# A multiscale numerical modeling investigation on the significance of flow partitioning for the development of quartz c-axis fabrics

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#### Abstract

Quartz c-axis fabrics in natural mylonites can vary to such an extent that they apparently give opposite senses of shear in a single thin section. Many hypotheses have been invoked to explain this. Here, we couple our self-consistent multiscale approach for flow partitioning with the visco-plastic self-consistent model for crystallographic fabric simulation to investigate quartz c-axis fabric development. Quartz aggregates are regarded as microscale Eshelby inhomogeneities embedded in a macroscale medium whose effective rheology is represented by a hypothetical homogeneous equivalent medium which is rheologically isotropic or has a planar anisotropy. We reproduced the observed quartz c-axis fabrics. We found that, although the microscale flow fields are distinct from one another and from the macroscale flow, the microscale vorticity in every inhomogeneity has the same sense as the macroscale vorticity. This implies that one can use the average of the microscale vorticity axes determined through the crystallographic vorticity axis analysis to obtain the macroscale vorticity axis. However, quartz c-axis fabrics cannot be used to determine the vorticity number where flow partitioning is significant.

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20	c-axis fabrics cannot be used to determine the vorticity number where flow partitioning is
21	significant.
22	Keywords: quartz c-axis fabric; flow partitioning; multiscale modeling, MOPLA; VPSC

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#### 24 1. Introduction:

Quartz c-axis fabrics are widely used to infer flow kinematics (e.g. Lister and Hobbs, 25 1980; Price, 1985; Simpson and Schmid, 1983) as well as deformation temperature (e.g. Faleiros 26 et al., 2016; Law, 2014) and mechanisms (e.g. Schmid and Casey, 1986; Stipp et al., 2002) of 27 28 ductile shear zones in Earth's lithosphere. In terms of kinematics, the asymmetry of a c-axis fabric with respect to the shear zone coordinates is routinely used to infer sense of shear (e.g. 29 Lister, 1977; Lister and Price, 1978; Lister and Williams, 1979; Menegon et al., 2008; Price, 30 1985). Fig.1 summarizes the standard models for this practice (e.g. Passchier and Trouw, 2005). 31 32 Note we have adopted the convention of Lister (1977) to present the c-axis fabrics whereby the shear plane (C-foliation) is vertical east west and the shear direction (the Lc-lineation of Lin et 33 al., 2007) is horizontal east. This convention differs from the one that orients the S-foliation east 34 west and Ls-lineation horizontal east (e.g., Passchier and Trouw 2005). Natural quartz c-axis 35 fabrics mainly comprise of single- and cross-girdles. In the coordinate system used here (Fig.1), 36 37 the cross-girdle has its dominant girdle normal to the shear plane and the weaker girdle inclined antithetically to the shear sense (Fig.1a). Single c-axis girdles either incline antithetically to the 38 39 shear sense or are nearly normal to the shear plane (Fig.1b, c). Point maxima within the girdles may lie at the periphery, the center, or intermediate positions between the periphery and the 40 41 center. These are interpreted as reflecting the slip systems during deformation (e.g. Mainprice et al., 1986; Okudaira et al., 1995; Schmid and Casey, 1986; Simpson and Schmid, 1983). The 42 models summarized in Fig.1 were based on numerical modeling of pure quartz aggregates using 43 the Taylor-Bishop Hill model (e.g. Lister, 1977; Lister and Hobbs, 1980; Lister and Williams, 44 45 1979) and the visco-plastic self-consistent (VPSC) model (e.g. Morales et al., 2011; Nie and Shan, 2014; Wenk et al., 1989). Both model methods predicted that the c-axis girdle is antithetic 46 or normal to the shear zone boundary in the coordinate system used here. Modeling has never 47 generated girdles synthetically-inclined to the shear plane. 48

