A combined modeling and measurement approach to assess the nodal tide modulation in the North Sea

Robert Hagen¹, Andreas Plüß¹, Leon Jänicke², Janina Freund¹, Jürgen Jensen², and Frank Kösters¹

¹Federal Waterways Engineering and Research Institute ²University of Siegen

November 25, 2022

Abstract

The correct representation of the 18.61 year nodal tide is essential for an interpretation of the evolution of mean sea level, as errors cause misleading bias. The nodal tide is currently estimated by applying correction factors in harmonic analysis, which are derived from the equilibrium tide. From the equilibrium tide, correction values f for amplitude and u for phase are determined, which alter lunar tidal constituents, depending on the nodal cycle. This approach has proven to be valid for many tide gauges, even though the impact of the nodal tide in shelf seas has been shown to differ from their theoretical correction value. Hence, tidal constituents from tide records in the North Atlantic shelf region were analyzed for their nodal amplitude and phase lag with a new multiple, non-linear regression approach, which is able to approximate the nodal modulation quantitatively and its agreement to the theoretical equilibrium tide. Results show an overestimation of the lunar M and N constituents by the equilibrium of more than 2.7% in the Wadden Sea, while O and K are underestimated by 1 to 4.6%, which would produce an error of 2 to 5 cm e.g. in the German Wadden Sea. Additionally, a process-based model of the North Sea was applied at the diurnal minimum and maximum of the nodal cycle to calculate the spatial distribution of f and u. Model results reproduce a regionally varying pattern of f and u, indicating how the amplitude modulation of nodal constituents in shallow areas is distributed.

A combined modeling and measurement approach to assess the nodal tide modulation in the North Sea

Robert Hagen¹, Andreas Plüß¹, Leon Jänicke², Janina Freund¹, Jürgen Jensen² and Frank Kösters¹

 $^1{\rm Federal}$ waterways engineering and research institute Hamburg, Germany $^2{\rm Research}$ Institute for Water and Environment

Key Points:

1

2

3

5

7

8	•	Nodal modulation can be extracted from tide records through multiple, non-linear
9		fitting of annually analyzed tidal constituents.
10	•	Theoretical nodal modulation, derived from the equilibrium tide theory, does not
11		apply consistently in the North Sea.
12	•	Friction causes the generation of shallow water tides, which influence the nodal
13		modulation of lunar constituents and S_2 significantly.

Corresponding author: Robert Hagen, robert.hagen@baw.de

Abstract 14

The correct representation of the 18.61 year nodal tide is essential for an interpretation 15 of the evolution of mean sea level, as errors cause misleading bias. The nodal tide is currently 16 estimated by applying correction factors in harmonic analysis, which are derived from 17 the equilibrium tide. From the equilibrium tide, correction values f for amplitude and 18 u for phase are determined, which alter lunar tidal constituents, depending on the nodal 19 cycle. This approach has proven to be valid for many tide gauges, even though the impact 20 of the nodal tide in shelf seas has been shown to differ from their theoretical correction 21 value. Hence, tidal constituents from tide records in the North Atlantic shelf region were 22 analyzed for their nodal amplitude and phase lag with a new multiple, non-linear regression 23 approach, which is able to approximate the nodal modulation quantitatively and its agreement 24 to the theoretical equilibrium tide. Results show an overestimation of the lunar M_2 and 25 N_2 constituents by the equilibrium of more than 2.7% in the Wadden Sea, while O_1 and 26 K_2 are underestimated by 1 to 4.6%, which would produce an error of 2 to 5 cm e.g. in 27 the German Wadden Sea. Additionally, a process-based model of the North Sea was applied 28 at the diurnal minimum and maximum of the nodal cycle to calculate the spatial distribution 29 of f and u. Model results reproduce a regionally varying pattern of f and u, indicating 30 31

how the amplitude modulation of nodal constituents in shallow areas is distributed.

Plain Language Summary 32

The nodal tide is a part of the tidal regime, which changes the tidal range on a reoccurring 33 timescale of 18.61 years, originating from the gravitational force of the moon. A nodal 34 amplitude can be up to $30 \ cm$, which makes its accurate consideration essential for the 35 analysis of sea level rise. In current studies, the influence of the nodal tide is approximated 36 percentage-wise, as its reoccurrence interval is too long for conventional analysis. This 37 study has found, based on 31 tide records in the European North Sea, that current analysis 38 methods are inaccurate in the Northern English Channel and the Wadden Sea by several 39 centimeters based on the influence of the nodal tide. This is analyzed with a new method, 40 which uses statistical methods to approximate the nodal tide from measured tide records. 41 We conclude that the inaccurate estimate is restricted to shallow and geometrically complex 42 parts of the North Sea. As most tide gauges are located near the coast in shallow water, 43 these findings may have major implications on the correct approximation of the mean 44 sea level (MSL). 45

46 1 Introduction

The scientific assessment of past and future mean sea level (MSL) trends requires 47 reliable predictions of natural cyclic behavior on short and long time scales. Typical cycles 48 concerning sea level are tides, which are a result of the gravitational potential of sun and 49 moon, centrifugal force of the earth and meteorological forcing. Tides are distinguished 50 by their frequency, which is predominantly diurnal or semidiurnal, even though monthly, 51 interannual, annual and perennial frequencies exist as well. The nodal tide (Bradley, 1728) 52 is a harmonic signal with a period of 18.61 years, caused by the precession of the lunar 53 ascending node (Pugh, 1987). It is the most important low frequency tidal constituent 54 apart from the lunar perigee and it has shown to have an amplitude of up to 30 cm (Peng 55 et al., 2019). In order to consider the nodal tide in MSL analysis, the theoretical equilibrium 56 tide concept is applied (Proudman, 1960; Godin, 1986; Woodworth, 2012). Non-resolved 57 low frequency cyclic behavior of water levels may lead to an erroneous estimation of sea 58 level rise (SLR). The influence of the nodal cycle variations on the tidal potential of e.g. 59 M_2 is assumed to be 3.7 % on global average (Haigh et al., 2011) or 2.2 cm in global mean 60 amplitude (Baart et al., 2012). However, local effects of the nodal cycle can vary significantly 61 and the greatest values occur in diurnal regions with tidal ranges of $\geq 4 m$ (Haigh et 62 al., 2011). Spatial variations occur not only due to variable water depths but also due 63 to non-linear frictional, tidal-tide interactions (Ku et al., 1985), changing energy propagation 64 or/dissipation and other non-linear effects (Jay et al., 2015). The magnitude and spatial 65 dependence of these changes already make it evident that the nodal cycle cannot be neglected 66 for water level analysis based on tide gauge data, as it would cause a bias. Pugh (1987) 67 also emphasized that the nodal cycle is significant, but difficult to separate for MSL determinations. 68 Therefore, the nodal component of a lunar constituent must either be eliminated or equalized 69 by considering only full nodal periods. This applies not only to tidal analysis but to MSL 70 studies and tidal high and low water level analyses as well, especially when trends are 71 estimated (Jensen et al., 1988, 1992). The Dutch coast is an example for this, where a 72 non-consideration of the nodal cycle conceals the changes in MSL (Baart et al., 2012). 73 This necessity occurs not only in reconstructions, but also in projections. In the case of 74 reconstructions, a correction is necessary for both tidal analyses and MSL determinations 75 from gauge data in order to obtain unbiased results. 76

Even though long tide records do exist today, a reliable detection of the nodal tide 77 signal remains difficult, e.g. due to data quality limitations, noise (Rossiter, 1967; Trupin 78 & Wahr, 1990) or overlying trends (Woodworth & Blackman, 2004; Woodworth et al., 79 1991). The commonly applied correction for the nodal tide in harmonic analysis (e.g. 80 UTide by Codiga (2011) is based on assumptions from the equilibrium tide theory (Pugh, 81 1987). Tidal constituent amplitudes from harmonic analysis are modulated by a percentage-82 wise adjustment (f, i.e. nodal modulation) and a nodal phase lag (u), respectively. These 83 correction parameters are considered to be globally constant (Trupin & Wahr, 1990; Woodworth, 84 2012). The consideration of the nodal modulation (also nodal satellite variation Haigh 85 et al. (2011)) in amplitude and phase is therefore performed by applying the stationary 86 correction parameters f and u (also f - u correction following Pugh (1987)) to lunar, 87 tidal constituents. Nodal amplitudes and phase lags, as well as nodal satellite variation, 88 have been investigated globally (Cherniawsky et al., 2010; Menéndez & Woodworth, 2010) 89 and regionally e.g. in the North Sea (Amin, 1985; Hansen et al., 2015; Jensen et al., 1992; 90 Woodworth et al., 1991), the Gulf of Maine (Ray, 2006), the Mediterranean Sea (Shaw 91 & Tsimplis, 2010), the Chinese Sea (Feng et al., 2015) and the western coast of Australia 92 (Amin, 1993) to name only a few. Evaluations of the f-u correction parameters have 93 been published by Cherniawsky et al. (2010), who carried out a harmonic analysis of satellite 94 sea surface elevation data to determine nodal satellites. Their analyzed nodal amplitudes 95 overestimated the equilibrium tide parameters f and u, especially when dealing with small 96 amplitudes. Contrary to this, an analysis of tidal constituents in the Chinese seas has 97 shown an underestimation of the nodal modulation parameters for M_2 and N_2 , while O_1 98 and K_1 agree well with the theoretical values (Feng et al., 2015). In the Mediterranean 99 Sea, the nodal variation agrees well overall with the equilibrium assumption (Shaw & 100

Tsimplis, 2010). Hence, many findings either challenge or agree with the statements from
 Trupin and Wahr (1990), who stated that the amplitude and phase are close to their equilibrium
 amplitude and phase. However, it must be noted, that regional exceptions, e.g. for the
 North Sea, were made in their results.

