

SERMeQ model produces realistic retreat of 155 Greenland outlet glaciers

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Abstract

The rate of land ice loss due to iceberg calving is a key source of variability among model projections of 21st century sea-level rise. It is especially challenging to account for mass loss due to iceberg calving in Greenland, where ice drains to the ocean through hundreds of outlet glaciers, many smaller than typical model grid scale. Here, we apply a numerically efficient network flowline model (SERMeQ) forced by surface mass balance to simulate an upper bound on decadal calving retreat of 155 grounded outlet glaciers of the Greenland Ice Sheet—resolving five times as many outlets as was previously possible. We show that the upper bound holds for 91\% of glaciers examined and that simulated changes in terminus position correlate with observed changes. SERMeQ can provide a physically consistent constraint on forward projections of the dynamic mass loss from the Greenland Ice Sheet associated with different climate projections.

Abstract

The rate of land ice loss due to iceberg calving is a key source of variability among model projections of 21st century sea-level rise. It is especially challenging to account for mass loss due to iceberg calving in Greenland, where ice drains to the ocean through hundreds of outlet glaciers, many smaller than typical model grid scale. Here, we apply a numerically efficient network flowline model (SERMeQ) forced by surface mass balance to simulate an upper bound on decadal calving retreat of 155 grounded outlet glaciers of the Greenland Ice Sheet—resolving five times as many outlets as was previously possible. We show that the upper bound holds for 91% of glaciers examined and that simulated changes in terminus position correlate with observed changes. SERMeQ can provide a physically consistent constraint on forward projections of the dynamic mass loss from the Greenland Ice Sheet associated with different climate projections.

1 Introduction

The Greenland Ice Sheet is currently the largest single contributor to global mean sea level rise (van den Broeke et al., 2017). It discharges ice mass to the ocean through three main processes: release of surface meltwater, submarine melting where ice is in contact with the ocean, and the detachment (calving) of icebergs. The ice mass lost to submarine melting has only recently been directly observed (Sutherland et al., 2019) and remains difficult to estimate for the whole ice sheet (Beckmann et al., 2018), but it is clear that enhanced surface melting and calving processes have resulted in increased mass discharge since the late 1990s (van den Broeke et al., 2016; Enderlin et al., 2014; Khan et al., 2014).

Processes that control surface melt are increasingly resolved in regional models (Mottram et al., 2017; Noël et al., 2018). Iceberg calving, by contrast, remains poorly understood, with multiple contradictory parameterizations incorporated into ice sheet/glacier models (Benn, Cowton, et al., 2017; Morlighem et al., 2016; Levermann et al., 2012). Furthermore, iceberg calving can remove mass more rapidly than is possible through melting alone, contributing to rapid tidewater glacier retreat through mechanisms like tidewater glacier instability (Meier & Post, 1987) and the recently-described Marine Ice Cliff Instability (Bassis & Walker, 2012; Pollard et al., 2015).

Simulating discharge from the Greenland Ice Sheet is further complicated by the local factors affecting ice discharge at the nearly 200 outlet glaciers that connect the ice sheet to the ocean (e.g. Catania et al., 2018; Enderlin et al., 2018). For all but the largest outlets, iceberg calving occurs at smaller scales than are captured in continental-scale ice sheet models. Existing estimates of dynamic mass loss from Greenland outlets have come from extrapolating perturbations on the largest outlets (Price et al., 2011; Nick et al., 2013), simulating the sea level contribution from only selected outlets (Choi et al., 2017; Morlighem et al., 2019), or simulating the entire ice sheet at a spatial resolution of 500 m (Aschwanden et al., 2016, 2019) to resolve about 30 of the nearly 200 glaciers that drain the Greenland Ice Sheet.

Despite these achievements, more than 100 outlet glaciers, responsible for $\sim 1/3$ of current Greenland Ice Sheet discharge (Enderlin et al., 2014), are not routinely simulated, and their dynamics cannot necessarily be inferred from the dynamics of larger outlets. Another layer of spatial complexity arises in that many outlet glaciers collect ice from several interacting tributary branches that are themselves also smaller than typical ice sheet model grid scale. The small scale of tributary glacier networks feeding outlets makes them especially challenging to simulate in continental ice sheet models, requiring model resolution of hundreds to tens of meters to adequately resolve.

A more fundamental challenge in projecting mass loss due to calving is the incompatibility of fracture-driven iceberg calving with the assumption of continuum deforma-

tion inherent in most ice sheet models (e.g. Price et al., 2015; Winkelmann et al., 2011; Greve, 2000). Simple empirical parameterizations can relate calving rate to continuous variables, such as proglacial water depth (Brown et al., 1982; Hanson & Hooke, 2000), but may not hold into the future as climate forcing enters a new statistical regime. Physically-based calving laws, such as the fracture field approach developed by Albrecht and Levermann (2012) or von Mises calving law developed for Greenland by Morlighem et al. (2016), often impose an empirically-adjustable calving rate parameter. Recent work has sought to simulate ice failure using continuum damage mechanics, with some success in a variety of case studies (Borstad et al., 2012; Duddu et al., 2013; Krug et al., 2014; Sun et al., 2017; Mercenier et al., 2019). However, at present the evolution of the damage field through a damage production function is also empirical, with multiple tuned parameters that are poorly constrained by laboratory or field measurements (Emetç et al., 2018). Another recent approach couples a granular model that allows true fracture and calving to a finite-element model that solves an approximation to the Stokes equations for viscous deformation, offering a very promising basis for process-scale simulation of fully-dynamic calving (Benn, Åström, et al., 2017). Unfortunately, the coupled approach remains too computationally expensive for century-scale projections. Despite their promise, neither continuum damage models nor granular calving models have been able to reproduce observed multi-annual evolution of calving front positions in Greenland.

Improving projections of 21st-century sea level rise requires models that can (i) reproduce complex patterns of glacier advance and retreat currently observed in Greenland and (ii) efficiently simulate dynamic discharge and iceberg calving from individual outlet glaciers for a spectrum of climate scenarios. To address this, we have developed a simple model to simulate advance, retreat, and dynamic mass loss due to calving on networks of marine-terminating glaciers (Ultee & Bassis, 2016, 2017; Bassis & Ultee, 2019). Our model framework, called SERMeQ, is able to directly simulate decadal-to-century-scale evolution of hundreds of outlet glaciers in response to surface mass balance forcing across multiple climate scenarios. This explicit simulation capability, together with recent observations of more than 200 Greenland outlet glacier termini (Joughin et al., 2015, updated 2017a), makes it possible to evaluate our model’s performance in a wide range of glacier environments. Here, we show that SERMeQ bounds retreat rates, and reproduces patterns of present-day observed changes in terminus position of 155 Greenland outlet glaciers, providing one of the largest validations of any calving parameterization. On the basis of this validation, our model physics can be incorporated into global glacier and ice sheet models to compute a physically-consistent upper constraint on the century-scale glaciological contribution to global sea level rise.

2 Methods

2.1 SERMeQ ice dynamics model

SERMeQ—the Simple Estimator of Retreat Magnitude and ice flux (Q), *sermeq* meaning “glacier” in Greenlandic—is a width-averaged, vertically-integrated model that determines centerline glacier surface elevation corresponding to a given terminus position. The ice dynamics are based on a perfectly-plastic limiting case of a viscoplastic rheology (Nye, 1951; Bassis & Ultee, 2019), with modifications to allow calving at a grounded ice-water interface (Ultee & Bassis, 2016) and interaction between multiple tributary glaciers (Ultee & Bassis, 2017). Our flowline-modeling approach is compatible with other flowline-based models such as the Open Global Glacier Model (Maussion et al., 2019), but SERMeQ focuses specifically on near-terminus dynamics of marine glaciers to simulate the calving process.

