

The Shear Deformation Zone and the Smoothing of Faults with Displacement

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Abstract

We use high-resolution earthquake locations to characterize the three-dimensional structure of active faults and how it evolves with fault structural maturity. We investigate the distribution of aftershocks of several recent large earthquakes that occurred on crustal strike slip faults of various structural maturity (i.e. various cumulative fault displacement, length, initiation age and slip rate). Aftershocks define a tabular zone of shear deformation surrounding the mainshock rupture plane. Comparing this to geological observations, we conclude that this results from the re-activation of secondary faults. We observe a rapid fall off of the number of aftershocks at a distance range of 0.06-0.25 km from the main fault surface of mature faults, and 0.7-1.5 km from the fault surface of immature faults. The total width of the active shear deformation zone surrounding the main fault plane reaches ~1.5 km and 2.5-6 km for mature and immature faults, respectively. We find that the width of the shear deformation zone decreases as a power law with cumulative fault displacement. Comparing with an existing dynamic rough fault model, we show that the narrowing of the shear deformation zone agrees quantitatively with earlier estimates of the smoothing of faults with displacement, both of which are aspects of fault wear. We compare this evolution of fault structure with several attributes of earthquakes, and find that earthquake stress drop decreases with fault displacement and hence with increased smoothness.

1 **The Shear Deformation Zone and the Smoothing of Faults with Displacement**

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10

11 **Keypoints:**

12 Across strike distributions of aftershocks of large earthquakes describe the width of the
13 shear deformation zone around large faults.

14

15 The zone of active shear deformation scales with fault roughness and narrows as a
16 power law with fault displacement.

17

18 Earthquake stress drop decreases with fault displacement and hence fault roughness.

19

20

21 **Keywords:**

22 Fault maturity; shear deformation zone; large earthquakes; aftershock distributions;
23 scaling laws.

24

25

26 **Plain Language Summary**

27 Active fault zones worldwide are 3D features made of a parent fault and secondary
28 faults and fractures that damaged the surrounding medium. During and soon after a
29 large earthquake, these structures are reactivated, highlighted by numerous smaller
30 events, also called aftershocks. Their distribution allows us to characterize the zone of
31 shear deformation around the fault plane. In this study, we show that the width of the
32 shear deformation zone is narrower around mature faults than around immature faults.
33 It decreases as a power law with cumulative fault displacement as the result of the
34 smoothing of the fault with wear through geological times. Our study provides some
35 relations to better understand and anticipate the size of off-fault deformation
36 reactivated during and after an earthquake, based on geological fault parameters.

37

38 **Abstract**

39 We use high-resolution earthquake locations to characterize the three-dimensional
40 structure of active faults and how it evolves with fault structural maturity. We
41 investigate the distribution of aftershocks of several recent large earthquakes that
42 occurred on crustal strike slip faults of various structural maturity (i.e. various
43 cumulative fault displacement, length, initiation age and slip rate). Aftershocks define a
44 tabular zone of shear deformation surrounding the mainshock rupture plane.
45 Comparing this to geological observations, we conclude that this results from the re-
46 activation of secondary faults. We observe a rapid fall off of the number of aftershocks at
47 a distance range of 0.06 – 0.25 km from the main fault surface of mature faults, and 0.7-
48 1.5 km from the fault surface of immature faults. The total width of the active shear
49 deformation zone surrounding the main fault plane reaches ~1.5 km and 2.5-6 km for
50 mature and immature faults, respectively. We find that the width of the shear

51 deformation zone decreases as a power law with cumulative fault displacement.
52 Comparing with an existing dynamic rough fault model, we show that the narrowing of
53 the shear deformation zone agrees quantitatively with earlier estimates of the
54 smoothing of faults with displacement, both of which are aspects of fault wear. We
55 compare this evolution of fault structure with several attributes of earthquakes, and find
56 that earthquake stress drop decreases with fault displacement and hence with increased
57 smoothness.

58

59 **1. Introduction**

60 A fault zone is a complex brittle-frictional system that wears as slip occurs on it. It is
61 formed of three main features, that will evolve with fault growth (Fig. 1): (i) the
62 cataclastic core contains the cataclastic detritus of wear of the slipping surfaces of the
63 fault. Its width (W_c in Fig. 1) increases linearly with fault displacement at a rate that
64 depends on the strength of the wall rock (Scholz, 1987, 2019, pp 132). For
65 displacements greater than a few hundred meters, growth of the fault core levels off at a
66 thickness of a few tens of meters (Scholz, 2019, pp 132); (ii) Beyond the fault core lies a
67 region of pervasive tensile fracturing which defines the “dilatant damage zone” (W_D , Fig.
68 1; e.g. Faulkner et al., 2011; Savage & Brodsky, 2011; Vermilye & Scholz, 1998). The
69 fracture density in this zone dies off as a power law with distance from the fault (e.g.,
70 Ostermeijer et al., 2020 and references therein). The dilatant damage zone width
71 increases linearly with fault displacement, and typically levels out at several hundred
72 meters for fault displacements exceeding several hundred meters (Savage & Brodsky,
73 2011); (iii) Including and extending beyond the dilatant damage zone is what we call the
74 “shear deformation zone” (W_S ; Fig. 1) which is defined by a region of enhanced
75 seismicity, first pointed out by Powers & Jordan, 2010. This zone shows a region of high

76 activity near the fault with a power law fall-off beyond a corner at W_{S1} to a full half-
77 width of W_{S2} (Fig. 1).

78

79 The above definitions allow us to distinguish two types of damage zones: the “dilatant
80 damage zone” dominated by volumetric strains, and the “shear deformation zone”
81 dominated by shear strains. The tensile (Mode I) cracks in the dilatant damage zone are
82 dilatant cracks that align parallel to the maximum compression direction and
83 perpendicular to the minimum principal stress. Hence their orientation provides
84 evidence for the several different mechanisms responsible for them (Wilson et al.,
85 2003). The shear deformation zone is characterized by secondary faults (Mode II and III
86 cracks) and hence are oriented parallel to the maximum Coulomb stress. For example, in
87 the case of a strike-slip fault, this zone is defined by a conjugate set of secondary faults
88 (Little, 1995).

89

90 The evolution of these three zones defines what is called fault maturity. The three zones
91 can be viewed as regions controlled by wear processes, and the fault structural maturity
92 can hence be measured by its degree of wear, which depends primarily on the net fault
93 displacement. However, previous studies have shown that, in the absence of data on net
94 fault displacement, several other fault parameters such as the fault initiation age and
95 the geological slip rate can be also used as a proxy of net displacement in evaluating the
96 overall maturity of the fault (e.g. Choy et al., 2006; Choy & Kirby, 2004; Dolan &
97 Haravitch, 2014; Hecker et al., 2010; Ikari et al., 2011; Manighetti et al., 2007; Niemeijer
98 et al., 2010; Perrin et al., 2016a; Stirling et al., 1996; Wesnousky, 1988). As these
99 parameters increase, the fault grows and becomes more “mature”. Prior studies have
100 suggested that the structural maturity may have a strong impact on earthquake

101 behavior, such as magnitude, stress drop, distribution of slip, ground motion amplitude,
102 and number of ruptured segments (e.g., Cao & Aki, 1986; Dolan & Haravitch, 2014;
103 Hecker et al., 2010; Malagnini et al., 2010; Manighetti et al., 2007; Perrin et al., 2016a;
104 Radiguet et al., 2009; Stirling et al., 1996; Wesnousky, 1988).

105

106 The widths of the fault core and dilatant damage zones saturate at fault lengths
107 comparable to the seismogenic thickness, so that for large faults, the evolution of fault
108 maturity involves only changes in the shear deformation zone. In this paper we are
109 concerned with the scaling of large faults (i.e. which reach the brittle seismogenic depth)
110 and their associated large earthquakes, so we are only concerned with the shear
111 deformation zone. There is evidence that indicates that large faults become smoother
112 with net displacement (Stirling et al., 1996; Wesnousky, 1988). This smoothing is
113 probably the prime attribute of fault maturity. Here we show that the width of the shear
114 deformation zone of large faults decreases with fault displacement, as a consequence of
115 this smoothing.

116

117 Precise earthquake locations can be used to image the internal structure of fault and the
118 zone of brittle deformation, often at a resolution similar to field observations (e.g.
119 Powers & Jordan, 2010; Hauksson, 2010; Valoroso et al., 2014). Powers & Jordan (2010)
120 studied the association of small earthquakes with large faults in California. They found
121 that the frequency of small earthquakes is highest in a narrow region surrounding faults
122 and then falls off as a power law at greater distances. They modeled this behavior with a
123 fault model with rough (fractal) topography (Dieterich & Smith, 2009), showing that
124 such a rough fault model would produce high stresses near the fault that could account
125 for the seismicity. The seismicity they used was from the interseismic period of the

126 faults. Although stacked profiles from many fault sections show the association with the
127 faults, individual sections and map views, both in Powers & Jordan (2010) and Hauksson
128 (2010) show that such a tight correlation with the fault is not typical of individual fault
129 segments, for which a wide variety of distributions of seismicity can be observed. As
130 Hauksson (2010) observed, this variability is likely due to many factors, such as
131 heterogeneity in lithology, the effect of nearby faults both mapped and unmapped, and
132 fault offsets and bends.

133

134 As Hauksson (2010) observed further, aftershocks of large earthquakes, in contrast,
135 always show a tight clustering around the main fault. The majority of aftershocks of
136 large earthquakes occur close to the rupture surface, and are often used to delineate it.
137 In an earthquake model with a smooth rupture surface, the near-fault area lies in a deep
138 stress shadow (Kostrov & Das, 1984). Near-fault aftershocks therefore are an indication
139 of a rough fault, as near-fault stresses are generated by dynamic slip on rough
140 topography. They are greatest right after the mainshock, after which they are relaxed by
141 aftershocks and other relaxation mechanisms. In this study, in order to estimate the
142 roughness of active faults, and how they evolve with displacement, we use high-
143 precision aftershock locations of large earthquakes on faults with different net
144 displacements.

145

146 **2. Data analysis**

147 *2.1 High-resolution earthquake location*

148 We use high-resolution earthquake catalogs available in the literature to analyze the
149 aftershock distribution of eight large ($M_w \geq 6$) continental strike slip earthquakes: the
150 1984 Morgan Hill, 2004 Parkfield, and 2014 South Napa earthquakes in northern and

151 central California (Waldhauser, 2009; Waldhauser & Schaff, 2008), the 1987
152 Superstition Hills, 1992 Landers, 1999 Hector Mine, and 2010 El Mayor Cucapah
153 earthquakes in Southern California/Mexico (Hauksson et al., 2012), and the 2000
154 Tottori earthquake in Japan (Fukuyama et al., 2003). These earthquakes were selected
155 because high precision catalogues were available for their aftershocks and because they
156 occurred on faults with a wide range of net displacement. In order to perform an
157 appropriate and homogeneous analysis of all cases, we selected events of $M_w > 1$ within
158 2 months of each mainshock, all relocated by double difference techniques (Waldhauser
159 & Ellsworth, 2000).

160

161 For each aftershock sequence we determine the three-dimensional fault geometry by
162 applying a principal component analysis (PCA) to all events within boxes that are
163 between 3 and 10 km long along strike and between 3 and 20 km wide across strike (i.e.
164 centered on the surface fault trace in map view), stepping at 1 km intervals along the
165 fault trace (Perrin et al., 2019). For each box, we obtain a plane that best fits the
166 locations of aftershocks. For simplicity, we assume, in each box, a constant dip of the
167 calculated planes as a function of depth (see also Perrin et al., 2019). Then we deduce
168 the orthogonal distance between each event and the calculated fault plane segment, and
169 sum up the the number of aftershocks on each side of the fault within bins of 50 m from
170 the fault plane (but 20 m for Parkfield) (gray curves in Fig. 2b, d, e, f, g and Supp. Fig. S1).
171 These gray distributions are normalized by the total number of aftershocks in each box.
172 We use the mean values of the normalized number of events in each bin (black curve in
173 Fig. 2 and Supp. Fig. 1) to describe the smoothed distribution of aftershocks away from
174 the fault plane.

175

176 We use two parameters to describe the smoothed near-fault aftershock distribution: the
177 location where the number of events begins to fall off with distance from the fault (W_{S1}),
178 and the location where the background level of seismic activity is reached (W_{S2}). In
179 order to find these parameters we use a power law function to fit the mean normalized
180 aftershock distribution (red fit in Fig. 3 and Supp. Fig. 2) and defined W_{S1} at the location
181 where the function reaches a maximum in its 2nd derivative. W_{S2} corresponds to the
182 distance where the mean distribution departs from the fit (see Fig. 3), as defined also in
183 Powers and Jordan (2010). In a few cases (e.g., Hector Mine, Superstition Hills, Landers),
184 W_{S2} cannot be determined because the background level cannot be estimated due to the
185 presence of subparallel or sub-perpendicular fault sections that bias the number of
186 events. In these cases, we use the W_{S2} values determined from other fault segments that
187 broke during the same earthquake, hence assuming a similar background seismicity
188 level away from the different fault sections.

189

190 As an example of our approach, the analyses of the 2004 Parkfield and 1999 Hector Mine
191 aftershocks are presented in figure 2 and 3 (see Supp. Fig. S1 and S2 for all earthquake
192 cases). The near-fault aftershock distribution at Parkfield (black curve, Fig. 3a) describes
193 a rapid fall off at ~ 0.06 km away from the fault plane (W_{S1}) until they reach background
194 seismicity levels at ~ 0.8 km from the fault plane (W_{S2}). In cases with multiple rupture
195 traces (i.e. Hector Mine, Landers, El Mayor Cucapah), we separately analyzed each main
196 section that broke during the earthquake (Fig. 2c, d, e, f, g, 3b, c, d, e and Supp. Fig. S1
197 and S2). In these cases, the aftershocks distributions were fairly similar for the different
198 traces. Hence, we averaged W_{S1} and W_{S2} , when possible, so that single values could be
199 assigned to each earthquake sequence. Table 1 lists measurements for the eight
200 earthquakes analyzed in this study.

