Upper Mantle Seismic Anisotropy as a Constraint for Mantle Flow and Continental Dynamics of the North American Plate

Wanying $Wang^{1,1}$ and Thorsten Becker^{1,1}

¹The University of Texas at Austin

November 30, 2022

Abstract

The alignment of intrinsically anisotropic olivine crystals under convection is typically invoked as the cause of the bulk of seismic anisotropy inferred from shear-wave splitting (SWS). This provides a means of constraining the interplay between continental dynamics and the deep mantle, in particular for densely instrumented regions such as North America after USArray. There, a comparison of "fast orientations" from SWS with absolute plate motions (APM) suggests that anisotropy is mainly controlled by plate motions. However, large regional misfits and the limited realism of the APM model motivate us to further explore SWS based anisotropy. If SWS is estimated from olivine alignment in mantle circulation instead, plate-driven flow alone produces anisotropy that has large misfits with SWS. The addition of large-scale mantle density anomalies and lateral viscosity variations significantly improves models. Although a strong continental craton is essential, varying its geometry does, however, not improve the plate-scale misfit. Moreover, models based on higher resolution tomography degrade the fit, indicating issues with the flow model assumptions and/or a missing contributions to anisotropy. We thus compute a "lithospheric complement" to achieve a best-fit, joint representation of asthenospheric and frozen-in lithospheric anisotropy. The complement shows coherent structure and regional correlation with independently imaged crustal and upper mantle anisotropy. Dense SWS measurements therefore provide information on depth-dependent anisotropy with implications for tectonics, but much remains to be understood about continental anisotropy and its origin.

Upper Mantle Seismic Anisotropy as a Constraint for Mantle Flow and Continental Dynamics of the North American Plate

Wanying Wang^{a,b,*}, Thorsten W. Becker^{a,b}

 ^aInstitute for Geophysics, Jackson School of Geosciences, University of Texas at Austin, Austin, Texas, USA
 ^bDepartment of Geological Sciences, Jackson School of Geosciences, University of Texas at Austin, Austin, Texas, USA

Abstract

The alignment of intrinsically anisotropic olivine crystals under convection is typically invoked as the cause of the bulk of seismic anisotropy inferred from shear-wave splitting (SWS). This provides a means of constraining the interplay between continental dynamics and the deep mantle, in particular for densely instrumented regions such as North America after USArray. There, a comparison of "fast orientations" from SWS with absolute plate motions (APM) suggests that anisotropy is mainly controlled by plate motions. However, large regional misfits and the limited realism of the APM model motivate us to further explore SWS based anisotropy. If SWS is estimated from olivine alignment in mantle circulation instead, plate-driven flow alone produces anisotropy that has large misfits with SWS. The addition of large-scale mantle

Preprint submitted to Earth Planet. Sci. Lett.

^{*}Corresponding author Email address: wanying@utexas.edu (Wanying Wang)

density anomalies and lateral viscosity variations significantly improves models. Although a strong continental craton is essential, varying its geometry does, however, not improve the plate-scale misfit. Moreover, models based on higher resolution tomography degrade the fit, indicating issues with the flow model assumptions and/or a missing contributions to anisotropy. We thus compute a "lithospheric complement" to achieve a best-fit, joint representation of asthenospheric and frozen-in lithospheric anisotropy. The complement shows coherent structure and regional correlation with independently imaged crustal and upper mantle anisotropy. Dense SWS measurements therefore provide information on depth-dependent anisotropy with implications for tectonics, but much remains to be understood about continental anisotropy and its origin. *Keywords:* continental dynamics, seismic anisotropy, North American plate

1 1. Introduction

Upper mantle seismic anisotropy is suggested to be mainly caused 2 by the alignment of olivine aggregates in mantle flow. This is referred 3 to as olivine lattice preferred orientation (LPO), and LPO is expected 4 to align with shear under convection. This relationship provides a link 5 between asthenospheric flow and seismic observations, in particular to 6 study the relationships between surface geology and the underlying 7 mantle dynamics in continental plates (e.g. Silver, 1996; Long and Becker, 2010). In order to obtain information about upper mantle flow, shear-wave splitting (SWS) analysis of teleseismic phases is widely used to infer 10 azimuthal anisotropy. SWS measures the separation of shear waves 11 into two orthogonally polarized pulses upon traversing an anisotropic 12 The polarization plane orientation of the faster shear wave medium. 13 pulse is often called the "fast azimuth", and is expected to parallel the 14 alignment of the seismically fast [100]-axes of the olivine aggregates and 15 the sense of shear. The delay time between the fast and slow wave 16 arrivals at the surface indicates the anisotropy magnitude accumulated 17 along the path, and by inference, the depth extent or layer thickness of 18 the anisotropic part of the mantle or lithosphere (e.g. Silver, 1996; Savage, 19 1999). Teleseismic SWS measurements use SKS, SKKS and PKS phases 20 that have nearly vertical ray paths and sample the upper mantle beneath 21 the seismic stations with poor vertical, but good lateral resolution. 22

23

Recently, the USArray seismometer deployment during the EarthScope

effort provided unprecedented coverage of United States, renewing
efforts to investigate mantle dynamics within and underneath the North
American plate (e.g. Hongsresawat et al., 2015; Long et al., 2016; Zhou
et al., 2018). Here, we compare a range of mantle flow model predictions of
upper mantle anisotropy to the observed SWS fast orientations to advance
our understanding of North America upper mantle dynamics (Fig. 1).

The SWS dataset used in this study is shown in Fig. 1b and newly spans the whole continent at roughly uniform station spacing. The SWS compilation consists of 14,326 splits from the updated compilation of Becker et al. (2012), as well 29,061 standardized splits from Liu et al. (2014), Refayee et al. (2014), and Yang et al. (2016, 2017). We also include results from offshore experiments (Bodmer et al., 2015; Ramsay et al., 2015; Lynner and Bodmer, 2017).

As has been discussed earlier based on more limited compilations, the 37 fast SWS orientation within the U.S. are generally E-W to NW-SE (e.g. 38 Silver, 1996), exhibit a circular pattern beneath the Great Basin (e.g. Zandt 39 and Humphreys, 2008; Hongsresawat et al., 2015), and orogen-parallel 40 orientation beneath and around the Appalachians (e.g. Long et al., 2016) 41 (Fig. 1b). While we mainly consider fast azimuths below, we note that the 42 delay times of SWS vary in systematic fashion. Broadly speaking, delay 43 times are larger beneath most of the western U.S. and the south central 44 U.S., and smaller beneath the interior plain, the Appalachians and the 45 southern Great Basin (Fig. 1b). 46

In order to link those observations of azimuthal anisotropy to 47 continental dynamics, we can consider the geological history of the 48 region. In the broadest of strokes, we note that the western U.S. has been 49 tectonically active since the late Mesozoic, from the Laramide orogeny to 50 the ongoing subduction-related orogenesis in the Cascades and extension 51 in the Basin and Range. A relatively thinner lithosphere in the west 52 likely plays a role in suggested scenarios where active mantle flow affects 53 lithospheric deformation beneath the Basin and Range, the Colorado 54 plateau and the Rockies (e.g. Savage and Sheehan, 2000; Karlstrom et al., 55 2012). Likewise, mantle flow itself may have eroded part of the lithosphere 56 and caused thinning and extension at the Basin and Range (e.g. Lekić and 57 Fischer, 2014). A thinner lithosphere relative to the cratonic eastern U.S. 58 also implies a reduced role of possible shallow, frozen in anisotropy (e.g. 59 Silver, 1996), and perhaps a more readily understandable link between 60 asthenospheric flow and SWS. 61

The area through the central U.S. to the west of the Appalachian 62 mountains is within the extent of the North American Craton, which is 63 part of the oldest lithosphere on Earth that had been stable for over 1.7 64 Ga (e.g. Hoffman, 1989). The lithospheric root beneath the craton extends 65 to over 200 km depth (e.g. Gung et al., 2003; Steinberger and Becker, 2016), 66 and is suggested to have higher viscosity than the surrounding mantle 67 (e.g. Lenardic and Moresi, 1999). Beneath the central U.S., the oldest 68 part of the cratonic region is stable since the Archean, and may preserve 69

relatively larger degrees of shallow, frozen-in anisotropy. On the other 70 hand, the cratonic root may divert upper mantle flow, perturbing flow 71 at the craton's edge and inducing counter flow beneath it, which could 72 possibly strengthen regional lithosphere-asthenosphere coupling (e.g. 73 Silver, 1996; Fouch et al., 2000). This phenomenon is likely important for 74 understanding the details of upper mantle flow dynamics and the origin of 75 azimuthal anisotropy beneath the eastern U.S., which sits atop the cratonic 76 boundary and edge. 77

