Ion and electron heating at quasi-parallel bow shocks

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Abstract

Measurements from the Magnetospheric Multiscale (MMS) mission indicate that the density gradients associated with nonlinear compressional structures (shocklets) in a quasi-parallel bow shock trigger sequentially two instabilities that heat ions and electrons. The Lower-Hybrid-Drift (LHD) instability, triggered by the diamagnetic drift of ions, produces electric fields and ExB drift of electrons that triggers the Electron-Cyclotron-Drift (ECD) instability. Both instabilities create large amplitude electric fields $\sinh 20-200 \text{ mV/m}$ at wavelengths comparable to the electron gyroradius. Strong gradients of the electric field lead to stochastic heating of both ions and electrons, controlled by a dimensionless function $\c) = m.iq.i^{-1} B^{-2} \mathrm{div}(\mathbf{E}_-\perp)$, which represents a universal, non-resonant heating mechanism for particles species with mass m_i and charge $\ q_i$, independent of the type of waves and instabilities.

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5	Key Points:
6	• Density gradients of nonlinear compressional structures (shocklets) in quasi-parallel
7	shocks trigger the Lower-Hybrid-Drift (LHD) instability.
8	• The LHD instability creates fast ExB drifts of electrons, which trigger the Electron-
9	Cyclotron-Drift (ECD) instability.
10	• Both LHD and ECD instabilities create large amplitude electric fields, which via
11	a stochastic mechanism lead to ion and electron heating at shock waves.

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12 Abstract

Measurements from the Magnetospheric Multiscale (MMS) mission indicate that the den-13 sity gradients associated with nonlinear compressional structures (shocklets) in a quasi-14 parallel bow shock trigger sequentially two instabilities that heat ions and electrons. The 15 Lower-Hybrid-Drift (LHD) instability, triggered by the diamagnetic drift of ions, pro-16 duces electric fields and ExB drift of electrons that triggers the Electron-Cyclotron-Drift 17 (ECD) instability. Both instabilities create large amplitude electric fields $\sim 20-200 \text{ mV/m}$ 18 at wavelengths comparable to the electron gyroradius. Strong gradients of the electric 19 field lead to stochastic heating of both ions and electrons, controlled by a dimensionless 20 function $\chi = m_i q_i^{-1} B^{-2} \operatorname{div}(\mathbf{E}_{\perp})$, which represents a universal, non-resonant heating 21 mechanism for particles species with mass m_i and charge q_i , independent of the type of 22 waves and instabilities. 23

²⁴ Plain Language Summary

Collisionless shocks in space represent amazing natural phenomena associated with 25 a number of physical problems that attract a great deal of attention: turbulence, stochas-26 ticity, wave-particle interactions, nonlinear structures, shocklets, particle heating and ac-27 celeration. In astrophysics, shock acceleration is considered to be the primary acceler-28 ation mechanism. Using measurements from the Magnetospheric Multiscale (MMS) mis-29 sion we demonstrate that ion and electron heating at the bow shock is caused by a stochas-30 tic mechanism related to gradients of the electric fields produced by the Lower-Hybrid-31 Drift (LHD) instability and the Electron-Cyclotron-Drift (ECD) instability. 32

33 1 Introduction

Collisionless shocks in space represent amazing natural phenomena associated with a number of physical problems that attract a great deal of attention: turbulence, stochasticity, wave-particle interactions, nonlinear structures, shocklets, particle heating and acceleration. In astrophysics, shock acceleration is considered to be the primary acceleration mechanism. Wherever energetic particles are produced, shocks are either observed to occur or are expected to do so, e.g., solar flares, corotating interaction regions in the solar wind, supernovae remnants, and accreting binary systems.

