Vertical Land Motion from present-day deglaciation in the wider Arctic

Carsten Ludwigsen^{1,1}, Shfaqat Abbas Khan^{2,2}, Ole Baltazar Andersen^{3,3}, and Ben Marzeion^{4,4}

¹Technical University of Denmark ²DTU Space ³DTU Space, National Space Institute ⁴University of Bremen

November 30, 2022

Abstract

Vertical land motion (VLM) of Earth's surface can aggravate or mitigate ongoing relative sea level change. The near-linear process of Glacial Isostatic Adjustment (GIA) is normally assumed to govern regional VLM. However, present-day deglaciation of primarily the Greenland Ice Sheet causes a significant non-linear elastic uplift of >1 mm yr -1 in most of the wider Arctic. The elastic VLM exceeds GIA at 14 of 42 Arctic GNSS-sites, including sites in non-glaciated areas in the North Sea region and along the east coast of North America. The combined elastic VLM + GIA model is consistent with measured VLM at three-fourth of the GNSS-sites (R=0.74), which outperforms a GIA-only model (R=0.60). Deviations from GNSS-measured VLM, are interpreted as estimates of local circumstances causing VLM. Future accelerated ice loss on Greenland, will increase the significance of elastic uplift for North America and Northern Europe and become important for coastal sea level projections.

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Carsten Ankjær Ludwigsen¹, Shfaqat Abbas Khan¹, Ole Baltazar And ersen¹ and Ben Marzeion²

 $^{1}\mathrm{DTU}$ Space, Technical University of Denmark $^{2}\mathrm{Institute}$ of Geography and MARUM – Center for Marine Environmental Sciences, University of Bremen, Germany

Key Points:

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9	•	Elastic VLM from present-day ice loss in the Arctic causes significant uplift of coast-
10		lines in North America and Northern Europe.
11	•	A combined VLM-model that includes GIA and elastic VLM, yields good agree-
12		ment with GNSS-stations in the wider Arctic.
13	•	Residuals between GNSS and modeled VLM provides an approximation of extraor-
14		dinary VLM caused by local circumstances.

Corresponding author: Carsten Ankjær Ludwigsen, caanlu@space.dtu.dk

15 Abstract

Vertical land motion (VLM) from past and ongoing glacial changes can amplify or mit-16 igate ongoing relative sea level change. We present a high resolution VLM-model for the 17 wider Arctic, that includes both present-day ice loading (PDIL) and glacial isostatic ad-18 justment (GIA). The study shows that the non-linear elastic uplift from PDIL is signif-19 icant (0.5-1 mm y^{-1}) in most of the wider Arctic and exceeds GIA at 15 of 54 Arctic GNSS-20 sites, including sites in non-glaciated areas of the North Sea region and the east coast 21 of North America. Thereby the sea level change from PDIL (1.85 mm y^{-1}) is significantly 22 mitigated from VLM caused by PDIL. The combined VLM-model was consistent with 23 measured VLM at 85% of the GNSS-sites (R=0.77) and outperformed a GIA-only model 24 (R=0.64). Deviations from GNSS-measured VLM can be attributed to local circumstances 25

26 causing VLM.

27 Plain Language Summary

From 2003 to 2015, the Northern Hemisphere lost more than 6,000 gigatons of land 28 ice, which added nearly 18 mm to the global mean sea level rise. Loss of land-based ice 29 results in the vertical deformation of the Earth's surface. Ongoing rebounding or sub-30 sidence caused by the end of the last ice age is often assumed to govern vertical defor-31 mation. However, present-day ice loss from Greenland and Arctic glaciers also cause an 32 immediate vertical deformation. By using an vertical deformation model, that includes 33 both components, we can explain GPS-measured deformation occurring in the Arctic. 34 Our results show that the present-day Arctic ice loss contribution to vertical deforma-35 tion is approximately 0.5 to 1 mm y^{-1} in the wider northern region. This exceeds de-36 formation caused by the disappearance of the last ice ages at many coastal regions, in-37 cluding the North Sea region and the North American Atlantic coast. The Arctic present-38 day ice loss included in the VLM-model equals a global sea level rise of 1.5 mm y^{-1} , which 39 means that 30-80% of the sea level rise caused by Arctic ice loss is mitigated by surface 40 uplift caused by the same ice loss. 41

42 **1** Introduction

The Arctic region is warming faster than any other region on Earth (Post et al., 2019). Deglaciation of Arctic land-based ice accounts for 70% of all barystatic sea level change (Abram et al., 2019) and has increased the sea level rise by 0.035 mm y⁻² over the last three decades (Nerem et al., 2018). From 2003 to 2015 the Greenland Ice Sheet and adjoining glaciers produced 1 cm of sea level rise, while the contribution of other Arctic glaciers was 0.8 cm (Zemp et al., 2019).

⁴⁹ Change in ice loading not only contributes to sea level change, but also alters Earth's ⁵⁰ solid surface, which commonly is called Vertical Land Motion (VLM). Accurate quan-⁵¹ tification of VLM and its causes is key for understanding relative sea level (RSL) (Watson ⁵² et al., 2015; Wöppelmann & Marcos, 2016), which is the sea level change measured by ⁵³ tide gauges (TG).

VLM can be modeled for a given ice loading by employing the sea level equation 54 of Farrell and Clark (1976) or in its elastic adaptation by Clark and Lingle (1977). vis-55 coelastic relaxation of Earth's surface caused by past ice loading changes, also known 56 as Glacial Isostatic Adjustment (GIA), has historically been the most important com-57 ponent of VLM (Farrell & Clark, 1976; Tushingham & Peltier, 1991; Milne & Mitrovica, 58 1998; Peltier et al., 2015) and is often assumed to be the key contributor to VLM in sea 59 level studies from tide gauges (Church & White, 2011; Jevrejeva et al., 2014). This as-60 sumption is in particular inadequate in the Arctic region (Henry et al., 2012), where the 61 change in present-day ice loading (PDIL) is extensive and the corresponding VLM equals 62 GIA in order of magnitude. 63

Here we quantified the VLM resulting from changes in PDIL from 2003-2015 in the
 wider Arctic (the region above 50 deg latitude). After considering GIA, ocean loading,
 rotational feedback (RF) and non-secular geocenter motion, the total VLM uplift is pre dicted and compared to GNSS-measured VLM at 54 locations.

