

Estuarine Circulation, Mixing, and Residence Times in the Salish Sea

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Abstract

A realistic numerical model is used to study the circulation and mixing of the Salish Sea, a large, complex estuarine system on the United States and Canadian west coast. The Salish Sea is highly productive and supports many important fisheries but is threatened by recurrent hypoxia and ocean acidification, so a clear understanding of its circulation patterns and residence times is of value. The estuarine exchange flow is quantified at 39 sections over three years (2017-2019) using the Total Exchange Flow method. Vertical mixing in the 37 segments between sections is quantified as opposing vertical transports: the efflux and reflux. Efflux refers the rate at which deep, landward-flowing water is mixed up to become part of the shallow, seaward-flowing layer. Similarly, reflux refers to the rate at which upper layer water is mixed down to form part of the landward inflow. These horizontal and vertical transports are used to create a box model to explore residence times in a number of different sub-volumes, seasons, and years. Residence times from the box model are generally found to be longer than those based on simpler calculations of flushing time. The longer residence times are partly due to reflux, and partly due to incomplete tracer homogenization in sub-volumes. The methods presented here are broadly applicable to other estuaries.

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Key Points:

- The estuarine circulation throughout the Salish Sea is estimated over three years from a realistic numerical model, focusing on the exchange flow.
- The vertical mixing, or “reflux” is stronger at sills, but is also large when integrated over the basins between sills.
- Residence time is calculated in three ways, quantifying the extent to which it is increased (often more than doubled) by reflux and incomplete homogenization within a volume.

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26 complex estuarine system on the United States and Canadian west coast. The Salish Sea is
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38 partly due to incomplete tracer homogenization in sub-volumes. The methods presented here are
39 broadly applicable to other estuaries.

40 Plain Language Summary

41 The Salish Sea is a large estuarine system that includes the cities of Vancouver on the Strait of
42 Georgia and Seattle on Puget Sound. Despite the many rivers flowing into the Salish Sea, the
43 water in the system is mostly ocean water, and there is rapid exchange with the ocean. This
44 exchange is important because it brings in most of the nutrients that feed the ecosystem, and it
45 flushes the system relatively rapidly, leading to generally good water quality. Nonetheless, there
46 are places and times in the Salish Sea that experience problems like hypoxia and fish kills. The
47 goal of this work is to clearly describe the patterns of circulation and mixing throughout the
48 Salish Sea so that we may understand the causes and potential future changes in these water
49 quality problems. We use a realistic computer simulation, tested against many observations, to
50 predict the circulation and mixing patterns. We then use those currents to estimate residence
51 times in different parts of the Salish Sea for different seasons and years. The most important
52 result is that we find that the mixing of surface water with deep water can distribute water
53 properties throughout the Salish Sea, increasing the residence time.

54 **1 Introduction**

55 The exchange flow is widely recognized as a defining property of tidally averaged estuarine
56 circulation. The persistent inflow of deep, salty water and outflow of shallow, somewhat fresher
57 water is often many times greater in volume flux than all the rivers entering a system. As a result,
58 the exchange flow controls residence times and biogeochemical gradients. Physically this
59 circulation is a result of the density contrast between ocean and river water, combined with
60 mixing and advection from tidal currents (Geyer & MacCready, 2014; MacCready & Geyer,
61 2010). The theory of estuarine exchange flow was developed and tested for shallow, straight
62 coastal plain estuaries such as the Hudson (Hansen & Rattray, 1965; Ralston et al., 2008) but is
63 less well-developed for more complex systems. In this paper we focus on the circulation of one
64 of these complex systems - the Salish Sea, a large, interconnected system of very deep basins and
65 shallow straits forced by strong tides and many rivers. Despite the extreme bathymetric
66 irregularity of the Salish Sea, it develops a vigorous exchange flow (Bretschneider et al., 1985;
67 Geyer & Cannon, 1982; D. A. Sutherland et al., 2011; Richard E. Thomson et al., 2007). The
68 deep inflow and shallow outflow through the mouth of the system average around $140,000 \text{ m}^3 \text{ s}^{-1}$,
69 about 70% of the flow of the Amazon River. This is one of the largest exchange flows on the
70 planet, although it is only about $1/7^{\text{th}}$ the magnitude of the inverse estuarine circulation of the
71 Mediterranean Sea (Pinardi et al., 2019).

72 A key insight of early researchers was that the Salish Sea may be thought of as a system of large,
73 relatively quiescent basins, joined by straits with strong tidal currents and mixing (Ebbesmeyer
74 & Barnes, 1980). The mixing at straits causes “reflux” in which a significant amount, perhaps
75 up to half (Ebbesmeyer et al., 1988) of the outflowing branch of the exchange flow is mixed
76 down and becomes part of the inflowing branch of the exchange flow. The implications for
77 residence time were recognized immediately: refluxing could mean that it takes much longer for
78 the system to flush out conservative tracers. The mathematical framework for reflux was
79 developed rigorously by Cokelet and Stewart (1985) calling it “efflux/reflux” (efflux is the water
80 mixed up which then heads seaward; reflux is the water mixed down which then heads
81 landward). In the present work we use three years of a realistic numerical simulation and new
82 analytical tools to calculate the size and consequences of exchange and reflux in the Salish Sea.

83 A history of circulation studies in the region is given in Section 2. The model setup and
84 evaluation against data are presented in Section 3, with more detail given in the Supplementary
85 text. The analysis of model fields to calculate the exchange flow and efflux/reflux throughout
86 the system is given in Section 4. A box model is constructed using these transports. Box model
87 results focusing on the residence time are given in Section 5. Further discussion is provided in
88 Section 6.

89 We find that the exchange flow varies smoothly along the system, increasing nearly linearly
90 from the landward bays to the seaward end at the Strait of Juan de Fuca (Fig. 1), consistent with
91 findings in D. A. Sutherland et al. (2011). This finding is not consistent with the exchange flow
92 being interrupted at the sills as hypothesized in Ebbesmeyer and Barnes (1980). This smooth
93 variation we find is often seen in coastal plain estuaries, but is perhaps not expected in a place
94 like the Salish Sea where mixing is tightly concentrated at a few energetic sills (Ebbesmeyer et
95 al., 1988; Gregg & Pratt, 2010; Seim & Gregg, 1994). Use of the Total Exchange Flow method
96 (MacCready, 2011) is required for correct estimation of the exchange flow in places where the
97 salt flux is significantly influenced by tidal correlation of salinity and transport. We also find
98 that the vertical efflux/reflux transports, while strongest at sills, are also important throughout the
99 basins when considered as an area integral. The box model is used to calculate the movement of
100 passive tracers in the Salish Sea in different years and seasons. From it we find that residence
101 times which account for reflux, and for incomplete homogenization within basins, may be two or
102 more times longer than standard flushing times.

103 **2 A brief history of studies of Salish Sea Circulation**

104 The pattern and variability of circulation, mixing, and water properties in the Salish Sea has been
105 the subject of many studies in the past seven decades. The overall conclusion is that the system
106 functions like an estuary, with strong, localized mixing and a very large exchange flow despite
107 the fjord-like, glacier-carved basins. Early data on water properties in Puget Sound was
108 collected in 1952-1966 and presented in hand-contoured plots in Collias et al. (1974). Similarly,
109 Crean and Ages (1971) present observations from twelve cruises in 1968 in the Straits of
110 Georgia and Juan de Fuca (see Fig. 1 for place names). Early studies of Juan de Fuca prompted
111 its inclusion as an extreme end member in the famous Hansen and Rattray (1965) paper on the
112 physics of the estuarine exchange flow.

113 Spurred by concerns over the fate of contaminants in the system and the causes of hypoxia,
114 observational studies accelerated greatly in the 1970's. Early Canadian research is reviewed in
115 LeBlond (1983), highlighting important current meter observations of the average exchange flow
116 in Juan de Fuca and Johnstone Strait (the channel at the northern end of Strait of Georgia that
117 connects to the Pacific). On the U.S. side of the international border the National Oceanic and
118 Atmospheric Administration (NOAA) initiated the MESA (Marine Ecosystems Analysis) Puget
119 Sound Program, with results reviewed in Ebbesmeyer et al. (1988) and many NOAA reports.
120 Simultaneously, large advances were made in understanding the complex pattern of tides
121 (Lavelle et al., 1988; Mofjeld & Larsen, 1984) that are the dominant factor governing currents
122 and mixing in the Salish Sea. While Puget Sound has been the subject of a great deal of study, it
123 only comprises about 8% of the nearly 2000 km³ volume of the Salish Sea.

124 In the four decades since 1980 there have been many observational studies of the Salish Sea
125 ecosystem and circulation. Notable additions to our knowledge have come from the
126 accumulation of long time series from sustained observational programs such as the extensive
127 seasonal surveys conducted by the Canadian Institute of Ocean Sciences (Masson & Peña, 2009),
128 and the Washington (WA) State Dept. of Ecology monthly CTD stations initiated around 1990.
129 Long term change and interannual variability are summarized in Riche et al. (2014) where the
130 gradual warming of the system, and other changes, are made apparent.

131 Evolving with, and somewhat lagging behind the observational advances, modeling has emerged
132 as a useful scientific tool for Salish Sea studies. The fact that accurate 3-D models of the system
133 only arrived in the last decade is due to the extreme bathymetric complexity of the Salish Sea.
134 This complexity prompted the early creation of simpler models that could be used to predict
135 high-value quantities such as residence time. These typically divide the region into a number of
136 segments horizontally and two layers vertically. Cokelet et al. (1991) developed such a model for
137 Puget Sound, exploiting the Knudsen (1900) relations to diagnose the exchange flow from
138 known river flow and salinity distributions; see Burchard et al. (2018) for a translation of
139 Knudsen's paper. A similar approach, allowing for time-dependence, is presented in Hagy et al.
140 (2000) for a tributary of the Chesapeake. Li et al. (1999) used a more dynamical approach in a
141 box model of the Strait of Georgia – Juan de Fuca system, incorporating a physical
142 parameterization of exchange as a function of along channel density gradients. Babson et al.
143 (2006) used a similar dynamical approach in a box model of Puget Sound. A novel two-tracer

144 approach to diagnosing the exchange flow and mixing, applied to parts of the Salish Sea, is
145 presented in R. Pawlowicz (2001).

146 Realistic models of the Salish Sea were also attempted in past decades but were significantly
147 hampered by lack of computing power. Modern, realistic models of the Salish Sea only
148 appeared in the last decade (Khangaonkar et al., 2017; Khangaonkar et al., 2011; Moore et al.,
149 2015; Olson et al., 2020; Peña et al., 2016; Soontiens et al., 2015; D. A. Sutherland et al., 2011).
150 The present model continues this realistic numerical approach.