Thus, as the nodal modulation does not follow the equilibrium tide theory consistently 105 across all coastal waters, the first major aim of this study is to develop a method to quantify 106 the nodal satellite variation, i.e. nodal correction parameters f and u, from tide records. 107 We use a multiple, non-linear regression approach to calculate the nodal modulation at 108 gauges in the European North Sea from tidal constituents, before comparing them to the 109 equilibrium value. The second goal of this study is the identification and description of 110 the processes causing the deviation from equilibrium modulation. In order to assess the 111 spatial distribution for f and u, numerical simulations are carried out. In fact, Woodworth 112 (2012) already suggested a barotropic approach for 19 consecutive years without explicit 113 loading as a way to advance the topic of the accuracy of the current nodal correction formulation. 114 In this study, we deploy a three-dimensional, astronomically forced, numerical model of 115 the North Sea at the diurnal minimum and maximum of nodal modulation in order to 116 obtain spatial distributions through differences. These results provide detailed, spatial 117 information about the regional nodal modulation and phase lag. Based on these results, 118 a recommendation on how to consider nodal satellite variation in the future can be made, 119 which is the third major aim of this study. 120

This paper is organized as follows: The applied data and the preprocessing are discussed in the first part from Section 2.1 to 2.3. Afterwards a brief description of the numerical model and its validation are given in Section 2.4. Section 3.1 to 3.4 describe the results from the multiple non-linear regression fitting approach, before the outcome of the numerical simulations is described in Section 3.5. Results are interpreted and discussed in Section

126 4.

¹²⁷ 2 Material and methods

128

2.1 Nodal Tide Modulation

Modern harmonic tidal analyses extract amplitude and phase of tidal constituents, 129 defined by given astronomical frequencies, from tide records. The astronomical frequencies 130 (i.e. tidal constituents) are defined by their lunar or solar origin and their reoccurance 131 interval, hence the semidiurnal moon tide is called M_2 . The harmonic analysis (i.e. satellite 132 method) follows the development of tidal potential theory (Doodson, 1921, 1928) and 133 is well documented with its modern formulations (Foreman et al., 2009; Godin, 1972; Pugh, 134 1987). Tidal constituents underlie interannual, annual and perennial fluctuations, which 135 have an influence on the results of a harmonic analysis (Feng et al., 2015; Gräwe et al., 136 2014; Hansen et al., 2015; Müller et al., 2014). In this study, we will focus on fluctuations 137 with an interannual frequency. These are most prominently represented by the nodal tide 138 (18.61 years) and the lunar perigee (8.85 years), while the solar perigee is negligible for 139 practical applications due to its long timescale of 20,392 years. For a full review on the 140 scientific background to the nodal tide and the lunar perigee we recommend Haigh et 141 al. (2011). In order to consider the nodal tide variation, tidal constituents are modified 142 in harmonic analysis based correction parameters from the equilibrium tide theory (Pugh, 143 1987). The modulation effect amounts to an amplitude adjustment of 3.7~% or phase lag 144 of -2.1 ° for the M_2 or 28.6 % and -17.7 ° for K_2 constituent for example. This correction 145 procedure is referred to as f - u correction. Since tidal records are typically analyzed 146 for less than a full nodal cycle in practice, tidal constituents are corrected for the nodal 147 variation within a harmonic analysis. However, the f-u satellite correction (i.e. Table 148 1 following Pugh (1987)) assumes that nodal modulation always follows the equilibrium 149 tide theory, which is valid for most gauges (Trupin & Wahr, 1990), but has been shown 150 to be inappropriate locally, especially in shelf seas. 151

Table 1: Nodal correction parameters f (amplitude) and u (phase) derived from the equilibrium tide. N is the longitude of the moon's ascending node in ° with 0 ° being the time at which diurnal terms are at a maximum, e.g. in November, 1987 or June 2006.

	f (amplitude)	u (phase)
$\overline{M_m}$	$1.000 - 0.130 \cos(N)$	0.0 °
M_f	$1.043 + 0.414 \cos(N)$	$-23.7 \circ sin(N)$
Q_{1}, O_{1}	$1.009 + 0.187 \cos(N)$	$10.8 \circ sin(N)$
K_1	$1.006 + 0.115 \cos(N)$	$-8.9 \circ sin(N)$
M_2, N_2	$1.000 - 0.037 \cos(N)$	$-2.1 \circ sin(N)$
K_2	$1.024 + 0.286 \cos(N)$	$-17.7 \circ sin(N)$

Table 1 lists the correction values f and u for lunar tidal constituents. Note that 152 the amplitude and phase lag are maximal for the diurnal constituents at $N = 0^{\circ}$ for M_f , 153 Q_1, O_1, K_1 and K_2 , which would be in June 2006, and for M_2, N_2 at $N = 180^{\circ}$ which 154 would be e.g. in October 2015. Thus, if one imagines an exemplary mean amplitude of 155 1 m for M_2 , the f-u correction procedure would correct M_2 in June 2006 (minimum) 156 to 0.963 m and in October 2015 (maximum) to 1.037 m, giving M_2 a nodal amplitude 157 of 0.037 m. If K_2 had a mean amplitude of 1 m, its amplitude would be 1.286 m in June 158 2006 and 0.714 m in October 2015. 159

¹⁶⁰ 2.2 Tide Records

This study utilizes 31 North Sea and North Atlantic tide records from Germany, 161 Great Britain, France, the Netherlands and Denmark as a data basis for harmonic analysis. 162 Figure 1 lists all gauges and the period of valid data hereinafter. The longest tide records 163 are located in Brest, France (1845-2019), Delfzijl, the Netherlands (1879-2019), Esbjerg, 164 Denmark (1889-2015), Newlyn, Great Britain (1915-2016) and Cuxhaven, Germany (1918-165 2018). Most Dutch and British tidal records start in the 1970s, while the German measurements 166 start predominately in the late 1990s. The data was carefully controlled by visual inspection, 167 checked for anomalies and harmonized to equidistant hourly values, as required for harmonic 168 analyses (Codiga, 2011). Otherwise, tide records remain unchanged, thus they were not 169 cleared from MSL trend, surge or noise. In order to determine the nodal component, a 170 time series of at least 19 years is required and we define, in accordance with Peng et al. 171 (2019), a minimum completeness of at least 60 % valid hourly entries for each year and 172 tide record for further analysis. 173



Figure 1: Tide records used in this study in the northern Atlantic and the North Sea from 1846 to 2019 with a temporal resolution of 1 hour. The data is arranged in the direction of the propagation of the Kelvin wave (counterclockwise) in the North Sea (Lerwick to Lowestoft), the English Channel (Brest to Ijmuiden) and the Dutch and German Wadden Sea (Vlieland Haven to Esbjerg).

2.3 Nodal Tide Fitting

174

In literature, different techniques are applied to extract the nodal tide from water 175 level signals. Most recently, the quantile fitting method (Woodworth & Blackman, 2004) 176 was applied to gauges worldwide showing clear nodal signals in 371 of 527 gauges (Peng 177 et al., 2019) in the 90 % quantile. The harmonic analysis for the nodal constituents has 178 also been carried out globally (Cherniawsky et al., 2010), using a 16 year long satellite 179 altimetry data set. Additionally, multiple non-linear regressions of annual tidal characteristic 180 values (Jensen et al., 1988, 1992; Woodworth et al., 1991), mean sea level (Baart et al., 181 2012; Hansen et al., 2015) and tidal constituents (Feng et al., 2015; Shaw & Tsimplis, 182

2010) was conducted to obtain information about the amplitude and phase of the nodal
 tide.

The results of the quantile method for tidal characteristic values or their percentiles 185 as well as water level quantiles in the western English Channel and the Wadden Sea were 186 inconclusive in this study, as neither nodal nor lunar perigee signal could be detected. 187 We suspect that frequent wind and storm surge events as well as strong shallow water 188 effects deform the signals and limit the applicability of the quantile analysis method. Thus, 189 the nodal modulation model is applied to tidal constituents. The model is a non-linear, 190 least square fitting approach shown in Equation 1 (Feng et al., 2015; Jensen et al., 1992; 191 Peng et al., 2019) including an acceleration trend term (Baart et al., 2012). We chose 192 an annual analysis period (January to December) for a reliable estimation of "true" (Pugh, 193 1987) tidal constituents and to minimize the effect of interannual variation of partial tides 194 in shelf seas (Gräwe et al., 2014; Menéndez & Woodworth, 2010; Müller et al., 2014). 195

In Equation 1 the parameter a_0 denotes the initial sea level, a_1 accounts for the linear and a_2 for an accelerated trend with a time lag φ_1 . The nodal tide term is represented by the amplitude a_3 , the nodal frequency ω and a phase lag φ_2 . The variable t represents the time in Julian years (365.25 d).

$$H(t) = a_0 + a_1 t + a_2 (t - \varphi_1)^2 + a_3 \sin(\omega t - \varphi_2))$$
(1)
$$\omega = \frac{2\pi}{18.61}$$

