

Beach slopes from satellite-derived shorelines

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Abstract

The steepness of the beach face is a fundamental parameter for coastal morphodynamic research. Despite its importance, it remains extremely difficult to obtain reliable estimates of the beach-face slope over large spatial scales (1000's of km of coastline). In this letter, a novel approach to estimate this slope from time-series of satellite-derived shoreline positions is presented. This new technique uses a frequency-domain analysis to find the optimum slope that minimises high-frequency tidal fluctuations relative to lower-frequency erosion/accretion signals. A detailed assessment of this new approach at 8 locations spanning a range of tidal regimes, wave climates and sediment grain sizes shows strong agreement ($R = 0.9$) with field measurements. The automated technique is then applied across 1000's of beaches in eastern Australia and California USA, revealing similar regional-scale distributions along these two contrasting coastlines and highlights the potential for new global-scale insight to beach-face slope spatial distribution, variability and trends.

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Key Points [140 characters each]:

- Novel remote sensing technique to estimate beach-face slopes from satellite imagery and modelled tides.
- Time-series of shoreline change are transformed into frequency domain to find the slope that minimises high-frequency tidal fluctuations.
- Validation against in situ data shows high accuracy across sites ranging in grain size, tidal range and wave climate.

Abstract [150 words]

The steepness of the beach face is a fundamental parameter for coastal morphodynamic research. Despite its importance, it remains extremely difficult to obtain reliable estimates of the beach-face slope over large spatial scales (1000's of km of coastline). In this letter, a novel approach to estimate this slope from time-series of satellite-derived shoreline positions is presented. This new technique uses a frequency-domain analysis to find the optimum slope that minimises high-frequency tidal fluctuations relative to lower-frequency erosion/accretion signals. A detailed assessment of this new approach at 8 locations spanning a range of tidal regimes, wave climates and sediment grain sizes shows strong agreement ($R^2 = 0.93$) with field measurements. The automated technique is then applied across 1000's of beaches in Eastern Australia and California USA, revealing similar regional-scale distributions along these two contrasting coastlines and

highlights the potential for new global-scale insight to beach-face slope spatial distribution, variability and trends.

Plain Language Summary [Optional]

How steep a beach is can dictate the way the beach interacts with the incoming ocean waves and therefore is of paramount importance for coastal scientists and engineers, coastal flood modelers and swim-safety officers. However, despite its importance, it is impractical to obtain reliable estimates of the ‘typical’ beach-face slope along large lengths of sandy coastlines (100’s to 1000’s of km) because of the logistics that would be necessary to visit many sites repeatedly to obtain these measurements. This letter describes a new technique to estimate the beach-face slope in the absence of field observations, relying instead on long-term publicly available satellite observations and a global tide model. This technique is then applied to 1000’s of beaches along the coastlines of Eastern Australia and California in the USA.

1 Introduction

The beach face is the most seaward region of the subaerial beach, where remaining ocean wave energy, following dissipation across the surf zone, is converted to potential energy in the form of wave runup and setup (Stockdon et al., 2006). The steepness of the beach face is closely related to grain size (Bujan et al., 2019), with gravel beaches typically adopting a steeper beach face ($\tan\beta > 0.1$) and finer sand beaches a flatter beach face ($\tan\beta \sim 0.01$ - 0.1). It is one of the key parameters controlling the elevation of wave runup and total swash excursion at the shoreline, processes that are of primary concern for assessing coastal inundation hazards along the coastal boundary (Senechal et al., 2011; Stockdon et al., 2007). The beach-face slope is also a useful proxy for surf zone morphology (Harley et al., 2015), which in the absence of difficult-to-obtain surf-zone bathymetric measurements, can inform surf-zone hydrodynamics (Battjes, 1974) such as wave breaker type (i.e., spilling, plunging or surging waves), wave set-up across the surf zone (Stephens et al., 2011), as well as beach swimmer safety (Short et al., 1993).

While the beach-face slope can be readily measured at individual beaches using conventional survey techniques, beach-face slope estimates at large spatial scales (i.e., regional, national or global) has to-date remained a core challenge. More significantly, while in recent decades Airborne Lidar (Stockdon et al., 2002) and UAV-based photogrammetry (Turner et al., 2016a) have considerably increased our ability to collect coastal topographic data over large spatial scales, applying these remote sensing methods across the intertidal profile and swash zone remains a challenge due to episodic submergence by the tide and wave run-up. The absence of large-scale datasets of beach-face slope estimates has been reported as a key limitation in the development of operational coastal inundation forecasting systems at the national scale (e.g., O’Grady et al., 2019) as well as in quantifying the contribution of wave run-up and setup at the shoreline relative to global sea-level-rise (Melet et al., 2018; Vitousek et al., 2017). Notably, these and other studies have attempted to overcome this limitation by assuming a global-constant beach-face slope of $\tan\beta = 0.1$ (or slope-independent runup formulations), an approach which has been challenged by peers (e.g., Aucan et al., 2019). In this context, a new method to estimate the typical beach-face slope across large spatial scales is needed.

This letter presents and demonstrates an innovative method to obtain estimates of the beach-face slope across the globe using satellite-derived shorelines. This approach follows recent efforts combining 30 years of satellite-derived shorelines with tidal models to create intertidal digital elevation models at the national scale (Bishop-Taylor et al., 2019a; Tseng et al., 2017). However, whereas these recent approaches obtain an approximation of the intertidal zone by assuming that the intertidal morphology at all coastal locations remains constant over time, this new approach inherently incorporates the highly dynamic nature of the intertidal zone that is observed at many sites worldwide, making it robust to the wide range of coastal environments found globally. To illustrate, Figure 1 highlights the challenges of estimating the beach-face slope at a dynamic beach where, as a result of naturally occurring cross-shore shoreline variability, the intertidal beach profile cannot be simply reconstructed from multiple shoreline observations at different tidal stages. This is due to the significant scatter induced by the dynamic beach profile, necessitating a more robust approach to estimate the beach-face slope.

A rigorous validation is presented of this new technique using both real and synthetic test cases ranging in slope, tidal range and wave energy. The automated method is then applied across 1000's of beaches along the coastlines of Eastern Australia and California, USA, to determine the distribution of beach-face slopes along these two coastlines located on opposite sides of the Pacific.

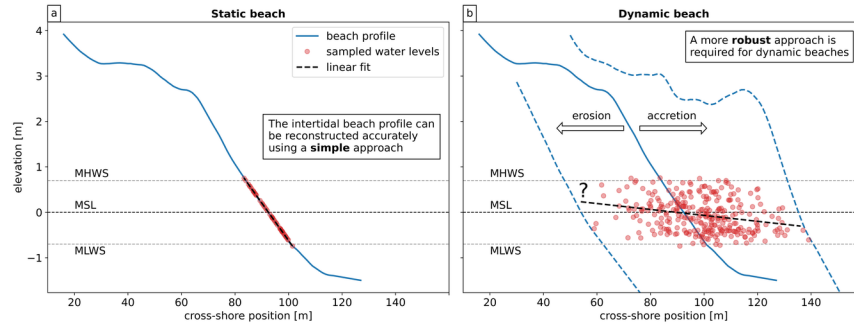


Figure 1 . Challenges of estimating the steepness of the intertidal zone in a dynamic coastal environment where the beach face is constantly fluctuating landwards/seawards due to erosion/accretion processes. Red dots indicate long-term satellite-derived shoreline measurements (x coordinate) sampled at various tidal elevations (y coordinate). **a)** Hypothetical example of a static beach profile where the cross-shore variations in the water line are entirely due to the rise and fall of the tide and therefore the intertidal beach profile can be accurately reconstructed. **b)** Real-world example of a surveyed profile at Narrabeen Beach (Australia) where the continuous erosion and accretion of the beach results in scattered observations from which it is not possible to reconstruct the intertidal beach profile.

2 Materials and Methods

2.1 Test sites

To quantify and assess the capability of this novel technique to estimate beach-face slopes, eight diverse locations across three continents are considered. The selected sites exhibit a large range of beach-face slope, grain size and tidal range. Among the eight sites, two are macrotidal beaches (Slapton Sands, UK and Cable Beach, Australia), three are mesotidal beaches (Tairua, New Zealand, Torrey Pines, USA and Ensenada, Mexico), and three are microtidal beaches (Narrabeen and Moruya-Pedro, Australia and Duck, USA). The sites were selected based on availability of repeat *in situ* topographic surveys to calculate the temporal-average beach-face slope, defined for each cross-shore transect from mean sea level (MSL) to mean high water springs (MHWS). Table 1 summarises the key characteristics at each site (average beach slope, mean spring tidal range, mean deep-water significant wave height and sediment grain size) and the geographical locations are presented in Figure S1 (Supporting Information). The broad range of temporal-average beach-face slopes range from 0.025 at Cable Beach to 0.14 at Slapton Sands.