Rather than imposing an empirical calving rate, SERMeQ self-consistently calculates the maximum rate of terminus advance or retreat at each time step for a given climate forcing. Terminus position evolves in response to near-terminus stretching, bedrock

115 topography, and changes in catchment-wide surface mass balance as described in Ultee
 116 (2018) and Bassis and Ultee (2019),

$$\frac{dL}{dt} = \frac{\dot{a} - H \frac{\partial U}{\partial x} - U \frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x}}. \quad (1)$$

117 In Equation 1, $H = H(x, t)$ is the ice thickness, $U = U(x, t)$ the ice velocity, $\dot{a} = \dot{a}(x, t)$
 118 the net ice accumulation rate, H_y the thickness at which effective stress within the ice
 119 reaches its yield strength (Equation S1), and all terms are evaluated at the instantaneous
 120 terminus position, $x = L(t)$ (see Supplementary Text S1-2). For a change in terminus
 121 position determined from Equation 1, SERMeQ calculates a new steady-state glacier sur-
 122 face elevation profile and calculates change in glacier volume above buoyancy (Supple-
 123 mentary Figure S1). The latter produces a net contribution to global mean sea level (ex-
 124 ample in Supplementary Text S1, not evaluated in this validation exercise).

125 The only adjustable model parameters are ice temperature T , which is used to calcu-
 126 late the horizontal stretching rate $\partial U / \partial x$ at the terminus, and yield strength τ_y , which
 127 is used to calculate the yield thickness H_y (Supplementary Text S1-S3). Both are ma-
 128 terial quantities that can be independently constrained by laboratory and field measure-
 129 ments. Crucially, we do not tune either of our parameters to match changes in termi-
 130 nus position. Comparison of simulated with observed terminus position thus provides
 131 a completely independent validation.

132 Here, we extend the physical realism and applicability of our model to demonstrate
 133 that it can simulate calving retreat of a wide variety of marine-terminating glaciers. Novel
 134 elements of SERMeQ specific to this application include upstream forcing with surface
 135 mass balance from a regional climate model (Mottram et al., 2018) and the automatic
 136 selection of networks of flowlines with varying width (traced from Joughin et al., 2015,
 137 updated 2017b, see Supplementary Text S5).

138 2.2 Identification of flowline networks

139 We first identified 181 Greenland outlet glaciers that have multiple terminus po-
 140 sitions recorded in Joughin et al. (2015, updated 2017a). For each glacier, we then de-
 141 fined a network of interacting flowlines with spatially variable width by tracing ice sur-
 142 face velocity from Joughin et al. (2015, updated 2017b, and see Supplementary Text S5).
 143 We extracted ice surface and bed elevation from BedMachine version 3 (Morlighem et
 144 al., 2017) and applied a Gaussian filter to produce width-averaged topography. Where
 145 the data suggested the presence of short, transient ice tongues, we removed the floating
 146 portion from consideration and simulated the grounding line as the “terminus”. We re-
 147 moved three glaciers with long, persistent ice tongues, as SERMeQ is unable to simu-
 148 late ice tongue evolution. Thirteen of the 181 outlets had initial termini grounded above
 149 sea level and iceberg calving is thus unlikely to dominate dynamic mass changes there.
 150 We removed those thirteen glaciers from consideration as well. Noisy or missing data that
 151 produced unphysical bed topography caused us to remove ten additional outlets, leav-
 152 ing 155 glaciers for our analysis.

153 For the remaining 155 outlet glaciers, we defined the initial terminus as the grounded-
 154 ice point along our central flowline that lies closest to the centroid of the 2006 terminus
 155 reported in Joughin et al. (2015, updated 2017a). We optimized a single parameter, the
 156 yield strength of ice, to best fit the 2006 observed surface profile, as described in Ultee
 157 and Bassis (2017). We used a best-guess ice temperature T of -10° C for all glaciers.
 158 We then found the catchment-wide, annual mean surface mass balance forcing for each
 159 outlet, \dot{a} in Equation 1, from HIRHAM regional climate model reanalysis (Mottram et
 160 al., 2018; Rae et al., 2012; Lucas-Picher et al., 2012), and simulated resulting changes
 161 between 2006 and 2014 in ice extent (Figures 1-3) and volume above buoyancy (Figure
 162 4 and Supplementary Figure 1). Finally, we compared the simulated changes in termi-

163 nus position with observed changes reported in Joughin et al. (2015, updated 2017a) for
 164 the same period. Because our optimization of τ_y considers only the initial observed sur-
 165 face profile, and the changes in terminus position are an independent response to changes
 166 in surface mass balance, this comparison examines an independent model prediction that
 167 is not tuned to match observations.

168 **2.3 Comparison with observations**

169 We extracted all available terminus position records from (Joughin et al., 2015, up-
 170 dated 2017a) for each year within our simulated period: 2006, 2007, 2009, 2013, and 2014.
 171 Each terminus position record consists of one or more points; records with multiple points
 172 trace across-flow variation in terminus position. We projected all available points from
 173 a given record onto the central flowline of the corresponding glacier network, and we iden-
 174 tified the space between the most seaward and most landward points of that projection
 175 as the “observational range”. We also tracked the change over time in the position of
 176 the terminus centroid projected on the flowline, which we identified as the “observed (terminus-
 177 centroid) retreat rate”. Finally, we compared the simulated retreat rates with the ob-
 178 served terminus-centroid retreat rates (Figure 2) and the simulated terminus positions
 179 with the observational range (Figures 3-4a).