In recent years, data products from the Gravity Recovery And Climate Experiment (GRACE) satellite mission have been used to estimate PDIL and the corresponding VLM (Adhikari et al., 2016; Riva et al., 2017; Frederikse et al., 2019). While this is a reasonable estimate for regional and global VLM-patterns, the native resolution of GRACE is around 300-km half width at the equator (Tapley et al., 2004) which is insufficient for estimating VLM close to glaciers and ice sheets.

Here we combined a high-resolution (2x2 km) ice mass balance data in the Arctic to compute VLM from PDIL (VLM_{PDIL}) , with a resolution that is suitable in both the near- and far-field in the Arctic region.

77 2 Data and Method

The solid-earth response of PDIL is assumed to be purely elastic and the viscoelastic response is considered to be negligible. This includes the ongoing solid-earth response from modern changes in ice loading prior to 2003, which is not considered in the applied GIA-models. In particular, the deglaciation after the Little Ice Age (LIA) that ended in the 19th century can create a GIA-like viscoelastic response that is not captured by GIA-models (Simon et al., 2018).

Contrary to studies using GRACE-measurements for ice loading, we used mass balance data from glaciers (Marzeion et al., 2012; Pfeffer et al., 2014; Zemp et al., 2019) that were transformed into an ice-elevation model (details in Supporting Information S1) with a 2x2 km spatial resolution by applying a mass balance distribution function and assuming a uniform density of 917 kg m⁻³. Glaciers were combined with elevation changes from Greenland (updated version of the data from S. A. Khan et al. (2013), see section 2.1).

Separately, Antarctic yearly mass equivalent surface elevation changes for 2003-2015 from 90 Schröder et al. (2019) were used to estimate the present-day Antarctic contribution to

91 VLM in the Arctic. 92

The elastic VLM (VLM_{PDIL}) was computed with REAR (Regional Elastic Rebound 93 calculator) (Melini et al., 2014, 2015). REAR calculates the elastic response to a disc 94 load (Farrell, 1972) and assumes a solid, non-rotating and isotropic earth. Load Defor-95 mation Constants (LDC's) used for solving the Green's Functions were obtained from 96 the REF6371 model by Kustowski et al. (2007) which is similar to the PREM-model (Dziewonski 97 & Anderson, 1981), however the REF6371 model includes more realistic seismic properties of the crust (Kustowski et al., 2007). The LDC's from REAR are by default de-99 fined with respect to Earth's center of mass (CM-frame), which is consistent with the 100 GIA-model of Caron et al. (2018). The ICE6G_D-model of Peltier et al. (2018) is ref-101 erenced to the center of solid-earth (CE). The surface loading change included in GIA 102 is however prehistoric and current viscoelastic mass transport induces a negligible CM-103 CE motion (King et al., 2012; Argus et al., 2014). 104

Rotational feedback (Milne & Mitrovica, 1998) was added to the elastic VLM-model 105 by using equation 1 and 2 from King and Watson (2014). Position changes of the pole 106 (x_p, y_p) for ITRF2008 are available from IERS (Bizouard & Gambis, 2009). Since REAR 107 is not solving the sea level equation (Farrell & Clark, 1976; Milne et al., 1999), it does 108 not account for the effect of extra water mass added to the oceans because of PDIL, which 109 results in a measurable deformation (van Dam et al., 2012; Santamaría-Gómez & Mémin, 110 2015). Non-tidal ocean loading (NOL) is predicted by estimating the elastic deforma-111 tion of ocean bottom pressure (OBP, shown in Figure S2.2 in Supporting Information) 112 grids from the latest version of Estimating the Circulation and Climate of the Ocean (ECCO) 113 project (version 4, release 4) (Fukumori et al., 2019; Forget et al., 2015). 114

GNSS data are referenced to ITRF2008 (Altamimi et al., 2011), which has secu-115 lar trends in CM, while non-secular trends of ITRF are in center of figure (CF) (Dong 116 et al., 2003). Therefore, when studying ongoing mass changes, we need to make a ITRF 117 to CM translation by considering non-linear geocenter motion (GCM). GCM is obtained 118 from first-order Stokes coefficients from 2002-2019 provided by Sun et al. (2016) avail-119 able from https://grace.jpl.nasa.gov/data/get-data/geocenter/, which are de-120 trended in order to make the ITRF to CM translation. An VLM-model (eq. 2) is cre-121 ated that is comparable to adjusted GNSS-measured VLM (eq. 3): 122

$$VLM_{elg}^{CM} = VLM_{PDIL}^{CM} + VLM_{NOL}^{CM} + VLM_{rot}$$
(1)

$$LM_{model}^{CM} = VLM_{CIA}^{CM} + VLM_{elg}^{CM}$$
⁽²⁾

$$VLM_{ela}^{CM} = VLM_{PDIL}^{CM} + VLM_{NOL}^{CM} + VLM_{rot}$$
(1)

$$VLM_{model}^{CM} = VLM_{GIA}^{CM} + VLM_{ela}^{CM}$$
(2)

$$VLM_{GNSS}^{CM} = VLM_{GNSS}^{ITRF} - GCM^{ITRF-CM}$$
(3)

Where VLM_{ela}^{CM} is the elastic VLM-model, VLM_{GIA}^{CM} represents VLM caused by GIA, VLM_{rot} indicates the deformation caused by rotational feedback and VLM_{NOL} is the 123 124 contribution from NOL. VLM_{GNSS}^{CM} is GNSS-measured VLM after non-secular geocen-125 ter motion is removed. Average VLM-rates from 2003-2015 are shown in Figure 1, while 126 VLM_{model}^{CM} is evaluated against VLM_{GNSS}^{CM} in section 3. The contribution of Antarctic 127 ice loading (including Southern Hemisphere glaciers) is shown together with the contri-128 bution of VLM_{NOL}^{CM} and VLM_{rot} in Figure S2.1 in Supporting Information. 129

Caron2018 (Caron et al., 2018) is the default GIA-model throughout this study. 130 Caron2018 used 128000 forward models of different 1D Earth rheologies and ice eleva-131 tion histories to create a statistical distribution of the GIA signal representative of long 132 term GNSS observations and relative sea level records from paleo RSL indicators. In some 133 parts of the analysis, we include the ICE-6G_D GIA model of Peltier et al. (2018), since large discrepancies between the VLM_{model}^{CM} and VLM_{GNSS}^{CM} can be explained by the choice 134 135

of GIA-model. Recent study using an ensemble of simulations with 3D-earth rheologies (Li et al., 2020), seems to favor the results GIA-rates of Peltier et al. (2018).