Tectonic features in the eastern U.S. include the Proterozoic rifting and 78 Paleozoic compressional orogenic events, followed by extensional events 79 in the Mesozoic. Based on SWS splitting and modeling, Fouch et al. (2000) 80 suggested that the observed anisotropy reveals the combined effect from 81 the lithospheric and sublithospheric anisotropy in this region. Small-scale 82 upper mantle density variations and lithospheric thickness variations exist 83 in this region (Fig. 2) and might cause perturbations in anisotropy as well. 84 For example, the northern Appalachian upwelling that can be inferred 85 from slow seismic tomography anomalies (Schmandt and Lin, 2014) might 86 relate to the Great Meteor hot spot track, and possibly indicate convection 87 on relatively small scales in the surrounding mantle (e.g. Schmandt and 88 Lin, 2014; Levin et al., 2018). Lithospheric thickness appears to decrease 89 rapidly from the plateau to the east of the Appalachian, and is suggested 90 to relate to lithospheric weakness from Eocene delamination (e.g. Mazza 91 et al., 2014). 92

Convective flow models should be able to predict the current 93 sublithospheric LPO to match the SWS observations if the models capture 94 the major contributors that affect the present day upper mantle strain (e.g. 95 Long and Becker, 2010). Given the extensive tectonic activity and prior 96 sampling, much of the geodynamic SWS modeling previously focused on 97 the western U.S.. For example, Silver and Holt (2002) jointly interpreted 98 splitting and GPS observations to infer eastward mantle flow. Becker 99 et al. (2006b) computed LPO from mantle flow modeling, and showed that 100 SWS outside the Basin and Range domain could be fit well with relatively 101 simple flow models as long as a downwelling associated with the Farallon 102 slab was included. More recently, Zhou et al. (2018) computed anisotropy 103 from more complex models with lateral viscosity variations (LVVs) and 104 were able to reproduce the circular pattern discussed by Zandt and 105 Humphreys (2008). 106

Given the long geological history of the North American plate, we 107 expect that the lithosphere-asthenosphere system will reflect different 108 contributions to anisotropy. Based on joint surface wave and SWS 109 analysis, Yuan and Romanowicz (2010) suggested layering with various 110 lithospheric azimuthal anisotropy orientations beneath North America, 111 and many authors have made the case that variations in SWS fast 112 orientations with back-azimuth are best explained by a significant 113 lithospheric anisotropy source (Silver, 1996; Savage, 1999). 114

115

Here, we seek to address azimuthal anisotropy underneath the U.S.,

explore which role small-scale lateral variations in density and viscosity
play for predictions of asthenospheric anisotropy, and then return to the
question of lithospheric anisotropy.

119 2. Methods

¹²⁰ Mantle flow modeling

This study broadly follows the approach of Becker et al. (2006b) and Miller and Becker (2012). Under the Boussinesq and infinite Prandtl number approximations, the conservation equations for mass and momentum for mantle flow are given by

$$\nabla \cdot u = 0,$$

$$-\nabla p + \nabla \cdot \eta (\nabla u + \nabla^T u)] - \delta \rho g \hat{e}_r = 0.$$

Here, *u* is the velocity vector, *p* is the dynamic pressure, η is the viscosity, 125 $\delta \rho$ is the density anomaly, g is the gravitational acceleration and \hat{e}_r is the 126 radial unit vector. We solve the conservation equation using the finite 127 element software CitcomS (Zhong et al., 2000) in a 3-D spherical domain. 128 The surface boundary condition of most of our models are prescribed plate 129 motions in the no-net-rotation (NNR) reference frame (NNR-NUVEL-1, 130 by Argus and Gordon, 1991). The mechanical boundary condition at the 131 core-mantle boundary is free-slip. Therefore, the absolute reference frame 132 of the plate motions is irrelevant for relative velocities, and hence mantle 133

¹³⁴ flow predicted anisotropy.

Density variations outside continental cratons are assumed to be 135 purely thermal and scaled from seismic tomography anomalies $\ln v_S$ with 136 a simplified scaling of $R = \frac{d \ln \rho}{d \ln V_S}$. To ensure that the system is dynamically 137 consistent, the resulting vigor of density-driven flow is adjusted via R138 such that when the same density variation is used in a model with 139 free-slip surface boundary conditions, the same RMS surface velocity as 140 for prescribed absolute plate motion (APM) results. The resulting R = 0.24141 is in line with prior work (e.g. Miller and Becker, 2012). Inputs for the 142 density variations come from two models: SMEAN is a composite, global 143 S-wave tomography model (Becker and Boschi, 2002) used for reference 144 (Fig. 2a). In order to capture the possible effect of small scale density 145 anomalies beneath the U.S., we merge the regional tomography model 146 of Schmandt and Lin (2014) with SMEAN to obtain MERGED where the 147 edges of the embedded high resolution region are smoothed (Fig. 2b). 148

Within cratons, where we expect compositional anomalies (e.g. Jordan, 149 1978; Forte and Perry, 2000), we assume the lithosphere to be neutrally 150 buoyant by setting craton-related seismic velocity anomalies to zero. The 151 depth of the cratonic root is suggested to be $\sim 200 - 250$ km, for example 152 by Yuan and Romanowicz (2010) and Gung et al. (2003), and geodynamic 153 inversions (Forte and Perry, 2000). Since the tomography models we use 154 show fast velocity anomalies that extend to ~ 300 km beneath the North 155 American Craton, we use 300 km depth as the extent of the neutrally 156

¹⁵⁷ buoyant zone, for simplicity. The viscosity of the cratonic root is important
¹⁵⁸ in maintaining its long term stability. Convection modeling suggests it to
¹⁵⁹ be 100 to 1000 times more viscous than the ambient mantle (e.g. Lenardic
¹⁶⁰ and Moresi, 1999). Here we assume it to be 10 times more viscous than the
¹⁶¹ continental lithosphere, which is 500 times the regular asthenosphere.

Both radial and lateral viscosity variations are considered. The 162 viscosity model is built upon a three layered radial viscosity structure 163 (RVV). The viscosity of each of the 0 - 100 km, 100 - 660 km, and 660 - 100 km 164 2891 km layers is 150, 1, and 60 times the reference value. For the 100 -165 660 km depth range, a temperature dependent lateral viscosity variation 166 (LVV) is applied to the three layered RVV structure, and the viscosity is 167 given by equation: $\eta = \eta_0 \exp E(T - T_{ref})$. In this equation η_0 is from 168 the RVV structure, E scales the effect of temperature dependence with a 169 value of 7, T is the non-dimensional temperature at each point inferred 170 from the tomography models, and T_{ref} is the non-dimensional reference 171 temperature that equals to 0.5. In the upper 300 km, η is then multiplied 172 by a structure dependent viscosity factor to account for the LVVs. 173

The viscosity factor at each of the plate boundaries, the oceanic and continental lithosphere, cratonic keels and oceanic asthenosphere is 0.01, 1, 50, 500, 0.01, respectively (cf. Miller and Becker, 2012). Focusing on continental keels underneath the U.S., we test two viscosity structures, models LVV1 and LVV2. The cratonic keel geometry of LVV1 is inferred from global tomography using the approach of Steinberger and Becker (2016) and the model SL2013 (Schaeffer and Lebedev, 2013). In LVV1, the
minimum lithospheric thickness is 50 km in both continental and oceanic
regions (Fig. 2c). LVV2 is taken from the reference craton model of Miller
and Becker (2012) where keel geometry is simpler, and keel depth constant
at 300 km (Fig. 2d).

¹⁸⁵ Asthenospheric and lithospheric anisotropy modeling

Based on the mantle circulation models, we then use particle tracking 186 and the D-Rex mineral physics approximation (Kaminski et al., 2004) to 187 compute LPO as the tracers are advected until a logarithmic saturation 188 strain of 0.75 is reached (Becker et al., 2006b; Miller and Becker, 2012). 189 We assume that mantle circulation is stationary over the few Myr that it 190 takes to achieve this strain (cf. Becker et al., 2003, 2006a). Depth-dependent 191 single crystal elasticity constants and Voigt averaging are then used to 192 determine the elasticity tensor C at 25 km spaced locations underneath 193 each of the stations where SWS is measured. 194

¹⁹⁵ While *SKS* splitting is well known to not linearly average over **C** along ¹⁹⁶ the path, such differences are generally limited as long as anisotropy does ¹⁹⁷ not vary strongly with depth (e.g. Becker et al., 2012). We conducted tests ¹⁹⁸ using the full-waveform approach of Becker et al. (2006b) and found that ¹⁹⁹ regionally, details of the SWS predictions were affected. However, our ²⁰⁰ overall conclusions regarding the flow model predictions would be the ²⁰¹ same. Here, we therefore mainly consider the simplified, depth-averaged tensor approach, computing an average for the 25 to 375 km depth range, but we revisit a two layer case below. Under the tensor-averaging assumption, the Christoffel equation is then solved for the equivalent SWS delay times and fast azimuths using a back-azimuthal average.