151 **3 Model Setup and Evaluation**

152 The realistic numerical model used here is created using the Regional Ocean Modeling System
153 (ROMS) (Haidvogel et al., 2000; Shchepetkin & McWilliams, 2005) which integrates the
154 Reynolds averaged, Boussinesq, incompressible equations of motion and tracer concentration on
155 a rotating, spherical grid. The model configuration used here is called LiveOcean. The model
156 domain covers all of Oregon, Washington, and Vancouver Island coastal waters, and the Salish
157 Sea – the name for the combined inland waters of Puget Sound, Strait of Georgia, and the Strait
158 of Juan de Fuca (Fig. 1). The model grid follows lines of constant longitude and latitude, with
159 500 m spacing in most of the Salish Sea and Washington coastal estuaries, stretching up to 3 km
160 at open boundaries. There are 30 vertical levels, following the bathymetry and free surface. The
161 model is configured to be as realistic as possible, with 45 rivers, 8 tidal constituents, open ocean
162 conditions from a global data-assimilative model, and high-resolution atmospheric forcing from
163 a regional weather forecast model. The model builds upon prior realistic configurations focused
164 inside of the Salish Sea (D. A. Sutherland et al., 2011) and on the open coast (Giddings et al.,
165 2014). Details of the model setup are given in Supplementary Text S1. The model run analyzed
166 here was initialized December 15, 2016 and runs through the present because it makes quasi-
167 operational daily forecasts. Here we work only with the three-year period 2017-2019. During
168 2019 the Salish Sea experienced low river flows (Fig. 1c) causing the system to grow
169 progressively saltier.

170 The three-year model hindcast has been extensively compared to observations. A summary of
171 those comparisons is presented in Supplementary Text S2. Focusing on one aspect of the
172 evaluation most relevant to the exchange flow, along-channel sections of the salinity for 2017 are

173 plotted in Fig. 2. Here we use the cast data averaged over the upper and lower parts of the water
174 column at CTD stations to test the model skill at reproducing the along-channel salinity gradient
175 and stratification. The along-channel salinity gradient is thought to provide the driving pressure
176 gradient for the estuarine exchange flow (Giddings & MacCready, 2017; MacCready & Geyer,
177 2010) and the size of the exchange flow as estimated from Knudsen's Relations depends
178 critically on the stratification. Evaluating these for the three Puget Sound along-channel sections
179 shown in Fig. 2 we find that the model salinity gradient is somewhat too weak, being 78-85% of
180 that observed. The model stratification is 64-116% of that observed, with the lower value
181 representative of model performance in Hood Canal. The stratification results are most easily
182 related to the exchange flow because the Knudsen's Relations state that the exchange flow is
183 inversely proportional to the stratification (Burchard et al., 2018), so this range suggests our
184 exchange transports may be overestimated by as much as 56% or underestimated by as much as
185 14%. As mentioned in Supplementary Text S2, there was a significant temporal increase of
186 salinity in the Salish Sea: 0.68 g kg^{-1} over three years estimated from CTD data. Comparing to
187 these data, the salinity bias of the model for stations inside Puget Sound stayed roughly the same
188 in each year (0.62, 0.60, 0.53) implying that the modeled salinity drift was capturing a real trend,
189 and not a spurious model artifact.

190 **4 Calculation of the Exchange Flow and Mixing**

191 The analysis of modeled circulation in the Salish Sea is done in three steps. Our focus will be on
192 subtidal and longer timescales, and on how the exchange flow and mixing affect residence times
193 and tracer concentrations in general. In the first step we calculate the tidally averaged exchange
194 flow, following methods described in MacCready (2011), through many sections (Fig. 3).
195 Second, we make seasonal and annual averages of the two-layer exchange flow and use these to
196 calculate vertical mixing rates throughout the system. Finally, we use the overall pattern of
197 horizontal transports (the exchange flow) and vertical transports (mixing) to construct an
198 efficient box model of the Salish Sea. The box model is used to explore residence times in

199 different years and seasons. The box model is also used to calculate the concentration and age of
200 a tracer injected from various sources such as a river.

201 4.1 The Total Exchange Flow

202 The exchange flow is calculated at 39 cross-sections throughout the Salish Sea (Fig. 3). At each
203 section we extract hourly snapshots of section-normal transport and salinity in each grid cell.

204 The sections are aligned with the model grid and located on velocity points of the ROMS C-grid,
205 e.g. for a N-S section such as *jdf1* the cross section is on the model u-grid. Keeping the sections
206 on the model grid minimizes interpolation errors (MacCready, 2011). The three-year average
207 error in the system-wide volume budget is 0.42% of the average net river flow, and the error in
208 the salt budget is 0.016% of the average salt flux of the inward exchange flow. The largest error
209 found was 2.44% for the Hood Canal 2018 volume budget. For any budget calculations it is
210 essential that volume be conserved as well as possible since any errors in volume transport will
211 propagate through all tracer transport calculations. Comparing the error to mean river flow in a
212 basin, as we do here, is a conservative approach because typically the exchange flow transports
213 are an order of magnitude larger.

214 The exchange flow is calculated at each section using the Total Exchange Flow (TEF) method
215 (MacCready, 2011). Here transport is sorted into salinity classes, tidally averaged and then the
216 sum of the transport in all inward flowing salinity classes is called Q_{in} . The flux-weighted
217 salinity of the inflow is S_{in} . Similarly, the outflow is quantified as Q_{out} and S_{out} . The sign
218 convention is that Q_{out} is negative. These TEF variables thus consist of four tidally averaged
219 time series at each section. The reason for using salinity classes is that it accounts for tidal
220 variation in the spatial structure of the salt flux (MacCready, 2011). The TEF variables give the
221 total inward and outward salt flux through a section as $Q_{in}S_{in} + Q_{out}S_{out}$ regardless of whether the
222 salt flux was due to steady exchange flow or tidal pumping. TEF has been found to give a clear
223 representation of the exchange flow in many systems (Burchard et al., 2018; Chen et al., 2012;
224 Conroy et al., 2020; Geyer & MacCready, 2014; Lorenz et al., 2020; Rayson et al., 2017; D. A.
225 Sutherland et al., 2011). Using the TEF method is especially appropriate in the Salish Sea
226 because the system is known to have large basins with exchange organized by depth (deep saltier

227 inflow, shallow fresher outflow) punctuated by energetic sill like Tacoma Narrows where the
228 exchange is organized by time (saltier flood, fresher ebb).

229 We calculate transport in 1000 salinity bins and then integrate over these to form inflowing and
230 outflowing layers using the “dividing salinity” method (MacCready et al., 2018) which has been
231 shown to give reliable results even for nearly well-mixed cases (Lorenz et al., 2019). We allow
232 for the existence of more than two layers in calculating our initial layer averages (Lorenz et al.,
233 2019), but then combine these into just two layers, conserving net salt flux in either direction.
234 An example of the results is plotted as time series for section *ai3* in Fig. 4. At this section there
235 is a clear annual cycle of the salinity of the two layers, growing saltier and with less salinity
236 difference between in- and outflow in the late fall when river flows have been low for some
237 months. The daily values show evidence of increased salinity of the inflow during weak neap
238 tides (Fig. 4a), consistent with the observations of Geyer and Cannon (1982). The exchange
239 flow transport (Fig. 4b) also shows annual and fortnightly variation. The dynamics controlling
240 these is of great importance but will not be addressed in this paper because we are focusing
241 instead on describing the circulation and its implications for residence time. About half of the
242 sections could be characterized as having more than two layers at times, and this is an important
243 caveat on our subsequent calculations using transports that have been expressed somewhat
244 artificially as two layers. A more nuanced approach allowing three or four layers is presented in
245 Rich Pawlowicz et al. (2007) for the Strait of Georgia. We proceed by assuming that a two-layer
246 estuarine circulation is adequate for understanding the broad patterns of circulation in the Salish
247 Sea, but caution that the details of stratification and water residence time in a given basin are best
248 handled by calculations using a realistic model, albeit at substantially greater computing cost.

249 The two-layer transports for all sections averaged over 2017 are plotted in Fig. 5. In general, the
250 magnitude of the exchange flow transport increases steadily moving seaward. However, the
251 increase is not perfectly monotonic, e.g. between sections *tn2* and *tn3* at Tacoma Narrows (Fig.
252 5b). This is consistent with previous results (D. A. Sutherland et al., 2011) that also used the
253 TEF method. The results are inconsistent with the characterization of the Salish Sea circulation
254 presented in Ebbesmeyer and Barnes (1980) and Khangaonkar et al. (2017) which did not use the
255 TEF method. The places where our results differ most is at the sills, with the exchange flow in
256 Khangaonkar et al. (2017) at Admiralty Inlet being about half what we find, and that in Tacoma

257 Narrows being about one-tenth of what we find. This is not to say that the Khangaonkar et al.
258 (2017) model is incorrect; indeed it has circulation patterns and validation statistics that are
259 similar to what we present here. The difference is that the TEF method is required to correctly
260 quantify the exchange flow at energetic places like sills where salt flux due to tidal pumping may
261 be an important mechanism. This is because at sills there is local enhancement of tidal currents
262 and often distortions of the salinity field due to rough bathymetry that may lead to local tidal
263 correlation of salinity and transport (i.e. tidal pumping). The TEF method, by construction,
264 includes tidal pumping as part of the net advective flux. This distinction is important for our
265 understanding of the circulation of the Salish Sea. In Ebbesmeyer and Barnes (1980) the
266 circulation was described as a two layer flow that was interrupted at sills, with the seaward-
267 flowing surface layer being largely sent downward by refluxing at a sill, resulting in a conceptual
268 model in which the basins were much more isolated from each other than our calculations
269 suggest. Nonetheless, there is a lot of vertical mixing and refluxing of water at sills, but it does
270 not interrupt the horizontal exchange flow in the way envisioned by previous authors. We
271 explore this distinction further below. More TEF section results are given in the Supplementary
272 Text S3, showing patterns of tidal energy flux and net volume transport.

273 The TEF properties are a compact way to represent the system behavior. A three-year time
274 series of S_{in} and S_{out} for the Puget Sound sub-volume (with bounding sections at *ail* and *dp*) is
275 plotted in Fig. 6a. Also plotted is the volume-mean salinity over that time period, which
276 increases by about 0.7 g kg^{-1} while the salinity difference between inflow and outflow, $\Delta S \equiv$
277 $S_{in} - S_{out}$, decreases. The exchange flow over that time did not exhibit a clear multi-year trend
278 (Fig. 6b), although it does have a strong annual cycle, peaking in winter when the river flow
279 (Fig. 6d) is strong. The annual mean river flows entering Puget Sound were close to average in
280 2017, dropped a bit in 2018, and dropped by a third in 2019 (Fig. 6d). Similar budgets (not
281 shown) were formed for other sub-volumes of the Salish Sea, and for the complete system, and
282 in all cases the salinities had a sensible relationship to the net river flow: during times of low
283 flow like the late summer or 2019 the salinity was increasing and ΔS was decreasing. The
284 exchange flow, in contrast, was much harder to explain. There was no consistent phasing
285 between exchange flow and net river flow, nor was there an interannual trend. This may
286 represent the unusual plumbing of the system. Taking the Puget Sound volume (Fig. 6) as an
287 example, the biggest freshwater source in the Salish Sea is seaward of Puget Sound and peaks

288 some months later than Puget Sound Rivers (Fig. 1). The exchange flow may also be influenced
 289 by the density of water upwelled on the coast during spring and summer (Babson et al., 2006),
 290 the seasonal variation of wind (D. A. Sutherland et al., 2011), and tides (Deppe et al., 2018).