201

202 Also listed in Table 1 are data from the Awatere fault. This right-lateral strike-slip fault
203 is a first order splay of the Alpine fault of New Zealand. It crosses the coast at a sea-cliff
204 that offers an almost complete exposure of the entire fault zone from the fault core
205 through the shear deformation zone. This was mapped by Little (1995), who showed
206 that the shear deformation zone consists of a set of conjugate strike-slip secondary
207 faults that decreased in frequency with distance from the primary fault in the same
208 manner as the aftershocks do in our study. The right-lateral set of the secondary faults is
209 nearly sub-parallel to the main fault and the left-lateral set about 60° from that. Values
210 of W_{S1} and W_{S2} obtained from that data are indicated in Table 1. An exposure at mid-
211 crustal depths of a strike-slip fault in Austria shows just the same orientation of
212 secondary faults (Frost et al., 2009). These observations provide the ‘ground truth’ for
213 the structures upon which the near-fault aftershocks occur.

214

215 *2.2 Fault parameters*

216 We collect key parameters describing the degree of evolution of the faults that broke
217 during the selected earthquakes. Since faults propagate laterally through time, their
218 structural maturity varies also along strike (Perrin et al., 2016a; 2016b). Thus, it is
219 necessary to use fault parameters that describe the local fault maturity where the
220 rupture occurred. This is particularly true for long faults, such as the San Andreas Fault,
221 for which fault initiation age varies greatly along the fault, from ancient fault sections in
222 Central California (24 to 29 Ma at Parkfield; e.g. Atwater & Stock, 1998; Liu et al., 2010)
223 to younger fault sections in Southern California (<12 Ma, e.g. Powell & Weldon, 1992;
224 Sims, 1993), and therefore have different local net displacements. Table 1 presents the
225 fault parameters used in this study. The eight fault sections span a wide range of

226 structural maturity, with various initiation ages (1.1 to 29 Ma), cumulative
227 displacements (1 to 315 km) and geological slip rates (0.1 to 26 mm/yr).

228

229 In the case of the Tottori earthquake the cumulative displacement of the Komachi-Odani
230 fault is not known. We estimated it based on the empirical relation from Schlische et al.
231 (1996) that shows that crustal fault displacement scales with their length as 2×10^{-2} to
232 8×10^{-2} . If we take the fault length from the aftershocks distribution (Fukuyama et al.,
233 2003) to be 35 km, this would give a cumulative displacement in the range 0.7 to 2.8 km
234 (Table 1). In the case of the Awatere fault we do not have aftershock locations, but
235 instead use the width of the shear deformation zone as inferred from field data
236 measured by Little (1995) across an immature section of the Awatere fault zone, in New
237 Zealand (cumulative slip : $< 2 \pm 1$ km, initiation age : $< 4 \pm 1$ My, long-term slip rate : 5 ± 1
238 mm/yr near its northeastern tip; Little, 1995 and references therein).

239

240 **3. Results**

241 We investigate the relationship between the two independent datasets: the aftershock
242 distributions and the fault parameters (Table 1). Our first observation is that W_{S1} (i.e.
243 the half distance from the calculated fault plane where the aftershock rate saturates)
244 and W_{S2} (i.e. the full half-width of the shear deformation zone) correlate with each other
245 (Fig. 4), indicating that these two parameters are not independent and that the shape of
246 the shear deformation zone grows in a self-similar way (although there is an indication
247 that W_{S1} becomes relatively narrower for more mature faults). Figure 5 represents the
248 evolution of the width of the shear deformation zone (i.e. W_{S1} and W_{S2}) as a function of
249 the cumulative fault slip (Fig. 5a and 5b, respectively). Both plots show the same trend:
250 the width of the shear deformation zone, measured with both parameters, decreases

251 with net displacement as a power law with an exponent of -0.55 and -0.35 for W_{S1} and
252 W_{S2} , respectively. These results indicate that the two parameters W_{S1} and W_{S2} scale
253 similarly with displacement.

254 Note that the field measurements across the Awatere fault (red symbol in Fig. 5) are in
255 good agreement with the trends highlighted from seismological data. This supports the
256 interpretation that the shear deformation zone defined by the width of the aftershock
257 zone corresponds to the width of the zone of active secondary faulting.

258

259 As W_{S1} and W_{S2} are found to decrease with cumulative displacement, we observe a
260 similar decrease of these parameters with fault initiation age and slip rate, showing a
261 wider shear deformation zone for younger fault sections (Supp. Fig. S3) and smaller
262 geological slip rates (Supp. Fig. S4), also in good agreement with geological observations
263 across the Awatere fault.

264

265 Figure 6a shows the near-fault aftershock distribution as a function of fault
266 perpendicular distance for the eight earthquake sequences considered in this study (see
267 also black curves in Fig. 2 and Supp. Fig. S1). These distributions show a clear pattern:
268 mature fault sections (warm colors in fig. 6a, b and c) are characterized by aftershocks
269 concentrated mainly close to the fault plane. The rapid fall-off in activity away from the
270 fault plane describes a narrow deformation zone at the scale of hundreds of meters. In
271 contrast, immature faults (cold colors in fig. 6a, b and c) exhibit a wider deformation
272 zone at the kilometer scale where events are more widely distributed within the
273 surrounding medium (i.e. lower maximum number of events in the near-field of
274 immature faults than of mature fault sections; fig. 6a and b). The distributions remain
275 proportional to one another, indicating the shape of the shear deformation zone remains

276 constant. Here again, field measurements of cumulative number of faults across the
277 Awatere fault (black squares, fig. 6a; Little, 1995) show a similar trend and corroborate
278 our seismological observations.

279

280

281 **4. Discussion**

282 *4.1. The Nature of the Shear Deformation Zone and the Smoothing of Faults*

283 In this study we show that for fault displacements greater than 1 km the width of the
284 shear deformation zone, defined by W_{S1} and W_{S2} , decreases with fault displacement. So,
285 what determines the width of the zone of near-fault aftershocks? Models of a mainshock
286 employing smooth faults would indicate a deep stress shadow in this area, precluding
287 the presence of such near-fault aftershocks (Kostrov & Das, 1984). On the other hand,
288 models with rough faults predict high stresses within a well-defined region close to the
289 fault, which corresponds to the shear deformation zone. Powers & Jordan (2010)
290 interpreted their data in just that way, using a rough static fault model of Dieterich &
291 Smith (2009).

292

293 Here we consider the model of Aslam & Daub (2018) which calculates the stresses
294 resulting from dynamic ruptures propagating on a rough surface. They characterized the
295 fault as a self-affine fractal with Hurst exponent H and roughness measured by the RMS
296 height to wavelength ratio. This is a fairly realistic rendition of the observed topography
297 of faults (e.g. Candela et al., 2012). Their model predicts large changes in the Coulomb
298 Failure Function ($CFF = \tau + \mu\sigma$), within a well-defined narrow region close to the fault.
299 The receiver faults they assumed are parallel to the primary fault: this would be
300 consistent with the orientation of the secondary faults observed by Little (1995) and

301 Frost et al. (2009). They find that the width of this near-fault region of high stresses is
302 insensitive to H but decreases as the RMS roughness decreases. If we identify our
303 observed shear deformation zone with that near-fault region of high stresses, this
304 indicates that the observed decrease of W_{S2} with fault displacement is the result of
305 smoothing of the fault with slip.

306

307 Aslam & Daub (2018) found that the half width of the near fault zone is ~ 2.7 and ~ 0.9
308 km for fault profiles with RMS height to wavelength ratios of 0.01 and 0.001,
309 respectively. Comparing these results with the range of W_{S2} in figure 5 indicates that
310 more than an order of magnitude of roughness change will be required to explain these
311 observations. This indicates a wear rate far greater than that which occurs for the
312 roughness of individual fault segments (Brodsky et al., 2011). However, faults are
313 composed of many segments or sub-faults at many scales (Ferrill et al., 1999; Klinger,
314 2010; Manighetti et al., 2015; Scholz, 1998) and of nested sub-faults offset from one
315 another (Ben-Zion & Sammis, 2003; de Jossineau & Aydin, 2009; Segall & Pollard,
316 1980). The length distribution of sub-faults follows a power law (Scholz, 1998) and they
317 are offset by jogs that are self-similar (de Jossineau & Aydin, 2009). It therefore would
318 be possible that this combination would produce a fractal topography at a hierarchy
319 higher than that of the roughness of the individual sub-fault.

320

321 Geological observations indicate that fault roughness, as measured by segment offsets,
322 decreases with fault slip (de Jossineau & Aydin, 2009; Stirling et al., 1996; Wesnousky,
323 1988). Stirling et al. (1996) show an approximately linear reduction of fault roughness,
324 measured as segments per unit of fault length, with fault displacement. If we make the
325 reasonable assumption that the fault jog offsets identified by Stirling et al are of order 1

326 km then the height to wavelength ratios of 0.001 and 0.01 correspond to fault
 327 displacements of 100 and 10 km, respectively. Combining these with the corresponding
 328 deformation zone widths of Aslam & Daub (2018) give the two data points in Figure 7.
 329 The solid black line there is the best fit of the data for W_{S2} from Figure 5b. The excellent
 330 agreement confirms the hypothesis that narrowing of the shear deformation zone with
 331 fault displacement is the consequence of the smoothing of the fault with wear.

332

333 *4.2. Relations of Earthquake Parameters with Fault Maturity*

334 The primary feature of the maturation of faults is that their surfaces become smoother
 335 with displacement through the process of frictional wear. It might also be supposed that
 336 the characteristics of earthquakes may differ according to the maturity of the fault upon
 337 which they occur. It has been suggested, for example, that earthquake stress drop,
 338 apparent stress, and radiation efficiency vary with fault maturity (Choy et al., 2006;
 339 Hecker et al., 2010; Ross et al., 2018). These are not entirely independent parameters.

340 The radiation efficiency, η_R , is given by:

$$341 \quad (1) \quad \eta_R = \frac{E_R}{E_R + E_G} = \frac{2\mu E_R}{\Delta\sigma M_0} = \frac{2\sigma_a}{\Delta\sigma}$$

342 where E_R is radiated energy, E_G is the energy dissipated in damage of various types, $\Delta\sigma$
 343 is stress drop, σ_a is apparent stress, M_0 is seismic moment, and μ is the shear modulus.
 344 Table 2 gathers these parameters for four earthquakes we have studied and for which
 345 this information was available in the literature. Although this list is short, it is expansive,
 346 in the sense that it covers four orders of magnitude in fault displacement, which give us
 347 the opportunity to test the different hypothesis.

348

349 The idea that radiation efficiency increases with fault maturity was based entirely on a
350 comparison of the Tottori and Parkfield earthquakes (Ross et al., 2018). The other two
351 earthquakes in our collection do not support that contention. Our data also do not
352 support the claim of Choy et al. (2006) that apparent stress decreases with fault
353 maturity (Table 2). Their definition of maturity was qualitative and compared faults in
354 different tectonic settings and lithologies. For example, their highest apparent stress
355 was for intraplate oceanic strike-slip faults, and the lowest for subduction zone thrusts.
356 The latter must have a much greater net displacement than the former and hence must
357 be much more mature. However, McGarr (1999) and Choy & McGarr (2002) argue that
358 apparent stress is proportional to strength. If they are correct, then the strength of the
359 oceanic lithosphere, being much greater than the clay-rich and over-pressured oceanic
360 sediments that coat the frictional interface of subduction megathrusts, results in a
361 correspondingly higher apparent stress. The earthquakes in our Table 2, on the other
362 hand, are all strike-slip continental earthquakes so their lithologies are comparable and
363 the variables strength and maturity have been separated so that we can reach a clearer
364 conclusion regarding the effect of maturity on apparent stress.

365

366 Hecker et al. (2010) measured the maximum slip to length ratio of prehistoric
367 earthquake scarps on intraplate dip-slip faults in the western U.S. They found that this
368 ratio, an indicator of stress drop, tends to decrease with net fault displacement. Our data
369 is consistent with this finding: figure 8 presents the stress drop ($\Delta\sigma$) as a function of the
370 fault cumulative displacement (D), and show that $\Delta\sigma \propto D^{-0.45}$. Combining this result
371 with our earlier finding that $W_{S2} \propto D^{-0.35}$ implies that $\Delta\sigma \propto W_{S2}$ and hence is linearly
372 proportional to the mean fault roughness, as measured as RMS height to wavelength
373 ratio.

374

375 The secondary faults that form the framework of the shear deformation zone must be
376 formed early in the process, when the primary fault is very immature. They are
377 subsequently reactivated by aftershocks in a halo around the fault that gradually
378 narrows as the fault topography smooths with wear (fig. 6). In the early, fault-forming
379 stage, E_G must be much larger relative to E_R and hence η_R will be much smaller than at
380 later stages (Scholz, 2019 pp 137). This might explain the low value of η_R in the Tottori
381 case as compared to earthquakes in later stages.

382

383 *4.3. Fault Structure and Aftershock Distributions: Strength and Limitations of our Study.*

384 As mentioned earlier, Powers & Jordan (2010) estimated the normal distance of the
385 seismicity away from a single vertical fault plane inferred from the surface trace of the
386 fault. They defined the zone of shear deformation from the near fault seismicity during
387 the interseismic period and averaged over the entire fault length, possibly neglecting
388 local variations in fault plane orientation and leading to wider zones as compared to our
389 results. In addition, geological heterogeneity and other effects may play a role, as
390 pointed out by Hauksson (2010).