Upon having predicted the inferred LPO anisotropy caused by mantle 207 flow in the asthenosphere, we compare it with the SWS observation and 208 compute the absolute angular misfit, $\Delta \alpha$, between the two ($\Delta \alpha \in [0^{\circ}, 90^{\circ}]$) 209 for a range of flow models. Given the relatively poor overall fit for the 210 study area of those predictions (Fig. 4 to 7) compared to earlier work 211 (e.g. Miller and Becker, 2012), we also explore the possible contributions 212 of the lithosphere more extensively. For this, we assume that there are 213 two anisotropy layers, and the bottom layer is fixed to the flow model 214 predicted anisotropy, which represents the depth averaged asthenospheric 215 anisotropy. Then we invert for the best-fit "lithospheric complement" 216 based on a parameter space exploration and Silver and Savage's (1994) 217 approach, and find the fast azimuth and delay time of the top layer 218 anisotropy that, results in the best match to the back-azimuthally 219 distributed SWS observations at each station. 220

221 **3. Results**

222 SWS alignment with absolute plate motions

Assuming that plate motions at the surface in some absolute reference 223 frame (APM) are reflective of the orientation of shear between the 224 lithosphere and mantle, APM alignment is a first order test for the origin 225 of anisotropy (Silver, 1996). The SWS fast orientation beneath the U.S. are 226 indeed found to be generally aligned with plate motion directions (e.g. 227 Hongsresawat et al., 2015). Figure 3 substantiates earlier analyses using 228 our denser SWS dataset by comparing it with APM in the NNR reference 229 frame (Argus and Gordon, 1991), and the spreading-aligned reference 230 frame (Becker et al., 2015). 231

On a plate scale, SWS fast axes have NE-SW orientations similar to 232 the NNR APM orientation of North America, especially in the western 233 U.S. (Fig. 3a), leading to a plate-scale mean misfit of $\langle \Delta \alpha \rangle \approx 30^{\circ}$. The 234 spreading-aligned APM is more similar to the SWS fast orientations and 235 $\langle \Delta \alpha \rangle$ is further reduced by ~ 5° (Fig. 3b). While misfit values thus depend 236 on different APM reference frames (e.g. Becker et al., 2015), similar local 237 misfit fluctuations are observed, and those may be related to mantle flow 238 deviating from implied APM shear. For example, in the southeastern 239 Rockies (Fig. 3), the large angular misfit might relate to local lithospheric 240 thickness variations (Refayee et al., 2014; Hongsresawat et al., 2015). 241 Another significant misfit is found at the eastern U.S. and the southern 242 Appalachian Mountains (Fig. 3), where anisotropy possibly contains a 243

lithospheric frozen-in component (e.g. Levin et al., 2018; Long et al., 2016).

²⁴⁵ *Flow model predictions for SWS*

We now test the role of asthenospheric convection other than APM 246 shearing by predicting anisotropy from the sublithospheric flow that is 247 driven by plate motion alone, or in addition by density variations. We 248 investigate the effect of viscosity variations caused by cratons, a weak 249 oceanic asthenosphere layer, and plate boundary weak zones. For each 250 flow model, we explore the flow itself, and compute the misfit between 251 predicted and observed anisotropy, $\Delta \alpha$ (Table 1). We find it helpful to 252 visualize the effect of shearing in flow models by plotting the vector 253 difference \vec{v}_{shear} between the horizontal flow velocities at the surface 254 $\vec{v}_{surface}$ and at a typical, 200 km depth \vec{v}_{200km} with 255

$$\vec{v}_{shear} = \vec{v}_{200km} - \vec{v}_{surface}$$

²⁵⁶ as such differential velocities can be a rough proxy for LPO alignment.

²⁵⁷ The effect of plate motion induced circulation with LVVs

Our starting Model 1 only has radial viscosity variations and is purely driven by prescribed plate motions. Given the effects of geometry and return flow, we expect that the induced asthenospheric shearing will be different from the APM model of Fig. 3 even for this simple circulation model (e.g. Long and Becker, 2010), and this is indeed the case.

Figure 4a shows that beneath the western and central U.S., the 263 direction of \vec{v}_{200km} deviates from the plate motion direction due to the 264 flow perturbation at the Pacific-North America plate boundary. The flow 265 direction is to the W to SW and the shear direction forms an 110° to 266 150° angle with the plate motion in this region. While details depend 267 on the viscosity structure (cf. Becker et al., 2006b), this plate boundary 268 flow perturbation extends almost throughout half the continent. In the 269 Eastern U.S., sublithospheric Couette flow (Fig. 5a) is more in line with 270 APM, such that shear is roughly into the opposite direction (Fig. 4a). The 271 mis-alignment of shear and plate motion vectors is subdued in the eastern 272 U.S. but still of order 20° to 30° . 273

Since there are no small-scale flow perturbation or abrupt changes 274 in viscosity, the orientation of differential velocities of Fig. 4a are 275 representative of the predicted anisotropy (Fig. 4b). W-E oriented 276 predicted fast axes fit well with the SWS observation onshore in NW 277 U.S.. However, there are large misfits with regions of consistent $\sim 90^{\circ}$ 278 misalignment such as the in the southern Rockies. The overall match 279 between SWS and predictions is very poor at $\langle \Delta \alpha \rangle \approx 45^{\circ}$ (which is the 280 expectation for random). This indicates that plate-induced shear flow 281 without density anomalies is actually a much worse model in this case 282 compared to the APM hypothesis of Fig. 3. 283

Based on Model 1, Model 2 adds in weak plate boundaries and strong
 cratonic keels from viscosity model LVV1. Comparing Models 1 and 2,

changes in horizontal flow mainly occur beneath and around the craton 286 The spatial extent of this change is shown in the (Figs. 4a and c). 287 differential flow velocity profile in Fig. 5d. Due to its high viscosity, 288 the craton maintains and enhances plate-like motion down to ~ 300 km 289 depth, as shown in Fig. 4c, and transfers it to the sublithospheric mantle. 290 The craton also causes minor flow perturbations in the radial direction 291 at the lithospheric thickness discontinuities beneath the Colorado Plateau 292 (Fig. 5d). However, the directional change in flow introduced by the keel 293 is overall small, such that the anisotropy predictions of Models 1 and 2 are 294 fairly similar (Figs. 4b and d). The weak plate boundary effect of Model 2 295 changes the flow and shear direction beneath the Juan de Fuca Plate, for 296 example, slightly reducing $\Delta \alpha$ there (Fig. 4d). 297

Model 3 adds in a 200 km thick oceanic asthenosphere that is 100 298 times weaker than the ambient mantle compared to Model 2 (cf. Becker, 299 2017). Comparing the flow fields in Models 2 and 3, we see significant 300 differences in flow pattern beneath the oceanic plates and adjacent areas 301 (Figs. 4c and e). Differential velocities, \vec{v}_{200km} , and the APM within the 302 oceanic region are nearly parallel in Model 2 (Fig. 4c), while in Model 3 303 they are perpendicular within the Pacific and form 40° to 60° angles within 304 the Atlantic domain (Fig. 4e). The flow modification leads to a rotation in 305 predicted anisotropy orientations from NW-SE in Model 2 to W-E in Model 306 3 (Figs. 4b and d). 307



Angular misfits $\Delta \alpha$ in Model 3 are reduced to $< 10^{\circ}$ in parts of

the western and eastern U.S. (Fig. 4f). We see misfit reduction relative 309 to Model 2 result (Fig. 4d) through most of the study area. Here, the 310 weak sub-oceanic asthenosphere causes flow directional change to become 311 more APM parallel than Model 2 through the south central and south 312 eastern U.S.. This effect, though small, can be seen from the change in 313 shear direction and magnitude. At greater depth the flow changes to 314 westward, so the depth-averaged shear vector and predicted fast axes 315 orient approximately W-E instead of parallel to the plate motion. Overall, 316 the weak asthenosphere in plate-driven flow models accommodates the 317 lithospheric shear beneath the Pacific plate, slows down the westward 318 sublithospheric flow motion beneath the U.S., and amplifies return flow at 319 400 km depth (Figs. 5c and e). The misfit is overall reduced to $\langle \Delta \alpha \rangle \approx 36^{\circ}$ 320 for Model 3. These tests suggests that a sub-oceanic viscosity reduction, as 321 a much larger-scale feature compared to plate boundaries and continental 322 cratons, can have a major control over the plate-driven shear (cf. Conrad 323 and Lithgow-Bertelloni, 2006). 324

³²⁵ The effect of density driven flow

We next investigate the effect of density-driven flow by adding anomalies inferred from SMEAN and MERGED tomography models to Model 2, resulting in Models 4 and 5, respectively. The direction of \vec{v}_{200km} in Model 4 changes nearly 180° from the western to central U.S. (Fig. 6a) relative to Model 2, also clearly seen in the flow profile of Fig. 6e. This flow patterns results from an upwelling underneath the western U.S. and a lower-mantle, Farallon-related slab sinker anomaly. Those were earlier shown to lead to strong, APM opposite counter flow underneath the western half of the U.S. (e.g. Becker et al., 2006b), and are here seen to be further modulated by the cratonic keel.