The most investigated plasma shock wave is the terrestrial bow shock formed at 41 a distance of 14 R_E in front of the Earth, where the solar wind collides with the outer-42 most regions of the magnetosphere. It is well known that shocks thermalise incoming so-43 lar wind, and produce also some energetic particles. There are a variety of processes that 44 can heat and energise particles in a collisionless plasma. In reviews by Wu et al. (1984); 45 Gary (1993); Treumann (2009); Burgess et al. (2012) one can find a long list of insta-46 bilities that could play a role in ion and electron heating – however, insufficient support 47 from observations put the question on the dominant mechanism into inconclusive state. 48

On the basis of measurements from the Magnetospheric Multiscale MMS mission 49 (Burch et al., 2016), it has been shown (Stasiewicz, 2020) that particle heating at quasi-50 perpendicular bow shocks is related to two drift instabilities: the Lower-Hybrid-Drift, 51 and the Electron-Cyclotron-Drift instability. The LHD instability is a cross-field current-52 driven instability generated on the density gradients, when the diamagnetic drift of ions 53 (assumed protons) $V_d = T_p (m_p \omega_{cp} L_n)^{-1} = v_{tp} (r_p / L_n)$ is comparable to the thermal ion speed, $v_{tp} = (T_p / m_p)^{1/2}$, or equivalently when the scale of the density gradient $L_n = (N^{-1} |\nabla N|)^{-1}$ is comparable to the ion cyclotron radius $r_p = v_{tp} / \omega_{cp}$. Here, T_p , m_p , ω_{cp} 54 55 56 are proton temperature, mass, and cyclotron frequency. The maximum growth rate is 57 at $k_{\perp}r_e \sim 1$, i.e., at wavelengths of a few electron gyroradii (Davidson et al., 1977; Huba 58 et al., 1978; Daughton, 2003). 59

The LHD instability creates electric fields, which lead to strong ExB drifts of elec-60 trons only, because ions are not subject to this drift due to the large gyroradius in com-61 parison to the width of drift channels, and also due to frequency much greater than the 62 ion gyrofrequency. When the electron drift speed becomes comparable to the thermal 63 speed, $V_E \sim v_{te}$, the ECD instability is initiated, which produces shorter wavelengths 64 and occurs at the resonance $k_{\perp}V_E \sim n\omega_{ce}$ that couples electron Bernstein modes with 65 ion-acoustic waves (Forslund et al., 1972; Lashmore-Davies, 1971; Muschietti & Lembége, 66 2013). The ECD waves have been identified at the bow shock in measurements from STEREO. 67 Wind and MMS (Wilson III et al., 2010; Breneman et al., 2013; Goodrich et al., 2018). 68 It is interesting to note that the same ExB drift of electrons excites the ECD instabil-69 ity in space and in Hall ion thrusters (Boeuf & Garrigues, 2018). 70

These two instabilities generate large amplitude electric fields 20–200 mV/m on short spatial scales ($\sim r_e$) that perturb orbits of gyrating ions and electrons by breaking the magnetic moments and causing chaotic particle movements. This facilitates efficient stochastic heating by the present electric fluctuations, and even by the DC field. The condition for stochastic heating of particles with mass m_i , charge q_i is (Stasiewicz, 2020)

$$\chi_i(t, \mathbf{r}) = \frac{m_i}{q_i B^2} \operatorname{div}(\mathbf{E}_\perp); \ |\chi_i| > 1.$$
(1)

This condition with divergence reduced to the directional gradient $\partial_x E_x$, has been used 76 by several authors to explain heating of particles in laboratory and space (Cole, 1976; 77 McChesney et al., 1987; Karney, 1979; Balikhin et al., 1993; Gedalin et al., 1995; Mishin 78 & Banaszkiewicz, 1998; Stasiewicz et al., 2000; Stasiewicz, 2007; Vranjes & Poedts, 2010; 79 Stasiewicz et al., 2013; See et al., 2013; Yoon & Bellan, 2019). The heating function can 80 be regarded as a quantitative measure of the demagnetisation of the particle species m_i . 81 It is also related to the charge non-neutrality, because $\chi = (N_c/N)(c^2/V_{Ai}^2)$, where $V_{Ai}^2 =$ 82 $B^2/(\mu_0 N m_i)$, upon substitution div $(\mathbf{E}) = N_c q_i/\epsilon_0$. However, only \mathbf{E}_{\perp} is put into (1) 83 to exclude modes with E_{\parallel} , like Langmuir or ion acoustic waves that do not contribute 84 to the stochasticity. 85

The scenario outlined above has been deduced from the analysis of MMS measurements at a quasi-perpendicular shock, so it would be interesting to check whether it is applicable also for quasi-parallel shocks, which is the purpose of this Letter.

