# Source parameters of moderate-to-large Chinese earthquakes from the time evolution of P-wave peak displacement on strong motion recordings

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#### Abstract

In this work we propose and apply a straightforward methodology for the automatic characterization of the extended earthquake source, based on the progressive measurement of the P-wave displacement amplitude at the available stations deployed around the source. Specifically, we averaged the P-wave peak displacement measurements among all the available stations and corrected the observed amplitude for distance attenuation effect to build the logarithm of amplitude vs. time function, named LPDT curve. The curves have an exponential growth shape, with 31 an initial increase and a final plateau level. By analyzing and modelling the LPDT curves, the information about earthquake rupture process and earthquake magnitude can be obtained. We applied this method to the Chinese strong motion data from 2007-2015 with MS ranging between 4 and 8. We used a refined model to reproduce the shape of the curves and different source models based on magnitude to infer the source-related parameters for the study dataset. Our study shows that the plateau level of LPDT curves has a clear scaling with magnitude, with no saturation effect for large events. By assuming a rupture velocity of 0.9Vs, we found a consistent self-similar, constant stress drop scaling law for earthquakes in China with stress drop mainly distributed between a lower level (0.23Mpa) and a higher level (3.74Mpa). The derived relation between the magnitude and rupture length can be used for probabilistic hazard analyses and real-time applications of Earthquake Early Warning systems.

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5	Yuan Wang <sup>1</sup> , Simona Colombelli <sup>2,*</sup> , Aldo Zollo <sup>2</sup> , Jindong Song <sup>1</sup> , Shanyou Li <sup>1,*</sup>
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14	Key Points:
15	• The time evolution of P-wave displacement amplitude is a proxy for the moment rate
16	function;
17	• The time evolution of the P-wave amplitude carries information about source
18	magnitude and extent;
19	• The earthquake rupture extent can be estimated from the analysis of the early
20	P-wave data;
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22	
23	
24	Abstract
25	In this work we propose and apply a straightforward methodology for the automatic
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29	available stations and corrected the observed amplitude for distance attenuation effect to
30	build the logarithm of amplitude vs. time function, named LPDT curve. The curves have an

exponential growth shape, with an initial increase and a final plateau level. By analyzing and 31 modelling the LPDT curves, the information about earthquake rupture process and 32 earthquake magnitude can be obtained. We applied this method to the Chinese strong motion 33 data from 2007-2015 with M<sub>s</sub> ranging between 4 and 8. We used a refined model to 34 reproduce the shape of the curves and different source models based on magnitude to infer 35 the source-related parameters for the study dataset. Our study shows that the plateau level of 36 LPDT curves has a clear scaling with magnitude, with no saturation effect for large events. 37 38 By assuming a rupture velocity of 0.9Vs, we found a consistent self-similar, constant stress drop scaling law for earthquakes in China with stress drop mainly distributed between a 39 lower level (0.23Mpa) and a higher level (3.74Mpa). The derived relation between the 40 magnitude and rupture length can be used for probabilistic hazard analyses and real-time 41 42 applications of Earthquake Early Warning systems.

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Keywords: P-wave amplitude parameter, magnitude, rupture length, stress drop, Earthquake
Early Warning

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### 56 1 Introduction

The characterization of the seismic source in terms of earthquake magnitude and source 57 58 radius (or length of the rupture) is now a routinely operation in any standard seismological laboratory. However, both parameters are generally computed off-line, through fairly 59 complex procedures, mainly performed in the frequency domain. The seismic moment, for 60 example, is estimated from the low frequency amplitude of displacement spectra. The source 61 radius is typically obtained from the spectral corner frequency (Brune 1970; Madariaga 1976) 62 63 or from time-domain, source duration measurements, generally available several minutes after the earthquake occurrence (Boatwright 1980; Duputel et al. 2012). Although the fitting 64 of spectral shapes is a straightforward operation, a major issue is the adequate correction of 65 the observed spectra for path attenuation and site response effects. 66

With this in mind, Colombelli and Zollo (2015) looked at the time evolution of the early 67 68 P-wave information and used it as a proxy for the rupture process of earthquakes to extract the seismic moment and rupture extent of moderate-to-large Japanese earthquake records. 69 More recently, Nazeri et al. (2019) explored a similar approach using strong-motion data of 70 71 the 2016-2017 Central Italy sequence and estimated moment magnitude, fault length and average stress drop for each single event. Following the idea of Colombelli and Zollo (2015) 72 73 and Nazeri et al. (2019), in this study we explore a similar approach for the robust estimation of the earthquake magnitude and rupture length and applied it to a database of 74 moderate-to-large Chinese earthquake records. The proposed method is a remarkably simple 75 and straightforward approach to rapidly and automatically estimate two main source 76 parameters, the earthquake magnitude and the expected length of the rupture. The 77 78 methodology used in this work is also able to provide an estimation of the average stress drop 79  $(\Delta \sigma)$  for the earthquakes in our dataset.

Furthermore, the proposed methodology can be used to quickly characterize the earthquake magnitude and the expected length of the rupture, and to provide an approximate estimate of the average stress drop to be used for Earthquake Early Warning and rapid response purposes, for which accurate estimation of the rupture extend at the early stage of the process can be a useful piece of information to add to the early shake-map computation for more precise ground shaking prediction.

The aim is twofold: 1) establish source scaling relationships for moderate to large earthquakes in China and 2) build the foundation for further studying the feasibility of a network-based EEW method based on the time evolution of the early P-wave peak displacement amplitude.

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### 91 **2 Data and methodology**

# 92 2.1 Data selection

93 For the present analysis, we selected the earthquakes occurred in China in the period 2007–2015. The magnitude of the events (typically, surface magnitude,  $M_s$ ) varies between 94 4.0 and 8.0. To avoid the inclusion of bad quality data in our analysis, we selected seismic 95 records with an epicentral distance smaller than 120 km, but for the M8 event we expanded 96 97 the limit to 200 km and required that each event had at least three records. A total of 1293, 3-component accelerometric waveforms, relative to 88 earthquakes and to 540 stations was 98 used. Two main seismic regions (Sichuan-Yunnan and Xinjiang regions) in China have been 99 selected and Fig. 1a shows the epicentral position of the selected earthquakes and the location 100 101 of stations. Fig. 1b shows the histogram distribution of the analyzed records as a function of 102 the epicentral distance and magnitude.