Density anomalies from SMEAN as incorporated in Model 4 result 336 in shear and predicted anisotropy fast axes oriented W-E to WSW-ENE 337 beneath the north western U.S. and west central U.S., W-E to WNW-ESE 338 beneath the east central U.S. and north eastern U.S., and SW-NE beneath 339 the south eastern U.S. (Figs. 6a and b). In these regions, the predicted 340 anisotropy fits the SWS observation nearly as well as the APM model 341 (Fig. 3), and the overall misfit is $\langle \Delta \alpha \rangle \approx 32^{\circ}$. This substantiates that a 342 contribution of density-induced flow to plate-driven shear is needed for 343 an appropriate prediction of LPO anisotropy, and hence a realistic mantle 344 circulation estimate, as has been argued for global models (e.g. Behn et al., 345 2004; Becker et al., 2015). 346

The flow pattern and predicted anisotropy orientation in Model 5 based on MERGED are overall similar to Model 4 (Figs. 6c, d and Fig. 6f), but have, expectedly, more small-scale perturbations due to the higher resolution, regional tomography model of Schmandt and Lin (2014). Those features include the radial flow beneath Yellowstone and Snake River Plain (e.g. Savage and Sheehan, 2000), Salton Trough, northern Great Valley, Rio Grande Rift, New England and central Appalachian

Some of these smaller-scale flow structures inferred from (Fig. 2b). 354 For example, MERGED affect the predicted anisotropy significantly. 355 beneath the northern Great Valley, which corresponds to a $\sim 5^{\circ} \times 5^{\circ}$ 356 region with large $\Delta \alpha$ in Model 4, the dense structure that is suggested 357 to be a lithospheric instability (Zandt et al., 2004) changes the predicted 358 anisotropy orientation from nearly N-S in Model 4 to either SW-NE or 359 NW-SE in Model 5, and results in a $\sim 45^{\circ}$ improvement in $\Delta \alpha$ values 360 locally. 361

However, on balance, a degradation of the fit to SWS results on the 362 scale of the whole U.S. is seen when the presumably better resolved 363 MERGED tomography is used, with mean misfit increased to $\langle \Delta \alpha \rangle \approx$ 364 38° (Fig. 6d). This means that asthenospheric flow is sensitively and 365 diagnostically mapped into SWS predictions, but simply adding newer 366 density models to existing flow computations at constant scaling does not 367 provide a more consistent description of mantle dynamics. In fact, the 368 opposite is true. 369

³⁷⁰ The effect of different LVVs in density and plate-driven flow models

LVVs were seen to improve the fit of purely plate-driven flow to SWS observations (cf. Figs. 4b and f). Adding density-driven flow on large scales further improved the fit to observation to a level that is comparable to the APM model (Fig. 6b), but not for the smaller-scale anomalies of MERGED (Fig. 6d). We therefore explore the other major contribution to ³⁷⁶ flow besides density, viscosity variations, further.

To complement the tests of Figs. 4 and 6 and focus on LVVs specifically, 377 we explore six additional models (Figs. 7 and 8). For the tomography 378 model SMEAN, we build a new reference, Model 6, by prescribing density 379 variations to Model 1. We then build Models 7 and 8 by prescribing LVV 380 models LVV1 and LVV2 to Model 6. Model 7 is different from Model 4 381 because it has the oceanic asthenosphere to allow for full investigation 382 of the LVVs and also to help to distinguish the effect of the craton from 383 the oceanic asthenosphere when comparing to Model 4. Similarly, for 384 tomography model MERGED, we have Model 9 in which there are no 385 LVVs, and Models 10 and 11 that use LVV1 and LVV2. 386

³⁸⁷ Without LVVs, the anisotropy predicted by Model 6 has W-E ³⁸⁸ orientation beneath the north western U.S. and west central U.S. and fits ³⁸⁹ the observed SWS regionally quite well (Fig. 7a). Other regions have very ³⁹⁰ large angular misfits, raising the average to $\langle \Delta \alpha \rangle \approx 50^{\circ}$, worse than for ³⁹¹ pure plate-driven shear (Fig. 4b). Model 9 shows similar patterns (Fig. 7d), ³⁹² besides the southeastern edge of the western U.S., for example.

³⁹³ Comparing Model 7 to 6 (Figs. 7a and b) and Model 10 to 9 (Figs. 7d ³⁹⁴ and e), we see that prescribing LVVs in flow models degrades the fit ³⁹⁵ offshore the east coast, improves the fit between predicted and observed ³⁹⁶ anisotropy in the central and eastern U.S., and largely modifies, although ³⁹⁷ does not improve, the predicted anisotropy in the western U.S. (overall ³⁹⁸ drop in $\langle \Delta \alpha \rangle$ is $\approx 6^{\circ}$ compared to no LVVs). Craton flow modification

(Figs. 8b and e) affects regional misfits but does not lead to an overall 399 improvement compared to the best flow model of Fig. 6b. Changing 400 the viscosity structure to the LVV2 models leads to better coupled flow 401 with the plate motion beneath the craton and thus changes the predicted 402 anisotropy orientation in the northern part of the central and eastern U.S. 403 (Figs. 7-c and f). LVV1 and LVV2 have different keel shapes (Figs. 2c 404 and d) and deflect or lead the flow differently. Indeed, comparing the 405 regional mean misfits of Fig. 7b and c, as well as e and f, we can see 406 changes particularly for the MERGED model. However, these effects of 407 anisotropy modification are not overall beneficial, and the mean misfit 408 values for models with the two viscosity structures are comparable. 409

Comparing flow profile residuals of the SMEAN flow models (Figs. 8b 410 and c), they both show better coupled sublithospheric flow velocity 411 beneath south central U.S. to the plate motion. The craton slows down the 412 eastward flow beneath the western U.S., and speeds up the westward flow 413 beneath the eastern U.S., relative to simpler viscosity models. For SMEAN, 414 LVV1 causes more perturbations on the radial direction to the flow 415 beneath it, while LVV2 mainly leads the sublithospheric flow horizontally. 416 The MERGED flow models have similar residual flow pattern overall, but 417 see more variations in magnitude and direction upon adding the cratons 418 (Figs. 8e and f), suggesting that the LVVs can amplify the density variation 419 effects. 420

In summary, we find that the effects of different assumptions on

asthenospheric density anomalies lead to the largest differences in 422 predicted anisotropy. Yet, presumably higher resolution tomography 423 does not improve the fit to SWS observations without additional model 424 adjustments. Lateral viscosity variations help improve the fit when 425 cratons and sub-oceanic viscosity reductions are introduced. Modifying 426 the keel geometries between models LVV1 and LVV2 does improve the fit 427 to SWS locally, but none of the modified LVV models we considered can 428 make up for the degradation of fit observed for MERGED compared to 429 SMEAN density anomalies. 430

Model	Viscosity Structures	Density	Average
Number		Variations ($\delta \rho$)	Misfit (°)
1	no LVVs	no $\delta \rho$	44.6°
2	cratons and plate boundaries in LVV1	no δho	45.0°
3	cratons, plate boundaries and oceanic asthenosphere in LVV1	no δho	35.5°
4	cratons and plate boundaries in LVV1	SMEAN	32.5°
5	cratons and plate boundaries in LVV1	MERGED	38.2°
6	no LVVs	SMEAN	49.9°
7	all structures in LVV1	SMEAN	40.5°
8	all structures in LVV2	SMEAN	40.1°
9	no LVVs	MERGED	45.1°
10	all structures in LVV1	MERGED	41.8°
11	all structures in LVV2	MERGED	40.9°

Table 1: Summary of the main information of all flow models discussed in this paper, through Model 1 to 11. Column 2 and 3 list the corresponding viscosity structure and density variation model of each flow model. Column 4 lists the average angular misfit between model predicted anisotropy and SWS observation. The surface boundary condition is prescribed APM for all flow models.