However, synthetically-inclined girdles have been observed in both natural shear zones
(e.g. Keller and Stipp, 2011; Kilian et al 2011, Law et al., 2010; Little et al., 2016) and creep
experiments of quartz aggregates (e.g. Heilbronner and Tullis, 2006; Kilian and Heilbronner,
2017). Heilbronner and Tullis (2006) suggested that the synthetical orientation is due to rotation
with vorticity of earlier antithetic girdles as finite strain increases. But this is not supported by

any numerical modeling work with fairly large shear strains (up to 5, e.g. Jessell and Lister, 54 1990; Morales et al., 2011). Little et al (2016) suggested that general plane-strain flows may lead 55 to synthetically-inclined c-axis girdles. The VPSC models of Takeshita et al. (1999) and Nie and 56 Shan (2014) considered such flows but did not produce any synthetically-inclined c-axis girdles. 57 However, their model did not consider cases where prism<a> and rhomb<a> slips are more 58 59 significant than basal <a> slip. Through VPSC modeling, Keller and Stipp (2011) produced synthetically-inclined c-axis girdle with rhomb <a>, prism <a>, and prism <c> all active and all 60 more significant than the basal  $\langle a \rangle$  slip system. However, there are natural samples with 61 synthetically-inclined c-axis girdles (e.g. Little et al 2016, Kilian et al 2011; Law et al 2010) that 62 were clearly produced in the temperature range ~350-550°C much below that required for the 63 activation of prism <c> slip (Toy et al., 2008). Furthermore, c-axis fabrics with both 64 65 synthetically- and antithetically-inclined c-axis girdles have been observed in the same thin section (Kilian et al., 2011 their fig. 8, 9). Therefore, it is important to clarify if the combination 66 of rhomb<a> and prism<a> slip, without prism <c>, can generate these synthetically-inclined c-67 axis girdles. 68

69 The standard models summarized in Fig.1 are based on the deformation of pure quartz 70 aggregates under limited (mostly simple shearing) single-scale uniform flows (e.g. Lister et al., 71 1978; Lister and Hobbs, 1980; Lister and Williams, 1980; Keller and Stipp, 2011; Morales et al., 2014; Nie and Shan, 2014; Wenk et al., 1989). The spatial variation of quartz c-axis fabrics is a 72 manifestation of heterogeneous deformation and, we suspect, is related to flow partitioning (e.g., 73 Jiang, 1994a, 1994b; Lister and Williams, 1983) and strain buildup in rheologically distinct 74 75 domains. Most natural mylonites are made of polyphase minerals in which the microscale rheology varies from one domain to another which facilitates flow partitioning. In fact, many 76 authors have referred to flow partitioning qualitatively (e.g., Killian et al. 2011; Garcia Celma, 77 1982; Jerabek et al., 2007; Larson et al., 2014; Law, 1987; Lister and Price, 1978; Passchier, 78 1983; Pauli et al., 1996; Peternell et al., 2010) to explain observed c-axis fabric variations. 79

In this contribution, we apply a multiscale numerical modeling approach to quantitatively investigate the consequence of flow partitioning on the development of quartz c-axis fabrics and compare our modeling results with natural and experimental observations. Specifically, we use the mylonite thin-section photomicrograph of Killian et al (2011, Fig.8 there) as a model and

seek to understand if flow partitioning can produce the observed variation in quartz c-axisfabrics.

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# 87 2. Approach

Fig.2a shows the thin-section photomicrograph from Kilian et al (2011). The rock is 88 comprised of quartz domains (from which c-axis fabrics were presented), feldspar 89 porphyroclasts, and a matrix of fine-grained quartz, feldspar, and mica. According to Kilian et al. 90 91 (2011), the microstructure was produced in a simple shearing flow which is consistent with the geometric pattern of the foliation (Ramsay, 1980; Ramsay and Graham, 1970). In this 92 investigation, we consider plane-strain general shearing flows as the bulk flow field to 93 understand how the partitioning of the bulk flow into rheologically distinct quartz domains may 94 95 affect the c-axis fabrics in those domains. Our method here also applies to any 3D general 96 shearing flows (e.g. Jiang and Williams, 1998).

97 In the coordinate system used in this investigation (Fig.2c), a general plane-strain general
98 shearing flow is defined by the following Eulerian velocity gradient tensor:

99 
$$\mathbf{L} = \begin{pmatrix} \dot{\varepsilon} & \dot{\gamma} & 0 \\ 0 & -\dot{\varepsilon} & 0 \\ 0 & 0 & 0 \end{pmatrix}$$
(1)

100 where  $\dot{\gamma}$  is the shear strain rate for the simple shearing component and  $\dot{\varepsilon}$  is the strain rate 101 parallel to the X-axis. The flow in Eq.1 corresponds to a kinematic vorticity number

102 
$$W_k = \frac{\dot{\gamma}}{\sqrt{4\dot{\varepsilon}^2 + \dot{\gamma}^2}}$$
 (Jiang and White, 1995; Li and Jiang, 2011; Truesdell, 1953). We