391

392 Our approach of fitting only one fault plane to the local aftershock distribution as we
393 step along the fault assumes that the rupture occurred mainly on one fault strand and
394 that aftershocks are homogeneously distributed in the medium around. While individual
395 secondary faults can be clearly distinguished around mature fault sections (see for
396 instance oblique linear streaks around Morgan hill in Supp. Fig. S1), it is more difficult to
397 identify them around immature fault sections (scattered aftershock distribution; i.e.
398 Hector Mine, Landers; Supp. Fig. S1). Yukutake & Iio (2017), for example, analyzed each

399 identifiable secondary strand associated with the main Komachi-Odani fault that broke
400 during the 2000 Tottori earthquake and found smaller across-strike distance for each of
401 them. Moreover, fault zone architectures worldwide are complex and not necessarily
402 symmetrical, especially near their propagating fault tip where secondary faults can be
403 observed on one side of the primary fault (e.g., Perrin et al., 2016b). We do not depict
404 this complexity in our study and simplify it as we sum the number of events on each side
405 of the best fitting plane. However, the seismic signature of secondary faults is included
406 in our smoothed across-strike distributions, which allow us to highlight the overall
407 volume around immature fault zones which is involved in the rupture during
408 earthquakes such as Hector Mine, Landers, Tottori, El Mayor Cucapah and Superstition
409 Hills.

410

411 In our study we compare an averaged normal distribution of aftershocks with fault
412 parameters, considering for each case a homogeneous local fault structural maturity
413 along the entire rupture length. But it has been shown that the fault maturity can vary
414 along strike and this can affect the heterogeneity of fracture density around the fault
415 core (Ostermeijer et al., 2020), the distribution of secondary faults at greater distances
416 away from the fault (Perrin et al., 2016b) and finally the behavior of earthquakes (e.g.,
417 Huang, 2018; Perrin et al., 2016a). Consequently, it is possible that for long earthquake
418 ruptures or multiple broken faults scenarii, the normal distribution of aftershocks can
419 change along strike, following locally a similar trend (i.e. a wider shear deformation
420 zone in the most immature parts of the rupture) at a local scale that we observe in our
421 study at greater scales. This would be in good agreement with mapped faults at the
422 surface that shows that the off-fault damage zone widens in the direction of long-term

423 fault propagation (e.g., Manighetti et al., 2001; Perrin et al., 2016b). Future work is
424 needed to relate such observations to the occurrence of seismicity.

425

426 **5. Conclusion**

427 Our study presents strong correlations between independent datasets, i.e. the near-fault
428 distribution of aftershocks following large earthquakes and the associated geological
429 parameters of the long-term faults involved in the rupture (cumulative displacement,
430 initiation age, slip rate). We find that for large faults, defined as those that have ruptured
431 the entire brittle thickness, the zone of active shear deformation narrows as a power law
432 with fault displacement, hence with fault maturity. This result is predicted by a dynamic
433 rough fault model in which fault roughness decreases with displacement. We find that
434 earthquake stress-drop also decreases with fault displacement and hence fault
435 roughness. Our relations show how the volume around fault zones can be reactivated
436 during large earthquakes, depending on fault maturity (i.e. its degree of wear
437 approached here by fault cumulative displacement). Our study can be useful to
438 anticipate across-strike distributions of aftershocks around major fault zones which are
439 not covered by a dense seismic network, based on known geological fault parameters.

440

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445 [tools/altcatalogs.html](https://scedc.caltech.edu/research-tools/altcatalogs.html). This paper is LDEO contribution XXX and IPGP contribution XXX.

446

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718 wear processes, Punchbowl Fault, San Andreas system, California. *Journal of*
719 *Structural Geology*, 25(11), 1855–1873. [https://doi.org/10.1016/S0191-](https://doi.org/10.1016/S0191-8141(03)00036-1)
720 [8141\(03\)00036-1](https://doi.org/10.1016/S0191-8141(03)00036-1)

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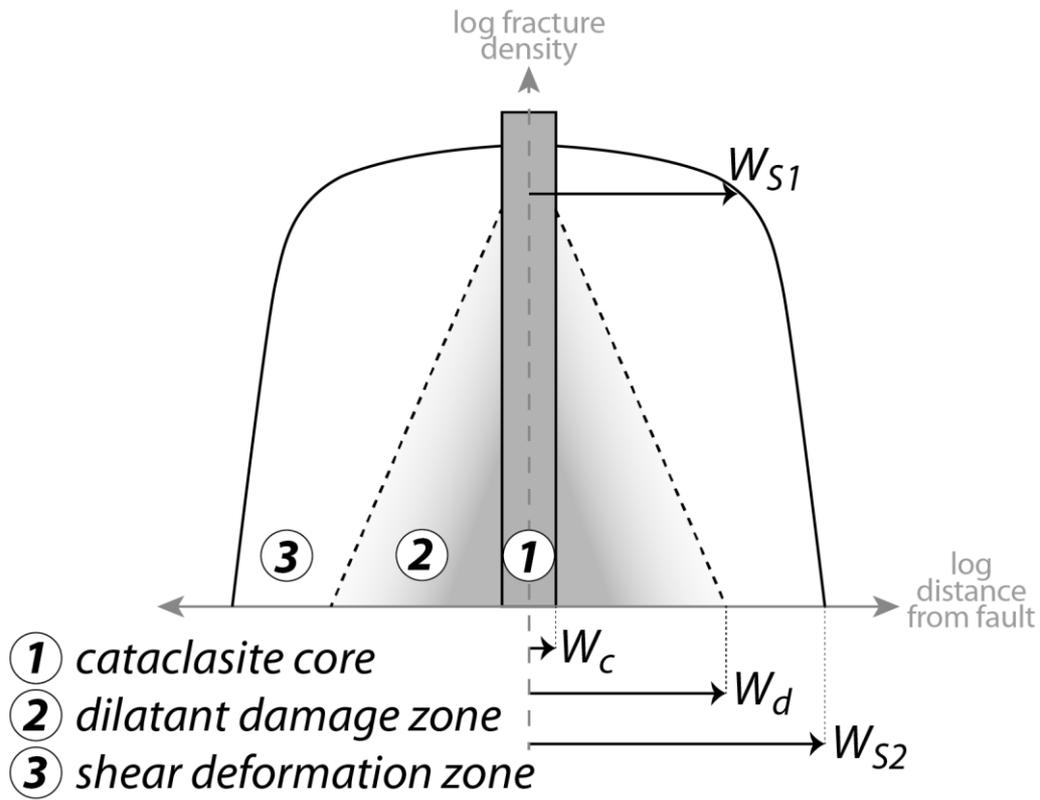
723 and focal mechanism distributions. *Earth, Planets and Space*, 69(1), 68.

724 <https://doi.org/10.1186/s40623-017-0650-2>

725

726

727 **Figures and figure captions:**



728 **Figure 1; Perrin et al.**

729 **Figure 1:** Simplified view of the architecture of a fault zone and the density of
730 fractures and seismicity away from the fault core.

731

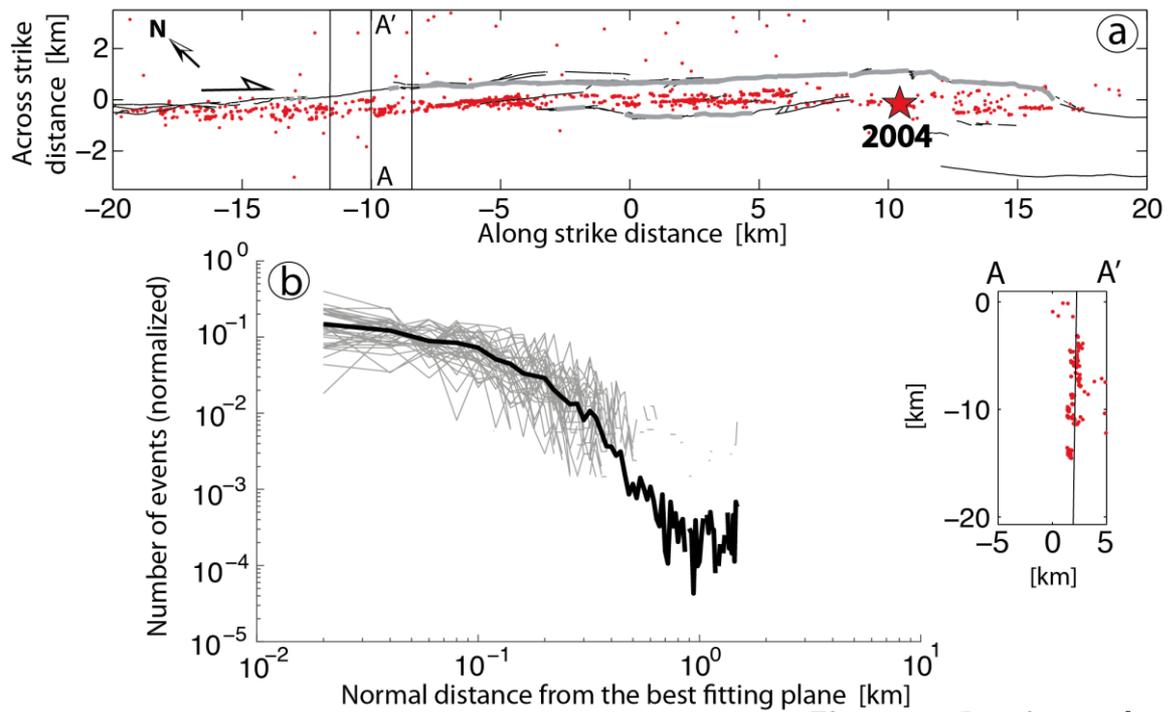


Figure 2; Perrin et al.

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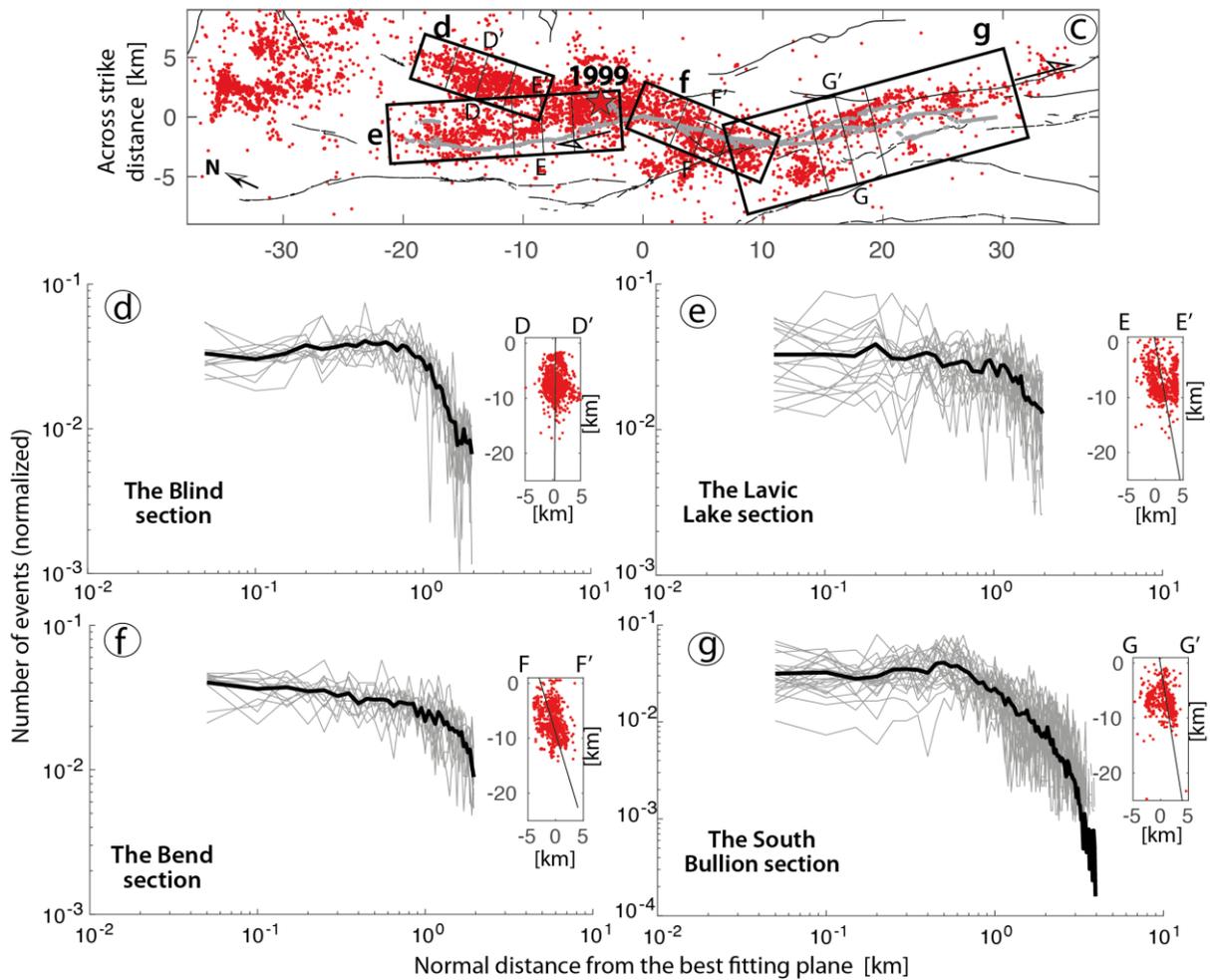


Figure 2 (following); Perrin et al.

