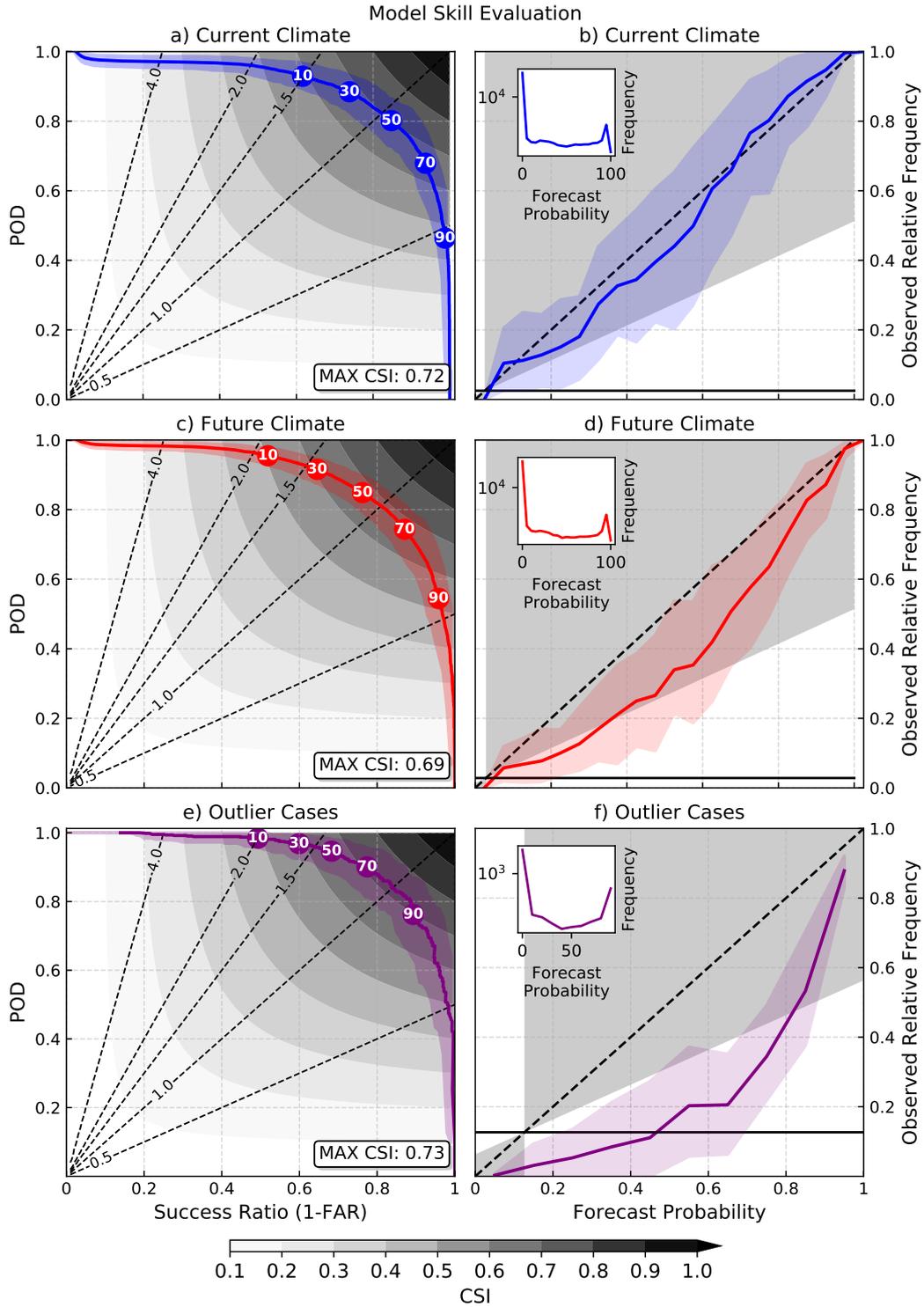


Figure 3. Performance diagrams (a,c,e) show curves that represent CNN skill as a function of the probability of detection (POD) and success ratio (1-FAR [false alarm ratio]) across various probability thresholds. The grayscale filled contours show the critical success index (CSI), the dashed lines display the bias, and circles along the curves display probability thresholds (a,c,e). Attributes diagrams are also displayed, which show forecast probabilities against observed relative frequency, using a forecast probability bin size of 0.05 (b,d) and 0.1 (f). Inset panels in the top left show the frequency of forecast probabilities and the grey-shading shows regions where resolution exceeds reliability (b,d,f). 95th percentile confidence intervals (two-tailed) computed from a 1,000-member bootstrap shown with shading (a-f).

Table 3. Table contains various skill metrics used for evaluation of CNN performance during the current and future climate. Also shown are the total number of true positive (i.e., hits), false positive (i.e., false alarms), false negative (i.e., misses), and true negative predictions made by the CNN. Future thunderstorms that have higher low-level moisture content than most cases in the future climate (i.e., outlier cases with $\geq 99^{th}$ percentile of 1 km water vapor mixing ratio in the future climate), are also shown. Metrics were computed using a 0.5 forecast probability threshold for the current, future, and outlier thunderstorms.

Climate	Current	Future	Outlier
True positives	9,089	10,984	601
False positives	1,633	3,420	280
False negatives	2,250	1,954	34
True negatives	441,270	440,109	3,652
AUC	0.90	0.92	0.94
CSI	0.70	0.67	0.66
Hit Rate	0.80	0.85	0.95
Bias	0.95	1.11	1.39
BSS	0.74	0.70	0.59
Resolution	0.02	0.02	0.08
Uncertainty	0.02	0.03	0.11

309 The performance diagrams (Fig. 3a,c,e) show that despite being trained with thun-
310 derstorm objects extracted from the current climate model simulation, CNN skill remains
311 consistent and high (0.69 max CSI) when classifying thunderstorms of the future climate
312 model simulation (Fig. 3c). These results suggest that a CNN is capable of learning spa-
313 tial representations and variable relationships that are transferable to a warmer and more
314 moist climate. Figure 4a shows that correctly classified strongly-rotating thunderstorms
315 (according to the ground truth label) of the future climate contained approximately 4
316 g kg^{-1} more low-level moisture (at 1 km) than correctly classified strongly-rotating thun-
317 derstorms of the current climate. The consistency in CNN skill could be partly related
318 to bulk wind shear (1-5 km) distributions that remained relatively stationary between
319 both climate model simulations (Fig. 4a). Despite the imbalance between the majority
320 and minority classes, the CNN was able to perform the classification task skillfully, sug-
321 gesting that techniques to augment minority classes may not always be necessary (e.g.,
322 Chawla et al., 2002). However, model bias exhibits some sensitivity to the forecast thresh-
323 old used. We note that the same forecast threshold values were evaluated for current,
324 future, and outlier thunderstorms (10,000 values evenly spaced between 0 and 1) in Fig-
325 ure 3 and only a threshold of 0.5 was used for all thunderstorm classes in Table 3. Max
326 CSI and lower bias were achieved when evaluating model skill using a probability thresh-
327 old of approximately 0.6 in the future climate and 0.5 in the current climate (Fig. 3c).
328 A probability threshold of 0.5 results in a small over forecasting bias (>1) of strongly
329 rotating thunderstorms of the future (Table 3), which shows that the CNN generally has
330 lower confidence in classifying strongly rotating thunderstorms of the warmer and more
331 moist climate.