Site	Average beach-face slope *	Mean springs tidal range [m]	Mean deep-water H_s [m]	D_{50} [mm]	TR/ $\tan\beta$ ** [m]	Reference publication
Slapton Sands UK	0.14	4.3	0.5 - 1	2-10	30.7	Ruiz de Alegria-Arzaburu and Masselink (2010)
Tairua NZ	0.13	2	1.4	0.6	15.4	Blossier et al. (2017)

Site	Average beach-face slope *	Mean springs tidal range [m]	Mean deep-water H_s [m]	D_{50} [mm]	TR/ $\tan\beta$ ** [m]	Reference publication
Duck USA	0.1	1.2	1	0.3	12	Larson and Kraus (1994)
Narrabeen AUS	0.09	1.3	1.6	0.3	14.4	Turner et al. (2016b)
Moruya/Pedro AUS	0.08	1.3	1.2 - 1.4	0.35	16.2	Short et al. (2014)
Torrey Pines USA	0.04	2.3	1	0.23	57.5	Ludka et al. (2019)
Ensenada MEX	0.03	2.3	1	0.25	76.6	Ruiz de Alegría-Arzaburu et al. (2017)
Cable Beach AUS	0.025	8.2	0.5	0.11-0.13	328	Masselink & Pattiaratchi, (2000) Wright et al. (1982)

Table 1. Summary of the eight study sites, including average beach slope, tidal range, significant wave height (H_s) and grain size (D_{50}). For further details on the individual sites refer to the cited publications.

* beach slope is calculated between MSL and MHWS.

** ratio between tidal range and beach-face slope.

2.2 Beach-face slope estimation algorithm

The objective of the automated algorithm developed here is to estimate the beach-face slope at any site worldwide without the requirement for *in situ* measurements (e.g., topographic surveys, tide gauges, etc) but instead relying exclusively on remotely-sensed data. This new technique fully leverages the capabilities of satellite remote sensing in the coastal zone, including the use of optical imagery for mapping shoreline changes and altimetry for measuring water level changes.

Recent developments in shoreline mapping now make it possible to extract instantaneous shorelines from publicly available satellite imagery (Bishop-Taylor et al., 2019b; Pardo-Pascual et al., 2018; Vos et al., 2019a). Note that these shorelines are referred to as ‘instantaneous’ because they are mapped on individual satellite images acquired at different and arbitrary stages of the tide. Consequently, time-series of cross-shore change obtained from these instantaneous shorelines also implicitly include the superposition of tidal excursion and sediment transport processes – i.e., beach erosion/accretion. In order to estimate the slope of the beach face, the fluctuations caused by tidal excursions must be isolated from the horizontal changes resulting from erosion and/or accretion of the beach. To do this a frequency-domain analysis is applied to isolate the high-frequency tidal signal in the cross-shore shoreline time-series from the typically lower-frequency morphological changes. The step-by-step methodology to estimate the typical beach-face slope from satellite-derived shorelines and modelled tide levels is illustrated in Figure 2 and described below.

Extract satellite-derived shorelines from Landsat imagery (Figure 2a):

Satellite-derived instantaneous shorelines are extracted using *CoastSat* (Vos et al., 2019a), an open-source toolbox that enables users to obtain time-series of cross-shore shoreline position at any sandy coastline worldwide from 30+ years of publicly available satellite imagery (Landsat 5, 7, 8 and Sentinel-2) accessed

via Google Earth Engine (Gorelick et al., 2017). A target sampling period of no more than 8 days was maintained by the use of all Landsat images between 1999 and 2019 (i.e., 16-day revisit with at least 2 satellites concurrently in orbit). Sentinel-2 images were excluded as the poor cloud masking algorithm hampered a fully automated shoreline extraction. The cross-shore accuracy of the mapped shorelines varies between 10 and 15 m depending on site characteristics, as was previously reported in Vos et al. (2019b). Time-series of cross-shore shoreline change were obtained by intersecting the mapped shorelines with shore-normal transects at each site. An example of the resulting raw time-series of shoreline change at Cable Beach is shown in Figure 2a.

Tide levels from a global tide model and peak tidal frequency (Figures 2b and 2d):

Once the satellite-derived shorelines have been mapped, the corresponding tide levels at the time of image acquisition are obtained from the FES2014 global tide model (Carrere et al., 2016). This model was chosen as it ranks amongst the best barotropic ocean tide models for coastal regions (Stammer et al., 2014). The next step is to identify in the tide elevation time-series (sub-sampled according to availability of satellite-derived shorelines) the frequency at which the tidal signal is the strongest. This frequency, hereafter referred to as ‘peak tidal frequency’, is determined by computing the Power Spectrum Density (PSD) of the tide level time-series. Importantly, the PSD cannot be computed with a traditional Fourier Transform (e.g., FFT) as the tide level time-series are unevenly sampled due to the presence of clouds within the associated satellite images. However, an alternative algorithm, the Lomb-Scargle transform (VanderPlas, 2018), widely used to analyse astronomical observations, is specifically suited to the calculation of the PSD from irregularly sampled time-series (see comparison with FFT in Supporting Information Figure S2).

The PSD of the tidal signal, depicted in Figure 2d, indicates how much tidal energy is contained at a given frequency, with the peaks revealing the frequency of the tidal harmonic constituents. Since the tide is sub-sampled at 8-day intervals, the higher-frequency semi-diurnal and diurnal components of the tide are completely missed, but some of the lower-frequency components can be resolved (e.g., spring-neap fortnightly cycle, monthly and annual cycles). Figure 2d shows the PSD of the sub-sampled tide time-series, indicating that the highest peak for this example is located at a period of 17.5 days. This energy corresponds to the spring-neap fortnightly cycle, which has a period of 14.76 days, but as the *Nyquist limit* is 16 days (twice the sampling period), the 14.76 days periodic signal is slightly aliased to 17.5 days. The aliasing of the tidal signal and the effect of the sampling frequency are further discussed in Supporting Information S3.

Tidal correction with a range of beach-face slope values (Figure 2c):

Tidal correction consists of the projection of individual instantaneous shorelines, acquired at different stages of the tide, to a standard reference elevation, for example Mean Sea Level (MSL). A simple tidal correction is applied by translating horizontally the shoreline points along a cross-shore transect using a linear slope:

$$x_{\text{corrected}} = x + \frac{z_{\text{tide}}}{\tan\beta}(1)$$

where $x_{\text{corrected}}$ is the tidally-corrected cross-shore position, x is the instantaneous cross-shore position, z_{tide} is the corresponding tide level and $\tan\beta$ is the beach-face slope. Using Eq. (1) the raw time-series of cross-shore shoreline positions are tidally corrected using a range of potential slope values from 0.01 to 0.2, the latter considered “a universally relevant upper limit of sandy beach-face slopes” (Bujan et al., 2019).

Find the slope that minimises the tidal component of the shoreline time-series (Figures 2e and 2f):

As the final step in this automated process, the Lomb-Scargle transform is employed to compute the PSD of each of the tidally-corrected time-series. Figure 2e shows the PSD curves resulting from the tidally-corrected time-series depicted in Figure 2c. An inset on the peak tidal frequency band (17.5 days) demonstrates how the magnitude of this peak is modulated by the slope value used for tidal correction. In this example (Cable Beach), the 17.5 days peak is entirely suppressed when using a slope of 0.025 (as indicated by the blue dashed curve, Figure 2e).

Finally, the typical beach-face slope can be estimated by finding the slope value that, when used to tidally-

correct the shoreline time-series, minimises the amount of tidal energy. Figure 2f shows the ‘tidal energy’ (i.e., the integral of PSD inside the peak tidal frequency band) as a function of the slope value used for tidal correction, indicating a distinct minimum for a slope of 0.025. For this site, this leads to the conclusion that $\tan\beta = 0.025$ is the temporal-average beach-face slope at this macro-tidal, fine sand grain size location.