- 103 consider the variation of the flow by varying  $W_k$  from 0 to 1.
- 104 The progression of the finite strain is measured by a strain intensity defined as  $\rho = \sqrt{\left(ln\frac{s_1}{s_2}\right)^2 + \left(ln\frac{s_2}{s_3}\right)^2}$  where  $s_1, s_2, s_3$  are the three principal stretches  $(s_1 > s_2 > s_3)$  of the

finite strain ellipsoid (e.g., Yang et al., 2019). In the event of simple shearing ( $W_k = 1$ ), the strain can also be measured by the shear strain  $\gamma$ . The relation between  $\gamma$  and  $\rho$  in simple shearing situation is shown in Fig.3.

We use the Visco-Plastic-Self-Consistent(VPSC) model, originally due to Molinari et al 109 (1987) and further developed by Lebensohn and Tome (1993), to simulate the quartz c-axis 110 fabric development in a flow field. Specifically, VPSC7 (Lebensohn and Tomé, 2009) for 111 Windows is used in this investigation. We track the c-axis evolution of 500 quartz crystals whose 112 initial orientations are randomly distributed in 3D space (Jiang 2007b). The initial shapes of 113 114 grains are equant. The crystal shapes evolve with strain and the grain fragmentation scheme of Beyerlein et al. (2003) is used to limit the aspect ratio of quartz grains to mimic some effect of 115 dynamic recrystallization. The VPSC output of c-axis data are plotted using the MTEX toolbox 116 (Bachmann et al., 2010). Since we are concerned with variation in quartz c-axis fabrics, we 117 present pole figures of the (0001) directions here. Pole figures of other crystal directions are 118 provided in the supplementary material. 119

120 The relative activity of slip systems is modulated in VPSC by their relative critical resolved shear stress (CRSS). A lower CRSS corresponds to higher activity. For quartz, the 121 CRSS for a slip system is largely temperature dependent with basal <a> slip occurring at about 122 350-500°C, rhomb<a> and prism<a> slip at ~ 500-600°C, and prism<c> slip at >650°C (e.g. 123 Toy et al., 2008). Table 1 summarizes the slip system combinations used in this study based on 124 previous work (e.g. Lister and Paterson, 1979; Morales et al., 2014; Wenk et al., 1989). They are 125 labelled as Model-A to F. Morales et al (2014) and Keller and Stipp 2011) made a distinction 126 between rhomb (+)  $slip{r}$  in <a> direction and rhomb (-)  $slip{z}$  in <a> direction in their 127 modelling works. This distinction may be important in regime 1 dislocation creep (Hirth and 128 Tullis, 1992) but it is not necessary for our work here on the effect of flow partitioning. 129

In the single scale case, the flow field defined in Eq.1 is used in the VPSC directly for the simulation of the resulting quartz c-axis fabric development. In the multiscale case, Eq.1 defines the bulk macroscale flow which must be partitioned into different rheologically distinct quartz domains (Figs. 2b and d) before the quartz c-axis fabric development in those domains can be simulated with VPSC. We use the self-consistent Multi Order Power Law Approach (MOPLA) (Jiang and Bentley 2012; Jiang 2016, 2014; Qu et al., 2016; and Lu 2020) to obtain the

partitioned flow fields in quartz domains. The multiscale approach can be illustrated using the 136 thin section sample in Fig.2a as follows: Quartz domains, feldspar porphyroclasts, and mica 137 138 seams are referred to as Rheologically Distinct Elements (RDEs). The sample as a whole was subjected to a *macroscale* flow field like Eq.1. In micromechanics terms, the macroscale flow is 139 140 the bulk flow averaged on a Representative Volume Element (RVE) which represents the mineral assemblage for the sample. It is reasonable to regard the thin section as a section of the 141 RVE for the macroscale flow. The microscale flow field in each constituent RDE such as a 142 quartz domain is distinct and differs from the macroscale flow, because each RDE is unique in 143 its rheology, shape, and orientation (Eshelby, 1957; Mura, 1987; Jiang 2014, 2016). Clearly, it is 144 the microscale (or partitioned) flows in quartz domains that are responsible for the quartz c-axis 145 fabric development. 146