332 Performance metrics were also computed for the outlier future thunderstorms, which
333 were characterized by higher low-level moisture content than the 99th-percentile of the
334 future climate, in order to further quantify the out-of-sample robustness of the CNN (Ta-
335 ble 2). Results show that CNN classification skill with outlier thunderstorms of the fu-
336 ture climate remains high, with a max CSI of 0.73 (Fig. 3e) which is comparable to the

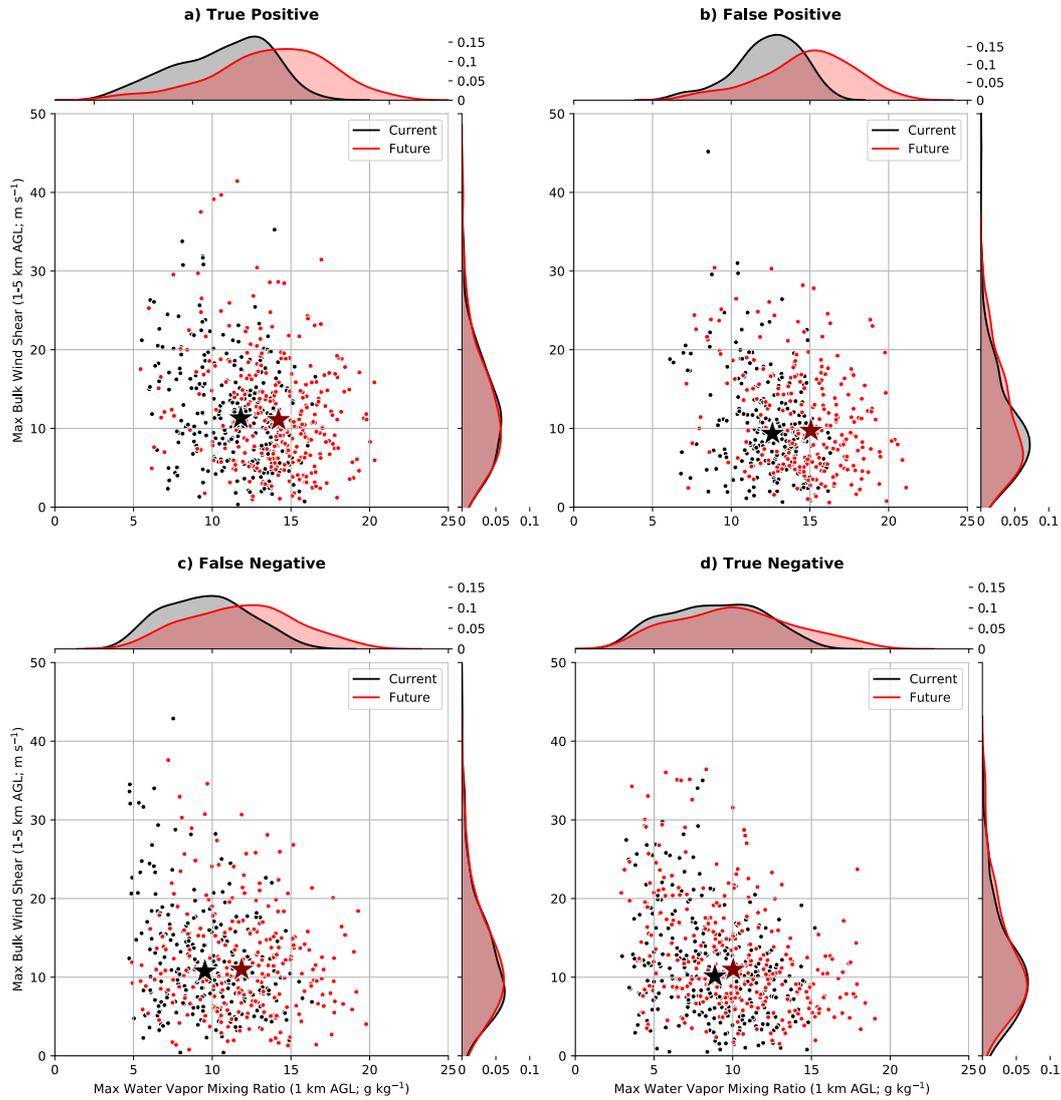


Figure 4. Scatter plots showing water vapor mixing ratio (1 km AGL) against bulk wind shear (1-5 km AGL) for thunderstorm objects of the current and future climate evaluated as (a) hits, (b) false alarms, (c) misses, and (d) correct negatives. The dots represent individual thunderstorm objects of the current (black) and future (red) climates, while the stars show the mean of the respective climate thunderstorm objects. Bivariate density distributions are also shown with marginal plots created using Gaussian kernels. Random subsets of thunderstorm objects are shown for easier visualization.

Table 4. Same as Table 3, but using a model trained with class imbalance addressed (equal sample sizes of potentially severe and non-severe thunderstorms). All other CNN hyperparameters were kept consistent.

Climate	Current	Future	Outlier
True positives	10,987	12,422	593
False positives	14,275	13,659	483
False negatives	434	713	26
True negatives	429,055	429,910	3,468
AUC	0.96	0.96	0.92
CSI	0.43	0.46	0.54
Hit Rate	0.96	0.95	0.96
Bias	2.21	1.99	1.74
BSS	0.11	0.25	0.39
Resolution	0.02	0.02	0.07
Uncertainty	0.02	0.03	0.12

337 current and future climate subsets (Fig. 3a,c). These results further substantiate that
 338 a CNN can exhibit out-of-sample robustness in climate applications. Results also sug-
 339 gest that deep learning can sufficiently generalize relationships among input variables
 340 and remain skillful with extreme events. However, over forecasting of strongly rotating
 341 outlier thunderstorms was identified (bias >1) with a probability threshold of 0.5 (Fig.
 342 3e; Table 3), which implies overconfidence in classifying thunderstorms with extreme low-
 343 level moisture. Like thunderstorms of the future climate, the consistency in CNN skill
 344 could be partly related to bulk wind shear (1-5 km) distributions that remained relatively
 345 stationary between current climate and future outlier thunderstorms (Fig. 5a). However,
 346 in addition to high-end low level moisture content, future outlier thunderstorms also con-
 347 tained substantially higher moisture content in mid-to-upper levels, as shown in figure
 348 5 for 5 km maximum water vapor mixing ratio. This result suggests that the spatial ar-
 349 rangement of meteorological fields likely also plays an important role in CNN prediction
 350 skill in addition to variable relative magnitudes. We note that a model consisting of the
 351 same architecture was trained with class imbalance addressed (i.e., equal sized poten-
 352 tially severe and non-severe classes) and resulted in more substantial bias (Table 4) than
 353 the model trained with large class imbalance (Table 3).

354 The Brier skill score (BSS) was used as an additional evaluation metric and can
 355 be visualized with the attributes diagram (Fig. 3b,d,f), which shows forecast probabil-
 356 ities against observed relative frequencies (Hsu & Murphy, 1986; Wilks, 2011). An at-
 357 tributes diagram provides a measure of forecast reliability, where the dashed 45-degree
 358 line represents perfect reliability. Attributes diagrams show forecast probabilities (be-
 359 tween 0 and 1), which are plotted against the observed relative frequency for that fore-
 360 cast probability (Wandishin et al., 2005). An example of “perfect reliability” for a 0.6
 361 forecast probability (e.g., x-axis in Fig. 3b,d,f) is when that forecast probability corre-
 362 sponds to a similar observed relative frequency (e.g., y-axis in Fig. 3b,d,f). The solid hor-
 363 izontal line in figure 3b,d,f shows the climatological probability of strongly rotating thun-
 364 derstorms occurring within the respective climate sample, which is higher in outlier cases
 365 than in the current and future climates. Since attributes diagrams consider climatolog-
 366 ical and forecast probability frequency, they also show how different forecasts are from
 367 climatology (i.e., resolution). The gray shading in figure 3b,d,f show areas contributing
 368 to positive BSS, which are areas where BSS resolution exceeds reliability (Gagne II et
 369 al., 2019). Inset plots (Fig. 3b,d,f) show the frequency of forecast probabilities for each