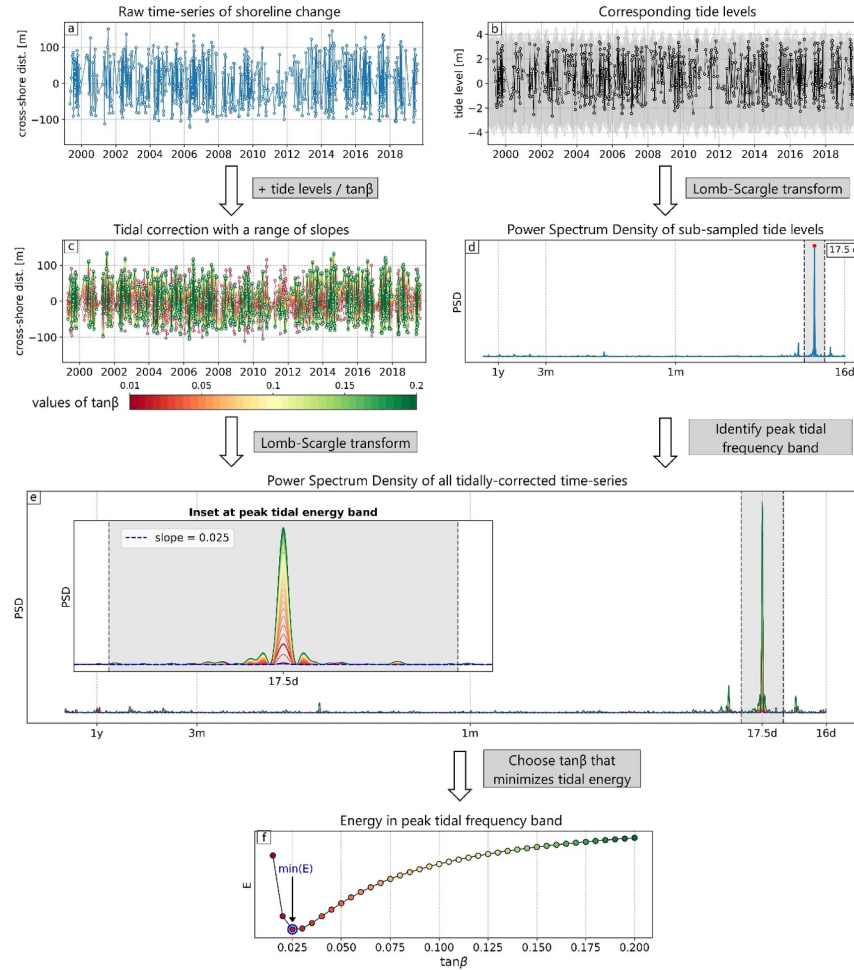


Figure 2 . Step-by-step description of the algorithm developed to estimate typical beach-face slope from satellite-derived shorelines. The time-series of shoreline change and tide levels shown here are from Cable Beach (Western Australia). **a)** Raw (i.e., non-tidally corrected) time-series of shoreline change along the southern shore-normal transect at Cable Beach (see Figure S1 in Supporting Information). **b)** Modelled tide levels associated with the satellite-derived shorelines (black line). The grey shaded area indicates the overall tidal fluctuations, noting that the vertical bias here is due to the sun-synchronous orbit of Landsat satellites (refer to Bishop-Taylor et al., 2019a). **c)** Ensemble of tidally-corrected time-series of shoreline change using slope values ranging from 0.01 (red) to 0.2 (green). **d)** Power Spectrum Density (PSD) of the sub-sampled tide level time-series. The peak tidal frequency band (grey shaded area) is centred at a frequency of 17.5 days and stretches 10^{-8} Hz each side. **e)** PSD of the ensemble of tidally-corrected shoreline time-series. The inset zooms on the peak tidal frequency band and shows how the magnitude of the peak at this frequency is entirely suppressed when using a slope of 0.025 (blue dashed line). **f)** Energy in the peak tidal frequency band for the range of slopes tested. The slope that minimises the energy inside the peak tidal frequency band is selected as the best estimate of the beach-face slope.

3 Results

The beach-face slope estimation algorithm described in the previous section was applied to the eight test sites along the transects depicted in Figure S1 (39 transects in total) and compared to *in situ* measurements. The measured beach-face slope at each transect was computed as the average of all the available surveys (calculated from MSL to MHWS), except at Cable Beach where only two known surveys were conducted (Masselink & Pattiaratchi, 2000; Wright et al., 1982). Figure 3a shows a 1:1 plot comparing the satellite-derived beach-face slopes ($\tan\beta_{\text{satellite}}$) to the *in situ* beach-face slopes ($\tan\beta_{\text{in situ}}$). For the *in situ* data (x-axis), a horizontal bar indicates one standard deviation around the average to highlight the degree of temporal variability in beach-face slope observed at each location.

Overall, there is a strong correlation between satellite-derived estimates and *in situ* averages, with a coefficient of determination (R^2) of 0.93 and no systematic under- or over-estimation observed. While the slope estimation algorithm performed very well along the gentle sloping profiles ($\tan\beta_{\text{in situ}} < 0.05$) of Cable Beach, Ensenada and Torrey Pines, as well as along the steeper ($\tan\beta_{\text{in situ}} > 0.12$) profiles at Slapton Sands and Tairua, relatively more scatter is observed at the more intermediate sites (Duck, Moruya/Pedro and Narrabeen). These intermediate sites ($0.5 < \tan\beta_{\text{in situ}} < 0.12$) are also characterised by a larger temporal variability in beach slope as indicated by the width of the standard deviation bars. In terms of accuracy, the standard deviation of the errors was 0.01 with 90% of the errors falling below 0.015.

While this new capability may become highly valuable for a range of applications as it does not rely on any field measurements, there are limitations. Firstly, this method relies on the existence of a measurable tidal excursion signal in the satellite-derived shoreline time-series. Since the horizontal accuracy of the satellite-derived shorelines is $\sim 10\text{m}$, in order to capture the tidal excursion signal, the amplitude of this fluctuation needs to be significantly larger than 10m – e.g., a tidal excursion of 20 m has a signal-to-noise ratio of 2. In turn, the amplitude of the tidal excursion depends on the tidal range and on the angle of the intertidal zone.

To identify the range of tidal regimes and beach-face slopes over which this method is applicable, additional synthetic time-series of shoreline change were generated for a planar beach with specified slope and tidal range (the details on how these time-series were generated are included in Supporting Information S4). Figure 3b summarises the accuracy of the estimated beach-face slopes – i.e., Normalised Mean Absolute Error (MNAE) based on 100 synthetic time-series – as a function of tidal range (TR) and beach-face slope ($\tan\beta$). As anticipated, the accuracy declines with decreasing tidal range and increasing beach-face slope, as a decrease in the ratio $\text{TR}/\tan\beta$ is equivalent to reducing the amplitude of the horizontal tidal excursions. Based on these synthetic data, the errors can be as much as 30% for $\text{TR}/\tan\beta$ ratios smaller than 10 (i.e., $\text{TR} < 1\text{ m}$ and $\tan\beta > 0.1$). Consequently, in order to obtain accurate slope estimates, it is recommended that the technique be applied at any site where $\text{TR}/\tan\beta$ is larger than 10. This is further emphasised by the fact that every one of the eight test sites, for which the tidal ranges and average *in situ* beach-face slopes are also included in Figure 3b, are situated at locations where $\text{TR}/\tan\beta > 10$ (exact ratios reported in Table 1).

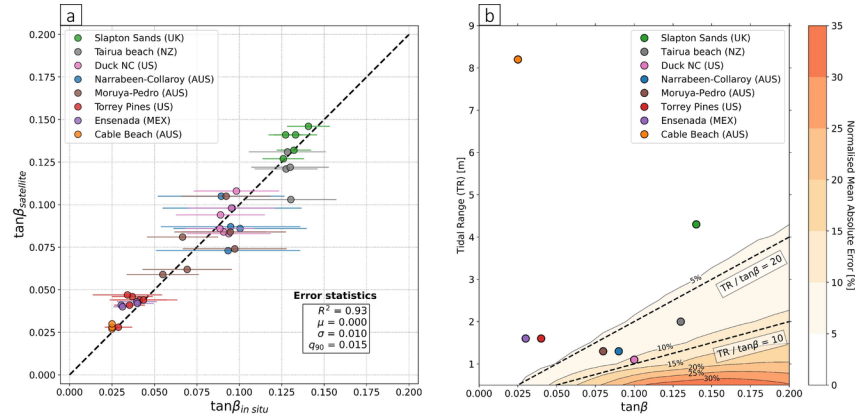


Figure 3 . Quantitative assessment of the beach-face slope estimation technique. **a)** 1:1 plot illustrating the comparison between *in situ* measurements of the beach-face slope (x-axis) and satellite-derived estimates (y-axis) at the eight test sites (total of 39 cross-shore transects). The horizontal bars represent one standard deviation from the average *in situ* slope and indicate the degree of temporal variability in beach-face slope at each transect. **b)** Synthetic analysis showing that the accuracy of the method declines with decreasing tidal range to beach-face slope ratio $TR/\tan\beta$. The orange contours represent the Normalised Mean Absolute Error (NMSE) for each combination of tidal range and beach-face slope based on 100 synthetic shoreline time-series (described in Supporting Information S4). The two black dashed lines indicate respectively a ratio of tidal range to beach-face slope of 10 and 20. The dots indicate the tidal range and average beach-face slope at each of the eight test sites.