733

734 **Figure 2: Aftershocks distribution of the (a, b) 2004 Parkfield and (c, d, e, f, g)**
735 **1999 Hector Mine earthquakes** (see Supp. Fig. 1 for all cases). (a) Map view showing
736 the San Andreas fault (black lines) and the surface rupture (thick grey line) of the 2004
737 Parkfield earthquake (epicenter indicated by the red star). Red dots are aftershocks that
738 occurred within 2 months after the mainshock (Waldhauser & Schaff, 2008; Perrin et al.,
739 2019). (b) Gray profiles are fault-normal earthquake distributions measured from the
740 best fitting plane in each moving box along the rupture trace. Black curves are the mean
741 of the gray profiles. Inset: cross section going through the hypocenter area. Depth in y-
742 axis; across strike distance in x-axis. Black line is best fitting plane minimizing fault-
743 normal distance to aftershock hypocenters (red dots); (c) same as (a) but for the 1999
744 Hector Mine earthquake (earthquake catalog from Hauksson et al., 2012). Boxes include
745 earthquakes used in d-g. (d-g) Same as (b) but for the 1999 Hector Mine earthquake. The
746 four sub-figures are based on earthquakes included in boxes shown in (c).
747

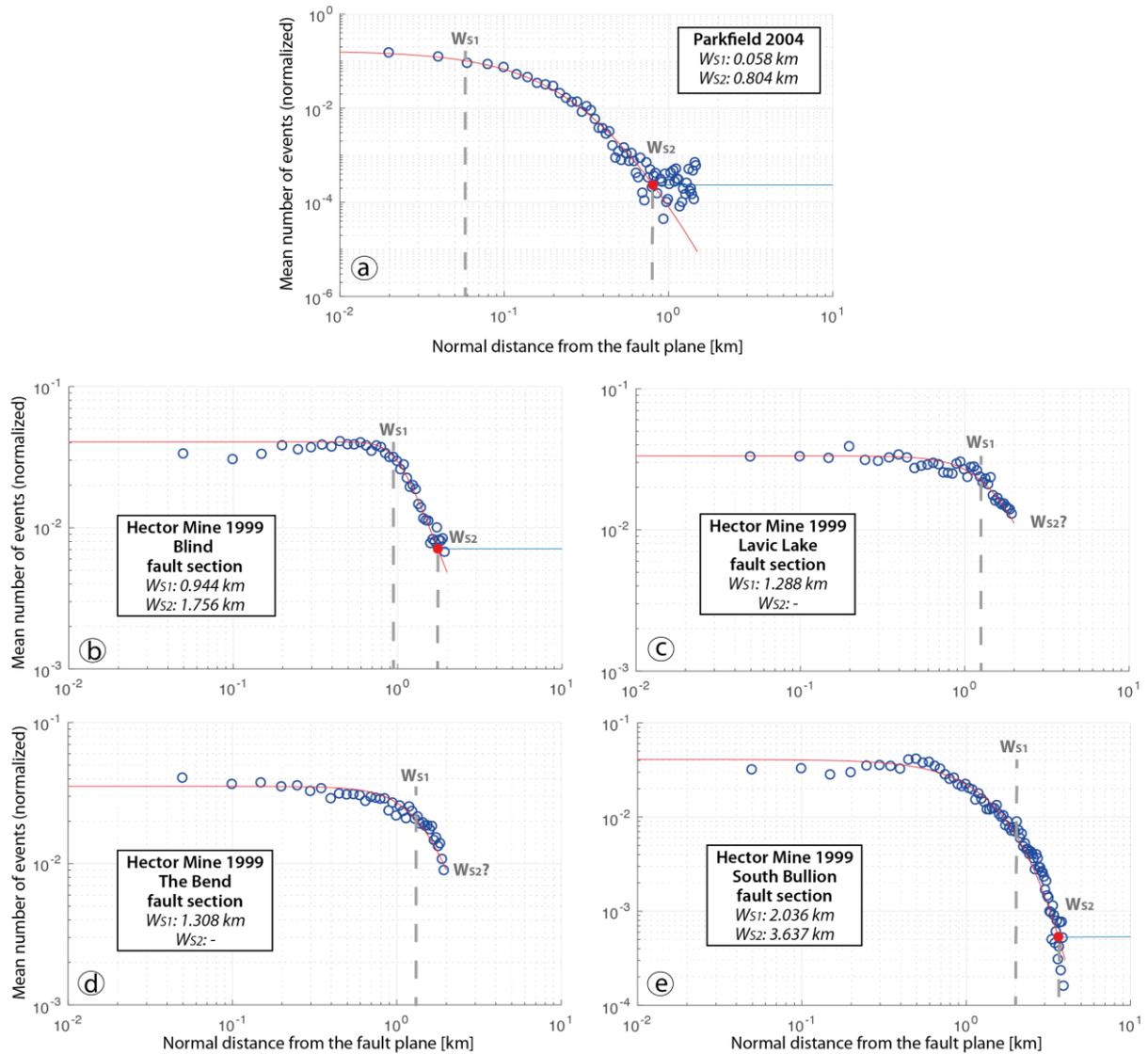


Figure 3 ; Perrin et al.

748

749 **Figure 3: Determination of W_{S1} and W_{S2} parameters from the aftershocks**

750 **distribution of the (a) Parkfield 2004 and (b, c, d, e) Hector Mine 1999**

751 **earthquakes** (see Supp. Fig. 2 for all cases). Blue dots represent the mean distribution

752 of each fault section (see black curve in Fig. 2 and Supp. Fig. 1). The red curve is the best

753 fit of the distribution. The vertical gray dashed lines labeled W_{S1} and W_{S2} point out the

754 locations where the numbers of earthquakes decrease rapidly and where they reach

755 background level, respectively. W_{S1} is defined as the maximum of the 2nd derivative of

756 the red fit. W_{S2} is defined by the red dot, which is the intersection between the red fit

757 and the background level (horizontal blue line), when identified. .

Location	Earthquake name /date	Half width of seismicity fall off W_{S1} (km)	Half width of the shear deformation zone W_{S2} (km)	Name of fault section(s)	Initiation age (Ma)	Cumulative slip (km)	Long-term slip rate (mm/yr)	References for fault parameters
Japan	Tottori, 2000	0.684 ± 0.050	3.777 ± 0.050	Komachi-Odani	~ 5	0.7 to 2.8†	~ 0.1	Sugiyama et al., 2005 ; Active fault database of Japan*
USA	El Mayor Cucapah, 2010	1.554 +1128/-0.702 (mean value)	6.335 ± 1783 (mean value)	Elsinore (southern section)	~ 1.1	1 to 2	1 to 2	Dorsey et al., 2012; K. E. K. Fletcher et al., 2011 and references therein
USA	Hector Mine, 1999	1.394 +0.642/-0.302 (mean value)	2.697 ± 940.5 (mean value)	Lavic Lake-Bullion	< 10	10 to 20	~ 0.8	Dibblee, 1961; Dokka, 1983; Dokka & Travis, 1990; Garfunkel, 1974; Jachens et al., 2002; Oskin et al., 2007
USA	Landers, 1992	0.954 +0.144/-0.254 (mean value)	3.736 ± 0.050	Emerson-Camp Rock-Homestead Valley-Johnson Valley	< 10	3.5 to 4.6	0.2 to 0.7	Dibblee, 1961; Dokka, 1983; Dokka & Travis, 1990; Garfunkel, 1974; Jachens et al., 2002; Rockwell et al., 2000; Rubin & Sieh, 1997
USA	Morgan Hill, 1984	0.094 ± 0.050	1.457 ± 0.050	Calaveras	~ 12	60 to 70	3 to 25	Stirling et al., 1996; Wakabayashi, 1999 and references therein
USA	Parkfield, 2004	0.058 ± 0.020	0.804 ± 0.020	San Andreas (central section)	24 to 29	~ 315	~ 26	Atwater & Stock, 1998; Critelli & Nilsen, 2000; Crowell, 1979; Graham et al., 1989; Liu et al., 2010; Matthews, 1976; Revenaugh & Reasoner, 1997; Toké et al., 2011
USA	South Napa, 2014	0.268 ± 50	0.907 ± 0.050	West Napa (considered as part of the Calaveras fault zone)	~12	60 to 70	3 to 25	Stirling et al., 1996; Wakabayashi, 1999 and references therein
USA	Superstition Hills, 1987	0.858 ± 50	> 2.500	San Jacinto (southern section)	< 2	~ 4	~ 4	Blisniuk et al., 2010; Dorsey et al., 2012; Gurrola & Rockwell, 1996; Hudnut & Sieh, 1989; Kirby et al., 2007; Lutz et al., 2006

<i>New Zealand</i>	-	<i>0.120 to 1.830 (field measurements)</i>	<i>~2800 (field measurements)</i>	<i>Awatere</i>	<i>< 4</i>	<i>< 2</i>	<i>~ 5</i>	<i>Little, 1995 and references therein</i>
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Table 1: Fault and aftershock distribution parameters for the eight earthquake sequences analyzed in this study. Minimum uncertainties are defined by the bin of normal distribution in single earthquake cases. For multiple broken fault sections (Hector Mine, Landers, El Mayor Cucapah), W_{S1} and W_{S2} are mean values, when possible, and the uncertainties represent the minimum and maximum range of values (see detailed measurements in Supp. Figure S2). Field measurements of the Awatere fault from Little et al. (1995) are also indicated (for details see text).

* available at: <https://gbank.gsj.jp/activefault/>

† deduced from scaling relations in Schlische et al., 1996 (see text for details)

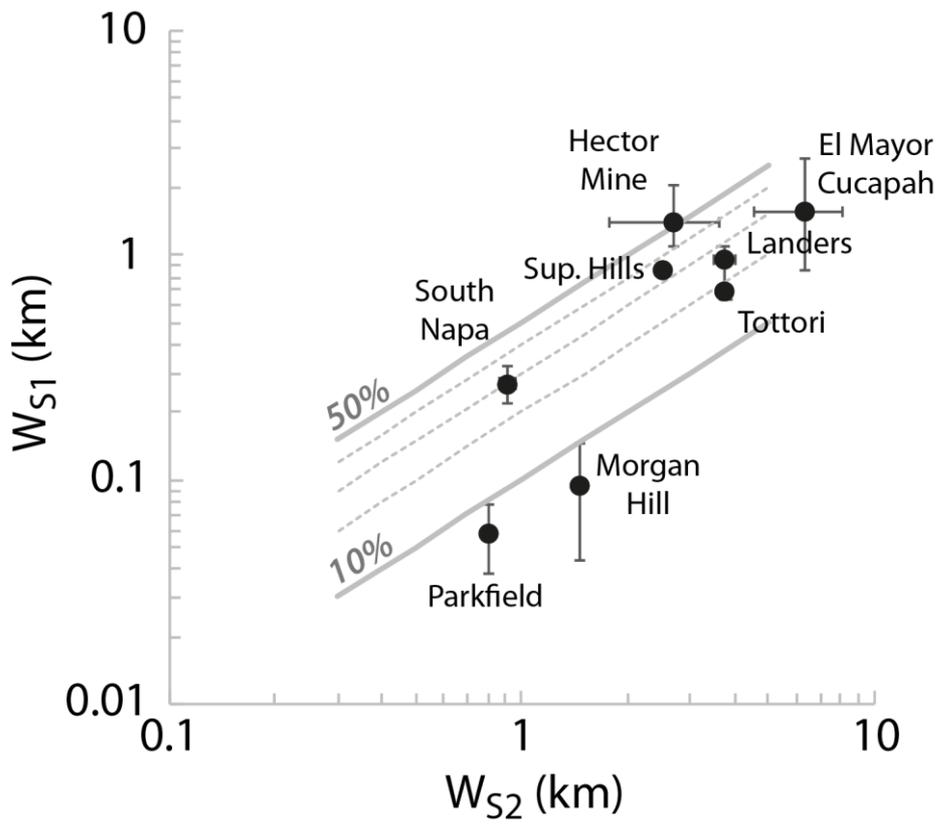


Figure 4; Perrin et al.

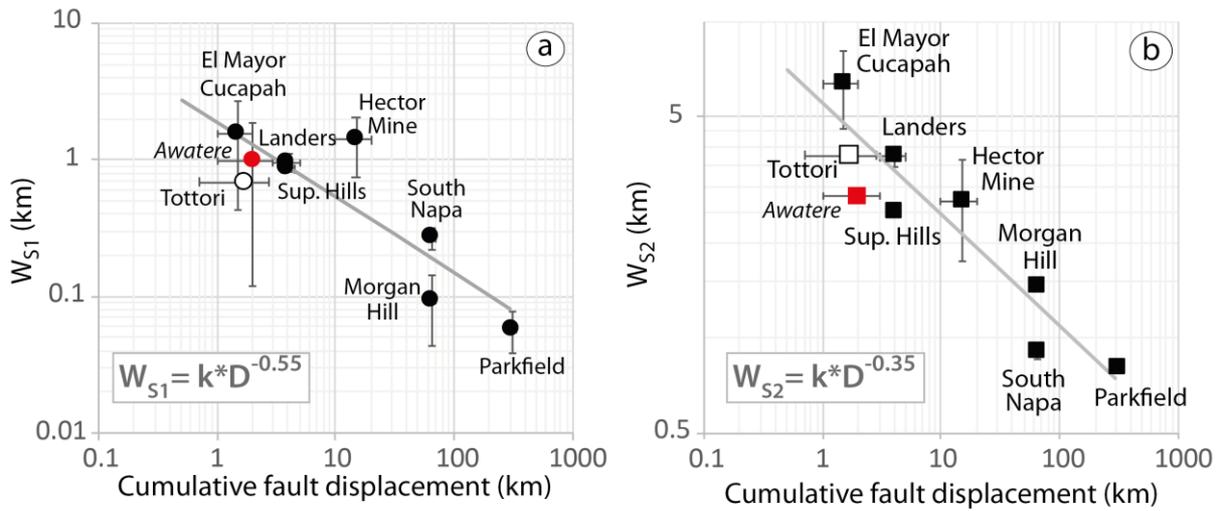
766

767 **Figure 4:** Relations between W_{S1} and W_{S2} for the eight earthquakes analyzed in

768 this study.

769

770



771

Figure 5; Perrin et al.

772 **Figure 5:** Relations between (a) W_{S1} and (b) W_{S2} of eight earthquake sequences
773 and the cumulative slip of their host fault taken from literature (solid symbols)
774 and inferred (empty symbols) (see Table 1 for details). Power laws are indicated by
775 grey lines. For comparison, red symbols indicate geological surface measurements along
776 the Awatere fault (from Little, 1995). D is the cumulative fault displacement, k is a
777 constant.