To account for the rapid change in tidal constituents from the 1980s (Haigh et al., 201 2019; Müller, 2011) a time lag φ_1 has been added to the acceleration term a_2 (Baart et 202 al., 2012; Houston & Dean, 2011). The goodness-of-fit between data and the non-linear 203 model estimation is described by the coefficient of determination R^2 . R^2 compares the 204 dependence of two data sets with 1 being a perfect estimation. Following Peng et al. (2019) 205 we chose results with a value of $R^2 \leq 0.5$ to be statistically insignificant in this study. 206 Note, that fitting of the lunar perigee cycle was attempted by adding an additional term 207 to Equation 1 analog to a_3 with a period of 4.4 years. However, results rarely produced 208 statistical significance within the entire study area for the lunar perigee, which is consistent 209 with previous results (Haigh et al., 2011; Menéndez & Woodworth, 2010). Whenever there 210 was a satisfying agreement for the lunar perigee $(R^2 \ge 0.5)$, its amplitude was more 211 than 10 times smaller than the nodal amplitude. Therefore the lunar perigee has not been 212 considered in the following. 213

214

200

2.4 Hydrodynamic Model

Even though the North Sea is monitored by one of the most closely meshed measurement 215 networks worldwide (Sündermann & Pohlmann, 2011) information between tide gauges 216 and far-off the coast is very limited. In order to close these gaps, this study deploys a 217 numerical North Sea model, which is located on the European continental shelf in the 218 northeastern Atlantic (Figure 2). The majority of the grid cells has been located within 219 the German Bight and the Dutch Wadden Sea, as complex bathymetry with steep slopes 220 and shallow embankments requires high grid resolution in order to reproduce realistic 221 energy dissipation (Rasquin et al., 2020). 203.500 unstructured, horizontal elements have 222 been used with an increasing grid resolution from typically 7.5 km in the open North Sea 223 to 350 m in the Wadden Sea to less than 50 m in the estuaries of the German Bight. 224

The UnTRIM² model (Casulli & Walters, 2000) with the novel subgrid approach (Casulli, 2009) has been applied in order to consider complex bathymetry details at low computational cost. By applying a finer subgrid (increasing 4 to 12 times of the horizontal grid resolution) within the computational grid, the bathymetric information and therefore volume can be estimated with less effort than in conventional grids (Sehili et al., 2014). The hydrodynamic model has been thoroughly validated with measurements (Bundesanstalt für Wasserbau et al., 2019b) and the validation results from e.g. the year 2012 show a ²³² root mean square error (RMSE) of $3.3 \ cm / 2.8^{\circ}$ for the M_2 , $1.1 \ cm / 4.1^{\circ}$ for the S_2 ²³³ and $0.7 \ cm / 3.5^{\circ}$ for the N_2 tidal constituent, respectively. Water levels display a RMSE ²³⁴ between 8 and 15 $\ cm$. The model uses a spatially varying bottom roughness, which has ²³⁵ been calibrated to optimally fit the M_2 constituent.

In this study, the three dimensional, hydrodynamic model is applied with a clear 236 focus on tidal dynamics. Other processes have not been considered (i.e. waves, salinity, 237 temperature, sediments, surge and meteorology) in order to isolate the astronomical forcing 238 entirely. Tidal constituents from the global tide model FES (FES2014 was produced by 239 Noveltis, Legos and CLS and distributed by Aviso+, with support from Cnes (https:// 240 www.aviso.altimetry.fr/)) were reconstructed with ut_reconstr (Codiga, 2011) at the 241 open boundary (blue line in Figure 2), using the default f - u correction. The model 242 bathymetry within the German Bight has been adapted from the EasyGSH-DB (http:// 243 easygsh-db.org/) project for the year 2006 (Bundesanstalt für Wasserbau et al., 2019a). 244 Bathymetry for the Dutch Wadden Sea was obtained from Rijkwaterstaat, for the English 245 coast from UKHO and for the French coast from SHOM. The remaining data gaps have 246 been filled with data from the EMODnet database (EMODnet Bathymetry Consortium, 247 2016).248



Figure 2: The study area North Sea, showing the grid lines in grey, the open boundary in blue and the closed boundary in black. The bottom right shows a representative grid resolution around the island of Norderney in Eastern Frisia, Germany.

249 **3 Results**

250

3.1 Fitting Evaluation

The dominant tidal constituents in the North Sea are the M_2 , S_2 , N_2 , O_1 , K_1 and K_2 components. In the following, the tidal constituents from measured tide gauge records given in Figure 1 are analyzed for their nodal amplitude modulation and phase lag using the fitting function from Equation 1. All harmonic analyses in the following are completed with the UTide algorithm (Codiga, 2011). UTide is applied using default settings with all tidal constituents available and without nodal correction.

The results of the analysis are shown in Figure 3 for two example locations, which have been chosen because of their different, geographical setting. Brest is located westwards from the North Sea in the north Atlantic Ocean while Büsum is placed within the German Bight near the Elbe and Eider estuary in the Wadden Sea. In order to quantify the goodnessof-fit, the R^2 has been calculated for each constituents nodal amplitude and phase lag in Brest and Büsum in Figure 4.



Figure 3: Fitting results for the tidal constituents M_2 , S_2 , N_2 , O_1 , K_1 and K_2 for Brest from 1846 - 2019 (top) and Büsum from 1954 - 2015 (bottom). The gray dots represent the resulting amplitude in m (left) and the phase in degree (right) of a harmonic annual analysis of water levels with their 95 % confidence interval from UTide. The dashed gray line indicates the linear and squared trend of the constituents, while the solid blue line represents the results of the multiple, non-linear regression fit.

The R^2 values indicate for Brest that the non-linear fitting method is reliable $(R^2 > 0.8)$ for all constituents but S_2 . In Büsum, the method yields only reliable results for O_1 and K_2 ($R^2 > 0.8$), while K_1 , M_2 and S_2 are on the verge of statistical insignificance ($R^2 > 0.5$). However, visual inspection of the amplitude fitting of e.g. M_2 or K_1 in Figure 3 suggests agreement between the fitting approach and available data. In Brest, R^2 is usually between 0.05 to 0.25 higher, while phase and amplitude R^2 are comparable. The fitting of N_2 was unsuccessful in Büsum for phase and amplitude with a $R^2 < 0.5$.



Figure 4: Coefficient of determination R^2 from the fitting for the tide records Brest and Büsum from Figure 3 with the function from Equation 1. A denotes the amplitude and gthe phase of each tidal constituent.

The R^2 distribution from Figure 4 is extended to all stations and tidal constituents in Figure 5 below. The gauges have been sorted in the direction of the counterclockwise propagating Kelvin wave in the North Sea with a break in Lowestoft, where the tidal waves from Scotland (Lerwick to Lowestoft) and the English Channel (Brest to Ijmuiden) unite towards the Dutch and German Wadden Sea (Vlieland Haven to Esbjerg). In the following, as the agreement between phase and amplitude coincides at most gauges, their R^2 will be discussed together.

The index of agreement R^2 is consistently ≥ 0.85 at all locations for O_1 and K_2 , 277 showing that these constituents are steadily extractable from all tide records. M_2 also 278 demonstrates high values for R^2 with several local exceptions such as the Dutch west coast 279 in the northeastern English Channel (Hoek van Holland to Ijmuiden), West-Terschelling 280 and Cuxhaven, whose R^2 is ≤ 0.5 for the amplitude modulation, even though the phase 281 lag agrees well for all stations. For K_1 , R^2 is between 0.6 and 0.93 with the exception 282 of Dunkerque (0.5). K_1 's R^2 diminishes in the English Channel from 0.83 in Cherbourg 283 to 0.61 Dover before improving slightly in the north eastern English Channel near Hoek 284 van Holland to a mean of 0.7. N_2 shows strong correlation (0.8 to 0.95) from Lerwick 285 to Dover, before its R^2 decreases in the northern English Channel in Westkapelle near 286 its amphidromical point, similar to M_2 . Further eastwards, N_2 fitting remains inconclusive 287 due to low statistical significance with the exception of Esbjerg where its nodal amplitude 288 is lower than 0.5 cm. S_2 shows sufficient R^2 from the English Channel to the Wadden 289 Sea, contrary to N_2 . Nevertheless, low correlation $(R^2 \ge 0.5)$ for S_2 can be seen for the 290 amplitude in Lerwick to Dunkerque excluding Immingham, North Shields and Lowestoft. 291 The phase of S_2 could not be fitted consistently, as R^2 is mostly ≤ 0.5 , though slight 292 phase modulation takes place in the Dutch and German Wadden Sea. The values for R^2 293 vary from 0.75 to 0.85 between Vlieland Haven and Büsum. 294



Figure 5: R^2 of amplitude and phase fitting as indicator for the goodness-of-fit of the multiple, non-linear regression approach for the components M_2 , S_2 , N_2 , O_1 , K_1 and K_2 . R^2 for the amplitude (A) is drawn in black, while the results of the phase (g) fitting are represented in gray. The x-axis shows the tide record locations from Figure 1.

3.2 Seasonal Variation

Since tidal constituents underlie constant interannual variations (Gräwe et al., 2014; 296 Müller et al., 2014), a sensitivity study is performed in order to quantify the effect of meteorological 297 forcing on the estimation of nodal amplitudes with Equation 1. The method described 298 with Equation 1 is now applied to all tide records in Table 2 for the constituent M_2 in 299 the summer s (May to October) and winter w (November to April) half year as well as 300 a full hydrological year a. In the following chapters, n denotes the nodal satellite of a 301 tidal constituent. The chosen gauges represent a region in the North Sea study area. The 302 303 English east coast (Aberdeen, Lowestoft), the English Channel (Brest, Roscoff, Dunkerque, Lowestoft), the Dutch Wadden Sea (Harlingen, Huibertgat) and the German Wadden 304 Sea (Alte Weser, Büsum) are investigated for seasonal effects. 305

Table 2: Comparison between the summer and winter half-year to quantify the meteorological impact on the the non-linear, multiple regression fitting of nodal modulation from Section 2.3. s denotes summer, w winter, a the full hydrological year and n a nodal satellite. R^2 (coefficient of determination) is given in order to describe the goodness-of-fit for each scenario.