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#### 104 **2.2 P-wave peak measurements and LPDT curve**

105 We preliminary identified the onset of the P wave on the vertical component of acceleration records, using a standard short-term/long-term average method for automatic 106 picking (Allen, R. V., 1978). Then, we visually inspected all the available waveforms and 107 made manual picks where necessary, to adjust potential mistakes from the automatic picking 108 109 algorithm. After removing the mean value and the linear trend, the acceleration waveforms 110 are integrated once to velocity and twice to get displacement. Finally, we applied a 0.075Hz high-pass Butterworth filter to remove the low frequency drift on displacement records. We 111 impose the zero-crossing of the signal amplitude at the onset of the P-wave, to eliminate any 112 potential residual noise contaminations resulting from the double integration operation. 113

We then measure the absolute maximum of the initial P-wave amplitude on the vertical component of displacement (named Pd) using an expanding time window, starting at the

arrival of the P-wave and moving forward with a time step of 0.01s. The peak amplitude is related to the earthquake magnitude (M) and to the source-to-receiver distance (R) through an attenuation relationship of the general form (Wu & Zhao, 2006; Zollo et al.,2006):

$$log_{10}(Pd) = A + B \cdot M + C \cdot log_{10}(R) \tag{1}$$

where Pd is the P-wave peak measurements and A, B and C are coefficients empirically determined. To estimate the coefficients of equation (1), we performed a least-squares multiple regression analysis, in which we fixed the distance attenuation coefficient (C) and chose a fixed length of the P-wave time window for the parameter measurements, which was set at 3s for M $\leq$ 7 and 9s for 5.5<M $\leq$ 7, respectively. Further details about the estimation of the coefficients of equation (1) are provided in Supplementary Material.

We selected 31 events with at least 10 records and magnitude ranging from 4 to 8 for the computation of the LPDT curve. For each event, the peak amplitudes Pd of all records are measured at every P-wave time window and the distance-corrected amplitudes  $(\log P^c d)$  are obtained as  $\log P^c d = \log Pd - C \log R$ .

In order to avoid the contamination of the S-waves on the selected portion of the P-wave, we picked out 4 stations with clear seismic phase randomly from the dataset in each distance bin (every 20km) and manually picked the S-wave arrival time to estimate the coefficients of the following equation:

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$$Ts - Tp = b \cdot k \cdot R \tag{2}$$

where Tp is the P-wave onset time, Ts is the arrival time of the S-wave, R is the hypocentral 135 distance in km, b = 0.13 is the coefficient derived from a linear regression analysis and k is a 136 scale factor which was set at 0.8, to account for the uncertainty of the regression analysis. 137 138 Using equation (2), as the time window increases, the stations with the expected S-wave arrivals were automatically excluded to make sure only P-wave part involved in the 139 computation. Finally, the LPDT curve is obtained by averaging the distance-corrected 140 amplitude of all the valid stations at each time window. The computation of the curves stops 141 when the number of stations is less than a minimum of data (5 stations). Fig.2 shows an 142 example of computation of the LPDT curve for the M4.6 event. 143

### 145 **2.3 Observation and modelling of LPDT curve**

As shown in Fig.2, the LPDT curve has an exponential growth shape with an initial increase, a gradual intermediate curvature and a final plateau level. Generally, the LPDT curve of larger event needs more time to reach the plateau and the plateau level of the curves scale with the final magnitude (Fig. 3a).

150 The shape of the LPDT curve, as obtained from the average of many stations distributed over azimuth and distance, can be interpreted as a proxy of the Moment Rate Function 151 (MRF), from the initial time up to its maximum peak value. Therefore, two essential features 152 of the MRF, i.e., peak value and peak time, which are both related to the source properties, 153 should be embodied in the LPDT curves. Following the idea of Colombelli and Zollo, 2015, 154 for near-triangular source time functions, the peak value of the MRF (related to the 155 magnitude) will correspond to the plateau level of the LPDT curve, and the peak time of the 156 MRF (related to rupture half-duration) is a proxy for the time at which the LPDT curve 157 reaches its plateau level (Plateau Time). With this in mind, the magnitude and rupture 158 duration can be estimated from the plateau level and the plateau time of the curves. 159

160 To model the LPDT curves, we fit data using the following function (Colombelli et al.,161 2020):

$$log_{10}P_{d}(t) = P_{L}\left\{1 - \left[ae^{-t/T1} + (1-a)\left(e^{-t/T2}\right)\right]\right\} + y_{0}$$
(3)

where  $y_0$  is fixed as the first point of the curve,  $P_L$  is the interval between  $y_0$  and the plateau 163 level, **a** is the weighting factor which is set to 0.5,  $T_1$  and  $T_2$  are the time parameters (here we 164 define the larger value as  $T_2$ ).  $T_1$  controls the very initial part which usually has a faster 165 166 increasing speed and  $T_2$  represents the second part, whose increasing speed gradually become slower. This double corner time, exponential model accounts finely for the two different 167 behaviors of LPDT curve-that is to say, a sharp increase to the plateau (ramp-like) for small 168 events and a more gentle and smooth increase (exponential) for largest events. The model 169 parameters are shown in Fig. 2. 170