778

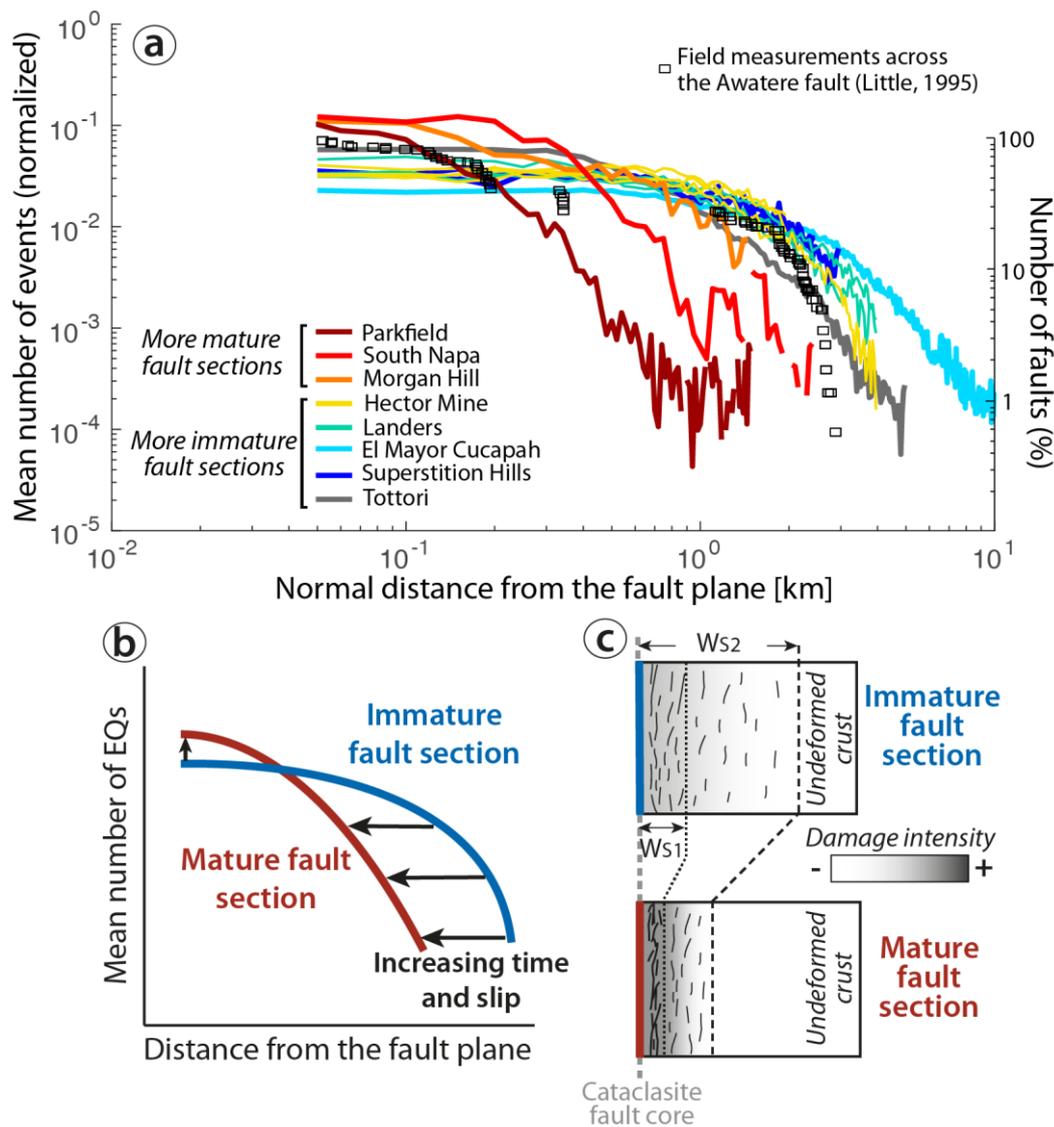


Figure 6; Perrin et al.

779

780 **Figure 6:** (a) Normal distribution of the mean number of aftershocks as a function

781 of distance from the fault, for the eight earthquake sequences analyzed in this

782 study (see also black curves in Fig. 2 and Supplementary Figure S1). Each colored curve

783 represents one earthquake sequence. Curves with the same color are distinct fault

784 sections that broke during one earthquake. Warm colors are more mature, cool colors

785 more immature fault sections. For comparison, black squares indicate the cumulative

786 number of faults (right y axis) measured at surface from the Awatere fault (modified

787 from Little, 1995). (b) Sketch summarizing the fault-normal distributions of aftershocks

788 for immature (blue curve) and mature (red curve) fault sections. (c) Interpretative

789 cross-section describing the structural makeup of immature (blue) and mature (red)
790 faults. As fault structural maturity increases, then inner and outer bounds of the shear
791 deformation zone (WS1 and WS2, respectively) decrease, as expressed by a decreasing
792 width of the fault-normal aftershock distribution. See text for more discussion.
793

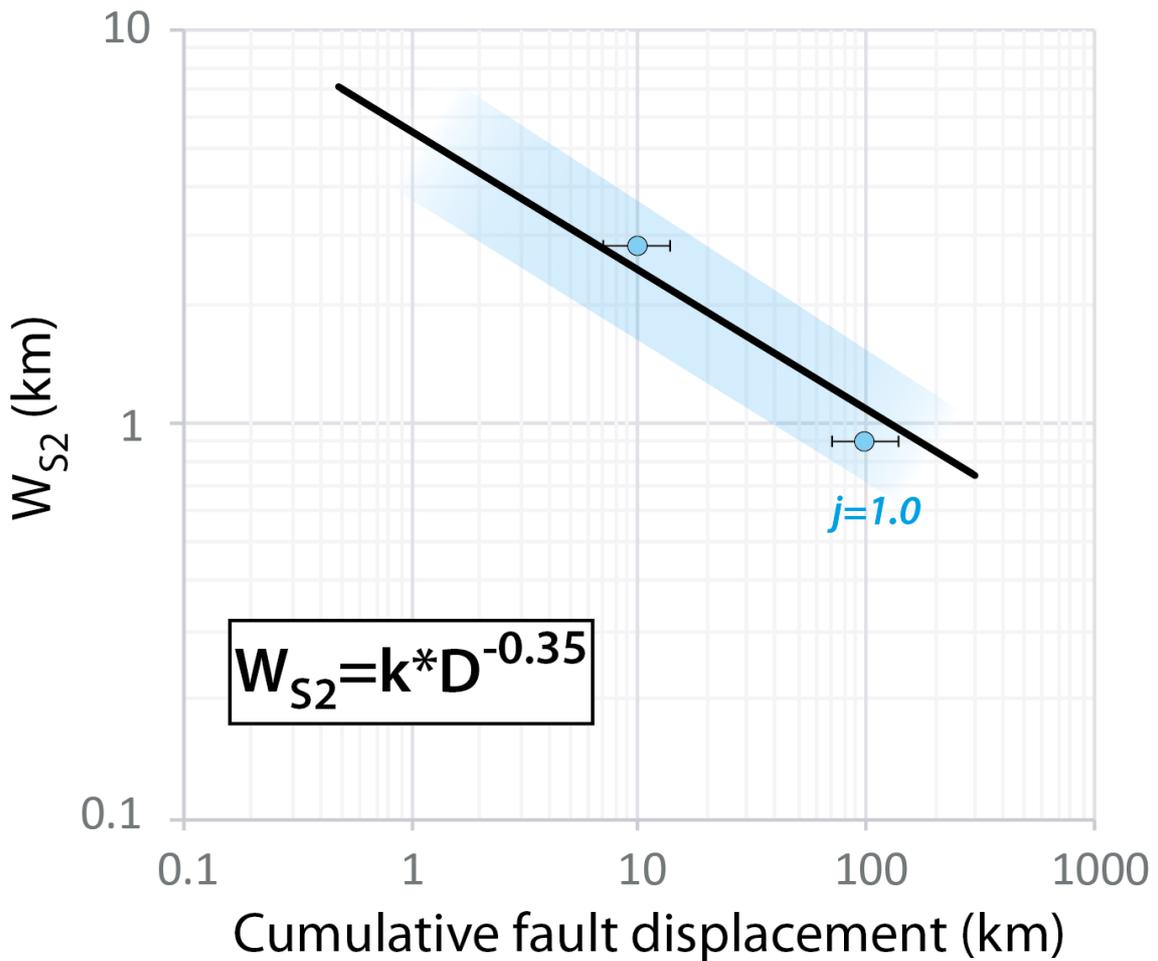


Figure 7; Perrin et al.

794

795 **Figure 7:** Comparison between power law deduced from the outer bound of the shear
 796 deformation zone (W_{S2} ; black line) and power law built from observations and models in
 797 Stirling et al., 1996 and Aslam & Daub, 2018 (blue dots and shaded area). Blue dots are
 798 assuming typical jog heights $j = 1$ km, the blue shaded area bounds the blue dots
 799 assuming $j=0.5$ and 2 km.

800

801

Earthquake name	E_R (J)	M_0 (Nm)	E_R/M_0	$\Delta\sigma$ (MPa)	σ_a (MPa)	η_R (%)	References.
2000 Tottori	5.7e13	2.5e18	2.3e-5	23	0.7	6	Ross et al., 2018
1992 Landers	4e15	8e19	4e-5	11	1.7	25	J. B. Fletcher & McGarr, 2006
1999 Hector Mine	3e15	6e19	5e-5	6	1.5	50	Kaverina, 2002
2004 Parkfield	1.1e13	1e18	1.1e-5	2	0.3	25	Kim & Dreger, 2008; Ma et al., 2008

802

803 **Table 2: Mainshock parameters for four earthquakes.** E_R is radiated energy, E_G is804 the energy dissipated in damage of various types, $\Delta\sigma$ is stress drop, σ_a is apparent805 stress, M_0 is seismic moment, and η_R is the radiation efficiency.

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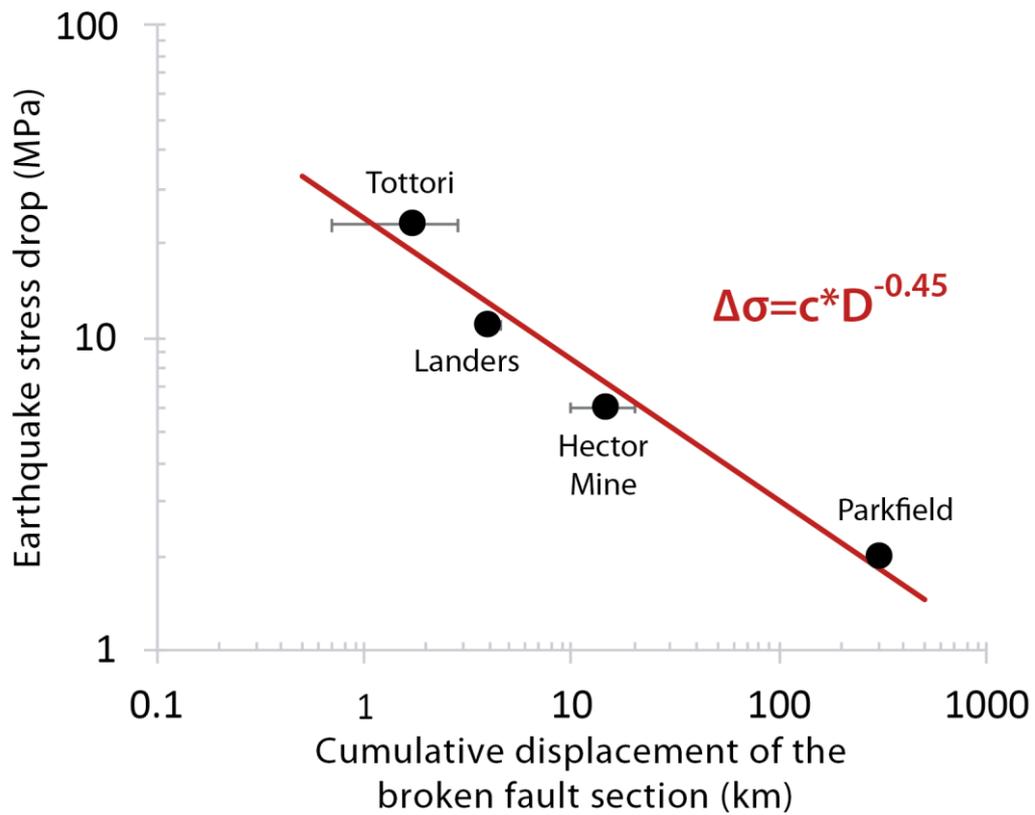


Figure 8; Perrin et al.

808

809 **Figure 8:** Earthquake stress drop ($\Delta\sigma$) as a function of cumulative displacement of the
 810 broken fault section (D) for earthquakes listed in Table 2. Parameter c is a constant.