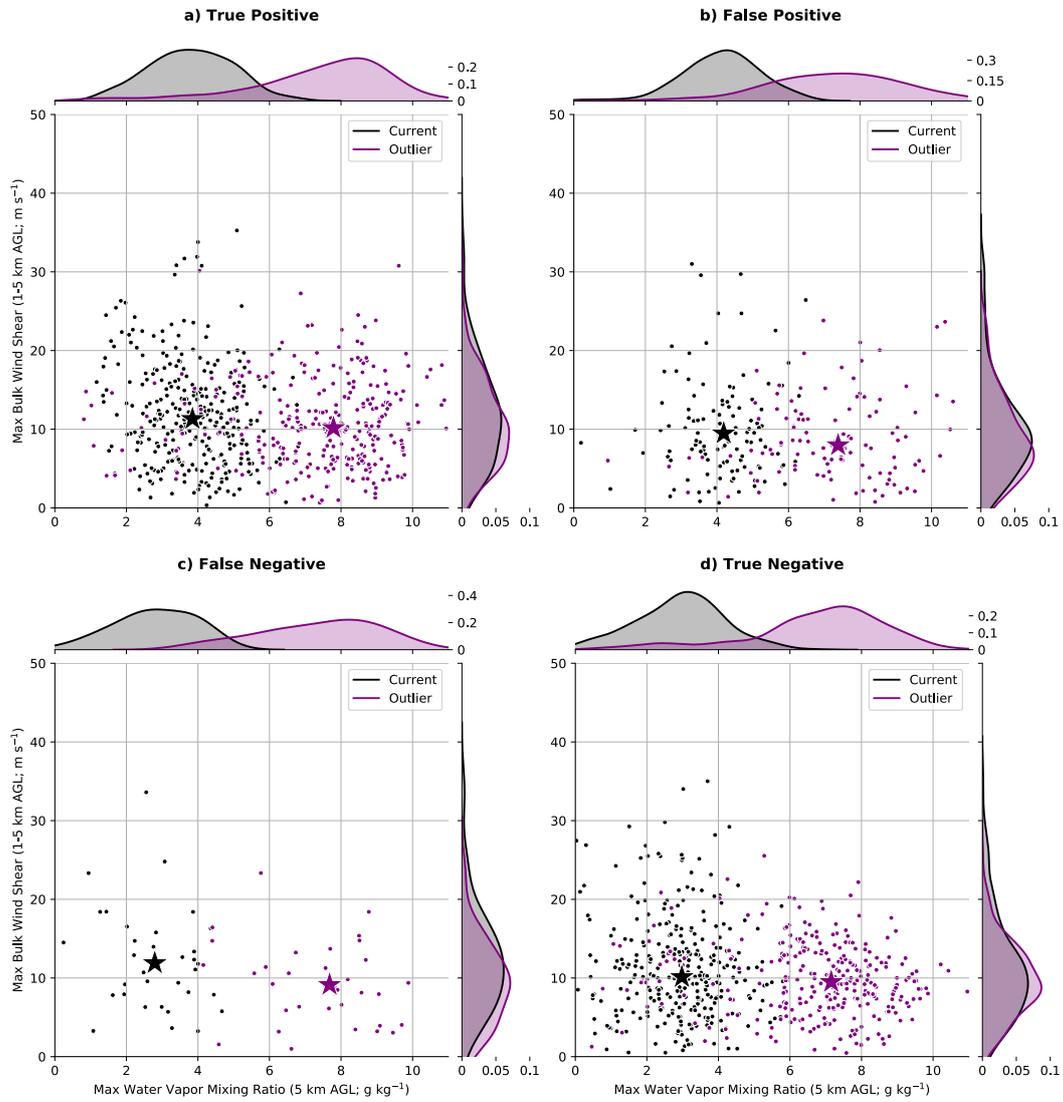


Figure 5. Same as 4, but for outlier thunderstorms and water vapor mixing ratio at 5 km AGL.

370 climate subset, which in this case features a bi-modal distribution, with peaks at low (≤ 0.05)
 371 and high (≥ 0.95) forecast probabilities. This bimodal distribution is most pronounced
 372 for outlier cases (Fig. 3f). The attributes diagram curve closely parallels the dashed 45-
 373 degree diagonal line across all forecast probabilities for the current climate (Fig. 3b), which
 374 conveys high forecast reliability. However, future and outlier cases have lower reliabil-
 375 ity between the 0.2-0.7 forecast probabilities and higher reliability at low (< 0.2) and high
 376 (> 0.7) forecast probabilities (Fig. 3d,f). These results corroborate the performance di-
 377 agram results, which show that the CNN has an over-forecasting bias for future and out-
 378 lier thunderstorms.

379 3.2 CNN Interpretation

380 Permutation feature importance (PFI) was conducted to determine the relative im-
 381 portance of input variables on CNN prediction skill. The area under the receiver oper-
 382 ating characteristic curve (AUC; Mason, 1982) was used, which is a scalar that repre-
 383 sents model performance encompassing the probability of detection and false detection.
 384 Using AUC, PFI reveals that zonal (u) and meridional (v) winds at 3 km have the high-
 385 est relative importance for CNN prediction (Fig. 6a,d). PFI is consistent for predictions
 386 generated using the current climate and future climate thunderstorms (Fig. 6a,d), which
 387 shows that mid-level kinematic fields play an important role in the proper classification
 388 of rotating convective storms. This result is physically reasonable given that UH (com-
 389 puted from 2 km to 5 km AGL) was used to create the thunderstorm labels that were
 390 subsequently used to train the CNN. The climatological homogeneity between current
 391 and future climate mid-level winds (Table 2) also likely contributed to the consistency
 392 in variable importance across climate subsets. Zonal and meridional winds at 1 km and
 393 5 km were also identified as relatively important (Fig. 6a,d). Several thermodynamic vari-
 394 ables also ranked in the top 50th percentile in importance, suggesting that the CNN also
 395 relies on characteristics of physical variables that were not included in the UH compu-
 396 tation. These relatively higher ranking thermodynamic variables include, temperature
 397 at 5 km and water vapor mixing ratio at 1 km and 7 km (Fig. 6a,d).

398 Additional skill metrics were used for PFI in order to explore the sensitivity of the
 399 analysis to the respective evaluation method. PFI using CSI, which is a skill evaluation
 400 metric that neglects true negative events (as described earlier), further emphasizes the
 401 relative importance of mid-level kinematic fields (Fig. 6b,e). BSS was also used for PFI
 402 (Fig. 6c,f) and results generally align with AUC and CSI results in regards to the rel-
 403 ative importance of mid-level kinematic fields. Interestingly however, moisture at 5 km
 404 ranked most important when evaluating the CNN classification skill for current and fu-
 405 ture climate (Fig. 6c) thunderstorms. This result suggests that mid-level moisture is an
 406 important variable for classification of strongly-rotating thunderstorms, given the lower
 407 ranking found using AUC, which also takes into account correct classification of non-strongly
 408 rotating thunderstorms (according to the ground truth label).

409 PFI offers insight into the relative importance of variables based on modulations
 410 to the CNN prediction skill, but the method does not provide reasons for the rankings.
 411 For instance, it is not immediately clear why water vapor mixing ratio at 5 km has greater
 412 relative importance than at 1 km. To explore the reasons for PFI rankings, visualiza-
 413 tions were created of thunderstorms that were initially classified as strongly rotating but
 414 switched to a non-strongly rotating classification as a result of the permuted variable (Fig.
 415 7). Figure 7c shows an example strongly rotating thunderstorm. Its associated water va-
 416 por mixing ratio at 5 km (Fig. 7a) was permuted to a field that had a greater overall
 417 magnitude of moisture (Fig. 7b) and peak moisture values that were offset from the thun-
 418 derstorm locations (Fig. 7c), which resulted in the non-strongly rotating classification.
 419 Various other thunderstorms also had a similar pattern; higher overall moisture content
 420 and shifted peak value locations in the permuted field resulted in non-strongly rotating
 421 classifications (not shown). Supercells generally form in environments characterized by