We used a non-linear, weighted-fitting approach to model our curves, accounting for the standard error on each point of LPDT curves. Specifically, at each time step, the weight is obtained as:

$$Weight = 1/(N \cdot SE^2) \tag{4}$$

where SE is the standard error in each P-wave time window, N is the number of stations used 175 for that time window. Fig. 3b shows that the LPDT (displacement) curves of all the events are 176 quite well reproduced by the fitting model, with an average residual of 0.3. Generally, at the 177 beginning of the curve computation, several stations from a broad range of distances and 178 azimuths are involved in the calculation, so that the scatter of data is large and the fitting 179 procedure gives a smaller weight to this part, as compared to the plateau of the curves, which 180 181 is instead, well reproduced. A slightly larger (about 0.7) difference between the real data and the model is observed for the initial part of the curve of the M 8.0 Wenchuan earthquake, 182 which could be related to the complexity of the source process of this peculiar event. Indeed, 183 184 when looking at the seismic moment release of this event (Fig. 4), a small peak value is observed at 4-5 seconds, before the arrival of the absolute main peak value (at about 25s), and 185 this leads to a sag of the LPDT curve around 4s. 186

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#### 188 **3 Results**

We fit the LPDT curves with our exponential model and obtain the three relevant 189 parameters mentioned above  $(T_1, T_2, P_L)$  while  $y_0$  has been fixed to the first point amplitude. 190 For simplicity, we defined a new variable called  $P_L^* = P_L + y_0$  to represent the true plateau 191 level of the LPDT curves. Both the amplitude parameter  $(P_L^*)$  and the two characteristic 192 times ( $T_1$  and  $T_2$ ) scale with earthquake magnitude. Fig. 5 shows the plateau level  $P_L^*$  as a 193 function of magnitude. A good correlation between PL\* and magnitude (the correlation 194 coefficient reaches 0.947) can be found. The parameters  $T_1$  and  $T_2$  extracted from our fitting 195 model are shown in Fig. 6 as a function of magnitude. As the best fitting line indicates, both 196 197 parameters linearly increase with magnitude (in logarithmic scale). Due to the very rapid initial increase of the curves,  $T_1$  and  $T_2$  are close to each other for small events, while they 198 gradually separate when the magnitude becomes larger and the initial part of the curves 199 increases gently. 200

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#### 202 **3.1 Magnitude estimation**

Once the observed amplitude has been corrected for the distance effect, the LPDT value at each P-wave time window can be associated to a corresponding magnitude using the coefficients of equation (Table S1). Fig. 3 shows the dynamic process of estimating magnitude for the LPDT curve. The y axis on the left stands for the distance corrected Pd, and the corresponding magnitude or estimated magnitude scale is shown on the right. The predicted magnitude (Mpre) then can be estimated accurately as follows:

$$Mpre = (P_L * - A)/B \tag{5}$$

where  $P_L^*$  is equal to the  $P_L + y_0$  which we fitted from our model, A and B are the 210 coefficients of the attenuation relationship listed in Table S1. As shown in Fig. 3, the 211 occurrence of the plateau for large events (M > 6-7) needs more than 9 seconds after the 212 213 P-wave arrival, suggesting that the typical approaches for the magnitude estimate using fixed 3-4s P-wave time windows (PTWs) would provide underestimated magnitudes for such large 214 events. Moreover, the B coefficient (calibrated using a 3 second PTW) could not be suitable 215 to compute the corresponding magnitude based on the P<sub>L</sub>\* obtained in a longer time window. 216 We therefore choose two magnitude ranges, with two different PTW lengths, to calibrate and 217 use the optimal coefficients (Table S1) for magnitude estimation. In this way, when an event 218 219 reached its plateau within 4s, we use the relation coefficients A and B for fixed 3s PTW, while we used the coefficients A and B established with a fixed 9s PTW when its LPDT curve 220 221 keeps increasing after 4s.

The estimated final magnitude based on the  $P_L^*$  for the LPDT curve and obtained with the two sets of coefficients for small and large events respectively, is plotted in Fig. 7 as a function of the catalog magnitude. As it can be seen in Fig. 7, most of the points are distributed around the dashed line representing the 1:1 relationship between the estimated magnitude and the catalog magnitude. The scatter of data is rather small, with an average estimated error of 0.229 magnitude units.

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# 229 **3.2 Prediction of rupture length and estimation of stress drop** $\Delta \sigma$

The rupture duration is the total duration of a seismic event, given by the whole time length of the moment rate function (Vallée, 2013). It is generally observed that the rupture

duration scales with magnitude and is related to the rupture length, assuming a value for the 232 rupture velocity (Wells & Coppersmith, 1994). As the moment rate function can be simplified 233 as a symmetric triangle (Bilek et al., 2004), the peak time of the MRF, corresponding to the 234 plateau time (T<sub>PL</sub>) of the LPDT curve, is a measure of the Half-duration of each event 235 (Colombelli & Zollo, 2015; Nazeri et al., 2019). Having in mind the Sato & Hirasawa model 236 (Sato & Hirasawa, 1973) here we investigate the relation between parameter T<sub>2</sub> of LPDT 237 curves and T<sub>PL</sub>, the time at which occurs the peak of the MRF. In the Sato & Hirasawa model, 238 239 the rupture spreads radially outwards at a constant velocity with a circular fault, and stress drop ( $\Delta\sigma$ ) and rupture velocity (Vr) are two relevant parameters controlling the earthquake 240 rupture process. Since  $\Delta \sigma$  and Vr of earthquakes can vary significantly for each event 241 (Allmann & Shearer, 2009), we performed a set of dedicated simulations to explore stress 242 drop values between 0.05Mpa and 20 MPa with rupture velocities between 0.5Vs and 0.9Vs, 243 244 for a total of 55 combinations of the two parameters.