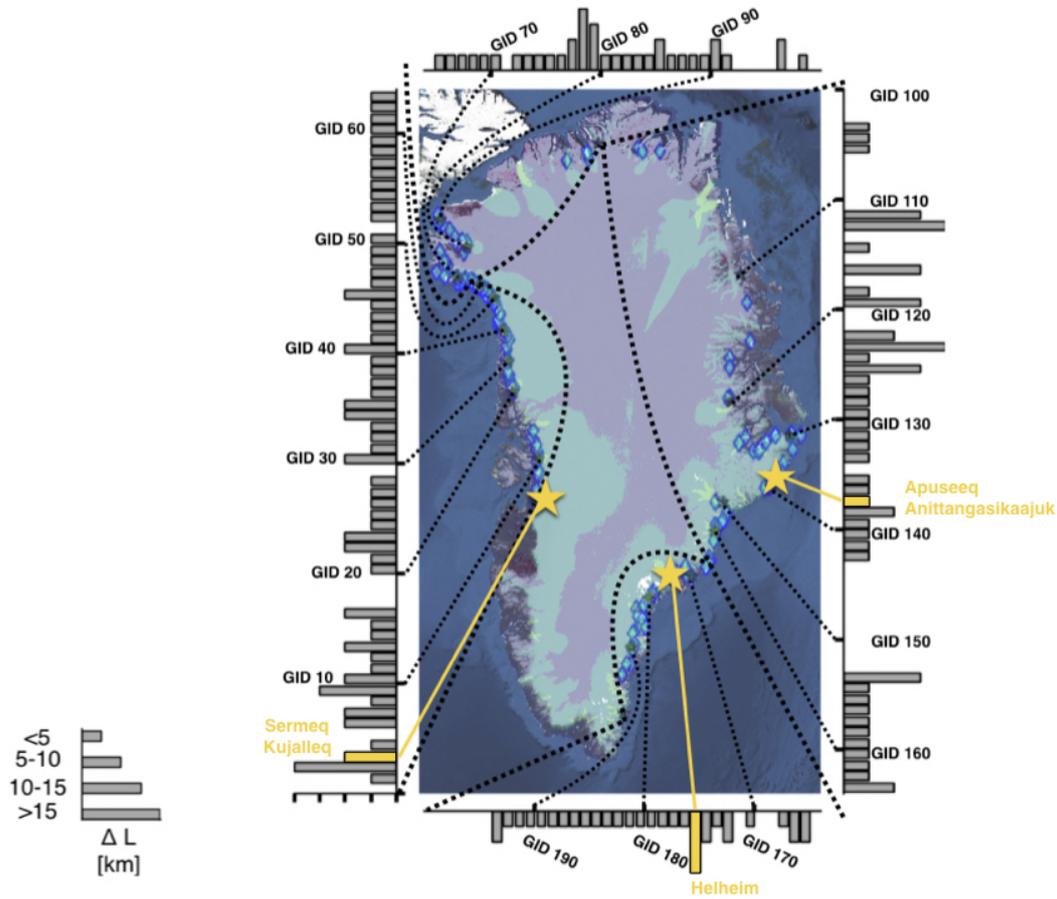
180 **3 Results**

193 **3.1 An upper bound on calving retreat for 155 Greenland outlets**

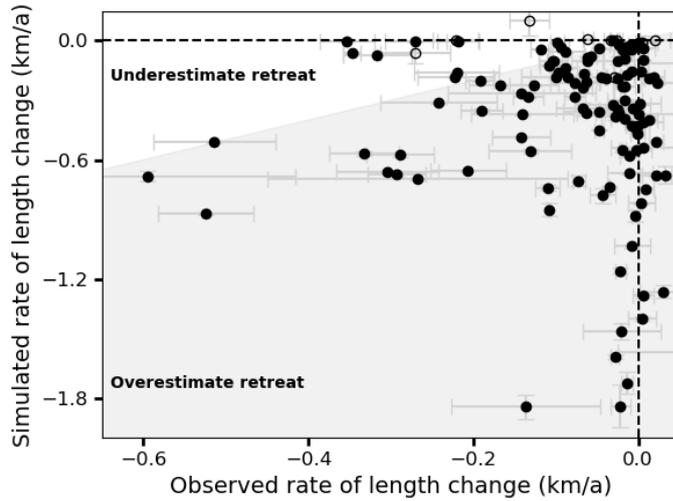
194 Figure 1 shows the total retreat we simulated for each glacier between 2006 and
 195 2014, arranged by approximate outlet position. SERMeQ simulates less than 5 km of
 196 length change during the observed period on most outlets. There is no relationship be-
 197 tween outlet glacier latitude and magnitude of upper-bound retreat: simulated glacier
 198 response to downscaled climate reanalysis forcing is not a simple function of annual av-
 199 erage temperature. Dynamic glacier response depends on glacier geometry, as previous
 200 studies have also highlighted (Felixson et al., 2017; Benn, Cowton, et al., 2017; Catania
 201 et al., 2018).

202 Equation 1 includes an assumption that the glacier calving front is a yield surface,
 203 which produces a theoretical upper bound on calving retreat for a given glacier geom-
 204 etry and surface mass balance (see Bassis & Ultee, 2019). Thus, provided there are no
 205 significant errors in the bed geometry and surface mass balance used, we anticipate that
 206 SERMeQ-simulated rates of retreat will generally overestimate observed rates. Figure
 207 2 shows that SERMeQ satisfies this expectation and overestimates retreat for 91% (108/119)
 208 of glaciers for which more than two terminus position observations are available to con-
 209 strain the observed retreat rate.

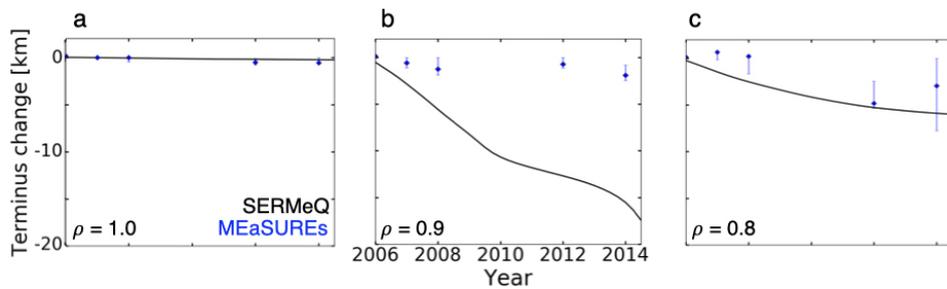
215 The bulk model results shown in Figures 1 and 2 summarize multi-annual change
 216 in terminus position simulated across Greenland. Figure 3 compares observed and sim-
 217 ulated terminus position change for example glaciers where SERMeQ underestimates,
 218 overestimates, or correctly captures the observed rate of retreat. Apuseeq Anittangasikkaa-
 219 juk, which is 2 km wide at the terminus and has a small floating ice tongue, is one of a
 220 handful of outlets where SERMeQ underestimates observed retreat (Fig. 3a). The sim-
 221 ulated terminus positions are still within the (small) observational range in that case.
 222 SERMeQ strongly overestimates retreat of Helheim Glacier, a large and high-flux glacier
 223 on Greenland’s east coast whose terminus approaches flotation (Fig. 3b). On Sermeq Ku-
 224 jalleq (Danish: Jakobshavn Isbræ), a very large and well-studied outlet glacier on the
 225 southwest coast of Greenland, the simulated retreat of 6 km is comparable to observed
 226 retreat (Fig. 3c).



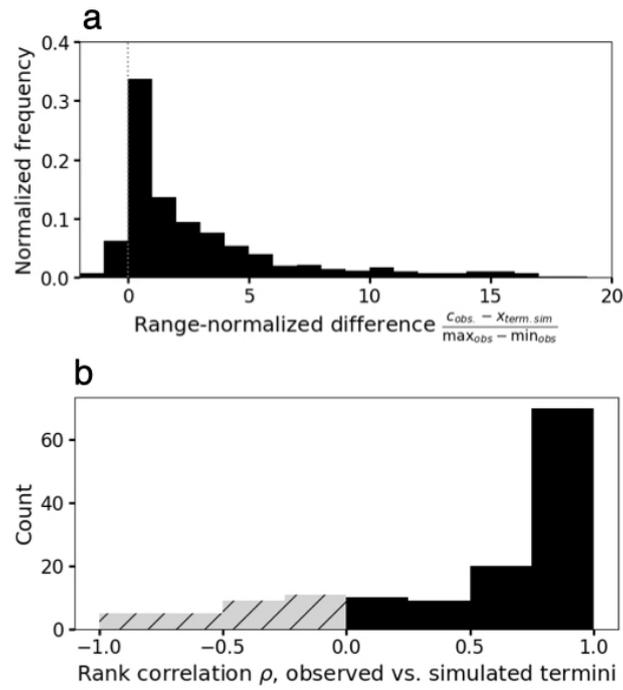
181 **Figure 1.** Map view of the 2006-2014 retreat simulated in this work. Bars indicate magnitude
 182 of simulated retreat for each glacier, with glaciers identified and ordered by their MEASURE
 183 outlet glacier ID number (1-200). Glacier ID 1, which is in the Disko Bay region, appears in the
 184 lower left; glacier IDs increase clockwise around the map border. Blue diamonds mark the map
 185 location of each outlet we simulated, and every 10th glacier ID is labelled and connected to its
 186 outlet location in black. A table of MEASURE glacier IDs and names appears in the Supple-
 187 mentary Material. Border spaces with no bar correspond to outlets where data was not sufficient
 188 to initialize a SERMeQ simulation, or where our analysis indicated SERMeQ would not be ap-
 189 plicable (see Section 2). Yellow bars and map stars show the case-study glaciers highlighted in
 190 Figure 3. Coloured overlay on the satellite map is ice velocity derived from Sentinel-1 observa-
 191 tions (ENVEO, 2017), shown on a logarithmic scale such that fast-moving outlet networks appear
 192 brighter than slow-moving inland ice.