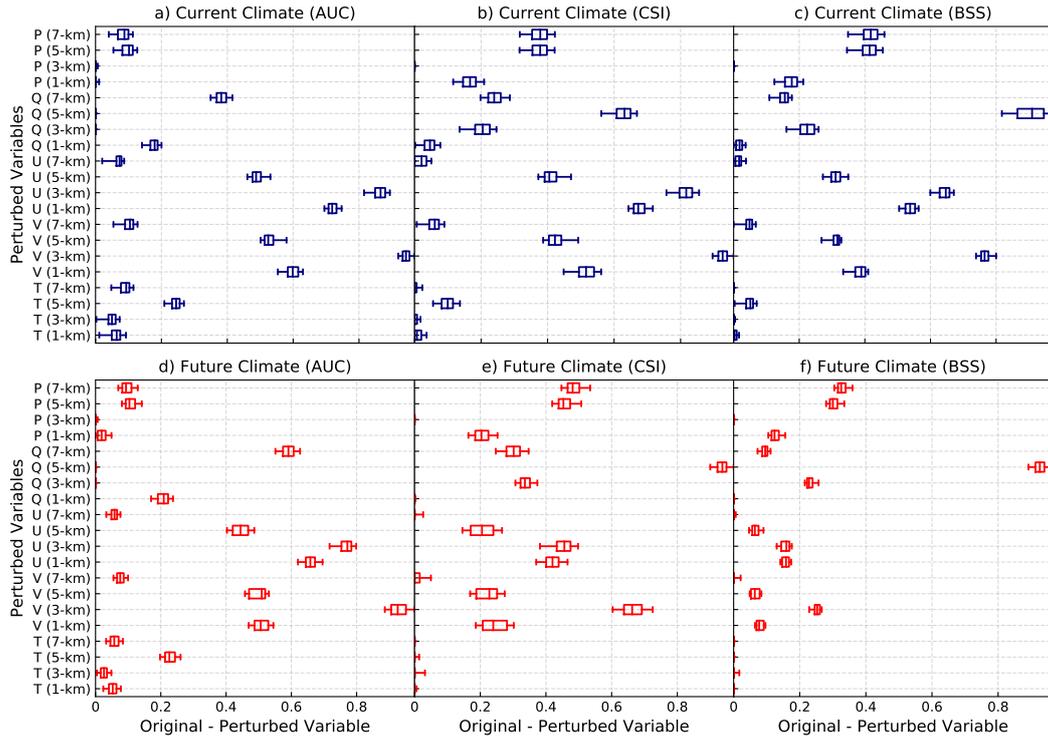


Figure 6. Permutation feature importance (PFI) analysis for the current climate (a-c) and future climate (d-f) thunderstorms shown using box and whisker plots. The median of 500 permutations is represented by the vertical line within the box and the whiskers represent all 500 measured changes in skill. PFI was conducted using various skill metrics, including area under the receiver operating characteristic curve (AUC; a,d), critical success index (CSI; b,e), and Brier skill score (BSS; c,f). Changes in skill were normalized by the maximum change in the respective climate subset and skill metric.

422 moist low-levels and drier mid-to-upper levels, while stratiform precipitation or less or-
 423 ganized convection could be characterized by higher and more homogeneous moisture
 424 profiles (Bunkers et al., 2006; R. L. Thompson et al., 2012). These examples show that
 425 moisture characteristics of vertical atmospheric profiles are likely a learned feature by
 426 the CNN. In regards to the high importance of zonal and meridional winds, thunderstorms
 427 that were classified as non-strongly rotating during PFI were generally due to the uni-
 428 formity of zonal or meridional winds in the permuted fields (Fig. 7e,h), as opposed to
 429 the overall magnitude of the horizontal winds. These results show that the CNN learned
 430 that wind directional shifts over a small region located near the thunderstorm core were
 431 indicative of strong rotation.

432 Visualizations were also created for thunderstorms that were initially classified as
 433 non-strongly rotating, but switched to a strongly rotating classification during PFI (Fig.
 434 8). The permuted moisture fields for these examples (e.g., Fig. 8b) were generally drier
 435 and contained large magnitude gradients in space that represented isolated and intense
 436 convection. Regarding kinematic fields, the original zonal (Fig. 8d) and meridional (Fig.
 437 8g) winds lacked rotational characteristics for the respective thunderstorms (Fig. 8f,i).
 438 However, the permuted fields contained strong rotational features (Fig. 8e,h) which likely
 439 resulted in the changed classification.

440 Individual thunderstorms from the future climate model simulation were chosen
 441 to visualize areas of saliency for predictions made by the CNN. Simulated radar reflect-
 442 ivity of the respective examples are shown in figure 9, which contains a true positive,
 443 false positive, false negative, and true negative case. High values of simulated radar re-
 444 flectivity (>65) are evident near the thunderstorm core of the true positive case (Fig.
 445 9a), which represents a region of high precipitation intensity. The false positive and false
 446 negative examples also contain thunderstorms with high reflectivity (>65 ; Fig. 9b,c), but
 447 the most intense region for the false negative case is located near the southern edge of
 448 the image. The true negative case (Fig. 9d) contains lower maximum reflectivity mag-
 449 nitudes than the other examples (<65), and convection that is smaller in size and less
 450 organized, which possibly contributed to the true negative classification by the CNN.

451 Saliency maps highlight the thunderstorm object areas of input features that con-
 452 tributed to the CNN prediction. For water vapor mixing ratio (right two columns in Fig.
 453 10), positive gradients demarcate the respective pixels that contributed positively to the
 454 model prediction. Moisture at low and mid level heights for the true positive case located
 455 near the thunderstorm core contributed positively to the prediction of strongly rotat-
 456 ing thunderstorms (Fig. 10c,d). While high moisture content may not be related to thun-
 457 derstorm rotation and horizontal kinematics, it does show that the CNN identified the
 458 thunderstorm core (region of high precipitation intensity, and thus moisture content) as
 459 relevant for the strongly rotating prediction. Non-salient regions of respective variables
 460 are zero gradients and therefore correspond to pixels that did not contribute to the model
 461 prediction. In the case of zonal and meridional winds at 3 km (left two columns in Fig.
 462 10), winds of higher absolute magnitude with opposing signs in close proximity to each
 463 other represent regions of rotational winds within the region of the thunderstorm’s up-
 464 draft. These features are evident at the thunderstorm core location, suggesting that the
 465 rotation signature contributed to the strongly rotating prediction. Similar gradient pat-
 466 terns are present in the maps of the false positive and false negative examples at thun-
 467 derstorm core locations (Fig. 10e-l). Saliency maps for true negative cases are substan-
 468 tially different (Fig. 10m-p)—gradients are no longer present across a small and focused
 469 region near the thunderstorm core, but rather across broad areas of the thunderstorm
 470 object. Additionally, gradients from zonal and meridional winds generally no longer align
 471 to form an organized circulation (Fig. 10m,n).

472 Another local and post hoc ML explanation method is input*gradient, which high-
 473 lights areas of relevance to the prediction, computed as the product of the local gradi-
 474 ent with the input itself (Shrikumar et al., 2016). Mamalakis et al. (2021) conducted an