For each given magnitude, we fixed  $\Delta \sigma$  and Vr, and generate the corresponding Sato & 245 Hirasawa moment rate Function (SHF) by changing the polar angle of the observation point 246 from  $0^{\circ}$  to  $90^{\circ}$  and computing the average SHF (an example of M5 event shown in the Fig.8a). 247 We then compute the log of the SHF (hereinafter LSHF) to get a curve with a similar shape of 248 our LPDT curve. Since most of the selected earthquakes in our database occurred at an 249 average depth of about 10km, we set the Vp=6.2km/s, Vs=3.4km/s based on the velocity 250 model for this region (Weilai Wang et al., 2014). Examples of the average SHF with fixed 251 Vr=0.7Vs and  $\Delta\sigma$ =0.1MPa is shown in Fig.8, while examples with other  $\Delta\sigma$  values are shown 252 in the supplemental material. For each available couple of stress drop and rupture velocity, 253 we used the exponential model (eq. 2) to fit the LSHF curve and extract the  $T_2$  parameter for 254 different magnitudes. As expected, we found that  $T_2$  has linear relationship with  $T_{PL}$  obtained 255 directly from the peak time of the generated SHF (in logarithmic scale) for the entire 256 magnitude range with a small deviation when exploring the  $\Delta \sigma$  and Vr, suggesting that the T<sub>2</sub> 257 258 parameter extracted from the observed curves can be used to predict  $T_{PL}$ :

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$$log_{10}(T_{PL}) = 1.111(0.051)log_{10}(T_2) + 0.542(0.030)$$
 (6)

260 For the circular model with a symmetric triangular shaped MRF, the obtained  $T_{PL}$  can be

regard as the Half-Duration (HD) of the source function. After averaging the peak time of the MRF from  $0^{\circ}$  to  $90^{\circ}$ , we obtain the averaged half-duration related to the source radius (Aki & Richards, 2002):

$$< HD >= \frac{\int_{0}^{\frac{\pi}{2}} \frac{a}{V_{r}} (1 - \frac{V_{r} \sin \theta}{V_{p}}) d\theta}{\frac{\pi}{2}} = \frac{a}{V_{r}} (1 - \frac{2}{\pi} \frac{V_{r}}{V_{p}})$$
(7)

where **a** is the source radius, Vr is rupture velocity and Vp is the P-wave velocity. Given the half-duration of the source, the source radius of the analyzed events can be estimated.

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Fig.9 shows the predicted source radius as a function of magnitude and its corresponding 267 half-duration with a fixed rupture velocity of 0.9Vs. Based on the computation of stress drop 268  $(\Delta \sigma)$  for the circular model using the source radius (a) and the seismic moment (M<sub>0</sub>) 269 (Keilis-Borok, 1959),  $\Delta \sigma = \frac{7}{16} \frac{M_0}{a^3}$ , the theoretical scaling lines of the source radius as a 270 function of M with a constant  $\Delta \sigma$ =0.1Mpa and 10Mpa were given in the same figure as a 271 comparison. The predicted source radius shows a similar increasing trend with the theoretical 272 273 lines, indicating that the source radius of the analyzed events has a consistent self-similar, constant stress drop scaling with magnitude. Due to this, we fit the source radius with a 274 weight-based fitting approach (same as eq. 4, here, the SE is the standard error of the source 275 radius computed from the predicted T<sub>PL</sub> and its error obtained by the error propagation 276 277 approach) to obtain the best-fit constant stress drop of 0.35Mpa. In addition, we repeated the process by setting Vr=0.7Vs and Vr=0.8Vs, and found that the mean value of  $\Delta\sigma$  are 0.99Mpa 278 and 0.57Mpa, respectively. 279

For a circular fault, we predict the rupture length as the twice of the predicted source radius. According to the results of LPDT curve shown in Fig.11, we obtain a rupture length of 68 km with a predicting source radius of 34 km for the M 7.0 Lushan earthquake, which agrees with the source inversion results of Zhang, et al. (2014a) (L~60km). For the M 8.0 Wenchuan earthquake, we obtained a predicted rupture length of 271km, which is slightly underestimated as compared to the estimate of Zhang, et al. (2014b) (L~300km).

The MRF of M 8.0 Wenchuan earthquake (download from USGS, shown in Fig. 4) has the major peak occurring at the beginning of the rupture and followed by a long-time duration coda. The circular model with a triangle-shape MRF is not able to correctly reproduce this kind of source function. For large earthquakes (M>6.7), indeed, the rupture length (L) extends with magnitude, but the rupture width (W) has a nearly constant value (20km) (Cheng et al., 2019). In the situation of L>>W for large events, the Haskell model with a trapezoid-shape MRF is often used.

The far-field displacement radiated by a Haskell type fault model is equivalent to the convolution of two box-car functions of different amplitude and durations: rise time ( $\tau$ ) and rupture time (T<sub>R</sub>). The resulting function has a trapezoidal shape with total duration given by the sum of  $\tau$  + T<sub>R</sub>. The rupture time T<sub>R</sub> depends on the finite length of the fault (L) and the azimuth ( $\vartheta$ ) between source and receiver (Haskell, 1964):

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$$T_R = \frac{L}{Vr} (1 - \frac{Vr}{Vp} \cos \theta)$$
(8)

The rise time  $\tau$  is independent of azimuth (Hwang et al., 2011) and can be obtained using the following relationship calibrated by Melgar and Hayes (2017) from a database of finite faults:

 $\log_{10}(\tau) = -5.323 + 0.293 \log_{10}(M_0)$ (9)

Fig.10 shows an example of changing the azimuth ( $\vartheta$ ) from 0° to 180° to compute the average total duration. Assuming that  $T_{PL}$  is the middle point of the average trapezoid plateau, the following relationship between L and  $T_{PL}$  can be obtained and be used for estimating rupture length of large events when assuming the Haskell model:

306 
$$T_{\rm PL} = \frac{1}{2} \left( \tau + \frac{L}{Vr} (1 - \frac{Vr}{Vp}) \right)$$
(10)

We computed the predicted rupture length for the two large events using the Haskell 307 model. Results are included in Fig.11. As shown in Fig. 11, with the same T<sub>PL</sub>, Haskell model 308 309 provides a rupture length slightly larger than the results using circular model for large events. The obtained earthquake scaling relationship in this study is comparable with the 310 magnitude-rupture scaling relation studied by Cheng et al. (2019) using 91 earthquakes in 311 Mainland China and the empirical scaling relation for strike-slip earthquakes with M 4.8 to M 312 8.1 proposed by Wells & Coppersmith (1994), especially in the moderate-large magnitude 313 314 range.