4 Regional-scale application: Eastern Australia and California USA coastlines

To demonstrate how this technique can be applied over large spatial scales, an example application at the regional scale along two stretches of coastline is presented here: the Eastern Australian coastline (~1800 km) and the California USA coast (~1500km). The methodology described in Section 2 was applied at 100 m alongshore-spaced intervals at sandy beaches along both coasts; in Eastern Australia this resulted in a total of 13,624 beach-face slope estimates; in California 8,147. The results are shown in Figures 4a and 4b and the complete dataset is available as an interactive web dashboard in the Data Availability section below. The regional-scale distributions of beach-face slopes are depicted in Figure 4c. In both Eastern Australia and California approximately 80% of time-averaged slopes are between 0.04 and 0.08, with the corresponding means of 0.062 (SE Australia) and 0.068 (California).

As a pointer to where the new availability of broad-scale beach slope information may find further application, an empirical relationship between beach-face slope and sediment size D_{50} was recently derived by Bujan et al. (2019) based on 2,144 individual field measurements. This equation can now be employed along the Eastern Australian and Californian coastlines to convert the beach-face slope estimates to the equivalent grain size (D_{50}) and obtain an estimate of the distribution of sediment grain sizes for beaches occurring along the full extent of both regions (see inset in Figure 4c). The detailed analyses of beach-face slope and sediment size distributions at regional scales are outside the scope of this letter, but this example demonstrates the significant potential of this technique to provide beach-face slope estimates as well as sediment size distributions at the global scale.

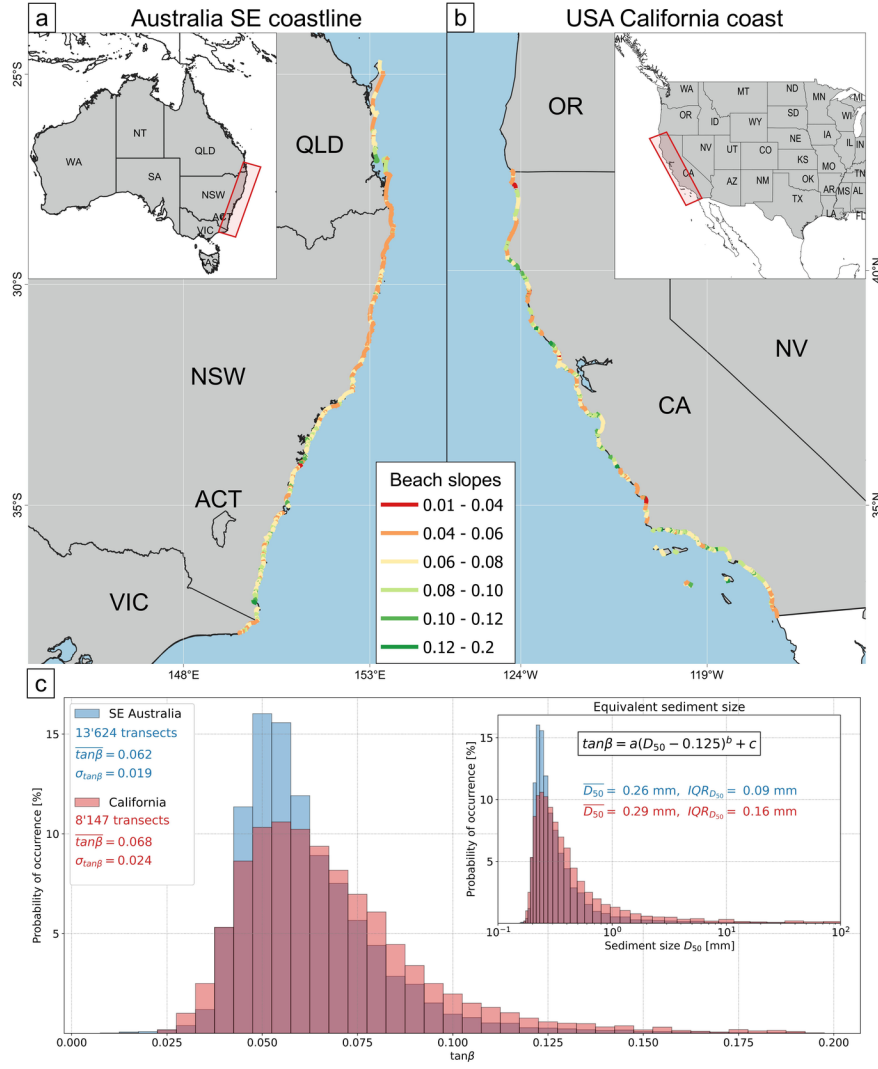


Figure 4 . Regional-scale application over SE Australia and California. The mean beach-face slope is 0.062 for SE Australia and 0.068 for California, with both regions showing similar spread around the mean (standard deviations of 0.019 and 0.024 respectively). **a)** Map of beach-face slopes estimated along 13'624 transects on the SE Australian coastline. **b)** Map of beach-face slopes estimated along 8'147 transects on Californian US west coast. **c)** Histogram of the distribution of beach-face slopes along the two stretches of coastline (SE Australia and California). In the top-right inset the equivalent sediment size distributions are obtained with the empirical relationship from Bujan et al. (2019). The mean D_{50} values are 0.26 and 0.29 mm respectively for SE Australia and California, with an inter-quartile range (IQR) of 0.09 and 0.16 mm.

5 Conclusions

A novel methodology to estimate beach-face slopes from satellite-derived shorelines and modelled tides is described here and evaluated along eight diverse sandy/gravel beaches spanning a broad range of tidal regimes, beach-face slopes and wave climates. This new technique employs a variant of the Fourier transform, the Lomb-Scargle transform, to identify the slope that, when used for tidal correction, minimises the tidal energy in the shoreline time-series.

A comparison with *in situ* (beach survey) topographic data along 39 transects demonstrates that this tech-

nique is capable of estimating the time-averaged beach-face slope in different coastal environments ranging from macrotidal, gentle-sloping beaches, to microtidal wave-dominated beaches. Further analysis using synthetic shoreline data reveals that the accuracy of this method declines significantly when the ratio between tidal range and beach-face slope is < 10 .

Finally, an example application spanning a section of the Eastern Australia and California USA coastlines demonstrates the capability of this technique to estimate beach-face slopes over large spatial scales, with the potential to now create and further investigate a global dataset of beach-face slopes. It is anticipated that the future availability of such a dataset will be a key variable to support global studies on the impact of sea level rise and increased storminess along world coastlines.

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Data availability

- The beach-face slope datasets for Eastern Australia and California can be visualised and downloaded on an interactive web dashboard at <http://coastsat.wrl.unsw.edu.au/>.
- The data sets have also been uploaded to the following open-access Zenodo data repository <https://doi.org/10.5281/zenodo.3747130>.
- The codes to estimate beach slopes with this technique are available in a Github repository (<https://github.com/kvos/CoastSat.slope>) uploaded to Zenodo with the following DOI: <https://doi.org/10.5281/zenodo.3872443>.

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Beach slopes from satellite-derived shorelines

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Key Points [140 characters each]:

- Novel remote sensing technique to estimate beach-face slopes from satellite imagery and modelled tides.
- Time-series of shoreline change are transformed into frequency domain to find the slope that minimises high-frequency tidal fluctuations.
- Validation against in situ data shows high accuracy across sites ranging in grain size, tidal range and wave climate.

Abstract [150 words]

The steepness of the beach face is a fundamental parameter for coastal morphodynamic research. Despite its importance, it remains extremely difficult to obtain reliable estimates of the beach-face slope over large spatial scales (1000's of km of coastline). In this letter, a novel approach to estimate this slope from time-series of satellite-derived shoreline positions is presented. This new technique uses a frequency-domain analysis to find the optimum slope that minimises high-frequency tidal fluctuations relative to lower-frequency erosion/accretion signals. A detailed assessment of this new approach at 8 locations spanning a range of tidal regimes, wave climates and sediment grain sizes shows strong agreement ($R^2 = 0.93$) with field measurements. The automated technique is then applied across 1000's of beaches in Eastern Australia and California USA, revealing similar regional-scale distributions along these two contrasting coastlines and highlights the potential for new global-scale insight to beach-face slope spatial distribution, variability and trends.