291 A complete salt budget may be formed from the TEF quantities, and the terms may be expressed
 292 most clearly by defining an exchange flow transport Q_e as the average of Q_{in} and $-Q_{out}$ (recall
 293 Q_{out} is defined as negative). We also define an average salinity of the exchange as \bar{S} , and the net
 294 river flow entering a volume as Q_R (defined as positive).

$$295 \quad Q_e \equiv \frac{(Q_{in} - Q_{out})}{2} \quad (1)$$

$$296 \quad \bar{S} \equiv \frac{(S_{in} + S_{out})}{2} \quad (2)$$

297 Then the tidally averaged, volume-integrated salt budget may be written in two ways:

$$298 \quad \frac{d}{dt} \int S \, dV = Q_{in}S_{in} + Q_{out}S_{out} \quad (3)$$

$$299 \quad \frac{d}{dt} \int S \, dV = -Q_R\bar{S} + Q_e\Delta S \quad (4)$$

300 The terms on the right-hand side of (4) are the TEF equivalent of the classic estuarine salt
 301 budget, e.g. Eqn. 10 in MacCready and Geyer (2010), but without the need for a tidal pumping
 302 term. Physically, the net river flow removes salt, and the exchange flow brings salt in. The
 303 terms in (4) are plotted in Fig. 6c. The gradual decrease of the exchange term, $Q_e\Delta S$, over time
 304 is driven by the decrease in stratification, ΔS , but this was more than matched by the decreasing
 305 magnitude of the river term, leading to the increase of mean salinity.

306 4.2 Efflux-Reflux Fractions and a Box Model

307 From the time-mean TEF two-layer transports and salinities we may also determine the net
 308 vertical mixing in any segment between TEF sections. The method was first developed in
 309 Cokelet and Stewart (1985) and was applied to Puget Sound in a series of NOAA reports and one
 310 conference paper (Cokelet et al., 1991). What the efflux-reflux formalism does is to split the

311 turbulent transport into independent upward and downward components. The advantage of
312 doing so is that it expresses the vertical fluxes as volume transports, making them the vertical
313 equivalent of the horizontal TEF fluxes. The advantage of using the TEF transports is that they
314 are the complete terms which allow (3) to be satisfied, in the same way that they satisfy the
315 Knudsen's relations (Burchard et al., 2018; MacCready, 2011), without the need for fluxes due to
316 tidal pumping, which may not be separated by layer. The existence of realistic numerical
317 simulations, as used here, and the TEF calculation method, represent the main advances in the
318 tools we may use with the efflux-reflux theory. The fact that these tools were not available to
319 Cokelet and Stewart (1985) motivates our effort here to revisit Salish Sea circulation and mixing.

320 Here we extend their method to the entire Salish Sea for multiple years and seasons and use it to
321 construct an efficient box model to calculate residence times for different basins, seasons, and
322 definitions of the residence time (see below). In its simplest form the efflux-reflux theory can be
323 applied to a single channel segment between two sections with no river input (Fig. 7a). The
324 segment is assumed to have two layers and known, steady, volume and salt transports through
325 the open sections on either side. Because of the complexity of applying this to many segments in
326 a complex geometry like the Salish Sea we define a local notation in which all transports are
327 positive, inflows are lower case (q or f) and outflows upper case (Q or F). In standard TEF
328 notation q would be Q_{in} , and f would be $Q_{in}S_{in}$, the inward salt flux. The efflux-reflux theory
329 determines what fraction of the deep (saltier) flow entering the segment must be mixed or
330 advected into the upper (fresher) flow leaving the segment, and this is called "efflux". Likewise,
331 the theory determines what fraction of the fresher flow entering the segment must be mixed or
332 advected down into the saltier flow leaving the segment. The fraction is called "reflux" because
333 in a typical estuarine channel it represents seaward-flowing surface water being mixed down and
334 pulled back landward. The importance of reflux is that it can retain tracers in the system,
335 increasing residence time. The theory determines the efflux-reflux fractions under the dual

336 constraints of volume and salt conservation, as detailed in Cokelet and Stewart (1985). The
 337 system of equations to be solved for the segment shown in Fig. 7a are, in matrix form:

$$338 \quad \begin{bmatrix} q_0 & q_1 & 0 & 0 \\ f_0 & f_1 & 0 & 0 \\ 0 & 0 & q_0 & q_1 \\ 0 & 0 & f_0 & f_1 \end{bmatrix} \begin{bmatrix} a_{00} \\ a_{10} \\ a_{01} \\ a_{11} \end{bmatrix} = \begin{bmatrix} Q_0 \\ F_0 \\ Q_1 \\ F_1 \end{bmatrix} \quad (5)$$

339 The four unknown coefficients, $a_{from,to}$, are then determined by standard matrix techniques. The
 340 existence of a solution requires that volume and salt be conserved, e.g. for salt flux:

$$341 \quad f_0 + f_1 = F_0 + F_1 \quad (6)$$

342 And the fractions must be positive and sum to 1, e.g. $a_{00} + a_{01} = 1$. The efflux and reflux could
 343 also be expressed in more familiar form as the sum of vertical advective transport and vertical
 344 turbulent transport. Vertical turbulent transport is physically caused by the net effect of upward
 345 and downward advection of water parcels, and in the formalism used here we keep track of up
 346 and down transports separately.

347 As pointed out at great length by Cokelet and Stewart (1985) there are many real-world
 348 complications to applying the theory to complex systems such as the Salish Sea. Chief among
 349 these is that for segments with rivers (e.g. W4) or with more than two bounding sections (e.g. J4)
 350 the resulting system of equations is underdetermined. For these cases we take a pragmatic,
 351 numerical approach, making many guesses for some of the a 's and then using the average of all
 352 physically possible solutions. In the rare cases with no solutions we impose a typical value of
 353 0.1 to the reflux coefficients (a_{00} , a_{11} , and so on). In one segment, A1, we adjusted the reflux
 354 fractions by hand to achieve a better result. To ensure exact volume and salt conservation we
 355 make very small adjustments (at most 0.5% and usually much smaller) to the fluxes bounding
 356 each segment before calculating the fractions. The lack of perfect conservation is due in part to
 357 the fact that the volume and salt budgets are not exact, as discussed above. In addition, the net
 358 salt in a segment may be changing over time, and this unsteadiness is neglected because it is

359 small compared to the other fluxes. Nonetheless we capture some aspects of temporal variability
 360 by calculating the efflux-reflux fractions over different years and seasons.

361 We then use the TEF transports and efflux-reflux fractions to create a box model for arbitrary
 362 tracers, as shown schematically in Fig. 7b. Each segment is composed of two volumes, with the
 363 upper (fresher) volume being 20% of the total in a given segment – an approximation of the
 364 observed structure of the Salish Sea. The residence time results presented below are not
 365 particularly sensitive to this choice, varying by only $\pm 7\%$ when the upper volume was 10% or
 366 30% of the total in a segment. The concentration of an arbitrary tracer in each volume is given
 367 by C , which can be time-dependent even though the circulation is steady. We take all the
 368 “reflux” parts of the efflux-reflux calculation and use them to determine upward and downward
 369 transports vertically between fresher and saltier volumes in a segment. Following the arrows and
 370 notation in Fig. 7b, the equation for tracer concentration in the fresher volume of the segment is:

$$371 \quad \frac{dC_f^{ii}}{dt} = C_f^{iii} q_i + C_s^{ii} q_0 a_{00} - C_f^{ii} (Q_0 + q_1 a_{11}) \quad (7)$$

372 In segments with more than two surrounding sections the vertical transports are formed by the
 373 sum of all the reflux terms. An example of the resulting upward and downward transports for the
 374 full year 2017 is plotted in Fig. 8. If they are equal in magnitude that means that there is vertical
 375 mixing but no mean vertical flow in a segment. In general, in Fig. 8 it is apparent that upward
 376 fluxes are usually larger than downward, implying that the mean transport is upward, consistent
 377 with conceptual sketches of estuarine circulation as in MacCready and Geyer (2010) (their Fig.
 378 1a). The net up and down transports in each channel are given as text in Fig. 8. Notably, the net
 379 upward flow is generally larger than the exchange flow at the seaward end of a channel (see Fig.
 380 5) because it must accommodate both the transformation of inflow to outflow and the vertical
 381 mixing. Numerically, the box model integrates 37×2 equations such as (7) using forward time-
 382 stepping and a time step of one hour (chosen for numerical stability). Had we plotted the
 383 transports as vertical velocities (i.e. dividing by the horizontal area of each segment) the sills

384 would show the largest values, but the area integrals in Fig. 8 demonstrate that mixing in basins
385 cannot be neglected.

386 The resulting box model of the Salish Sea can be tested by seeing how well it reproduces the
387 TEF salinities when the boundary conditions are $C = 0$ for all the rivers and $C = S_{in}$ at the two
388 open ocean boundaries. Results of this test for the full year 2017 are plotted in Fig. 9. Overall
389 the box model does a reasonable job of reproducing the along-channel gradient and stratification
390 ($S_{in} - S_{out}$) throughout the system. The model results are biased high in the three channels of
391 Puget Sound, however, and the model underestimates the stratification in Whidbey Basin.
392 Experiments with the box model in an idealized estuary (not shown) suggest that some of the
393 error may be due to the relatively coarse spatial resolution of the boxes. It is also possible that
394 different choices of efflux-reflux fractions in specific segments might improve the model. With
395 its imperfections in mind, we take the box model to be good enough for our purposes of
396 exploring residence times and other properties.

397 We perform two types of experiments with the box model. In the first, we introduce a steady
398 input of tracer with concentration $C = 1$ at a selected river or rivers. We call these “source
399 experiments.” The integration is run out to equilibrium (6 years – empirically found to be long
400 enough) and a result consists of the steady-state tracer concentration in each segment, both upper
401 and lower sub-volumes. We also run a tracer with the same boundary conditions but which
402 grows at a known rate, and use the ratio of the two tracers to estimate the “age” of the tracer
403 since it was introduced (e.g. from a river), as discussed for example in Rayson et al. (2016).

404 In the second type of experiment the tracer is introduced as an initial condition with $C = 1$ in a
405 volume V composed of selected segments. We will call these “initial condition experiments.”
406 We present results from experiments of this type in seven different basins of the Salish Sea and
407 for different time periods.

408 The concept of residence time has been used in many different ways as discussed for example in
409 Monsen et al. (2002), Delhez et al. (2004) and Lemagie and Lerczak (2015). Usually the
410 motivating question is water quality, e.g. hypoxia, and the time water spends in a region is just
411 one of several driving factors. Residence time is also greatly influenced by how it is defined.
412 Here we adopt the definition that the residence time, T_{res} , is defined through an initial condition

413 experiment: (i) we choose a volume to focus on – e.g. all the water in Puget Sound, (ii) we
 414 introduce a conservative tracer with concentration $C = 1$ in that volume at some time, and $C = 0$
 415 elsewhere, (iii) we allow advection and mixing to move the tracer around, and then (iv) calculate
 416 T_{res} as the time after the start when the integrated tracer concentration in the volume drops to $1/e$
 417 or about 37% of its original value. We recognize that formally “residence time” is defined for
 418 each water parcel (Monsen et al., 2002) and so is a function of space and time. Our T_{res} amounts
 419 to an average that describes the behavior of a collection of water parcels, and is analogous to
 420 what has variously been called the system residence time, turnover time, or particle tracking
 421 timescale.