147 In MOPLA, an RDE is regarded as an ellipsoidal Eshelby inhomogeneity embedded in and interacting with the macroscale material (Fig.2d). The rheology of the latter is approximated 148 149 by a homogeneous effective medium (HEM) and obtained from the rheologies of the constituent RDEs from a set of homogenization equations. The microscale or partitioned flows in an RDE is 150 151 related to the macroscale flow, which is assigned by Eq.1, by a set of partitioning equations (for details, see Jiang 2014, 2016). The partitioning and homogenization equations are solved 152 153 simultaneously to obtain the partitioned flow fields and the macroscale rheology. As the relevant rheology for mylonites are power-law viscous (Kohlstedt et al., 1995), the MOPLA formulation 154 155 adopts a linearization approach (Lebensohn and Tomé, 1993; Molinari et al., 1987) where linearized viscosities such as tangent viscosities are used in the formulation. As we are 156 157 concerned with quartz c-axis fabric development, we specifically use MOPLA to calculate the partitioned flow fields within quartz domains. 158

We consider two situations for the rheology of the quartz RDEs and HEM. In the first, both the RDEs and the HEM are isotropic. The rheological contrast between an RDE and the HEM is reduced to an effective viscosity ratio *r* between the RDE to the HEM. We do not consider the rheological anisotropy development in HEM as a result of fabric buildup with strain because anisotropic rheological response of the constituent RDEs are not available. Because of power-law rheology, *r* varies with time. We thus consider a range of constant *r* values. The quartz aggregates in Fig.2a all have convex shapes with surrounding matrix material wrapping

around them, suggesting that quartz RDEs were rheologically stronger (r > 1) than the ambient HEM. But *r* cannot be too high (e.g., r > 10) because of power-law rheology or the quartz RDEs would behave like rigid clasts (Jiang, 2007a; Xiang and Jiang, 2013) with no c-axis fabric formation. We consider the situations of *r* being 2, 5, and 10. The situation of r = 0.5 is also considered here for comparison to show what the c-axis fabrics might be like if quartz RDEs were mechanically weaker than the ambient medium.

In the second situation, we consider isotropic RDEs in a HEM of simple planar 172 anisotropy which approximates a foliated and/or layered material like natural mylonites. The 173 rheology of such a HEM can be characterized by two distinct viscosities:  $\eta_n$ , the normal 174 viscosity for the resistance to pure shearing along and perpendicular to the layering, and  $\eta_s$  the 175 shear viscosity measuring the resistance to shearing parallel to the layering (e.g. Jiang, 2016; 176 Fletcher, 2009; Johnson and Fletcher, 1994). The strength of anisotropy is measured by the ratio 177 m of  $\eta_n$  to  $\eta_s$ . For foliated and layered rocks, m > 1 (Treagus, 2003). The rheological contrasts 178 between the isotropic quartz RDE and HEM can be defined by the following two parameters: the 179 ratio,  $r_{eff}$ , between the viscosity of the RDE to  $\eta_n$  and m. In such case, the effective viscosity of 180 the RDE is simply given by  $r_{eff}\eta_n$ . Similar to the isotropic cases, we consider  $r_{eff}$  being 0.5, 2, 5, 181 and 10. Fig. 4 shows the geometric relation between the flow field and the plane of anisotropy. 182 183 Macroscale flow is simple shear with shear plane parallel to X-Z plane.

To cover the shape variation of quartz RDEs, we considered three reference initial shapes: prolate (5:1:1), oblate (5:5:1), sphere (1:1:1) and initial triaxial RDEs with long and short semi-axial length fixed to 5 and 1 respectively and intermediate semi-axial length ranging from 2-4. These initial RDEs will deform into various possible triaxial shapes in nature. The initial orientations of the RDEs are defined by spherical angles (Jiang, 2007b, 2007a) which are randomly assigned.

The partitioned flow for a quartz RDE computed from MOPLA is used as the input flow field to simulate the quartz c-axis fabrics in that RDE through the VPSC model. Because the partitioned flow field in any given RDE is non-steady as the RDE continuously changes shape and orientation during deformation, the coupled computation between MOPLA and VPSC is carried out as follows: With a given macroscale flow field defined in Eq.1, we use MOPLA

algorithm implemented in MATLAB (Lu, 2020; Jiang, 2016, 2014, 2007a; Jiang and Bentley,
2012; Qu et al., 2016) to calculate the partitioned flow in every quartz RDE, which is expressed
as a velocity gradient tensor. We export to a data file the RDE velocity gradient tensor for every
prescribed macroscale strain increment until a pre-set macroscale finite strain is reached. This
data file is then used as input flows into the VPSC code to calculate the c-axis fabric evolution
within the RDEs as macroscale strain increases until the set magnitude. The velocity gradient
tensor files for all the RDEs are available in the supplementary material.