As for the computation of stress drop, for larger events (L>>W), we used the following formula (Madariaga, 1977):

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$$\Delta \sigma = \frac{2}{\pi} \bullet \frac{M_0}{W^2 L} \tag{11}$$

318 where W is the rupture width, set to 20km for large events (M>6.7).

We therefore suggesting using the circular model for small-moderate events (M $\leq$ 6.7) and the 319 Haskell model (rectangle model) for large events (M>6.7) in the estimation of rupture length. 320 321 Based on the predicted source radius derived from different models, we compute the stress drop of each event shown in Fig.12. After applying the rectangle source model for larger 322 events, we obtain the stress drop = 4.88Mpa for M 8.0 Wenchuan earthquake, which is 323 comparable with the results of Meng et al. (2019) (3.5Mpa). However, both models in this 324 study provides an underestimated stress drop for M 7.0 Lushan earthquake when comparing 325 with the results (1.8Mpa) obtained by Li et al. (2017). The distribution of stress drops is 326 shown in Fig. 12b. The values vary from 0.1Mpa to 10Mpa, and two sets of values nearly 327 distributed with a logarithmic mean of 0.23Mpa and 3.74Mpa, respectively. All these source 328 329 parameters of the analyzed events are summarized in Table 1.

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#### 331 4 Discussion and Conclusion

In this study, we generalized the approach proposed by Colombelli and Zollo, 2015 to estimate the source parameters of a set of Chinese earthquakes with magnitude ranging from 4 to 8. The methodology is based on the use of the time evolution of the P wave (LPDT curve) as a proxy for the source time function to extract earthquake magnitude and rupture duration.

Comparing with the previous works by Colombelli and Zollo (2015) and Nazeri et al. (2019), we used the double corner time, exponential model proposed by Colombelli et al. (2020) for better modelling the behavior of LPDT curves. We improved the magnitude estimation based on the plateau level of LPDT curve, by using two different scaling coefficients with fixed C, which have been properly calibrated. A high correlation between magnitude and plateau level has been found and was used to predict the final magnitude accurately.

343 This paper proposes a method to obtain a reliable magnitude estimation using a

straightforward, time-domain signal processing technique, from the plateau level of the 344 LPDT curves are. Based on the analysis of 31 events in the magnitude range between 4 and 8, 345 we found that the plateau level of LPDT curves has a strong correlation with magnitude (the 346 coefficient of correlation is up to 0.947). Comparing with the catalog magnitude of the 347 analyzed events, our predicted magnitude from the displacement data shows an average 348 deviation of 0.229 magnitude units. Surprisingly, for the largest Wenchuan earthquake (Ms 349 8.0) we provide a magnitude estimation of 8.3, without saturation effects, typically observed 350 351 when using shorter P-wave time windows (Lomax et al., 2009; Bormann et al., 2009; Colombelli et al., 2012). 352

Together with the plateau level, the plateau time ( $T_{PL}$ ) of the LPDT curve has also a clear scaling with magnitude, being related to the half-duration of the source. In order to estimate the plateau time, we performed a series of simulations based on the Sato & Hirasawa (Sato & Hirasawa, 1973) model and on the assumption that  $T_{PL}$  corresponds to the peak time of the MRF. We generated a set of MRFs exploring  $\Delta \sigma$  and Vr values and studied the relation between  $T_{PL}$  and the time characteristic parameter  $T_2$ . Finally, we established a linear scaling relationship between the two parameters for predicting the  $T_{PL}$ .

Considering the circular model with a symmetric triangular-shaped MRF, the obtained 360 T<sub>PL</sub> can be regarded as the Half-Duration (HD) of the events to predict the source radius. The 361 obtained source radius in this study shows a consistent self-similar, constant stress drop 362 scaling with magnitude. We obtained the best-fit stress drop (0.35Mpa) for the 31 analyzed 363 events, with fixing rupture velocity to 0.9Vs. This value is lower than world-wide measured 364 median value of 4 MPa (Allmann and Shearer, 2009), but it is comparable with the mean 365 value of 0.52MPa by studying the strong-motion recordings of the Wenchuan aftershocks 366 (2008-2013) (Wang et al., 2018). 367

One major result of this paper concerns the determination of the scaling law of earthquakes in China. We obtained the rupture length (twice source radius) of the analyzed events and found the M 8.0 Wenchuan earthquake has a slightly shorter predicted rupture length with comparing to other results. We realize that for the largest events in the sequence, the circular model may underestimate the total rupture length. Thus, we suggested to estimate the rupture length of the large events (M>6.7) assuming the Haskell model. Our predicted rupture length of different source models as a function of M is close to the rupture scaling
relationship proposed by Cheng et al. (2019) and Wells & Coppersmith (1994). It could be
used for probabilistic hazard analyses, especially for moderate-large events.

To better investigate the distribution of the stress drop in the study dataset, we used the 377 rectangular model instead of the circular model to compute the stress drop of individual 378 earthquakes for larger events. The derived stress drop from displacement is mainly distributed 379 at a lower level (0.23Mpa) and a higher level (3.74Mpa) close to the world-wide measured 380 381 median value (4Mpa). The lower stress drop group ( $\Delta\sigma$ <0.6Mpa) consists of 18 events, in which half of the events are aftershock. Consistent with Wang et al. (2018), the lower stress 382 drop of aftershocks may result from the remaining locked parts on the fault plane of the 383 mainshock. Moreover, we notice that if there is a jump in the increasing process of the LPDT 384 curve (e.g. M 6.6 Ludian earthquake), our approach likely fits the event with a longer T<sub>2</sub> 385 386 causing lower stress drop.