422 For most of our experiments T_{res} is influenced by reflux: some of the water expelled from a
 423 channel by the outgoing branch of the exchange flow may be mixed down outside of the volume
 424 under consideration and be returned to the volume by the incoming branch of the exchange flow.
 425 The box model described above is an efficient platform for doing such calculations, taking just
 426 seconds for a 6-year integration. We may also define an alternate exchange flow, T_{resNX} , which
 427 is the “residence time without reflux.” It is also calculated from initial condition experiments,
 428 but with different rules: instead of allowing the tracer to freely flow and reflux throughout the
 429 system, we set $C = 0$ at all times outside of the volume in which the tracer was initialized. A
 430 third, and much more common, way to calculate a timescale is as the “flushing time,” defined as
 431 $T_{flush} = V/Q$ where V is the size of the volume being considered and Q is the water flux through
 432 the volume. In our case we take Q to be the sum of all the $-Q_{out}$, which is equivalent to the sum
 433 of all the Q_{in} and the river flows. If the tracer is continuously homogenized within a volume,
 434 then it is straightforward to prove that $T_{flush} = T_{resNX}$. However, in general the tracer is not
 435 homogenized – some segments of the volume are flushed faster than others, and this lack of
 436 homogeneity generally causes $T_{flush} < T_{resNX}$. By calculating all three timescales from our box
 437 model experiments we may quantify the relative importance of reflux and lack of
 438 homogenization which lead to T_{res} being greater than T_{flush} .

439 We computed TEF transports and vertical efflux-reflux transports for all segments for 15 cases:
 440 averages over each of the three years 2017-2019, and the four seasons in each year, defined as
 441 averages over three months in a given year: winter = JFM, spring = AMJ, summer = JAS, fall =
 442 OND. The transports used in the box model in each case are steady, the result of averaging the

443 full time-varying transports over the time interval in question. When the box model is run for a
444 given case it is different from the real system in the sense that a given circulation pattern and
445 river flow are maintained for much longer than three months or a year, so one can think of the
446 experiments as answering the hypothetical question: what would the residence time be under
447 these conditions if they persisted?

448 **5 Results from the Box Model**

449 An example from a source experiment in which the source was all the rivers in the Salish Sea is
450 shown in Fig. 10, with forcing from 2017, a year with average river flow. Notable results are
451 that river water rarely makes up more than 15% of a sub-volume; and only 8% in the main basin
452 of Puget Sound. The age of the water is on the order of 200-300 days, longer in the Strait of
453 Georgia and shorter in Puget Sound. The age represents the combination of transport pathways
454 of many rivers, however, and may be greatly influenced by the system-wide spread of Fraser
455 River water (Banas et al., 2014). The surface concentrations are generally higher (more river
456 influence) and younger.

457 A snapshot from an initial condition experiment is shown in Fig. 11. Here the tracer was
458 initialized in all sub-volumes of South Sound, and then advected and mixed with transports from
459 winter 2019. This was the experiment that had the largest difference between T_{res} and T_{flush} , as
460 discussed below, but it also nicely illustrates the pathways by which a tracer is dispersed
461 throughout the Salish Sea on its way to eventually exiting to the Pacific. In particular, while
462 tracer heads seaward in surface layers, it is also mixed (refluxed) downward, and may thereby
463 drift into other basins, following the deep inflow. This is apparent in all of the channels in Fig.
464 11.

465 Residence times were calculated from initial condition experiments with dye initialized in 7
466 different basins (Fig. 12 and Table 1). Twelve experiments were done in each basin, comprised
467 of three years and four seasons in each year.

468 For the full Salish Sea (all of the segments in Fig. 3a) the average residence time is almost a year
469 and is shortest in summer when the circulation is most affected by the large pulse of freshwater
470 delivered by the Fraser River (Fig. 12). Residence times increased by about 50 days over the

471 three years studied, presumably a result of the weaker river flow in 2019. The flushing time is
 472 less than half the residence time, and the difference is due to lack of complete homogenization
 473 within the volume. The other possible explanation, reflux, cannot affect this case because the
 474 tracer leaving the box model does not come back so $T_{resNX} = T_{res}$ in this case (Fig. 12).

475 Turning to the Strait of Georgia, the residence times are somewhat higher while the flushing
 476 times are slightly lower. The longer residence times reflect the fact that deep Strait of Georgia
 477 takes a long time to lose its tracer due to its large volume. The effect of reflux is evident in that
 478 $T_{resNX} < T_{res}$. From this difference we may calculate the fractional effect of reflux:

$$479 \quad f_{reflux} = 100 * \frac{(T_{res} - T_{resNX})}{(T_{res} - T_{flush})} \quad (8)$$

480 For this case the average value is $f_{reflux} = 22\%$ (Table 1), meaning that omitting reflux
 481 decreases the residence time relative to the flushing time by 22%. From this we may conclude
 482 that most (78%) of the reason that $T_{res} > T_{flush}$ is the lack of complete homogenization of tracer
 483 in the volume. Physically, much of the tracer is sequestered in parts of the volume that are
 484 flushed slowly, while tracer close to the boundaries is flushed very rapidly.

485 The average flushing time in the Strait of Georgia volume is found to be 125 days. This may be
 486 compared to estimates made by Rich Pawlowicz et al. (2007). They used time series of
 487 observations over three years, exploiting the annual cycle of water properties and the phase lag
 488 of properties inside of the Strait of Georgia compared to those of the primary source water in the
 489 Strait of Juan de Fuca. Their analysis recognizes the lack of complete homogenization, but they
 490 make assumptions consistent with those of the flushing time given above, so their numbers are
 491 most directly comparable to our T_{flush} . They examine four layers, the largest of these is the
 492 “intermediate layer” (analogous to most of our deep layer) for which they report a flushing time
 493 of 160 days. A volume-weighted average of all their layers gives flushing times of 112 days in
 494 summer and 172-319 days in winter. The longer times in winter are due to the extreme range (1-
 495 3 years) that they give for the flushing time of the deepest water in the Strait of Georgia,
 496 although these are never realized because of summer deep renewal events. These bound our
 497 estimated average flushing time. Most striking however, is the fact that our mean residence time,
 498 379 days, is three times longer than our flushing time, and as discussed above, most of the cause
 499 for this increase is lack of homogenization in the volume. Rich Pawlowicz et al. (2007) also

500 estimate that ocean water spends about 1.7 years in the Strait of Georgia after accounting for the
501 substantial reflux in Haro Strait that returns outgoing surface waters back as deep waters. In
502 “source” experiments with our box model (not shown) we find ocean water ages of about 1.2
503 years in the Strait of Georgia. However, there are many different assumptions that go into the
504 two estimates, so they are not exactly comparable. For our results the 50% uncertainty reported
505 in Rich Pawlowicz et al. (2007) is probably a reasonable estimate as well.

506 Similar results are evident in Puget Sound and its basins. Previous median flushing times from
507 D. A. Sutherland et al. (2011) are given in Table 1. These are most directly comparable to the
508 T_{flush} presented here because they used a similar numerical model of the Salish Sea and the Total
509 Exchange Flow method of exchange calculations. The only conceptual difference was that D. A.
510 Sutherland et al. (2011) used the saltwater flushing time whereas we use the volume flushing
511 time; these are very similar for volumes that are mostly seawater. Our results are 14-23% shorter
512 than the previous estimates but display the same pattern among basins: Hood Canal has the
513 longest flushing times, and Whidbey Basin and South Sound are much shorter. As in the Strait
514 of Georgia, the residence times from our box model are markedly longer, being 2-3 or even up to
515 6 times as long as the flushing time. Again, most of the longer time is explained by lack of
516 homogenization within the volume, with only 13-37% explained by reflux (Table 1) in most
517 cases.

518 The exception is the Hood Canal Inner volume which has $f_{reflux} = 83\%$. This experiment
519 differed from the others in that we only initialized tracer in the deeper parts of each segment
520 (H3-H8 in this case). Thus, tracer could be lost rapidly in the no-reflux experiments when it
521 escaped to the upper layer through vertical mixing and advection (i.e. efflux). This result
522 suggests that for a non-conservative tracer which is reset in the upper layer, e.g. by
523 photosynthesis or air-sea gas exchange, the residence time may be closer to the flushing time.

524 **6 Summary and Discussion**

525 In this paper we have presented results from a three-year hindcast of a realistic numerical
526 simulation of the Salish Sea and adjoining coastal waters of the Northeast Pacific. The model is
527 forced with realistic tides, winds, atmospheric heat fluxes, open ocean conditions, and rivers.
528 Based on extensive validation the model is shown to perform well in reproducing observed

529 fields. The model velocity and salinity fields are then used to calculate the exchange flow from
530 hourly snapshots at many sections, using the Total Exchange Flow method. The exchange flow
531 is strongest at the open boundaries, especially the mouth of the Strait of Juan de Fuca, and is
532 amplified by a factor of 20 or more compared to the net river flow. The strength of the exchange
533 flow decreases gradually, and nearly monotonically, going landward. This implies that the many
534 basins of the Salish Sea are intrinsically connected to each other by this exchange flow.

535 The vertical mixing throughout the system was quantified using the efflux-reflux method of
536 Cokelet and Stewart (1985). In this formalism vertical mixing and advection are expressed as
537 opposing upward and downward volume fluxes, analogous to the horizontal TEF fluxes.
538 Notably the downward fluxes highlight the many places where the outward flowing surface layer
539 is refluxed into the landward-flowing deep layer, fundamentally shaping the tracer transport
540 pathways. Low river flow in 2019 resulted in a clear increase of salinity in Puget Sound, and a
541 decrease in stratification, but no obvious change to the exchange flow. Nevertheless, residence
542 times were longer in 2019 compared to 2017-8. A box model for tracer transport was developed
543 using these horizontal and vertical fluxes, with transports from four seasons in each of three
544 years. The box model allowed rapid calculation of residence times for a number of sub-volumes.
545 In general, it was found that the tracer-based residence time from the box model was often a
546 factor of two longer than the more traditional calculation of flushing time. The increase was due
547 in part to refluxing which brings tracer back into a volume, but in larger measure the increase
548 was due to the fact that tracer was not mixed uniformly throughout a volume. The fact that
549 timescales for water renewal could be a factor of 2-3 different depending on the method of
550 estimation used means we should be cautious in interpreting the “residence time.” Based on
551 results here we may conclude that the *relative* timescales among basins are reasonably well
552 determined by all methods, but the actual values of the timescales requires consideration of other
553 factors that may influence a specific tracer, as for example the effects on hypoxia of
554 photosynthesis, air-sea gas exchange, and water column and benthic rates of the remineralization
555 of sinking organic matter.

556 There are a number of limitations of the box model presented here that should be kept in mind.
557 It is only as accurate as the LiveOcean transports used to create it, and these are hard to validate
558 directly because of the relative lack of current meter data. There is uncertainty in the estimation

559 of reflux coefficients, and in the translation of those to the box model. The box model assumes
560 static forcing over a season and so cannot capture events like large pulses of river flow. Finally,
561 the number of segments chosen can influence the results. For example, the flushing times are
562 essentially like the no-reflux residence times in the limit of a single box instead of many
563 segments and two layers, and the results in Fig. 12 and Table 1 clearly show that adding more
564 boxes increases residence time by resolving regions with slower flushing. It is an open question
565 whether or not adding more segments would significantly increase the residence time further.
566 Pursuing this line of reason leads to the conclusion that detailed problems are better studied with
567 the full model, whereas the box model excels as a very fast tool for initial estimation and
568 understanding.