431 **4. Discussion**

432 Sensitivity of mantle flow modeling

We confirm that lateral viscosity variations can play an important 433 role in controlling upper mantle flow underneath continental regions 434 (e.g. Fouch et al., 2000; Miller and Becker, 2012). Plate-motion 435 induced mantle-flow model predictions of SWS observations of azimuthal 436 anisotropy are much improved when LVVs are added (Figs. 4b and f). This 437 improvement is mainly due to the implementation of a strong cratonic 438 keel and a weak oceanic asthenosphere which lead to enhancement and 439 reduction of the coupling between plate motions and sublithospheric 440 mantle, respectively (e.g. Conrad and Lithgow-Bertelloni, 2006; Becker, 441 2017). However, for purely plate-driven flow, the addition of a stiff 442 craton does not cause significant regional flow deflection in lateral or 443 radial directions, unlike what might be expected given experiments using 444 simpler geometries (e.g. Fouch et al., 2000). Moreover, the fit to SWS 445 of plate-driven flow is worse than the likely unphysical assumption of 446 alignment with APM motions. 447

In models that also include the effect of mantle density anomalies for flow, in contrast, the craton amplifies the small-scale radial flow and causes more significant lateral deflection and strong downward deflection on scales that are relevant for regional anisotropy. In conjunction, the effects of density-driven flow and lateral viscosity variations are reflected in anisotropy, and SWS observations therefore do appear diagnostic of ⁴⁵⁴ both density and viscosity anomalies on scales of 100s of km.

SWS and flow dynamic studies have, of course, long suggested the 455 importance of density anomalies for North American plate dynamics, 456 for example related to the Juan de Fuca and Farallon slabs (e.g. Becker 457 et al., 2006b; Zandt and Humphreys, 2008), possible mantle drips (e.g. 458 West et al., 2009) and mantle upwellings (e.g. Savage and Sheehan, 459 2000). Such anomalies should be better captured by the MERGED model 460 based on regionally improved tomography, which makes it interesting 461 that the addition of smaller-scale mantle structure actually leads to 462 a worsening of the misfit between model predictions and azimuthal 463 anisotropy observations (Figs. 6b and d). This was unexpected given prior 464 successes of the general modeling approach. 465

Let us assume that structural models from seismology have in fact 466 improved thanks to USArray, and that the most fundamental assumptions 467 for our approach hold, i.e. that upper mantle anisotropy is at least partially 468 caused by LPO alignment under asthenospheric mantle flow, and that 469 mantle flow can be estimated with mantle circulation models (e.g. Long 470 and Becker, 2010). There are then several possible, not mutually exclusive, 471 reasons for why our best circulation-based model is one that is based on 472 plate-driven flow, the SMEAN large-scale mantle density anomalies, and 473 simple LVVs. 474

First, given the sensitivity of LPO predictions to details of the LVVs, different keel structures, non-linear rheology, variations in volatile

content, or additional compositional dependence of viscosity may all 477 lead to lateral viscosity variations that counterbalance the detrimental 478 effects of adding small-scale density structure of MERGED. A formal 479 inversion for these variations redis possible, but none of our forward tests 480 (most not shown) trying different LVV structures have led to plate-scale 481 improvement in mean misfit. Figure 7 illustrates the sorts of variations 482 in LPO predictions one might expect. These effects are in line with 483 arguments about local effects, e.g. of drips and the like, but we leave 484 the exploration of more complex mantle LVV models that could possibly 485 reconcile the predictions for later. The general applicability of such 486 optimized models will also be questionable should the LVVs not be based 487 on some additional, general physical relationship not explored here. 488

Second, our scaling between seismic tomography and density 489 anomalies might be wrong, and this is clearly the case in principle, 490 given the highly simplified nature of our linear, depth-independent 491 scaling. Besides temperature, other properties, especially compositional 492 heterogeneity and anelasticity, can also affect seismic wave velocity (e.g. 493 Forte and Perry, 2000; Cammarano et al., 2003). This might be of 494 particular importance for the high resolution tomography model, which 495 might demand lateral variations in the scaling factor. We expect that 496 cratonic regions of the continental lithosphere may be neutrally buoyant 497 ("isopycnic", Jordan, 1978) which is why we corrected for this effect in a 498 coarse fashion in our mantle flow models. The isopycnic assumption is not 499

expected to be perfectly true at all depths, nor is the extent of cratons or the
thickness of the lithosphere well constrained (e.g. Lekić and Fischer, 2014;
Steinberger and Becker, 2016). We therefore cannot rule out that more
sophisticated models including a wider range of compositional anomalies
would lead to better predictions of LPO based anisotropy using the high
resolution tomography models such as MERGED.

However, we conducted a range of tests where we varied the R scaling 506 step wise from zero to its reference value, and found that the signal 507 inherent in MERGED leads to a degradation of the fit compared to SMEAN 508 as soon as the density effects are felt by mantle flow. This implies that 509 compositional anomalies would have to cancel out much of the signal seen 510 in MERGED compared to SMEAN to at least not degrade the fit. This is 511 possible, but would also question the general interpretations of seismic 512 tomography for regional tectonics. 513

Third, time-dependence of mantle convection, and in particular changes in plate motions, may complicate the interpretation of LPO based anisotropy even for the relatively short time-scales needed to saturate fabrics within the asthenosphere (e.g. Kaminski et al., 2004; Becker et al., 2006a). On global scales, Becker et al. (2003) showed that this effect was detectable, but seismological models did not allow determining which models were better within uncertainty.

Regionally, the story may be different, and Zhou et al. (2018) explored such effects for the western U.S. in detail. The authors pointed out the ⁵²³ importance of the Juan de Fuca slab and a hot mantle anomaly beneath the
⁵²⁴ western U.S. for the formation of the circular anisotropy beneath the Great
⁵²⁵ Basin. However, the anisotropy adjacent to that pattern was not well fit,
⁵²⁶ implying similarly mixed results in terms of a comprehensive explanation
⁵²⁷ of SWS observations.

There are thus at least three plausible reasons why a purely asthenospheric origin of anisotropy appears to be a moderately successful explanation of the large-scale SWS signal for the U.S. at best. In the remainder, we will instead assume, for the sake of argument, that our computations are in fact very good predictions of asthenospheric anisotropy, so good that we can ask about a missing lithospheric component needed to fit SWS observations.

535 The lithospheric complement

A lithospheric, frozen-in origin of anisotropy has long been discussed 536 for the shallow oceanic lithosphere, as well as the bulk of the thicker 537 and petrologically more heterogeneous continental lithosphere (e.g. Silver, 538 1996). Assuming that the difference between the SWS observations and 539 flow predictions of LPO anisotropy arises entirely from the lithospheric 540 component, we can augment a flow model with its corresponding 541 lithospheric complement that would be needed to achieve a (near) perfect 542 fit to SKS splitting. 543

544 Figure 9 shows results for the lithospheric complements for the

27

best performing LPO based on flow models, Model 4 (SMEAN) and 5 545 (MERGED). The lithospheric complement is found by fitting individual 546 splits from Liu et al. (2014) with a two-layer model, in which the bottom 547 layer is fixed to the flow predicted anisotropy. The values of the apparent 548 splitting parameters from the hypothetical two-layer anisotropy and the 549 average of the SKS splits are similar (Fig. S1), with angular difference 550 of $\Delta \alpha \leq 5^{\circ}$, which would be within the typical "error" of SWS estimates. 551 For stations where the flow predicted anisotropy has similar orientation 552 to the bottom layer from an independent two-layer inversion of SKS 553 splits, the hypothetical lithospheric anisotropy is also similar to the top 554 layer from the independent inversion. This suggests the validity of this 555 approach for studying multi-layer anisotropy. Besides the two layer 556 parameter space exploration approach, we also explore a simple method 557 of matching SWS by inverting for the best-fit thickness and anisotropy 558 orientation of a lithospheric layer that consists of frozen-in anisotropy 559 represented by a single elastic tensor (supp. mat.). Using this method, the 560 inferred lithospheric complement has similar orientation with our current 561 approach, but the delay times are less realistic (Fig. S2). We leave the 562 exploration of back-azimuthal dependence of SKS splitting for a future 563 joint analysis with surface-wave depth-dependent anisotropy. 564

As Figs. 9a and b show, the patterns of the best fit lithospheric complement are fairly smooth over much of the study area. This might be expected from the spatial heterogeneity of SWS and seismic tomography, ⁵⁶⁸ but implies that there could be a relation with a deterministic tectonic or ⁵⁶⁹ convective process. The lithospheric complement is different for the two ⁵⁷⁰ flow models in detail, but there are also consistent features. That said, the ⁵⁷¹ connection of the lithospheric complement's azimuthal alignment patterns ⁵⁷² to geological history is not immediately apparent, at least to us.