The shape of the curves may change in real-time, when we do not have all the available 387 stations. As a perspective of the work, we could evaluate the feasibility of application in 388 389 real-time, that can be relevant for EEW applications. Thus, both estimated results can be jointly used to provide a specific early-Shakemap for EEWS. While in this off-line study we 390 used the post-earthquake location instead of the real-time estimation, a reliable estimation of 391 the earthquake location is needed for the real-time application. Having in mind that the 392 far-field stations must wait enough time to reach the plateau of the curve for large events, we 393 need more time to get the plateau information. Hence, the real-time application performance 394 and the timeliness based on the network distribution for this approach will be further studied. 395 A possible method could be that we can estimate the final curve at each time step with a 396 given probability and study the real-time curve reached how many percent of the final curve 397 (maybe after  $T_2$ ) can give a reliable probability for estimating final curve. 398

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**Fig.1 Data distribution**. Plot of (a) the epicentral position of the selected earthquakes and the location of stations and (b) the distribution of the analyzed records as a function of the epicentral distance and magnitude.



**Fig.2 The LPDT curve of M4.6 event and the model parameters.** The grey triangles stand for the corrected amplitude  $Pd^{C}$  for the available stations at each P-wave time window, then the circle represents the average  $Pd^{C}$  value of all these stations. Our exponential fit model is shown in black line. The time parameters  $T_1$  and  $T_2$  are shown in the empty triangles.



**Fig.3 The LPDT curve and the misfit.** (a) The average peak amplitude with distance corrected at each P-wave time window for different magnitude with color scale. (b) The difference between the observed value and the value form the fit model. (c) The normalized histograms of the misfit value.



**Fig.4 The LPDT curve of the M 8.0 Wenchuan earthquake and its fit model.** The grey and the dashed line represent the observed data and the best fit model, respectively. The moment rate function of this event provided by the USGS was shown in the bottom with grey area.



**Fig.5 Scaling relationship between P\_L^\* and magnitude**. The circles present the  $P_L^*$  value of each event. The dashed line indicates the best-fit relation between  $P_L^*$  and magnitude.



**Fig.6 Scaling relationship between T1 and T2 as a function of magnitude.** Triangles and circles represent T2 and T1, respectively, for both LPDT, LPVT and LPAT curves. The error bar on each single point is shown as black line (where visible). The best fitting line for each parameter is shown as dashed line.







Fig.8 The exploratory simulations for  $\Delta \sigma = 0.1$ Mpa. (a) Fitting of the Sato & Hirasawa function with exponential model. The dashed line represents the fitted model. (b) Relationship between T<sub>2</sub> and T<sub>PL</sub> for magnitude from 4 to 8 with an interval of 0.1 magnitude units. The dashed line shows the fitting relationship between T<sub>2</sub> and T<sub>PL</sub>.



Fig.9 The scaling relation between source radius and magnitude with a fixed rupture velocity of 0.9Vs. The right y-axis represents the corresponding Half-duration. The circles stand for the  $T_{PL}$  parameter extracted from LPDT curve. The dotted line and dashed line represent the theoretical scaling with constant  $\Delta\sigma$ =0.1Mpa and 10Mpa, respectively. The averaged constant  $\Delta\sigma$  of the analyzed dataset are shown in the solid line.



Fig.10 The trapezoid-like moment rate function (MRF) and the averaged MRF with azimuth from  $0^{\circ}$  to  $180^{\circ}$ . The dashed black line represents that the T<sub>PL</sub> of the LPDT curves (Plateau time) occurs at the middle point of the average trapezoid plateau.



**Fig.11** The scaling relationship between the predicted rupture length and M. The circles and the squares are the predicted rupture length from circular model and Haskell model, respectively. The dashed line is the linear regression relationship in mainland China calibrated by Cheng et al. (2019). The dotted line represents the relationship proposed by Wells and Coppersmith (1994). The diagonal cross and cross are the results of M 8.0 Wenchuan earthquake by Zhang et al. (2014a) and M 7.0 Lushan earthquake by Zhang et al. (2014b), respectively. The estimated error computed through the error propagation approach was shown by the vertical error bars.



**Fig.12** The estimated stress drop of the analyzed earthquakes. (a) The distribution of the estimated stress drop. The circles and the squares are the predicted stress drop from circular model and Haskell model, respectively. The average stress drop value (0.23 MPa and 3.74Mpa) is shown as a dashed line. The diagonal cross and cross are the results of M 8.0 Wenchuan earthquake by Meng et al. (2019) and M 7.0 Lushan earthquake by Li et al. (2017), respectively. (b) The normalized histograms of the predicted stress drop.

Table 1. List of source parameters including catalog magnitude (Ms), predicted magnitude (Ms<sup>PRED</sup>), half duration, source radius (SR), Rupture length (RL) and stress drop ( $\Delta\sigma$ ) determined in this study for moderate-larger events (M $\geq$ 5.5).

			Epic	enter	I	Magnitude		Half	duration		Rupture p	arameters	8						
No.	Location	Date	T.d	T		N PRED	$M_{ m W}$	LDDT	CONT	SR	RL	RL	SSD	Reference					
			Lat.	Long.	Ms	Ms	(source)	LPDI	GCM1	(km)	(km)	(WC94)	(Mpa)						
										135.5	271 (circular)	248	0.18	This is a					
											326 (Haskell)		4.9	This study					
							7.0							Zhang,					
1	Wenchuan	2008/05/12	31.00	103.40	8.0	8.3	(GCMT)	30.4	21.8		200			Wang,					
							(UCMI)				300			Zschau, et					
														al. (2014)					
														Meng et					
													3.5	al.,					
														(2019)					
	Wonchuon						5.6			3.4	6.8	7.1	5.34	This study					
2	(aftershock)	2008/05/13	31.43	104.06	5.8	5.9	(GCMT)	0.8	3 1.6	12			0.72	Wang et al.					
	(artershock)						(GCMI)			4.5			0.75	(2017)					
	Wenchuan						5.4			12.2	24.4	5.2	0.12	This study					
3	(aftershock)	2008/05/14	31.34	103.63	5.8	5.7	(GCMT)	2.7	1.3	7.5			0.17	Wang et al. (2017)					
4	Yaoan	2009/07/09	25.60	101.03	6.3	5.7	5.7 (GCMT)	3.6	1.8	16.0	32	8.3	0.30	This study					
5	Yiliang	2012/09/07	27.56	104.03	5.6	5.6	5.3 (GCMT)	3.1	1.1	14	28	4.5	0.04	This study					
6	Eryuan	2013/03/03	25.93	99.72	5.5	5.3	5.4 (GCMT)	1.7	1.2	7.4	14.8	5.2	0.19	This study					
7	Changji	2013/03/29	43.40	86.80	5.6	5.4	5.4 (GCMT)	1.5	1.3	6.7	13.4	5.2	0.37	This study					
															34	68 (circular)	33.4	0.35	+
							77.3 (Haskell)		0.65	This study									
8	Lushan	2013/04/20	30.30	103.00	7	7.0	6.6 (GCMT)	7.6	4.9		60			Zhang, Wang, Chen, et al. (2014)					
													1.8	Li et al., (2017)					
9	Minxian	2013/07/22	34.54	104.21	6.7	6.6	6.0 (GCMT)	2.4	2.4	10.6	21.2	13.2	4.16	This study					