Though we limited this study to the wider Arctic area, both the elastic VLM-components and GIA have a global impact. However, if we neglect the VLM caused by Antarctica, the VLM-signal from PDIL is relatively small ($< \pm 0.2 \text{ mm y}^{-1}$) outside the region of this study. The estimated uncertainty of the VLM^{CM}_{model} originates from the standard uncertainty of the ice model combined with a 10% uncertainty that represents the uncertainity from the REF6371 earth model (Wang et al., 2012).

While the ice model of Greenland is well constrained, mass balance errors of in-144 dividual glaciers from the glacial model can be large (several times the glacial signal). 145 We therefore divide the glacial model into 25x25 km tiles, which reduces the uncertainty 146 significantly, but might also introduce unrealistic low uncertainty in areas with large glacial 147 signals or where glaciers are poorly constrained. Glaciers are, however, still the largest 148 source of regional uncertainty (see Supporting Information Figure S3.1.). The Caron2018 149 GIA-model has standard uncertainty estimates included in the product, while there is 150 no uncertainty estimate associated with the ICE6G-model. Uncertainties of geocenter 151 motion from Sun et al. (2016) contributes to the GNSS-uncertainty estimate. The spa-152 tial distribution of the uncertainty estimates are shown in Supporting Information Fig-153 ure S3.1. 154

155 2.1 Ice Loading

The main component of VLM_{PDIL} is the ice loading model and consist of a com-156 bined water equivalent elevation model from Greenland and mass balance estimates from 157 glaciers. Rate of elevation change is shown in Supporting Information Figure S1.1. While 158 only Northern Hemisphere ice history is created with high resolution, changes of Antarc-159 tic and Southern Hemisphere ice loading is computed on a $0.5 \mathrm{x} 0.5^\circ$ grid and included 160 in the computation of VLM_{PDIL}^{CM} . The low resolution does not have any impact on VLM 161 in the Arctic. The total mass loss of the Southern Hemisphere is 140 Gt y^{-1} , equiva-162 lent of to 0.38 mm y^{-1} barystatic sea level rise. 163

2.1.1 Glaciers

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A total of 62,000 individual glaciers from the Randolph Glacier Inventory (RGI 6.0) (Pfeffer et al., 2014; RGI Consortium, 2017) located in North America, Russia, Scandinavia (incl. Svalbard) and Iceland have been included in this study. Mass loss from included glaciers accounts for 95 % of the registered glacial mass loss of the Northern Hemisphere and constitutes 80% of the global glacial mass loss (Zemp et al., 2019).

Mass change estimates for each glacier were estimated using an updated version 170 of a model reported in Marzeion et al. (2012). Direct mass balance observations (Zemp 171 et al., 2019) were used to calibrate and validate the glacier model. The glacier model trans-172 lates information about atmospheric conditions into glacier mass change, while consid-173 ering various feedback mechanisms that occur between glacier mass balance and glacier 174 geometry. Glacial mass balance was combined with a distribution function to calculate 175 glacier-wide surface elevation change. This ensured that the lower parts of glaciers are 176 thinning, while upper parts experience small elevation gains. This 'slope steepening' of 177 glaciers is characteristic of glaciers of many regions (Nuth et al., 2010; Foresta et al., 2016; 178 Ciracì et al., 2018) and is assumed to apply to all glaciers included in this study (see Sup-179 porting Information S1 for an enhanced description of glacial elevation change). 180



bottom three panels. Spatial distribution of uncertainity estimates of (a),(c) and (d) are shown in (d). Enlargements of the south coast of Alaska, Greenland and Svalbard of (d) is shown in the rebound from contemporary land ice loss (including ocean loading and corrected for rotational feedback) (VLM $_{ela}^{CM}$) with enlargement of Svalbard is displayed in (c). The total VLM-model, VLM_{model}^{CM} , (a + c), with the square color representing average GNSS-determined VLM-rates Caron2018(Caron et al., 2018) (a) and ICE6G_D (Peltier et al., 2018) (b). Modeled elastic Average VLM-rates (mm $\rm y^{-1})$ for 2003-2015 using the GIA-model of Supporting Information Figure S3.1. Figure 1.

181 2.1.2 Greenland

Glacial ice history was combined with elevation change of the Greenland Ice Sheet 182 and adjoining glaciers. We estimated the rate of ice volume change from 2003-2015 by 183 using altimeter surveys from NASA's ATM flights (Krabill, 2011) that took place be-184 tween 2003 and 2015 supplemented with high-resolution Ice, Cloud and land Elevation 185 Satellite (ICESat) data (Zwally et al., 2011) from 2003-2009 and CryoSat-2 data from 186 2011-2015 (Helm et al., 2014). Our procedure for deriving ice surface elevation changes 187 has previously been described in detail by S. A. Khan et al. (2013) and is similar to the 188 method used by, e.g. Ewert et al. (2012); Smith et al. (2009) and Kjeldsen et al. (2013). 189 We used the observed ice elevation change rates to interpolate (using collocation) ice el-190 evation changes onto the 2x2 km spatial grid. 191

2.2 GNSS data

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Timeseries of vertical deformation and uncertainty estimates of 54 GNSS-sites from 193 the sixth release of the consortium led by University of La Rochelle (ULR-6) (Santamaría-194 Gómez et al., 2017) were used. A detailed map and timeseries of all GNSS-sites are shown 195 in Supporting Information Figure S4.1 and Figure S5.1. ULR-6 includes 125 GNSS-sites 196 located within the area of interest, but only GNSS-sites with data for at least 120 of 156 197 months from 2003 to 2015 known not to be impacted by human activities were selected. 198 One GNSS site was selected based on lowest observed standard deviation of timeseries 199 when multiple GNSS sites were located within 100 km of each other. Nome (AT11), Es-200 bjerg City (ESBC) and Magadan (MAG0) were exempted from the temporal selection 201 criteria, because of their location which has a special interest for interpretation. 202

Annual averages and combined uncertainties were calculated for each GNSS-site from the vertical component and standard uncertainty included in URL-6a. Hereafter, the linear trend was calculated for the years available between 2003 and 2015.