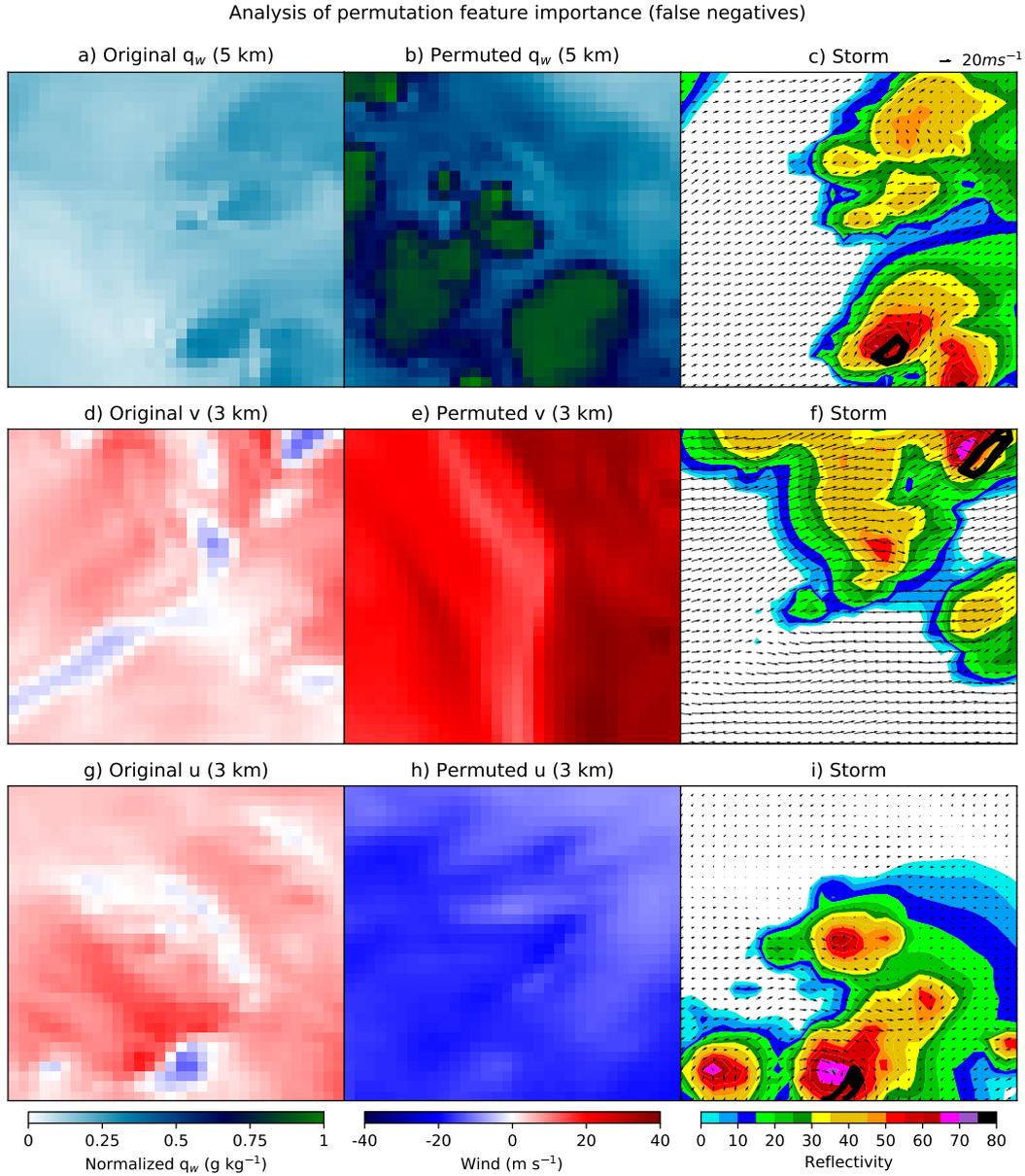


Figure 7. Three example cases (c, f, i) that were classified as non-strongly rotating thunderstorms during the permutation feature importance (PFI) analysis. The CNN classified these future climate thunderstorms as strongly rotating prior to PFI. The top row shows the original water vapor mixing ratio (q_w) field (a) for a pair of strongly-rotating thunderstorms (c), and the q_w field that replaced the original during PFI (b). The center and bottom rows show fields for other example thunderstorms, but for perturbed meridional (v) and zonal (u) winds respectively. Updraft helicity exceeding $75 \text{ m}^2\text{s}^{-2}$ is indicated with black contours (c, f, i). Vectors show winds at 3 km corresponding to the respective thunderstorm image (c, f, i). The q_w fields were normalized by the maximum value of both plots (a, b).

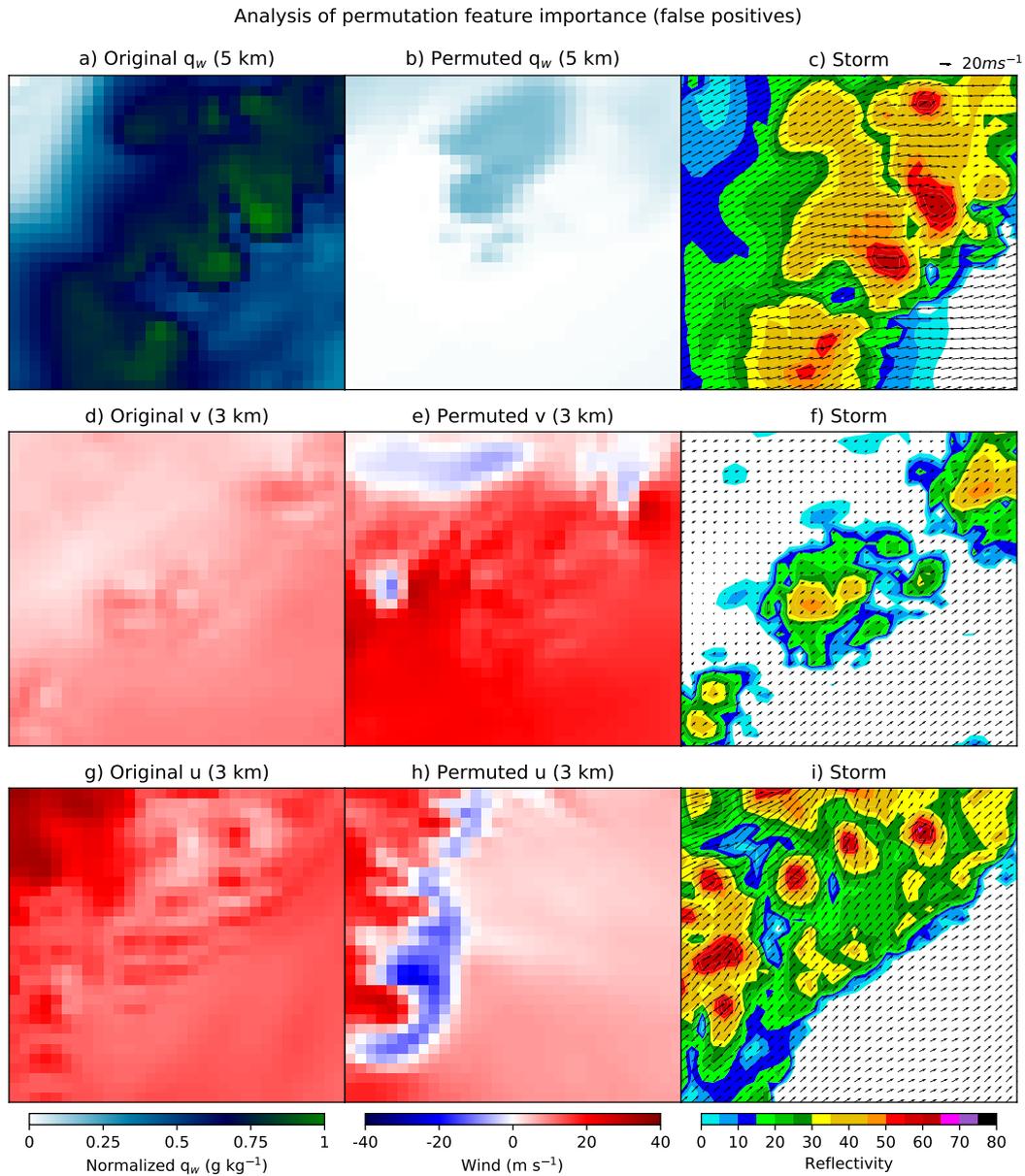


Figure 8. Same as figure 7, but for a subset of thunderstorms that were classified as strongly rotating. The CNN classified these thunderstorms as non-strongly rotating prior to PFI. No black contours are included in the thunderstorm plots (c, f, i) because updraft helicity did not exceed $75 \text{ m}^2\text{s}^{-2}$ for the shown examples.

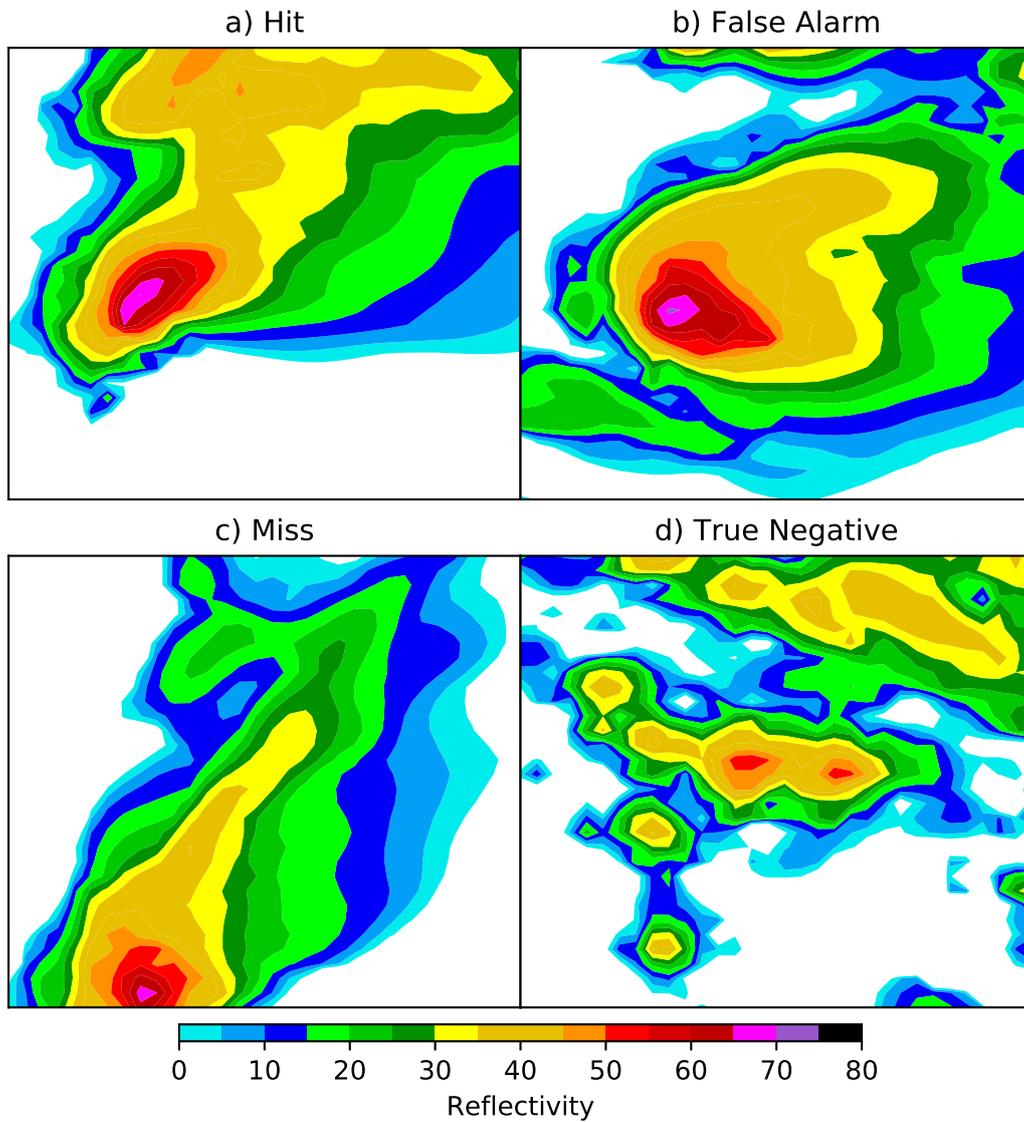


Figure 9. Simulated radar reflectivity for example thunderstorms extracted from the future climate simulation, evaluated as a hit (a), false alarm (b), miss (c), and correct negative (d).