	$M_{2n,s}$	$M_{2n,w}$	$M_{2n,a}$	$\frac{M_{2n,s}}{M_{2n,a}}$	$\frac{M_{2n,w}}{M_{2n,a}}$	$R^2{}_s$	$R^2{}_w$	$R^2{}_a$
	cm	cm	cm	_	_	—	—	—
Aberdeen	3.7	3.5	3.5	1.06	1.00	0.98	0.75	0.94
Lowestoft	3.3	3.3	3.2	1.03	1.03	0.93	0.88	0.91
Brest	3.8	3.8	3.7	1.03	1.03	0.97	0.97	0.98
Roscoff	3.5	3.7	3.5	1.00	0.95	0.96	0.98	0.99
Dunkerque	2.4	2.6	2.4	1.00	1.08	0.91	0.91	0.94
Harlingen	1.5	1.5	1.3	1.15	1.15	0.54	0.60	0.60
Huibertgat	_	2.0	1.6	_	1.25	0.49	0.67	0.60
Alte Weser	1.5	1.7	1.4	1.07	0.82	0.75	0.59	0.82
Büsum	1.7	2.0	1.7	1.00	1.18	0.54	0.56	0.64

Results from Table 2 show, that the seasonal dependence of M_2 's nodal modulation 306 is always lower than $\pm 0.4 \ cm$. The $M_{2n,s}$ and the $M_{2n,w}$ to $M_{2n,a}$ ratios deviate more 307 from 1 with a low R^2 (≤ 0.75). The nodal satellite for M_2 at robust estimations, such 308 as Aberdeen, Brest, Dunkerque or Roscoff, shows seasonal variation of less than 6 %, while 309 weaker R^2 , i.e. Harlingen, Huibertgat or Büsum produce an over- or underestimation 310 in summer or winter by a maximum of 25 % of \mathbb{R}^2 . As seasonal variation in M_{2n} 's amplitude 311 shows small variation, no bias due to seasonally heterogeneously sampled data is to be 312 expected, when applying Equation 1. The analysis also shows, that R^2 is usually larger, 313 after the analysis has been performed for an entire year. It is not surprising that we find 314 the approximation of true tidal constituents to become more robust on a longer time timescale 315 as this has already been stated by Pugh (1987). 316

3.3 Nodal Modulation at Gauges

317

After the nodal signal has been extracted successfully through multiple, non-linear regression fitting, its amplitude modulation f and phase lag u can be calculated from the regression parameters. If R^2 is ≤ 0.5 , results have been regarded as statistically insignificant and will not be included in the subsequent analysis. Differences of the calculated modulation from the theoretical f-u correction factors (i.e. Table 1) are given in Figure 6. Positive values represent an overestimation of the theoretical nodal correction factors f and u. For all constituents, the fitted nodal modulation and phase lag agree well with equilibrium



Figure 6: Differences between the fitted amplitude modulation in % (left y-axis, black) and phase lag in ° (right y-axis, gray) and the equilibrium nodal correction parameters (i.e. Table 1) for the constituents M_2 , S_2 , N_2 , O_1 , K_1 and K_2 . Data points with an insufficient R^2 are marked with a red dot.

The amplitude modulation of O_1 is overestimated most in Vlieland Haven (1.9 %) and Huibertgat (1.9 %) in the Dutch Wadden Sea. The following stations show differences ranging from 0.7 % (Eemshaven) towards an underestimation of -1.6 % at Alte Weser in the German Wadden Sea. K_1 's amplitude modulation is underestimated throughout all locations except for Cherbourg and Dover. At the east coast of the UK it is underestimated by -2.5 % in Aberdeen to -1.5 % in North Shields. The westerly stations Newlyn, Brest

and Roscoff underestimate K_1 by less than -0.7 %, while the maximum underestimation 333 is reached in Westkapelle (-2.8 %), Ijmuiden (-3.1 %) and West Terschelling (-3.4 %). 334 Though N_2 must be modulated by the nodal tide due to the laws of astronomy, its variation 335 could only be detected until Cherbourg in the southern English Channel and at the UK 336 east coast. Successfully fitted N_2 amplitude variation is underestimated slightly on the 337 English east coast from Aberdeen (-0.1 %) to Immingham (-1.1 %). Gauges in the southern 338 English Channel underestimate N_2 's amplitude modulation by less by -0.4 % in Newlyn 339 until -1.8 % in Dunkerque. The nodal component of the semidiurnal M_2 is underestimated 340 consistently after the Dover-Calais narrowing in the English Channel. In Westkapelle, 341 the M_2 modulation starts to be underestimated by -1.4 % and -0.7% in Dover. When 342 moving further northeastwards the nodal amplitude modulation of M_2 diminishes into 343 statistical insignificance until reaching the Dutch Wadden Sea. In Vlieland Haven, M_2 344 modulation is reduced by -2.6 %, although within the Wadden Sea itself, M_2 modulation 345 is mostly reduced by -2.0 % (Vlieland Haven to Wyk). Harlingen, West-Terschelling and 346 Cuxhaven did not meet the criterion for statistical significance. S_2 shows a similar behavior, 347 as its amplitude is modulated between Dover (2.0 %) and Esbjerg (2.0 %), peaking near 348 the S_2 amphidrome at Ijmuiden (6.2 %). In the Wadden Sea, S_2 is modulated consistently 349 between Vlieland Haven (4.1 %) and Büsum (3.5 %). Contrarily, the nodal amplitude 350 variation of K_2 is overestimated after the Dover-Calais narrowing by 1.1 % in Dover and 351 2.8 % in Westkapelle. The K_2 amplitude variation remains exaggerated by 4.8 % in Hoek 352 van Holland, 1.9 % in Vlieland Haven, 2.4 % in Huibertgat, 4.4 % in Alte Weser and 2.6 % 353 in Büsum within the Wadden Sea before reaching a smaller overestimation in Esbjerg 354 of 0.9 %. Although, the phase lags of all constituents do not deviate more than ± 2.0 ° at 355 any location, they show consistent variance from their equilibrium modulation value u356 with an overestimation between 0.5 to 2.0 ° of O_1 , K_1 , S_2 and M_2 for all gauges from 357 Dunkerque to Büsum. 358

3.4 The Impact of Shallow Water Constituents

359

When tides travel from the open sea towards coastal waters, embayments or estuaries, 360 energy dissipation through friction leads to the generation of new tidal constituents, which 361 are called shallow water tides. They are related to larger parent constituents, which are 362 astronomically predefined, e.g. M_2 or S_2 . In other words, the generation of shallow water 363 tides drains energy from parent constituents, which underlie the nodal tide modulation. 364 Hence, it is not prudent to imply a connection between bottom friction on nodal modulation, 365 especially because this has already been suspected in Feng et al. (2015) and Godin (1986). 366 However, the quantity and amplitude of shallow water tides vary regionally, which is why 367 the shallow water tide hypothesis above may not hold true for all coastal waters equally. 368 As the underestimation of f for K_2 and O_1 in section 3.3 coincides with an overestimation 369 of the nodal amplitude modulation of M_2 , N_2 and S_2 , we suspect interactions between 370 the parent constituents through their shallow water tides to be the dominant driver for 371 these deviations from the equilibrium tide in the North Sea. 372

To support the shallow water tide hypothesis, a harmonic analysis at representative 373 gauges near the British east coast and in the Wadden Sea was carried out for M_2 and 374 S_2 's shallow water constituents. In Büsum (Wadden Sea), for example, 10 shallow water 375 components with an amplitude larger than 3 cm were present in 2012 of which MSf, 376 $M_4, M_6, MU_2, MS_4, NU_2, 2MS_6$ and MN_4 are related to a lunar origin. If the constituents, 377 which are either solar or lunar influenced and the meteorological tide MSf are ruled out, 378 MS_4 and $2MS_6$ remain. Multiple, non-linear regression fitting (Equation 1) of MS_4 and 379 $2MS_6$ has shown that, a clear nodal signal could not be extracted from these components 380 at any of the locations presented in 3. However, significant amplitude differences of MS_4 381 and $2MS_6$ between the gauges do exist. If the M_2 to MS_4 or the M_2 to $2MS_6$ amplitude 382 ratios, respectively, are calculated, large values coincide with S_2 modulation as demonstrated 383 in Table 3. 384

Table 3: Ratios of significant shallow water components, which are created from S_2 and M_2 for representative gauges in the deeper North Sea (Brest, Lerwick, North Shields), the English Channel (Lowestoft) and the Wadden Sea (Vlieland Haven, Delfzijl, Büsum). $R^2 \geq 0.50$ indicates a successful fitting of nodal variation for S_2 .

	$rac{M_2}{MS_4}$ in -	$rac{M_2}{2MS_6}$ in -	R^2 for S_2
Brest	0.016	0.008	0.010
Lerwick	0.021	0.021	0.171
North Shields	0.012	0.005	0.093
Lowestoft	0.061	0.061	0.771
Vlieland Haven	0.039	0.061	0.830
Delfzijl	0.090	0.050	0.606
Büsum	0.040	0.015	0.604

While the ratios do not exceed 0.021 in Brest, Lerwick, North Shields at the UK east coast, larger ratios are observed in Lowestoft (0.061), Vlieland Haven (0.061), Delfzijl (0.09) or Büsum (0.04). These larger ratios coincide with significant index of agreement values of $R^2 > 0.5$, showing a relationship between the modulation of S_2 and large shallow water tide amplitudes. An analog analysis for K_2 has shown additionally, that the overestimation of K_2 (see also Figure 6) coincides with large K_2 to either MK_4 , $2MK_6$ or MKS_2 ratios.

