Statistical Study of Chorus Modulations by Background Magnetic Field and Plasma Density

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Abstract

In this study, we use observations of THEMIS and Van Allen Probes to statistically study the modulations of chorus emissions by variations of background magnetic field and plasma density in the ultra low frequency range. The modulation events are identified automatically and divided into three types according to whether the chorus intensity is correlated to the variations of magnetic field only (Type B), plasma density only (Type N) or both (Type NB). For THEMIS observations, the occurrences of the types B and N are larger than type NB, while for Van Allen Probes observations most events are Type N. The chorus intensity is mostly correlated to the magnetic field strength negatively and plasma density positively. Modulation event occurrences peak at the dawn sector. The chorus intensity tends to increase when the magnitude of the magnetic field perturbation increases, but little dependence on the amplitude of plasma density perturbation is found.

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X - 2 XIA ET AL.: STATISTICAL STUDY OF CHORUS MODULATION In this study, we use observations of THEMIS and Van Allen Abstract. 3 Probes to statistically study the modulations of chorus emissions by vari-4 ations of background magnetic field and plasma density in the ultra low fre-5 quency range. The modulation events are identified automatically and di-6 vided into three types according to whether the chorus intensity is correlated 7 o the variations of magnetic field only (Type B), plasma density only (Type 8 N) or both (Type NB). For THEMIS observations, the occurrences of the 9 types B and N are larger than type NB, while for Van Allen Probes obser-10 vations most events are Type N. The chorus intensity is mostly correlated 11 to the magnetic field strength negatively and plasma density positively. Mod-12 ulation event occurrences peak at the dawn sector. The chorus intensity tends 13 to increase when the magnitude of the magnetic field perturbation increases, 14 but little dependence on the amplitude of plasma density perturbation is found. 15

1. Introduction

Whistler-mode chorus emissions in the magnetosphere are right-hand polarized electro-16 magnetic waves generated near the geomagnetic equator outside the plasmasphere [?????]. 17 The chorus waves are usually separated into two frequency bands: the lower band from 18 0.1 to 0.5 f_{ce} and the upper band from 0.5 to 0.8 f_{ce} , where f_{ce} is the equatorial electron 19 cyclotron frequency [???]. The excitation of chorus waves is generally believed to involve 20 cyclotron resonance with anisotropic (nonuniform temperature distribution in different 21 directions) electrons that are usually injected from the plasma sheet into the inner mag-22 netosphere during geomagnetically active times [???]. The interactions between chorus 23 waves and particles are very important to the magnetospheric dynamics, including ac-24 celeration of electrons to relativistic energy level through energy diffusion [??????] and 25 precipitation of energetic electrons through pitch angle scattering [???]. The precipitating 26 electrons can penetrate into the atmosphere and produce both diffusive [e.g., ???] and 27 pulsating auroras [e.g., ????]. 28

Statistical studies indicate that the intensity and occurrence of chorus waves usually 29 increase under higher geomagnetic activity levels [???] and around the dawn sector (be-30 tween midnight and noon) [??????]. A recent study also shows a strong dependence of 31 chorus wave intensity on the solar wind parameters: the intensity increases during the 32 periods of higher solar wind speed and southward interplanetary magnetic field [?]. The 33 wave power spectra of chorus waves are often observed as on-off discrete elements with a 34 time scale of about a tenth to a few tenths of seconds [?]. Those discrete elements merge 35 together on a timescale from a few seconds to a few minutes, over which the averaged 36

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intensity can be modulated by the variations of background magnetic field and plasma 37 density [??????]. One primary source of the oscillations of background magnetic field and plasma density is Pc 4-5 ultra low frequency (ULF) waves, which were reported to 39 modulate the chorus intensity in both large L-shell (8 to 12) region [?] and the inner 40 magnetosphere [?]. In these two studies, the intensities of chorus waves show a positive 41 correlation with plasma density and a negative correlation with the background magnetic 42 field. The negative correlation between chorus intensity and plasma density in the ab-43 sence of ULF waves has also been observed [?]. The modulated chorus emission can lead 44 to modulated electron precipitation and the consequent pulsating aurora [??]. Under-45 standing the chorus modulation is of importance to interpret the process of whistler mode 46 wave excitation and the characteristics of pulsating aurora. 47