However, we can check if the features of the complement are at least 573 consistent with other possibly related observations. To this end, we 574 visually compare the complements with an azimuthal anisotropy model 575 inferred from 16 s period Rayleigh waves by Lin and Schmandt (2014) 576 (Fig. 9e). While mainly sensitive to the uppermost crust, the anisotropy 577 orientations appear related to tectonic regions, such as the Great Basin, 578 the Rockies and the Precambrian Rift Margin (Lin and Schmandt, 2014). 579 Without going to details of the relationship between crustal anisotropy 580 and tectonics, we note that there are fairly good correlations in orientations 581 between our lithospheric complement and the crustal anisotropy along the 582 west coast of the U.S., beneath the Columbia Plateau, the southern Basin 583 and Range, south of the Colorado plateau, Texas and the southern Coastal 584 Plain (Figs. 9a and b). Beneath the eastern U.S., Model 5's lithospheric 585 complement matches the crustal model while Model 4's does not. 586

To expand this comparison to the uppermost mantle, we further compare the Model 5 lithospheric complement with the Pn anisotropy model by Buehler and Shearer (2017) (Figs. 9f). This model provides information beneath the Moho. In this model, the NE-SW oriented

orogeny parallel anisotropy beneath the Appalachian mountain and east 591 central U.S. only exist in the central region (Fig. 9f). In other regions 592 of the eastern U.S., the anisotropy is E-W, which might relate to plate 593 motion (Buehler and Shearer, 2017). If this is the case, we would expect 594 orogeny parallel anisotropy at shallow depths, and more plate motion 595 parallel anisotropy beneath. This is true when we look at the Model 5 596 results, where the flow model predicted anisotropy parallels the plate 597 motion (Fig. 6d), and the lithospheric complement parallels the orogeny 598 (Fig. 9b). Since the SKS splits have a more dominant orogeny parallel 599 pattern compared to the uppermost mantle anisotropy, there might be 600 a significant crustal contribution in the SWS observation at the eastern 601 and east-central U.S., which partly explains the misfit we observed when 602 comparing the flow predicted anisotropy to SWS in this region. 603

To investigate the anisotropy at different depths in the eastern and 604 east-central U.S., we compare our lithospheric complement with the 605 regional model by Deschamps et al. (2008) (Fig. 9g). The lithospheric 606 complement of Model 5 (Fig. 9c) has similar patterns with the Rayleigh 607 wave anisotropy at periods < 60 s, which approximately shows the 608 lithosphere. The longer period (160 s) Rayleigh wave anisotropy, however, 609 does not match the lithospheric complement, but matches the flow 610 predicted anisotropy in the same region (Fig. 9d). This depth constraint 611 of anisotropy further suggests that the actual lithospheric anisotropy is 612 reasonably estimated by the lithospheric complement, and the lithosphere 613

has notable contribution to the SWS observation, at least in the eastern and
east-central U.S..

Good correlation between lithospheric complement the and 616 lithospheric anisotropy, and between flow model prediction and the 617 sublithospheric anisotropy in the eastern U.S. indicate the possibility that 618 MERGED predicts the sublithospheric anisotropy better than SMEAN 619 even if the asthenospheric LPO alone leads to a poor fit. This substantiates 620 importance of understanding lithospheric anisotropy, and may help to 621 resolve the connection between small-scale mantle structures and the 622 upper mantle anisotropy formation and SWS observation. 623

New insights into continental dynamics may yet be revealed by modeling anisotropy due to mantle flow. However, the answer might at least regionally have to involve more detailed study of the lithosphere and longer-term geological history. Such future work should be especially promising once noise and ballistic surface wave inferences for crustal and mantle anisotropy are adequately incorporated.

630 5. Conclusions

Azimuthal anisotropy in the upper mantle as seen by shear wave splitting throughout the U.S. and offshore portions of the North American plate can be modeled by mantle circulation models. These models allow exploring the effect of density anomalies and viscosity variations within the asthenosphere, which strongly affect predictions when acting

together. Large-scale flow models lead to misfits that are comparable 636 to the absolute plate motion alignment hypothesis for the study region. 637 This confirms the general validity of the approach, but smaller-scale 638 density anomalies of modern, EarthScope era tomography degrade the 639 fit, and none of the viscosity models we considered can make up for 640 "Lithospheric complements" can be estimated from the best flow it. 641 model based anisotropy, and those match independent estimates of crustal 642 anisotropy. This indicates promising avenues forward, but much is still to 643 be learned about the link between seismic anisotropy and mantle flow and 644 continental dynamics. 645

646 6. Acknowledgments

⁶⁴⁷ WW and TWB were partially supported by NSF EAR-1460479. All ⁶⁴⁸figures were prepared with the Generic Mapping Tools. We thank B. ⁶⁴⁹Schmandt and F. Lin for sharing their tomography and crustal anisotropy ⁶⁵⁰models with us. We thank our collaborators, K. Liu and S. Gao, for sharing ⁶⁵¹their SWS dataset with us. We also thank L. Fuchs and R. Porritt at the ⁶⁵²Geodynamics group at the Jackson School of Geosciences for help and ⁶⁵³discussions.

- Argus, D. F., Gordon, R. G., 1991. No-net-rotation model of current plate
 velocities incorporating plate motion model NUVEL-1. Geophys. Res.
 Lett. 18 (11), 2039–2042.
- Becker, T. W., 2017. Superweak asthenosphere in light of upper-mantle
 seismic anisotropy. Geochem., Geophys., Geosys. 18, 1986–2003.
- Becker, T. W., Boschi, L., 2002. A comparison of tomographic and
 geodynamic mantle models. Geochem., Geophys., Geosys. 3 (1).
- Becker, T. W., Chevrot, S., Schulte-Pelkum, V., Blackman, D. K., 2006a.
 Statistical properties of seismic anisotropy predicted by upper mantle
 geodynamic models. J. Geophys. Res. 111 (B8), B08309.
- Becker, T. W., Kellogg, J. B., Ekström, G., O'Connell, R. J., 2003.
 Comparison of azimuthal seismic anisotropy from surface waves and
 finite strain from global mantle-circulation models. Geophys. J. Int.
 155 (2), 696–714.
- Becker, T. W., Lebedev, S., Long, M. D., 2012. On the relationship between
 azimuthal anisotropy from shear wave splitting and surface wave
 tomography. J. Geophys. Res. Solid Earth 117 (B1).
- Becker, T. W., Schaeffer, A. J., Lebedev, S., Conrad, C. P., 2015. Toward
 a generalized plate motion reference frame. Geophys. Res. Lett. 42 (9),
 3188–3196.

674	Becker, T. W., Schulte-Pelkum, V., Blackman, D. K., Kellogg, J. B.,
675	O'Connell, R. J., 2006b. Mantle flow under the western United States
676	from shear wave splitting. Earth Planet. Sci. Lett. 247 (3-4), 235–251.

- Behn, M. D., Conrad, C. P., Silver, P. G., 2004. Detection of upper mantle
 flow associated with the African Superplume. Earth Planet. Sci. Lett.
 224, 259–274.
- Bodmer, M., Toomey, D. R., Hooft, E. E., Braunmiller, J., 2015. Seismic
 anisotropy beneath the Juan de Fuca plate system: Evidence for
 heterogeneous mantle flow. Geology 43.
- Buehler, J. S., Shearer, P. M., 2017. Uppermost mantle seismic velocity
 structure beneath USArray. J. Geophys. Res. Solid Earth 122 (1), 436–448.
- Cammarano, F., Goes, S., Vacher, P., Giardini, D., 2003. Inferring
 upper-mantle temperatures from seismic velocities. Phys. Earth Planet.
 Inter. 138 (3-4), 197–222.
- Conrad, C. P., Lithgow-Bertelloni, C., 2006. Influence of continental roots
 and asthenosphere on plate-mantle coupling. Geophys. Res. Lett. 33 (5),
 L05312.
- Deschamps, F., Lebedev, S., Meier, T., Trampert, J., 2008. Azimuthal
 anisotropy of Rayleigh-wave phase velocities in the east-central United
 States. Geophys. J. Int. 173 (3), 827–843.