3.5 Spatial Nodal Modulation

The amplitude modulation f and phase lag u has been shown to differ significantly 392 from expected equilibrium conditions in measured tide records (i.e. Figure 6). Furthermore, 393 the fitted nodal modulation shows regional tendencies, for example when the modulation 394 of the M_2 in the Dutch side of the English Channel is reviewed. The nodal modulation 395 corresponds to equilibrium values in Cherbourg, is overestimated near the Dover-Calais 396 narrowing at Dunkerque / Dover, before diminishing into statistical insignificance in Westkapelle 397 to Ijmuiden. Another example is the nodal amplitude variation of N_2 , which has not produced 398 any results between Westkapelle and Wyk due to statistical insignificance. 399

Therefore, we computed a complete spatial distribution of the amplitude and phase 400 correction parameters for the North Sea with the numerical model from Section 2.4 in 401 order to quantify the regional variation. As a consequence of the long time scale of 18.61 402 years a simulation would require a time period of roughly 19 years. For this reason, the 403 model has only been applied for 10 months with the diurnal amplitude modulation and 404 phase lag minima and maxima reached 5 months into the computation, as other solutions 405 would be computationally expensive. The diurnal phase lag minimum is in October 2001, its maximum in February 2011, while the diurnal amplitude modulation minimum is in 407 June 2006 and its maximum in October 2015, respectively (Pugh, 1987). The model is 408 forced astronomically at the open boundaries by f-u corrected, reanalyzed tidal constituents 409 from the FES 2014b (Section 2.4). Meteorology has been deactivated and the bathymetry 410 is not altered between each simulation. Model results have been interpolated from the 411 unstructured computational grid on a regular 7.5 km grid before the harmonic analysis 412 UTide without nodal correction has been applied. The spatial nodal modulation is then 413 calculated through the absolute amplitude difference between 2006 and 2015, divided by 414 their mean, and the phase lag is calculated by subtracting 2001 from 2011. The resulting 415 values must be halved, as an amplitude is only half of the sinusoidal range. 416

417

391

3.5.1 Computed Nodal Modulation at Gauges

Before determining the spatial distribution of amplitude modulation f and phase lag u, the model results are compared to the analysis results from tide records in Section 3.3. The index of agreement (R^2) is applied for the observed and modeled (predicted) nodal satellite variation. To quantify the quality of the computed nodal variation, a mean absolute error (MAE) and a root mean square error (RMSE) are given in Table 4. The actual model validation is referred to in Section 2.4.

	Parameter	O_1	K_1	N_2	M_2	S_2	K_2
	MAE	1.8	4.0	0.5	0.5	1.5	1.2
f	RMSE	2.1	4.1	0.8	0.7	1.7	1.5
	R^2	0.12	0.00	0.55	0.79	0.76	0.53
	MAE	0.7	0.8	0.5	0.5	0.7	0.6
u	RMSE	0.9	0.9	0.7	0.6	0.8	0.8
	R^2	0.00	0.00	0.04	0.05	0.03	0.14

Table 4: Validation parameters for modeled and observed nodal satellite variation correction parameters f and u. MAE and RMSE are displayed in % and °, respectively, and R^2 dimensionless.

The validation of the computed amplitude modulation shows $R^2 > 0.5$ for the semidiurnal 424 constituents N_2 , M_2 , S_2 and K_2 , proving a linear dependency between observed and computed 425 nodal modulation. The semidiurnal MAEs range between 0.5 and 1.5 % and the RMSEs 426 between 0.7 to 1.5 %, respectively. The differences result from a weaker model response 427 to amplitude modulation, especially for K_2 and S_2 , though the prediction of over- or underestimation, 428 of nodal modulation remains correct. The amplitude modulation of diurnal components 429 K_1 and O_1 , however demonstrates lower agreement to the predicted counterpart. The 430 model produces an overestimation of K_1 by an MAE of 1.8 % for O_1 and 4.0 % for K_1 . 431 The larger error residuals result from an overestimation of nodal amplitude variation in 432 the model. For K_1 especially, the model calculates an overestimation of the amplitude 433 modulation, while observations have shown an underestimation from the equilibrium value. 434 This holds true for O_1 as well, though prediction and observation display an overestimation 435 of O_1 s amplitude modulation with weak R^2 of 0.12. For the nodal phase lag, R^2 ranges 436 between 0 for O_1 and 0.14 for K_2 , which results from the models inability to reproduce 437 a nodal phase variation, which differs from the equilibrium tide. Opposing to the fitting 438 results from measurements, the model computes phase lags, which correlate with the equilibrium 439 value for all constituents. This results in low R^2 for the phase lag as can be seen in Table 440 4. 441

442

3.5.2 Modeled Nodal Variation

The amplitude of a nodal constituent (left), its nodal amplitude modulation (middle) and its phase lag (right), as computed in the numerical model are shown in Figure 7. We will focus on the nodal modulation of M_2 , N_2 , K_2 and O_1 subsequently, as these constituents have shown strong regional tendencies. In the following, the index n denotes the nodal satellite of a constituent.

The largest nodal amplitude is observed for M_{2n} with more than 15 cm in the southern 448 English Channel. The amplitude in the Wadden Sea ranges between 2 and $4 \ cm$, while 449 the Dutch west coast and the Danish north coast show amplitudes of $\leq 1 \ cm$. M_2 's nodal 450 amplitude modulation corresponds with the equilibrium value in the southern English 451 Channel and the UK east coast (3.7%). It is underestimated on the Dutch side of the 452 English Channel (1.5 to 2.0 %) and the eastern German Wadden Sea (2.0 to 3.0 %). The 453 phase lag u of M_2 shows low deviations between -2.1 to -2.4° in the southern North 454 Sea. The amplitude distribution of N_{2n} is similar to M_{2n} and K_{2n} , though the amplitude 455 of N_{2n} is significantly lower with a maximum of 4cm in the southern English Channel 456 and 0.5 to 1.2 cm in the Wadden Sea. N_{2n} 's amplitude is below 0.5 cm on the western 457 Dutch coast, Northern Frisia in Germany and the Danish North Sea coast, indicating, 458 why nodal amplitude modulation could not be derived from tide records at these locations. 459 The deviation from the theoretical phase lag u tends to be underestimated between 1.1 460 and 2.5 ° for N_2 . The amplitude distribution and magnitude of K_{2n} is again similar to 461 M_{2n} , with maximum amplitudes of 15 cm in the southern English Channel. K_2 's amplitude 462 modulation is overestimated by 1.5~% in the English Channel and the Dutch Wadden 463 Sea and by 3 % near the Dutch west coast. UK's east coast and the southern English 464 Channel remain unaffected as seen previously for M_{2n} and N_{2n} . The phase lag of K_{2n} 465 deviates less than 1.5 ° from its correction value u almost in the entire study area. O_{1n} 466 has its maximum amplitude in the UK Moray Firth and Thames estuary at $3.8\ cm$ and 467 its amplitude is $\leq 1 \ cm$ at the Norwegian coast, the Danish northwest coast and the 468 southern English Channel. The equilibrium tide nodal modulation is well represented 469 near the model boundaries (≤ 0.5 %), before the model reveals an amplification of O_1 470 amplitude modulation at the English east coast (1.0%), the eastern English channel (1.5%), 471 the Dutch west coast the Wadden Sea (2.5 %). The nodal phase lag u for O_{1n} shows small 472 regional deviation with maximum differences in the English Channel near its amphidromy 473 and in the Dutch and German Wadden Sea $(1.0 \circ)$. 474



Figure 7: Spatial distribution of the nodal amplitude in cm (left), the nodal modulation f in % (middle) and the nodal phase lag u in ° (right) for the tidal constituents M_2 , N_2 , K_2 and O_1 as computed by the numerical model. The theoretical nodal modulation and phase lag values from the equilibrium tide theory are placed in the center of the colorbar for the f (middle) and u (right) plots, with a range of ± 3 % and ± 2 °, respectively.

475 4 Discussion

This study has shown, based on measured tide records, that the nodal correction 476 parameters f (amplitude) and u (phase) for lunar tidal constituents in harmonic analysis 477 do not always follow the equilibrium tide theory, opposing to the statements in Trupin 478 and Wahr (1990). This analysis corroborates previous results, whom discussed the nodal 479 correction parameters based on the equilibrium tide assumption (e.g. Cherniawsky et 480 al. (2010); Feng et al. (2015); Godin (1986); Shaw and Tsimplis (2010) to name only a 481 few) and extends the current analysis methods for nodal tide estimation by introducing 482 483 a multiple, non-linear fitting approach for tidal constituents. Unlike the commonly applied quantile method (Woodworth & Blackman, 2004), the application of multiple, non-linear 484 regression to annually calculated, tidal constituents accounts for the accelerated change 485 in semidiurnal tides (Baart et al., 2012; Müller, 2011) and is applicable for tide records 486 with a duration of more than 19 years in the North Sea. 487