Despite existing event studies, the statistical relationship between fluctuations of mag-48 netic field and density and the variation of chorus emission intensity remains to be ex-49 plored. In this study, we use roughly 41 satellite-year observation in the inner mag-50 netosphere to build a database of chorus modulation events and statistically study the 51 relationships between the chorus emissions and perturbations of background magnetic 52 field and plasma density. The organization of the paper is as follows. Section 2 introduces 53 the THEMIS and Van Allen Probes satellites and corresponding instruments used. Sec-54 tion 3 describes the methods to automatically identify the chorus modulation events and 55 to sort the events into different categories. Section 4 shows the occurrences and spatial 56 distributions of different types of modulation events, and Section 5 gives a quantitative 57 analysis of the relationship between the chorus intensity and amplitudes of background 58 magnetic field and plasma density perturbations. 59

2. Spacecraft and Instruments

The Time History of Events and Macroscale Interactions during Substorms (THEMIS) 60 mission is a constellation of five identically-instrumented satellites, which started in Febru-61 ary 2007. Three of the satellites (THA, THD, and THE) are inner probes in nearly equa-62 torial orbits with apogees of 10-13 R_E and perigees below 2 R_E [?], suitable to observe 63 chorus waves outside the plasmasphere. The Fluxgate Magnetometer (FGM) [?] measures 64 the background magnetic fields and their low-frequency fluctuations (up to 64 Hz). The 65 Electric Field Instrument (EFI) measures three components of electric fields as well as 66 individual sensor potentials, providing onboard and ground-based estimate of spacecraft 67 floating potential and plasma density [??]. The Search Coil Magnetometer (SCM) [??] 68 provides the measurements of three components of wave magnetic fields with a frequency 69 range from 0.1 Hz to 4 kHz. The waveforms measured by EFI and SCM are digitized 70 and processed by the Digital Fields Board (DFB) [?] and finally transformed into two 71 types of spectral products: filter bank data (FBK) and Fourier power spectra (FFT). The 72 filter bank data are meant for survey-type monitoring of wave power, which has broad 73 frequency bands and relatively low time resolution. The THEMIS wave data used in this 74 study is the FBK magnetic spectra. 75

The Van Allen Probes (or Radiation Belt Storm Probes (RBSP)) [?] consist of two satellites with identical instruments with nearly similar near-equatorial highly elliptical orbits with perigee about 620 km and apogee about 5.8 R_E . The Electric and Magnetic Field Instrument Suite and Integrated Science (EMFISIS) [?], equipped with a triaxial fluxgate magnetometer (MAG) and a triaxial AC magnetic search coil magnetometer (MSC), can provide the measurement of wave magnetic field in frequency range between ⁸² 10 Hz and 400 kHz as well as the background magnetic field. The Electric Field and ⁸³ Waves Suite (EFW) [?], consisting of 4 spin-plane electric field antennae and 2 spin-axis ⁸⁴ tubular extendable booms, can provide not only the measurement of the electric field but ⁸⁵ also estimation of cold plasma densities above 10 cm⁻³ from spacecraft potential. Also, ⁸⁶ the EMFISIS Upper Hybrid resonance (UHR) lines can help to calibrate empirical plasma ⁸⁷ density-potential formula and improve the measurement of plasma density [e.g., ?].

In this study, 10-year measurement of the three inner THEMIS satellites from 2008/01/01 to 2017/12/31 and 5.5-year measurement of the two Van Allen Probe satellites from 2012/09/15 to 2018/05/30 are used. In total, roughly 41 satellite-year measurement is used.

3. Identification of Modulation Events

In this section, we first introduce automatic detection of the modulation events from the 92 observations of THEMIS and Van Allen Probes. The detection is achieved by calculating 93 the two correlation coefficients: C_B between the background magnetic field, B_0 , and 94 logarithm value of the chorus wave root mean square amplitude, $\log B_w$, and C_N between 95 the background plasma density N_0 and $\log B_w$. The value of B_w is the square root of the 96 integration of the wave magnetic field spectral density over the frequency band from 0.1 97 to 0.8 electron cyclotron frequency f_{ce} . Calculation of the correlation coefficients is done 98 over time intervals with high chorus wave amplitude outside the plasmasphere. First, we 99 only perform the detection procedure outside the plasmasphere, which can be achieved by 100 excluding the observation with corresponding plasma density larger than 10 cm^{-3} . Second, 101 we select time intervals (with duration T_e) when the wave magnetic field amplitude B_w 102 is at least twice the background value (which is obtained from the daily median value of 103