²⁰⁶ 3 Evaluating the VLM model

From Figure 1 it is seen that the VLM-model is dominated by the pattern of the 207 GIA-model, with rates above 20 mm y^{-1} east of the Hudson Bay and another local max-208 imum of over 15 mm v^{-1} in north-west Canada. The elastic rebound is evident in most 209 of the Arctic, particular in Greenland with large areas exceeding 10 mm y^{-1} , with max-210 imum value at Jakobshavn Isbræ (69.1N, 49.5W) with an average modeled uplift of 40 211 mm y^{-1} . Large areas around Svalbard and Alaska have modeled elastic VLM-rates of 212 more than 8 mm y^{-1} . The uncertainty is significantly larger in glaciated regions than 213 in the far field (see Figure 3.1 in Supporting Information). 214

Most depression zones are found over the ocean, with the Beaufort Sea and Labrador Sea subsiding with 2 mm y^{-1} and the Norwegian Sea with 1.5 mm y^{-1} . Subsiding coastal areas are found in North America, where Nova Scotia and most of the US east- and west coast subsides with more than 1 mm y^{-1} , while smaller subsidence (0.0 - 0.5 mm y^{-1}) is found in Northern Europe along the North Sea and Atlantic coastlines. From Figure 1 we see that most subsiding areas are caused by GIA.

Figure 2 shows that VLM_{model}^{CM} predicts VLM within the range of VLM_{GNSS}^{CM} at 46 of 54 GNSS locations considered. The mean absolute error (MAE) for the 54 GNSS-sites was 1.45 mm y⁻¹ (1.33 mm y⁻¹ for ICE6G_D), which was 0.53 mm y⁻¹ better than MAE from only VLM_{GIA} . For less than half (27) of the 54 GNSS-sites considered was the VLMmodel with Caron2018 outperforming the ICE6G_D GIA model.

Barystatic sea level change for VLM_{PDIL} was 1.5 mm y^{-1} (ice loss-mediated global average sea level change (excl. Antarctica)). As shown in Figure 2, elastic VLM values



Figure 2. Average VLM change (mm y⁻¹) from 2003-2015 determined using the elastic VLM model (blue) and GIA (red) at the 54 GNSS-sites from Figure 1 and Supporting Information Figure S4.1 are shown (top). Sites are listed from most west (left) to most east (right). The dotted-cyan line indicates the average barystatic sea level rise (~ 1.85 mm y⁻¹) from the ice loss used in this study. The total modeled VLM uncertainty are indicated with red error bars and the GNSS-measured VLM is shown with black errorbars. Light red indicates locations in which GIA is negative and overlaps the positive elastic VLM. Residuals between GNSS-measured VLM (VLM^{CM}_{GNSS}) and the VLM-model (VLM^{CM}_{model}) (blue) and GIA (red) are shown (bottom). The average of the absolute residuals (equivalent to mean absolute error) are 1.45 mm y⁻¹ and 1.98 mm y⁻¹ respectively. All values used in this figure are included within Table S4.1 in Supporting Information.

between 0.5-1 mm y^{-1} were observed at many far field GNSS-sites in this study and partly mitigated the barystatic sea level change.

The effect of non-cryospheric mass change is not included in VLM^{CM}_{model}. In particular terrestial water storage (TWS) causes a small uplift over large parts of North America (0.4 - 0.8 mm y⁻¹) and North-Central Siberia (0.2 - 0.4 mm y⁻¹), while TWS is causing a subsidence in most of Scandinavia of 0.2 - 0.4 mm y⁻¹ (Frederikse et al., 2019).

Glaciated regions show particularly large residuals between the predicted VLM and VLM measured by GNSS (Figure 3), but also exhibit the largest associated uncertainties of GNSS estimates. Predicted VLM at 26 of 54 GNSS-sites are within a range of 0.75 mm y⁻¹ to GNSS (the three center bins in the right panel of Figure 3). The VLM-model has a tendency to underestimate the GNSS-measured VLM, which is evident in North America and Europe. From figure 2, we see that a different choice of GIA-model would
yield enhance the accuracy of the VLM-model in these regions. The most significant discrepancies between measured and predicted VLM is explained in the following for every region.

3.1 North America

Alaska is located in the transition zone between GIA-uplift and GIA-subsidence, which is also reflected in the GNSS-rates. Nome (AB11), Prudhoe Bay (PBOC) and Inuvik (INVK) all experience an GIA-subsidence that is larger than the elastic uplift. While Nome and INVK are well matched with VLM_{GNSS}^{CM} , PBUC has the largest measured subsidence ($3.2\pm1.6 \text{ mm y}^{-1}$), while VLM_{model}^{CM} only shows a subsidence of $1.4\pm1.4 \text{ mm y}^{-1}$. An extraordinary subsidence is likely caused by oil extraction in the Prudhoe Bay area.

The Alaska south coast accounts for more than 25% of the total glacial melt and 250 is naturally dominated by elastic uplift while the uplift from GIA is below 1 mm yr^{-1} . 251 Seldovia (SELD) shows an observed average rate of 9.2 ± 1.0 mm yr⁻¹, while VLM^{CM}_{ela} 252 is only 0.3 ± 1.6 mm yr⁻¹ and GIA-rate -0.1 ± 0.8 mm yr⁻¹. Seldovia is located on the 253 Kenai Peninsula close to the Kenai Fjords, which experienced an accelerated glacial ice 254 loss in the 20th century (VanLooy et al., 2006). This is, however, not enough to explain 255 the increased measured uplift. GIA-estimates vary in the region (Larsen et al., 2005; Hu 256 & Freymueller, 2019), but is not more than around 1-2 mm yr^{-1} . The residual seems 257 explained by a postseismic signal following the Prince Willam Sound Earthquake in 1964 258 (Cohen & Freymueller, 2001; Huang et al., 2020) which is still causing a local uplift on 259 this side of the peninsula. The residuals estimates this effect to be 9.0 mm yr^{-1} from 260 2003-2015, which is slightly less than the value found by Cohen and Freymueller (2001) 261 of 9.3 mm yr^{-1} from 1994-2001. This rebound is expected to decay further over time, 262 but will still be relevant for decades to come (Cohen & Freymueller, 2001; Huang et al., 263 2020).264