In contrast to previous research (Godin, 1986; Shaw & Tsimplis, 2010), the nodal 488 modulation of constituents does not follow the equilibrium tide theory strictly, as O_1 and 489 K_2 are underestimated in the English Channel and the Wadden Sea (see Figure 6). M_2 's 490 nodal modulation agrees well with previous findings (Feng et al., 2015; Ku et al., 1985; 491 Woodworth et al., 1991), as it is reduced in the friction dominated areas of the study 492 site such as the Dutch east coast and the Wadden Sea. Nevertheless, the fitting of N_2 493 in the same areas remained inconclusive, which was associated with the friction induced 494 generation of shallow water tides and third order disturbances (Godin, 1986). The amplitude 495 modulation of the constituent K_1 differs from the other semidiurnal results, as nodal modulation 496 is already reduced in the Northern Atlantic (i.e. Lerwick, Newly, Brest in Figure 6), though 497 its amplitude modulation is consistently reduced at the Dutch east coast and the Wadden Sea. These findings disagree with Godin (1986), who stated that the nodal correction 499 of K_1, K_2 and O_1 is appropriate in any case. Moreover, the agreement found in the Mediterranean 500 Seas (Shaw & Tsimplis, 2010) can only be observed outside the English Channel and the 501 Wadden Sea. However, the interpretation of the results of this study must consider, that 502 the amplitude of the nodal satellites is often smaller than 5 cm in the North Sea. Therefore, 503 small error margins resulting e.g. from the 95 % confidence interval in harmonic analysis 504 may lead to under- or overestimation when reviewing small amplitudes. The amplitude 505 of $K_{1,n}$ for example rarely exceeds 1 cm in the entire study area. The underestimation 506 of K_2 and O_1 coincided with an overestimation of M_2 , N_2 and a nodal modulation of 507 the solar constituent S_2 . For this reason, we suspect interactions within these constituents 508 and their shallow water tides must be responsible. Furthermore, as an overestimated nodal 509 amplitude modulation for K_2 has not yet been documented in literature, other non-linear 510 effects such as diffraction, reflection or refraction may be present. The deviation from 511 the equilibrium for the nodal phase lag from tide records was be considered negligible 512 for all constituents, as the difference rarely exceeds 2.5 $^{\circ}$, which would correspond to approximately 513 5 minutes for the M_2 . 514

In order to fortify the hypothesis, that shallow water effects cause the deviation 515 from the equilibrium tide, a spatial distribution of nodal amplitude modulation f and 516 phase lag u was determined by numerical modeling to distinctively identify affected regions 517 as suggested by Woodworth (2012). The modeling approach has shown considerable skill 518 for the amplitude modulation of semidiurnal constituents, but is less suitable concerning 519 the diurnal components K_1 and O_1 and the nodal phase lag of all constituents. We find 520 certain limitations to arise from the accuracy of the numerical model itself, which has 521 been validated to an order of centimeters and minutes (Bundesanstalt für Wasserbau et 522 al., 2019b) and the harmonic analyses timespan, which differs marginally by 2 months 523 between the model and the tide records. The poor agreement concerning the phase lag 524 525 agreement could be related to the natural bathymetry changes in the North Sea between the years 2001 to 2015, but these are not included in the model. The link between tidal 526 constituents and bathymetry changes in the Wadden Sea is well established (Jacob et 527 al., 2016; Rasquin et al., 2020), which would suggest, that the deviation of the nodal phase 528 lag in tide records originates from morphodynamic changes. 529

Still, the question arises, why the diurnal constituent representation did not achieve 530 the same quality as the semidiurnals in the numerical model. Nevertheless, the model 531 results have revealed regionally deviating amplitude modulation in areas with strong friction 532 such as the English Channel or the Wadden Sea. Since meteorological and thus seasonal 533 influences were neglected in the modeling approach, friction remains as the only major 534 possible cause for shifts in nodal modulation. Friction is induced by the shallow water 535 of the continental shelf and complex basin geometry, which becomes increasingly relevant 536 in the English Channel and in the Wadden Sea. Therefore, we conclude, similar to Feng 537 et al. (2015) a friction induced generation of shallow water tides in the inner North Sea, 538 which leads to a reduced amplitude modulation of M_2 and N_2 . However, the amplitude 539 modulation of K_2 , S_2 and O_1 is also affected, which partially disagrees with the results 540 from the Chinese Seas (Feng et al., 2015), as K_{2s} modulation is significantly underestimated 541 while O_1 is overestimated in the North Sea. Since K_{2s} and O_{1s} deviation coincide with 542 the underestimation of M_2 and N_2 , we again suspect the energy transfer towards shallow 543 water constituents to be responsible. The shallow water tide hypothesis shows most obvious 544 in the modulation of the solar constituent S_2 , which should not be affected by the nodal 545 tide whatsoever. In fact, every time the modulation of M_2 was reduced, the variation 546 of K_2 and S_2 became enhanced. We have shown, that the modulation of S_2 links to high 547 amplitudes of the shallow water tides MS_4 and $2MS_6$ (i.e. Table 3), which for MS_4 has 548 also been shown in the Chinese Seas (Feng et al., 2015). An analog harmonic analysis 549 for the parent constituent K_2 has shown a similar relationship to its shallow water components 550 MK_4 , $2MK_6$ or MKS_2 . Even though the relationship between shallow water tides and 551 the deviation of the nodal amplitude modulation has been proven in this study, more 552 work is required in order to quantify the influence of shallow water tides on the nodal 553 tide, specifically. Other non-linear effects, such as shoaling, reflection, refraction or diffraction 554 may also disrupt the nodal modulation, especially in the English Channel. 555

556 5 Summary and conclusion

In sea level science, an accurate estimation of low frequency tides, such as the lunar 557 18.61 year nodal tidal cycle is crucial, as the nodal amplitude can be up to 30 cm (Peng 558 et al., 2019). Even though different methods, such as the quantile method (Woodworth 559 & Blackman, 2004), have been used to quantify a nodal amplitude and phase lag from 560 tide records, an accurate approximation is not yet consistently applicable at any geographical 561 location. Nodal modulation is defined as the correction of lunar tidal constituents from 562 harmonic tide analysis through the f (amplitude) and u (phase) correction parameters, 563 which are derived from the equilibrium tide theory (Pugh, 1987). Past studies have shown these correction parameters to be accurate (Godin, 1986; Shaw & Tsimplis, 2010; Trupin 565 & Wahr, 1990), overestimated (Feng et al., 2015) or underestimated (Cherniawsky et al., 566 2010) depending on the geographical location and analysis method. For this reason, the 567 correction parameters are calculated and compared to the equilibrium approach at various 568 tide records in the North Sea and North Atlantic region to find an approach, which accurately 569 extracts the nodal tide from gauge records. Furthermore, a numerical model is deployed 570 at the diurnal minimum and maximum of nodal amplitude modulation and phase lag 571 to provide spatial information in between the gauge network at the North Sea. The overall 572 aim is to develop and validate a method to extract the nodal signal from tide records 573 and to supply large-scale information on the nodal modulation in shelf seas, such as the 574 North Sea, as sea level sciences rely on accurate assumptions of the nodal cycle. 575

A multiple, non-linear regression analysis of annual tidal constituents at North Sea 576 gauges was chosen to approximate nodal amplitude and phase modulation. The results 577 have shown, that the amplitude correction parameter f is significantly overestimated for 578 M_2 , N_2 and underestimated for K_1 , K_2 , O_1 in shallow, friction dominated parts of the 579 North Sea, although the calculated phase lag coincides well with deviations of less than 580 2.0 °. Additionally, the solar constituent S_2 was shown to be modulated regionally in 581 the Northern English Channel and the Wadden Sea. We support the hypothesis from 582 literature (Feng et al., 2015; Pugh, 1987), whom state that energy transfer from M_2 and 583 S_2 towards shallow water tides such as MS_4 or $2MS_6$ leads to S_2 's modulation. Shallow 584 water effects also influence other diurnal and semidiurnal constituents such as O_1, K_1 , 585 K_2 or N_2 , though more research is needed on this subject. We could not identify the dominant 586 process behind the underestimation of amplitude modulation f for O_1 and K_2 , as well 587 as the overall overestimation of K_1 as similar effects have not yet been documented in 588 literature. A link between K_2 and the shallow water constituents MK_4 , $2MK_6$ or MKS_2 , 589 however, was established. A larger scale could provide more insight about the processes 590 at play, though we suspect shallow water dynamics to be responsible for the overestimation 591 of O_1 or K_2 . 592

The numerical modeling studies have confirmed, that friction affected areas, such 593 as the English Channel or the Wadden Sea, reduce the nodal amplitude modulation of M_2 , while the variation of O_1 , S_2 and K_2 is enhanced. The distribution of f is hereby 595 inhomogeneous, as regional and local differences are present due to the variety of generated 596 shallow water tides. An analysis of shallow water constituents of the tide record at Büsum, 597 for example, has revealed a larger M_2 to MS_4 or $2MS_6$ ratio when the modulation of 598 S_2 became significant. Thus, we concluded that the current f-u correction should only 599 be applied, whenever the influence of shallow water tides is negligible, as they influence 600 the nodal modulation of lunar constituents and S_2 . The application of u can hereby be 601 regarded reasonable due to low deviations of less than ± 2.5 °. It must be noted that these 602 recommendations do depend on the field of application and the user-desired degree of 603 accuracy. 604

Despite the wide acceptance of the f - u nodal correction methodology, it may significantly deviate from the equilibrium in friction affected areas. Additionally, the fu correction does not consider the modulation of S_2 . Therefore, the f-u correction parameters must be determined appropriately and if necessary, corrected. This process is simplified with the non-linear, multiple regression of tidal constituents presented in this study, which enables the calculation of accurate f and u correction values. Future work is recommended

towards the extension of these regional results to a global scale. This can be performed 611 numerically by global modeling scenarios or analytically by non-linear, multiple regression 612 analysis of satellite altimetry data. The resulting product would be a globally varying 613 data set providing appropriate f and u correction factors. A correction layer, which includes 614 non-lunar, yet modulated constituents such as S_2 , could stand behalf of the general correction 615 formulation for a more accurate, spatially varying nodal modulation correction. Future 616 work is also recommended towards quantifying the effect of shallow water tides on the 617 nodal satellite variation, especially as many gauges are located in complex coastal or estuarine 618 environments in practice. This would aid sea level science, as the correction of tide records 619 for nodal modulation would be more accurate and help to understand yet unexplained 620

621 phenomena.