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# 203 **3. Results:**

As mentioned above, we have simulated quartz c-axis fabric development in three situations. The first is in homogeneous macroscale plane-strain general shearing flows, without flow partitioning, with quartz slip system combinations that have not been covered by previous studies. The second situation is when rheologically distinct quartz domains are within an isotropic HEM, and the third is when the quartz domains are within a HEM of planar anisotropy.

209 3.1 Quartz c-axis fabric development in homogeneous plane-strain general shearing flows

Figs.5 and 6 present quartz c-axis fabrics produced for models-A-F (rows) under uniform macroscale flows of plane-strain general shearing from  $W_k = 0$  to  $W_k = 1$  (columns), at

212 macroscale strain states  $\rho = 2$  and 6.

In pure shearing ( $W_k = 0$ ), for models-A, C, and D, peripheral c-axis maxima form and remain at the maximum shortening direction regardless of strains (Figs. 5a,d, m,p,6a,d). For model-B, a cross-girdle (Figs 5g) form at  $\rho = 2$ , with its central segment lying along the maximum shortening direction. A single girdle is produced lying along the maximum shortening direction (Figs. 5j) at  $\rho = 6$ . For models-E and F, peripheral maxima develop and remains at the maximum stretching direction at both strain states (Figs. 6g, j, m, p).

When  $0 < W_k \le 1$ , for models-A, C, and D and at  $\rho = 2$ , peripheral c-axis maxima are developed inclining antithetically to the shear sense (Figs. 5b, c, n, o, 6b, c). As  $W_k$  increases, the angle between the peripheral c-axis maxima and the shear plane normal increases. The peripheral 222 maxima rotate with macroscale vorticity as finite strain increases but do not pass the shear plane normal (Figs. 5f, l, q, r, 6f). For model-B, a cross-girdle, with its central segment lying normal to 223 the shear plane, is formed at  $\rho = 2$  (Figs 5 h, i). At  $\rho = 6$ , this cross-girdle becomes a single girdle 224 225 lying normal to the shear plane (Figs. 5 k, l). In some general shear  $(0 < W_k < 1)$  cases, the c-axis girdles can be slightly synthetically-inclined at  $\rho = 6$  (Figs. 5e,k,6e), but the angle between the 226 peripheral c-axis maxima and the shear plane normal is small (< 10°). For models-E and F, the c-227 228 axis peripheral maxima are synthetically-inclined near the shear direction at  $\rho = 2$ . The angle between the peripheral c-axis maxima and the shear direction increases with  $W_k$  (Figs.6h, i, n, o). 229 The c-axis peripheral maxima rotate with vorticity toward the shear direction as the finite strain 230 increases (Figs.6 k, l, q, r). 231

#### 232 3.2 Quartz c-axis fabric development in quartz domains embedded in an isotropic HEM

Since models-A, B, C and D all produce similar c-axis fabrics with c-axis girdles 233 antithetically-inclined or nearly normal to the shear plane, we only present results for model-A 234 for multiscale deformation. Figs. 7 and 8 report ten results of c-axis fabrics produced in quartz 235 236 RDEs of varying initial shapes, orientations, and viscosity ratio r under a range of macroscale flow fields. These results can be summarized as follows: When  $0 < W_k \le 1$ , c-axis girdles are 237 always antithetically-inclined (Figs.7a,b,d,e,g,h, j, k, m, n, 8a,g,j,m) regardless of initial 238 conditions of RDEs up to the finite strain  $\rho \sim 4$ . With increase in finite strain, the girdles rotate 239 with bulk vorticity (rows of Figs.7 and 8) but do not pass the shear plane normal unless  $r \ge 5$ 240 (Figs. 7-i, l, o, 8-b, c, i, l, o). If the RDEs were weaker than the HEM (r = 0.5), c-axis girdles 241 remain close to normal (Figs. 7-c) to the shear plane even at very high finite strains ( $\rho \sim 6-7$ ). In 242 pure shearing, a cross girdle is produced at  $\rho \sim 2$  which becomes a single girdle at  $\rho \sim 6$  with 243 peripheral c-axis maxima always parallel to the maximum shortening direction (Figs.8-d, e, f). 244