569 While this paper focuses largely on the economically and ecologically important Salish Sea, the
570 methods and results are applicable across all estuaries. The combined use of TEF with
571 efflux/reflux is a valuable approach likely to prove fruitful in other systems. Moreover, the
572 importance of considering efflux/reflux and incomplete tracer homogenization are expected to be
573 critical to understanding residence times in many estuaries.

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589 All code used in the analysis is available at <https://github.com/parkermac/LiveOcean.git>, in
 590 particular in the x_tef folder. Model input parameters are in the folder
 591 forcing/dot_in/cas6_v3_lo8b. The TEF section extractions and processed files required to run
 592 the box model are archived and freely available here (start with the README.txt in the folder
 593 after extraction):

594 https://pm2.blob.core.windows.net/pm-share/LO_TEF_data_2020_11.tar.gz.

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 596 (Davis et al., 2014) (Egbert & Erofeeva, 2002) (Emery & Thomson, 1998) (Feely et al., 2016)
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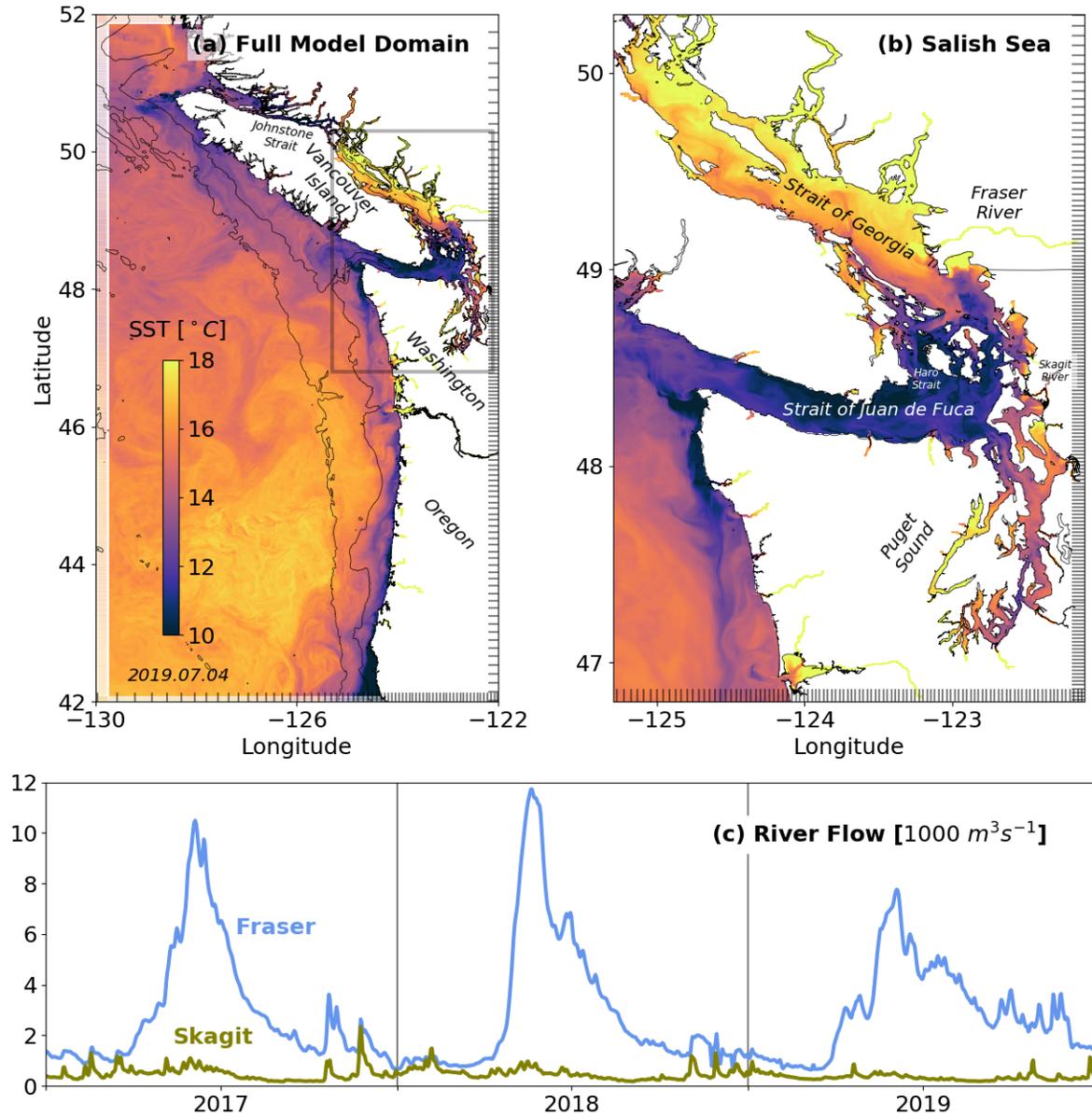
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813 Figure 1. LiveOcean model domain (a) colored by sea surface temperature for July 4, 2019.

814 Grid spacing is indicated with tick marks (only every 10th grid point is drawn). Region of

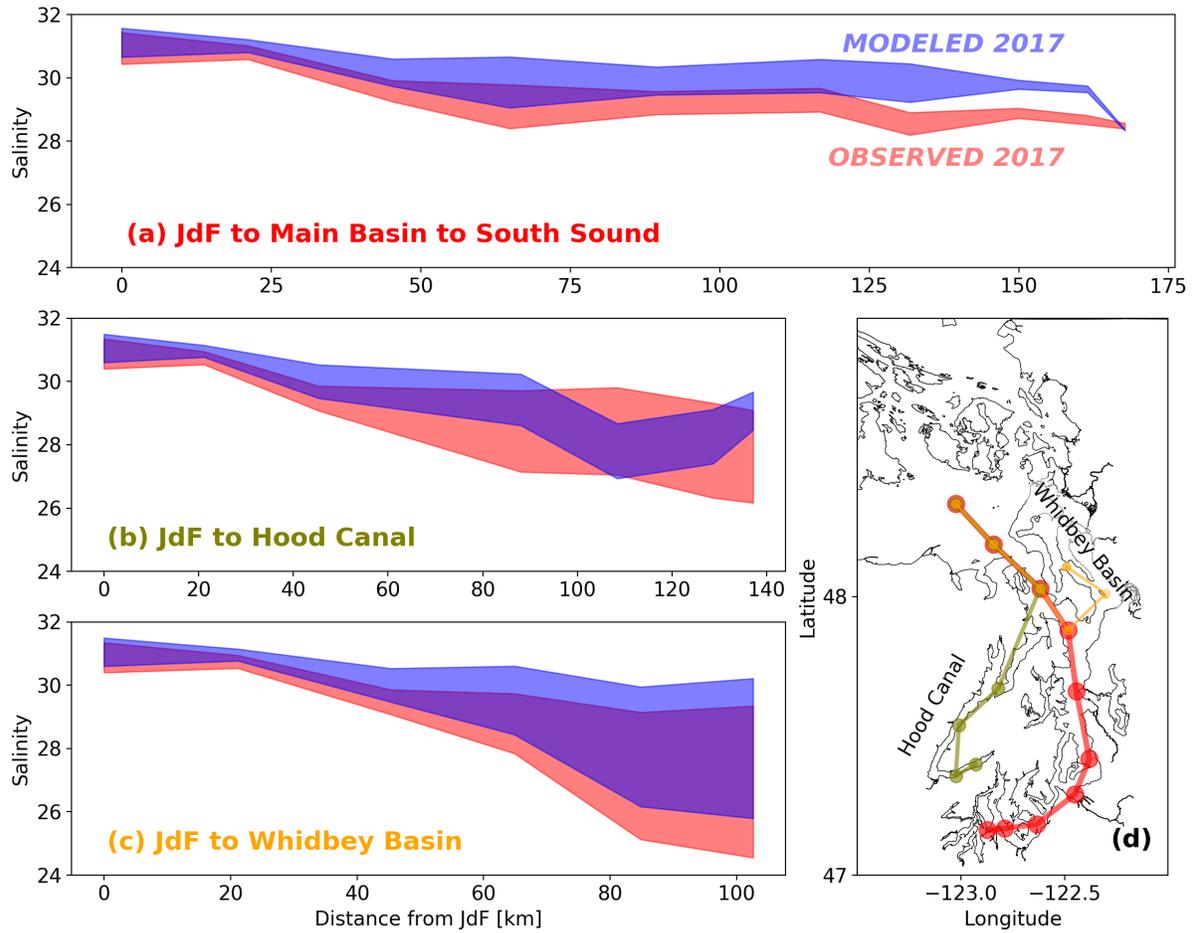
815 nudging to climatology at open boundaries is indicated by transparency. Bathymetry contours

816 for 200 m and 2000 m are plotted as black lines. Close up of the model (b) for the Salish Sea

817 with ticks for every 4th grid point. Three-year time series (c) of flow in the Fraser and Skagit

818 Rivers, year is labeled at the middle of the year.

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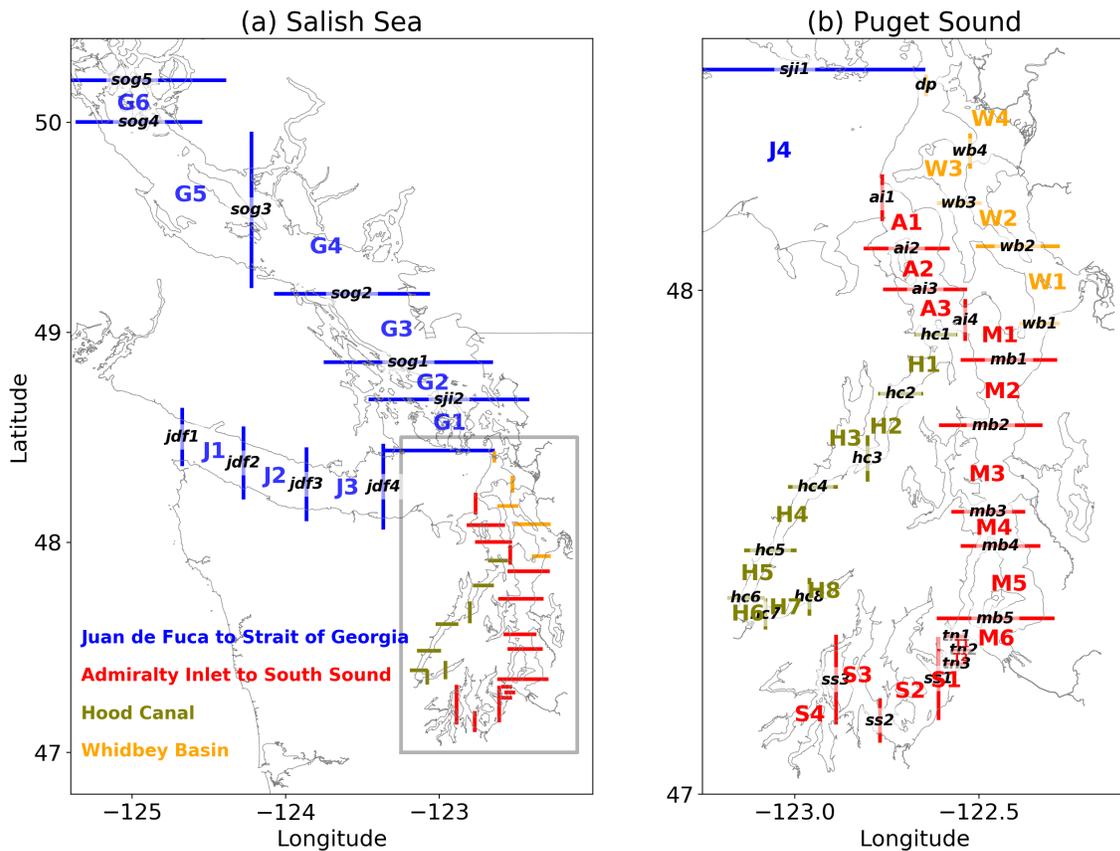
822 Figure 2. Along-channel salinity distribution calculated from 2017 annual-average salinity using
 823 monthly CTD casts (OBSERVED: red) and corresponding model fields (MODELED: blue).