Discrepancies between GNSS and modeled VLM in central North America, are likely 265 due to uncertain GIA-estimates. A significantly better alignment between VLM_{model}^{CM} and 266 GNSS is reached if Caron2018 is replaced by ICE-6G. The GIA-overestimate of Caron2018 267 in North America has been demonstrated by other studies (Schumacher et al., 2018; Fred-268 erikse et al., 2019) and is likely caused by large differences between estimated viscosity 269 properties of paleo-RSL indicators and GNSS in North America (Caron et al., 2018). TWS-270 change causes a small uplift below 1 mm y^{-1} over large parts of North America (Frederikse 271 et al., 2019), which enhances the difference between VLM_{model}^{CM} and VLM_{GNSS}^{CM} . 272

²⁷³ **3.2 Greenland**

Four GNSS-sites on Greenland and Alert (ALRT) on Baffin Island measure a significant elastic uplift. While Pittuffk/Thule (THU2) and ALRT agree with VLM^{CM}_{model}, Kangerlussuaq (KELY) is overestimated quite a bit and VLM^{CM}_{model} at Kulusuk (KULU) and Qaqortoq (QAQ1) is below VLM^{CM}_{GNSS}. GIA on Greenland is poorly constrained in Caron2018, which can exaggerate VLM-estimates from GIA. A low-viscosity zone stretching from Iceland beneath Southeast Greenland (S. A. Khan et al., 2016) enables a significant viscoelastic rebound caused by ice loss since LIA (S. Khan et al., 2014).

281 **3.3 Iceland**

The two GNSS-sites on Iceland show very different uplift rates of 0.0 ± 1.1 mm yr⁻¹ in Reykjavik (REYK) and 13.1 ± 1.1 mm yr⁻¹ at Hoefn (HOFN) at the southern edge of the largest ice cap on Iceland, Vatnajökull. VLM^{CM}_{model} overestimates the rebound in Reykjavik while it largely underestimates it at Hoefn. Similar to south east Greenland a soft viscoelastic mantle layer (Fleming et al., 2007) creates a present-day viscoelas-



Figure 3. VLM_{GNSS}^{CM} versus VLM_{model}^{CM} including associated uncertainties for all GNSS-sites. If the cross is above the dashed line the VLM_{model}^{CM} underestimate compared to VLM_{GNSS}^{CM} . A histogram of the difference between VLM_{model}^{CM} and VLM_{GNSS}^{CM} (in intervals of 0.5 mm y⁻¹) is shown in the right panel.

tic signal that is much larger than the ones predicted by the GIA-model. A thin crust,
also means that the uplift decreases faster with distance to the glacier (Fleming et al.,
2007; Sørensen et al., 2017), which could explain why Reykjavik shows little vertical deformation despite being less than 100 km from glaciers.

²⁹¹ **3.4 Svalbard**

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The majority of land in Svalbard is covered with ice, and VLM is highly affected 292 by ongoing ice-mass changes. At Ny Ålesund (NYAL), located on the west coast, VLM_{model}^{CM} is dominated by VLM_{ela}^{CM} of $4.6 \pm 5.3 \text{ mm yr}^{-1}$ and VLM_{GIA} of $0.5 \pm 0.4 \text{ mm yr}^{-1}$. In total this is 2.6 mm yr⁻¹ short of observed VLM_{GNSS}^{CM} . While ICE6G and Caron2018 293 294 295 agree within ± 0.2 mm yr⁻¹, more focused, but older studies predict a slightly higher 296 GIA contribution of around 1.5 mm yr⁻¹ (Sato et al., 2006; Kierulf et al., 2009). Also 297 on Svalbard, significant post-LIA deglaciation (Grove, 2001) is likely contributing to an 298 ongoing uplift (Mémin et al., 2014; Rajner, 2018). The effect is still uncertain (Rajner, 299 2018) and Mémin et al. (2014) estimated the post-LIA rebound to be 2-5 mm yr⁻¹ in 300 the beginning of 21st century, which explains the residual of 2.9 mm yr^{-1} . 301

3.5 Northern Europe and Scandinavia

GIA is dominating the vertical deformation in Scandinavia (Figure 1). Even though small glaciers exist in Norway, the elastic effect is very local and has almost negligible effect on the GNSS-sites in this study. However, VLM_{ela}^{CM} is still significant, and improves the correlation with observed VLM_{GNSS}^{CM} compared to a GIA-only model. This becomes more prominent for GNSS-sites in areas, where GIA is less dominant. Esbjerg (ESBC) on the west coast of Denmark is close to the zero-line of Caron2018 (-0.1 mm yr⁻¹), but is still measuring an uplift of about 0.6 mm yr⁻¹, which is partly explained by an elastic uplift of 0.3 mm yr⁻¹.

In Northern Europe, Caron2018 models a subsidence, which is mitigated by an elastic uplift caused by present day ice melt. Generally, VLM_{model}^{CM} is consistent with VLM_{GNSS}^{CM} in the North Sea and the Baltic region, while an VLM-model using ICE6G is at odds at several locations.

3.6 Siberia

Only a few available GNSS measurements exist in eastern Europe and Siberia. Caron2018 is also challenged by limited resources of paleo sea-level records, which makes the GIAmodel more dependent on the existing GNSS-records. It is commonly anticipated that Siberia had little or no ice during the last glacial cycle (Whitehouse et al., 2007), except north central Siberia and in the shallow waters in the Barents Sea between Svalbard and Novaya Zemlya (Root et al., 2015).

Also VLM_{ela}^{CM} is generally smaller than around 1 mm yr⁻¹. While the VLM_{GNSS}^{CM} is within the uncertainty-range of VLM_{model}^{CM} for the Siberian GNSS-sites (Arti (ARTU), Norilsk (NRIL), Tixi (TIXI) and Magadan (MAG0)), a GIA-only model has a better fit to the GNSS measurements which is likely due to increased dependence on GNSS in Caron2018.