811

4 **The Shear Deformation Zone and the Smoothing of Faults with Displacement**

5
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7
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12 * **Corresponding author: perrin@ipgp.fr**

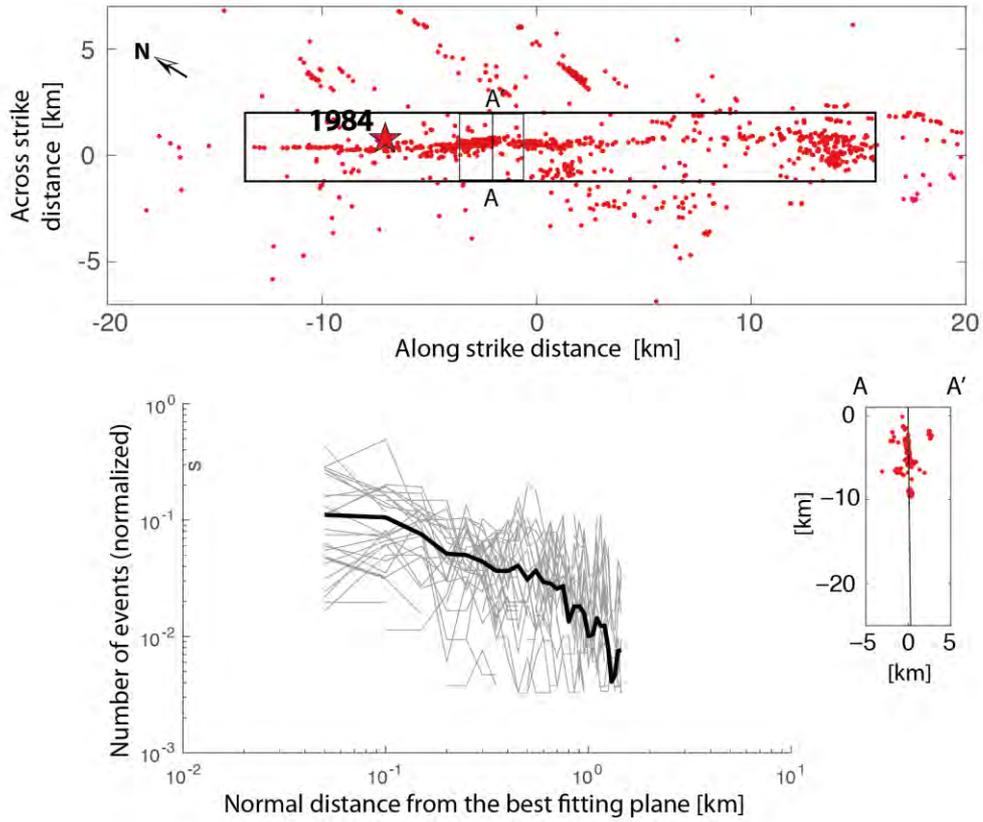
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14 **Contents of this file**

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16 Supplementary Figures S1 to S4

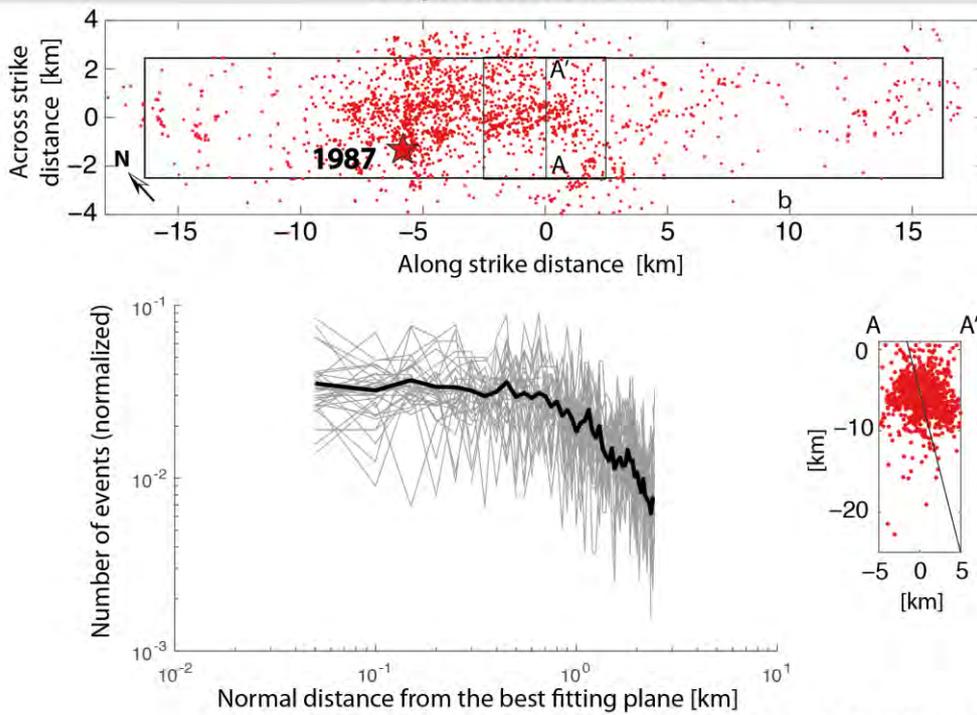
17
18 **Introduction**

19 The Supporting Information includes two figures denoted Supplementary Figure S1 and S2
20 that provide the analysis of the across-strike aftershock distributions for the eight earthquake
21 cases. Supplementary Figure S3 and S4 show other correlations between the size of the shear
22 deformation zone determined from the aftershock distributions and independent geological
23 parameters such as the initiation age and slip rate of the faults, respectively.

Morgan Hill 1984



Superstition Hills 1987

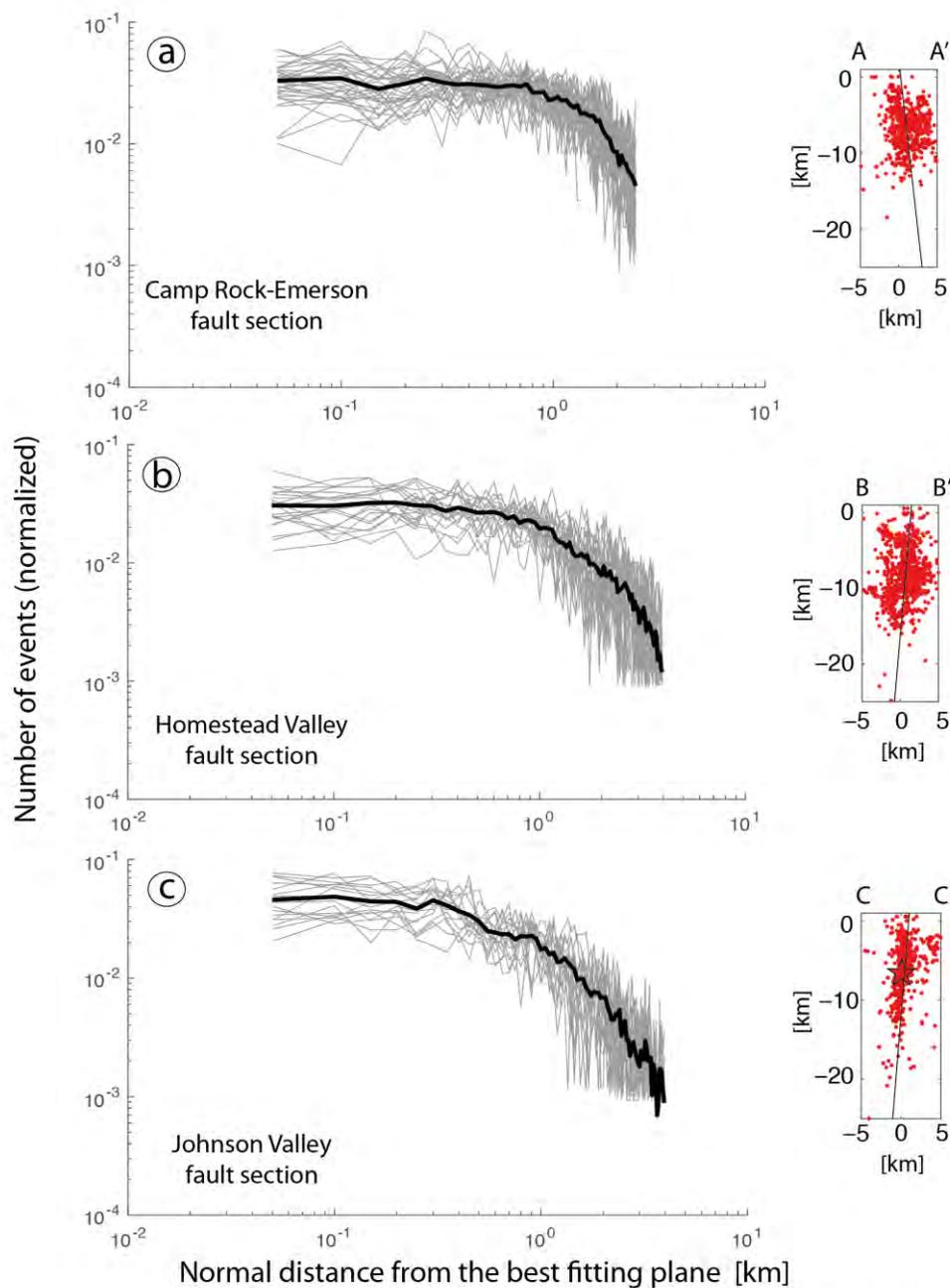
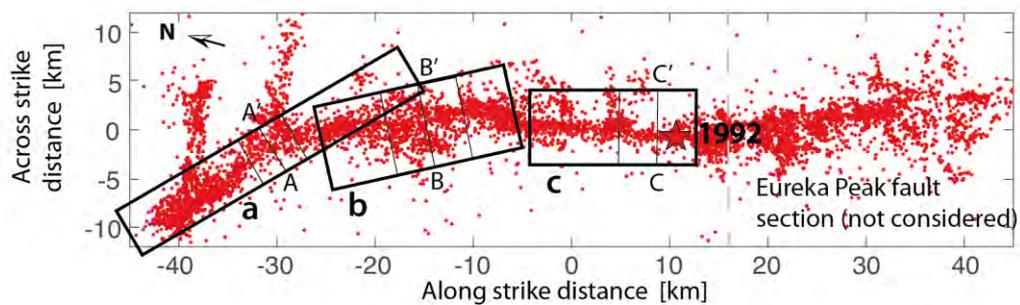


Supplementary Figure S1; Perrin et al.

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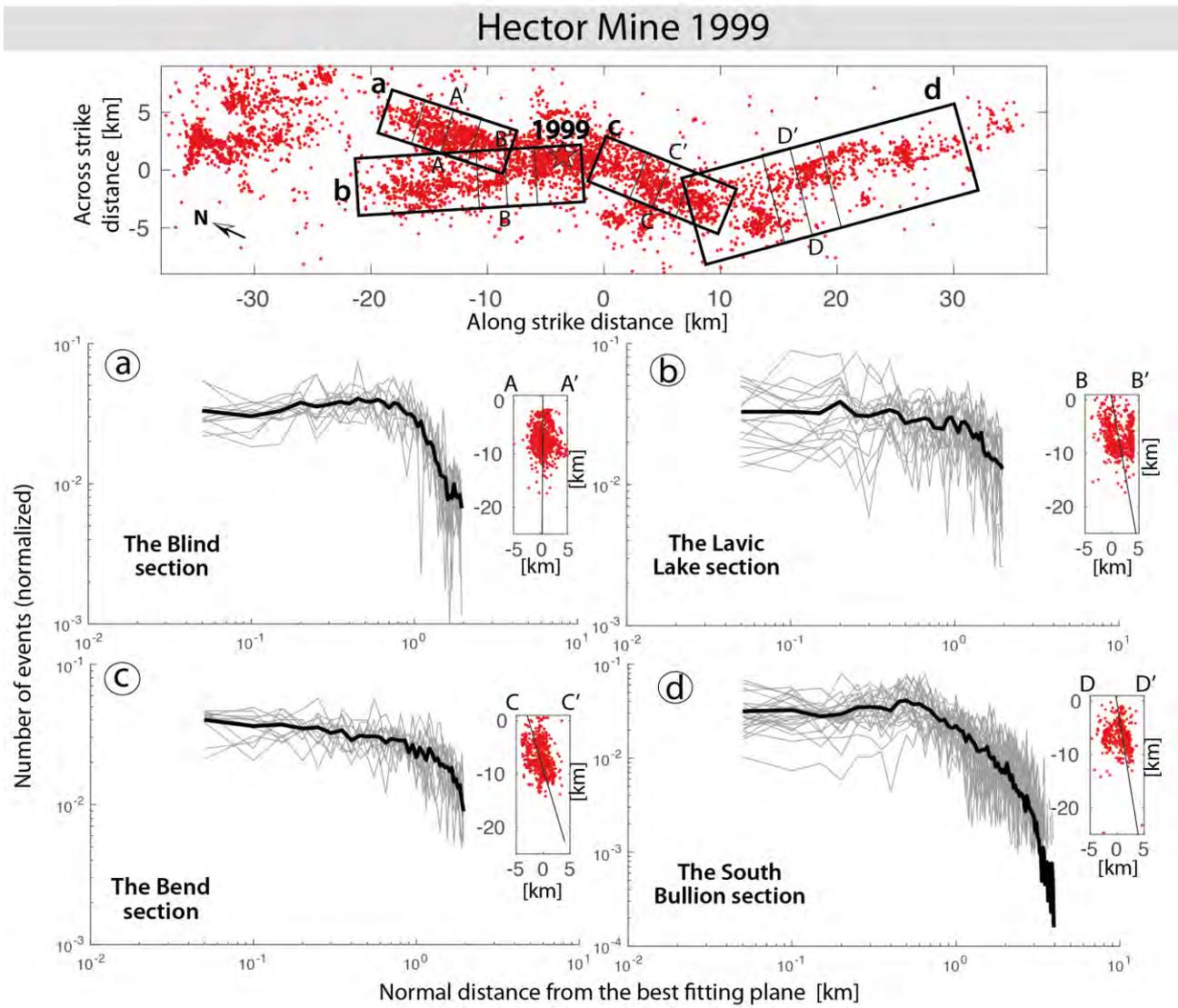
Landers 1992



Supplementary Figure S1 (following); Perrin et al.