210 **Figure 2.** Comparison of observed and simulated rate of retreat for all glaciers simulated.
 211 Markers indicate the slope of linear fits to the observed (x-axis) and simulated (y-axis) terminus
 212 positions over the 2006-2014 period. Error bars indicate the error on each linear regression. Open
 213 circles indicate oscillating termini that are not well captured by linear regression to simulated
 214 position ($p > 0.05$; $n = 9$).



227 **Figure 3.** Comparisons of observed and simulated terminus position change for (a) Apuseeq
 228 Anittangasikkaajuk (glacier ID 137), where SERMeQ underestimates the true rate of retreat; (b)
 229 Helheim Glacier (glacier ID 175), where SERMeQ overestimates retreat; (c) Sermeq Kujalleq
 230 (glacier ID 3), where SERMeQ captures observed retreat. Black curves indicate SERMeQ-
 231 simulated terminus positions, while blue markers indicate MEaSUREs observations. The blue
 232 lines show the most-advanced and most-retreated parts of the terminus projected onto the cen-
 233 terline, and blue diamonds indicate the centroid of the observed terminus projected onto the
 234 centerline. Lower left corner annotations give Spearman's rank correlation coefficient ρ between
 235 observed and simulated terminus position change for each glacier. Plots share both x- and y-axis
 236 scales.



237 **Figure 4.** Histograms of (a) Range-normalized difference in terminus position, where the sim-
 238 ulated terminus position $x_{term, sim}$ is compared with the centroid of the observed terminus c_{obs}
 239 and normalized by the range of observed terminus positions ($\max_{obs} - \min_{obs}$) along the flow-
 240 line in the same year; and (b) Spearman's rank-correlation coefficient, ρ , between observed and
 241 simulated terminus positions for all glaciers.

242 3.2 Upper bound retreat rates are realistic

243 A useful upper bound on calving retreat would consistently overestimate the rate
 244 of retreat (Figure 2), simulate terminus positions relatively close to observed termini, and
 245 correlate with observed changes. We quantify SERMeQ’s performance on the latter in-
 246 dicators in Figure 4.

247 The histogram in Figure 4a summarizes 404 comparisons of simulated versus ob-
 248 served terminus positions, normalized by each glacier’s observational range for each year,
 249 such that values within ± 1 indicate simulated terminus positions within the observed
 250 range. 40% of simulated terminus positions fall within that range, and 55% of simulated
 251 terminus positions are within twice the range of the observed—that is, the simulations
 252 are relatively close to the observations. Most simulated terminus positions are more re-
 253 treated than the observed (positive x-axis values in Figure 4), as expected for an upper
 254 bound.

255 Because we present an upper bound on retreat rather than a calibrated model fit,
 256 we do not expect a linear relationship between simulated and observed retreat. Instead,
 257 we assess Spearman’s rank correlation coefficient for each glacier’s terminus positions over
 258 time. The coefficient ρ ranges from -1 to 1 , where positive ρ indicates that retreat is
 259 observed when the model simulates retreat, advance is observed when the model sim-
 260 ulates advance, and larger magnitudes of observed and simulated change correspond. Of
 261 the 155 glaciers we simulate, ρ is positive for 103, as shown in Figure 4b. For 62 glaciers
 262 simulated, $\rho \geq 0.5$ and significant at the $p < 0.1$ level, which indicates a moderately
 263 strong and statistically significant relationship between simulated and observed termi-
 264 nus position over time. Only 2 glaciers have negative ρ significant at the same level. The
 265 mean ρ over all 155 glaciers is 0.5.

266 4 Discussion

267 Our simulated upper-bound rate of terminus retreat/advance emerges as a dynamic
 268 glacier response to climate forcing and glacier geometry (Equation 1) and does not rely
 269 on any tuning to match observations. The two model parameters, yield strength of glacier
 270 ice τ_y and ice temperature T , are physical quantities constrained by laboratory and field
 271 observations, and neither is optimized against observed retreat rates. The yield strengths
 272 we use for most Greenland outlet glaciers simulated here range from 50-250 kPa (Sup-
 273 plementary Text S3), well within the range of 50-500 kPa suggested by previous works
 274 (Nimmo, 2004; O’Neel et al., 2005; Cuffey & Paterson, 2010). We use an ice tempera-
 275 ture of -10°C , which is also within the range expected from simple physical scaling (van der
 276 Veen, 2013), observations (Clow et al., 1996), and modeling (Greuell & Konzelmann, 1994).
 277 It is possible an improved match to observed retreat rates could be found if we did al-
 278 low parameters to vary within and between glacier catchments or over time. However,
 279 that would sacrifice the physical upper bound in favor of empirical tuning that cannot
 280 be independently constrained by laboratory or field observations.

281 The upper-bound retreat rate computed from Equation 1 can far exceed the ob-
 282 served rate, as shown in Figures 2 and 3b. There are three notable sources of discrep-
 283 ancy between the modelled and observed retreat rates shown in Figures 2-4: (1) qual-
 284 ity of available model input data, (2) performance of automated flowline selection algo-
 285 rithm, and (3) presence of floating ice. First, on small outlets that are rarely visited or
 286 studied in detail, the bed topography and climate reanalysis data used as input for SER-
 287 MeQ may be poorly constrained. As a result, the simulated glacier evolves in response
 288 to conditions that do not accurately reflect the local environment, and the simulated change
 289 in terminus position is more likely to be inaccurate. Second, on small or slow-moving out-
 290 lets, or where there are gaps in Sentinel-1 velocity data, our method for tracing flowlines
 291 (Text S5) is prone to error. As a result, the simulated glacier has unrealistic geometry

and may flow over bedrock features that are not present in a true central flowline of the outlet. Finally, where floating tongues are present, we remove them and simulate the first grounded grid point as the “terminus”. This can change the near-terminus stress state, in some cases exposing an unstable wall of thick ice and initiating rapid retreat. Effects (1) and (2) are likely responsible for the underestimated retreat of Apuseeq Anittangasikkaajuk; effect (3) is likely responsible for the overestimated retreat of Helheim Glacier (see Supplementary Text S6). The first two effects can be mitigated with improved observational data and manual data processing where possible. The third effect reflects upper-bound retreat dynamics that are currently held in check by floating ice, but which we speculate could be activated if that floating ice were removed.

The 91% satisfaction of the intended upper bound on retreat rate (Figure 2) supports the utility of our model for producing upper bounds on calving retreat and dynamic mass loss. In contrast to existing estimates of 21st-century calving loss, our approach does not impose a uniform calving rate or outlet glacier speedup factor (Pfeffer et al., 2008; Graverson et al., 2011; Goelzer et al., 2013; DeConto & Pollard, 2016; Goelzer et al., 2020, accepted); instead, we calculate a theoretical maximum rate of calving retreat that can vary by glacier (Bassis & Ultee, 2019). The result is a physically consistent bound on terminus position change that correlates with observed changes for most glaciers (Figure 4b). By contrast, simpler bounding methods such as imposing a fixed minimum terminus position would have no relationship ($\rho = 0$) with observed terminus position change. Further, our model can track terminus retreat and mass loss from multiple interacting branches of a glacier tributary network (Ultee & Bassis, 2017; Ultee, 2018), ensuring that potentially important contributions to sea level are not overlooked. Within ice-sheet-scale models, our method could be implemented as a calving criterion at grounded ice-ocean interface cells or used as a module to enhance resolution of outlet glacier networks.