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315

4 Discussion and Conclusion

VLM of the wider Arctic region occurs mainly as a result GIA and elastic VLM. 327 Though this study is limited to the area surrounding the Arctic, VLM caused by deglacia-328 tion produces global effects (Riva et al., 2017; Kleinherenbrink et al., 2018; Frederikse 329 et al., 2019). By combining deglaciation that occurred since the last glacial maximum 330 (GIA) and present-day changes in land ice (elastic VLM), the VLM-model provides a 331 realistic estimate of VLM in the Arctic. By evaluating 54 GNSS-sites using a combined 332 VLM-model, we found that measured uplift of GNSS can be explained by either prehis-333 toric or present-day changes in land ice volume. For 46 of the GNSS sites, residuals be-334 tween GNSS-measured VLM values and the VLM-model were smaller than associated 335 uncertainties. 336

The 2x2-km spatial resolution of the used ice-model was much higher than simi-337 lar gravimetric satellite observations from GRACE (Adhikari et al., 2019). Increased spa-338 tial resolution improves VLM predictions accuracy in glaciated regions significantly, as 339 local elastic deformation tends to dominate regional averages observed via GRACE (Frederikse 340 et al., 2019). A VLM-model to GNSS comparison also indicated that the VLM-model 341 was inadequate in some regions due to local causes of VLM that were not included in 342 the VLM-model, such as subsurface properties, past seismic activity or 19–20th century 343 ice-loss (Mémin et al., 2014; Rajner, 2018). 344

In non-glaciated areas, GNSS measurements generally agree well with the VLMmodel. Contour lines shown in Figure 1, indicate that elastic uplift is centered around Greenland, except when close to other glaciated regions (e.g. Alaska and Svalbard), despite the fact that total Arctic glaciers mass loss is comparable with that of Greenland. Hence, the elastic uplift caused by ice melt in Greenland significantly affects the entire wider Arctic region, which includes coastlines of Northern Europe and the North American Atlantic.

Riva et al. (2017) showed that elastic uplift caused by ice loss in Greenland causes a subsidence in the Southern Hemisphere. Similar, it is assumed that Antarctic ice loss will cause a subsidence in the Northern Hemisphere. Antarctic ice loss averaged 105 Gt y^{-1} from 2003-2015 (Schröder et al., 2019), and resulted in an elastic subsidence of less than 0.1 mm y⁻¹ in the Northern Hemisphere. Since ice loss has the potential to occur rapidly in the future (Hay et al., 2017; Edwards et al., 2019), VLM caused by Antarc-

tic ice loss will be increasingly significant, and may be important for future coastal sea level projections in the Northern Hemisphere.

360 Acknowledgments

We wish to thank Lambert Caron, Matt King and one anonymous reviewer for their con-361 structive and helpful comments, which greatly improved the manuscript. Thanks to Danielle 362 Melini (Melini et al., 2014), for creating the REAR-code, which facilitated the creation 363 of the VLM-model. We also greatly appreciate the work of L. Caron (Caron et al., 2018) 364 on the Caron2018 GIA-model available from the NASA JPL website (https://vesl.jpl 365 .nasa.gov/solid-earth/gia/) and R. Peltier on the ICE-6G_D model (Peltier et al., 366 2018). elastic VLM and both GIA-models is available in a Arctic 5x5 km grid at data 367 .dtu.dk/articles/Arctic_Vertical_Land_Motion_5x5_km_/12554489. The project 368 was partially funded by the EU-INTAROS project (Grant agreement no. 727890) and 369 the ESA-Climate Change Initiative Sea level budget closure (Expro RFP/3-14679/16/I-370 NB). 371

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G23437A.1 doi: 10.1130/G23437A.1

Supporting Information for "Vertical Land Motion from Present-Day Deglaciation in the Wider Arctic"

Carsten Ankjær Ludwigsen¹, Shfaqat Abbas Khan¹, Ole Baltazar Andersen¹and Ben Marzeion²

¹DTU Space, Technical University of Denmark ²Institute of Geography and MARUM Center for Marine Environmental Sciences, University of Bremen,

 $\operatorname{Germany}$

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¹⁶ S1 Description of glacier ice model

As initial conditions, we use glacier outlines obtained from RGI6.0 (Pfeffer et al., 2014). The time stamp of these outlines differs between glaciers, but is typically around the year 2000. To obtain results before this time, the model uses an iterative process to find the glacier geometry in the year of initialization (e.g., 1901) that results in the observed glacier geometry in the year of the outlines time stamp (e.g., 2000) after the model was run forward.

The model relies on monthly temperature and precipitation anomalies to calculate the specific mass balance of each glacier. Here, we use the mean of seven different reanalysis products as boundary conditions. Temperature is used to estimate the ablation of glaciers following a temperature-index melt model, and to estimate the solid fraction of total precipitation, which is used to estimate accumulation.

Mass balance data for each glacier is distributed over the glacier according to a mathematical approximation, assuming conservation of mass and that the glacier has a elevation gain at the top which becomes a elevation decline further down the glacier. The altitude where the elevation change goes from positive to negative, E, is approximated by a simple function of the glacial altitude (Z) and the averaged ice height change, ($\bar{h} = \rho b A^{-1}$), and ρ is the ice density (917 kg m⁻³). Note that E is different from the equilibrium line altitude (ELA).

$$\mathbf{E} = (1 - \bar{\mathbf{h}})\tilde{Z} \tag{S1}$$

where \tilde{Z} is the median glacial height. For every glacier we define a distribution function,

D(i), where *i* represents a grid cell of the glacier:

$$D(i) = 1 - \exp\left(\frac{(2-\bar{\mathbf{h}})(\mathbf{E}-Z(i))}{Z_{max}}\right)$$
(S2)

For all glaciers, is the elevation change assumed to be exponentially declining with height, Z(i). The fraction in the exponential term makes sure that glaciers that on average gains

 $\Sigma(i)$. II

Corresponding author: Carsten Ankjær Ludwigsen, caanlu@space.dtu.dk

- ³² up to 2 m height, will have an elevation loss in the bottom of the glacier and elevation
- gain at the top, unless E is equal or to Z_{max} , in which case, the whole glacier will be loosing height.

The elevation change, dh/dt, is found by normalizing D, multiplying with the total mass balance, b, and converted to a height change by dividing with $\rho = 917$ kg m⁻³.

$$\frac{dh(i)}{dt} = -\frac{b}{\rho}\hat{D}(i) \qquad \text{where,} \tag{S3}$$

$$\hat{D}(i) = \frac{D(i)}{\sum_{i=1}^{k} D(i)}$$
(S4)

³⁷ S1.1 Data availability

The ice model is available as a NetCDF-4 file on data.dtu.dk/articles/Arctic JPUCPTical_Land_Motion_5x5_km_/12554489.



Figure S1.1. Ice elevation change from 2003 to 2015 in m yr⁻¹ (red-blue scale) resulting from the redistribution explained above. The most interesting regions (Alaskian Coast, Svalbard (on a wider colorscale), Novaya Zemlja and Iceland) are enlarged. There is no significant ice loss in mainland Siberia. The elevation change is not comparable with actual elevation change, since no model for firm has been applied. The values on the map a proportional with mass changes (assumed density of 917 kg m⁻³)



Figure S1.2. Ice loss from Greenland (including peripheral glaciers) and Arctic glaciers that goes in to the VLM calculations.