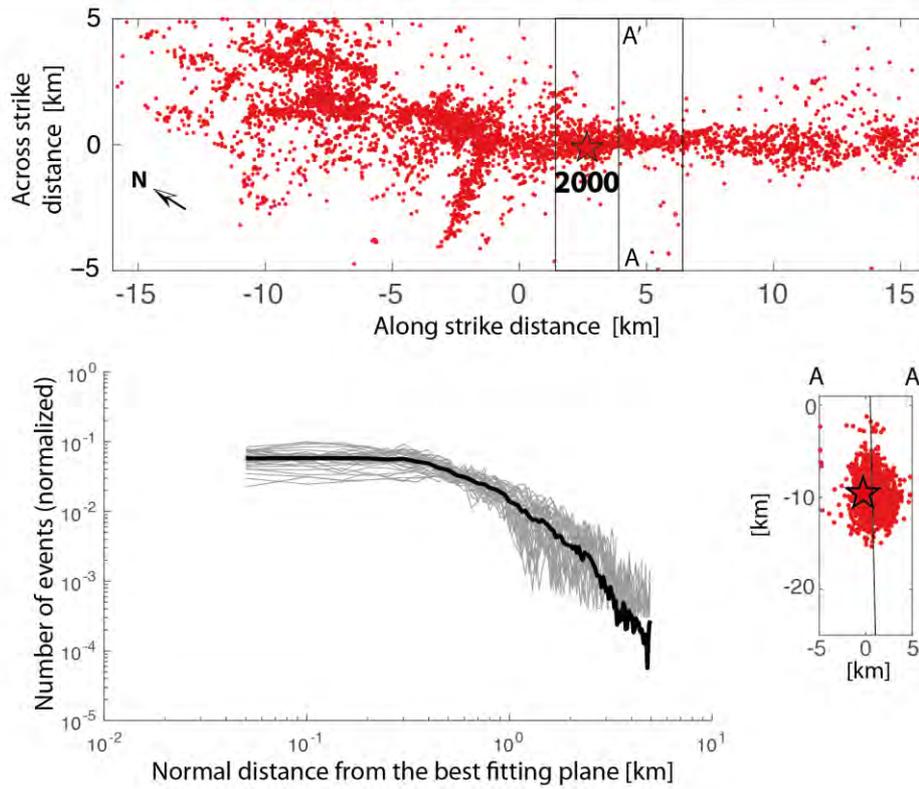
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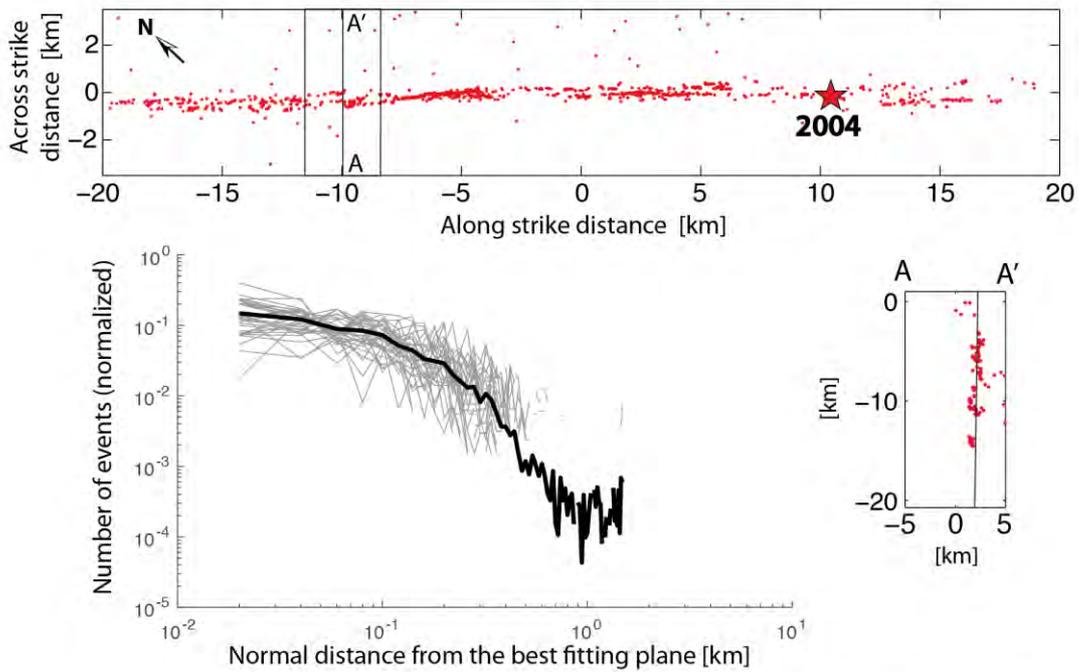


Supplementary Figure S1 (following); Perrin et al.

Tottori 2000



Parkfield 2004

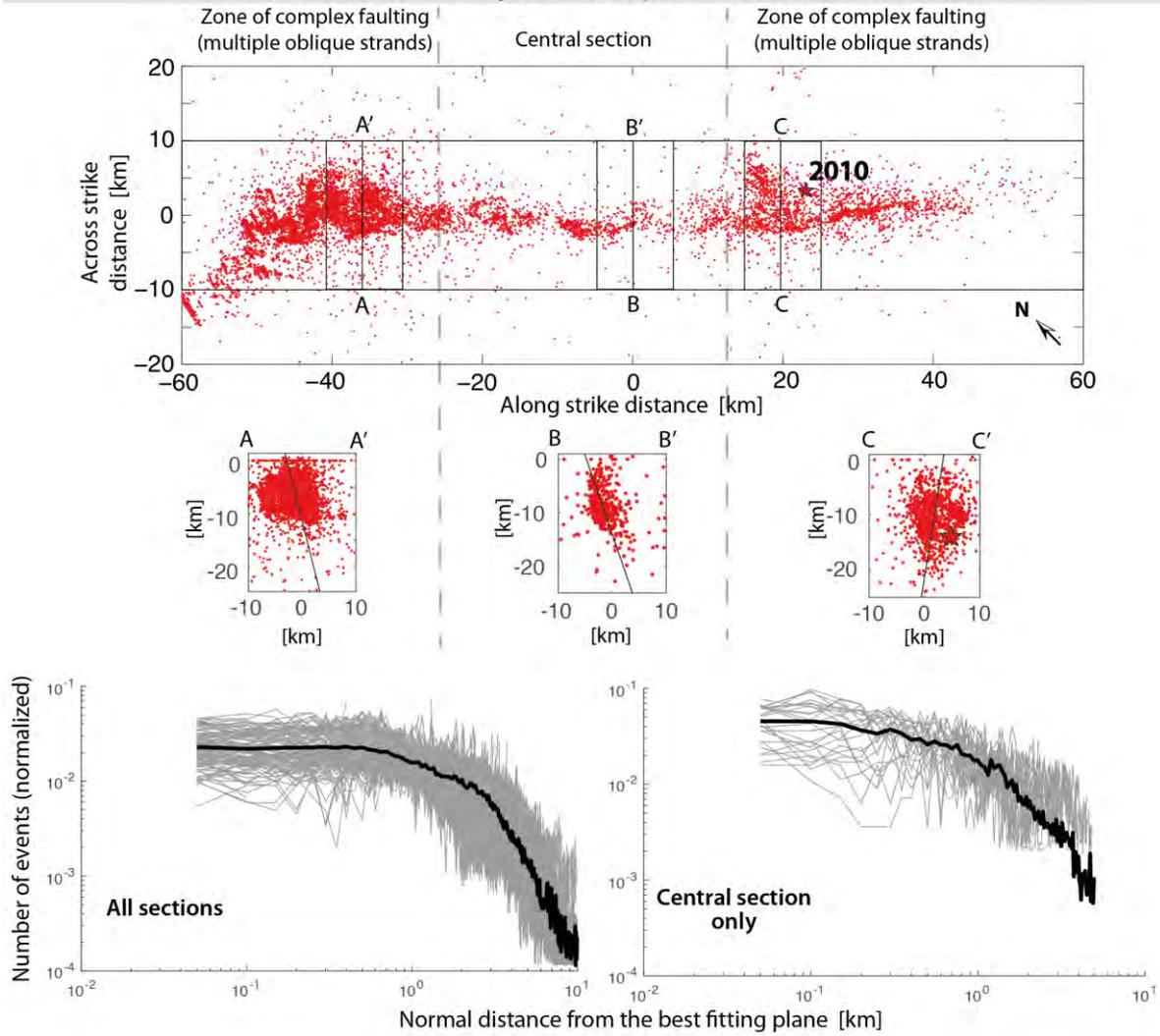


31

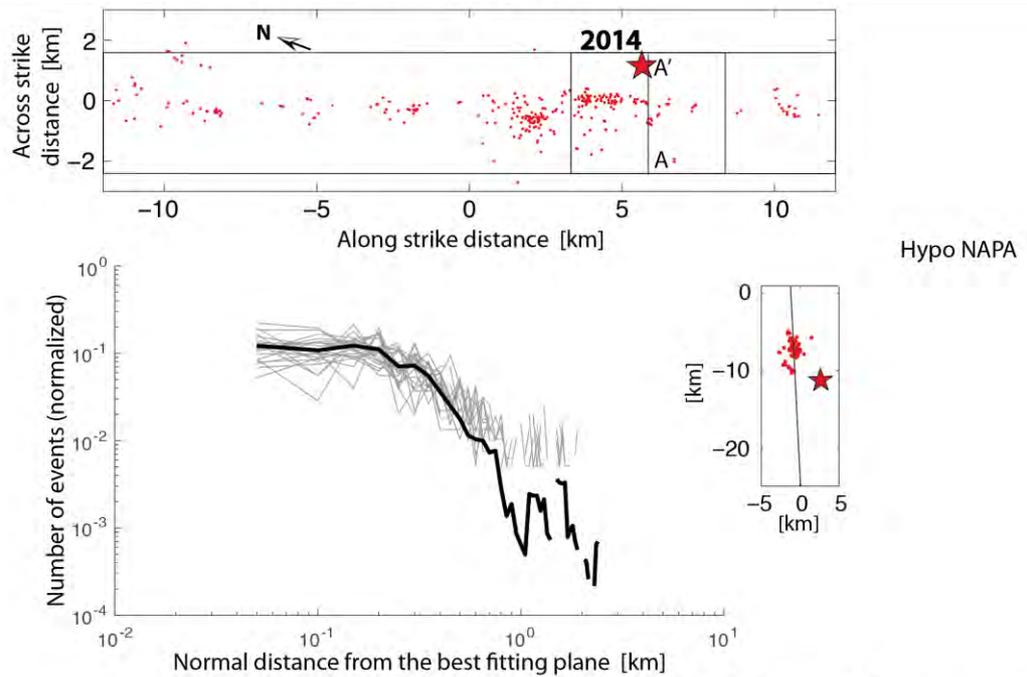
32

Supplementary Figure S1 (following); Perrin et al.

El Mayor Cucapah 2010

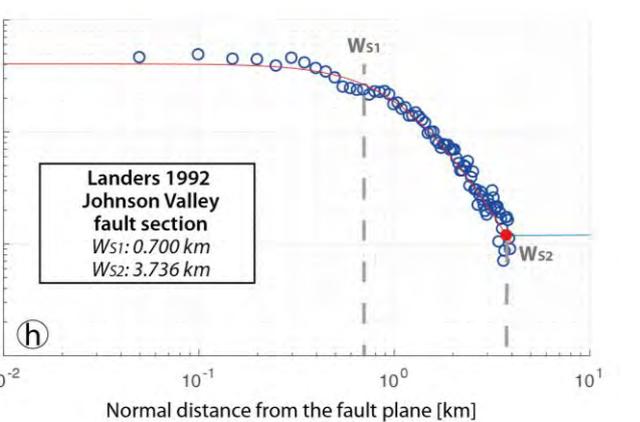
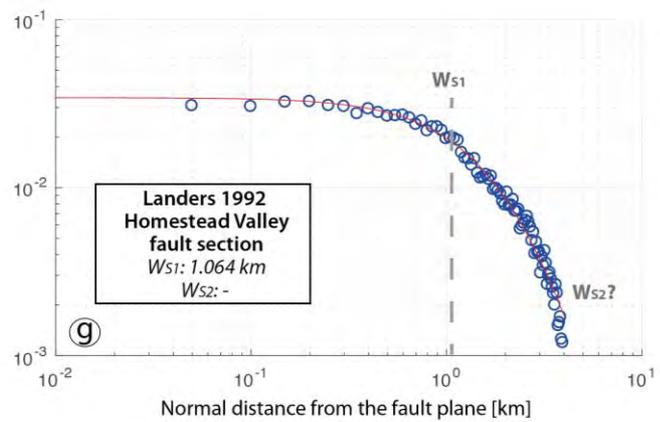
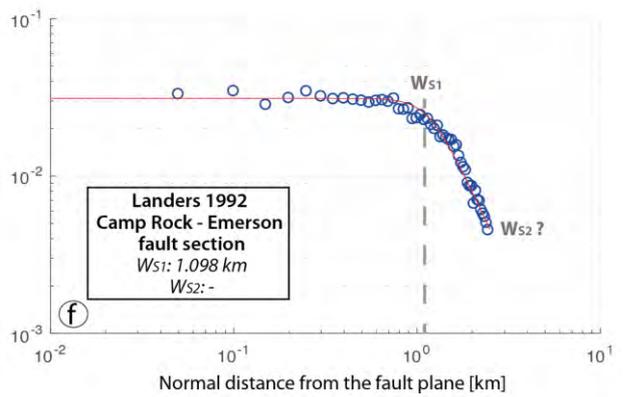
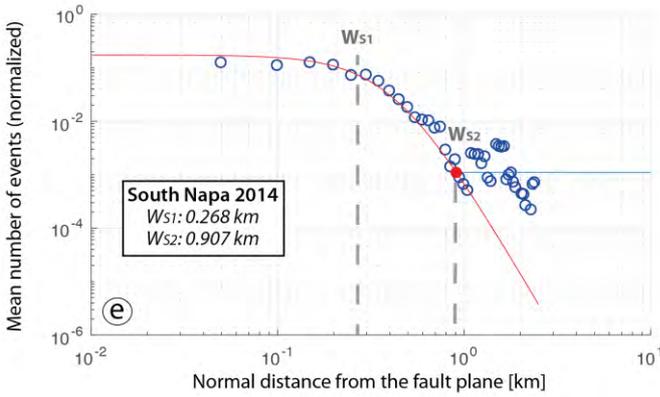
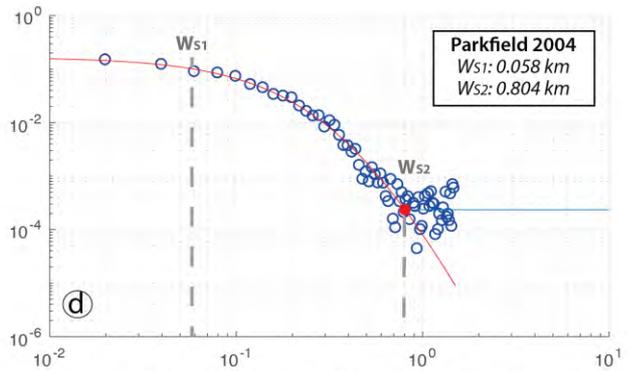
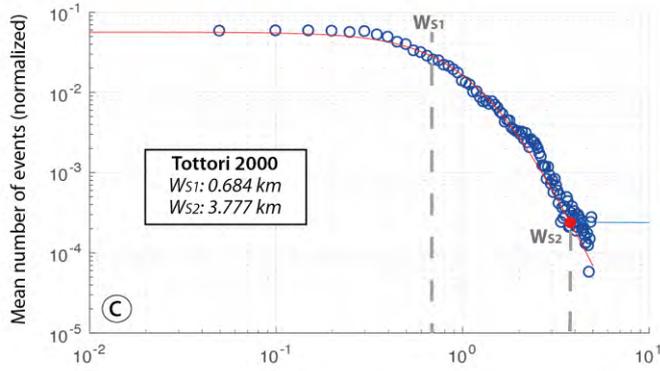
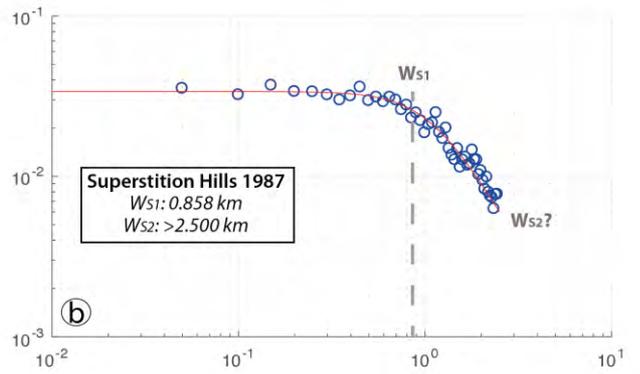
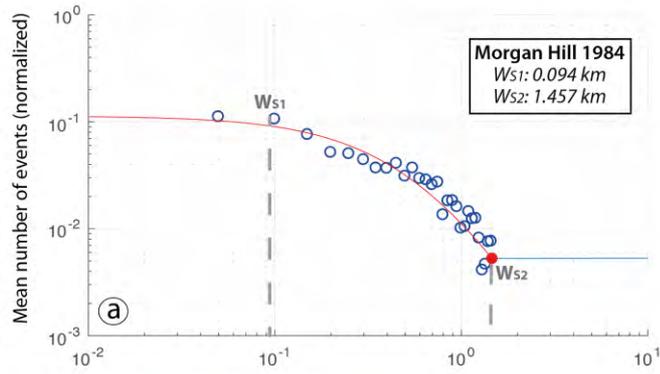