245 3.3 Quartz c-axis fabric development in quartz domains embedded in a planar anisotropic HEM

Figs. 9a-o report c-axis fabrics developed in quartz RDEs of varying initial shapes, orientations, and viscosity ratio  $r_{eff}$ , embedded in a planar anisotropic HEM of anisotropic strength *m* as described in Section-2. These results can be summarized as follows: The c-axis girdles are always antithetically-inclined (Figs.9a,d,g,j,m) at  $\rho \sim 2$  regardless of  $W_k$ ,  $r_{eff}$ , *m*, initial orientations and shapes of RDEs. The girdles rotate with bulk vorticity as  $\rho$  increases (rows of Figs.9) but do not pass the shear plane normal unless  $r_{eff} \ge 2$  (Figs. 9i, 1, o). If RDEs were weaker ( $r_{eff} = .5$ ), c-axis girdles are close to normal (Figs. 9c, f) to the shear plane even at high

253 finite strains ( $\rho \sim 6-7$ ).

# 254 **4. Discussion:**

In Section 2, we argued that r must be greater than 1 from microstructures (Fig.2a) but 255 not so high that the quartz RDEs do not develop enough internal strain for c-axis fabric 256 257 formation. In our modeling, we considered the range r between 2 and 10. Our modeling results 258 show that, with basal  $\langle a \rangle$ , rhomb  $\langle a \rangle$ , and prism  $\langle a \rangle$  slips, c-axis girdles in a quartz RDE always develop at an antithetical orientation initially. But the girdles rotate with vorticity as the 259 macroscale finite strain increases. If the RDE is sufficiently strong ( $r \ge 5$  in isotropic HEM case 260 and  $r_{eff} \ge 2$  in planar anisotropic HEM case), the girdles will rotate pass the shear zone normal 261 and lie in the synthetical sector at high strains ( $\rho \sim 6$ , Figs. 7-i, l, o, 8-b, c, i, l, o, 9-i, l, o). Our 262 263 modeling results show that for synthetically-inclined girdles, r should be between 5 and 10. These results are consistent with the strain gradient of the thin section (Fig.10, based on Killian 264 et al., 2011, Fig.9 there). The antithetically-inclined c-axis peripheral maxima (yellow in Fig.10) 265 266 correspond to a lower strain and synthetically-inclined c-axis peripheral maxima (red in Fig. 10) to a higher strain. 267

Despite the variability of the partitioned flow field in quartz RDEs, we found out that the 268 microscale vorticity in every quartz RDE still has the same sense as the macroscale vorticity. 269 Fig.11 shows the dot product of the unit vector  $\hat{\omega}$  parallel to the vorticity in a RDE and the unit 270 vector  $\widehat{\Omega}$  parallel to the macroscale vorticity.  $\widehat{\omega} \cdot \widehat{\Omega}$  is positive for all quartz RDEs (a few 271 selected ones are shown in Fig.11). In other words, there is no vorticity sense reversal in any 272 quartz RDEs. This implies that the volume-weighted average of microscale vorticity vectors is 273 parallel to the macroscale vorticity vector. Therefore, the crystallographic vorticity axis (CVA) 274 analysis (Giorgis et al., 2017; Michels et al., 2015) can still be used in every quartz RDE and 275 then the averaged microscale vorticity axes represent the macroscale vorticity axis. 276

Synthetically-inclined c-axis girdles have also been reported in some creep experiments
on pure quartz aggregates with similar slip systems (basal<a>, rhomb<a>, and prism<a>) at high
finite strains (Heilbronner and Tullis 2002, 2006). Although Keller and Stipp (2011) obtained

synthetically-inclined c-axis girdles by including prism<c> slip in their VPSC models, we have
further confirmed that without prism <c> slip (our model-D), synthetically-inclined c-axis
girdles cannot be produced (Figs. 5a-f), unless flow partitioning is considered. We suspect that
some degree of heterogeneous strain and therefore partitioned flow was responsible for such caxis girdle orientations. Heilbronner and Tullis (2006) themselves suggested that different
domains of polycrystal aggregates might exhibit different viscosities, which could have
facilitated partitioning of the flow among different domains.