Figure S2.1. 2003-2015 average trends of rotational feedback, Non-tidal ocean loading and Antarctic elastic VLM fingerprint $[mm yr^{-1}]$.

40 S2 Influence of rotational feedback, ocean loading and Antarctic ice loss

Rotational feedback is calculated using the eq.1 and eq.2 by King and Watson (2014). 41 Pole positions x_p , y_p used in the calculations are available from https://datacenter 42 .iers.org/eop.php. The Geocenter Motion subtracted from GNSS calculated as de-43 scribed in (Swenson et al., 2008) uses the degree-1 stokes coefficients based on the cal-44 culations by Sun et al. (2016) are available from https://grace.jpl.nasa.gov/data/ 45 get-data/geocenter/. The associated uncertainity of the geocenter motion has been 46 added to the GNSS-error estimate. The elastic VLM effect of Antarctic Ice Loss is es-47 timated from elevation changes by Schröder et al. (2019), which had an average mass 48 loss of 105 Gt yr^{-1} between 2003 and 2015 which agrees well with the result of IMBIE(Shepherd 49 et al., 2018). 50



Figure S2.2. 2003-2015 ocean mass trend [mm/y] from ECCOv4r4 OBP used to estimate the effect of NOL.

51 S3 Spatial distributions of of the VLM-model error



Figure S3.1. Standard deviation (σ) of GIA, elastic VLM and Geocenter Motion and combined for the total VLM-model [mm/yr] for 2003-2015.

52 S4 VLM at GNSS-sites

⁵³ In this section, we explain the VLM measured by GNSS in comparison to the VLM-⁵⁴ model for the regions covered in this study.



Figure S4.1. Location and name (and IGS abbreviation) of the 42 GNSS-sites used in this study ordered from most west to most east. The color indicates the linear trend from 2003-2015 $[mm yr^{-1}]$, while the size of the square is proportional with the standard error (as estimated in the URL6-product).

S5 Timeseries of vertical deformation at all GNSS sites 55

Figure S5.1 shows both measured and modeled vertical deformation from 2003-2015 56 of each individual GNSS-site. It also reflects, how elastic VLM is changing year by year, 57 while GIA is linear. 58

S6 Contribution of elastic VLM and GIA

59



Figure S5.1. Measured and predicted year-to-year VLM-change $[mm y^{-1}]$ from 2003 to 2015 for the 54 GNSS locations. GNSS is shown by the green line and the VLM model by the black line. The red and blue areas indicate the part of the VLM model that is elastic and GIA.