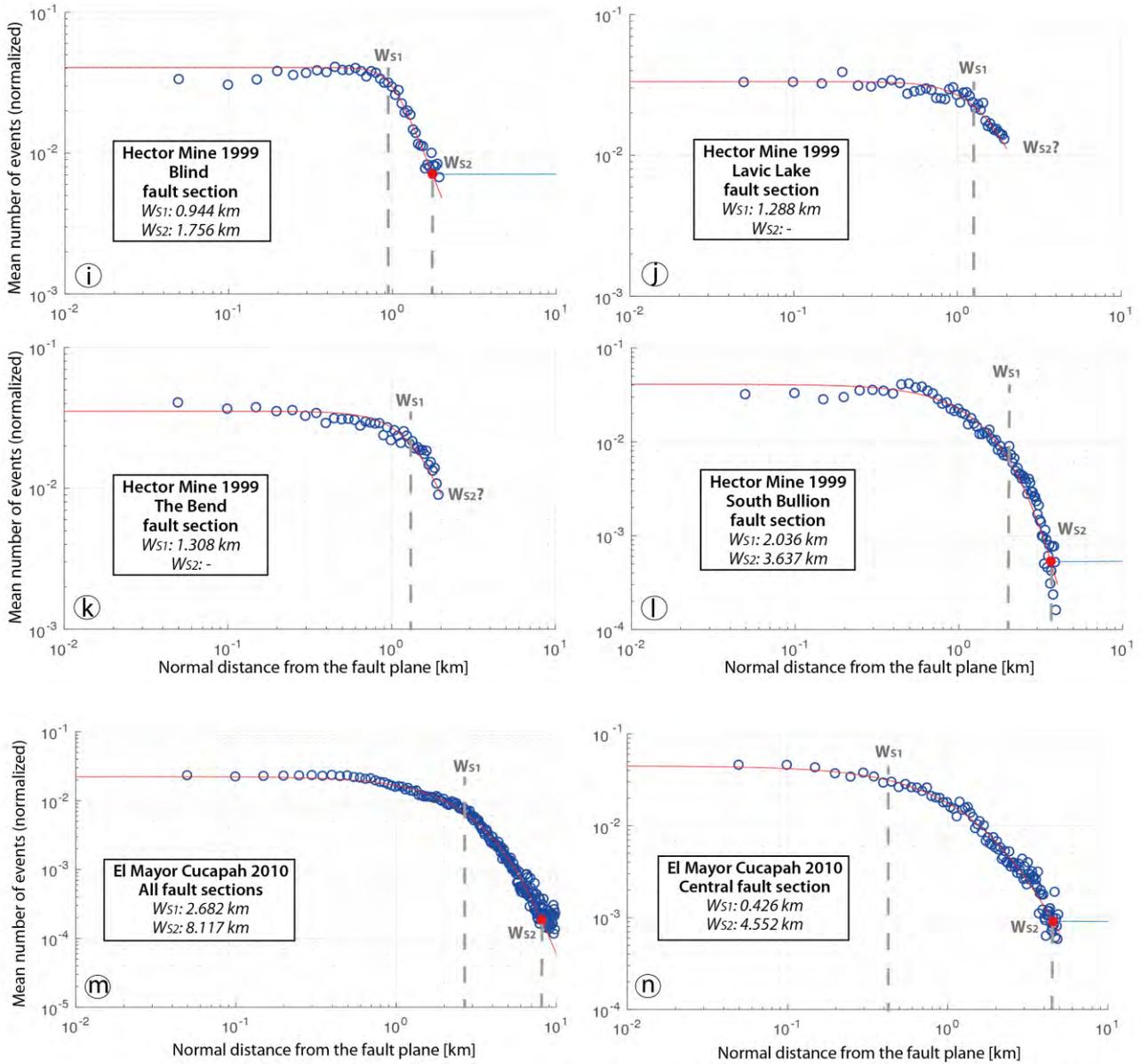
South Napa 2014



Supplementary Figure S1 (following); Perrin et al.

34 **Supplementary Figure S1: Aftershock distributions of the eight earthquakes analyzed**
35 **in this study (Morgan Hill 1984, Superstition Hills 1987, Landers 1992, Hector Mine**
36 **1999 Tottori 2000, Parkfield 2004, El Mayor Cucapah 2010 and South Napa 2014).** (Top
37 panels) Map view of the distribution of aftershocks (red dots) during the 2 months following
38 the mainshock (red star) for each earthquake. If indicated, the thick black box shows the area
39 selected to perform our analysis. (Bottom panels) Fault normal aftershock distribution (grey
40 curves) measured from the best fitting plane in each box moving along the rupture trace.
41 Black curves are the mean of the grey profiles. The small insets show selected cross sections
42 going through the aftershock sequence (for locations see top panel). Depth in y-axis; across
43 strike distance in x-axis. The black line is the plane best fitting the aftershocks using PCA (red
44 dots).
45





Supplementary Fig. 2 ; Perrin et al. (following)

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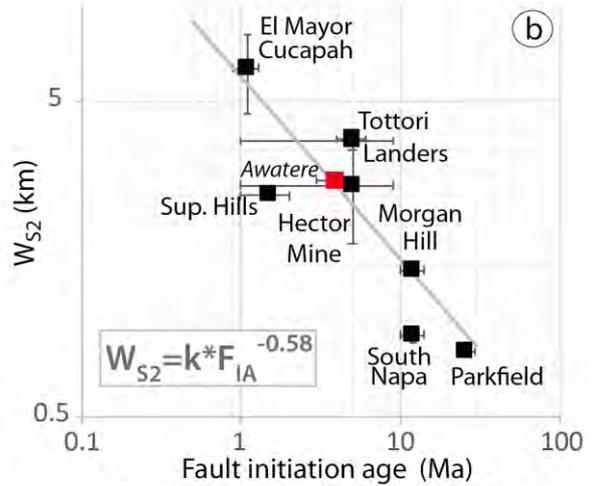
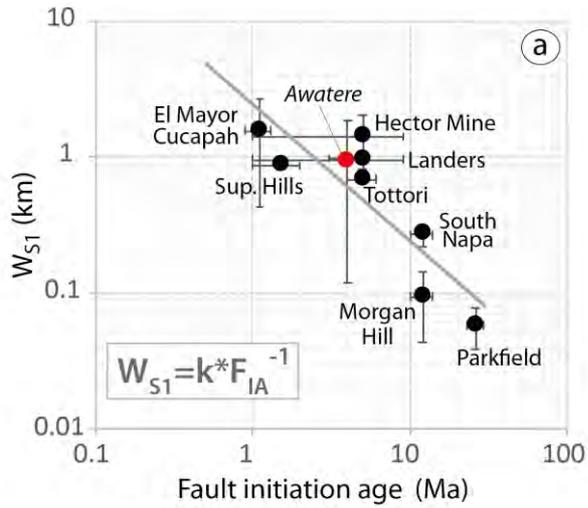
53 **Supplementary Figure S2: Determination of W_{S1} and W_{S2} parameters from the**
 54 **aftershock distribution of all earthquake cases: (a) Morgan Hill 1984 (b) Superstition**
 55 **Hills 1987 (c) Tottori 2000 (d) Parkfield 2004 (e) South Napa 2014, (f, g, h) Landers**
 56 **1992 (i, j, k, l) Hector Mine 1999 (m, n) El Mayor Cucapah 2010. Blue dots represent the**
 57 **mean distribution of each fault section (see black curve in Supp. Fig. S1). The red curve is the**
 58 **best fit of the distribution. The vertical gray dashed lines labeled W_{S1} and W_{S2} point out the**
 59 **locations where the numbers of earthquakes decrease rapidly and where they reach**

60 background level, respectively. W_{S1} is defined as location where the maximum in the 2nd
61 derivative is reached. W_{S2} is defined by the red dot, which is the intersection between the red
62 fit and the background level (horizontal blue line).

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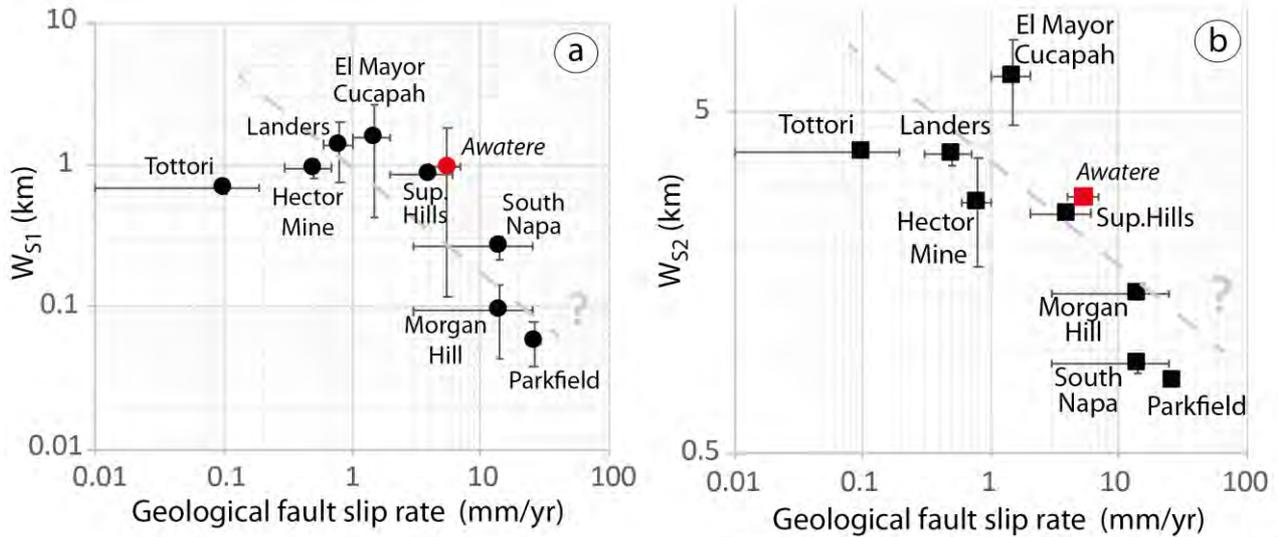
Supplementary Figure S3; Perrin et al.

66

67 **Supplementary Figure S3: Relations between (a) W_{S1} and (b) W_{S2} of the eight**
68 **earthquake fault zones considered in this study and the fault initiation age.** Power laws
69 are indicated by grey lines. For comparison, red symbols indicate geological surface
70 measurements along the Awatere fault (from Little, 1995).

71

72



Supplementary Figure S4; Perrin et al.

73

74 **Supplementary Figure S4: Relations between (a) W_{S1} , (b) W_{S2} of the eight earthquake**
75 **fault zones considered in this study and the geological fault slip rate.** Possible power
76 laws are suggested by grey dashed lines. For comparison, red symbols indicate geological
77 surface measurements along the Awatere fault (from Little, 1995).

78