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 B_w with gradient of $log_{10}(B_w) < 0.02$ nT). Third, for the selected intervals with duration 104 T_e longer than 36 seconds, we calculate the two correlation coefficients C_B and C_N in the 105 time window of $2T_e$ (extending the identified T_e interval backward and forward by 0.5 T_e 106 respectively). The coefficient calculation over the extended interval ensures that a high 107 correlation coefficient really corresponds to a modulation event of interest. Finally, the 108 time intervals with the absolute value of either C_B or C_N larger than 0.6 are recognized 109 as modulation events. The minimum time window of 36 seconds is used because this time 110 period lies in the ULF Pc 3 and Pi 1 bands and because this time period is a common 111 multiple of the sampling periods of the wave data used of the two satellite missions, 4 112 seconds for THEMIS FBK data and 6 seconds for Van Allen Probe EMFISIS data. 113

According to the values of C_B or C_N , we sort the modulation events into 3 types and 114 8 subtypes. The three types are Type B with only high C_B absolute value; Type N with 115 only high C_N absolute value; Type NB with both high C_B and C_N absolute values. For 116 Type B and Type N, there are subtypes B^+ and N^+ with positive C_B and C_N values 117 respectively and subtypes B^- and N^- with negative C_B and C_N respectively. For Type 118 NB, the four subtypes are N⁺B⁺ with both positive C_B and C_N ; N⁻B⁺ with positive C_B 119 and negative C_N ; N⁺B⁻ with negative C_B and positive C_N ; N⁻B⁻ with both negative 120 C_B and C_N . Examples of the eight subtypes of modulation events observed by THEMIS 121 are shown in Figures 1a-1h. For each subplot, the upper panel shows the variations of B_0 122 (blue line) and N_0 (red line) while the lower panel shows the magnetic power spectrum 123 density (colored spectrum) and the variation of B_w (red line). The white solid, dashed 124 and dot-dash lines denote the variations of f_{ce} , $0.5f_{ce}$ and $0.1f_{ce}$, respectively. 125

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4. Distribution of Modulation Events

After surveying THEMIS observations from Jan 2008 to Dec 2017, a total of 50851 126 modulation events are identified. For Van Allen Probes observation from September 2012 127 to May 2018, 3795 modulation events are identified. Now we sort these events into three 128 types and eight subtypes and analyze the spatial distribution of the modulation events 129 and compare the occurrences of different types of modulation events. The panels on the 130 left side of Figure 2 show those statistical results of the 50851 modulation events from 131 the THEMIS observation. Figures 2a - 2d exhibit the spatial distribution of modulation 132 event occurrence rate in the logarithm scale for all the modulation events, type B, type N 133 and type NB events respectively. The occurrence rate here, for a given spatial bin in MLT 134 and L, is calculated as the ratio of the total time interval of the identified modulation 135 events inside this bin to the total dwell time of the satellite inside the same bin. For the 136 MLT distribution of type B and NB events which both involve the modulation effect of 137 the background magnetic field, the modulation event occurrence maximizes at the dawn 138 sector and minimizes near the midnight. There also exists a secondary peak in the dusk 139 sector. However, for the type N events that involve only the modulation by plasma density, 140 the MLT distribution is relatively uniform, compared with that of type B and NB events. 141 The radial distribution peaks at L = 11-12 and decreases as L decreases for type B and 142 NB events, while for type N event, the radial dependence is weaker. For the region outside 143 L = 12, few observations due to the limit of THEMIS orbit are made and thus information 144 about the distribution of modulation events cannot be reliably obtained. Figure 2e shows 145 how chorus modulation is divided among the different types. The portions of the three 146 types of events are 39.9%, 43.1%, and 17.0% for type B, N and NB events respectively. 147

Most of the type B events are subtype B⁻ with negative C_B (29.6% of all the modulation 148 events) while most of the type N events are subtype N⁺ with positive C_N (33.3% of all 149 the modulation events). For type NB events, the main subtype is N^+B^- (10.5%), which 150 can be treated as the combination of subtype B^- and N^+ . Those proportions suggest that 151 the chorus wave amplitude is more likely modulated by background magnetic field with 152 negative correlation or by the plasma density with positive correlation. These modulation 153 relations are consistent with those of the ULF wave modulation events reported in the 154 outer [?] and inner magnetosphere [?]. 155