Plain Language Summary [Optional]

How steep a beach is can dictate the way the beach interacts with the incoming ocean waves and therefore is of paramount importance for coastal scientists and engineers, coastal flood modelers and swim-safety officers. However, despite its importance, it is impractical to obtain reliable estimates of the 'typical' beach-face slope along large lengths of sandy coastlines (100's to 1000's of km) because of the logistics that would be necessary to visit many sites repeatedly to obtain these measurements. This letter describes a new technique to estimate the beach-face slope in the absence of field observations, relying instead on long-term publicly available satellite observations and a global tide model. This technique is then applied to 1000's of beaches along the coastlines of Eastern Australia and California in the USA.

1 Introduction

The beach face is the most seaward region of the subaerial beach, where remaining ocean wave energy, following dissipation across the surf zone, is converted to potential energy in the form of wave runup and setup (Stockdon et al., 2006). The steepness of the beach face is closely related to grain size (Bujan et al., 2019), with gravel beaches typically adopting a steeper beach face ($\tan\beta > 0.1$) and finer sand beaches a flatter beach face ($\tan\beta \sim 0.01-0.1$). It is one of the key parameters controlling the elevation of wave runup and total swash excursion at the shoreline, processes that are of primary concern for assessing coastal inundation hazards along the coastal boundary (Senechal et al., 2011; Stockdon et al., 2007). The beach-face slope is also a useful proxy for surf zone morphology (Harley et al., 2015), which in the absence of difficult-to-obtain surf-zone bathymetric measurements, can inform surf-zone hydrodynamics (Battjes, 1974) such as wave breaker type (i.e., spilling, plunging or surging waves), wave set-up across the surf zone (Stephens et al., 2011), as well as beach swimmer safety (Short et al., 1993).

While the beach-face slope can be readily measured at individual beaches using conventional survey techniques, beach-face slope estimates at large spatial scales (i.e., regional, national or global) has to-date remained a core challenge. More significantly, while in recent decades Airborne Lidar (Stockdon et al., 2002) and UAV-based photogrammetry (Turner et al., 2016a) have considerably increased our ability to collect coastal topographic data over large spatial scales, applying these remote sensing methods across the intertidal profile and swash zone remains a challenge due to episodic submergence by the tide and wave run-up. The absence of large-scale datasets of beach-face slope estimates has been reported as a key limitation in the development of operational coastal inundation forecasting systems at the national scale (e.g., O’Grady et al., 2019) as well as in quantifying the contribution of wave run-up and setup at the shoreline relative to global sea-level-rise (Melet et al., 2018; Vitousek et al., 2017). Notably, these and other studies have attempted to overcome this limitation by assuming a global-constant beach-face slope of $\tan\beta = 0.1$ (or slope-independent runup formulations), an approach which has been challenged by peers (e.g., Aucan et al., 2019). In this context, a new method to estimate the typical beach-face slope across large spatial scales is needed.

This letter presents and demonstrates an innovative method to obtain estimates of the beach-face slope across the globe using satellite-derived shorelines. This approach follows recent efforts combining 30 years of satellite-derived shorelines with tidal models to create intertidal digital elevation models at the national scale (Bishop-Taylor et al., 2019a; Tseng et al., 2017). However, whereas these recent approaches obtain an approximation of the intertidal zone by assuming that the intertidal morphology at all coastal locations remains constant over time, this new approach inherently incorporates the highly dynamic nature of the intertidal zone that is observed at many sites worldwide, making it robust to the wide range of coastal environments found globally. To illustrate, Figure 1 highlights the challenges of estimating the beach-face slope at a dynamic beach where, as a result of naturally occurring cross-shore shoreline variability, the intertidal beach profile cannot be simply reconstructed from multiple shoreline observations at different tidal stages. This is due to the significant scatter induced by the dynamic beach profile, necessitating a more robust approach to estimate the beach-face slope.

A rigorous validation is presented of this new technique using both real and synthetic test cases ranging in slope, tidal range and wave energy. The automated method is then applied across 1000’s of beaches along the coastlines of Eastern Australia and California, USA, to determine the distribution of beach-face slopes along these two coastlines located on opposite sides of the Pacific.

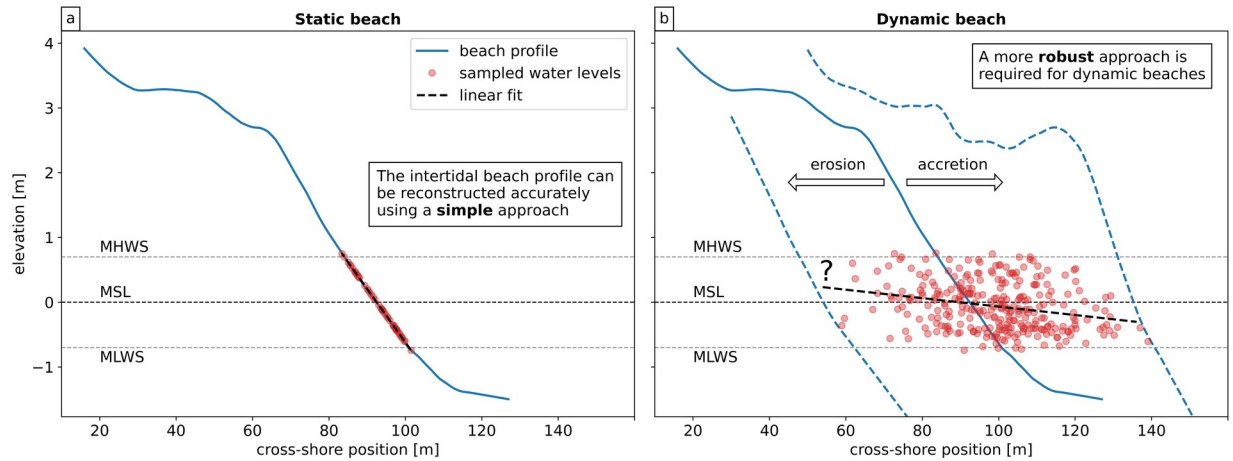


Figure 1. Challenges of estimating the steepness of the intertidal zone in a dynamic coastal environment where the beach face is constantly fluctuating landwards/seawards due to erosion/accretion processes. Red dots indicate long-term satellite-derived shoreline measurements (x coordinate) sampled at various tidal elevations (y coordinate). **a)** Hypothetical example of a static beach profile where the cross-shore variations in the water line are entirely due to the rise and fall of the tide and therefore the intertidal beach profile can be accurately reconstructed. **b)** Real-world example of a surveyed profile at Narrabeen Beach (Australia) where the continuous erosion and accretion of the beach results in scattered observations from which it is not possible to reconstruct the intertidal beach profile.

2 Materials and Methods

2.1 Test sites

To quantify and assess the capability of this novel technique to estimate beach-face slopes, eight diverse locations across three continents are considered. The selected sites exhibit a large range of beach-face slope, grain size and tidal range. Among the eight sites, two are macrotidal beaches (Slapton Sands, UK and Cable Beach, Australia), three are mesotidal beaches (Tairua, New Zealand, Torrey Pines, USA and Ensenada, Mexico), and three are microtidal beaches (Narrabeen and Moruya-Pedro, Australia and Duck, USA). The sites were selected based on availability of repeat *in situ* topographic surveys to calculate the temporal-average beach-face slope, defined for each cross-shore transect from mean sea level (MSL) to mean high water springs (MHWS). Table 1 summarises the key characteristics at each site (average beach slope, mean spring tidal range, mean deep-water significant wave height and sediment grain size) and the geographical locations are presented in Figure S1 (Supporting Information). The broad range of temporal-average beach-face slopes range from 0.025 at Cable Beach to 0.14 at Slapton Sands.

Site	Average beach-face slope *	Mean springs tidal range [m]	Mean deep-water H_s [m]	D_{50} [mm]	TR/tan β ** [m]	Reference publication
Slapton Sands UK	0.14	4.3	0.5 - 1	2-10	30.7	Ruiz de Alegria-

						Arzaburu and Masselink (2010)
Tairua NZ	0.13	2	1.4	0.6	15.4	Blossier et al. (2017)
Duck USA	0.1	1.2	1	0.3	12	Larson and Kraus (1994)
Narrabeen AUS	0.09	1.3	1.6	0.3	14.4	Turner et al. (2016b)
Moruya/Pedro AUS	0.08	1.3	1.2 - 1.4	0.35	16.2	Short et al. (2014)
Torrey Pines USA	0.04	2.3	1	0.23	57.5	Ludka et al. (2019)
Ensenada MEX	0.03	2.3	1	0.25	76.6	Ruiz de Alegría- Arzaburu et al. (2017)
Cable Beach AUS	0.025	8.2	0.5	0.11- 0.13	328	Masselink & Pattiaratchi, (2000) Wright et al. (1982)

Table 1. Summary of the eight study sites, including average beach slope, tidal range, significant wave height (Hs) and grain size (D50). For further details on the individual sites refer to the cited publications.