⁸⁹ 2 Observations

We use here plasma parameters provided by the Fast Plasma Investigation (Pollock et al., 2016) on MMS, measurements of the electric field (Lindqvist et al., 2016; Ergun et al., 2016; Torbert et al., 2016) and the magnetic field measured by the Fluxgate Magnetometer (Russell et al., 2016).

When the interplanetary magnetic field is in the direction quasi-parallel to the shock 94 normal, instead of a single ramp of the perpendicular bow shock, an extended foreshock region is formed, filled with nonlinear compressional structures (shocklets) similar to those 96 shown in Fig. 1a. These shocklets have spatial scales of $\sim 1,000$ km and represent com-97 pressions of the plasma density and the magnetic field by a factor 2-10 times the back-98 ground values (Schwartz & Burgess, 1991; Stasiewicz et al., 2003; Lucek et al., 2008; Wil-99 son III et al., 2013). The large amplitude shocklets are standing against the solar wind 100 flow and move with respect to spacecraft with speed of ~ 10 km/s. In the vicinity of 101 the shocklets in Fig. 1a we observe intense electron heating shown in panel 1b (increase 102 of T_e by a factor of 4), and the ion heating shown in panel 1c (increase of $T_i = T_p$ by 103 a factor of 8). 104

Figure 1a indicates presence of strong gradients of the density, so we expect that the region may be unstable for the LHD instability. To verify that this is the case we compute the gradient scale $L_N = (N^{-1}|\nabla N|)^{-1}$ for the plasma density using a gen-



Figure 1. MMS-1 measurements from a 3.5 min time interval of a quasi-parallel bow shock: (a) magnetic field B, and electron number density N that form large amplitude compressional structures (shocklets) – typical for parallel shocks. Perpendicular and parallel temperatures of electrons (b), and ions (c) exhibit spectacular heating events.

eral method for computing gradients from 4-point measurements developed for Cluster (Harvey, 1998). The same method is applied to compute div(\mathbf{E}_{\perp}), used in the function χ . This function is computed with the electric field in the frequency range 0.15-4096 Hz. The lowest frequencies were removed to avoid DC calibration offsets and possible effects of the satellite spin period (f=0.05 Hz, and harmonics). The mean characteristic frequencies in this interval are: the proton cyclotron $f_{cp}=0.2$ Hz, the lower hybrid $f_{lh}=7$ Hz, the electron cyclotron $f_{ce}=300$ Hz, and the proton plasma $f_{pp}=620$ Hz.

The result of L_N determination is shown in Fig.2a. In most of the region, $L_N/r_p < 1$, indicating that the region is strongly unstable for the LHD instability.

In the next step, we compute $V_E = \mathbf{E} \times \mathbf{B}/B^2$ to check if electrons are prone to the ECD instability. The result in panel 2b shows that in a significant part of the region we have condition $V_E > v_{te}$, that would produce strong ECD instability. The ExB drift is computed with the full spectrum of the measured electric field, including frequencies $> f_{ce}$, which would invalidate the drift approximation. Therefore it should not be assumed that bulk electrons attain everywhere the computed values of V_E .

The electric fields developed by LHD and ECD instabilities (maximum = 220 mV/m) 123 produce stochastic heating function χ shown in panel 2c that has maximum value $\chi =$ 124 $\chi_p=11,355$, computed with the proton mass. This is equivalent to the electron $\chi_e=6.1$, 125 indicating favourable conditions for strong stochastic heating of electrons, which is in-126 deed observed in Fig. 1b. Because the separation of the MMS constellation is about 15 127 km, we cannot properly compute gradients on scales less than 10 km, which means that 128 the computed values of χ may underestimate the real ones, because the ECD waves are 129 expected to have wavelengths on the order of the electron cyclotron radius $\sim 1 \text{ km}$ (Muschietti 130 & Lembége, 2013). Other errors in derivation of χ are the same as in measurements of 131 the electric field, i.e. ca 10% (Torbert et al., 2016). 132



Figure 2. Diagnostic parameters for the case of Fig. 1: (a) The gradient scale of the plasma density L_N is normalised with thermal ion gyroradius r_p (mean = 250 km). $L_N/r_p < 1$ implies that the region is strongly unstable for the LHD instability. (b) The computed ExB drift normalised with the electron thermal speed v_{te} (mean = 2300 km/s). $V_E/v_{te} > 1$ implies that the region is strongly unstable for the ECD instability. (c) Function χ (maximum = 11,355) derived from the data with equation (1) for the electric field 0.15–4096 Hz, and the proton mass, m_p .