475 attribution benchmark using attribution known a priori (i.e., ground truth) for regres-
 476 sion problems, and found the input*gradient method to produce more skillful explana-
 477 tions than saliency maps. While the benchmark used global sea surface temperatures
 478 and consisted of a very different spatial scale as compared to our application, we decided
 479 to also use the input*gradient method for further exploration of our model’s explana-
 480 tions. Explanations were generally consistent between the saliency maps and input*gradient
 481 methods, with a few minor exceptions (Fig. 11). For instance, the wind rotational sig-
 482 nature was mostly of one sign (positive) near the thunderstorm core using the input*gradients
 483 method for hits, false alarms, and misses (Fig. 11a,b,e,f,i,j). The spatial extent of the
 484 contour explanations were reduced for true negative cases and primarily of negative mag-
 485 nitude for all variables shown (Fig. 11m-p). The moisture fields at 1 and 5 km for the
 486 miss (false negative) example contain mixed signals (positive and negative) that were
 487 displaced away from the thunderstorm core, potentially explaining why the CNN failed
 488 to classify the supercell as strongly rotating (Fig. 11k,l). A challenge with comparing
 489 ML explanation methods without attribution ground truth is that we cannot quantify
 490 explanation skill and rely heavily on our domain knowledge to assess skill subjectively.
 491 It is also possible that certain explanation methods are more useful for certain spatial
 492 and temporal scales yet not others. These questions are beyond the scope of this study,
 493 but should be explored in future work.

494 Results generated using saliency maps and input*gradients can be corroborated
 495 by visualizing the frequency of maximum UH for all thunderstorms. Figure 12a shows
 496 that the CNN is able to identify strongly rotating thunderstorms across a broad range
 497 of UH values that exceed $75 \text{ m}^2\text{s}^{-2}$ and is therefore able to capture a variety of thun-
 498 derstorm rotation intensities. Thunderstorms that were classified as strongly rotating,
 499 but evaluated as false alarms because the corresponding UH did not exceed $75 \text{ m}^2\text{s}^{-2}$,
 500 are heavily skewed towards high UH values (mostly contained UH values that exceeded
 501 $40 \text{ m}^2\text{s}^{-2}$; Fig. 12b), which past studies have found to also be representative of super-
 502 cellular convection (Trapp et al., 2011). Missed classifications of strongly rotating thun-
 503 derstorms generally do not consist of large UH magnitudes ($<100 \text{ m}^2\text{s}^{-2}$), with most thun-
 504 derstorms characterized by UH values close to $75 \text{ m}^2\text{s}^{-2}$ (Fig. 12c). Most true negative
 505 cases consist of UH values below $40 \text{ m}^2\text{s}^{-2}$, which is characteristic of less organized con-
 506 vective storms (Fig. 12d). These results further demonstrate that a CNN is able to gen-
 507 eralize a target derived from a heuristic using learned features in the data that would
 508 be difficult to encode due to spatial complexity. There is sensitivity, however, to the thun-
 509 derstorm location within the thunderstorm object, which can be visualized with 2D his-
 510 tograms that contain the frequency of UH exceeding $75 \text{ m}^2\text{s}^{-2}$, typically located near
 511 the thunderstorm core (Fig. 13). Correctly classified strongly-rotating thunderstorms
 512 (according to the ground truth label) contained regions of high rotation ($\text{UH} > 75 \text{ m}^2\text{s}^{-2}$)
 513 near the center of the thunderstorm object (Fig. 13a,c), while missed classifications are
 514 located near the edges of the thunderstorm object (Fig. 13b,d) for thunderstorms dur-
 515 ing both the current and future climate. This comparison shows that CNNs can strug-
 516 gle with classifications of features located near the edges of a spatial region of interest,
 517 resulting in missed events.

518 4 Conclusions

519 A CNN was trained to learn relationships and identify features among meteoro-
 520 logical state variables in order to classify convection types, with a focus on rotation within
 521 the updraft core of a thunderstorm. Strong rotation and associated storm morphology
 522 could result in a higher likelihood of convection producing severe hazards, such as tor-
 523 nadoes and large hail, which are a dangerous threat to the public. We hypothesized that
 524 due to climate change, a trained CNN may fail to classify and identify convection that
 525 lies outside of the climatological distribution of data used for training. We conducted
 526 a test-case study to address our hypothesis. Using a thermodynamically driven future