622 Acknowledgments

We thank the German Federal Ministry of Transport (BMVI) for funding the mFUND project EasyGSH-DB (funding no. 19F2004A), which has made this research possible.

Also, we would like to thank the suppliers of tide records from Germany (German Waterways

and Shipping Administration (WSV) in cooperation with the German Federal Institute

of Hydrology (BfG), France (Shom), the UK (BODC) and the Netherlands (Rijkwaterstaat).

- Tide records can be retrieved from https://data.shom.fr/, https://www.bodc.ac.uk/ data/ and https://waterinfo.rws.nl/.
- RH would also like to thank his friend Dirk Hagemann personally for in depth discussions about advanced signal processing and analysis.

632 References

- 633Amin, M. (1985). Temporal variations of tides on the west coast of great britain.634Geophysical Journal International, 82(2), 279–299. doi: \url{10.1111/j.1365}635-246X.1985.tb05138.x}
- Amin, M. (1993). Changing mean sea level and tidal constants on the west coast
 of australia. Marine and Freshwater Research, 44(6), 911. doi: \url{10.1071/
 MF9930911}
- Baart, F., van Gelder, P. H. A. J. M., de Ronde, J., van Koningsveld, M., &
 Wouters, B. (2012). The effect of the 18.6-year lunar nodal cycle on regional
 sea-level rise estimates. *Journal of Coastal Research*, 280, 511–516. doi:
 \url{10.2112/JCOASTRES-D-11-00169.1}
- Bradley, J. (1728). An account of a new discovered motion of the fixed stars.
 Philosophical Transactions of the Royal Society of London, 35(406), 637–661.
 doi: \url{10.1098/rstl.1727.0064}
- Bundesanstalt für Wasserbau, Hagen, R., Freund, J., Plüß, A., & Ihde, R. (2019a). Jahreskennblatt easygsh-db 2015. kurzfassung der validierung: Untrim2
- 648- sedimorph unk.Bundesanstalt für Wasserbau.doi: \url{10.18451/649k2{\textunderscore}easygsh{\textunderscore}jkbl{\textunderscore}2015}
- Bundesanstalt für Wasserbau, Hagen, R., Freund, J., Plüß, A., & Ihde, R. (2019b).
 Validierungsdokument easygsh-db nordseemodell. teil: Untrim2 sedimorph –
 unk. Bundesanstalt für Wasserbau. doi: \url{10.18451/k2{\textunderscore}}
 easygsh{\textunderscore}1}
- Casulli, V. (2009). A high-resolution wetting and drying algorithm for free-surface
 hydrodynamics. International Journal for Numerical Methods in Fluids, 60(4),
 391–408. doi: \url{10.1002/fld.1896}
- Casulli, V., & Walters, R. A. (2000). An unstructured grid, three-dimensional model based on the shallow water equations. International Journal for Numerical Methods in Fluids, 32(3), 331–348. doi: \url{10.1002/(SICI)1097} -0363(20000215)32:3{\textless}331::AID-FLD941{\textgreater}3.0.CO;2-C}
- Cherniawsky, J. Y., Foreman, M. G., Kuh Kang, S., Scharroo, R., & Eert, A. J.
 (2010). 18.6-year lunar nodal tides from altimeter data. Continental Shelf
 Research, 30(6), 575–587. doi: \url{10.1016/j.csr.2009.10.002}
- Codiga, D. L. (2011). Unified tidal analysis and prediction using the utide matlab functions. Graduate School of Oceanography, University of Rhode Island. doi: \url{10.13140/RG.2.1.3761.2008}
- Doodson, A. T. (1921). The harmonic development of the tide-generating potential.
 Proceedings of the Royal Society A: Mathematical, Physical and Engineering
 Sciences, 100(704), 305–329. doi: \url{10.1098/rspa.1921.0088}
- Doodson, A. T. (1928). The analysis of tidal observations. Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences, 227(647-658), 223-279. doi: \url{10.1098/rsta.1928.0006}
- 673
 EMODnet Bathymetry Consortium. (2016). Emodnet digital bathymetry (dtm 2016).

 674
 Author. doi: \url{10.12770/c7b53704-999d-4721-b1a3-04ec60c87238}
- Feng, X., Tsimplis, M. N., & Woodworth, P. L. (2015). Nodal variations and longterm changes in the main tides on the coasts of china. *Journal of Geophysical Research: Oceans*, 120(2), 1215–1232. doi: \url{10.1002/2014JC010312}
- 678Foreman, M. G. G., Cherniawsky, J. Y., & Ballantyne, V. A.
harmonic tidal analysis: Improvements and applications.(2009).Versatile679harmonic tidal analysis: Improvements and applications.
Atmospheric and Oceanic Technology, 26(4), 806–817.Journal of
doi: \url{10.1175/
6816802008JTECHO615.1}
- Godin, G. (1972). The analysis of tides. *Liverpool University Press*, 264 pp.
- Godin, G. (1986). The use of nodal corrections in the calculation of harmonic constants. *International Hydrographic Review*(63 (2)).
- Gräwe, U., Burchard, H., Müller, M., & Schuttelaars, H. M. (2014). Seasonal
 variability in m 2 and m 4 tidal constituents and its implications for the