Minima of L_N in Figure 2a correspond to the maxima of V_E in panel 2b, and also 133 with maxima of the heating function in panel 2c. This indicates that the heating of both 134 ions and electrons is initiated by the LHD instability on density gradients that evolves 135 in place into the ECD instability created by V_E drifts, as seen in panel 2b. It is also seen 136 that the regions with $L_N/r_p > 4$ have reduced V_E in panel 2b (weak electric field), and 137 small values of the heating function in panel 2c. This means that the observed onset of 138 the LHD instability is surprisingly close to the theoretical threshold, $L_N/r_p < (m_p/m_e)^{1/4} \approx$ 139 6, derived some 40 years ago (Huba et al., 1978). 140

Generally, all diagnostic parameters shown in Figure 2 are consistent with the heating observed in Figure 1, and also with the scenario described in the Introduction. The highest temperatures of electrons in Fig. 1b correspond to $\chi_e=6.1$ in Fig. 2c, which clearly associates electron heating with function χ .

In the following we shall investigate in detail properties of waves responsible for electron and ion heating observed in Fig. 1.

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2.1 Electron heating and ECD waves

In Figure 3 we show some details of the electron heating event from Fig. 1b. The maximum of the electron temperature corresponds to $\chi_e = 6.1$. Such a large value for the heating function is related to the local minimum of B. Heating of both electrons and ions (see also Fig. 6) occur preferentially in the local minima of B, consistent with χ as the controlling function, because of dependence $\chi \propto B^{-2}$. Quenching of the heating at B > 20 nT is also consistent with this mechanism.



Figure 3. Zoom (30 s) of the electron heating event from Fig. 1: (a) Electron and ion temperatures $(T_{i\perp}/10)$, (b) χ function, (c) magnetic field *B*.



Figure 4. Waves measured by MMS-1 in the region of Fig. 3. The electric field perpendicular component $E_{y\perp}$ is decomposed in discrete frequency dyads in the range 256–4096 Hz that correspond to the Electron-Cyclotron-Drift waves.



Figure 5. Continuation of Fig. 4 to lower frequencies that cover Lower-Hybrid-Drift waves, 8–128 Hz.

Figure 4 shows the measured signal $E_{u\perp}$ decomposed into discrete frequency dyads 154 with orthogonal wavelets (Mallat, 1999). Orthogonality means that the time integral of 155 the product of any pair of the frequency dyads is zero, and the decomposition is exact, 156 i.e., the sum of all components gives the original signal. This frequency range corresponds 157 to the Electron-Cyclotron-Drift waves that start around $f_{ce} \sim 300$ Hz and extend to the 158 upper frequency of the measurements. The border frequencies should not be regarded 159 as strict, because Doppler shifts of short wavelengths would produce considerable spread 160 and overlap of modes. The labels on the v-axis represent dyad numbers, and the unit 161 range corresponds to the amplitude 50 mV/m. Waves in this frequency range have been 162 analyzed with use of high-time resolution measurements obtained by THEMIS (Mozer 163 & Sundqvist, 2013; Wilson III et al., 2014), who noted large parallel electric field com-164 ponents in these modes and attributed it to ion acoustic waves. The presence of elec-165 tron cyclotron harmonics in the spectra has led to their identification as ECD waves (Wilson 166 III et al., 2010; Breneman et al., 2013; Goodrich et al., 2018; Stasiewicz, 2020). 167

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2.2 Ion heating and LHD waves

Figure 5 is the extension of Fig. 4 to lower frequencies covered by Lower-Hybrid-Drift waves that start from $f_{lh} \sim 7$ Hz and extend to f_{ce} . They exhibit perpendicular direction for the Poynting flux and rapidly diminishing magnetic component with increasing frequency. Obliquely propagating whistler and/or magnetosonic waves are also observed in this region at frequencies below f_{lh} . LH and LHD waves have been observed also in other regions of the magnetosphere (Bale et al., 2002; Vaivads et al., 2004; Norgren et al., 2012; Graham et al., 2017).