*beach slope is calculated between MSL and MHWS.

** ratio between tidal range and beach-face slope.

2.2 Beach-face slope estimation algorithm

The objective of the automated algorithm developed here is to estimate the beach-face slope at any site worldwide without the requirement for *in situ* measurements (e.g., topographic surveys, tide gauges, etc) but instead relying exclusively on remotely-sensed data. This new technique fully leverages the capabilities of satellite remote sensing in the coastal zone, including the use of optical imagery for mapping shoreline changes and altimetry for measuring water level changes.

Recent developments in shoreline mapping now make it possible to extract instantaneous shorelines from publicly available satellite imagery (Bishop-Taylor et al., 2019b; Pardo-Pascual et al., 2018; Vos et al., 2019a). Note that these shorelines are referred to as ‘instantaneous’ because they are mapped on individual satellite images acquired at different and arbitrary stages of the tide. Consequently, time-series of cross-shore change obtained from these instantaneous shorelines also implicitly include the superposition of tidal excursion and sediment transport processes – i.e., beach erosion/accretion. In order to estimate the slope of the beach face, the fluctuations caused by tidal excursions must be isolated from the horizontal changes resulting from erosion and/or accretion of the beach. To do this a frequency-domain analysis is applied to isolate the high-frequency tidal signal in the cross-shore shoreline time-series from the typically lower-frequency morphological changes. The step-by-step methodology to estimate the typical beach-face slope from satellite-derived shorelines and modelled tide levels is illustrated in Figure 2 and described below.

1) *Extract satellite-derived shorelines from Landsat imagery (Figure 2a):*

Satellite-derived instantaneous shorelines are extracted using *CoastSat* (Vos et al., 2019a), an open-source toolbox that enables users to obtain time-series of cross-shore shoreline position at any sandy coastline worldwide from 30+ years of publicly available satellite imagery (Landsat 5, 7, 8 and Sentinel-2) accessed via Google Earth Engine (Gorelick et al., 2017). A target sampling period of no more than 8 days was maintained by the use of all Landsat images between 1999 and 2019 (i.e., 16-day revisit with at least 2 satellites concurrently in orbit). Sentinel-2 images were excluded as the poor cloud masking algorithm hampered a fully automated shoreline extraction. The cross-shore accuracy of the mapped shorelines varies between 10 and 15 m depending on site characteristics, as was previously reported in Vos et al. (2019b). Time-series of cross-shore shoreline change were obtained by intersecting the mapped shorelines with shore-normal transects at each site. An example of the resulting raw time-series of shoreline change at Cable Beach is shown in Figure 2a.

2) *Tide levels from a global tide model and peak tidal frequency (Figures 2b and 2d):*

Once the satellite-derived shorelines have been mapped, the corresponding tide levels at the time of image acquisition are obtained from the FES2014 global tide model (Carrere et al., 2016). This model was chosen as it ranks amongst the best barotropic ocean tide models for coastal regions (Stammer et al., 2014). The next step is to identify in the tide elevation time-series (sub-sampled according to availability of satellite-derived shorelines) the frequency at which the tidal signal is the strongest. This frequency, hereafter referred to as ‘peak tidal frequency’, is determined by computing the Power Spectrum Density (PSD) of the tide level time-series. Importantly, the PSD cannot be computed with a traditional Fourier Transform (e.g., FFT) as the tide level time-series are unevenly sampled due to the presence of clouds within the associated satellite images. However, an alternative algorithm, the Lomb-Scargle transform (VanderPlas, 2018), widely used to analyse astronomical observations, is specifically suited to the calculation of the PSD from irregularly sampled time-series (see comparison with FFT in Supporting Information Figure S2).

The PSD of the tidal signal, depicted in Figure 2d, indicates how much tidal energy is contained at a given frequency, with the peaks revealing the frequency of the tidal harmonic constituents. Since the tide is sub-sampled at 8-day intervals, the higher-frequency semi-diurnal and diurnal components of the tide are completely missed, but some of the lower-frequency components can be resolved (e.g., spring-neap fortnightly cycle, monthly and annual cycles). Figure 2d shows the PSD of the sub-sampled tide time-series, indicating that the highest peak for this example is located at a period of 17.5 days. This energy corresponds to the spring-neap fortnightly cycle, which has a period of 14.76 days, but as the *Nyquist limit* is 16 days (twice the sampling period), the 14.76 days periodic signal is slightly aliased to 17.5 days. The aliasing of the tidal signal and the effect of the sampling frequency are further discussed in Supporting Information S3.

3) *Tidal correction with a range of beach-face slope values (Figure 2c):*

Tidal correction consists of the projection of individual instantaneous shorelines, acquired at different stages of the tide, to a standard reference elevation, for example Mean Sea Level (MSL). A simple tidal correction is applied by translating horizontally the shoreline points along a cross-shore transect using a linear slope:

$$\Delta x_{corrected} = \Delta x + \frac{z_{tide}}{\tan\beta} \quad (1)$$

where $\Delta x_{corrected}$ is the tidally-corrected cross-shore position, Δx is the instantaneous cross-shore position, z_{tide} is the corresponding tide level and $\tan\beta$ is the beach-face slope. Using Eq. (1) the raw time-series of cross-shore shoreline positions are tidally corrected using a range of potential slope values from 0.01 to 0.2, the latter considered “a universally relevant upper limit of sandy beach-face slopes” (Bujan et al., 2019).

4) *Find the slope that minimises the tidal component of the shoreline time-series (Figures 2e and 2f):*

As the final step in this automated process, the Lomb-Scargle transform is employed to compute the PSD of each of the tidally-corrected time-series. Figure 2e shows the PSD curves resulting from the tidally-corrected time-series depicted in Figure 2c. An inset on the peak tidal frequency band (17.5 days) demonstrates how the magnitude of this peak is modulated by the slope value used for tidal correction. In this example (Cable Beach), the 17.5 days peak is entirely suppressed when using a slope of 0.025 (as indicated by the blue dashed curve, Figure 2e).

Finally, the typical beach-face slope can be estimated by finding the slope value that, when used to tidally-correct the shoreline time-series, minimises the amount of tidal energy. Figure 2f shows the ‘tidal energy’ (i.e., the integral of PSD inside the peak tidal frequency band) as a function of the slope value used for tidal correction, indicating a distinct minimum for a slope of 0.025. For this site, this leads to the conclusion that $\tan\beta = 0.025$ is the temporal-average beach-face slope at this macro-tidal, fine sand grain size location.