							()			30.0	60 18.0 0.13	This study		
10	Ludian	2014/08/03	27.11	103.33	6.6	6.5	6.2	6.7	2.9		10			Cheng et
							(GCM1)				12			al., (2015)
										9.8	19.6	15.4	5.4 1.85 This stud	This study
							61				20			Fang et al.,
11	Kangding	2014/11/22	30.29	101.68	6.4	6.2		2.2	2.8		20	18.0       0.13       Th         18.0       0.13       Th         11.0       1.00       C         11.0       1.85       Th         11.1       1.10       Th         11.1       1.11       Th         11.1	(2015)	
							(GCM1)				16			Jiang et al.,
											16			(2015)
10	K	2014/11/25	20.20	101.75	5.0	5.6	5.7	0.72	1.0	2.2	6.4	0.2	0.02	771 1
12	Kangding	2014/11/25	30.20	101.75	5.9	5.6	(GCMT)	0.75	1.8	3.2	6.4	8.3	9.03	This study
12	Lingary	2014/12/06	22.22	100.50	5.9	6.0	5.5	1.0	1.5	4.4	0.0	6.1	2.61	This study.
15	Jinggu	2014/12/06	23.32			6.0	(GCMT)	1.0	1.5	4.4	8.8	0.1	3.01	This study
$M_{\rm S}^{\rm PRE}$	D = Predicted	d Ms, SR = so	ource rad	ius, RL =	rupture le	ngth =2*s	source rad	ius, W	C94 = W	ells an	d Coppers	smith (19	94), SS	SD = statics

stress drop,

GCMT data are available at <u>www.globalcmt.org</u> (last accessed May.6, 2020)

#### 540 Supplementary Material

541

## 542 Text S1. Coefficients of amplitude parameters attenuation relationship

We first use the least squared multiple regression to fit the data and found the coefficients in a 543 fixed 3s time window. However, this time window is not enough to properly describe the 544 amplitude for the far-field waveform of the large events. Then, we tried to apply the changed 545 coefficients at each time window, but the changed coefficient C will induce the step change 546 547 and discontinuity of the LPDT curve. Considering that coefficient C is critical in correcting distance attenuation and is closely connected with the shape of the LPDT curve, we 548 determine the C value for each P-wave peak measurements first, and then selecting records 549 that only P-wave included at each corresponding time window length with following 550 selection and the relationships will be calibrated by using fixed C value. Coefficients of 551 attenuation relationship for a short fixed 3s PTW and a long fixed 9s PTW were listed in 552 Table S1. 553

554

555 **Table S1. Coefficients of equation (1) for each magnitude range in different PTW** 

Coefficient	M≤7 & Fixed 3s PTW	5.5 <m≤7 &="" 9s="" fixed="" ptw<="" th=""></m≤7>						
А	-2.16±0.13	$-3.02 \pm 0.69$						
В	$0.54 \pm 0.02$	$0.73 \pm 0.11$						
С	-1.59							



Figure S1. The exploratory simulations for  $\Delta \sigma = 1$  and 10 Mpa. (a) Fitting of the Sato & Hirasawa function with exponential model. The dashed line represents the fitted model. (b) Relationship between T<sub>2</sub> and T<sub>PL</sub> for magnitude from 4 to 8 with an interval of 0.1 magnitude units. The dashed line shows the fitting relationship between T<sub>2</sub> and T<sub>PL</sub>.

Figure 1.





Figure 2.



Figure 3.



Figure 4.



Figure 5.



CatalogMagnitude





Figure 6.



Figure 7.





Figure 8.



Figure 9.



Figure 10.

![](_page_51_Figure_0.jpeg)

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![](_page_51_Picture_2.jpeg)

Figure 11.

![](_page_53_Figure_0.jpeg)

Figure 12.

![](_page_55_Figure_0.jpeg)

Figure S1.

![](_page_57_Figure_0.jpeg)

![](_page_57_Figure_1.jpeg)