Besides the statistical study of THEMIS data, we also perform a similar analysis on the 156 measurements of Van Allen Probes from September 2012 to May 2018. The statistical 157 results of Van Allen Probes data are plotted in the right column of Figure 2. Due to the 158 orbit of Van Allen Probes, most of the 3798 events are detected within $L = \sim 6$, which 159 greatly supplement the THEMIS observation of the events mostly at the outer L-shell. 160 From the distribution of the proportions of different types of events shown by Figure 161 2j, we can see that most of the modulation events (64.1%) are type N⁺, with positively 162 correlated plasma density only. Also, there is a considerable number of type N^- events 163 (12.8%) while the portion of the combined other types corresponding to the background 164 magnetic field variation is about 23%. This proportion distribution may be due to the 165 fact that the Van Allen Probes travel in the spatial region of relatively small L where the 166 perturbations of plasma density are more frequent than the perturbations of background 167 magnetic field. Looking into the MLT distribution of event occurrence rate, most of the 168 events occur uniformly over a broad region from pre-midnight to pre-dusk region. For the 169

radial distribution, most of the events occur near $L = \sim 6$ and the event number decreases as L decreases.

Combining the results of both THEMIS and Van Allen Probes measurements, at larger 172 L shell region (L > 10), most of the modulation events take place around the dawn sector 173 while for regions of small L shell (L < 10), the MLT distribution of the modulation events 174 become more uniform. Both THEMIS and Van Allen Probes measurements indicate that 175 the number of modulation events decreases as L decreases. The occurrence rate near 176 L = 6 obtained from THEMIS measurement and Van Allen Probes measurement are very 177 close (~ $10^{-3} - 10^{-2}$), which shows a consistency between the observations of the two 178 satellite missions. 179

5. Effects of Density and Magnetic Field Perturbations' Amplitudes

We have demonstrated that the intensity of the chorus wave can be modulated by 180 the perturbations of the background magnetic field and plasma density. For modulation 181 events, the relation between the intensity of the chorus wave and the amplitudes of the os-182 cillations also needs to be investigated quantitatively to better understand the mechanism 183 of the modulation events. To achieve this goal, we find out the maximum amplitudes of 184 the chorus waves for all the modulation events, calculate the standard deviations of the 185 corresponding variations of background magnetic field and plasma density, and analyze 186 the quantitative relation between the maximum wave amplitudes and the deviations. 187

Figures 3a and 3b show the relationship between the logarithm values of chorus wave amplitudes and the logarithm values of standard deviations of background magnetic field for events observed by THEMIS satellites with positive C_B (subtypes B⁺, N⁺B⁺ and N⁻B⁺) and negative C_B (subtypes B⁻, N⁺B⁻ and N⁻B⁻) respectively. The chorus wave

amplitudes and the magnetic field standard deviations are normalized by the mean back-192 ground magnetic field over the corresponding event interval. The blue dots stand for type 193 B events with only background magnetic field modulation (subtype B^- in 3a and B^+ in 194 3b) while the black dots are type NB events with both background magnetic field and 195 plasma density modulations (subtypes N^+B^+ and N^-B^+ in 3a; N^+B^- and N^-B^- in 3b). 196 The blue and black solid lines are linear fitting lines for dots with corresponding colors 197 and the dashed lines outline the boundaries of the corresponding 95% predicting intervals 198 (obtained by $y \pm 2\Delta$, where y is the predicted value of the linear fit and Δ is the stan-199 dard error for prediction). In Figure 3b, the dots of the two different colors concentrate 200 near the corresponding fitting lines with correlation coefficients of 0.65 (blue dots) and 201 0.70 (black dots), which indicates strong positive correlations between the intensity of 202 chorus wave and the standard deviations of background magnetic field. The two corre-203 sponding fitting lines in the figure denotes two relations of $B_w/B_0 = 10^{-2.07} (\sigma_B/B_0)^{0.57}$ 204 and $B_w/B_0 = 10^{-2.10} (\sigma_B/B_0)^{0.57}$ for the blue and black dots, respectively. The correla-205 tions in Figure 3a are weaker with correlation coefficients of 0.51 (blue dots) and 0.37206 (black dots) with two corresponding fitting lines denoting $B_w/B_0 = 10^{-2.39} (\sigma_B/B_0)^{0.48}$ 207 and $B_w/B_0 = 10^{-2.65} (\sigma_B/B_0)^{0.34}$ for the blue and black dots, respectively. These positive 208 correlations suggest that stronger oscillations of the background magnetic field (larger 209 magnitude) tend to result in more intense chorus waves, especially for the events with 210 negative C_B . Figures 3c and 3d show the relationship between the logarithm values of 211 normalized chorus intensity and the logarithm values of normalized standard deviations 212 of plasma density (normalized by the mean plasma density over the event interval) for 213 events observed by THEMIS satellites with positive C_N (subtypes N⁺, N⁺B⁺ and N⁺B⁻) 214