The current version of SERMeQ does not explicitly simulate frontal ablation by submarine melting, which can be a large component of mass loss from both floating tongues and grounded glacier fronts (Rignot et al., 2010; Enderlin & Howat, 2013; Wood et al., 2018). Our derivation of Equation 1, which we emphasise is an upper bound on retreat rate, is consistent with high submarine melt that prevents the glacier terminus from advancing (see Supplementary Text S4 and Ma, 2018; Ma & Bassis, 2019). However, changes in ocean conditions over time can affect glacier terminus dynamics such that the rate of terminus position change becomes closer to or farther from the theoretical maximum. For example, a decrease in submarine melt rate has been implicated in the recent slowing of Sermeq Kujalleq’s retreat (Khazendar et al., 2019). Future implementations of our method in larger-scale models may therefore benefit from modifications to account for time-varying submarine melt rates.

5 Conclusions

We have applied a flowline network model of ice dynamics, SERMeQ, to evaluate an upper bound on annual to decadal-scale calving retreat of 155 Greenland outlet glaciers in response to variable climate forcing. Comparison with nearly a decade of terminus position records from MEaSUREs (Joughin et al., 2015, updated 2017a) shows that the model bounds retreat rate for 91% of glaciers examined, and that 55% of simulated terminus positions are within twice the observed range. SERMeQ can also evolve upstream surface elevation with each change in terminus position and compute the resultant loss of ice mass above buoyancy (Supplementary Text S1; Ultee, 2018). The upper bound on retreat rate that we construct with SERMeQ will produce a corresponding high-end estimate of the loss of grounded ice mass, consistent with efforts to find an upper bound on the ice-dynamics contribution to 21st century sea level rise. Our approach is especially promising in constraining the dynamic sea level contribution from smaller outlet glaciers that are difficult to resolve in larger-scale continental ice sheet models.

Acknowledgments

Data on Greenland outlet glacier terminus position and surface ice velocity comes from the MEaSUREs project (Joughin et al., 2015, updated 2017a, 2010, 2015, updated 2017b), available from the National Snow and Ice Data Center. Surface mass balance forcing comes from the HIRHAM regional climate model for Greenland, maintained by the Danish Meteorological Institute and available from <http://prudence.dmi.dk/data/temp/RUM/HIRHAM/GREENLAND/>. Python code for data processing (inc. network selection), simulation, and analysis is maintained in a public GitHub repository, which can be inspected at <http://github.com/ehultee/plastic-networks>. This work is supported by the DOMINOES project, a component of the International Thwaites Glacier Collaboration, under National Science Foundation grant number AWD005578.

The authors have declared that no conflict of interest exists.

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1 **Supporting Information for**
 2 **“SERMeQ model produces realistic retreat of 155 Greenland out-**
 3 **let glaciers”**

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8 **Contents**

- 9 1. Text S1 to S6
 10 2. Figures S1 to S6

11 **Additional Supporting Information (Files uploaded separately)**

- 12 1. Table S1, a list of all Greenland outlet glaciers in the MEaSUREs dataset with
 13 their glacier ID number, name(s), optimal yield strength found, and notes on
 14 inclusion in the analysis. The note “Flagged for bad flowline trace” indicates
 15 glaciers that required manual intervention to complete data processing, but
 16 which are now included in the analysis.

17 **Introduction**

18 **Text S1. Ice dynamics in SERMeQ**

The ice dynamics in our model are based on a perfectly-plastic limiting case of a viscoplastic rheology (Bassis & Ultee, 2019). This rheology describes a glacier with two characteristic timescales: viscous deformation (slow) and mass loss by calving (fast). Modifications to the simple plastic formulation allow calving at a grounded ice-water interface (Ultee & Bassis, 2016) and interaction between multiple tributary glaciers (Ultee & Bassis, 2017). By requiring instantaneous stress balance across the glacier terminus, this formulation finds that the ice thickness H_{terminus} at a given terminus position, in water of depth D , is limited by the yield strength and cannot exceed the yield thickness,

$$H_y = 2 \frac{\tau_y}{\rho_i g} + \sqrt{\frac{\rho_w}{\rho_i} D^2 + 2 \frac{\tau_y}{\rho_i g}}, \quad (\text{S1})$$

19 with τ_y the yield strength of glacier ice, $\rho_i = 920 \text{ kg m}^{-3}$ the density of glacier ice,
 20 $\rho_w = 1020 \text{ kg m}^{-3}$ the density of seawater, and $g = 9.81 \text{ m s}^{-2}$ the acceleration due
 21 to gravity (Ultee & Bassis, 2016).

In a perfectly plastic glacier (Nye, 1951), the upstream ice thickness H along a central flowline, with along-flow direction x and ice surface elevation s , is also controlled by the yield strength:

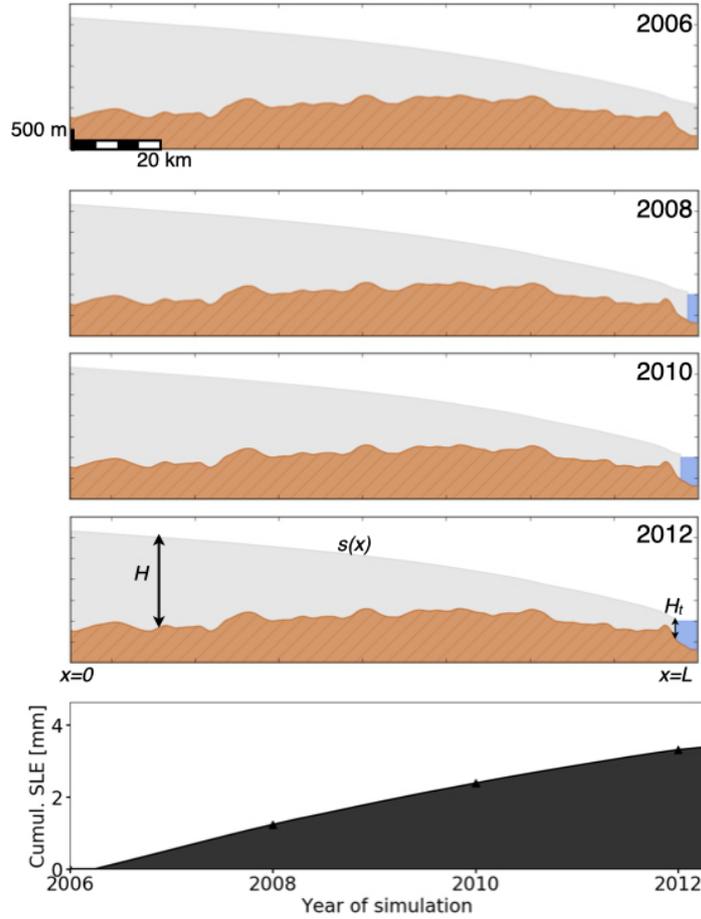
$$H \frac{\partial s}{\partial x} = \frac{\tau_y}{\rho_i g}. \quad (\text{S2})$$

22 This approximation corresponds to a case where the glacier bed is (nearly) plastic
 23 and the glacier stress balance is dominated by shear at the glacier bed and valley
 24 walls—appropriate for most Greenland outlet glaciers. We also account for longitudinal

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25 stresses in a boundary layer near the terminus, where they are more likely to be
 26 important (Bassis & Ultee, 2019).

27 Finally, we use mass continuity to derive an expression for the rate of terminus
 28 advance or retreat due to calving (see Text S2, below). With each change in terminus
 29 position, we calculate a new surface profile according to Equations S1-S2, and we
 30 integrate the changes in ice volume above buoyancy throughout the catchment to
 31 deduce a contribution to global mean sea level. Figure S1 shows an example sequence
 32 of glacier profiles and corresponding sea level contribution as calculated by SERMeQ.