Li and Jiang (2011) raised issues with the practice of vorticity estimation using rigid 287 porphyroclasts under the assumption of steady-state homogeneous flow histories. The 288 significance of flow partitioning as demonstrated by our modeling based on microstructures of 289 natural mylonites raises further issues with using quartz c-axis fabrics to estimate the 290 (macroscale) vorticity (e.g. Vissers, 1989; Wallis, 1995, 1992; Xypolias, 2009; Law, 2010). 291 First, where quartz c-axis fabrics have resulted from partitioned flow, the steady-state flow 292 293 assumption is invalid. As we have shown, there is a distinct microscale vorticity history, not a constant vorticity number, in every quartz RDE, which cannot be determined from the final c-294 axis fabric. In principle, the microscale vorticity in a quartz RDE does not have a simple relation 295 to the macroscale vorticity. Second, even for the single-scale case where no flow partitioning is 296 297 considered, our modeling demonstrates that the assumption commonly used in vorticity determination that the dominant c-axis girdle is perpendicular to the shear plane is not always 298 299 valid.

Peripheral c-axis maxima close to the shear direction have commonly been taken to reflect prism <c> slip (Passchier and Trouw, 2005). Our modeling suggests that they can also be significantly rotated peripheral basal <a> maxima from certain quartz RDEs (Fig.8c). Larson et al (2014) have reported a possible example of this. They presented peripheral c-axis maxima close to the shear direction in a temperature condition much below that required for the activation of prism <c> and used the concept of flow partitioning to explain their observation. Our modeling lends support to this explanation.

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# **309 5. Conclusions:**

The co-existence of both synthetically-inclined and antithetically-inclined quartz c-axis girdles in a single thin section can be explained by flow partitioning at the thin section scale. The antithetically-inclined girdles correspond to relatively low finite strains and the syntheticallyinclined girdles to high finite strains.

Although the microscale flow fields vary from one quartz RDE to another and are distinct from the macroscale flow, the sense of vorticity in every quartz RDEs remains the same as the macroscale vorticity.

Because of flow partitioning, it is not possible to estimate the vorticity number of the macroscale flow from quartz c-axis fabrics. But, it is still possible to obtain the macroscale vorticity axis by averaging the microscale vorticity axes from quartz RDEs. The latter can be obtained through the crystallographic vorticity axis analysis .

As a result of partitioned flows, the dominant quartz c-axis girdle can lie antithetical, normal, synthetical to the shear plane. The basal <a> peripheral maxima may end up lying close to the shear direction at high macroscale strains. Caution should be taken not to misinterpret these peripheral maxima as reflecting prism<c> slip.

325

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#### 532 Figure Captions:

533 Figure 1: Current models for interpreting quartz c-axis fabrics at low to medium temperatures  $\sim$ 350-550°C presented in the shear zone coordinate system. The sense of shear is dextral. Cross-534 535 girdle and single girdle c-axis fabrics are commonly observed. (a) c-axis cross girdle pattern with one girdle normal to the shear plane while the other antithetic to the shear sense. (b) a single c-axis 536 537 girdle with Y-maxima, inclined either antithetically to the shear sense or normal to the shear plane. (c) a single c-axis girdle inclined either antithetically to the shear sense or normal to the shear 538 539 plane. The c-axes near the periphery, the center, and in between are interpreted to reflect basal<a>, prism<a>, and rhomb<a> slips respectively. 540

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Figure 2: Illustration of the multiscale approach used in this paper. (a) The thin section 542 photomicrograph of a natural mylonite from Kilian et al. (2011) used as a model. (b) Sketch of 543 544 (a). The thin section can be viewed as a 2D section of the representative volume element (RVE) for the shear zone material, which is composed of quartz domains, feldspar porphyroclasts, and 545 mica seams in a fine-grained matrix. The quartz domains and feldspar clasts are referred to as 546 Rheologically Distinct Elements (RDEs). We are concerned with partitioned flows in quartz 547 548 RDEs in this paper. (c) Coordinate system to define the macroscale flow field used in modeling investigation (d) Each quartz RDE is regarded as a heterogeneous Eshelby inclusion embedded 549 550 in the composite shear zone material that is idealized as the Homogeneous Equivalent Matrix (HEM). Microscale fields (strain rate  $\varepsilon$ , and vorticity w) are related to respective macroscale 551 fields (**E** and **W**) by partitioning equations, where **A** is the strain partitioning tensor, **S** and  $\Pi$ 552 are respectively the 4<sup>th</sup>-order symmetric and anti-symmetric Eshelby tensors (Jiang 2014). 553