824 The vertical thickness of each line expresses the average stratification: the upper and lower limits
 825 are the salinity averaged below and above a chosen depth. The section down Main Basin (a)
 826 used 20 m for the chosen depth, while (b) and (c) used 10 m because Hood Canal and Whidbey
 827 Basin are more strongly stratified than Main Basin. Station locations are plotted in (d). The
 828 colored lines in (d) are the transects shown in (a)-(c).

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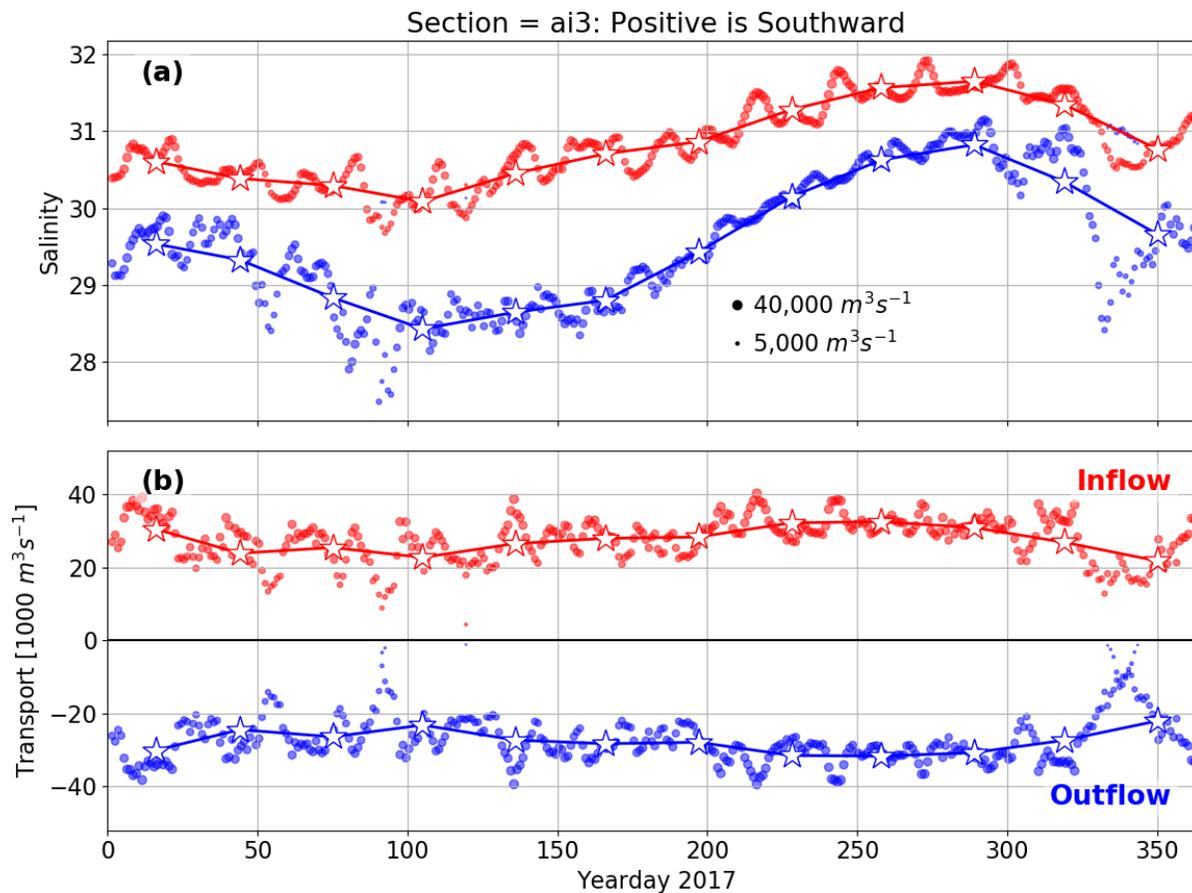
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834 Figure 3. Sections used for the Total Exchange Flow analysis in the Salish Sea (a). Sections are
 835 shown as lines and lower-case names like *jdf1*. A close up of Puget Sound sections is shown in
 836 (b). The names of segments (the volumes in-between sections) such as J1 are also shown.

837 Segment letters denote the following basins or sills in Puget Sound (b): A = Admiralty Inlet, M =
 838 Main Basin, T = Tacoma Narrows, S = South Sound, H = Hood Canal, W = Whidbey Basin. In
 839 the larger Salish Sea (a) J = Strait of Juan de Fuca, G = Strait of Georgia. Section *sog5* at the top
 840 of (a) is the start of Johnstone Strait which is a minor connection between the Strait of Georgia
 841 and the Pacific Ocean. Section *dp* near the top of (b) is Deception Pass which connects the north
 842 end of Whidbey Basin to the eastern Strait of Juan de Fuca. The sections *tn1*, *tn2*, and *tn3* in (b)
 843 are at Tacoma Narrows which connects South Sound to Main Basin.

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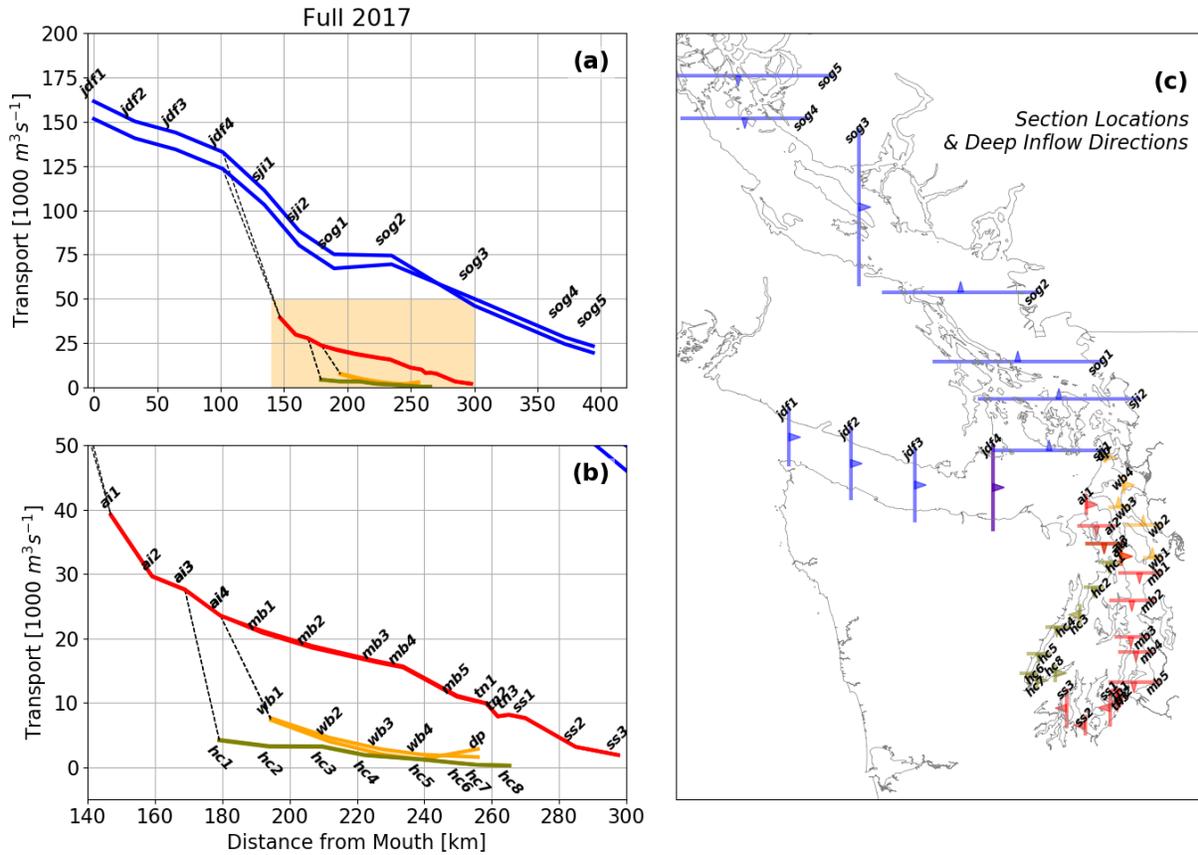
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847 Figure 4. Total Exchange Flow salinity (a) and transport (b) at section *ai3* in Admiralty Inlet
 848 plotted vs. yearday for 2017. The red and blue dots show tidally averaged daily salinity or
 849 transport from the multi-layer TEF analysis. Dot size is proportional to transport. The monthly
 850 averaged two-layer TEF terms S_{in} , S_{out} and Q_{in} , Q_{out} are shown as stars connected by lines.

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855 Figure 5. Total Exchange Flow volume transports averaged over 2017 for the four main

856 channels of the Salish Sea (a). The lines are Q_{in} and $-Q_{out}$, so the higher of the two blue lines in

857 (a) is the outflow. An expanded view of Puget Sound transports is plotted in (b). Section

858 locations and names are shown in (c) with the spike on each section line showing the direction of

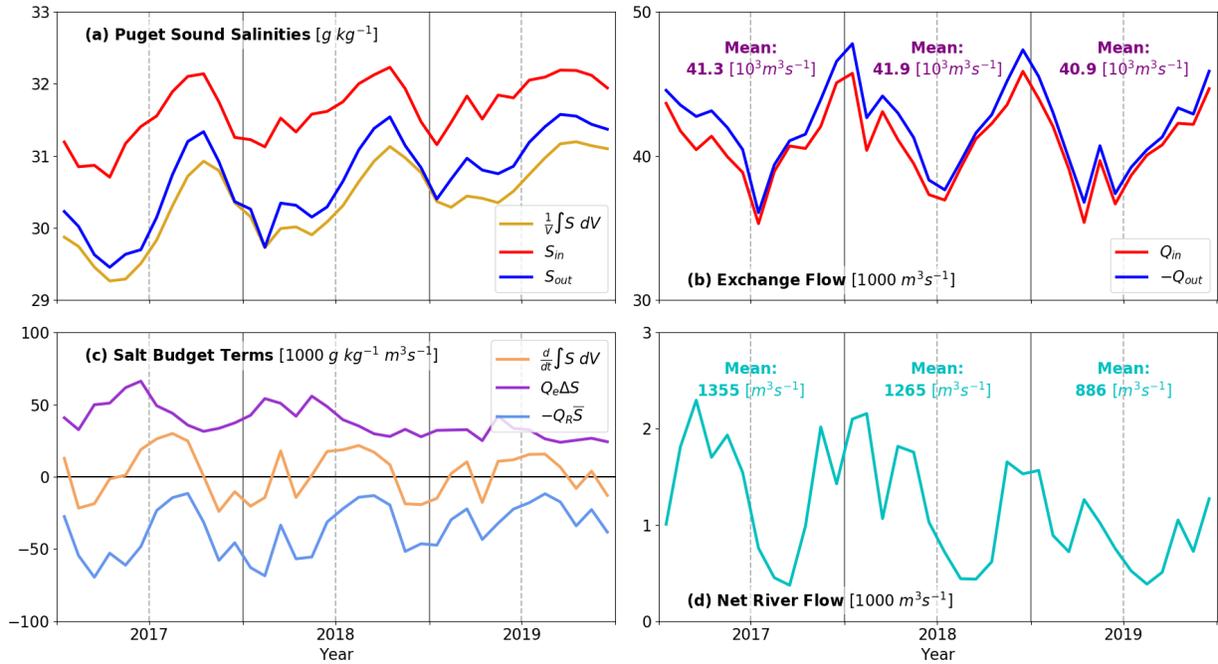
859 the deep inflow. Note that the exchange flow reverses sign in the Strait of Georgia between

860 sections *sog2* and *sog3*. The dashed lines at the seaward end of basins, e.g. from *hc1* to *ai3* in (b)

861 indicate connections between the channels.