33 **Figure S1.** Surface profiles produced by SERMeQ along a flowline in the central part of Ser-
 34 meq Kujalleq’s catchment, with corresponding cumulative sea level contribution (SLE) below.
 35 Profiles show glacier ice in grey, bedrock in brown, and fjord water in blue. Spatial scale is in-
 36 dicated on the 2006 panel and consistent throughout. Labels on 2012 panel indicate along-flow
 37 direction x , ice surface elevation $s(x)$, ice thickness H , terminus ice thickness H_t , and terminus
 38 location $x=L$ as used in Equations S1-S6. Cumulative SLE on bottom panel reflects catchment-
 39 integrated loss of ice volume above buoyancy converted to an equivalent volume of seawater and
 40 distributed over the area of the global ocean.

41 Despite the simplicity of the model, preliminary experiments have shown promise
 42 in reproducing both surface elevation profiles and advance/retreat rates of glaciers in
 43 Alaska and Greenland (Ultee & Bassis, 2016, 2017). However, our model only applies to
 44 grounded glaciers and cannot simulate the dynamics of floating ice tongues or shelves.

45 **Text S2. Time evolution of the terminus position**

46 Glacier terminus position in SERMeQ evolves in response to near-terminus stretching,
 47 bedrock topography, and changes in catchment-wide surface mass balance as
 48 described in Ultee (2018) and Bassis and Ultee (2019). Below is a brief summary
 49 derivation of the terminus evolution condition as implemented in SERMeQ code.

50 Let $x = 0$ represent the ice divide and $x = L$ the terminus, where $L = L(t)$ is the
 51 length of the glacier (labelled in Figure S1). The time derivative dL/dt then represents
 52 the change in terminus position over time.

Taking the material derivative of the terminus ice thickness $H = H_y$ (constrained
 by Equation S1), we find

$$\begin{aligned} \left. \frac{DH}{Dt} \right|_{x=L} &= \left. \frac{DH_y}{Dt} \right|_{x=L} \\ \left[\frac{\partial H}{\partial t} + \frac{dL}{dt} \frac{\partial H}{\partial x} \right]_{x=L} &= \frac{\partial H_y}{\partial t} + \frac{dL}{dt} \frac{\partial H_y}{\partial x} \\ \left. \frac{\partial H}{\partial t} \right|_{x=L} &= \frac{dL}{dt} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \right]_{x=L}. \end{aligned} \quad (\text{S3})$$

Mass continuity requires

$$\frac{\partial H}{\partial t} + \frac{\partial}{\partial x}(HU) = \dot{a} \quad (\text{S4})$$

53 where $H = H(x, t)$ is the ice thickness, $U = U(x, t)$ the ice velocity, and $\dot{a} = \dot{a}(x, t)$
 54 the net ice accumulation rate, for all (x, t) .

Substituting equation (S4) into (S3), we find

$$\dot{a} - H \frac{\partial U}{\partial x} - U \frac{\partial H}{\partial x} = \frac{dL}{dt} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \right]_{x=L} \quad (\text{S5})$$

$$\frac{dL}{dt} = \frac{\dot{a} - H \frac{\partial U}{\partial x} - U \frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x}}, \quad (\text{S6})$$

55 with all terms of equation (S6) evaluated at $x = L$, the terminus of the glacier (compare
 56 with Equation 54 of Bassis and Ultee (2019)). With the exception of ice accumulation
 57 rate \dot{a} , all terms are determined by the rheology of ice.

Upstream from the terminus, we assume a plastic yielding layer at the bed of the
 glacier. A perfectly plastic glacier would have a rigid ice plug above the yielding layer,
 but the perfect plastic approximation is a limiting case of several other rheologies that
 could be used to describe the slow deformation of ice in a pseudo-plug (e.g. Balmforth
 et al., 2006). Here we choose to describe the slow deformation of intact ice with
 the familiar Glen’s flow law. At the terminus, as in Ultee and Bassis (2016, 2017),
 we require a vertical yield surface to describe the more rapid motion of fractured,
 disarticulated ice as it calves away from the intact glacier. This implies that the
 effective stress in a region of length δ upstream from the terminus is within ϵ of the
 yield strength τ_y . Near the terminus, we have

$$\begin{aligned} \frac{\partial U}{\partial x} &= \dot{\epsilon}_{xx} = A\tau_{xx}^n \\ &= A\tau_y^n, \end{aligned} \quad (\text{S7})$$

58 where flow law exponent $n = 3$ and A is the flow rate parameter of Glen’s flow law.

We integrate equation (S4) in x to find

$$\int_0^L \frac{\partial H}{\partial t} dx + (HU)|_{x=L} = \int_0^L \dot{a} dx \quad (\text{S8})$$

$$U(x=L) = \frac{1}{H_{\text{terminus}}} \int_0^L \left[\dot{a} - \frac{\partial H}{\partial t} \right] dx, \quad (\text{S9})$$

and by the chain rule $\frac{\partial H}{\partial t} = \frac{\partial H}{\partial L} \frac{dL}{dt}$. Separating the integral in equation (S9) and expanding $\frac{\partial H}{\partial t}$ gives

$$U(x=L) = \frac{\dot{\alpha}L}{H_{\text{terminus}}} - \frac{dL}{dt} \frac{1}{H_{\text{terminus}}} \int_0^L \frac{\partial H}{\partial L} dx, \quad (\text{S10})$$

59 where $\dot{\alpha} = \frac{1}{L} \int_0^L \dot{a} dx$ is the spatially-averaged ice accumulation rate along the flowline.

We now substitute our expressions (S7, S10) in to equation (S4) and rearrange to find

$$\frac{dL}{dt} = \frac{\dot{a} - A\tau_y^3 H_{\text{terminus}} + \frac{\dot{\alpha}L}{H_{\text{terminus}}} \frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \left(1 - \frac{1}{H_{\text{terminus}}} \int_0^L \frac{\partial H}{\partial L} \right)}. \quad (\text{S11})$$

60 We implement a discretized version of Equation S11 to describe the time evolution
61 of glacier terminus position in SERMeQ.

62 **Text S3. The role of adjustable parameters**

63 **Yield strength τ_y**

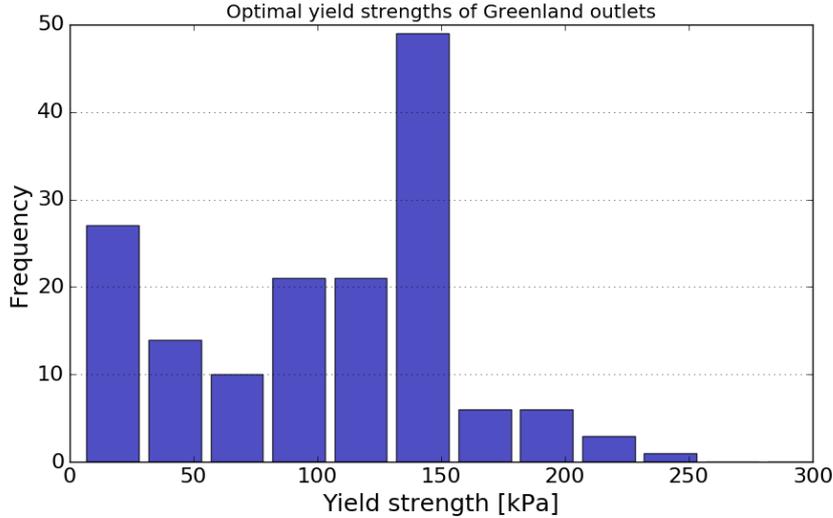
64 For each glacier, we optimize the yield strength τ_y to find the best fit between
65 a reconstructed and observed centerline surface elevation profile. Glaciers with flat-
66 ter surface slopes, including those close to flotation, are best fit by lower values of
67 τ_y . Steeper surface slopes are better fit by higher values of the yield strength. The
68 optimization procedure is discussed in more detail in Ultee and Bassis (2016). The
69 optimal value of τ_y found for each glacier is listed in Supplementary Table 1. There
70 is no correlation between optimal yield strength and glacier latitude, and no other
71 spatial pattern is evident.