- ⁶⁹⁴ Forte, A. M., Perry, H. K., 2000. Geodynamic evidence for a chemically
 ⁶⁹⁵ depleted continental tectosphere. Science 290 (5498), 1940–1944.
- ⁶⁹⁶ Fouch, M. J., Fischer, K. M., Parmentier, E. M., Wysession, M. E., Clarke,
- ⁶⁹⁷ T. J., 2000. Shear wave splitting, continental keels, and patterns of mantle
- ⁶⁹⁸ flow. J. Geophys. Res. Solid Earth 105 (B3), 6255–6275.
- Gung, Y., Panning, M., Romanowicz, B., 2003. Global anisotropy and the
 thickness of continents. Nature 422 (6933), 707–711.
- Hoffman, P. F., 1989. Speculations on Laurentia's first gigayear (2.0 to 1.0
 Ga). Geology 17 (2), 135.
- Hongsresawat, S., Panning, M. P., Russo, R. M., Foster, D. A., Monteiller,
 V., Chevrot, S., 2015. USArray shear wave splitting shows seismic
 anisotropy from both lithosphere and asthenosphere. Geology 43 (8),
 667–670.
- Jordan, T. H., 1978. Composition and development of the continental
 tectosphere. Nature 274 (5671), 544–548.
- Kaminski, E., Ribe, N. M., Browaeys, J. T., 2004. D-Rex, a program
 for calculation of seismic anisotropy due to crystal lattice preferred
 orientation in the convective upper mantlé mantlé. Geophys. J. Int 158,
 744–752.
- 713 Karlstrom, K. E., Coblentz, D., Dueker, K., Ouimet, W., Kirby, E., Van Wijk,
- J., Schmandt, B., Kelley, S., Lazear, G., Crossey, L. J., Crow, R., Aslan, A.,

- ⁷¹⁵ Darling, A., Aster, R., MacCarthy, J., Hansen, S. M., Stachnik, J., Stockli,
- D. F., Garcia, R. V., Hoffman, M., McKeon, R., Feldman, J., Heizler,
- M., Donahue, M. S., 2012. Mantle-driven dynamic uplift of the Rocky
- Mountains and Colorado Plateau and its surface response: Toward a
 unified hypothesis. Lithosphere 4, 3–22.
- Lekić, V., Fischer, K. M., 2014. Contrasting lithospheric signatures across
 the western United States revealed by Sp receiver functions. Earth
 Planet. Sci. Lett. 402, 90–98.
- Lenardic, A., Moresi, L.-N., 1999. Some thoughts on the stability of
 cratonic lithosphere: Effects of buoyancy and viscosity. J. Geophys. Res.
 Solid Earth 104 (B6), 12747–12758.
- Levin, V., Long, M. D., Skryzalin, P., Li, Y., López, I., 2018. Seismic evidence
 for a recently formed mantle upwelling beneath New England. Geology
 46 (1), 87–90.
- Lin, F.-C., Schmandt, B., 2014. Upper crustal azimuthal anisotropy across
 the contiguous U.S. determined by Rayleigh wave ellipticity. Geophys.
 Res. Lett. 41 (23), 8301–8307.
- Liu, K. H., Elsheikh, A., Lemnifi, A., Purevsuren, U., Ray, M., Refayee, H.,
 Yang, B. B., Yu, Y., Gao, S. S., 2014. A uniform database of teleseismic
 shear wave splitting measurements for the western and central United
 States. Geochemistry, Geophysics, Geosystems 15 (5), 2075–2085.

- Long, M. D., Becker, T. W., 2010. Mantle dynamics and seismic anisotropy.
 Earth Planet. Sci. Lett. 297 (3-4), 341–354.
- Long, M. D., Jackson, K. G., McNamara, J. F., 2016. SKS splitting
 beneath Transportable Array stations in eastern North America and the
 signature of past lithospheric deformation. Geochemistry, Geophysics,
 Geosystems 17 (1), 2–15.
- Lynner, C., Bodmer, M., 2017. Mantle flow along the eastern North
 American margin inferred from shear wave splitting. Geology 45 (10),
 867–870.
- Mazza, S. E., Gazel, E., Johnson, E. A., Kunk, M. J., McAleer, R., Spotila,
 J. A., Bizimis, M., Coleman, D. S., 2014. Volcanoes of the passive margin:
 The youngest magmatic event in eastern North America. Geology 42 (6),
 483–486.
- Miller, M. S., Becker, T. W., 2012. Mantle flow deflected by interactions
 between subducted slabs and cratonic keels. Nat. Geosci. 5 (10), 726–730.
- Ramsay, J., Kohler, M. D., Davis, P. M., Wang, X., Holt, W., Weeraratne,
 D. S., 2015. North America plate boundary offshore southern California.
 Geophys. J. Int. 207.
- ⁷⁵⁴ Refayee, H. A., Yang, B. B., Liu, K. H., Gao, S. S., 2014. Mantle flow and
 ⁷⁵⁵ lithosphere–asthenosphere coupling beneath the southwestern edge of

- the North American craton: Constraints from shear-wave splitting
 measurements. Earth Planet. Sci. Lett. 402, 209–220.
- Savage, M. K., 1999. Seismic anisotropy and mantle deformation: What have we learned from shear wave splitting? Rev. Geophys. 37, 65–106.
 Savage, M. K., Sheehan, A. F., 2000. Seismic anisotropy and mantle flow from the Great Basin to the Great Plains, western United States. J.
 Geophys. Res. Solid Earth 105 (B6), 13715–13734.
- Schaeffer, A. J., Lebedev, S., 2013. Global shear speed structure of the upper
 mantle and transition zone. Geophys. J. Int. 194 (1), 417–449.
- Schmandt, B., Lin, F.-C., 2014. P and S wave tomography of the mantle
 beneath the United States. Geophys. Res. Lett. 41 (18), 6342–6349.
- Silver, P. G., 1996. Seismic anisotropy beneath the continents: Probing the
 depths of geology. Annu. Rev. Earth Planet. Sci 24, 385–432.
- Silver, P. G., Holt, W. E., 2002. The mantle flow field beneath Western North
 America. Science 295, 1054–1057.
- Silver, P. G., Savage, M. K., 1994. The Interpretation of Shear-Wave
 Splitting Parameters In the Presence of Two Anisotropic Layers.
 Geophys. J. Int. 119 (3), 949–963.
- Steinberger, B., Becker, T. W., 2016. A comparison of lithospheric thickness
 models. Tectonophysics.

- West, J. D., Fouch, M. J., Roth, J. B., Elkins-Tanton, L. T., 2009. Vertical
 mantle flow associated with a lithospheric drip beneath the Great Basin.
 Nat. Geosci. 2 (6), 439–444.
- Yang, B. B., Liu, K. H., Dahm, H. H., Gao, S. S., 2016. A Uniform
 Database of Teleseismic Shear-Wave Splitting Measurements for the
 Western and Central United States: December 2014 Update. Seismol.
 Res. Lett. 87 (2A), 295–300.
- Yang, B. B., Liu, Y., Dahm, H., Liu, K. H., Gao, S. S., 2017. Seismic
 azimuthal anisotropy beneath the eastern United States and its
 geodynamic implications. Geophys. Res. Lett. 44 (6), 2670–2678.
- Yuan, H., Romanowicz, B., 2010. Lithospheric layering in the North
 American craton. Nature 466 (7310), 1063–1068.
- Zandt, G., Gilbert, H., Owens, T. J., Ducea, M., Saleeby, J., Jones, C. H.,
 2004. Active foundering of a continental arc root beneath the southern
 Sierra Nevada in California. Nature 431 (7004), 41–46.
- Zandt, G., Humphreys, E., 2008. Toroidal mantle flow through the western
 U.S. slab window. Geology 36 (4), 295.
- Zhong, S., Zuber, M. T., Moresi, L. N., Gurnis, M., 2000. Role of
 temperature-dependent viscosity and surface plates in spherical shell
 models of mantle convection. J. Geophys. Res. 105, 11063–11082.

- ⁷⁹⁶ Zhou, Q., Hu, J., Liu, L., Chaparro, T., Stegman, D. R., Faccenda, M., 2018.
- ⁷⁹⁷ Western U.S. seismic anisotropy revealing complex mantle dynamics.
- ⁷⁹⁸ Earth Planet. Sci. Lett. 500, 156–167.



Figure 1: Study area showing topography and physio-graphic regions (a) and station-averaged shear-wave splitting measurements (b). In a), elevation is shown in the background; green lines are the orographic boundaries here used to define the western, central and eastern U.S.; white lines are the boundaries of different physio-graphic regions; blue profile shows the location of the cross section of the flow profiles discussed below. Main physio-graphic regions that are discussed in this paper are marked with numbers, they are: 1) Columbia Plateau, 2) Basin and Range, 3) Colorado Plateau, 4) Southern Rocky Mountains, 5) Northern Rocky Mountains, 6) Interior Plains, 7) Coastal Plains, 8) Appalachian Mountain Range, and 9) New England province. In b), fast orientation and delay times (δt) of the SWS measurement compilation are shown by stick orientation and color, respectively.