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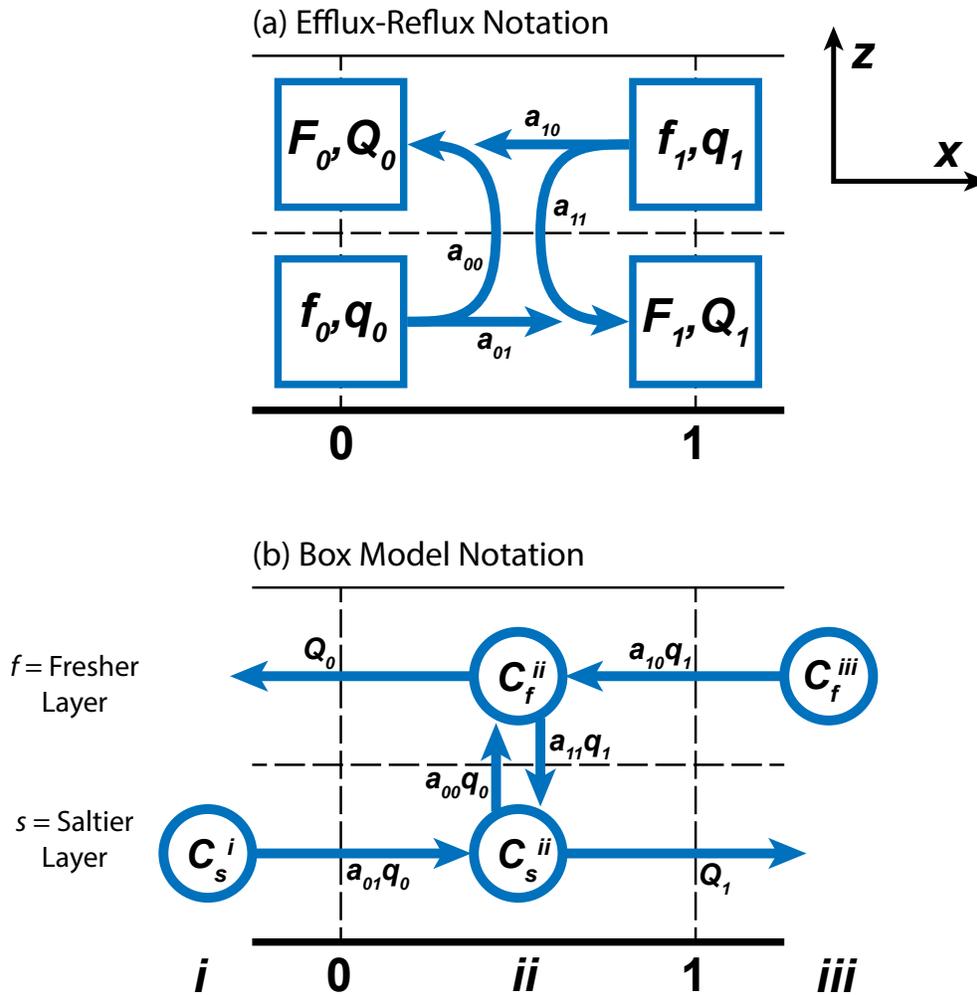


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866 Figure 6. Three-year TEF analysis time series for Puget Sound salinity. The bounding sections
 867 for the volume are ail and dp . Salinities of the in- and outflow are plotted in (a) along with the
 868 mean salinity in the volume. The term $V^{-1} \int S\ dV$ is lower than S_{in} and S_{out} because is it the
 869 average over the whole volume of Puget Sound, not the average of S_{in} and S_{out} . All values are
 870 monthly averages. The exchange flow transports are plotted in (b) with annual means shown for
 871 each year as text. Terms in the exchange flow salt budget are plotted in (c). The net river flow is
 872 plotted in (d) with annual means shown for each year as text. Year labels are at the middle of the
 873 year.

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877 Figure 7. Sketch of notations used for (a) the efflux-reflux calculations, and (b) the box model.

878 Each panel represents three segments (i - iii) divided by sections 0 and 1. Each segment has two

879 layers in the vertical, a deep saltier one and a shallow fresher one. TEF volume and salt fluxes

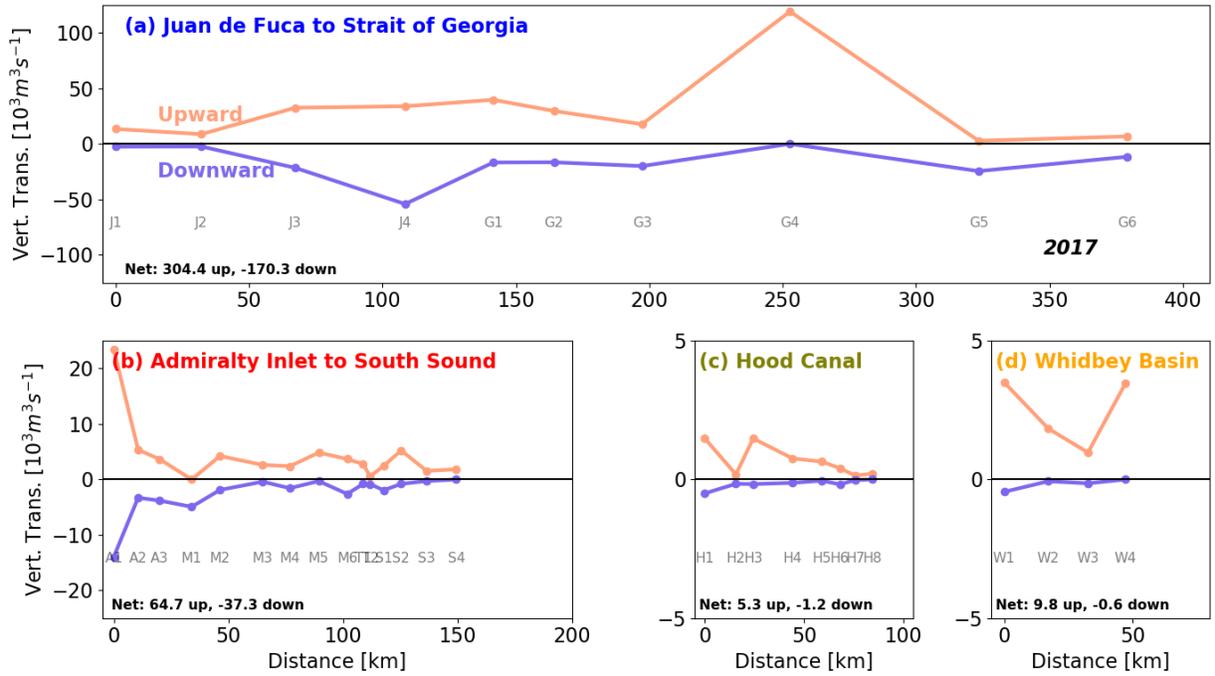
880 are denoted by Q , q , and F , f in (a), and the efflux-reflux fractions are a_{00} and so on ($a_{from,to}$). In

881 the box model (b) C denotes the concentration of an arbitrary tracer, and the subscripts f and s

882 denote the “vertical” delineation.

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887 Figure 8. Vertical transports in segments for each channel from the efflux-reflux box model.

888 Values shown are for the full year 2017. In each segment there may be both upward and

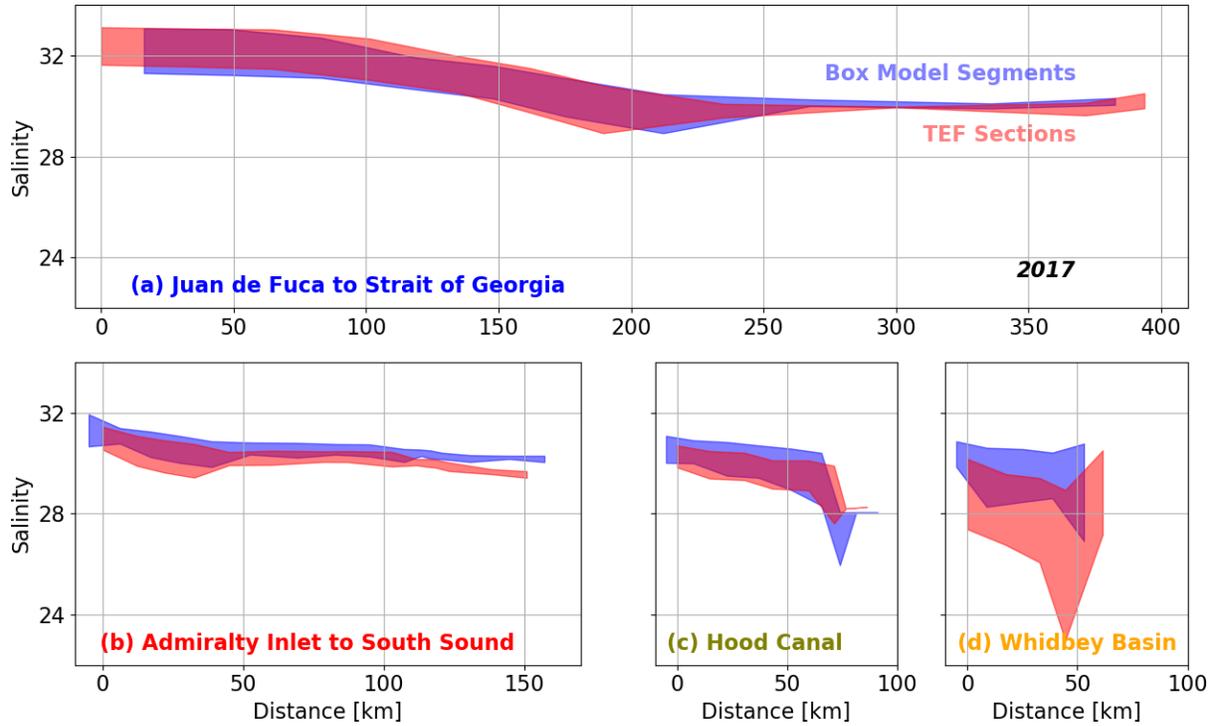
889 downward transports, which is an alternate way of quantifying the effects of vertical advection

890 and mixing. Note that the y-axis scales change for each panel. The sum of all up or down

891 transports in each channel is shown in text at the lower left [$10^3 \text{ m}^3 \text{ s}^{-1}$].