72 Figure S2 shows a histogram of the best-fit values of τ_y obtained for the Greenland
73 outlets we simulated. A central peak in the distribution shows that approximately 1/3
74 of the glaciers we simulate have an optimal yield strength between 125 kPa and 150
75 kPa. A smaller peak shows that there are also several glaciers in our set best fit by
76 yield strengths between 5 kPa-25 kPa.
77

78 In this work, we have used a single value of τ_y at both the ice-bed interface
79 and the calving front. It is plausible that the ice-bed interface could be deforming
80 more readily than the pure ice at the calving front, for example if the glacier bed is
81 composed of saturated marine sediments or if the ice is very close to flotation. Such a
82 case would lead to low ice surface slopes and a low optimal value of τ_y , even though
83 pure ice throughout the glacier may be stronger. We discuss the case of $\tau_{\text{bed}} < \tau_{\text{ice}}$ in
84 Bassis and Ultee (2019).

85 **Ice temperature T**

86 The ice temperature T is used to select an appropriate value of the flow-rate
87 parameter A in Glen's flow law. Here, we use an ice temperature constant in space
88 and time and do not optimize for its value. In our previous work, we have found that
89 warmer ice ($T = -2^\circ \text{C}$) is softer and more prone to rapid retreat. Conversely, colder
90 ice ($T = -30^\circ \text{C}$) is stiffer and retreats more slowly. For more details, we refer the
91 interested reader to Ultee (2018).



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Figure S2. Histogram of optimal yield strength value found for each glacier.

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Text S4. Inclusion of submarine melt

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We do not explicitly simulate loss of ice from glacier termini by submarine melting. Rather, we have constructed an upper-bound estimate of retreat that is consistent with high submarine melt rates. Our requirement that effective stress near the glacier terminus must equal the yield strength of ice (see Text S1) makes an implicit constraint on the submarine melt rate, because the rate of submarine melt shapes the stress field near glacier termini (Ma, 2018; Ma & Bassis, 2019). There are three cases to consider:

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Case I The submarine melt rate is very small compared with the terminus velocity, $u_s \ll u_t$. In this case, the terminus would be able to advance and thin episodically. However, advance and thinning would lower the effective stress at the glacier terminus, such that it would fall below the yield strength of ice and no longer satisfy our criterion. We therefore disallow Case I.

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Case II The submarine melt rate is comparable to the terminus velocity, $u_s \sim u_t$. In this case submarine melt would balance the tendency of ice near the terminus to stretch and thin, maintaining the terminus ice thickness at the yield thickness.

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Case III The submarine melt rate is very large compared with the terminus velocity, $u_s \gg u_t$. In this case, the erosion of the terminus by high submarine melt would create an overhang and promote calving (Ma & Bassis, 2019). Considered at long enough time scales, e.g. the 0.25 annum standard time step in SERMeQ rather than the hours to days considered in finer-scale process models, high submarine melting and enhanced calving would also maintain the terminus ice thickness at the yield thickness.

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Both Cases II and III are consistent with our assumption that there is a yielding boundary layer at the glacier front that constrains the terminus ice thickness (see Bassis & Ultee, 2019). The maximum rate of length change computed in Equation 1 is compatible with both cases, and the ice mass lost in each time step can be considered a combination of mass lost to calving and to submarine melting.

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The upper-bound retreat rate that we have sought in this work does not require explicit simulation of the submarine melt rate. Nevertheless, future adaptations of



136 **Figure S3.** Network of flowlines on Kangerlussuaq Glacier, MEaSUREs Glacier ID 153, as
 137 defined with our tracing and filtering algorithm.

121 our method to simulate calving in larger-scale models may seek to add a mechanism
 122 for forcing by time-varying submarine melt. We suggest that those efforts begin by
 123 allowing submarine melt rate u_s to modify the terminus velocity, U in Equation 1,
 124 with the understanding that doing so may introduce scenarios that are incompatible
 125 with our original assumptions.

126 **Text S5. Flowline network selection**

127 We apply our depth-integrated, width-averaged model on a network of interacting
 128 glacier flowlines, as described in Ultee and Bassis (2017). Previous applications have
 129 used flowlines selected by hand (Ultee & Bassis, 2016; Ultee, 2018) or by an automated
 130 method that detects valley walls of mountain glacier networks (Kienholz et al., 2014;
 131 Ultee & Bassis, 2017). Neither method is suitable for the hundreds of Greenland
 132 outlet glaciers we consider here. It is impractical to select hundreds of flowlines by
 133 hand, and outlets of the Greenland Ice Sheet, unlike mountain glaciers, expand to a
 134 nearly featureless catchment upstream with no valley walls to aid in flowline selection.
 135 We therefore apply a new selection algorithm based on tracing ice surface velocity.

138 We begin with a surface velocity composite covering the entire ice sheet (ENVEO,
 139 2017). For each glacier included in the MEaSUREs dataset (Joughin et al., 2015, up-
 140 dated 2017), we extract all points observed along the 2006 terminus position. We then
 141 trace each point up the surface velocity field until a pre-determined minimum velocity
 142 cutoff (identical for all glaciers); our viscoplastic approximation is most suitable near
 143 the glacier terminus (Ultee & Bassis, 2017; Bassis & Ultee, 2019), so we do not extend
 144 our simulated catchments all the way to the ice divide. Finally, we filter the set of
 145 full-length flowlines so that the most central flowline is defined as the “main trunk”.
 146 The parallel portions of the remaining flowlines are trimmed and network intersec-
 147 tions defined where the angle between flowlines exceeds a threshold value (identical
 148 for all glaciers). The code used in network selection is available in our public GitHub
 149 repository, and an example network is shown in Figure S3.

150 The tracing and filtering of flowlines from surface velocity is prone to error where
 151 the velocity dataset is noisy or includes holes. Errors in flowline tracing generally
 152 become apparent in later data-processing steps, for example if no optimal yield strength

153 value can be found. Networks affected by such errors include the note “Flagged for
154 bad flowline trace” in Table S1.

155 **Text S6. Detailed case studies**

156 As described in the main article text, 40% of terminus positions simulated by
157 SERMeQ fall within the range of observed terminus position for the same year. Be-
158 cause SERMeQ is sensitive to bed topography features (Ultee, 2018) and is forced by
159 climate reanalysis data, model performance will generally be best where those data
160 products are most accurate. The agreement between modelled and observed retreat
161 of Sermeq Kujalleq (glacier ID 3, also called Jakobshavn Isbræ, main text Figure 3c),
162 where bed topography has been especially well examined by previous glaciological
163 studies, illustrates this point.

164 It is our aim to produce an upper bound on outlet glacier retreat and associated
165 mass loss. We demonstrated in Bassis and Ultee (2019) that Equation 1 is a theoretical
166 bound on the rate of calving retreat. Thus, we anticipate that the rate of retreat
167 simulated by SERMeQ will generally exceed the observed rate of retreat. To support
168 future implementation of this calving-rate bound in our model or others, it is important
169 to understand where it does not perform as expected. There are two cases to consider:
170 (1) the retreat rate simulated by SERMeQ is slower than the rate observed, or (2) the
171 retreat rate simulated by SERMeQ far exceeds the rate observed (by a factor of 5 or
172 more). We describe three illustrative examples here.