The LHD waves in Fig. 5 maximise at the minima of L_N , i.e., at the maxima of 176 the density gradients, and have theoretical maximum growth rate at $k_{\perp}r_e \sim 1$. The elec-177 tric field of these waves generates ExB drift of electrons that ignites the ECD instabil-178 ity via the resonance $k_{\perp}V_E \sim n\omega_{ce}$. This resonance condition can be expressed equiv-179 alently by $k_{\perp}r_e \sim nv_{te}/V_E$, which means that the ECD waves resonate/couple with struc-180 tures created by the LHD instability, $k_{\perp}r_e \sim 1$ when $nv_{te}/V_E = 1$. There is smooth 181 transition and co-location of LHD, and ECD waves, seen in Figures 4,5 which is possi-182 bly related to the matching condition between these two instabilities. The n=1 ECD mode 183



Figure 6. Zoom at the ion heating event from Fig. 1: (a) Ion temperature, (b) χ function, (c) magnetic field *B*. Note that heating occurs preferentially in depressions of *B*, consistent with Equation (1).

can be naturally excited in drift channels created by the LHD instability when $V_E = v_{te}$.

In Figure 6 we concentrate on the ion heating event from Fig. 1c. The ion heating is remarkably strong in this event but the amplitude of LHD waves in this case is only ~10 mV/m, significantly smaller than for waves shown in Fig. 5. The heating function is, however, quite large because *B* drops below 5 nT in this case. Ions perturbed stochastically by $\chi_p \gg 1$ can be energised either by fluctuating, wave fields, and/or by the DC field,

$$\Delta W = q_i \langle \mathbf{v} \cdot (\mathbf{E}_0 + \delta \mathbf{E}) \rangle. \tag{2}$$

The quasi-DC field (below $f_{cp} \approx 0.2$ Hz) in this region is $E_0 \sim 2.5$ mV/m, while the gy-192 roradius is $r_p \sim 800$ km. On the distance of r_p we have potential of 2000 V, sufficient 193 to explain the observed energisation of ions. The stochastic acceleration on fluctuating 194 fields would represent a diffusive process, requiring longer times with statistically sig-195 nificant number of interactions, while the DC acceleration, or generally by the electric 196 field of waves with frequencies lower than the gyrofrequency and wavelengths larger than 197 the gyroradius, could be a rapid, single step event (Stasiewicz, 2007). In this model a 198 cold particle is convected on a single $\partial_x E_x$ structure and acquires large gyroradius af-199 ter encounter. The perpendicular energisation is done by the convection potential after 200 stochastic demagnetisation by $\chi > 1$. Details of the heating process, the relative im-201 portance of the DC- and wave- acceleration, dependence on the ratio of scales of the struc-202 tures/gyroradius, and the frequency of waves/gyrofrequency can be resolved by suitable 203 simulations, which will be the subject of a separate publication. 204

205 **3** Conclusions

The analysis of the MMS measurements leads to the following conclusions on the heating mechanism at quasi-parallel shock waves: Large amplitude shocklets, i.e., compressions of N and B observed at quasi-parallel shocks are associated with density gradients on spatial scales exceeding the threshold for the onset of the Lower-Hybrid-Drift instability, $L_N < r_p$.

The LHD instability creates electric fields, $E \sim 20 \text{ mV/m}$ in the frequency range $[f_{lh}, f_{ce}]$, that cause ExB drift of electrons in narrow channels, $k_{\perp}r_e \sim 1$, with speed $V_E > v_{te}$, that leads to the Electron-Cyclotron-Drift instability.

The ECD instability creates larger electric fields, $E \sim 200 \text{ mV/m}$ at frequencies $f \geq f_{ce}$, on wavelengths $\sim r_e$, and smaller, Doppler spread over wide frequency range.

Large gradients of the electric fields created by LHD and ECD instabilities produce conditions such that the heating functions (1) become $\chi_p \gg 1$, and $\chi_e \gg 1$, which leads to the stochastic heating of ions and electrons.

The non-adiabatic heating of ions and electrons occurs preferentially at the local minima of B, consistent with Equation (1).

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Figure1.



Figure2.



Figure3.



Figure4.



Figure5.



Figure6.