			Epicenter		Magnitude			Half duration					
No.	Location	Date	Lat.	Long.	Ms	$M_{s}^{PRED}$	$M_{ m W}$	LPDT	GCMT	SR	RL	SSD	Reference
				. 81	5	5	(source)			( <i>km</i> )	( <i>km</i> )	(Mpa)	
										135.5	2/1 (circular) 326 (Haskell)	0.18	This study
											520 (Haskell)	4.0	Zhang
1	XX7	2008/05/12	21.00	102.40	0.0	0.2	7.9	20.4	21.0		200		Wang,
1	wenchuan	2008/03/12	51.00	105.40	8.0	8.5	(GCMT)	50.4	21.8		500		Zschau, et al.
													(2014)
												3.5	Meng et al.,
										34	6.8	5 34	2019 This study
2	Wenchuan	2008/05/13	31.43	104.06	5.8	5.9	5.6	0.77	1.6	5.4	0.0	0.54	Wang et al.
	(aftershock)						(GCMT)			4.3		0.73	(2017)
	Wenchuan						54			12.2	24.4	0.12	This study
3	(aftershock)	2008/05/14	31.34	103.63	5.8	5.7	(GCMT)	2.7	1.3	7.5		0.17	Wang et al.
	. ,									16.0	20	0.20	(2017) This study
4	Yaoan	2009/07/09	25.60	101.03	63	57	5.7	36	18	10.0	32	0.30	Wang et al
	ruoun	2003/01/03	20100	101100	0.0	017	(GCMT)	5.0	110		15		(2011)
5	Fengnan	2010/04/09	39.59	118.11	4.1	4.1		0.3		1.5	3.0	0.19	This study
							5.0			2.1	4.2	3.00	This study
6	Qingchuan	2011/11/01	32.60	105.30	5.2	4.8	(GCMT)	0.47	0.8	2.3		1.29	Wang et al.
							47						(2017)
7	Tangshan	2012/05/28	39.71	118.47	4.7	4.7	(GCMT)	0.9	0.6	4.0	8.0	0.08	This study
8	Baodi	2012/06/18	39.61	117.56	4.0	3.3	(000000)	0.1		0.5	1.0	2.95	This study
0	Baowing	2012/07/20	33.04	110 57	19	19	5.0	1.0	0.8	15	9.0	0.11	This study
,	Baoying	2012/07/20	55.04	119.57	4.9	4.7	(GCMT)	1.0	0.8	4.5	9.0	0.11	This study
10	Yiliang	2012/09/07	27.56	104.03	5.6	5.6	5.3	3.1	1.1	14.0	28	0.04	This study
11	Vongning	2012/11/20	38.43	106.34	4.6	4.6	(GCMT)	0.2		0.0	1.8	4.44	This study
11	Tongning	2012/11/20	50.45	100.54	4.0	4.0	5.4	0.2		0.7	1.0	4.44	This study
12	Eryuan	2013/03/03	25.93	99.72	5.5	5.5	(GCMT)	1.7	1.2	7.4	14.8	0.19	This study
13	Changij	2013/03/29	43 40	86.80	5.6	54	5.4	15	13	67	13.4	0.37	This study
15	Changji	2013/03/27	+5.40	00.00	5.0	5.4	(GCMT)	1.5	1.5	0.7	15.4	0.37	This study
										34	68	0.35	This study
											//.5 (Haskell)	0.05	Zhang
14	Lushan	2013/04/20	30.30	103.00	7	7.0	6.6	7.6	4.9		60		Wang, Chen,
							(GCMT)						et al. (2014)
												18	Li et al.,
	x 1											110	(2017)
15	Lushan (aftershock)	2013/04/20	30.28	102.93	4.8	4.2		0.7		3.3	6.6	0.19	This study
	Lushan										_		
16	(aftershock)	2013/04/20	30.25	102.83	4.7	4.6		0.8		3.5	7	0.12	This study
17	Lushan	2013/04/20	30.28	102.99	49	47		12		52	10.4	0.07	This study
17	(aftershock)	2013/04/20	50.20	102.77	ч.)	4.7		1.2		5.2	10.4	0.07	This study
18	Lushan (aftersheek)	2013/04/20	30.33	102.92	4.3	4.0		0.4		1.6	3.2	0.32	This study
	Lushan						54						
19	(aftershock)	2013/04/20	30.24	102.94	5.4	5.4	(GCMT)	3.3	1.2	14.6	29.2	0.02	This study
20	Lushan	2013/04/20	30.31	103.04	4.0	3.6		0.2		0.0	1.8	0.59	This study
20	(aftershock)	2013/04/20	50.51	105.04	4.0	5.0		0.2		0.7	1.0	0.57	This study
21	Lushan	2013/04/21	30.36	103.05	5.4	4.8	4.8	0.6	0.6	2.7	5.4	2.65	This study
	(aftersnock)						(GCMT)						
22	(aftershock)	2013/04/21	30.26	103.00	4.9	4.6	(GCMT)	1.4	0.8	6.1	12.2	0.04	This study
22	Lushan	2012/04/21	20.24	102.00	5.4	5.1	5.2	1.2	0.0	56	11.2	0.22	This study
23	(aftershock)	2013/04/21	30.34	105.00	5.4	3.1	(GCMT)	1.2	0.9	5.0	11.2	0.52	This study
										10.6	21.2	4.16	This study
24	Minuton	2012/07/22	24.54	104 21	67	6.6	6.0	2.4	2.4		11		Sun et al.,
24	winixian	2015/07/22	54.54	104.21	0.7	0.0	(GCMT)	2.4	2.4				Wang et al
											10		2014c
25	Manuar	2012/00/20	27 72	101 52	5.2	5 1	5.1	1.0	0.0	٨٢	0	0.41	This state
23	wienyuan	2015/09/20	51.15	101.55	5.5	5.1	(GCMT)	1.0	0.8	4.3	7	0.41	This study
										30.0	60	0.13	This study
26	Ludian	2014/08/03	27.11	103.33	6.6	6.5	6.2 (GCMT)	6.7	2.9		12		Cheng et al.,
							(GCIVIT)				12		et al., 2014d
27	Kangding	2014/11/22	30.29	101.68	6.4	6.2	6.1	2.2	2.8	9.8	19.6	1.85	This study

							(GCMT)				20		Fang et al., 2015b
											16		Jiang et al., 2015
											12		Yi et al., 2015
28	Kangding	2014/11/25	30.20	101.75	5.9	5.6	5.7 (GCMT)	0.7	1.8	3.2	6.4	9.02	This study
29	Jinggu	2014/12/06	23.32	100.50	5.9	6.0	5.5 (GCMT)	1.0	1.5	4.4	8.8	3.61	This study
30	Leshan	2015/01/14	29.30	103.20	5.0	4.8	4.9 (GCMT)	0.5	0.7	2.4	4.8	1.03	This study
31	Songming	2015/03/09	25.33	103.10	4.5	4.9	4.8 (GCMT)	0.2	0.6	1.1	2.2	1.94	This study
	MSPRED = Predicted Ms, SR = source radius, RL = rupture length =2*source radius, SSD = statics stress drop, GCMT data are available at <u>www.globalcmt.org</u> (last accessed May.6, 2020)												