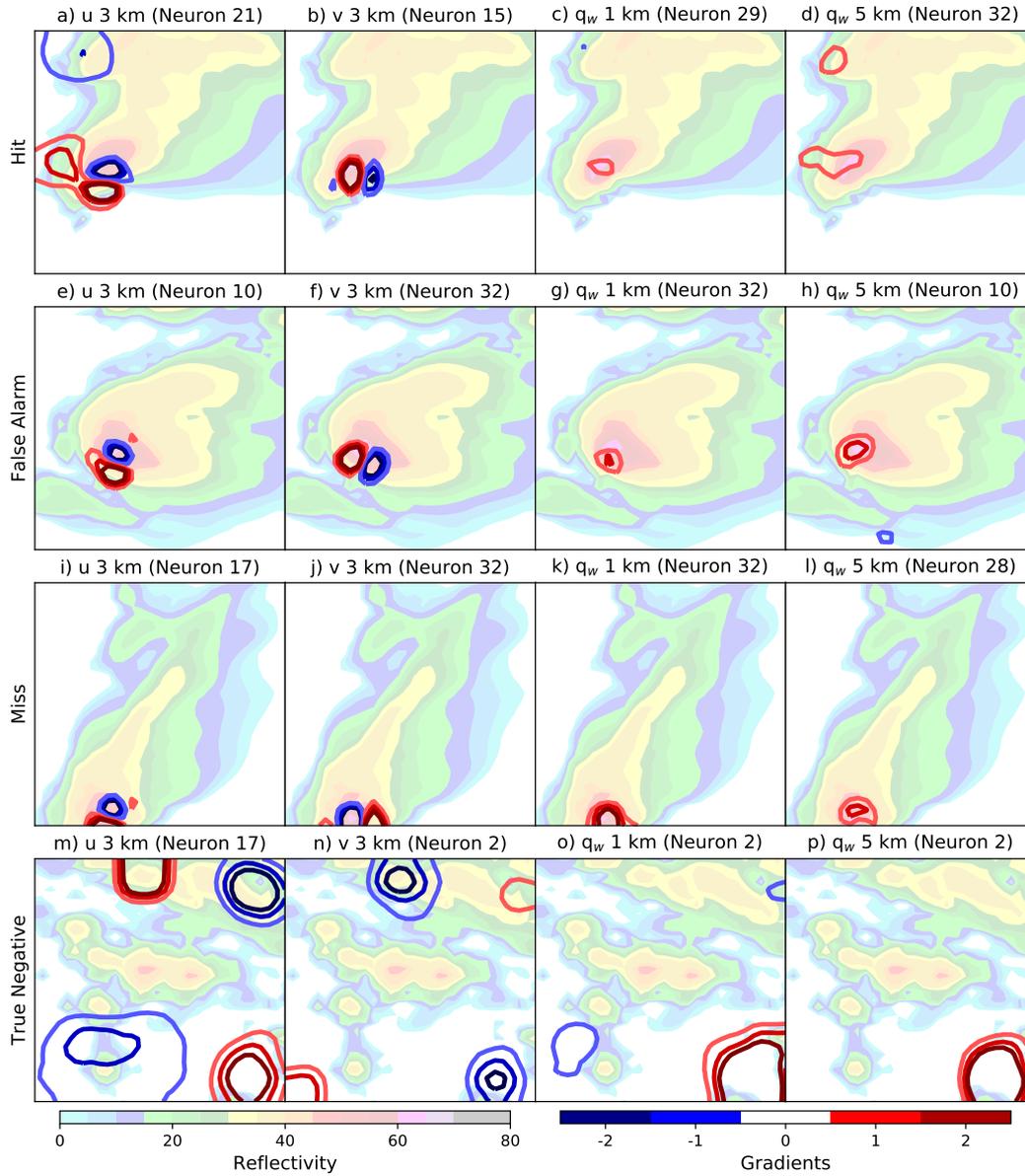


Figure 10. Saliency maps for representative examples of future climate thunderstorms, including true positive (a-d), false positive (e-h), false negative (i-l), and true negative (m-p) cases. Variables shown include several denoted as important by the PFI analysis, such as 3 km zonal (a,e,i,m) and meridional (b,f,j,n) winds, and water vapor mixing ratio (q_w) at 5 km (d,h,l,p). Mixing ratio (q_w) at 1 km is also shown (c,g,k,o).

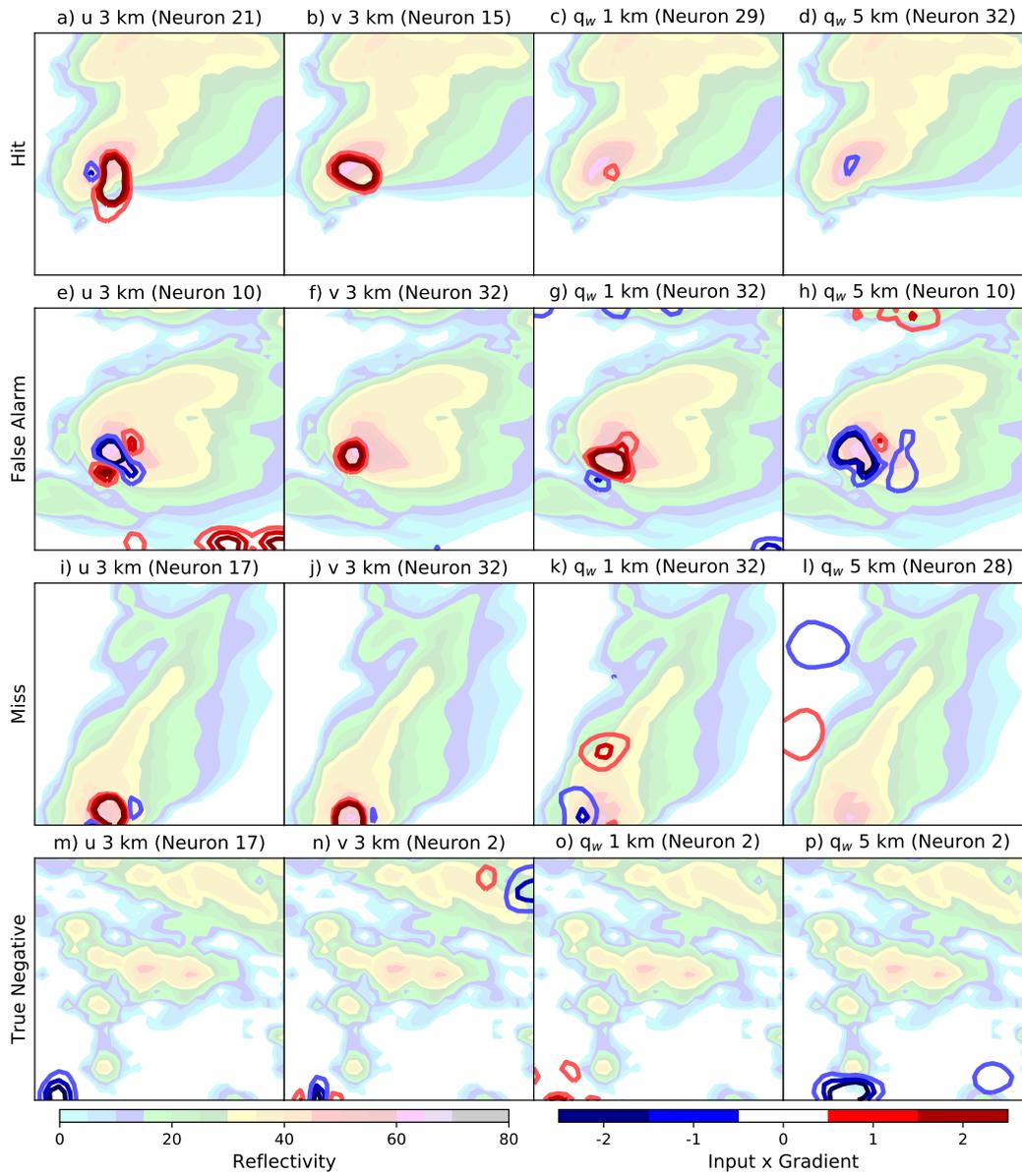


Figure 11. The same as figure 10, but input*gradient values are displayed instead of saliency maps.

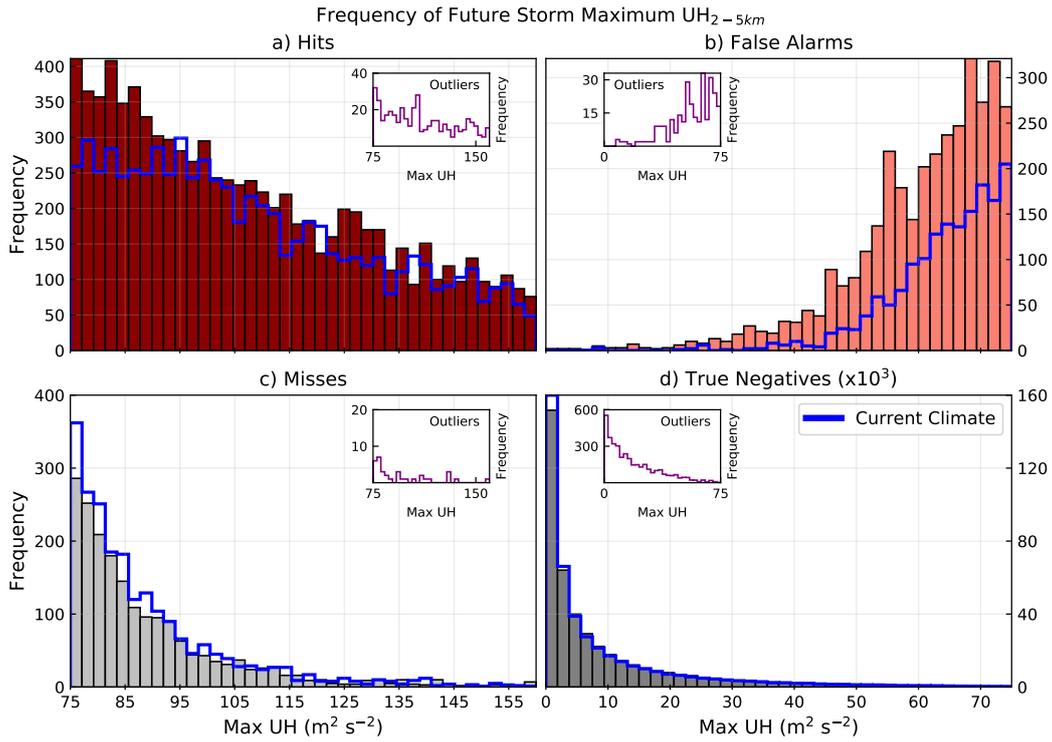


Figure 12. Histograms show the frequency of maximum updraft helicity (UH) for future climate thunderstorms separated into four subsets: hits (a), false alarms (b), misses (c), and true negatives (d). Frequency of true negatives (d) are $\times 10^3$ magnitude. For comparison, the frequencies of the maximum UH for current climate thunderstorms are shown with blue lines and for future outlier thunderstorms in the inset plots.