and negative C_N (subtypes N⁻, N⁻B⁺ and N⁻B⁻) respectively. The red dots stand for 215 type N events with only plasma density modulation (subtype N^+ in 3c and N^- in 3d) 216 while the black dots are type NB events with both background magnetic field and plasma 217 density modulations (subtypes N^+B^+ and N^+B^- in 3c; N^-B^+ and N^-B^- in 3d). The 218 effect of plasma density oscillation amplitude on chorus intensity is not as significant as 219 that of background magnetic field since the data dots distribute more uniformly and the 220 correlation coefficients for Figures 3c and 3d are all very low (absolute values $\langle 0.15 \rangle$). 221 Figures 3e-3h show the analysis results for observations of the Van Allen Probes in 222 the same format as Figures 3a-3d. The effect of magnetic field oscillation is noticeable 223 (Figures 3e and 3f) but not as significant as that in Figure 3b due to lack of measurements 224 of events with modulation by the magnetic field. The effect of plasma density is still very 225 weak (Figures 3g and 3h) from the results of Van Allen Probes' observations. In sum, 226 the results from these two magnetospheric satellites missions indicate the chorus intensity 227 increases when the amplitude of background magnetic field perturbation increases, but 228 does not show a clear dependence on the amplitude of plasma density perturbation. 229

6. Conclusions and Discussion

In this study, we use nearly ten years of observations of three THEMIS satellites (A, D, E) and over 5.5 years of observations of two Van Allen Probes (A, B) to statistically study the modulations of chorus emissions by background magnetic field and density oscillations. The modulation events are identified automatically by calculating the correlation coefficients between the magnetic field strength (and plasma density) and the chorus emission intensity (calculated by integrating the magnetic wave power spectral density from 0.1 to 0.8 electron cyclotron frequency f_{ce}). The modulation events are divided into three types according to whether the chorus intensity is highly correlated to the variations of magnetic field strength (type B), plasma density (type N), or both (type NB). The three types are also sorted into eight subtypes according to the sign of correlation coefficients. The oc-

²⁴⁰ currence rates and the proportions of the three types of modulation events are analyzed.
²⁴¹ Finally, we analyze the relationships between chorus wave amplitudes and amplitudes of
²⁴² the magnetic field and plasma density perturbations, respectively. The conclusions are
²⁴³ listed below:

1. The proportions of types B and N are comparable ($\sim 2/5$ of total events) and slightly larger than that of type NB ($\sim 1/5$) for the THEMIS observations, while for the Van Allen Probes observations at relatively smaller L-shell most of the events are type N.

247 2. The chorus intensity is mostly correlated to the magnetic field strength negatively
 248 and plasma density positively.

3. The occurrence rate of the modulation events is favored on the dawn sector for all
 the three types and at higher L-shell.

4. For the modulation events, chorus intensity is larger when the amplitude of the
 magnetic field perturbation is larger but has no clear dependence on the amplitude of
 plasma density perturbation.

²⁵⁴ We have also tested modulation event identification with a different critical C_N and ²⁵⁵ C_B value (0.8) and the plasmapause identification with a different critical density ²⁵⁶ (100 cm^{-3}). As a result of the two tests, the event number decreases and increases ²⁵⁷ respectively. However, these do not affect our main conclusions about the spatial distri-²⁵⁸ bution of the modulation events and the relationship between the chorus intensity and ²⁵⁹ the amplitude of the background parameter perturbations.