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896 Figure 9. Test of the ability of the box model to reproduce the TEF salinities that were used to
 897 construct it. Each panel is for one of the four channels of the Salish Sea, and shows the range
 898 between upper- and lower-layer salinities as the vertical line thickness, vs. along channel
 899 distance. For the box model these salinities are in the segments, whereas for the TEF sections
 900 they are S_{out} and S_{in} on the sections.

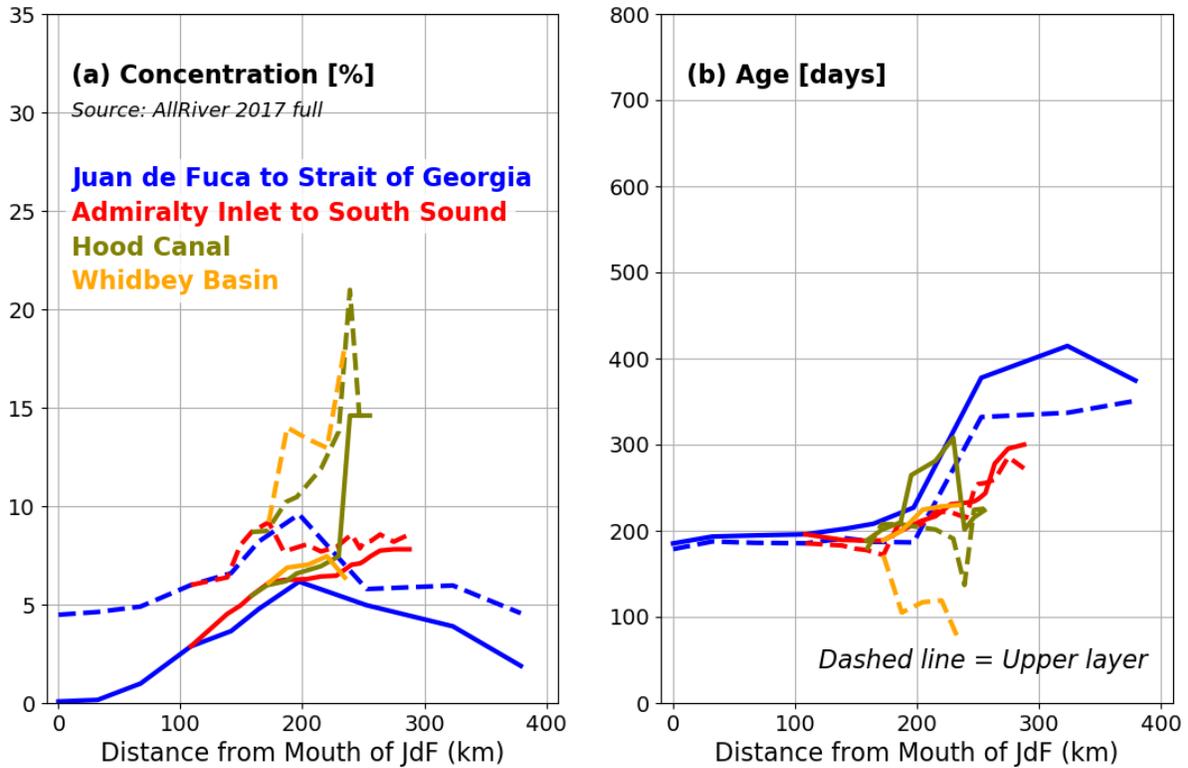
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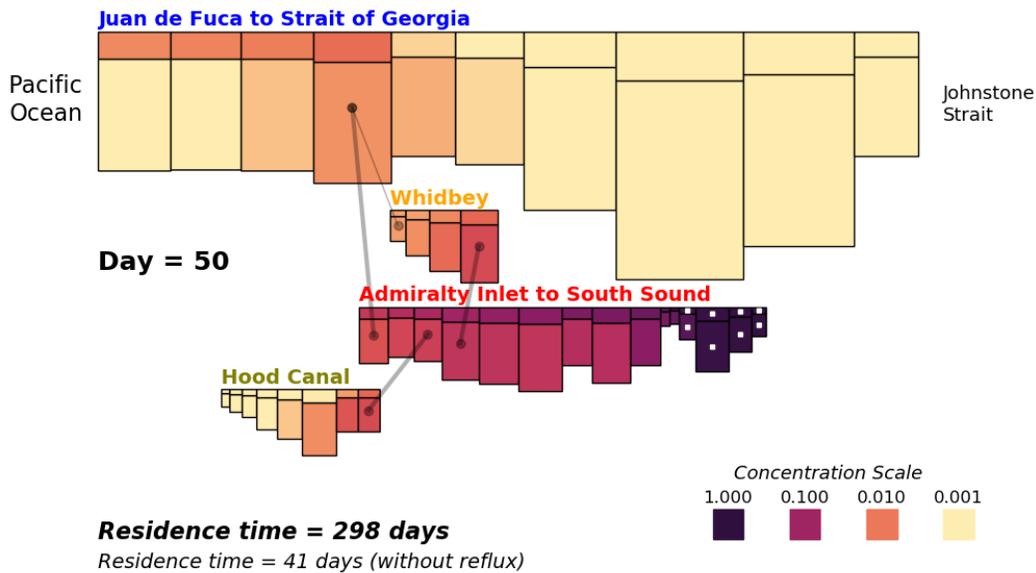
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909 Figure 10. Result for the final state of a box model source experiment with a tracer of
 910 concentration 1 coming out of all the rivers. The circulation, mixing, and river flows are
 911 assumed to have the values of the mean of 2017 for the entire six-year integration. Final
 912 concentration is shown in (a) and age in (b). The solid lines are the bottom sub-volumes of each
 913 segment, and the dashed lines are for the surface sub-volumes.

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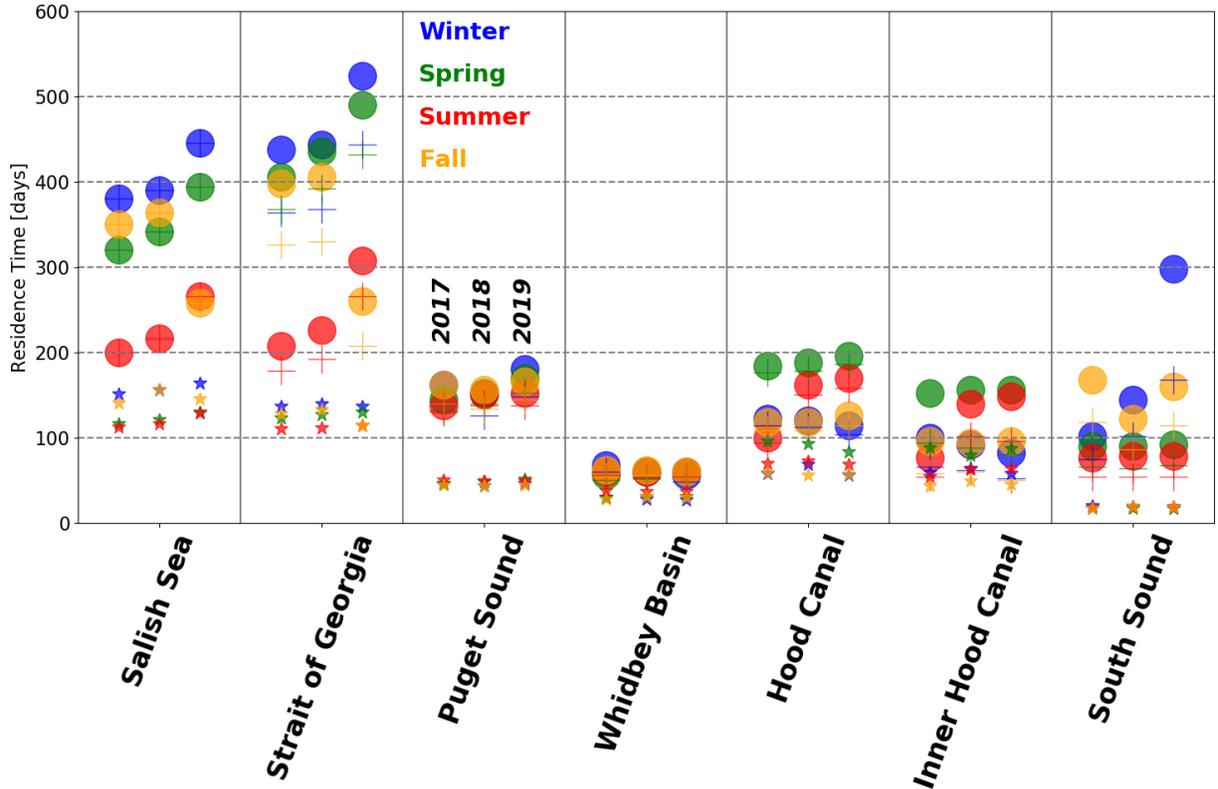
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918 Figure 11. Snapshot of a time-dependent integration of a box model experiment in which there
 919 is a tracer initial condition, but no tracer coming in from the river or ocean sources. In this case
 920 the tracer was set to 1 in the volumes of South Sound (dark color with white squares) and
 921 allowed to advect and mix at rates from winter 2019. The snapshot is from 50 days into the
 922 integration, with color indicating \log_{10} of the concentration. Each segment is shown as a
 923 rectangle (divided into upper and lower sub-volumes) and the rectangle size is proportional to
 924 segment volume. Connections between channels are shown as gray lines – the thin gray line
 925 connecting Whidbey Basin to the Strait of Juan de Fuca is Deception Pass.

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930 Figure 12. Residence times from box model initial condition experiments for various basins in
 931 four seasons (colors). Each basin has values for three different years (separated horizontally as
 932 indicated for Puget Sound). The large filled circles are T_{res} , the residence times calculated from
 933 the box model as the e -folding time of a tracer initialized with concentration 1 in the segments of
 934 that basin and 0 elsewhere. The smaller stars are T_{flush} . The crosses are T_{resNX} . The Hood Canal
 935 Inner volume consists of just the deeper portions of segments H3-H8.

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	T_{res}	T_{resNX}	T_{flush}	f_{reflux}	Sutherland et al. (2011)	Pawlowicz et al. (2007)
Salish Sea	327	327	136	0%		
Strait of Georgia	379	322	125	22%		112-319
Puget Sound	157	138	47	17%	57	
Whidbey Basin	60	53	31	24%	24	
Hood Canal	143	134	70	13%	81	
Hood Canal Inner	116	72	63	83%		
South Sound	125	85	18	37%	21	

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941 Table 1. Residence and flushing times in days, averaged over all years and seasons in each basin
 942 (Fig. 12) are given in the left three columns. Three different timescales are given, as defined in
 943 the text, along with the fraction f_{reflux} by which T_{res} is changed when reflux is not included.
 944 Comparisons to selected previous results are shown in the right two columns, as discussed in the
 945 text.

946