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556 Figure 3: The macroscale finite strain of the shear zone, measured by the strain intensity  $\rho$ , as a function of computation steps for varying  $W_k$ . The increase of the shear strain y in the simple 557 shear case  $(W_k = 1)$  is also plotted for comparison. 558 559 560 Figure 4: Geometric relation between the macroscale flow field and anisotropy plane in the planar anisotropic HEM. 561 562 Figure 5: C-axis fabrics in single-scale deformation with varying  $W_k$  from pure shearing to 563 simple shearing and for models-A-C. The final strain intensity is between  $\rho = 2$  and 6. The pole 564 densities are contoured in multiples of uniform distribution. 565 566 Figure 6: Same as Figure 5 but for models-D-F. 567 568 **Figure 7**: C-axis fabrics in selected quartz RDEs in an isotropic HEM under simple shearing ( $W_k$ 569 570 =1). (a)-(o) are the resultant c-axis fabrics developed. The first column presents the initial conditions for the RDEs [ r : viscosity ratio of the RDE to HEM, initial shape defined by semi-571 axes of the RDE ( $a_1 : a_2 : a_3$ , where  $a_1 \ge a_2 \ge a_3$ ), and initial orientation given by spherical angles 572  $(\theta_1, \Phi_1, \theta_2)$  for general RDEs or  $(\theta, \Phi)$  for spheroidal RDEs]. Each row presents the results for 573 the RDE as the macroscale strain increases. 574 575 576 Figure 8: Same as Figure 7 except that the macroscale flow is plane strain general shearing  $(0 < W_k < 1).$ 577 578 Figure 9: C-axis fabrics in selected quartz RDEs in a HEM with planar anisotropy under simple 579

shearing flow  $(W_k = 1)$  (a)-(o) are the resultant c-axis fabrics developed. The first column presents

the initial conditions for the RDEs [ $r_{eff}$ - viscosity ratio of the RDE to HEM's  $\eta_n$ , initial shape defined by semi-axes of the RDE ( $a_1 : a_2 : a_3$ , where  $a_1 \ge a_2 \ge a_3$ ), initial orientation given by spherical angles ( $\theta_1$ ,  $\Phi_1$ ,  $\theta_2$ ) for general RDEs or ( $\theta$ ,  $\Phi$ ) for spheroidal RDEs, and anisotropic strength m]. Each row presents the results for the RDE as the macroscale strain increases.

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**Figure 10:** Sketch of the thin-section sample showing c-axis fabric variation in quartz domains (based on Kilian et al., 2011, Fig. 9 there). C-axis fabrics comprise of peripheral c-axis maxima that are antithetically-inclined (yellow), nearly normal (blue), and synthetically-inclined (red) to the shear plane. The sense of shear is dextral. The arrow at the top-left shows the direction of increase in strain gradient.

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Figure 11: Plot of dot product  $\widehat{\omega} \cdot \widehat{\Omega}$  with increasing macroscale strain  $\rho$ , for 50 RDEs with random initial shapes and orientations, r = 0.5, 2 and 5(rows) and  $W_k = 1$  and .75 (columns).  $\widehat{\omega}$ and  $\widehat{\Omega}$  are, respectively, the unit vectors parallel to the microscale vorticity vector in an RDE and the macroscale vorticity vector.  $\widehat{\omega} \cdot \widehat{\Omega}$  is close to unity for the RDEs. Therefore, the microscale vorticity vectors are always of the same sense as and nearly parallel to the macroscale vorticity vector.

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599 Table 1: Quartz slip systems and the relative CRSS values for different models used in VPSC600 simulation.

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Figure 1.



Figure 2.









Figure 3.



Figure 4.



Figure 5.



Figure 6.



Figure 7.



Figure 8.



Figure 9.



Figure 10.



Figure 11.

 $W_k = 1$ 

W<sub>k</sub>=0.75









3 ρ 4

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1

0.97



Glin Cartana	CRSS ratio					
Shp Systems	Model A	Model B	Model C	Model D	Model E	Model F
Basal <a> {0001} &lt; 1210 &gt;</a>	1	3	3	3	3	3
Rhomb <a> {1011} &lt; 1210 &gt;</a>	5	5	1	1	5	3
Prismatic <a> {1010} &lt; 1210 &gt;</a>	5	1	3	1	5	1
Prismatic <c> {1010} &lt; 0001 &gt;</c>	10	10	10	10	1	1
Approximate Temperature Range	350-500°C	500-600 °C	500-600 °C	500-600 °C	650 °C	650°C