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The linear theory ? could partially explain the excitation of chorus waves especially for 260 small amplitude chorus waves. As discussed in ??, the mechanism of chorus modulation 261 by compressional ULF waves corresponding to the linear growth rate can be decomposed 262 as the changes of the ratio between the resonant electrons and the total electrons $R(V_R)$ 263 $(V_R = \frac{\omega - |\Omega_e|}{k}$ is the nonrelativistic, parallel velocity of electrons that interact with whistler 264 waves through the first order resonance, where ω is the wave frequency and Ω_e is the 265 electron cyclotron frequency) as well as the electron anisotropy $A(V_R)$. The value of 266 $R(V_R)$ is affected by both the electron density and the minimum resonant energy. The 267 minimum resonant energy can be calculated by $E_{min} = \frac{B_0^2}{8\pi N_0} \frac{\Omega_e}{\omega} (1 - \frac{\omega}{\Omega_e})^3$ (Equation (1) 268 in ?). Consider a fixed value of $\frac{\Omega_e}{\omega}$, E_{min} increases (and thus the number of resonant 269 electrons increases) as B_0^2/N_0 increases. This explains the reason that most type B events 270 have negative values of C_B and the monotonic correlation between the chorus intensity 271 and amplitude of the magnetic oscillation is significant. ? also confirms that the growth 272 rate increases monotonically as background magnetic field increases or decreases when 273 the density ratio between total and hot electrons is much larger than 1 or close to 1, 274 respectively. The effects of total electron density variation on the linear growth rate is 275 more complex. As discussed in ?, both density enhancement (DE) and depletion (DD) 276 can increase the value of $R(V_R)$ and thus the linear growth rate. The DE can increase 277 $R(V_R)$ by reducing E_{min} (and thus increasing the number of resonant electron), while 278 the DD can increase $R(V_R)$ by reducing the total electron density. From our statistical 279 result, the events with positive C_N are several times more often than the events with 280 negative C_N . This indicates that the effect of N_0 on the number of resonant electrons is 281 more important than the change of N_0 itself in the magnetosphere, especially in the inner 282

region $(L < 6, \text{ shown by the Van Allen Probes results of a larger proportion of Type <math>N^+$ 283 events than the THEMIS events). This complex effect of the total density may explain 28 why there is no significant monotonic relationship between the chorus intensity and the 285 amplitude of density perturbation. Another possible reason is the additional effect of the 286 total electron density on $A(V_R)$. According to Equation 3 of ?, the dependence of whistler 287 wave growth rate on cold plasma density is non-monotonic, and the relation between 288 the two strongly depends on the hot electron anisotropy and wave frequency. As a final 289 remark, our statistical study here focuses on the dependence on wave amplitudes, while 290 ignoring the effects of density and magnetic field modulation on wave frequency and wave 291 polarization features, which are left for future investigation. 292

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References



Figure 1. Representative events of the eight subtypes of chorus modulation events from the observations of THEMIS satellites. For each subplot, the upper panel shows the variations of the background magnetic field (blue line) and plasma density (red line) and the lower panel shows the magnetic wave spectrum overplotted with the variation of chorus wave root mean square amplitude B_w (red line) as well as the variations of f_{ce} , $0.5f_{ce}$ and $0.1f_{ce}$ (white solid, dashed, dash-dot lines).



Figure 2. Spatial distribution of the occurrence rates of different modulation types and the proportions of different subtypes. The spatial distribution of modulation events numbers for all types (a), type B (b), type N (c) and type NB (d) respectively from THEMIS observation. (e): the proportion of different subtypes of events from THEMIS observation. (f) - (j) show similar content to (a) - (e) except for Van Allen Probes observation of modulation events.



Figure 3. Relationship between the chorus intensity and the amplitudes of the perturbations of background magnetic field and plasma density for different types of chorus modulation events. (a) and (b) show relation between normalized chorus wave intensity (y axis) and normalized amplitude of background magnetic field perturbation (x axis) for events observed by THEMIS (blue: type B, Black: type NB) with (a) positive and (b) negative correlations, respectively. (c) and (d) show relation between normalized chorus wave intensity (y axis) and normalized amplitude of plasma density perturbation (x axis) for events observed by THEMIS (red: type N, Black: type NB) with (c) positive and (d) negative correlations, respectively. (e) - (f) show similar content to (a) - (d) except for Van Allen Probes observations. The solid lines are linear fitting lines for dots with corresponding colors and the dashed lines outline the boundaries of the corresponding 95% predicting intervals.

Figure 1.











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Figure 2.







Figure 3.