 5563-5570. doi: \url{10.1002/2014GL060517} Haigh, I. D., Eliot, M., & Pattiaratchi, C. (2011). Global influences of the 18.61 year nodal cycle and 8.85 year cycle of lumar perigee on high tidal levels. Journal of Geophysical Research, 116(C6), 25249. doi: \url{10.1029/2010JC006645} Haigh, I. D., Pickering, M. D., Green, J. M., Arbic, B. K., Arns, A., Dangendorf, S., Woodworth, P. L. (2019). The tides they are a-changin': A comprehensive review of past and future non-astronomical changes in tides, their driving mechanisms and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG00636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sca-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remoter response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–600. doi: \url{10.1007/s10236-016-049-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s1237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1929). Analyse der wasserstandsentwicklung in der deutschen bucht: Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Schönfeld, W. (1988). Untersuchungen zur wasserstandsentwicklung in der de
 Haigh, I. D., Eliot, M., & Pattiaratchi, C. (2011). Global influences of the 18.61 year nodal cycle and 8.85 year cycle of lunar perigee on high tidal levels. Journal of Geophysical Research, 116(C6), 25249. doi: \url{10.1029/2010JC00645} Haigh, I. D., Pickering, M. D., Green, J. M., Arbic, B. K., Arns, A., Dangendorf, S., Woodworth, P. L. (2019). The tides they are a changin' A comprehensive review of past and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sca-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: 10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.1212/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Occan Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum Rfdi-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(
 nodal cycle and 8.85 year cycle of hunar perigee on high tidal levels. Journal of Geophysical Research, 116(C6), 25249. doi: 10.1029/2010JC006645 Haigh, I. D., Pickering, M. D., Green, J. M., Arbic, B. K., Arns, A., Dangendorf, S., Woodworth, P. L. (2019). The tides they are a-changin': A comprehensive review of past and future non-astronomical changes in tides, their driving mechanisms and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sca-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (castern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: 10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum klki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Vischer, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135–161. Ret
 Geophysical Research, 116(C6), 25249. doi: \url{10.1029/2010JC006645} Haigh, I. D., Pickering, M. D., Green, J. M., Arbic, B. K., Arns, A., Dangendorf, S., Woodworth, P. L. (2019). The tides they are a-changin': A comprehensive review of past and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved fron https:
 Haigh, I. D., Pickering, M. D., Green, J. M., Arbic, B. K., Arns, A., Dangendorf, S., Woodworth, P. L. (2019). The tides they are a c-changin': A comprehensive review of past and future non-astronomical changes in tides, their driving mechanisms and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: 10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135-161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation
 S Woodworth, P. L. (2019). The tides they are a-changin': A comprehensive review of past and future non-astronomical changes in tides, their driving mechanisms and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: L along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 1145–433. doi: \url{10.1007/s1237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(47
 comprehensive review of past and future non-astronomical changes in tides, their driving mechanisms and future implications. Reviews of Geophysics. doi: \url{10.1029/2018RG00636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: 10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: L along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: 10.1126/ science.230.4721.68}
 their driving mechanisms and future implications. Reviews of Geophysics. doi: \\un1225/121222018RG000636 Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041-1056. doi: \\un1225/12222000000000000000000000000000000
 \url{10.1029/2018RG000636} Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefnederfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiu
 Hansen, J. M., Aagaard, T., & Kuijpers, A. (2015). Sea-level forcing by synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht: Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101341} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997}
 synchronization of 56- and 74-year oscillations with the moon's nodal tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: L along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} <l< td=""></l<>
 tide on the northwest european shelf (eastern north sea to central baltic sea). Journal of Coastal Research, 315, 1041–1056. doi: \url{10.2112/JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: L along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since upper level accomplexee data set. Journal of Geophysi
 sea). Journal of Coastal Research, 315, 1041–1056. doi: 10.2112/ JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the hunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 JCOASTRES-D-14-00204.1} Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801-807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671-690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135-161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.129/2009JC005997}
 Houston, J. R., & Dean, R. G. (2011). Accounting for the nodal tide to improve estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 1160 (2011). Rapid change in semi-durant tides in the north atlantic since data of the lunar semidiurnal tides in the north atlantic since data of the lunar semidiurnal tides in the north atlantic since data of the lunar semidiurnal tides in the north atlantic since data of the lunar semidiurnal tides in the north atlantic since data of the lunar semid-lunal tides in the n
 estimates of sea level acceleration. Journal of Coastal Research, 276, 801–807. doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https:// hall.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 doi: \url{10.2112/JCOASTRES-D-11-00045.1} Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671-690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135-161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 Jacob, B., Stanev, E. V., & Zhang, Y. J. (2016). Local and remote response of the north sea dynamics to morphodynamic changes in the wadden sea. Ocean Dynamics, 66(5), 671–690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415–433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 below, D., Verner, D. (2010), (2010). Lotentar intermet intermeting intermet intermet intermet interme
 Dynamics, 66(5), 671-690. doi: \url{10.1007/s10236-016-0949-8} Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from \url{https://hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135-161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC00597} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since (2000).
 Jay, D. A., Leffler, K., Diefenderfer, H. L., & Borde, A. B. (2015). Tidal-fluvial and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Die Küste(47), 135-161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 1090. (Deutscient P. 2005)
 and estuarine processes in the lower columbia river: I. along-channel water level variations, pacific ocean to bonneville dam. Estuaries and Coasts, 38(2), 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from \url{https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135-161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: \url{10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 10900 Combusing P. L. U. V. (1000)
 level variatine protocol in the order order of the level variation (location protocol) in the order of the level variation (location) (location)
 415-433. doi: \url{10.1007/s12237-014-9819-0} Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211-275. Retrieved 01.08.2019, from \url{https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135-161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: \url{10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 1090 Corebusid P. M. K. (1991). (no.1020/2009JC005997)
 Jensen, J., Mügge, H. E., & Schönfeld, W. (1992). Analyse der wasserstandsentwicklung und tidedynamik in der deutschen bucht: Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 1000. Combined R.
 ¹¹¹¹¹²¹¹³¹¹⁴¹¹⁴¹¹⁴¹¹⁴¹¹⁴¹¹⁴¹¹⁴
 Abschlussbericht zum kfki-projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(53), 211–275. Retrieved 01.08.2019, from \url{https:// hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 ¹¹¹ buchtabberlate bar min projects. Retrieved 01.08.2019, from https:// hdl.handle.net/20.500.11970/101341} ¹¹⁷ Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} ¹²⁰ Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: 10.1126/ science.230.4721.69} ¹²⁶ Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} ¹²⁹ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 0.000 for the semi-diarene in the semi-diarene i
 hdl.handle.net/20.500.11970/101341} Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 Jensen, J., Mügge, H. E., & Visscher, G. (1988). Untersuchungen zur wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 ¹¹¹ Wasserstandsentwicklung in der deutschen bucht: Zwischenbericht zum kfki- ¹¹² projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), ¹¹³ 135–161. Retrieved from \url{https://hdl.handle.net/20.500.11970/ ¹¹¹ 101279} ¹¹² Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal ¹¹³ modulation of the lunar semidiurnal tide in the bay of fundy and gulf of ¹¹⁴ maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ ¹¹⁵ science.230.4721.69} ¹¹⁵ Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels ¹¹⁶ based on a quasi-global tide-gauge data set. Journal of Geophysical Research, ¹¹⁷ 115(C10), 267. doi: \url{10.1029/2009JC005997} ¹¹⁸ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 ¹¹³ projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), ¹²⁹ projekt - wasserstandsentwicklung in der deutschen bucht. Die Küste(47), ^{135-161.} Retrieved from \url{https://hdl.handle.net/20.500.11970/ ^{101279}} ¹²² Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal ¹²³ modulation of the lunar semidiurnal tide in the bay of fundy and gulf of ¹²⁴ maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ ¹²⁵ science.230.4721.69} ¹²⁶ Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels ¹²⁷ based on a quasi-global tide-gauge data set. Journal of Geophysical Research, ¹²⁸ 115(C10), 267. doi: \url{10.1029/2009JC005997} ¹²⁹ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 135-161. Retrieved from https://hdl.handle.net/20.500.11970/ 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69-71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 101279} Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115(C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 Ku, L. F., Greenberg, D. A., Garrett, C. J., & Dobson, F. W. (1985). Nodal modulation of the lunar semidiurnal tide in the bay of fundy and gulf of maine. Science (New York, N.Y.), 230 (4721), 69–71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 ¹⁷²³ modulation of the lunar semidiurnal tide in the bay of fundy and gulf of ¹⁷²⁴ maine. Science (New York, N.Y.), 230(4721), 69–71. doi: \url{10.1126/ ¹⁷²⁵ science.230.4721.69} ¹⁷²⁶ Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels ¹⁷²⁷ based on a quasi-global tide-gauge data set. Journal of Geophysical Research, ¹⁷²⁸ 115 (C10), 267. doi: \url{10.1029/2009JC005997} ¹⁷²⁹ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 maine. Science (New York, N.Y.), 230(4721), 69–71. doi: 10.1126/ science.230.4721.69} Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 ⁷²⁵ science.230.4721.69} ⁷²⁶ Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels ⁷²⁷ based on a quasi-global tide-gauge data set. Journal of Geophysical Research, ⁷²⁸ 115 (C10), 267. doi: \url{10.1029/2009JC005997} ⁷²⁹ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since
 Menéndez, M., & Woodworth, P. L. (2010). Changes in extreme high water levels based on a quasi-global tide-gauge data set. Journal of Geophysical Research, 115 (C10), 267. doi: \url{10.1029/2009JC005997} Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since 1080 Combining Proceeding 1080 (11) (1080)
hieroniales, hier
¹²¹ 115 (C10), 267. doi: \url{10.1029/2009JC005997} ²²⁹ Müller, M. (2011). Rapid change in semi-diurnal tides in the north atlantic since ¹⁰⁸⁰ 1080 1
$\begin{array}{ccc} \text{Müller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Muller, M.} & (2011). & \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\ \text{Rapid change in semi-diurnal tides in the north atlantic since} \\$
125 matrix, 11000 (2011). Tuple change in some further interior in the forth a statistic since 1000 (2011). 11000 (2011)
$_{220}$ [980] Geophysical Research Letters $3X(11)$ n/a-n/a doi: \11rl{10}[0]29/
2011GL047312}
$\frac{1}{2010} \qquad \qquad$
Seasonal variation of the m 2 tide $Ocean Dunamics 6l(2)$ 159–177 doi:
$\sqrt{1000} = 1000 \text{ scalar variation of the m 2 tide. \sqrt{1000} = 1000 \text{ scalar variation of the m 2 tide.}$
Peng D Hill E M Meltzner A I & Switzer A D (2010) Tide gauge records
show that the 18.61-year nodal tidal cycle can change high water levels by up
t_{22} to 30 cm Journal of Geophysical Research: Oceans $19/(1)$ 736–740 doi:
$1238 $ \url{10.1029/2018.JC014605}
220 Proudman J (1960) The condition that a long-period tide shall follow the
⁷³⁹ Proudman, J. (1960). The condition that a long-period tide shall follow the equilibrium-law. <i>Geophysical Journal International</i> 3(2) 244–249 doi:

Pugh, D. T. (1987). *Tides, surges and mean sea level*. Chichester: Wiley.

752

753

754

755

756

757

- Rasquin, C., Seiffert, R., Wachler, B., & Winkel, N. (2020). The significance
 of coastal bathymetry representation for modelling the tidal response to
- mean sea level rise in the german bight. Ocean Science, 16(1), 31-44. doi: \url{10.5194/os-16-31-2020}
- Ray, R. D. (2006). Secular changes of the m tide in the gulf of maine. Continental Shelf Research, 26(3), 422–427. doi: \url{10.1016/j.csr.2005.12.005}
- Rossiter, J. R. (1967). An analysis of annual sea level variations in european waters.
 Geophysical Journal International, 12(3), 259–299. doi: \url{10.1111/j.1365
 -246X.1967.tb03121.x}
 - Sehili, A., Lang, G., & Lippert, C. (2014). High-resolution subgrid models: Background, grid generation, and implementation. Ocean Dynamics, 64(4), 519–535. doi: \url{10.1007/s10236-014-0693-x}
 - Shaw, A., & Tsimplis, M. N. (2010). The 18.6yr nodal modulation in the tides of southern european coasts. Continental Shelf Research, 30(2), 138–151. doi: \url{10.1016/j.csr.2009.10.006}
- Sündermann, J., & Pohlmann, T. (2011). A brief analysis of north sea physics.
 Oceanologia, 53(3), 663–689. doi: \url{10.5697/oc.53-3.663}
- Trupin, A., & Wahr, J. (1990). Spectroscopic analysis of global tide gauge sea level data. Geophysical Journal International, 100(3), 441–453. doi: \url{10.1111/ j.1365-246X.1990.tb00697.x}
- Woodworth, P. L. (2012). A note on the nodal tide in sea level records. Journal of
 Coastal Research, 280, 316–323. doi: \url{10.2112/JCOASTRES-D-11A-00023}
 .1}
- 766Woodworth, P. L., & Blackman, D. L.(2004).Evidence for systematic767changes in extreme high waters since the mid-1970s.Journal of Climate,76817(6), 1190-1197.doi: $url{10.1175/1520-0442(2004)017{\textless}1190:}$ 769EFSCIE{\textgreater}2.0.CO;2}
- Woodworth, P. L., Shaw, S. M., & Blackman, D. L. (1991). Secular trends in
 mean tidal range around the british isles and along the adjacent european
- $_{772}$ coastline.Geophysical Journal International, 104(3), 593–609.doi: $_{773}$ $url\{10.1111/j.1365-246X.1991.tb05704.x\}$