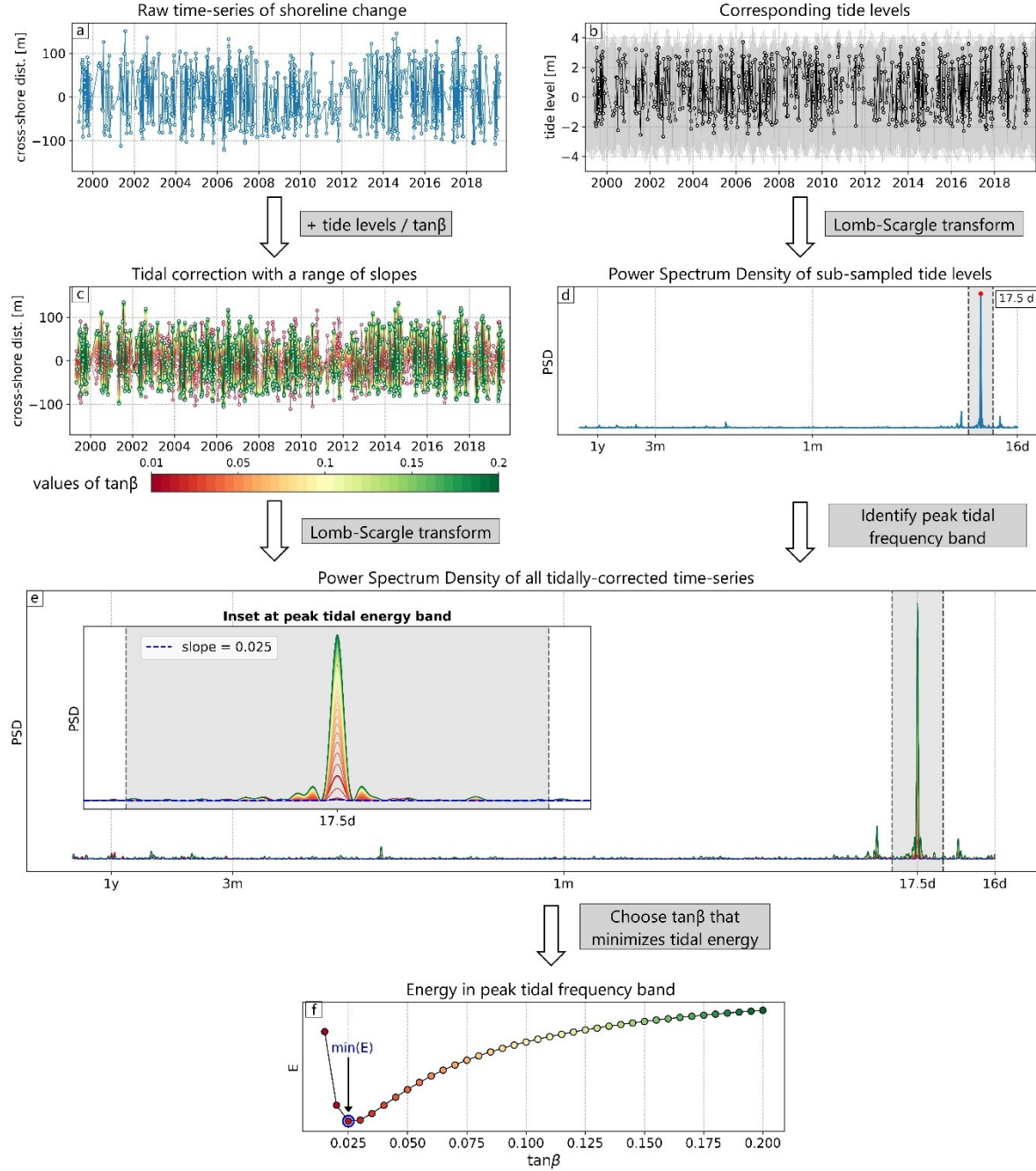


Figure 2. Step-by-step description of the algorithm developed to estimate typical beach-face slope from satellite-derived shorelines. The time-series of shoreline change and tide levels shown here are from Cable Beach (Western Australia). **a)** Raw (i.e., non-tidally corrected) time-series of shoreline change along the southern shore-normal transect at Cable Beach (see Figure S1 in Supporting Information). **b)** Modelled tide levels associated with the satellite-derived shorelines (black line). The grey shaded area indicates the overall tidal fluctuations, noting that the vertical bias here is due to the sun-synchronous orbit of Landsat satellites (refer to Bishop-Taylor et al., 2019a). **c)** Ensemble of tidally-corrected time-series of shoreline change using slope values ranging from 0.01 (red) to 0.2 (green). **d)** Power Spectrum Density (PSD) of the sub-sampled tide level time-series. The peak tidal frequency band (grey shaded

area) is centred at a frequency of 17.5 days and stretches 10^{-8} Hz each side. **e)** PSD of the ensemble of tidally-corrected shoreline time-series. The inset zooms on the peak tidal frequency band and shows how the magnitude of the peak at this frequency is entirely suppressed when using a slope of 0.025 (blue dashed line). **f)** Energy in the peak tidal frequency band for the range of slopes tested. The slope that minimises the energy inside the peak tidal frequency band is selected as the best estimate of the beach-face slope.

3 Results

The beach-face slope estimation algorithm described in the previous section was applied to the eight test sites along the transects depicted in Figure S1 (39 transects in total) and compared to *in situ* measurements. The measured beach-face slope at each transect was computed as the average of all the available surveys (calculated from MSL to MHWS), except at Cable Beach where only two known surveys were conducted (Masselink & Pattiaratchi, 2000; Wright et al., 1982). Figure 3a shows a 1:1 plot comparing the satellite-derived beach-face slopes ($\tan\beta_{\text{satellite}}$) to the *in situ* beach-face slopes ($\tan\beta_{\text{in situ}}$). For the *in situ* data (x-axis), a horizontal bar indicates one standard deviation around the average to highlight the degree of temporal variability in beach-face slope observed at each location.

Overall, there is a strong correlation between satellite-derived estimates and *in situ* averages, with a coefficient of determination (R^2) of 0.93 and no systematic under- or over-estimation observed. While the slope estimation algorithm performed very well along the gentle sloping profiles ($\tan\beta_{\text{in situ}} < 0.05$) of Cable Beach, Ensenada and Torrey Pines, as well as along the steeper ($\tan\beta_{\text{in situ}} > 0.12$) profiles at Slapton Sands and Tairua, relatively more scatter is observed at the more intermediate sites (Duck, Moruya/Pedro and Narrabeen). These intermediate sites ($0.5 < \tan\beta_{\text{in situ}} < 0.12$) are also characterised by a larger temporal variability in beach slope as indicated by the width of the standard deviation bars. In terms of accuracy, the standard deviation of the errors was 0.01 with 90% of the errors falling below 0.015.

While this new capability may become highly valuable for a range of applications as it does not rely on any field measurements, there are limitations. Firstly, this method relies on the existence of a measurable tidal excursion signal in the satellite-derived shoreline time-series. Since the horizontal accuracy of the satellite-derived shorelines is $\sim 10\text{m}$, in order to capture the tidal excursion signal, the amplitude of this fluctuation needs to be significantly larger than 10m – e.g., a tidal excursion of 20 m has a signal-to-noise ratio of 2. In turn, the amplitude of the tidal excursion depends on the tidal range and on the angle of the intertidal zone.

To identify the range of tidal regimes and beach-face slopes over which this method is applicable, additional synthetic time-series of shoreline change were generated for a planar beach with specified slope and tidal range (the details on how these time-series were generated are included in Supporting Information S4). Figure 3b summarises the accuracy of the estimated beach-face slopes - i.e., Normalised Mean Absolute Error (MNAE) based on 100 synthetic time-series - as a function of tidal range (TR) and beach-face slope ($\tan\beta$). As anticipated, the

accuracy declines with decreasing tidal range and increasing beach-face slope, as a decrease in the ratio $TR/\tan\beta$ is equivalent to reducing the amplitude of the horizontal tidal excursions. Based on these synthetic data, the errors can be as much as 30% for $TR/\tan\beta$ ratios smaller than 10 (i.e., $TR < 1$ m and $\tan\beta > 0.1$). Consequently, in order to obtain accurate slope estimates, it is recommended that the technique be applied at any site where $TR/\tan\beta$ is larger than 10. This is further emphasised by the fact that every one of the eight test sites, for which the tidal ranges and average *in situ* beach-face slopes are also included in Figure 3b, are situated at locations where $TR/\tan\beta > 10$ (exact ratios reported in Table 1).

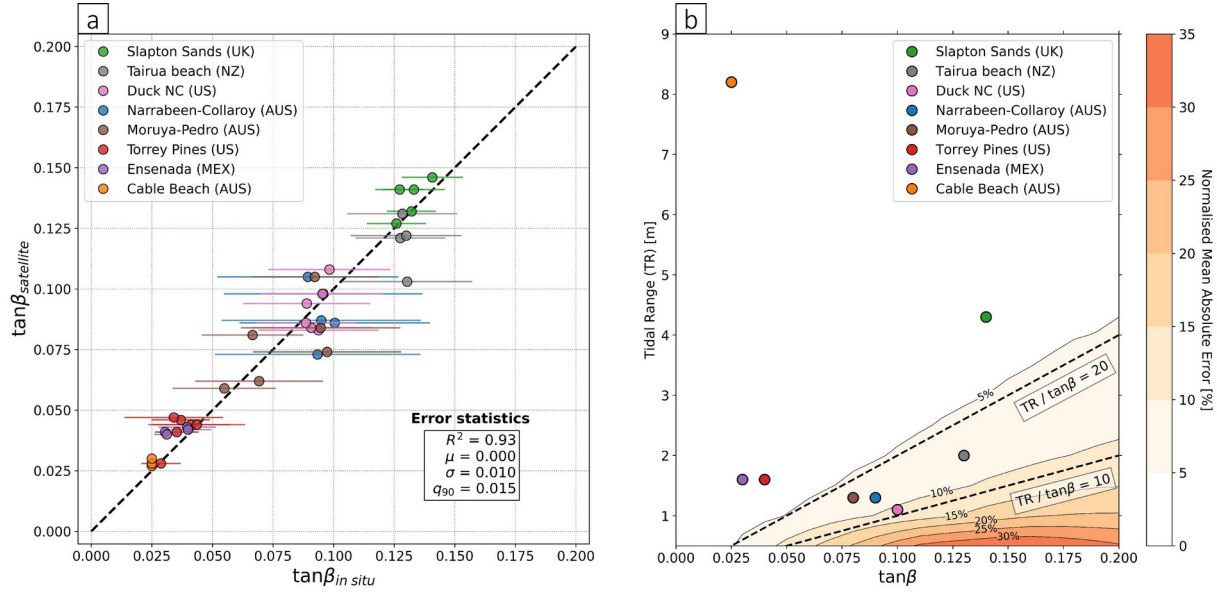


Figure 3. Quantitative assessment of the beach-face slope estimation technique. **a)** 1:1 plot illustrating the comparison between *in situ* measurements of the beach-face slope (x-axis) and satellite-derived estimates (y-axis) at the eight test sites (total of 39 cross-shore transects). The horizontal bars represent one standard deviation from the average *in situ* slope and indicate the degree of temporal variability in beach-face slope at each transect. **b)** Synthetic analysis showing that the accuracy of the method declines with decreasing tidal range to beach-face slope ratio $TR/\tan\beta$. The orange contours represent the Normalised Mean Absolute Error (NMSE) for each combination of tidal range and beach-face slope based on 100 synthetic shoreline time-series (described in Supporting Information S4). The two black dashed lines indicate respectively a ratio of tidal range to beach-face slope of 10 and 20. The dots indicate the tidal range and average beach-face slope at each of the eight test sites.