Figure 2: Tomography (a and b) and lithospheric thickness (c and d) models. Colors in a) and b) indicate *S* wave velocity anomalies (δV_S) for the SMEAN (Becker and Boschi, 2002) and MERGED (cf. Schmandt and Lin, 2014) tomography models, respectively, at 200 km depth. In plot b), the outlined features are upper mantle anomalies that are discussed in the result section, they are: 1). Yellowstone and Snake River Plain, 2). Salton Trough, 3). northern Great Valley, 4). Rio Grande Rift, 5). New England, and 6) central Appalachian. Colors in c) and d) show the inferred depth of the lithosphere in viscosity models LVV1 and LVV2, respectively.



Figure 3: Absolute angular misfit ($\Delta \alpha$) between *SKS* splits and absolute plate motion (APM) orientations in the no-net-rotation (NNR) reference frame of Argus and Gordon (1991) (a), and in the spreading-aligned reference frame of Becker et al. (2015) (b). $2^{\circ} \times 2^{\circ}$ grid averaged *SKS* splits (based on Fig. 1b) are shown by red sticks. APM motions are indicated by white, open vectors. Background color indicates the value of $\Delta \alpha$, and title shows the map-wide and regional means of $\Delta \alpha$ for the sub domains indicated by heavy white lines, $\langle \Delta \alpha \rangle$.



Figure 4: Upper mantle flow (a, c, and e) and the resulting angular misfit ($\Delta \alpha$) between *SKS* splits and flow-model predicted anisotropy (b, d, and f) of Models 1 (plate-induced shear, a and b), 2 (added cratons and weak zones, c and d), and 3 (added oceanic weak asthenosphere, e and f). In plot a), c), and e), radial flow is shown in background coloring (upwelling positive); surface velocities, flow at 200 km depth, and their vector difference (amplified by 5) are indicated by yellow, red and green vectors, respectively. In plot b), d), and f), $\Delta \alpha$ is shown in the background; SWS observed and flow model predicted SWS fast orientations depicted by red and white vectors, respectively. Title for b), d), and f) shows mean angular misfits as in Fig. 2.



Figure 5: Cross-section of mantle flow for Models 1 (a), 2 (b), and 3 (c) along the profile shown in Fig. 1a. Background color shows the decadic logarithm of the upper mantle normalized viscosity. and orange vectors show flow velocity with the length scale shown beneath the bottom left corner of plot c). Sub-plots d) and e) show the differences in flow field and viscosity between Models 1 and 2 (d), and between Models 1 and 3 (e). Length scale of the differential flow vectors is shown beneath plot e).



Figure 6: Effect of density anomalies. Flow field at 200 km depth (a and c), the resulting $\Delta \alpha$ between *SKS* splits and flow predicted anisotropy (b and d) of Model 4 (SMEAN density driven flow, a and b) and 5 (MERGED density, c and d), and velocity and viscosity profiles for Models 4 (e) and 5 (f). Scale of velocity vector length is shown beneath plot f). See Fig. 4 and Fig. 5 for details.



Figure 7: Effect of lateral viscosity variations. $\Delta \alpha$ between *SKS* splits and flow-model predicted anisotropy of Models 6 (a), 7 (b), 8 (c), 9 (d), 10 (e), and 11 (f). See Fig. 4 for details.



Figure 8: Flow profiles of Models 6 (a) and 9 (f) with velocity vector length scale shown beneath plot f). Plots c), e), h) and j) show the differences in velocities and viscosity between Models 7 and 6 (c), Models 8 and 6 (e), Models 10 and 9 (h), and Models 11 and 9 (f). Differential velocity vector length scale is shown beneath plot j). See Fig. 5 for details.



Figure 9: Inferred lithospheric anisotropy resulting from matching Model 4 (a) and 5 (b) flow-predicted anisotropy to the SWS dataset. c) shows the Model 5 lithospheric anisotropy orientation within the white rectangular box in b), and d) shows the Model 5 flow predicted anisotropy within the same region. e) shows crustal anisotropy from Lin and Schmandt (2014). f) shows the uppermost mantle anisotropy from Buehler and Shearer (2017). g) shows regional Rayleigh wave anisotropy model from Deschamps et al. (2008), with each of the subplots showing different Rayleigh wave periods as noted on the upper left corner. In all plots, the red vector shows fast orientation. The background color shows the delay time in a) and b), shows the peak to peak amplitude in e), anisotropy magnitude in f), and shows 2ψ anisotropy magnitude in g).

Supplementary Material

Wanying Wang, Thorsten W. Becker

February 25, 2019

Here, we discuss additional material for the lithospheric complement 1 computation discussed in the main text. Whenever we estimate average 2 asthenospheric anisotropy, we compute an arithmetic average of tensors 3 and then use the Christoffel matrix approach and that mean tensor to get 4 average SKS. To match average splitting, we align and scale a lithospheric 5 tensor before averaging by means of a parameter space search. When 6 accounting for back-azimuth dependence, we use a parameter space 7 search and Silver and Savage's (1994) approach. 8

To illustrate that our approach of inverting for best-fit lithospheric anisotropy layer gives reliable results, we picked 11 stations throughout the study area, and show in Fig. S1 that the apparent splitting parameters from the resulting hypothetical two-layer anisotropy are similar to the station averaged splitting parameters from SWS. Moreover, the two layer model from the constrained inversion where we fix the asthenospheric (lower) layer to that expected from an average of our flow model predicted LPO is usually similar to that of a station measurement only based two
 layer model.

We do not expect the resulting lithospheric complement to be exactly the same as the top layer from SWS two-layer inversion. However, when the flow predicted anisotropy has similar orientation with the bottom layer from the two-layer inversion of SWS, the hypothetical lithospheric anisotropy is also similar to the top layer of the SWS two-layer inversion (Fig. S1), suggesting the validity of this approach.

Figs. S2a and b show a comparison between the SWS top layer 24 anisotropy and our hypothetical lithospheric complement. The SWS top 25 layer anisotropy has a wider range of azimuthal orientations and delay 26 times (Fig. S2a), while the hypothetical lithospheric complement shows 27 more smooth and regionally consistent anisotropy patterns, and less 28 variation in delay times. Although differences exist, we see consistency 29 between the two top layer anisotropy estimations in the central U.S. where 30 there is relatively small delay time, in the Great Basin where there is the 31 near circular anisotropy pattern, in the southern Basin and Range where 32 there is the NE-SW anisotropy pattern, and in the eastern U.S. where there 33 is the Appalachian Mountain parallel anisotropy pattern. 34

We also explore a simple method of matching the SWS observation by inverting for the best-fit thickness and anisotropy orientation of a lithospheric layer that consists of frozen-in anisotropy represented by a single elastic tensor. The tensor used here is an averaged single-crystal

tensor with 70% olivine and 30% pyroxene from Estey and Douglas 39 (1986). Instead of using a two layer fit and accounting for back-azimuth 40 dependence of splits, we then only seek to match the average fast 41 axes by means of a simple averaging approach. Using this simple 42 method, the resulting hypothetical lithospheric anisotropy show similar 43 orientations to our two layer inversion approach, but the delay time is 44 overall larger (Fig. S2b and c). With the result from this, we can try fit 45 the two-layer anisotropy from this simple method for $\pi/2$ backazimuth 46 distribution, and compare it to the fit from our two layer inversion 47 approach of computing the lithospheric complement. In Fig. S1, the 48 current lithospheric complement approach (solid curve) fits well with the 49 SKS splits, while the simple method (dashed curve) fitting is off at some 50 stations. 51

52 References

- Estey, L. H., Douglas, B. J., 1986. Upper mantle anisotropy: A preliminary
 model. J. Geophys. Res. 91 (B11), 11393.
- Silver, P. G., Savage, M. K., 1994. The Interpretation of Shear-Wave
 Splitting Parameters In the Presence of Two Anisotropic Layers.
 Geophys. J. Int. 119 (3), 949–963.



Figure S1: Examples of statistics at stations showing the shear wave splitting (SWS) two-layer inversion results, and the flow model (Model 5) hypothetical two layer anisotropy (top layer: flow model predicted anisotropy, and bottom layer: the hypothetical lithospheric complement). Caption continues on next page.



Figure S1: Continues from last page. The average values of the SWS top layer, bottom layer, and station average are shown by the solid blue line, solid green line, and solid red line, respectively. The average values of the top layer, bottom layer, and station average from the hypothetical two layer anisotropy are shown by the dashed blue line, dashed green line, and dashed red line, respectively. Caption continues on next page.



Figure S1: Continues from last page. Splitting parameters from SWS are shown by the black circles, and the vertical lines through the circles show estimated errors. The solid black curve shows the two-layer fitting of the hypothetical two layer anisotropy. The dashed black curve shows the two layer fitting for the simple method of computing lithospheric complement. The location of each station is shown by red dot on the map.



Figure S2: The top-layer anisotropy from a) station by station SWS two-layer inversion, b) method used for the main text of computing the lithospheric complement, and c) the simple method of computing lithospheric complement based on modeling average angles.