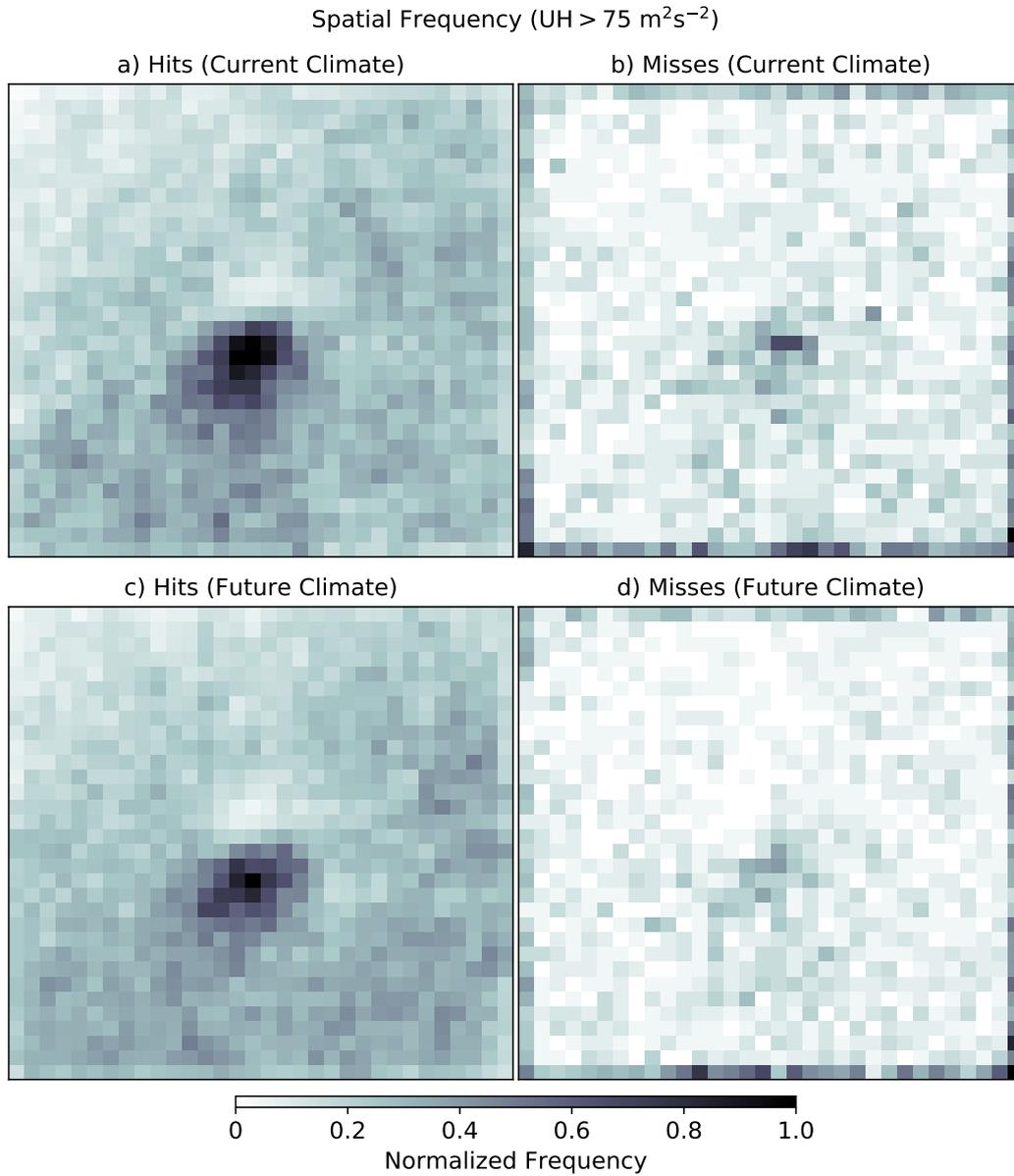


Figure 13. Spatial histograms show the frequency of updraft helicity (UH) exceeding 75 m²s⁻² normalized by maximum frequency for thunderstorm objects classified as hits (a,c) and misses (b,d) during the current (a,b) and future climates (c,d).

527 climate model simulation, our results show that a CNN can remain skillful in classify-
 528 ing convective storms via learned representations of physical variables.

529 The key results that provide answers to the questions posed in the introduction follow:

- 530 1. A CNN trained using a current climate model simulation can skillfully classify out-
 531 of-sample (with regards to moisture content) thunderstorms in a thermodynam-
 532 ically driven future climate. This is possibly partly due to the use of batch nor-
 533 malization and spatial dropout; an equivalent model trained without batch nor-
 534 malization and spatial dropout results in an under-forecasting bias (about 0.84)
 535 in the current and future climate.
- 536 2. Kinematic fields and mid-level moisture were identified as important variables for
 537 skillful classification by the CNN. Spatially, wind rotation signatures with concu-
 538 rrently overlaid sharp mid-level moisture gradients were also important.
- 539 3. Thunderstorm classifications that were incorrect according to the associated ground
 540 truth label included cases that were near the thunderstorm object edge or had a
 541 UH value that was near but on the opposite side of the predefined threshold.

542 Key result 1 shows that a CNN is robust to out-of-sample cases during convection
 543 classification, which is a promising result given the changes already occurring to large-
 544 scale environments and moisture advection patterns associated with severe thunderstorms
 545 (Gensini & Brooks, 2018; Molina & Allen, 2020). Key results 2 and 3 also show that a
 546 CNN can learn complex relationships among input features using labels derived from heuris-
 547 tics. Physical features were not prescribed but rather learned from the data, such as the
 548 importance of dry air at mid-levels for intense thunderstorm development when low-level
 549 moisture is present (i.e., convective available potential energy). We emphasize that UH
 550 was only used to create the labels and was not used as an input attribute into the CNN
 551 during training. Unlike computer vision classification tasks (Russakovsky et al., 2015),
 552 humans can bypass generating a large number of hand labeled data for training mod-
 553 els to perform atmospheric feature classifications, which would also pose challenges given
 554 conflicting definitions of atmospheric phenomena in the scientific literature. Addition-
 555 ally, results show that large imbalances in labeled data may be overcome with sufficient
 556 hyperparameter tuning. Overall, results show that the CNN can classify thunderstorms
 557 as strongly rotating that were near the UH threshold and appeared supercellular, learn-
 558 ing to generalize prescribed UH labels.

559 There are several limitations that are important to acknowledge, however. The fo-
 560 cus in this study lies on a future climate that was thermodynamically driven in order
 561 to isolate competing thermodynamic and kinematic signals, but it is possible that a CNN
 562 may not generalize well with a future climate that accounts for both changes in the ther-
 563 modynamic and large-scale dynamics. We do note that there is a 14% increase in future
 564 strongly rotating thunderstorms as compared to the current climate, which is a substan-
 565 tial increase and an indication that changes in large-scale dynamics may not pose a sig-
 566 nificant issue to the CNN. An additional limitation is that physical interpretation meth-
 567 ods require substantial human interpretation, making it possible to miss important fea-
 568 tures or fail to discover new physical relationships. However, this is a broader issue within
 569 machine learning explanations (i.e., interpretability), as it introduces the potential for
 570 confirmation bias from human scientists attempting to explain results. Future work should
 571 explore incorporating feature uncertainty or physics within the CNN model architecture
 572 to explore the differences to results contained herein. Additionally, methods to amelio-
 573 rate missed classifications near the edges of study domains should be explored. As so-
 574 cietal exposure to severe hazards continues to increase (e.g., Ashley & Strader, 2016),
 575 it is important to continue better identifying and understanding severe hazards within
 576 climate model simulations. The use of deep learning methods that do not impose rigid
 577 thresholds or expert systems decisions should continue to be explored, since meteoro-

578 logical phenomena generally do not neatly fit into predefined classes. Deep learning of-
579 fers a viable avenue to continue to better understand weather and climate extremes.

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595 NCAR Research Data Archive hosted by CISL at [https://rda.ucar.edu/datasets/
596 ds612.0/](https://rda.ucar.edu/datasets/ds612.0/). The software developed for this research is available on Github [https://github
597 .com/mariajmolina/deep-conus](https://github.com/mariajmolina/deep-conus). Processed data shown in the figures is archived on
598 Zenodo (Molina, Gagne, & Prein, 2020). The convolutional neural network was trained
599 using the high-level Python-based Keras deep learning library (Chollet et al., 2015) with
600 the TensorFlow (version 2.3.1) low-level backend (Abadi et al., 2016). We are grateful
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