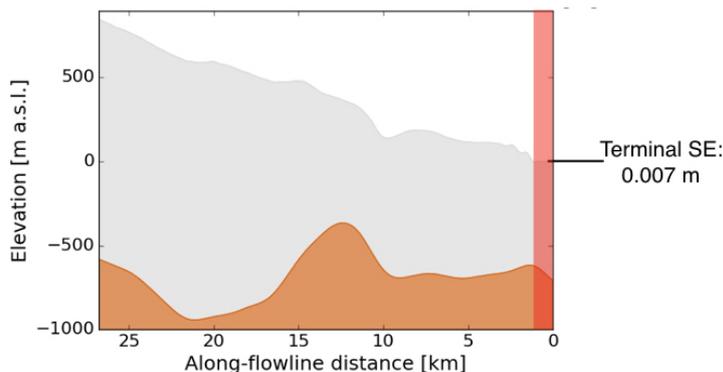
173 **Mean simulated retreat slower than observed**

174 Main text Figure 3a shows the simulated and observed changes in length for
175 Apuseeq Anittangasikkaajuk (MEaSURES Glacier ID 137), a small outlet glacier on
176 the east coast of Greenland. Our analysis shows that the mean rate of simulated
177 (single point) terminus retreat was 31 m/a, while the mean observed rate of retreat
178 of the terminus centroid was 87 m/a. This is one of only a handful of cases in which
179 the mean observed rate over the 2006-2014 period exceeds the supposed upper-bound
180 rate produced by Equation 1. However, in this case both rates are small, and the
181 simulated terminus position remains within the observed range of terminus positions.
182 We also note that Apuseeq Anittangasikkaajuk is seldom included in other studies of
183 Greenland outlets; as such, the quality of bed topography and climate data for this
184 outlet may be relatively lower.

185 **Mean simulated rate far exceeds observed**

186 Main text Figure 3b shows the simulated and observed changes in length for Hel-
187 heim Glacier (MEaSURES Glacier ID 175), a large and well-studied outlet in southeast
188 Greenland. The data quality for this outlet should be comparatively high. Neverthe-
189 less, SERMeQ simulates a mean retreat rate of 1980 m/a, which far exceeds the mean
190 observed retreat rate of 313 m/a. We attribute this rapid retreat to features in the
191 bed topography, combined with the no-flotation condition we have implemented in
192 SERMeQ.

193 The terminus of Helheim Glacier has been observed to float in some years, and
194 was likely floating at the beginning of our simulation period according to bed and
195 surface topography from Morlighem et al. (2017). The glacier bed is more than 600
196 m below sea level and retrograde for several kilometers upstream of the present ter-
197 minus, as shown in Figure S4. As explained in main text section 2 and in Ultee and
198 Bassis (2016, 2017), SERMeQ does not allow floating ice tongues to form. Where
199 small tongues are present, we remove them and simulate the first grounded point as
200 the “terminus”. In the case of Helheim Glacier, when we removed floating ice, the



206 **Figure S4.** Near-terminus bed topography of Helheim Glacier. Brown filled region shows
 207 glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017). Note 10:1
 208 exaggeration in vertical scale. A red overlay indicates floating ice that was removed in our simu-
 209 lation. Annotation at figure left indicates the ice surface elevation at the terminus as recorded in
 210 Morlighem et al. (2017), further evidence that the initial terminus could not have been grounded
 211 ice.

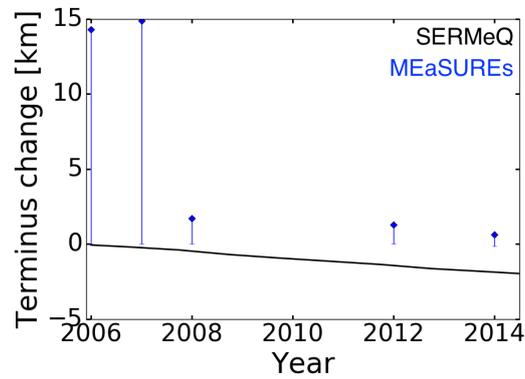
201 simulated terminus was pushed onto the retrograde bed, where it began an unstable
 202 retreat. In summary, the true near-terminus dynamics and stress field of Helheim
 203 Glacier are shaped by the presence of floating ice that interacts with the fjord walls.
 204 SERMeQ does not include these dynamics and therefore simulates an upper-bound
 205 retreat that could occur in the absence of floating ice.

212 Successive under- and over-estimates within observed period

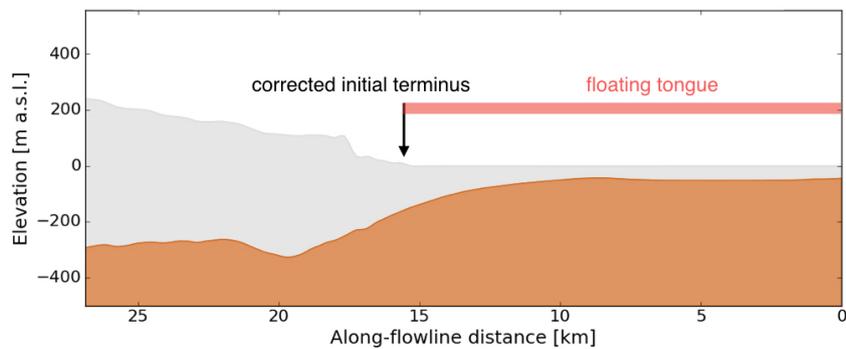
213 In a handful of other cases, the rate of retreat observed during a short period
 214 exceeds the rate simulated during the same period. Underestimated retreat in one
 215 time period is nearly always coupled with overestimated retreat in another period,
 216 such that the aggregate effect over the course of the simulation remains an upper-
 217 bound estimate of net retreat. For example, between 2007 and 2008, the floating ice
 218 tongue of Hagen Brae (MEaSURES Glacier ID 105) disintegrated (Solgaard et al.,
 219 2020). The resulting observed rate of retreat, more than 10 km/a, far exceeded the
 220 rate simulated by SERMeQ (< 1 km/a) over the same period (Figure S4). However,
 221 our model initialization had already removed the floating portion of the glacier as
 222 of 2006, so the SERMeQ-simulated terminus position was still more retreated than
 223 the observed. In the subsequent period between 2008 and 2012, SERMeQ slightly
 224 overestimated the observed retreat rate. Figure S5 illustrates this history. In Figure
 225 S6, we have annotated the floating ice removed upon initialization, the collapse of
 226 which was responsible for anomalously high observed retreat between 2007 and 2008.

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227 **Figure S5.** Observed and simulated change in terminus position on Hagen Brae (glacier ID
 228 105). Black curves indicate SERMeQ-simulated terminus positions, while blue markers indicate
 229 MEaSUREs observations. The blue lines show the most-advanced and most-retreated parts of the
 230 terminus projected onto the centerline, and blue diamonds indicate the centroid of the observed
 231 terminus projected onto the centerline. Positive y-axis values indicate terminus positions more
 232 advanced than the initial position; negative y-axis values indicate terminus positions retreated
 233 from the initial position.



234 **Figure S6.** Near-terminus bed topography of Hagen Brae (glacier ID 105). Brown filled re-
 235 gion shows glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017).
 236 Note 10:1 exaggeration in vertical scale. A red bar shows the length of floating ice that was re-
 237 moved during our model initialization, and a black arrow indicates the first grounded point where
 238 SERMeQ could establish an initial terminus.

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