4 Regional-scale application: Eastern Australia and California USA coastlines

To demonstrate how this technique can be applied over large spatial scales, an example application at the regional scale along two stretches of coastline is presented here: the Eastern Australian coastline (~1800 km) and the California USA coast (~1500km). The methodology described in Section 2 was applied at 100 m alongshore-spaced intervals at sandy beaches along both coasts; in Eastern Australia this resulted in a total of 13,624 beach-face slope estimates; in California 8,147. The results are shown in Figures 4a and 4b and the complete dataset is

available as an interactive web dashboard in the Data Availability section below. The regional-scale distributions of beach-face slopes are depicted in Figure 4c. In both Eastern Australia and California approximately 80% of time-averaged slopes are between 0.04 and 0.08, with the corresponding means of 0.062 (SE Australia) and 0.068 (California).

As a pointer to where the new availability of broad-scale beach slope information may find further application, an empirical relationship between beach-face slope and sediment size D_{50} was recently derived by Bujan et al. (2019) based on 2,144 individual field measurements. This equation can now be employed along the Eastern Australian and Californian coastlines to convert the beach-face slope estimates to the equivalent grain size (D_{50}) and obtain an estimate of the distribution of sediment grain sizes for beaches occurring along the full extent of both regions (see inset in Figure 4c). The detailed analyses of beach-face slope and sediment size distributions at regional scales are outside the scope of this letter, but this example demonstrates the significant potential of this technique to provide beach-face slope estimates as well as sediment size distributions at the global scale.

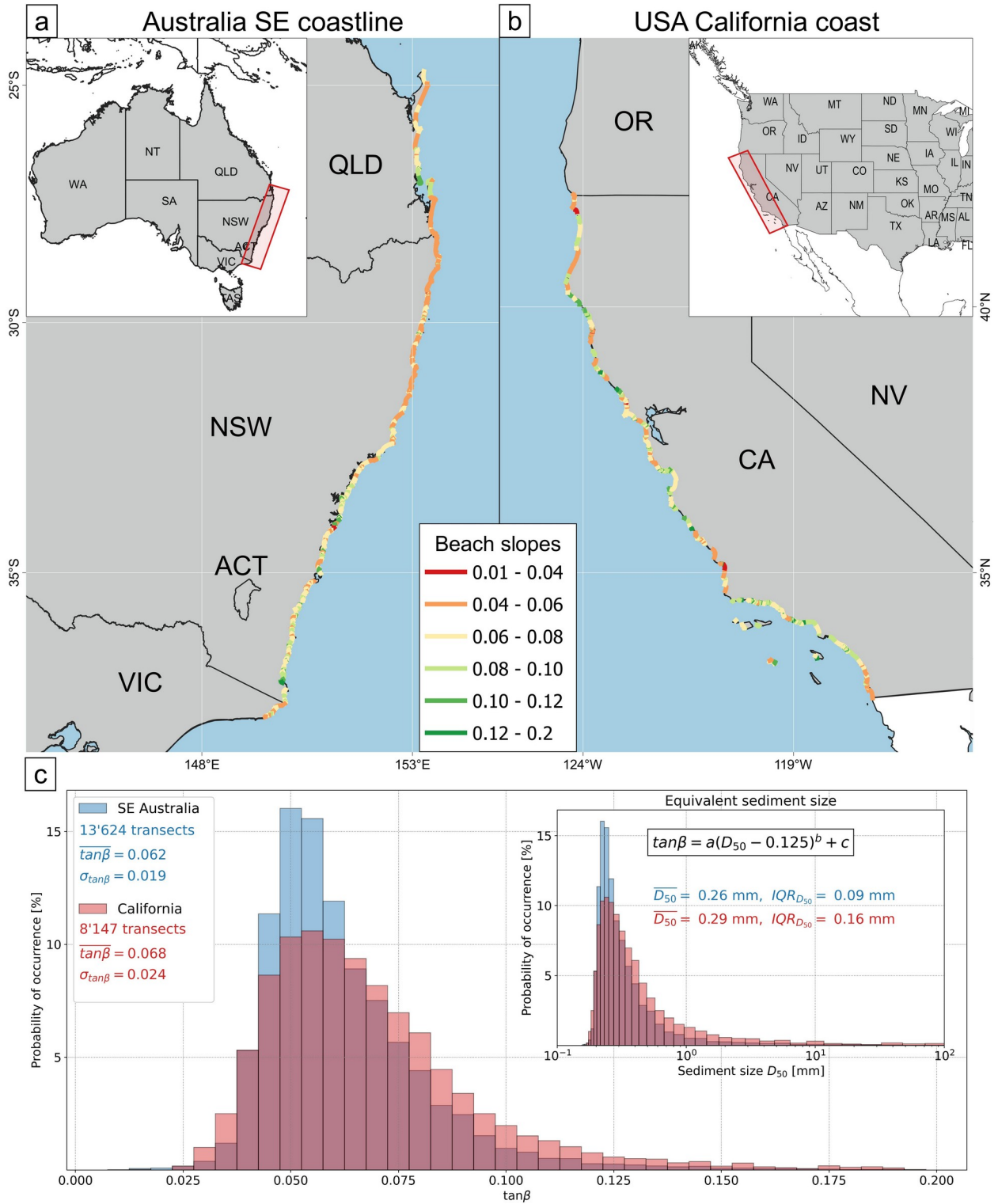


Figure 4. Regional-scale application over SE Australia and California. The mean beach-face slope is 0.062 for SE Australia and 0.068 for California, with both regions showing similar spread around the mean (standard deviations of 0.019 and 0.024 respectively). **a)** Map of beach-face slopes estimated along 13'624 transects on the SE Australian coastline. **b)** Map of beach-face slopes estimated along 8'147 transects on Californian US west coast. **c)** Histogram of the distribution of beach-face slopes along the

two stretches of coastline (SE Australia and California). In the top-right inset the equivalent sediment size distributions are obtained with the empirical relationship from Bujan et al. (2019). The mean D_{50} values are 0.26 and 0.29 mm respectively for SE Australia and California, with an inter-quartile range (IQR) of 0.09 and 0.16 mm.

5 Conclusions

A novel methodology to estimate beach-face slopes from satellite-derived shorelines and modelled tides is described here and evaluated along eight diverse sandy/gravel beaches spanning a broad range of tidal regimes, beach-face slopes and wave climates. This new technique employs a variant of the Fourier transform, the Lomb-Scargle transform, to identify the slope that, when used for tidal correction, minimises the tidal energy in the shoreline time-series.

A comparison with *in situ* (beach survey) topographic data along 39 transects demonstrates that this technique is capable of estimating the time-averaged beach-face slope in different coastal environments ranging from macrotidal, gentle-sloping beaches, to microtidal wave-dominated beaches. Further analysis using synthetic shoreline data reveals that the accuracy of this method declines significantly when the ratio between tidal range and beach-face slope is < 10 .

Finally, an example application spanning a section of the Eastern Australia and California USA coastlines demonstrates the capability of this technique to estimate beach-face slopes over large spatial scales, with the potential to now create and further investigate a global dataset of beach-face slopes. It is anticipated that the future availability of such a dataset will be a key variable to support global studies on the impact of sea level rise and increased storminess along world coastlines.

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Data availability

- The beach-face slope datasets for Eastern Australia and California can be visualised and downloaded on an interactive web dashboard at <http://coastsat.wrl.unsw.edu.au/>.
- The data sets have also been uploaded to the following open-access Zenodo data repository <https://doi.org/10.5281/zenodo.3747130>.
- The codes to estimate beach slopes with this technique are available in a Github repository (<https://github.com/kvos/CoastSat.slope>) uploaded to Zenodo with the following DOI: <https://doi.org/10.5281/zenodo.3872443>.

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