	IGS id	Abbr.	elastic VLM	Caron2018	VLM-model	GNSS VLM	Residual
Nome	4	AB11	-0.4 ± 0.7	-0.8 ± 0.3	-1.1 ± 1.0	-0.1 ± 0.9	-1.0 ± 1.4
Seldovia	517	SELD	0.3 ± 1.6	-0.1 \pm 0.8	0.2 ± 2.4	9.2 ± 1.0	-9.0 ± 2.6
Prudhoe Bay	433	PBOC	0.1 ± 0.9	-1.5 ± 0.5	-1.4 ± 1.4	-3.2 ± 1.6	1.8 ± 2.1
Whitehorse	651	WHIT	1.1 ± 2.6	0.9 ± 1.3	2.0 ± 3.9	2.0 ± 0.8	0.0 ± 4.0
Inuvik	232	INVK	0.3 ± 1.0	-1.7 ± 0.9	-1.4 ± 1.9	-0.8 ± 1.0	-0.6 \pm 2.1
Nanoose	341	NANO	-0.1 \pm 0.6	1.5 ± 2.7	1.5 ± 3.3	1.6 ± 1.0	-0.2 \pm 3.4
Friday Harbor	508	SC02	-0.2 \pm 0.5	1.3 ± 2.6	1.1 ± 3.1	0.4 ± 1.3	0.7 ± 3.4
Whistler	656	WSLR	0.3 ± 0.6	2.5 ± 3.1	2.8 ± 3.8	4.5 ± 1.3	-1.7 ± 4.0
Holman	218	HOLM	0.3 ± 1.0	1.1 ± 0.8	1.4 ± 1.8	3.1 ± 1.1	-1.7 ± 2.1
Yellowknife	664	YELL	0.4 ± 0.8	7.6 ± 1.5	8.0 ± 2.3	6.8 ± 0.8	1.2 ± 2.4
Flin Flon	168	FLIN	0.2 ± 0.6	8.3 ± 1.6	8.4 ± 2.2	3.0 ± 0.9	5.4 ± 2.4
Lac du Bonnet	143	DUBO	0.1 ± 0.5	3.7 ± 1.1	3.8 ± 1.6	1.0 ± 0.9	2.8 ± 1.8
Resolute	477	RESO	1.1 ± 2.2	3.1 ± 0.9	4.2 ± 3.1	6.0 ± 1.2	-1.8 ± 3.3
Churchill	106	CHUR	0.4 ± 0.7	8.4 ± 2.8	8.8 ± 3.5	10.4 ± 0.8	-1.6 ± 3.6
Thule (Pittufik)	583	THU2	5.3 ± 3.3	0.1 ± 2.1	5.4 ± 5.4	6.6 ± 0.9	-1.2 ± 5.5
Schefferville	510	SCH2	0.4 ± 0.6	15.7 ± 2.3	16.1 ± 2.9	11.0 ± 0.7	5.0 ± 3.0
Halifax	211	HLFX	-0.5 ± 0.4	-1.5 ± 0.8	-2.0 ± 1.2	-1.1 ± 1.6	-0.9 \pm 2.0
Alert	27	ALRT	3.4 ± 4.0	4.1 ± 1.5	7.6 ± 5.6	6.6 ± 1.2	1.0 ± 5.7
Nain	340	NAIN	0.4 ± 0.7	4.0 ± 1.0	4.4 ± 1.7	4.6 ± 1.5	-0.2 \pm 2.3
St. Johns	548	STJO	-0.5 ± 0.4	-1.4 ± 0.3	-1.8 ± 0.8	-0.2 ± 0.8	-1.6 ± 1.1
Kangerlussuaq	247	KELY	6.6 ± 2.5	2.9 ± 3.4	9.4 ± 5.8	4.6 ± 1.2	4.8 ± 5.9
Qaqortoq	467	QAQ1	4.1 ± 1.5	-1.7 ± 1.4	2.4 ± 2.8	4.9 ± 0.8	-2.5 ± 3.0
Kulusuk	265	KULU	5.1 ± 1.6	-1.5 ± 1.0	3.6 ± 2.6	7.8 ± 1.0	-4.2 ± 2.8
Reykjavik	479	REYK	1.4 ± 1.4	0.2 ± 1.4	1.6 ± 2.8	-0.0 ± 1.1	1.6 ± 3.1
Hoefn	215	HOFN	1.9 ± 3.9	-0.1 \pm 1.0	1.8 ± 4.9	13.1 ± 1.1	-11.3 ± 5.1
Newlyn (UK)	347	NEWL	0.1 ± 0.4	-1.1 ± 0.2	-0.9 ± 0.6	-0.2 ± 1.3	-0.7 ± 1.4
Guipavas	202	GUIP	0.2 ± 0.3	-1.0 ± 0.2	$\textbf{-0.9}\pm0.6$	-0.4 ± 1.7	-0.4 ± 1.8
Aberdeen	10	ABER	0.4 ± 0.5	-0.5 \pm 0.4	$\textbf{-}0.1\pm0.9$	0.9 ± 1.2	-1.0 ± 1.5
Heauville	206	HEAU	0.1 ± 0.3	-0.8 \pm 0.2	-0.7 ± 0.6	-0.3 ± 1.5	-0.4 ± 1.6
Portsmouth	446	PMTG	0.3 ± 0.4	-0.8 ± 0.3	-0.5 ± 0.6	0.1 ± 1.2	-0.6 ± 1.4
Lowestoft	286	LOWE	0.1 ± 0.4	-0.8 ± 0.5	-0.7 ± 0.9	-0.4 ± 1.8	-0.2 ± 2.0
Dunkerque	134	DGLG	0.2 ± 0.4	-0.7 ± 0.5	-0.6 ± 0.8	-0.3 ± 0.9	-0.3 ± 1.2
West-Terschelling	568	TERS	0.1 ± 0.4	-0.9 ± 0.7	-0.8 ± 1.1	-0.2 ± 0.8	-0.6 ± 1.4
Esbjerg Center	153	ESBC	0.3 ± 0.4	-0.1 ± 0.5	0.2 ± 0.9	0.6 ± 0.8	-0.4 ± 1.2
Hirtshals	210	HIRS	0.4 ± 0.5	2.2 ± 0.8	2.7 ± 1.3	2.8 ± 1.9	-0.1 ± 2.3
Trondheim	596	TRDS	0.8 ± 0.6	4.6 ± 1.1	5.4 ± 1.7	4.3 ± 0.8	1.1 ± 1.9
Oslo	378	OSLS	0.7 ± 0.5	5.0 ± 1.8	5.7 ± 2.3	5.2 ± 0.8	0.5 ± 2.4
Ny Ålesund	370	NYAL	4.6 ± 5.3	0.5 ± 0.4	5.1 ± 5.7	7.9 ± 0.9	-2.9 ± 5.7
Warnemünde	647	WARN	0.6 ± 0.4	-0.1 ± 0.5	0.5 ± 0.9	0.6 ± 0.8	-0.0 ± 1.2
Copenhagen	75	BUDP	0.6 ± 0.4	0.9 ± 0.5	1.6 ± 0.9	1.6 ± 3.7	-0.1 ± 3.8
Maartsbo	306	MAR6	0.8 ± 0.5	7.6 ± 2.4	8.3 ± 2.9	7.8 ± 0.8	0.5 ± 3.0
Visby	639	VIS0	0.8 ± 0.4	3.3 ± 1.1	4.0 ± 1.6	3.3 ± 0.8	0.8 ± 1.8
Tromsø	599	TRO1	0.9 ± 0.8	1.7 ± 0.7	2.5 ± 1.5	3.0 ± 0.8	-0.5 ± 1.7
Olstyn	274	LAMA	0.7 ± 0.4	0.1 ± 0.5	0.8 ± 0.9	-0.0 ± 0.7	0.8 ± 1.2
Skellefteaa	534	SKE0	0.9 ± 0.6	8.5 ± 2.1	9.4 ± 2.7	10.3 ± 7.0	-0.9 ± 7.5
Kiruna	252	KIR0	0.9 ± 0.7	5.2 ± 0.9	6.1 ± 1.6	6.8 ± 0.8	-0.6 ± 1.8
Vaasa	625	VAAS	0.9 ± 0.6	8.3 ± 2.2	9.1 ± 2.7	9.0 ± 0.9	0.1 ± 2.9
Vardoe	630	VARS	0.9 ± 0.8	2.0 ± 0.6	2.9 ± 1.4	3.0 ± 0.9	-0.2 ± 1.7
Poltava	452	POLV	0.7 ± 0.3	-0.4 ± 0.3	0.2 ± 0.5	0.2 ± 1.0	0.0 ± 1.1
Mendeleevo	323	MDVJ	0.8 ± 0.4	-0.7 ± 0.8	0.2 ± 1.2	0.7 ± 1.1	-0.5 ± 1.6
Arti	36	ARTU	0.8 ± 0.3	-0.2 ± 0.2	0.6 ± 0.6	0.7 ± 0.9	-0.1 ± 1.0
Norilsk	360	NRIL	0.9 ± 0.6	1.9 ± 0.2	2.8 ± 0.8	1.8 ± 0.8	1.0 ± 1.2
Tixi	587	TIXI	0.2 ± 0.6	-0.3 ± 0.3	-0.1 ± 0.9	1.0 ± 1.0	-1.1 ± 1.3
Magadan	298	MAG0	-0.2 ± 0.3	-0.2 ± 0.2	-0.4 ± 0.5	-0.3 ± 1.0	-0.1 ± 1.2

Table S4.1. Measured and modelled VLM for each GNSS-site in mm yr^{-1} . VLM-model is the

sum of elastic VLM and GIA VLM.



Figure S6.1. Percentage contribution of GIA-rate and elastic VLM-rate to total VLM-rate (in absolute terms) are shown. Red colors indicate areas in which GIA dominates VLM, while blue colors indicate areas in which elastic VLM is dominant.

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